```
二分
优先队列
struct cmp1{
                                                                  do{
    bool operator ()(int &a,int &b){
                                                                      mid = (l + r) >> 1;
         return a>b;//最小值优先 写
                                                                      if(check(mid)) I = mid + 1,ans = mid;
                                                                      else r = mid - 1;
};
                                                                  }while(I <= r);
struct cmp2{
    bool operator ()(int &a,int &b){
         return a<b;//最大值优先 默认
                                                                  约瑟夫环
};
                                                                  int arr[30010];
int main(){
                                                                  int main(){
    priority_queue<int,vector<int>,cmp2> q;
                                                                      int n,m;
                                                                      cin >> n >> m;
Prime 表
                                                                      int loc = 1;
                                                                       for(int i = 1;i <= n;i ++)
bool prime[5000010];
                                                                           arr[i] = i;
void Primelist(int n){
                                                                      for(int i = n; i > 0; i --){
    prime[1] = 1;
                                                                           loc = (loc + m - 1) \% i;
    for(int i = 2; i <= n; i ++){
                                                                           if(loc == 0) loc = i;
        if(!prime[i])
                                                                           cout << arr[loc] << " ";
            for(int j = 2;j * i <= n;j ++)
                                                                           for(int j = loc; j < i; j ++)
                 prime[i * j] = 1;
                                                                                arr[j] = arr[j + 1];
                                                                       return 0;
```

KMP 算法 N皇后 int next[1000010]; int arr[20]; int ans; int n,ans; void Next(string pat){ bool Judge(int a,int b){ int loc,k,len = pat.length(); for(int i = 1; i < a; i ++)for (loc = 1,k = 0;loc < len;loc ++)if(arr[i] == b | | fabs(arr[i] - b) == fabs(a - i)) while(k > 0 && pat[loc] != pat[k]) return 0; k = next[k - 1];return 1; if (pat[loc] == pat[k]) k ++; void dfs(int dep){ next[loc] = k; $if(dep == n + 1){}$ } ans ++;return; void kmp(string str,string pat){ for(int $i = 1; i <= n; i ++){$ int loc,len_str = str.length(),len_pat = pat.length(); arr[dep] = i; Next(pat); if(!Judge(dep,i)){ for (int i = 0, loc = 0; $i < len str; i ++){}$ arr[dep] = 0;continue; while(loc > 0 && pat[loc] != str[i]) loc = next[loc - 1]; dfs(dep + 1);arr[dep] = 0;if (pat[loc] == str[i]) loc ++; } if (loc == len_pat) //printf("Pattern occurs with shift:%d\n",(i - len pat + 1)); int main(){ cin >> n;dfs(1); ans ++; cout << ans << endl; return 0;

快速幂

```
long long Qpow(long long m,long long n,long long k){
    long long res = 1;
    while(n > 0){
        if(n & 1)
            res = res * m % k;
        n = n >> 1;
        m = m * m % k;
    return res;
String 字符串替代
string& replace_all(string& str,const string& old_value,const
string& new value)//replace all(str,pat,sub); 串 模板 替换
串
    while(true){
         string::size_type pos(0);
         if((pos=str.find(old_value))!=string::npos)
str.replace(pos,old_value.length(),new_value);
         else break;
    }
    return str;
```

多重背包

```
void ZeroOne(int vi,int w){
    for(int i = v;i >= vi;i --)
        F[i] = \max(F[i],F[i-vi] + w);
void Multiple(int v,int w,int amount){
    int k = 1;
    while(amount > k){
        ZeroOne(k * v,k * w);
        amount = amount - k;
        k = k * k;
    ZeroOne(amount * v,amount * w);
```

组合数

```
long long C(int n,int m){
    long i = m, ans = 1;
    while(i != 0) ans *= n,n --,i --;
    while(m != 0) ans /= m,m --;
    return ans;
卡特兰数
const int N =
long long K[N + 10];
void katelan(){
    K[1] = 1, K[0] = 1;
    for(int i = 2;i <= N;i ++)
        K[i] = ((4 * i - 2) / (double)(i + 1)) * K[i - 1];
```

贝尔数

```
const int mod =
const int N =
long long T[N + 10], B[N + 10];
void Bell(){
    B[0] = 1,B[1] = 1,T[0] = 1;
    for(int i = 2; i < N; i ++){
         T[i-1] = B[i-1];
         for(int j = i - 2; j >= 0; j --)
             T[j] = (T[j] + T[j + 1]) \% mod;
         B[i] = T[0];
    }
```

Matrix fast_mod(Matrix base,long long n){ 广义 Fibonacci Matrix res = $\{1,0,0,1\}$; while(n > 0){ if(n & 1) //六个变量分别是 Fn = p * Fn-1 + q * Fn-2 F1 = a1 F2 res = multi(res,base); =a2 第n项 mod n >>= 1; base = multi(base,base); const int MAX = 2; typedef struct{ return res; long long arr[2][2]; }Matrix; int main(){ long long mod; long long p,q,a1,a2,n; Matrix multi(Matrix a, Matrix b){ cin >> p >> q >> a1 >> a2 >> n >> mod; Matrix c; Matrix base = $\{p,q,1,0\}$; for(int i = 0;i < MAX;i ++) Matrix ans = fast_mod(base,n - 2); $for(int j = 0; j < MAX; j ++){}$ if(n == 1) c.arr[i][j] = 0; cout << a1 << endl; for(int k = 0; k < MAX; k ++)else if(n == 2) c.arr[i][j] = (c.arr[i][j] + a.arr[i][k] * cout << a2 << endl; b.arr[k][j]) % mod; else cout << (ans.arr[0][0] * a2 % mod + ans.arr[0][1] * return c; a1 % mod) % mod << endl; return 0;

```
最短路径 Bellman
typedef struct{
    int from,to,cost;
}EDGE;
EDGE es[MAX_E];
int dis[MAX_D];
int V,E;
void shortest_path(int s){
    for(int i = 0;i < V;i ++) dis[i] = INF;
    dis[s] = 0;
    while(1){
        bool update = false;
        for(int i = 0; i < E; i ++){
            edge e = es[i];
            if(dis[e.from] != INF && dis[e.to] > dis[e.from] +
            e.cost){
                 dis[e.to] = dis[e.from] + e.cost;
                 update = true;
        if(!update) break;
```

```
bool find_negative_loop(){
    memset(dis,0,sizeof(dis));
    for(int i = 0; i < V; i ++){
        for(int j = 0; j < E; j ++){
             edge e = es[j];
             if(dis[e.to] > dis[e.from] + e.cost){
                  d[e.to] = d[e.from] + e.cost;
                  if(i == V - 1) return true;
    return false;
```

Dijkstra

```
const int INF = 1e9;
const int V = MAX V;
int cost[V + 1][V + 1];
int dis[V + 1];
bool used[V + 1];
void dijkstra(int s){
    for(int i = 1; i <= V; i ++)
         dis[i] = INF,used[i] = 0;
    dis[s] = 0;
    while(1){
         int v = -1;
         for(int u = 1; u \le V; u ++)
             if(!used[u] && (v == -1 || dis[u] < dis[v]))
                  v = u;
         if(v == -1) break;
         used[v] = 1;
         for(int u = 1; u \le V; u ++)
             dis[u] = min(dis[u], dis[v] + cost[v][u]);
```

Dijkstra 堆优化

```
typedef struct{
    int to, cost;
}edge;
typedef pair<int,int> P;
const int V = 52; const int INF = 1e9;
vector<edge> G[V + 1];
int dis[V + 1];
void dijkstra(int s){
    priority_queue<P,vector<P>,greater<P> > q;
    for(int i = 1;i <= V;i ++)
         dis[i] = INF;
    dis[s] = 0;
    q.push(P(0,s));
    while(!q.empty()){
         P p = q.top();q.pop();
         int v = p.second;
         if(dis[v] < p.first) continue;</pre>
         for(int i = 0;i < G[v].size();i ++){
             edge e = G[v][i];
             if(dis[e.to] > dis[v] + e.cost){
                  dis[e.to] = dis[v] + e.cost;
                  q.push(P(dis[e.to],e.to));
```

Floyd int dis[V + 1][V + 1]; void floyd(){ for(int k = 1;k <= V;k ++) for(int i = 1;i <= V;i ++) for(int j = 1;j <= V;j ++) dis[i][j] = min(dis[i][j],dis[i][k] + dis[k][j]);

Gcd 和 Lcn

```
long long gcd(long long n,long long m){
    long long r;
    while(1){
        r = n % m;
        if(r == 0) return m;
        n = m; m = r;
    }
}
long long lcn(long long n,long long m){
    return (m * n / gcd(n,m));
}
```

Prim

```
int V;
const int MAX V = 100;
const int INF = 1e9;
int cost[MAX_V + 1][MAX_V + 1];
int mincost[MAX_V + 1];
bool used[MAX_V + 1];
int prim(){
    for(int i = 1;i <= V;i ++)
        mincost[i] = INF,used[i] = 0;
    mincost[1] = 0;
    int res = 0;
    while(1){
        int v = -1;
        for(int u = 1; u \le V; u ++)
            if(!used[u] && (v == -1 || mincost[u] <
            mincost[v])) v = u;
        if(v == -1) break;
        used[v] = 1;
        res += mincost[v];
        for(int u = 1;u <= V;u ++)
             mincost[u] = min(mincost[u],cost[v][u]);
    return res;
```

Kruskal

```
int par[MAX_V];
int rank[MAX_V];
void init(int n){
    for(int i = 0; i < n; i ++)
         par[i] = i,rank[i] = 0;
int find(int x){
    if(par[x] == x) return x;
    else return par[x] = find(par[x]);
void unite(int x,int y){
    x = find(x), y = find(y);
    if(x == y) return;
    if(rank[x] < rank[y]) par[x] = y;</pre>
    else par[y] = x;
    if(rank[x] == rank[y]) rank[x] ++;
bool same(int x,int y){
    return find(x) == find(y);
```

```
typedef struct{
    int u,v,cost;
}edge;
edge es[MAX_E];
int V,E;
bool cmp(edge e1,edge e2){
    return e1.cost < e2.cost;
}
int kruskal(){
    sort(es + 1, es + E + 1, cmp);
    init(V + 1);
    int res = 0;
    for(int i = 1;i <= E;i ++){
        edge e = es[i];
        if(!same(e.u,e.v))
             unite(e.u,e.v),res += e.cost;
    return res;
```

SCC 强连通分量

```
int V;
vector<int> G[MAX V + 10];
vector<int> rG[MAX V + 10];
vector<int> vs;//后续遍历顶点列表
bool vis[MAX_V + 10];
int cmp[MAX_V + 10];//所属强连通分量的拓排序
void add(int from,int to){
    G[from].push back(to);
    rG[to].push back(from);
void dfs(int v){
    vis[v] = true;
    for(int i = 0;i < G[v].size();i ++)
        if(!vis[G[v][i]]) dfs(G[v][i]);
    vs.push_back(v);
void rdfs(int v,int k){
    vis[v] = true;
    cmp[v] = k;
    for(int i = 0;i < rG[v].size();i ++)
        if(!vis[rG[v][i]]) rdfs(rG[v][i],k);
```

```
int scc(){
    memset(vis,0,sizeof(vis));
    vs.clear();
    for(int v = 0;v < V;v ++)
         if(!vis[v]) dfs(v);
    memset(vis,0,sizeof(vis));
    int k = 0;
    for(int i = vs.size() - 1;i >= 0;i --){
         if(!vis[vs[i]]) rdfs(vs[i],k ++);
    return k;
}
//x1,y1 为最高点
double x1, y1, x2, y2, x3, y3;
scanf("%lf%lf%lf%lf%lf%lf", &x1, &y1, &x2, &y2, &x3, &y3);
printf("%.2f\n",
(y3-y1)*(x2-x3)*(x2-x3)*(x2-x3)/6.0/(x1-x3)/(x1-x3));
//错排原理
f[1] = 0, f[2] = 1, f[3] = 2;
f[i] = (i - 1) * (f[i - 1] + f[i - 2]);
```

LCA 最小公共祖先 二分 vector<int> G[MAX V]; int root; int parent[MAX_LOG_V][MAX_V]; int depth[MAX V]; void dfs(int v,int p,int d){ parent[0][v] = p; depth[v] = d;for(int i = 0;i < G[v].size();i ++) if(G[v][i] != p) dfs(G[v][i],v,d + 1);void init(int V){ dfs(root,-1,0); for(int $k = 0; k + 1 < MAX_LOG_V; k ++){$ for(int $v = 0; v < V; v ++){$ if(parent[k][v] < 0) parent[k + 1][v] = -1;else parent[k + 1][v] = parent[k][parent[k][v]];

```
int lca(int u,int v){
    if(depth[u] > depth[v]) swap(u,v);
    for(int k = 0;k < MAX_LOG_V;k ++){
        if((depth[v] - depth[u]) >> k & 1)
             v = parent[k][v];
    if(u == v) return u;
    for(int k = MAX\_LOG\_V - 1; k \ge 0; k --){
        if(parent[k][u] != parent[k][v]){
             u = parent[k][u];
             v = parent[k][v];
    return parent[0][u];
```

并查集

```
int par[MAX_N];
int rankk[MAX_N];
void init(int n){
    for(int i = 0; i < n; i ++)
         par[i] = i,rankk[i] = 0;
int find(int x){
    if(par[x] == x) return x;
    else return par[x] = find(par[x]);
void unite(int x,int y){
    x = find(x), y = find(y);
    if(x == y) return;
    if(rankk[x] < rankk[y]) par[x] = y;</pre>
    else par[y] = x;
    if(rankk[x] == rankk[y]) rankk[x] ++;
bool same(int x,int y){
    return find(x) == find(y);
```

最长序列

```
int dp[10000]
int max_length_dp;
int numbers[10000];
int dping(int loc){
    int max = 0;
    for(int i = 0;i < loc;i ++)
        if(numbers[loc] >= numbers[i] && dp[i] > max)
             max = dp[i];
    dp[loc] = max + 1;
    return dp[loc];
int main(){
    int n; cin >> n;
    numbers = new int[n];
    dp = new int[n];
    for(int i = 0; i < n; i ++)
        cin >> numbers[i];
    for(int i = 0;i < n;i ++)
        if(dping(i) > max_length_dp)
             max_length_dp = dping(i);
    cout << max_length_dp;</pre>
    return 0;
 }
```

树状数组1、2 int tree[100010],n,m; void add(int k,int num){ while($k \le n$) tree[k] += num, k += k & -k;int read(int k){ int sum = 0; while(k) sum += tree[k], k -= k & -k;return sum; int main(){ cin >> n; int ele; for(int i = 1; i <= n; i ++)cin >> ele,add(i,ele); cin >> m; while(m --){ int a,b,c; cin >> a >> b >> c: if(a == 1) add(b,c); else cout << read(c) - read(b - 1) << endl;</pre> return 0;

```
int arr[1000010],crr[1000010];
int n,m;
void add(int k,int num){
    while(k) crr[k] += num, k -= k \& -k;
int read(int k){
    int sum = arr[k];
    while(k \le n) sum += crr[k],k += k & -k;
    return sum;
int main(){
    cin >> n;int ele;
    for(int i = 1; i <= n; i ++)
        cin >> arr[i];
    cin >> m;
    while(m --){
        int opr;cin >> opr;
        if(opr == 1){
             int a,b,c;
             cin >> a >> b >> c;
             add(b,c);add(a - 1,-c);
        else{
             int a; cin >> a;
             cout << read(a) << endl;
       return 0;
```

DP 题

```
石子归并
int main(){
    int n,w[106],f[106][106],st;
    cin >> n;
    memset(f,0x3f3f3f3f,sizeof(f));
    for(int i = 1; i <= n; i ++){
         cin >> st;
         w[i] = w[i - 1] + st;
         f[i][i] = 0;
    for(int j = 2; j <= n; j ++)
         for(int i = j - 1; i >= 1; i --)
             for(int k = i; k < j; k ++)
                  f[i][j] = min(f[i][j],f[i][k] + f[k + 1][j] + w[j] -
                  w[i - 1]);
    cout << f[1][n] << endl;
    return 0;
```

乘积最大

```
long long arr[50],sum[50][50],f[50][50];
int main()
    int n,m;
     string str;
     cin >> n >> m;
     cin >> str;
    for(int i = 1; i <= n; i ++)
         arr[i] = str[i - 1] - '0',sum[i][i] = arr[i];
     for(int i = 1; i < n; i ++)
         for(int j = i + 1; j <= n; j ++)
              sum[i][j] = sum[i][j - 1] * 10 + arr[j];
    for(int i = 1; i <= n; i ++)
         f[i][0] = sum[1][i];
    for(int j = 1; j <= m; j ++)
         for(int i = j + 1; i <= n; i ++)
              for(int k = j; k \le i - 1; k ++)
                   f[i][j] = max(f[i][j],f[k][j-1] * sum[k+1][i]);
     cout << f[n][m] << endl;
     return 0;
```

数的划分 线段覆盖 typedef pair<int,int> Moran; int dp[210][210]; Moran moran[110]; int main(){ bool cmp(Moran a, Moran b){ int n,m; return a.second < b.second; cin >> n >> m; dp[0][0] = 1;int main() { for(int i = 1;i <= m;i ++) int n; for(int $j = 0; j <= n; j ++){$ cin >> n; if(i - i >= 0)for(int $i = 0; i < n; i ++){$ dp[i][i] = dp[i - 1][i] + dp[i][i - i];cin >> moran[i].first >> moran[i].second; else if(moran[i].first > moran[i].second) dp[i][j] = dp[i - 1][j]; swap(moran[i].first ,moran[i].second); sort(moran,moran + n,cmp); cout << dp[m][n] - dp[m - 1][n] << endl;//dp[m][n]表示 int st = moran[0].second; n 个数分成不超过 m 份方法数 int cnt = 1; return 0; for(int i = 1; i < n; i ++)if(moran[i].first >= st) cnt ++,st = moran[i].second; cout << cnt << endl; return 0;

最长公共序列

```
const int N = ;
int longest[N][N];
int LCS(string s1,string s2){
     int i,j,len1,len2;
     len1 = s1.length();
     len2 = s2.length();
     longest[0][0] = 0;
    for(i = 1;i <= len1;i ++) longest[i][0] = 0;
    for(i = 1;i <= len1;i ++) longest[0][i] = 0;
    for (i = 1;i <= len1;i ++){
          for (j = 1; j \le len2; j ++){
                if(s1[i-1] == s2[j-1])
                     longest[i][j] = longest[i - 1][j - 1] + 1;
                else if(longest[i - 1][j] > longest[i][j - 1])
                     longest[i][j] = longest[i - 1][j];
                else
                     longest[i][j] = longest[i][j - 1];
          }
     return longest[len1][len2];
```

最长上升子序列 nlogn

```
int arr[maxn],b[maxn];
int n;
int LIS(){
    int len = 1,j;
    b[1] = arr[1];
    for(int i = 2;i <= n;i ++){
        if(arr[i] > b[len]) j = ++len;
        else j = lower_bound(b + 1,b + 1 + len,arr[i]) - b;
        b[j] = arr[i];
    }
    return len;
}
```

import java.util.*; import java.math.*; public class Main{ public static void main(String []args){ Scanner cin=new Scanner(System.in); BigDecimal x,y; String a,b; while(cin.hasNext()){ a=cin.next(); b=cin.next(); x=new BigDecimal(a); y=new BigDecimal(b); System.out.println(x.add(y).stripTrailingZeros(). toPlainString());

Java 大数

```
BigInteger mod = new BigInteger("2333333333");
while(Inx.hasNext()){
       n=Inx.nextBigInteger();
       m = Inx.nextBigInteger();
       BigInteger yu = m.remainder(BigInteger.valueOf(3));
       BigInteger end = m.divide(BigInteger.valueOf(3));
       end = end.add(n);
       BigInteger temp = new BigInteger("0");
       temp =temp.add(n);
       temp = temp.add(BigInteger.valueOf(1));
       temp = temp.add(end);
       temp = temp.multiply(end.subtract(n));
       temp = temp.divide(BigInteger.valueOf(2));
       temp = temp.multiply(BigInteger.valueOf(3));
       int r = yu.intValue();
       for(int i = 0; i < r; i ++){
             temp = temp.add(BigInteger.valueOf(i));
             temp = temp.add(end);
        temp = temp.remainder(mod);
        System.out.println(temp);
```

DP 硬币 max 和 min

```
int dpmax(int S) {
    if(vis[S]) return d[S];
    vis[S] = 1;
    int &ans = d[S];
    ans = -1 << 30;
    for(int i = 1; i <= n; ++i) {
         if(S \ge V[i]) ans = max(ans, dpmax(S - V[i]) + 1);
    }
    return ans;
int dpmin(int S) {
    if(vis[S]) return d[S];
    vis[S] = 1;
    int &ans = d[S];
    ans = -1 >> 30;
    for(int i = 1; i <= n; ++i) {
         if(S \ge V[i]) ans = min(ans, dpmin(S - V[i]) + 1);
    }
    return ans;
```

逆序对

```
long long arr[100010],sum[100010],temp[100010],cnt;
void merge(int l,int mid,int r){
    int i = l, j = mid + 1, loc = l;
    while(i \leq mid && j \leq r){
        if(sum[i] > sum[j]){
             temp[loc ++] = sum[j ++];
             cnt += mid - i + 1;
        else temp[loc ++] = sum[i ++];
    while(i \le mid) temp[loc ++] = sum[i ++];
    while(j \le r) temp[loc ++] = sum[j ++];
    for(int i = l;i <= r;i ++) sum[i] = temp[i];
void mergesort(int l,int r){
    if(l < r)
        int mid = (l + r) >> 1;
        mergesort(I,mid);
        mergesort(mid + 1,r);
        merge(l,mid,r);
```

凸包面积 typedef struct{ double x,y; }POINT; POINT pot[200]; double Cross(POINT a,POINT b){ return a.x * b.y - a.y * b.x; int main(){ int n; cin >> n; double sum = 0; for(int $i = 1; i <= n; i ++){$ cin >> pot[i].x >> pot[i].y; for(int i = 1; i < n; i ++)sum += fabs(Cross(pot[i],pot[i + 1])); sum += fabs(Cross(pot[1],pot[n])); cout << sum / 2 << endl; return 0;

三角形外心

}

```
typedef struct{
    double x,y;
}POINT;
POINT waixin(POINT a, POINT b, POINT c){
    POINT ans;
    double a1 = b.x - a.x, b1 = b.y - a.y, c1 = (a1 * a1 + b1 *
b1) / 2;
    double a2 = c.x - a.x, b2 = c.y - a.y, c2 = (a2 * a2 + b2 * b2)
/ 2;
    double d = a1 * b2 - a2 * b1;
    ans.x = a.x + (c1 * b2 - c2 * b1) / d;
    ans.y = a.y + (a1 * c2 - a2 * c1) / d;
    return ans;
三角形有向面积两倍
double area(double x0,double y0,double x1,double
y1,double x2,double,y2){
```

return x0*y1+x2*y0+x1*y2-x0*y2-x1*y0-x2*y1;

组合博弈

```
int arr[5000];
1、巴什博弈 n=(m+1)*r+s
                                                       int main(){
2、威佐夫博弈
                                                           int n;
int main(){
                                                           while(cin >> n){
   int a,b,k,a_k;
                                                              if(n == 0) break;
   while(scanf("%d%d",&a,&b)!=EOF){
                                                              int temp = 0;
         k = abs(a-b);
                                                              for(int i = 1;i <= n;i ++){
         a = a < b? a : b;
                                                                  cin >> arr[i];
         a k = floor(k*(1.0 + sqrt(5.0))/2);
                                                                  temp = temp ^ arr[i];
         printf("%d\n",a!=a k);
         //输出为0,说明该点为必败点,1为必胜点
                                                              int cnt = 0;
   }
                                                              for(int i = 1; i <= n; i ++){
    return 0;
                                                                  int st = arr[i] ^ temp;
                                                                  if(st < arr[i])</pre>
3、尼姆博弈
                                                                      cnt ++;
全部亦或 为 0 则为 T 不为 0 为 S
取火柴 1: 取完胜 先手必胜为 S 必败为 T
                                                              cout << cnt << endl;
取火柴 2: 取完败 先手必胜态为 TO S2 S1 必败态为 S0 T2
                                                           return 0;
取火柴1时候 第一步选择数
```

```
匈牙利算法
const int maxn = ; bool vis[maxn],f[maxn][maxn];
int n,m,linkk[maxn];
bool find(int x){
    for(int i = 1;i <= n;i ++){
        if(f[x][i] && !vis[i]){
            vis[i] = 1;
            if(linkk[i] == -1 | | find(linkk[i])){
                 linkk[i] = x;
                 return 1;
    return 0;
int maxmatch(){
    int num = 0;
    memset(linkk,-1,sizeof(linkk));
    for(int i = 1;i <= n;i ++){
        memset(vis,0,sizeof(vis));
        if(find(i)) num ++;
    }
    return num;
```