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AUGUST

SATURDAY

Google Online.

8 Every language has a function to generate a random number.  
How is this function made?

9 3 → weight.

10 5 → weight.

11 2 → weight.

Highest weight → Highest probability.

12 528 Random Pick with Weight.

1  $w[i] = \text{weight of } i^{\text{th}} \text{ index}$

2  $w[i] = [1, 3]$   
0 1

3 probability of 0<sup>th</sup> index =  $\frac{1}{4} = 25\%$

probability of 1<sup>th</sup> index =  $\frac{3}{4} = 75\%$

27 Approach One.

SUNDAY

E = 

0	1	1	1
---	---	---	---

  
0 1 2 3.

rand(). an index

This return.

$E[\text{rand}()]$ .

S	M	T	W	T	F	S	S	M	T	W	T	F	S	S	M	T	W	T	F	S
17	18	19	20	21	22	23	24	25	26	27	28	29	30							

AUGUST

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MONDAY

$$W = [4, 7, 2, 5]$$

$$\text{sum}(W) = 18$$

Prefix Sum Array = P.

$$p[i] = p[0] + \dots + p[i]$$

$$P = [4, 11, 13, 18]$$

rand() % total

$$r = \text{rand}() \% \text{total} \quad r \in (0, \text{total} - 1)$$

$$r \Rightarrow [0, \dots, 17]$$

$$P = [4, 11, 13, 18]$$

0-3 4-10 11-12 13-17.

To search  $r$  we can do Linear Search.

$$r = 5 \text{ so it lies in } 4-10 \rightarrow \text{index} = 11.$$

Code :-

```
vector<int> prefix;
Solution(vector<int> &w) {
    int n = w.size();
    prefix.resize(n);
    prefix[0] = w[0];
    for (int i = 0; i < n; i++) {
        prefix[i] = w[i] + prefix[i-1];
    }
}
```



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M	T	W	T	F	S	S	M	T	W	T	F	S	S	M	T	W	T	F	S	S
					1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16
17	18	19	20	21	22	23	24	25	26	27	28	29	30	31						

TUESDAY

Simple  $\Rightarrow$  Linear Search.

8  $p = [4, 11, 13, 18]$   
           0-3    4-10    11-12    13-17.

9 To find the range in which  $x$  lies we need to find  
 10 UpperBound  
 11  $\hookrightarrow$  First index that is greater than  $x$ .

12 So basically we apply binary search. instead of linear search.  
 as we get time complexity  $O(\log n)$  instead of  $O(n)$

```

1 int pickIndex() {
2     int total = prefix.back();
3     int rand int r = rand() % total;
4     int lo = 0; int hi = prefix.size() - 1;
5     int ans = 0;
6     while (lo <= hi) {
7         int mid = (lo + hi) / 2;
8         if (prefix[mid] <= r) {
9             lo = mid + 1; // go to right side for ↑ w
10        }
11        else {
12            ans = mid;
13            hi = mid - 1;
14        }
15    }
16    return ans;
17 }
```