This is a part of SFQED-Loops script collection developed for calculating loop processes in Strong-Field Quantum Electrodynamics.

The scripts are available on https://github.com/ArsenyMironov/SFQED-Loops

If you use this script in your research, please, consider citing our papers:

- A. A. Mironov, S. Meuren, and A. M. Fedotov, PRD 102, 053005 (2020), https://doi.org/10.1103/PhysRevD.102.053005
- A. A. Mironov, A. M. Fedotov, arXiv:2109.00634 (2021) If you have any questions, please, don't hesitate to contact: mironov.hep@gmail.com

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NotebookEvaluate[NotebookOpen[NotebookDirectory[] <> "definitions.nb"]]

FeynCalc 9.2.0. For help, use the documentation center, check out the wiki or write to the mailing list.

See also the supplied examples. If you use FeynCalc in your research, please cite

- V. Shtabovenko, R. Mertig and F. Orellana,
   Comput. Phys. Commun., 207C, 432–444, 2016, arXiv:1601.01167
- R. Mertig, M. Böhm, and A. Denner, Comput. Phys. Commun., 64, 345–359, 1991.

Electron propagator in  $E_p$  - representation satisfies the equation  $S^c(p,q) = (2\pi)^4 \delta(p-q) S^c(p)$ 

$$[\gamma p - m - M (p)] S^{c} (p) = i$$

Let

$$D \ (p) = \gamma p - m - M \ (p) = S + \gamma V + \sigma T + \gamma A \gamma^5$$
 
$$S = m \ S \ \left(p^2 \ , \ \chi_p\right) \ ,$$

$$V^{\mu} = p^{\mu} v_1 (p^2, \chi_p) + \frac{e^2 (F^2 p)^{\mu}}{m^4 \chi^2} v_2 (p^2, \chi_p),$$

$$T_{\mu\nu} = \frac{eF_{\mu\nu}}{m\,\chi}\,\text{t}\,\left(p^2\,\text{,}\,\chi_p\right)\,\text{,}$$

$$A^{\mu} = \frac{e (F^* p)^{\mu}}{m^2 \chi} a_s (p^2, \chi_p), \text{ where s stands for 'scalar';}$$

then

$$\begin{split} S^{c} \; \left( p \right) \; &= \; \dot{\mathbb{1}} D^{-1} \; \left( p \right) \; = \; \frac{\dot{\mathbb{1}}}{2} \; \left( S - \gamma V - \sigma T + \gamma A \gamma^{5} \right) \left[ \\ &= \frac{1}{D_{+} \; \left( p^{2} , \; \chi_{p} \right)} \; \left( 1 + \gamma \varepsilon^{(2)} \; \gamma^{5} \right) \; + \; \frac{1}{D_{-} \; \left( p^{2} , \; \chi_{p} \right)} \; \left( 1 - \gamma \varepsilon^{(2)} \; \gamma^{5} \right) \right] \; = \\ &= \; \frac{\dot{\mathbb{1}}}{2} \left[ m \; s \; \left( p^{2} , \; \chi_{p} \right) \; - \; \left( \gamma p \right) \; V_{1} \; \left( p^{2} , \; \chi_{p} \right) \; - \; \frac{e^{2} \; \left( \gamma F^{2} \; p \right)}{m^{4}} \; V_{2} \; \left( p^{2} , \; \chi_{p} \right) \; - \\ &= \; \frac{e \; \sigma F}{m} \; t \; \left( p^{2} , \; \chi_{p} \right) \; + \; \frac{e \; \left( \gamma F^{*} \; p \right) \; \gamma^{5}}{m^{2}} \; a_{s} \; \left( p^{2} , \; \chi_{p} \right) \; \right] \times \\ &= \; \left[ \; \frac{1}{D_{+} \; \left( p^{2} , \; \chi_{p} \right)} \; \left( 1 + \gamma \varepsilon^{(2)} \; \gamma^{5} \right) \; + \; \frac{1}{D_{-} \; \left( p^{2} , \; \chi_{p} \right)} \; \left( 1 - \gamma \varepsilon^{(2)} \; \gamma^{5} \right) \; \right] \; , \\ &\in \, ^{(2)} \; _{\mu} \; = \; \frac{e \; \left( F^{*} \; p \right)^{\mu}}{m^{3} \; \chi_{p}} \; , \end{split}$$

### Electron propagator

$$S^{c}(x_{2}, x_{1}) = \Lambda^{4-D} \int \frac{d^{D}p}{(2\pi)^{D}} E_{p}(x_{2}) S^{c}(p) \overline{E}_{p}(x_{1})$$

$$x = x_2 - x_1,$$
 $X = \frac{1}{2} (x_1 + x_2),$ 
 $\xi^2 = -\frac{e^2 a^2}{m^2},$ 

 $[\Lambda] = m - mass scale,$ 

$$\begin{split} \mathsf{E}_{\mathsf{p}} \; (\mathsf{x}_2) \; &= \; \left[ \, 1 \, - \, \frac{\mathsf{e} \; (\gamma \mathsf{k}) \; (\gamma \mathsf{a})}{2 \; (\mathsf{k} \mathsf{p})} \; (\mathsf{k} \mathsf{x}_2) \, \, \right] \\ &= \; \mathsf{E} \mathsf{x} \mathsf{p} \left[ - \, \dot{\mathbb{I}} \; (p \; \mathsf{x}_2) \, + \, \dot{\mathbb{I}} \; \frac{\mathsf{e} \; (a \; p)}{2 \; (k \; p)} \; (k \; \mathsf{x}_2)^{\, 2} \, + \, \dot{\mathbb{I}} \; \frac{a^2 \; \mathsf{e}^2}{6 \; (k \; p)} \; (k \; \mathsf{x}_2)^{\, 3} \, \right] ; \end{split}$$

NewMomentum["p"]

NewCoordinate["x1"]

NewCoordinate["x2"]

NewCoordinate["x"]

NewCoordinate["X"]

$$\left\{p^{\alpha}, p^{2}, k \cdot p, \operatorname{Fp}^{\alpha}, \operatorname{FFp}^{\alpha}, \operatorname{FDp}^{\alpha}, a \cdot p, 0, 0, 0, -a^{2}(k \cdot p), 0, 0, -\frac{m^{6} \chi p^{2}}{\rho^{2}}, -\frac{m^{6} \chi p^{2}}{\rho^{2}}, \frac{m^{6} \chi p^{2}}{\rho^{2}}, 0, 0, 0, 0, 0, 0\right\}$$

$$\{x1^{\alpha}, x1^{2}, k \cdot x1, a \cdot x1, Fx1^{\alpha}, FFx1^{\alpha}, FDx1^{\alpha}, k \cdot x1, 0, 0, 0, -a^{2}(k \cdot x1), \}$$

$$0, 0, -\frac{m^2 \xi^2 (k \cdot x1)^2}{g^2}, -\frac{m^2 \xi^2 (k \cdot x1)^2}{g^2}, \frac{m^2 \xi^2 (k \cdot x1)^2}{g^2}, 0, 0, 0, 0, 0, 0$$

$$\{x2^{\alpha}, x2^{2}, k \cdot x2, a \cdot x2, Fx2^{\alpha}, FFx2^{\alpha}, FDx2^{\alpha}, k \cdot x2, 0, 0, 0, -a^{2}(k \cdot x2),$$

$$0, 0, -\frac{m^2 \xi^2 (k \cdot x^2)^2}{e^2}, -\frac{m^2 \xi^2 (k \cdot x^2)^2}{e^2}, \frac{m^2 \xi^2 (k \cdot x^2)^2}{e^2}, 0, 0, 0, 0, 0, 0$$

$$\{x^{\alpha}, x^{2}, k \cdot x, a \cdot x, \operatorname{Fx}^{\alpha}, \operatorname{FFx}^{\alpha}, \operatorname{FDx}^{\alpha}, k \cdot x, 0, 0, 0, -a^{2}(k \cdot x),$$

$$0, 0, -\frac{m^2 \xi^2 (k \cdot x)^2}{2}, -\frac{m^2 \xi^2 (k \cdot x)^2}{2}, \frac{m^2 \xi^2 (k \cdot x)^2}{2}, \frac{m^2 \xi^2 (k \cdot x)^2}{2}, 0, 0, 0, 0, 0, 0\right\}$$

$$\{X^{\alpha}, X^2, k \cdot X, a \cdot X, FX^{\alpha}, FFX^{\alpha}, FDX^{\alpha}, k \cdot X, 0, 0, 0, -a^2(k \cdot X),$$

$$0, 0, -\frac{m^2 \xi^2 (k \cdot X)^2}{e^2}, -\frac{m^2 \xi^2 (k \cdot X)^2}{e^2}, \frac{m^2 \xi^2 (k \cdot X)^2}{e^2}, 0, 0, 0, 0, 0, 0$$

DdInv[sgn] == 
$$D_{sgn} (p^2, \chi_p)$$
  
 $\in == \in (2)$ 

```
FToak = {Ft[\alpha_, \beta_] \rightarrow kv[\alpha] av[\beta] - av[\alpha] kv[\beta], DiracGamma[Momentum[Fp, D], D] \rightarrow
             DiracGamma[Momentum[k, D], D] Pair[Momentum[a, D], Momentum[p, D]] -
                  DiracGamma[Momentum[a, D], D] Pair[Momentum[k, D], Momentum[p, D]],
        DiracGamma[Momentum[FFp, D], D] → -av2 DiracGamma[Momentum[k, D], D]
                  Pair[Momentum[k, D], Momentum[p, D]],
          FFpv[\mu] \rightarrow -av2 kp kv[\mu]
FToEps =
      \{FDpv[\mu_{-}] \rightarrow Contract[1/2 Eps[LorentzIndex[\mu, D], LorentzIndex[\nu, D], LorentzIndex[\nu, D], LorentzIndex[\mu, D], LorentzIndex[\nu, D], LorentzIndex
                                \alpha 2, D], LorentzIndex[\alpha 3, D]] (kv[\alpha 2] av[\alpha 3] - av[\alpha 2] kv[\alpha 3]) pv[\nu]]
Gamma5toTrippleGamma = \{GAD[\mu_{-}].GA[5] Eps[LorentzIndex[\mu_{-}, D],
                      Momentum[a_, D], Momentum[b_, D], Momentum[c_, D]] \rightarrow
             Contract[I Pair[LorentzIndex[α1, D], Momentum[a, D]] Pair[LorentzIndex[α2, D],
                           Momentum[b, D]] Pair[LorentzIndex[\alpha3, D], Momentum[c, D]] (GAD[\alpha1, \alpha2, \alpha3] -
                                 \left( MTD[\alpha 1, \alpha 2] GAD[\alpha 3] + MTD[\alpha 2, \alpha 3] GAD[\alpha 1] - MTD[\alpha 1, \alpha 3] GAD[\alpha 2] \right) \right]
\left\{F(\alpha_{-},\beta_{-}) \rightarrow a^{\beta} k^{\alpha} - a^{\alpha} k^{\beta}, \gamma \cdot \text{Fp} \rightarrow (a \cdot p) \gamma \cdot k - \gamma \cdot a(k \cdot p), \gamma \cdot \text{FFp} \rightarrow a^{2} (-(\gamma \cdot k)) (k \cdot p), \text{FFp}^{\mu_{-}} \rightarrow a^{2} (-k^{\mu}) (k \cdot p)\right\}
\left\{ \operatorname{FDp}^{\mu_{-}} \to -\epsilon^{\mu \, \overline{a} \, \overline{k} \, \overline{p}} \right\}
\left\{\gamma^{\mu_{-}}.\overline{\gamma^{5}}\,\epsilon^{\mu_{-}\,\overline{a_{-}}\,\overline{b_{-}}\,\overline{c_{-}}}\rightarrow -i\,\left(a\cdot b\right)\,\gamma\cdot c+i\,\left(a\cdot c\right)\,\gamma\cdot b-i\,\gamma\cdot a\,(b\cdot c)+i\,\left(\gamma\cdot a\right).(\gamma\cdot b).(\gamma\cdot c)\right\}
```

```
FxToak = \{Ft[\alpha_{\beta}] \rightarrow kv[\alpha] \ av[\beta] - av[\alpha] \ kv[\beta], \ DiracGamma[Momentum[Fx, D], D] \rightarrow kv[\alpha] \ av[\beta] \ av[\beta] \ av[\beta], \ DiracGamma[Momentum[Fx, D], D] \ av[\beta] \ av[\beta] \ av[\beta], \ DiracGamma[Momentum[Fx, D], D] \ av[\beta] \ av[\beta] \ av[\beta], \ DiracGamma[Momentum[Fx, D], D] \ av[\beta] \ av[\beta], \ DiracGamma[Momentum[Fx, D], D] \ av
           DiracGamma[Momentum[k, D], D] Pair[Momentum[a, D], Momentum[x, D]] -
              DiracGamma[Momentum[a, D], D] Pair[Momentum[k, D], Momentum[x, D]],
       DiracGamma[Momentum[FFx, D], D] → -av2 DiracGamma[Momentum[k, D], D]
               Pair[Momentum[k, D], Momentum[x, D]],
        FFxv[\mu] \rightarrow -av2 kx kv[\mu], \sigma F \rightarrow
           -2 I DiracGamma[Momentum[a, D], D].DiracGamma[Momentum[k, D], D] }
FxToEps = \{FDx[\mu_{-}] \rightarrow Contract[1/2 Eps[LorentzIndex[\mu, D], LorentzIndex[\nu, D],
                      LorentzIndex[\alpha 2, D], LorentzIndex[\alpha 3, D]] (kv[\alpha 2] av[\alpha 3] - av[\alpha 2] kv[\alpha 3])
                  xv[v]], DiracGamma[Momentum[FDx, D], D].DiracGamma[5] →
           Contract [1/2 \text{ Eps}[LorentzIndex}[\mu, D], LorentzIndex}[\nu, D],
                      LorentzIndex[α2, D], LorentzIndex[α3, D]]
                   (kv[\alpha 2] av[\alpha 3] - av[\alpha 2] kv[\alpha 3]) xv[\nu] GAD[\mu].DiracGamma[5]]
Gamma5toTrippleGammax = {DiracGamma[LorentzIndex[\(\mu_\), D], D].DiracGamma[5]}
               Eps[LorentzIndex[\mu_, D], Momentum[a_, D], Momentum[b_, D], Momentum[c_, D]] \rightarrow
           Contract[I Pair[LorentzIndex[α1, D], Momentum[a, D]] Pair[LorentzIndex[α2, D],
                     Momentum[b, D]] Pair[LorentzIndex[\alpha3, D], Momentum[c, D]] (GAD[\alpha1, \alpha2, \alpha3] -
                          \{ MTD[\alpha 1, \alpha 2] GAD[\alpha 3] + MTD[\alpha 2, \alpha 3] GAD[\alpha 1] - MTD[\alpha 1, \alpha 3] GAD[\alpha 2] \} \}
\{F(\alpha_{-}, \beta_{-}) \rightarrow a^{\beta} k^{\alpha} - a^{\alpha} k^{\beta}, \gamma \cdot Fx \rightarrow (a \cdot x) \gamma \cdot k - \gamma \cdot a (k \cdot x),
     \gamma \cdot \text{FFx} \rightarrow a^2 \left( -(\gamma \cdot k) \right) (k \cdot x), \text{ FFx}^{\mu_-} \rightarrow a^2 \left( -k^{\mu} \right) (k \cdot x), \sigma F \rightarrow -2 i (\gamma \cdot a).(\gamma \cdot k)
\left\{ \mathrm{FDx}(\mu_-) \to -\epsilon^{\mu\,\overline{a}\,\overline{k}\,\overline{x}}, \; (\gamma \cdot \mathrm{FDx}).\overline{\gamma}^5 \to -\gamma^{\mu}.\overline{\gamma}^5 \; \epsilon^{\mu\,\overline{a}\,\overline{k}\,\overline{x}} \right\}
\left\{\gamma^{\mu_{-}}.\overline{\gamma^{5}}\,\epsilon^{\mu_{-}} \overline{a_{-}} \overline{b_{-}} \overline{c_{-}} \rightarrow -i\,(a\cdot b)\,\gamma\cdot c + i\,(a\cdot c)\,\gamma\cdot b - i\,\gamma\cdot a\,(b\cdot c) + i\,(\gamma\cdot a).(\gamma\cdot b).(\gamma\cdot c)\right\}
S = m sf
V[\mu_{-}] = pv[\mu] v1 + e^2 FFpv[\mu] / m^4 / \chi p^2 v2
T[\mu_{-}, \nu_{-}] = e Ft[\mu, \nu] / m / \chi p tf
A[\mu] = e FDpv[\mu] / m^2 / \chi p af
\epsilon [\mu] = e FDpv[\mu] / m^3 / \chi p
m \, sf
 \frac{e^2 \text{ v2 FFp}^{\mu}}{m^4 \chi \text{p}^2} + \text{v1 } p^{\mu}
 e \operatorname{tf} F(\mu, \nu)
      m\chi p
af e \, \mathrm{FDp}^{\mu}
    m^2 \chi p
  m^3 \chi p
```

 $Scp[sgn_] = (S - GAD[\alpha] V[\alpha] - I/2 (GAD[\alpha, \beta] - GAD[\beta, \alpha]) T[\alpha, \beta] + A[\alpha] GAD[\alpha].GA[5]).$  $(1 + sgn \in [\mu] GAD[\mu] \cdot GA[5])$  /. FToEps /. FToak /. Gamma5toTrippleGamma

$$\left( -\frac{\operatorname{af} e \left( i \left( a \cdot p \right) \gamma \cdot k - i \gamma \cdot a \left( k \cdot p \right) + i \left( \gamma \cdot a \right) . \left( \gamma \cdot k \right) . \left( \gamma \cdot p \right) \right)}{m^{2} \chi p} - \gamma^{\alpha} \left( \operatorname{v1} p^{\alpha} - \frac{a^{2} e^{2} \operatorname{v2} k^{\alpha} \left( k \cdot p \right)}{m^{4} \chi p^{2}} \right) - \frac{i e \operatorname{tf} \left( \gamma^{\alpha} . \gamma^{\beta} - \gamma^{\beta} . \gamma^{\alpha} \right) \left( a^{\beta} k^{\alpha} - a^{\alpha} k^{\beta} \right)}{2 m \chi p} + m \operatorname{sf} \right) \left( 1 - \frac{e \operatorname{sgn} \left( i \left( a \cdot p \right) \gamma \cdot k - i \gamma \cdot a \left( k \cdot p \right) + i \left( \gamma \cdot a \right) . \left( \gamma \cdot k \right) . \left( \gamma \cdot p \right) \right)}{m^{3} \chi p} \right)$$

Epx2 = Ep[x2, p]

EpBarx1 = EpC[x1, p]

$$\left\{1 - \frac{e(k \cdot x2)(\gamma \cdot k).(\gamma \cdot a)}{2(k \cdot p)}, \frac{a^2 e^2 (k \cdot x2)^3}{6(k \cdot p)} + \frac{e(a \cdot p)(k \cdot x2)^2}{2(k \cdot p)} - p \cdot x2\right\} \\
\left\{1 - \frac{e(k \cdot x1)(\gamma \cdot a).(\gamma \cdot k)}{2(k \cdot p)}, - \frac{a^2 e^2 (k \cdot x1)^3}{6(k \cdot p)} - \frac{e(a \cdot p)(k \cdot x1)^2}{2(k \cdot p)} + p \cdot x1\right\}$$

Matrix = Epx2[[1]].Scp[g].EpBarx1[[1]]

Coeff =  $i / 2 \Lambda^{(4-D)} / (2\pi) D/ DdInv[\xi]$ 

Phase = Epx2[[2]] + EpBarx1[[2]]

$$\left(1 - \frac{e\left(k \cdot \mathbf{x2}\right)\left(\gamma \cdot k\right).\left(\gamma \cdot a\right)}{2\left(k \cdot p\right)}\right) \cdot \left(-\frac{\operatorname{af} e\left(i\left(a \cdot p\right)\gamma \cdot k - i\gamma \cdot a\left(k \cdot p\right) + i\left(\gamma \cdot a\right).\left(\gamma \cdot k\right).\left(\gamma \cdot p\right)\right)}{m^{2} \chi \mathbf{p}} - \frac{\gamma^{\alpha} \left(\operatorname{v1} p^{\alpha} - \frac{a^{2} e^{2} \operatorname{v2} k^{\alpha} \left(k \cdot p\right)}{m^{4} \chi \mathbf{p}^{2}}\right) - \frac{i e \operatorname{tf}\left(\gamma^{\alpha}.\gamma^{\beta} - \gamma^{\beta}.\gamma^{\alpha}\right)\left(a^{\beta} k^{\alpha} - a^{\alpha} k^{\beta}\right)}{2 m \chi \mathbf{p}} + m \operatorname{sf}\right) \cdot \\ \left(1 - \frac{e \zeta\left(i\left(a \cdot p\right)\gamma \cdot k - i\gamma \cdot a\left(k \cdot p\right) + i\left(\gamma \cdot a\right).\left(\gamma \cdot k\right).\left(\gamma \cdot p\right)\right)}{m^{3} \chi \mathbf{p}}\right) \cdot \left(1 - \frac{e\left(k \cdot \mathbf{x1}\right)\left(\gamma \cdot a\right).\left(\gamma \cdot k\right)}{2\left(k \cdot p\right)}\right) \cdot \left(1 - \frac{e\left(k \cdot \mathbf{x1}\right)\left(\gamma \cdot a\right).\left(\gamma \cdot k\right)}{2\left(k \cdot p\right)}\right) \cdot \left(1 - \frac{e\left(k \cdot \mathbf{x1}\right)\left(\gamma \cdot a\right).\left(\gamma \cdot k\right)}{2\left(k \cdot p\right)}\right) \cdot \left(1 - \frac{e\left(k \cdot \mathbf{x1}\right)\left(\gamma \cdot a\right).\left(\gamma \cdot k\right)}{2\left(k \cdot p\right)}\right) \cdot \left(1 - \frac{e\left(k \cdot \mathbf{x1}\right)\left(\gamma \cdot a\right).\left(\gamma \cdot k\right)}{2\left(k \cdot p\right)}\right) \cdot \left(1 - \frac{e\left(k \cdot \mathbf{x1}\right)\left(\gamma \cdot a\right).\left(\gamma \cdot k\right)}{2\left(k \cdot p\right)}\right) \cdot \left(1 - \frac{e\left(k \cdot \mathbf{x1}\right)\left(\gamma \cdot a\right).\left(\gamma \cdot k\right)}{2\left(k \cdot p\right)}\right) \cdot \left(1 - \frac{e\left(k \cdot \mathbf{x1}\right)\left(\gamma \cdot a\right).\left(\gamma \cdot k\right)}{2\left(k \cdot p\right)}\right) \cdot \left(1 - \frac{e\left(k \cdot \mathbf{x1}\right)\left(\gamma \cdot a\right).\left(\gamma \cdot k\right)}{2\left(k \cdot p\right)}\right) \cdot \left(1 - \frac{e\left(k \cdot \mathbf{x1}\right)\left(\gamma \cdot a\right).\left(\gamma \cdot k\right)}{2\left(k \cdot p\right)}\right) \cdot \left(1 - \frac{e\left(k \cdot \mathbf{x1}\right)\left(\gamma \cdot a\right).\left(\gamma \cdot k\right)}{2\left(k \cdot p\right)}\right) \cdot \left(1 - \frac{e\left(k \cdot \mathbf{x1}\right)\left(\gamma \cdot a\right).\left(\gamma \cdot k\right)}{2\left(k \cdot p\right)}\right) \cdot \left(1 - \frac{e\left(k \cdot \mathbf{x1}\right)\left(\gamma \cdot a\right).\left(\gamma \cdot k\right)}{2\left(k \cdot p\right)}\right) \cdot \left(1 - \frac{e\left(k \cdot \mathbf{x1}\right)\left(\gamma \cdot a\right).\left(\gamma \cdot k\right)}{2\left(k \cdot p\right)}\right) \cdot \left(1 - \frac{e\left(k \cdot \mathbf{x1}\right)\left(\gamma \cdot a\right).\left(\gamma \cdot k\right)}{2\left(k \cdot p\right)}\right) \cdot \left(1 - \frac{e\left(k \cdot \mathbf{x1}\right)\left(\gamma \cdot a\right).\left(\gamma \cdot k\right)}{2\left(k \cdot p\right)}\right) \cdot \left(1 - \frac{e\left(k \cdot \mathbf{x1}\right)\left(\gamma \cdot a\right)}{2\left(k \cdot p\right)}\right) \cdot \left(1 - \frac{e\left(k \cdot \mathbf{x1}\right)\left(\gamma \cdot a\right)}{2\left(k \cdot p\right)}\right) \cdot \left(1 - \frac{e\left(k \cdot \mathbf{x1}\right)\left(\gamma \cdot a\right)}{2\left(k \cdot p\right)}\right) \cdot \left(1 - \frac{e\left(k \cdot \mathbf{x1}\right)\left(\gamma \cdot a\right)}{2\left(k \cdot p\right)}\right) \cdot \left(1 - \frac{e\left(k \cdot \mathbf{x1}\right)\left(\gamma \cdot a\right)}{2\left(k \cdot p\right)}\right) \cdot \left(1 - \frac{e\left(k \cdot \mathbf{x1}\right)\left(\gamma \cdot a\right)}{2\left(k \cdot p\right)}\right) \cdot \left(1 - \frac{e\left(k \cdot \mathbf{x1}\right)\left(\gamma \cdot a\right)}{2\left(k \cdot p\right)}\right) \cdot \left(1 - \frac{e\left(k \cdot \mathbf{x1}\right)\left(\gamma \cdot a\right)}{2\left(k \cdot p\right)}\right) \cdot \left(1 - \frac{e\left(k \cdot \mathbf{x1}\right)\left(\gamma \cdot a\right)}{2\left(k \cdot p\right)}\right) \cdot \left(1 - \frac{e\left(k \cdot \mathbf{x1}\right)\left(\gamma \cdot a\right)}{2\left(k \cdot p\right)}\right) \cdot \left(1 - \frac{e\left(k \cdot \mathbf{x1}\right)\left(\gamma \cdot a\right)}{2\left(k \cdot p\right)}\right) \cdot \left(1 - \frac{e\left(k \cdot \mathbf{x1}\right)\left(\gamma \cdot a\right)}{2\left(k \cdot p\right)}\right) \cdot \left(1 - \frac{e\left(k \cdot \mathbf{x1}\right)\left(\gamma \cdot a\right)}{2\left(k \cdot p\right)}\right) \cdot \left(1 - \frac{e\left(k \cdot \mathbf{x1}$$

$$\frac{i \, 2^{-D-1} \, \pi^{-D} \, \Lambda^{4-D}}{\text{DdInv}(\zeta)}$$

 $-\frac{a^2 e^2 (k \cdot x1)^3}{6 (k \cdot p)} + \frac{a^2 e^2 (k \cdot x2)^3}{6 (k \cdot p)} - \frac{e (a \cdot p) (k \cdot x1)^2}{2 (k \cdot p)} + \frac{e (a \cdot p) (k \cdot x2)^2}{2 (k \cdot p)} + p \cdot x1 - p \cdot x2$ 

Matrix1 = Contract[DiracSimplify[Matrix]] Coeff1 = Coeff; Phase1 = Phase;

$$\frac{i\, v2\, \zeta\, (\gamma\cdot k).(\gamma\cdot a)\, a^2\, (\,k\cdot\,p)^2\, e^3}{m^7\, \chi p^3} + \frac{af\, \zeta\, (\gamma\cdot a).(\gamma\cdot k)\, a^2\, (\,k\cdot\,p)\, (\,k\cdot\,x1)\, e^3}{2\, m^5\, \chi p^2} + \frac{af\, \zeta\, (\gamma\cdot k).(\gamma\cdot a)\, a^2\, (\,k\cdot\,p)\, (\,k\cdot\,x2)\, e^3}{2\, m^5\, \chi p^2} - \frac{i\, v1\, \zeta\, (\gamma\cdot a).(\gamma\cdot k)\, a^2\, (\,k\cdot\,x1)\, (\,k\cdot\,x2)\, e^3}{m^5\, \chi p^2} - \frac{af\, \zeta\, a^2\, (\,k\cdot\,p)^2\, e^2}{m^5\, \chi p^2} + \frac{v2\, \gamma\cdot k\, a^2\, (\,k\cdot\,p)\, e^2}{m^4\, \chi p^2} + \frac{2\, tf\, \zeta\, \gamma\cdot k\, a^2\, (\,k\cdot\,p)\, e^2}{m^4\, \chi p^2} - \frac{af\, \zeta\, (\gamma\cdot k).(\gamma\cdot a)\, (\,a\cdot\,p)\, (\,k\cdot\,p)\, e^2}{m^5\, \chi p^2} + \frac{i\, sf\, \zeta\, \gamma\cdot k\, a^2\, (\,k\cdot\,x1)\, e^2}{2\, m^2\, \chi p} + \frac{i\, af\, \gamma\cdot k\, a^2\, (\,k\cdot\,x1)\, e^2}{2\, m^2\, \chi p} + \frac{i\, af\, \gamma\cdot k\, a^2\, (\,k\cdot\,x1)\, e^2}{2\, m^3\, \chi p} + \frac{i\, v1\, \zeta\, (\gamma\cdot p).(\gamma\cdot k)\, a^2\, (\,k\cdot\,x1)\, e^2}{2\, m^3\, \chi p} + \frac{i\, v1\, \zeta\, (\gamma\cdot p).(\gamma\cdot k)\, a^2\, (\,k\cdot\,x1)\, e^2}{2\, m^3\, \chi p} + \frac{i\, v1\, \zeta\, (\gamma\cdot k).(\gamma\cdot a)\, (\,a\cdot\,p)\, (\,k\cdot\,x2)\, e^2}{2\, m^3\, \chi p} + \frac{i\, v1\, \zeta\, (\gamma\cdot k).(\gamma\cdot a)\, e^2}{m^3\, \chi p} + \frac{i\, v1\, \zeta\, (\gamma\cdot k).(\gamma\cdot a)\, (\,a\cdot\,p)\, (\,k\cdot\,x2)\, e^2}{m^3\, \chi p} + \frac{i\, v1\, \zeta\, (\gamma\cdot k).(\gamma\cdot a)\, e}{m^3\, \chi p} + \frac{i\, v1\, \zeta\, (\gamma\cdot k).(\gamma\cdot a)\, e}{m^3\, \chi p} + \frac{i\, v1\, \zeta\, (\gamma\cdot k).(\gamma\cdot a)\, e}{m^3\, \chi p} + \frac{i\, v1\, \zeta\, (\gamma\cdot k).(\gamma\cdot a)\, e}{m^3\, \chi p} + \frac{i\, v1\, \zeta\, (\gamma\cdot k).(\gamma\cdot a)\, e}{m^3\, \chi p} + \frac{i\, v1\, \zeta\, (\gamma\cdot k).(\gamma\cdot b)\, e}{m^3\, \chi p} + \frac{i\, v1\, \zeta\, (\gamma\cdot k).(\gamma\cdot b)\, e}{m^3\, \chi p} + \frac{i\, v1\, \zeta\, (\gamma\cdot k).(\gamma\cdot b)\, e}{m^3\, \chi p} + \frac{i\, v1\, \zeta\, (\gamma\cdot k).(\gamma\cdot b)\, e}{m^3\, \chi p} + \frac{i\, v1\, \zeta\, (\gamma\cdot k).(\gamma\cdot b)\, e}{m^3\, \chi p} + \frac{i\, v1\, \zeta\, (\gamma\cdot k).(\gamma\cdot b)\, e}{m^3\, \chi p} + \frac{i\, v1\, \zeta\, (\gamma\cdot k).(\gamma\cdot b)\, e}{m^3\, \chi p} + \frac{i\, v1\, \zeta\, (\gamma\cdot k).(\gamma\cdot b)\, e}{m^3\, \chi p} + \frac{i\, v1\, \zeta\, (\gamma\cdot k).(\gamma\cdot b)\, e}{m^3\, \chi p} + \frac{i\, v1\, \zeta\, (\gamma\cdot k).(\gamma\cdot k)\, e}{m^3\, \chi p} + \frac{i\, v1\, \zeta\, (\gamma\cdot k).(\gamma\cdot k)\, e}{m^3\, \chi p} + \frac{i\, v1\, \zeta\, (\gamma\cdot k).(\gamma\cdot k)\, e}{m^3\, \chi p} + \frac{i\, v1\, \zeta\, (\gamma\cdot k).(\gamma\cdot k)\, e}{m^3\, \chi p} + \frac{i\, v1\, \zeta\, (\gamma\cdot k).(\gamma\cdot k)\, e}{m^3\, \chi p} + \frac{i\, v1\, \zeta\, (\gamma\cdot k).(\gamma\cdot k)\, e}{m^3\, \chi p} + \frac{i\, v1\, \zeta\, (\gamma\cdot k).(\gamma\cdot k)\, e}{m^3\, \chi p} + \frac{i\, v1\, \zeta\, (\gamma\cdot k).(\gamma\cdot k)\, e}{m^3\, \chi p} + \frac{i\, v1\, \zeta\, (\gamma\cdot k).(\gamma\cdot k)\, e}{m^3\, \chi p} + \frac{i\, v1\, \zeta\, (\gamma\cdot k).(\gamma\cdot k)\, e}{m^3\, \chi p} + \frac{i\, v1\, \zeta\, (\gamma\cdot k).(\gamma\cdot k)\, e}{m^3\, \chi p} + \frac{i\, v1\, \zeta\, (\gamma\cdot k).(\gamma\cdot k)\, e}{m^3\, \chi p} + \frac{i\, v1\, \zeta\, (\gamma\cdot k).(\gamma\cdot k)\, e$$

(\*a small test\*)

$$\begin{array}{l} \left( \left( \operatorname{Matrix1} / . \left\{ \operatorname{sf} \to \mathbf{1}, \, \operatorname{v1} \to -\mathbf{1}, \, \operatorname{v2} \to \mathbf{0}, \, \operatorname{t} \to \, \mathbf{0}, \, \operatorname{af} \to \mathbf{0}, \, \mathcal{E} \to \, \mathbf{1} \right\} \right) + \\ \left( \operatorname{Matrix1} / . \left\{ \operatorname{sf} \to \mathbf{1}, \, \operatorname{v1} \to -\mathbf{1}, \, \operatorname{v2} \to \mathbf{0}, \, \operatorname{t} \to \, \mathbf{0}, \, \operatorname{af} \to \mathbf{0}, \, \mathcal{E} \to -\mathbf{1} \right\} \right) \right) / 2 \\ \\ \frac{1}{2} \left( -\frac{a^2 \, e^2 \, \gamma \cdot k \, (k \cdot \operatorname{x1}) \, (k \cdot \operatorname{x2})}{k \cdot p} - \frac{e \, m \, (k \cdot \operatorname{x1}) \, (\gamma \cdot a) \cdot (\gamma \cdot k)}{k \cdot p} - \frac{e \, m \, (k \cdot \operatorname{x2}) \, (\gamma \cdot k) \cdot (\gamma \cdot a)}{k \cdot p} + \frac{2 \, i \, \operatorname{etf} \, (\gamma \cdot a) \cdot (\gamma \cdot k)}{m \, \chi \operatorname{p}} - \frac{2 \, i \, \operatorname{etf} \, (\gamma \cdot k) \cdot (\gamma \cdot a) \cdot (\gamma \cdot e)}{k \cdot p} - \frac{e \, (k \cdot \operatorname{x2}) \, (\gamma \cdot k) \cdot (\gamma \cdot a) \cdot (\gamma \cdot p)}{k \cdot p} + 2 \, m + 2 \, \gamma \cdot p \right) \end{array}$$

Matrix2 = Expand[ExpandScalarProduct[

```
Matrix1 /. {Momentum[x1, D] → Momentum[X, D] - Momentum[x, D] /2,
                                                                                                                                                                                               Momentum[x2, D] \rightarrow Momentum[X, D] + Momentum[x, D] / 2 ] ]
Coeff2 = Coeff1;
Phase2 = Expand
                                                                            ExpandScalarProduct[Phase1 /. \{Momentum[x1, D] \rightarrow Momentum[X, D] - Momentum[x, D] / 2,
                                                                                                                                                                                               Momentum[x2, D] \rightarrow Momentum[X, D] + Momentum[x, D] / 2 ]
    \frac{i\, \text{v2}\, \zeta\, (\gamma \cdot k). (\gamma \cdot a)\, a^2\, (\,\,k \cdot p\,)^2\, e^3}{m^7\, \,\text{vp}^3} + \frac{i\, \text{v1}\, \zeta\, (\gamma \cdot a). (\gamma \cdot k)\, a^2\, (\,\,k \cdot x\,)^2\, e^3}{8\, \,m^3\, \,\text{vp}} - \frac{i\, \text{v1}\, \zeta\, (\gamma \cdot a). (\gamma \cdot k)\, a^2\, (\,\,k \cdot X\,)^2\, e^3}{2\, \,m^3\, \,\text{vp}}
                                                                  \frac{\operatorname{af}\zeta\left(\gamma\cdot a\right).\left(\gamma\cdot k\right)a^{2}\left(k\cdot p\right)\left(k\cdot x\right)e^{3}}{4\;m^{5}\;\chi\mathrm{p}^{2}}+\frac{\operatorname{af}\zeta\left(\gamma\cdot k\right).\left(\gamma\cdot a\right)a^{2}\left(k\cdot p\right)\left(k\cdot x\right)e^{3}}{4\;m^{5}\;\chi\mathrm{p}^{2}}+\frac{\operatorname{af}\zeta\left(\gamma\cdot a\right).\left(\gamma\cdot k\right)a^{2}\left(k\cdot p\right)\left(k\cdot X\right)e^{3}}{2\;m^{5}\;\chi\mathrm{p}^{2}}+\frac{\operatorname{af}\zeta\left(\gamma\cdot a\right).\left(\gamma\cdot k\right)a^{2}}{2\;m^{5}\;\chi\mathrm{p}^{2}}+\frac{\operatorname{af}\zeta\left(\gamma\cdot a\right).\left(\gamma\cdot k\right)a^{2}}+\frac{\operatorname{af}\zeta\left(\gamma\cdot a\right).\left(\gamma\cdot k\right)a^{2}}{2\;m
                                                              \frac{\operatorname{af}\zeta\left(\gamma\cdot k\right).\left(\gamma\cdot a\right)a^{2}\left(k\cdot p\right)\left(k\cdot X\right)e^{3}}{2\;m^{5}\;\chi \mathsf{p}^{2}}-\frac{\operatorname{af}\zeta\,a^{2}\left(\;k\cdot p\;\right)^{2}\,e^{2}}{m^{5}\;\chi \mathsf{p}^{2}}-\frac{\operatorname{v1}\;\gamma\cdot k\;a^{2}\left(\;k\cdot x\right)^{2}\,e^{2}}{8\left(k\cdot p\right)}+\frac{\operatorname{v1}\;\gamma\cdot k\;a^{2}\left(\;k\cdot X\right)^{2}\,e^{2}}{2\left(k\cdot p\right)}+\frac{\operatorname{v1}\;\gamma\cdot k\;a^{2}}{2\left(k\cdot p\right)}+\frac{\operatorname{v1}\;\gamma\cdot k\;a^{2}}
                                                              \frac{\text{v2}\,\gamma\cdot k\,a^{2}\,(k\cdot p)\,e^{2}}{m^{4}\,\chi\text{p}^{2}}+\frac{2\,\text{tf}\,\zeta\,\gamma\cdot k\,a^{2}\,(k\cdot p)\,e^{2}}{m^{4}\,\chi\text{p}^{2}}-\frac{\text{af}\,\zeta\,(\gamma\cdot a).(\gamma\cdot k)\,(a\cdot p)\,(k\cdot p)\,e^{2}}{m^{5}\,\chi\text{p}^{2}}-\frac{\text{af}\,\zeta\,(\gamma\cdot k).(\gamma\cdot a)\,(a\cdot p)\,(k\cdot p)\,e^{2}}{m^{5}\,\chi\text{p}^{2}}
                                                              \frac{i\operatorname{sf}\zeta\gamma\cdot k\,a^{2}\left(k\cdot x\right)e^{2}}{2\,m^{2}\,\chi\mathrm{p}}-\frac{i\operatorname{af}\gamma\cdot k\,a^{2}\left(k\cdot x\right)e^{2}}{2\,m^{2}\,\chi\mathrm{p}}+\frac{i\operatorname{v1}\zeta\left(\gamma\cdot k\right).\left(\gamma\cdot p\right)a^{2}\left(k\cdot x\right)e^{2}}{4\,m^{3}\,\chi\mathrm{p}}+\frac{i\operatorname{v1}\zeta\left(\gamma\cdot p\right).\left(\gamma\cdot k\right)a^{2}\left(k\cdot x\right)e^{2}}{4\,m^{3}\,\chi\mathrm{p}}+\frac{i\operatorname{v1}\zeta\left(\gamma\cdot p\right)a^{2}\left(k\cdot x\right)e^{2}}{4\,m^{3}\,\chi\mathrm{p}}+\frac{i\operatorname{v1}\zeta\left(\gamma\cdot p\right)a^{2}}{4\,m^{3}\,\chi\mathrm{p}}+\frac{i\operatorname{v1}\zeta\left(\gamma\cdot p\right)a^{2}}{4\,m^{3}\,\chi\mathrm{p}}+\frac{i\operatorname{v1
                                                              \frac{i\, \text{v1}\, \zeta\left(\gamma \cdot a\right).\left(\gamma \cdot k\right)\left(a \cdot p\right)\left(k \cdot x\right)\, e^{2}}{2\,\, m^{3}\, \chi\text{p}} + \frac{i\, \text{v1}\, \zeta\left(\gamma \cdot k\right).\left(\gamma \cdot a\right)\left(a \cdot p\right)\left(k \cdot x\right)\, e^{2}}{2\,\, m^{3}\, \chi\text{p}} + \frac{i\, \text{v1}\, \zeta\left(\gamma \cdot k\right).\left(\gamma \cdot p\right)\, a^{2}\, \left(k \cdot X\right)\, e^{2}}{2\,\, m^{3}\, \chi\text{p}} - \frac{i\, \text{v1}\, \zeta\left(\gamma \cdot k\right).\left(\gamma \cdot p\right)\, a^{2}\, \left(k \cdot X\right)\, e^{2}}{2\,\, m^{3}\, \chi\text{p}} - \frac{i\, \text{v1}\, \zeta\left(\gamma \cdot k\right).\left(\gamma \cdot p\right)\, a^{2}\, \left(k \cdot X\right)\, e^{2}}{2\,\, m^{3}\, \chi\text{p}} - \frac{i\, \text{v1}\, \zeta\left(\gamma \cdot k\right).\left(\gamma \cdot p\right)\, a^{2}\, \left(k \cdot X\right)\, e^{2}}{2\,\, m^{3}\, \chi\text{p}} - \frac{i\, \text{v1}\, \zeta\left(\gamma \cdot k\right).\left(\gamma \cdot p\right)\, a^{2}\, \left(k \cdot X\right)\, e^{2}}{2\,\, m^{3}\, \chi\text{p}} - \frac{i\, \text{v1}\, \zeta\left(\gamma \cdot k\right).\left(\gamma \cdot p\right)\, a^{2}\, \left(k \cdot X\right)\, e^{2}}{2\,\, m^{3}\, \chi\text{p}} - \frac{i\, \text{v1}\, \zeta\left(\gamma \cdot k\right).\left(\gamma \cdot p\right)\, a^{2}\, \left(k \cdot X\right)\, e^{2}}{2\,\, m^{3}\, \chi\text{p}} - \frac{i\, \text{v1}\, \zeta\left(\gamma \cdot k\right).\left(\gamma \cdot p\right)\, a^{2}\, \left(k \cdot X\right)\, e^{2}}{2\,\, m^{3}\, \chi\text{p}} - \frac{i\, \text{v1}\, \zeta\left(\gamma \cdot k\right).\left(\gamma \cdot p\right)\, a^{2}\, \left(k \cdot X\right)\, e^{2}}{2\,\, m^{3}\, \chi\text{p}} - \frac{i\, \text{v1}\, \zeta\left(\gamma \cdot k\right).\left(\gamma \cdot p\right)\, a^{2}\, \left(k \cdot X\right)\, e^{2}}{2\,\, m^{3}\, \chi\text{p}} - \frac{i\, \text{v1}\, \zeta\left(\gamma \cdot k\right).\left(\gamma \cdot p\right)\, a^{2}\, \left(k \cdot X\right)\, e^{2}}{2\,\, m^{3}\, \chi\text{p}} - \frac{i\, \text{v1}\, \zeta\left(\gamma \cdot k\right).\left(\gamma \cdot p\right)\, a^{2}\, \left(k \cdot X\right)\, e^{2}}{2\,\, m^{3}\, \chi\text{p}} - \frac{i\, \text{v2}\, \zeta\left(\gamma \cdot k\right).\left(\gamma \cdot p\right)\, a^{2}\, \left(k \cdot X\right)\, e^{2}}{2\,\, m^{3}\, \chi\text{p}} - \frac{i\, \text{v2}\, \zeta\left(\gamma \cdot k\right).\left(\gamma \cdot p\right)\, a^{2}\, \left(k \cdot X\right)\, e^{2}}{2\,\, m^{3}\, \chi\text{p}} - \frac{i\, \text{v2}\, \zeta\left(\gamma \cdot k\right).\left(\gamma \cdot p\right)\, a^{2}\, \left(k \cdot X\right)\, e^{2}}{2\,\, m^{3}\, \chi\text{p}} - \frac{i\, \text{v2}\, \zeta\left(\gamma \cdot k\right).\left(\gamma \cdot p\right)\, a^{2}\, \left(k \cdot X\right)\, e^{2}}{2\,\, m^{3}\, \chi\text{p}} - \frac{i\, \text{v2}\, \zeta\left(\gamma \cdot k\right).\left(\gamma \cdot p\right)\, a^{2}\, \left(k \cdot X\right)\, e^{2}}{2\,\, m^{3}\, \chi\text{p}} - \frac{i\, \text{v2}\, \zeta\left(\gamma \cdot k\right).\left(\gamma \cdot p\right)\, a^{2}\, \left(k \cdot X\right)\, e^{2}}{2\,\, m^{3}\, \chi\text{p}} - \frac{i\, \text{v2}\, \zeta\left(\gamma \cdot k\right).\left(\gamma \cdot p\right)\, a^{2}\, \zeta\left(\gamma \cdot k\right). e^{2}\, q^{2}}{2\,\, m^{3}\, \chi\text{p}} - \frac{i\, \text{v2}\, \zeta\left(\gamma \cdot k\right).\left(\gamma \cdot p\right)\, a^{2}\, \zeta\left(\gamma \cdot k\right). e^{2}\, \zeta\left(\gamma \cdot k\right). e
                                                              \frac{i\,\mathrm{v1}\,\zeta\left(\gamma\cdot p\right).\left(\gamma\cdot k\right)\,a^{2}\,\left(k\cdot X\right)\,e^{2}}{2\,m^{3}\,\chi\mathrm{p}}+\frac{i\,\mathrm{v1}\,\zeta\left(\gamma\cdot a\right).\left(\gamma\cdot k\right)\left(a\cdot p\right)\left(k\cdot X\right)\,e^{2}}{m^{3}\,\chi\mathrm{p}}+\frac{i\,\mathrm{v1}\,\zeta\left(\gamma\cdot k\right).\left(\gamma\cdot a\right)\left(a\cdot p\right)\left(k\cdot X\right)\,e^{2}}{m^{3}\,\chi\mathrm{p}}+\frac{i\,\mathrm{v1}\,\zeta\left(\gamma\cdot k\right).\left(\gamma\cdot k\right)\left(a\cdot p\right)\left(a\cdot k\right)}{m^{3}\,\chi\mathrm{p}}+\frac{i\,\mathrm{v1}\,\zeta\left(\gamma\cdot k\right).\left(\gamma\cdot k\right)\left(a\cdot p\right)\left(a\cdot k\right)}{m^{3}\,\chi\mathrm{p}}+\frac{i\,\mathrm{v1}\,\zeta\left(\gamma\cdot k\right).\left(\gamma\cdot k\right)\left(a\cdot p\right)\left(a\cdot k\right)}{m^{3}\,\chi\mathrm{p}}+\frac{i\,\mathrm{v1}\,\zeta\left(\gamma\cdot k\right).\left(\gamma\cdot k\right)\left(a\cdot p\right)}{m^{3}\,\chi\mathrm{p}}+\frac{i\,\mathrm{v1}\,\zeta\left(\gamma\cdot k\right).\left(\gamma\cdot k\right)}{m^{3}\,\chi\mathrm{p}}+\frac{i\,\mathrm{v1}\,\zeta\left(\gamma\cdot k\right)}{m^{3}\,\chi\mathrm{p}}+\frac{i\,\mathrm{v1}\,\chi\mathrm{p}}{m^{3}\,\chi\mathrm{p}}+\frac{i\,\mathrm{v1}\,\chi\mathrm{p}}{m^{3}\,\chi\mathrm{p}}+\frac{i\,\mathrm{v1}\,\chi\mathrm{p}}{m^{3}\,\chi\mathrm{p}}+\frac{i\,\mathrm{v1}\,\chi\mathrm{p}}{m^{3}\,\chi\mathrm{p}}+\frac{i\,\mathrm{v1}\,\chi\mathrm{p}}{m^{3}\,\chi\mathrm{p}}+\frac{i\,\mathrm{v1}\,\chi\mathrm{p}}{m^{3}\,\chi\mathrm{p}}+\frac{i\,\mathrm{v1}\,\chi\mathrm{p}}{m^{3}\,\chi\mathrm{p}}+\frac{i\,\mathrm{v1}\,\chi\mathrm{p}}{m^{3}\,\chi\mathrm{p}}+\frac{i\,\mathrm{v1}\,\chi\mathrm{p}}{m^{3}\,\chi\mathrm{p}}+\frac{i\,\mathrm{v1}\,\chi\mathrm{p}}{m^{3}\,\chi\mathrm{p}}+\frac{i\,\mathrm{v1}\,\chi\mathrm{p}}{m^{3}\,\chi\mathrm{p}}+\frac{
                                                         \frac{i \operatorname{tf} (\gamma \cdot a).(\gamma \cdot k) \, e}{m \, \chi \mathrm{p}} - \frac{i \operatorname{tf} (\gamma \cdot k).(\gamma \cdot a) \, e}{m \, \chi \mathrm{p}} - \frac{i \operatorname{sf} \zeta \, (\gamma \cdot a).(\gamma \cdot k).(\gamma \cdot p) \, e}{m^2 \, \chi \mathrm{p}} - \frac{i \operatorname{af} (\gamma \cdot a).(\gamma \cdot k).(\gamma \cdot p) \, e}{m^2 \, \chi \mathrm{p}} - \frac{i \operatorname{af} (\gamma \cdot a).(\gamma \cdot k).(\gamma \cdot p) \, e}{m^2 \, \chi \mathrm{p}} - \frac{i \operatorname{af} (\gamma \cdot a).(\gamma \cdot k).(\gamma \cdot p) \, e}{m^2 \, \chi \mathrm{p}} - \frac{i \operatorname{af} (\gamma \cdot a).(\gamma \cdot k).(\gamma \cdot p) \, e}{m^2 \, \chi \mathrm{p}} - \frac{i \operatorname{af} (\gamma \cdot a).(\gamma \cdot k).(\gamma \cdot p) \, e}{m^2 \, \chi \mathrm{p}} - \frac{i \operatorname{af} (\gamma \cdot a).(\gamma \cdot k).(\gamma \cdot p) \, e}{m^2 \, \chi \mathrm{p}} - \frac{i \operatorname{af} (\gamma \cdot a).(\gamma \cdot k).(\gamma \cdot p) \, e}{m^2 \, \chi \mathrm{p}} - \frac{i \operatorname{af} (\gamma \cdot a).(\gamma \cdot k).(\gamma \cdot p) \, e}{m^2 \, \chi \mathrm{p}} - \frac{i \operatorname{af} (\gamma \cdot a).(\gamma \cdot k).(\gamma \cdot p) \, e}{m^2 \, \chi \mathrm{p}} - \frac{i \operatorname{af} (\gamma \cdot a).(\gamma \cdot k).(\gamma \cdot p) \, e}{m^2 \, \chi \mathrm{p}} - \frac{i \operatorname{af} (\gamma \cdot a).(\gamma \cdot k).(\gamma \cdot p) \, e}{m^2 \, \chi \mathrm{p}} - \frac{i \operatorname{af} (\gamma \cdot a).(\gamma \cdot k).(\gamma \cdot p) \, e}{m^2 \, \chi \mathrm{p}} - \frac{i \operatorname{af} (\gamma \cdot a).(\gamma \cdot k).(\gamma \cdot p) \, e}{m^2 \, \chi \mathrm{p}} - \frac{i \operatorname{af} (\gamma \cdot a).(\gamma \cdot k).(\gamma \cdot p) \, e}{m^2 \, \chi \mathrm{p}} - \frac{i \operatorname{af} (\gamma \cdot a).(\gamma \cdot k).(\gamma \cdot p) \, e}{m^2 \, \chi \mathrm{p}} - \frac{i \operatorname{af} (\gamma \cdot a).(\gamma \cdot k).(\gamma \cdot p) \, e}{m^2 \, \chi \mathrm{p}} - \frac{i \operatorname{af} (\gamma \cdot a).(\gamma \cdot k).(\gamma \cdot p) \, e}{m^2 \, \chi \mathrm{p}} - \frac{i \operatorname{af} (\gamma \cdot a).(\gamma \cdot k).(\gamma \cdot p) \, e}{m^2 \, \chi \mathrm{p}} - \frac{i \operatorname{af} (\gamma \cdot a).(\gamma \cdot k).(\gamma \cdot p) \, e}{m^2 \, \chi \mathrm{p}} - \frac{i \operatorname{af} (\gamma \cdot a).(\gamma \cdot k).(\gamma \cdot p) \, e}{m^2 \, \chi \mathrm{p}} - \frac{i \operatorname{af} (\gamma \cdot a).(\gamma \cdot k).(\gamma \cdot p) \, e}{m^2 \, \chi \mathrm{p}} - \frac{i \operatorname{af} (\gamma \cdot a).(\gamma \cdot k).(\gamma \cdot p) \, e}{m^2 \, \chi \mathrm{p}} - \frac{i \operatorname{af} (\gamma \cdot a).(\gamma \cdot k).(\gamma \cdot p) \, e}{m^2 \, \chi \mathrm{p}} - \frac{i \operatorname{af} (\gamma \cdot a).(\gamma \cdot k).(\gamma \cdot p) \, e}{m^2 \, \chi \mathrm{p}} - \frac{i \operatorname{af} (\gamma \cdot a).(\gamma \cdot k).(\gamma \cdot p) \, e}{m^2 \, \chi \mathrm{p}} - \frac{i \operatorname{af} (\gamma \cdot a).(\gamma \cdot k).(\gamma \cdot p) \, e}{m^2 \, \chi \mathrm{p}} - \frac{i \operatorname{af} (\gamma \cdot a).(\gamma \cdot k).(\gamma \cdot p) \, e}{m^2 \, \chi \mathrm{p}} - \frac{i \operatorname{af} (\gamma \cdot a).(\gamma \cdot k).(\gamma \cdot p) \, e}{m^2 \, \chi \mathrm{p}} - \frac{i \operatorname{af} (\gamma \cdot a).(\gamma \cdot k).(\gamma \cdot p) \, e}{m^2 \, \chi \mathrm{p}} - \frac{i \operatorname{af} (\gamma \cdot a).(\gamma \cdot k).(\gamma \cdot p) \, e}{m^2 \, \chi \mathrm{p}} - \frac{i \operatorname{af} (\gamma \cdot a).(\gamma \cdot k).(\gamma \cdot p) \, e}{m^2 \, \chi \mathrm{p}} - \frac{i \operatorname{af} (\gamma \cdot a).(\gamma \cdot k).(\gamma \cdot p) \, e}{m^2 \, \chi \mathrm{p}} - \frac{i \operatorname{af} (\gamma \cdot a).(\gamma \cdot k).(\gamma \cdot p) \, e}{m^2 \, \chi \mathrm{p}} - \frac{i \operatorname{af} (\gamma \cdot a).(\gamma \cdot k).(\gamma \cdot p) \, e}{m^2 \, \chi \mathrm{p}} - \frac{i \operatorname{af} (\gamma \cdot a).(\gamma \cdot k)
                                                              \frac{i\operatorname{sf}\zeta\gamma\cdot k\left(a\cdot p\right)e}{m^{2}\chi\mathrm{p}}-\frac{i\operatorname{af}\gamma\cdot k\left(a\cdot p\right)e}{m^{2}\chi\mathrm{p}}+\frac{2i\operatorname{v1}\zeta\left(\gamma\cdot k\right).\left(\gamma\cdot p\right)\left(a\cdot p\right)e}{m^{3}\chi\mathrm{p}}+\frac{i\operatorname{v1}\zeta\left(\gamma\cdot p\right).\left(\gamma\cdot k\right)\left(a\cdot p\right)e}{m^{3}\chi\mathrm{p}}+\frac{i\operatorname{v1}\zeta\left(\gamma\cdot p\right).\left(\gamma\cdot p\right)\left(a\cdot p\right)e}{m^{3}\chi\mathrm{p}}+\frac{i\operatorname{v1}\zeta\left(\gamma\cdot p\right).\left(\gamma\cdot p\right)e}{m^{3}\chi\mathrm{p}}+\frac{i\operatorname{v1}\zeta\left(\gamma\cdot p\right)e}{m^{3}\chi\mathrm{p}}+\frac{i\operatorname{v1}\zeta\left(\gamma\cdot p\right)e}{m^{3}\chi\mathrm{p}}+\frac{i\operatorname{v1}\zeta\left(\gamma\cdot p\right)e}{m^{3}\chi\mathrm{p}}+\frac{i\operatorname{v1}\zeta\left(\gamma\cdot p\right)e}{m^{3}\chi\mathrm{p}}+\frac{i\operatorname{v1}\zeta\left(\gamma\cdot p\right)e}{m^{3}\chi\mathrm{p}}+\frac{i\operatorname{v1}\zeta\left(\gamma\cdot p\right)e}{m^{3}\chi\mathrm{p}}+\frac{i\operatorname{v1}\zeta\left(\gamma\cdot p\right)e}{m^{3}\chi\mathrm{p}}+\frac{i\operatorname{v1}\zeta\left(\gamma\cdot p\right)e}{m^{3}\chi\mathrm{p}}+\frac{i\operatorname{v1}\zeta
                                                              \frac{i\operatorname{sf}\zeta\gamma\cdot a\left(k\cdot p\right)e}{m^{2}\chi\mathsf{p}}+\frac{i\operatorname{af}\gamma\cdot a\left(k\cdot p\right)e}{m^{2}\chi\mathsf{p}}-\frac{2i\operatorname{v1}\zeta\left(\gamma\cdot a\right).\left(\gamma\cdot p\right)\left(k\cdot p\right)e}{m^{3}\chi\mathsf{p}}-\frac{i\operatorname{v1}\zeta\left(\gamma\cdot p\right).\left(\gamma\cdot a\right)\left(k\cdot p\right)e}{m^{3}\chi\mathsf{p}}+\frac{i\operatorname{v1}\zeta\left(\gamma\cdot p\right).\left(\gamma\cdot p\right)\left(k\cdot p\right)e}{m^{3}\chi\mathsf{p}}+\frac{i\operatorname{v1}\zeta\left(\gamma\cdot p\right).\left(\gamma\cdot p\right)e}{m^{3}\chi\mathsf{p}}+\frac{i\operatorname{v1}\zeta\left(\gamma\cdot p\right).\left(\gamma\cdot p\right)\left(k\cdot p\right)e}{m^{3}\chi\mathsf{p}}+\frac{i\operatorname{v1}\zeta\left(\gamma\cdot p\right)}{m^{3}\chi\mathsf{p}}+\frac{i\operatorname{v1}\zeta\left(\gamma\cdot p\right)}{m^{3}\chi\mathsf{p}}+\frac{i\operatorname{v1}\zeta\left(\gamma\cdot p\right)}{m^{3}\chi\mathsf{p}}+\frac{i\operatorname{v1}\zeta\left(\gamma\cdot p\right)}{m^{3}\chi\mathsf{p}}+\frac{i\operatorname{v1}\zeta\left(\gamma\cdot p\right)}{m^{3}\chi\mathsf{p}}+\frac{i\operatorname{v1}\zeta\left(\gamma\cdot p\right)}{m^{3}\chi\mathsf{p}}+\frac{i\operatorname{v1}\zeta\left(\gamma\cdot p\right)}{m^{3}\chi\mathsf{p}}
                                                                  \frac{m\operatorname{sf}\left(\gamma\cdot a\right).\left(\gamma\cdot k\right)\left(k\cdot x\right)e}{4\left(k\cdot p\right)}-\frac{m\operatorname{sf}\left(\gamma\cdot k\right).\left(\gamma\cdot a\right)\left(k\cdot x\right)e}{4\left(k\cdot p\right)}+\frac{\operatorname{v1}\left(\gamma\cdot k\right).\left(\gamma\cdot a\right).\left(\gamma\cdot p\right)\left(k\cdot x\right)e}{4\left(k\cdot p\right)}
                                                              \frac{\operatorname{v1}\left(\gamma\cdot p\right).\left(\gamma\cdot a\right).\left(\gamma\cdot k\right)\left(k\cdot x\right)e}{4\left(k\cdot p\right)}-\frac{m\operatorname{sf}\left(\gamma\cdot a\right).\left(\gamma\cdot k\right)\left(k\cdot X\right)e}{2\left(k\cdot p\right)}-\frac{m\operatorname{sf}\left(\gamma\cdot k\right).\left(\gamma\cdot a\right)\left(k\cdot X\right)e}{2\left(k\cdot p\right)}
                                                              \frac{\text{v1}\left(\gamma \cdot k\right).\left(\gamma \cdot a\right).\left(\gamma \cdot p\right)\left(k \cdot X\right)e}{2\left(k \cdot p\right)} + \frac{\text{v1}\left(\gamma \cdot p\right).\left(\gamma \cdot a\right).\left(\gamma \cdot k\right)\left(k \cdot X\right)e}{2\left(k \cdot p\right)} + \frac{i\,\text{v1}\,\zeta\left(\gamma \cdot a\right).\left(\gamma \cdot k\right)\,p^{2}\,e}{m^{3}\,\chi\text{p}} + m\,\text{sf} - \text{v1}\,\gamma \cdot p\,\left(k \cdot x\right)\left(k \cdot x\right)e^{2} + \frac{i\,\text{v1}\,\zeta\left(\gamma \cdot a\right).\left(\gamma \cdot k\right)\,p^{2}\,e}{m^{3}\,\chi\text{p}} + \frac{i\,\text{v2}\,\zeta\left(\gamma \cdot a\right).\left(\gamma \cdot k\right)\,p^{2}\,\mu\text{p}} + \frac{i\,\text{v2}\,\zeta\left(\gamma \cdot a\right).\left(\gamma \cdot k\right)\,p^{2}\,\mu\text{p}} + \frac{i\,\text{v2}\,\zeta\left(\gamma \cdot a\right).\left(\gamma \cdot k\right)\,p^{2}\,\mu\text{p}} + \frac{i\,\text{v2}\,\zeta\left(\gamma \cdot a\right).\left(\gamma \cdot a\right
         \frac{a^{2} e^{2} \left(k \cdot x\right) \left(k \cdot X\right)^{2}}{2 \left(k \cdot p\right)}+\frac{a^{2} e^{2} \left(k \cdot x\right)^{3}}{24 \left(k \cdot p\right)}+\frac{e \left(a \cdot p\right) \left(k \cdot x\right) \left(k \cdot X\right)}{k \cdot p}-p \cdot x
```

Matrix3 =

(((Expand[Matrix2 /. TripleGamma]) /. EpsToF) /. FieldSubstitutions) /. akToF Coeff3 = Coeff2;

Phase3 = Phase2;

$$\frac{\text{v2}\,\zeta\,\sigma\text{F}\,a^{2}\,(\,k\cdot\,p\,)^{2}\,e^{3}}{2\,\,m^{7}\,\chi\text{p}^{3}} = \frac{\text{v1}\,\zeta\,\sigma\text{F}\,a^{2}\,(\,k\cdot\,x\,)^{2}\,e^{3}}{16\,\,m^{3}\,\chi\text{p}} + \frac{\text{v1}\,\zeta\,\sigma\text{F}\,a^{2}\,(\,k\cdot\,X\,)^{2}\,e^{3}}{4\,\,m^{3}\,\chi\text{p}} = \frac{i\,\,\text{af}\,\zeta\,\sigma\text{F}\,a^{2}\,(\,k\cdot\,p\,)\,(\,k\cdot\,x\,)\,e^{3}}{4\,\,m^{5}\,\chi\text{p}^{2}} = \frac{\text{af}\,\zeta\,a^{2}\,(\,k\cdot\,p\,)^{2}\,e^{2}}{8\,(\,k\cdot\,p\,)} + \frac{\text{v1}\,\gamma\cdot k\,a^{2}\,(\,k\cdot\,x\,)^{2}\,e^{2}}{2\,(\,k\cdot\,p\,)} + \frac{\text{v2}\,\gamma\cdot k\,a^{2}\,(\,k\cdot\,p\,)\,e^{2}}{m^{4}\,\chi\text{p}^{2}} + \frac{2\,\,\text{tf}\,\zeta\,\gamma\cdot k\,a^{2}\,(\,k\cdot\,x\,)\,e^{2}}{2\,\,m^{2}\,\chi\text{p}} + \frac{i\,\,\text{v1}\,\zeta\,(\,\gamma\cdot\,k\,)\,(\,\gamma\cdot\,p\,)\,a^{2}\,(\,k\cdot\,x\,)\,e^{2}}{4\,\,m^{3}\,\chi\text{p}} + \frac{i\,\,\text{v1}\,\zeta\,(\,\gamma\cdot\,k\,)\,(\,\gamma\cdot\,p\,)\,a^{2}\,(\,k\cdot\,x\,)\,e^{2}}{2\,\,m^{3}\,\chi\text{p}} + \frac{i\,\,\text{v1}\,\zeta\,(\,\gamma\cdot\,k\,)\,(\,\gamma\cdot\,p\,)\,a^{2}\,(\,k\cdot\,x\,)\,e^{2}}{2\,\,m^{3}\,\chi\text{p}} + \frac{i\,\,\text{v1}\,\zeta\,(\,\gamma\cdot\,k\,)\,(\,\gamma\cdot\,p\,)\,a^{2}\,(\,k\cdot\,x\,)\,e^{2}}{2\,\,m^{3}\,\chi\text{p}} + \frac{i\,\,\text{v1}\,\zeta\,(\,\gamma\cdot\,p\,)\,(\,\gamma\cdot\,k\,)\,a^{2}\,(\,k\cdot\,x\,)\,e^{2}}{2\,\,m^{3}\,\chi\text{p}} + \frac{i\,\,\text{v1}\,\zeta\,(\,\gamma\cdot\,p\,)\,(\,\gamma\cdot\,k\,)\,a^{2}\,(\,k\cdot\,x\,)\,e^{2}}{2\,\,m^{3}\,\chi\text{p}} + \frac{i\,\,\text{v1}\,\zeta\,(\,\gamma\cdot\,p\,)\,(\,\gamma\cdot\,k\,)\,a^{2}\,(\,k\cdot\,x\,)\,e^{2}}{2\,\,m^{3}\,\chi\text{p}} + \frac{i\,\,\text{v1}\,\zeta\,(\,\gamma\cdot\,p\,)\,(\,\gamma\cdot\,k\,)\,(\,\alpha\cdot\,p\,)\,e}{m^{3}\,\chi\text{p}} + \frac{i\,\,\text{v1}\,\zeta\,(\,\gamma\cdot\,p\,)\,(\,\gamma\cdot\,k\,)\,(\,\alpha\cdot\,p\,)\,e}{m^{3}\,\chi\text{p}} + \frac{i\,\,\text{v1}\,\zeta\,(\,\gamma\cdot\,p\,)\,(\,\gamma\cdot\,k\,)\,(\,\alpha\cdot\,p\,)\,e}{m^{3}\,\chi\text{p}} + \frac{i\,\,\text{v1}\,\zeta\,(\,\gamma\cdot\,p\,)\,(\,\gamma\cdot\,k\,)\,(\,\alpha\cdot\,p\,)\,e}{m^{3}\,\chi\text{p}} + \frac{i\,\,\text{v1}\,\zeta\,(\,\gamma\cdot\,p\,)\,(\,\gamma\cdot\,k\,)\,(\,\gamma\cdot\,p\,)\,(\,\alpha\cdot\,p\,)\,e}{m^{3}\,\chi\text{p}} + \frac{i\,\,\text{v1}\,\zeta\,(\,\gamma\cdot\,p\,)\,(\,\gamma\cdot\,k\,)\,(\,\gamma\cdot\,p\,)\,(\,\alpha\cdot\,p\,)\,e}{m^{3}\,\chi\text{p}} + \frac{i\,\,\text{v1}\,\zeta\,(\,\gamma\cdot\,p\,)\,(\,\gamma\cdot\,k\,)\,(\,\gamma\cdot\,p\,)\,(\,\alpha\cdot\,p\,)\,e}{m^{3}\,\chi\text{p}} + \frac{i\,\,\text{v1}\,\zeta\,(\,\gamma\cdot\,p\,)\,(\,\gamma\cdot\,k\,)\,(\,\gamma\cdot\,p\,)\,(\,\alpha\cdot\,p\,)\,e}{m^{3}\,\chi\text{p}} + \frac{i\,\,\text{v1}\,\zeta\,(\,\gamma\cdot\,p\,)\,(\,\gamma\cdot\,k\,)\,(\,\gamma\cdot\,p\,)\,(\,\gamma\cdot\,k\,)\,(\,\gamma\cdot\,p\,)\,(\,\gamma\cdot\,k\,)\,(\,\gamma\cdot\,p\,)\,(\,\gamma\cdot\,k\,)\,(\,\gamma\cdot\,p\,)\,(\,\gamma\cdot\,k\,)\,(\,\gamma\cdot\,p\,)\,(\,\gamma\cdot\,k\,)\,(\,\gamma\cdot\,p\,)\,(\,\gamma\cdot\,k\,)\,(\,\gamma\cdot\,p\,)\,(\,\gamma\cdot\,k\,)\,(\,\gamma\cdot\,p\,)\,(\,\gamma\cdot\,k\,)\,(\,\gamma\cdot\,p\,)\,(\,\gamma\cdot\,k\,)\,(\,\gamma\cdot\,p\,)\,(\,\gamma\cdot\,k\,)\,(\,\gamma\cdot\,p\,)\,(\,\gamma\cdot\,k\,)\,(\,\gamma\cdot\,p\,)\,(\,\gamma\cdot\,k\,)\,(\,\gamma\cdot\,p\,)\,(\,\gamma\cdot\,k\,)\,(\,\gamma\cdot\,p\,)\,(\,\gamma\cdot\,k\,)\,(\,\gamma\cdot\,p\,)\,(\,\gamma\cdot\,k\,)\,(\,\gamma\cdot\,p\,)\,(\,\gamma\cdot\,k\,)\,(\,\gamma\cdot\,p\,)\,(\,\gamma\cdot\,k\,)\,(\,\gamma\cdot\,p\,)\,(\,\gamma\cdot\,k\,)\,(\,\gamma\cdot\,p\,)\,(\,\gamma\cdot\,k\,)\,(\,\gamma\cdot\,p\,)\,(\,\gamma\cdot\,k\,)\,(\,\gamma\cdot\,p\,)\,(\,\gamma\cdot\,k\,)\,(\,\gamma\cdot\,p\,)\,(\,\gamma\cdot\,k\,)\,(\,\gamma\cdot\,p\,)\,(\,\gamma\cdot\,k\,)\,(\,\gamma\cdot\,p\,)\,(\,\gamma\cdot\,k\,)\,(\,\gamma\cdot\,p\,)\,(\,\gamma\cdot\,k\,)\,(\,\gamma\cdot\,p\,)\,(\,\gamma\cdot\,k\,)\,(\,\gamma\cdot\,p\,)\,(\,\gamma\cdot\,k\,)\,(\,\gamma\cdot\,p\,)\,(\,\gamma\cdot\,k\,)\,(\,\gamma\cdot\,p\,)\,(\,\gamma\cdot\,k\,)\,(\,\gamma\cdot\,p\,)\,(\,\gamma\cdot\,k\,)\,(\,\gamma$$

```
Matrix4 = Contract[
                                                              DiracOrder[
                                                                                                                        Matrix3 /. { DiracGamma [LorentzIndex [β, D], D].DiracGamma [5]
                                                                                                                                                                                                                                                 Pair[LorentzIndex[\beta, D], Momentum[FDp, D]] \rightarrow FVD[\gamma\gamma5FD, \alpha] pv[\alpha]}
                                                                                               ] /. {
                                                                                                                        DiracGamma[Momentum[p, D], D].DiracGamma[Momentum[p, D], D] \rightarrow FVD[\gamma a \gamma, \alpha] pv[\alpha],
                                                                                                                        DiracGamma[Momentum[p, D], D] \rightarrow FVD[\gamma k_{\gamma}, \alpha] pv[\alpha]}
                             ]
   Coeff4 = Coeff3;
       Phase4 = Phase3;
                                    \frac{a^2 \text{ af } e^2 \, \zeta (\,k \cdot p\,)^2}{m^5 \, \chi \mathrm{p}^2} + \frac{a^2 \, e^3 \, \zeta \, \sigma \mathrm{F} \, \mathrm{v2} \, (\,k \cdot p\,)^2}{2 \, m^7 \, \chi \mathrm{p}^3} - \frac{a^2 \, e^3 \, \zeta \, \sigma \mathrm{F} \, \mathrm{v1} \, (\,k \cdot x\,)^2}{16 \, m^3 \, \chi \mathrm{p}} + \frac{a^2 \, e^3 \, \zeta \, \sigma \mathrm{F} \, \mathrm{v1} \, (\,k \cdot X\,)^2}{4 \, m^3 \, \chi \mathrm{p}} - \frac{a^2 \, e^3 \, \zeta \, \sigma \mathrm{F} \, \mathrm{v1} \, (\,k \cdot X\,)^2}{4 \, m^3 \, \chi \mathrm{p}} - \frac{a^2 \, e^3 \, \zeta \, \sigma \mathrm{F} \, \mathrm{v1} \, (\,k \cdot X\,)^2}{4 \, m^3 \, \chi \mathrm{p}} - \frac{a^2 \, e^3 \, \zeta \, \sigma \mathrm{F} \, \mathrm{v1} \, (\,k \cdot X\,)^2}{4 \, m^3 \, \chi \mathrm{p}} - \frac{a^2 \, e^3 \, \zeta \, \sigma \mathrm{F} \, \mathrm{v1} \, (\,k \cdot X\,)^2}{4 \, m^3 \, \chi \mathrm{p}} - \frac{a^2 \, e^3 \, \zeta \, \sigma \mathrm{F} \, \mathrm{v1} \, (\,k \cdot X\,)^2}{4 \, m^3 \, \chi \mathrm{p}} - \frac{a^2 \, e^3 \, \zeta \, \sigma \mathrm{F} \, \mathrm{v1} \, (\,k \cdot X\,)^2}{4 \, m^3 \, \chi \mathrm{p}} - \frac{a^2 \, e^3 \, \zeta \, \sigma \mathrm{F} \, \mathrm{v1} \, (\,k \cdot X\,)^2}{4 \, m^3 \, \chi \mathrm{p}} - \frac{a^2 \, e^3 \, \zeta \, \sigma \mathrm{F} \, \mathrm{v1} \, (\,k \cdot X\,)^2}{4 \, m^3 \, \chi \mathrm{p}} - \frac{a^2 \, e^3 \, \zeta \, \sigma \mathrm{F} \, \mathrm{v1} \, (\,k \cdot X\,)^2}{4 \, m^3 \, \chi \mathrm{p}} - \frac{a^2 \, e^3 \, \zeta \, \sigma \mathrm{F} \, \mathrm{v1} \, (\,k \cdot X\,)^2}{4 \, m^3 \, \chi \mathrm{p}} - \frac{a^2 \, e^3 \, \zeta \, \sigma \mathrm{F} \, \mathrm{v1} \, (\,k \cdot X\,)^2}{4 \, m^3 \, \chi \mathrm{p}} - \frac{a^2 \, e^3 \, \zeta \, \sigma \mathrm{F} \, \mathrm{v1} \, (\,k \cdot X\,)^2}{4 \, m^3 \, \chi \mathrm{p}} - \frac{a^2 \, e^3 \, \zeta \, \sigma \mathrm{F} \, \mathrm{v1} \, (\,k \cdot X\,)^2}{4 \, m^3 \, \chi \mathrm{p}} - \frac{a^2 \, e^3 \, \zeta \, \sigma \mathrm{F} \, \mathrm{v1} \, (\,k \cdot X\,)^2}{4 \, m^3 \, \chi \mathrm{p}} - \frac{a^2 \, e^3 \, \zeta \, \sigma \mathrm{F} \, \mathrm{v1} \, (\,k \cdot X\,)^2}{4 \, m^3 \, \chi \mathrm{p}} - \frac{a^2 \, e^3 \, \zeta \, \sigma \mathrm{F} \, \mathrm{v1} \, (\,k \cdot X\,)^2}{4 \, m^3 \, \chi \mathrm{p}} - \frac{a^2 \, e^3 \, \zeta \, \sigma \mathrm{F} \, \mathrm{v1} \, (\,k \cdot X\,)^2}{4 \, m^3 \, \chi \mathrm{p}} - \frac{a^2 \, e^3 \, \zeta \, \sigma \mathrm{F} \, \mathrm{v1} \, (\,k \cdot X\,)^2}{4 \, m^3 \, \chi \mathrm{p}} - \frac{a^2 \, e^3 \, \zeta \, \sigma \mathrm{F} \, \mathrm{v1} \, (\,k \cdot X\,)^2}{4 \, m^3 \, \chi \mathrm{p}} - \frac{a^2 \, e^3 \, \zeta \, \sigma \mathrm{P} \, \mathrm{v1} \, (\,k \cdot X\,)^2}{4 \, m^3 \, \chi \mathrm{p}} - \frac{a^2 \, e^3 \, \zeta \, \sigma \mathrm{P} \, \mathrm{v1} \, (\,k \cdot X\,)^2}{4 \, m^3 \, \chi \mathrm{p}} - \frac{a^2 \, e^3 \, \zeta \, \sigma \mathrm{P} \, \mathrm{v1} \, (\,k \cdot X\,)^2}{4 \, m^3 \, \chi \mathrm{p}} - \frac{a^2 \, e^3 \, \zeta \, \sigma \mathrm{P} \, \mathrm{v1} \, (\,k \cdot X\,)^2}{4 \, m^3 \, \chi \mathrm{p}} - \frac{a^2 \, e^3 \, \zeta \, \sigma \mathrm{P} \, \mathrm{v1} \, (\,k \cdot X\,)^2}{4 \, m^3 \, \chi \mathrm{p}} - \frac{a^2 \, e^3 \, \zeta \, \sigma \mathrm{P} \, \mathrm{v1} \, (\,k \cdot X\,)^2}{4 \, m^3 \, \chi \mathrm{p}} - \frac{a^2 \, e^3 \, \zeta \, \sigma \mathrm{P} \, \mathrm{v1} \, (\,k \cdot X\,)^2}{4 \, m^3 \, \chi \mathrm{p}} - \frac{a^2 \, e^3 \, \zeta 
                                               \frac{a^2\,e^2\,\mathrm{vl}\,\gamma\cdot k\,(\,k\cdot x\,)^2}{8\,(k\cdot p)} + \frac{a^2\,e^2\,\mathrm{vl}\,\gamma\cdot k\,(\,k\cdot X\,)^2}{2\,(k\cdot p)} - \frac{i\,a^2\,\mathrm{af}\,e^3\,\zeta\,\sigma\mathrm{F}\,(k\cdot p)\,(k\cdot x)}{4\,m^5\,\chi\mathrm{p}^2} - \frac{i\,a^2\,\mathrm{af}\,e^2\,\gamma\cdot k\,(k\cdot x)}{2\,m^2\,\chi\mathrm{p}} + \frac{a^2\,e^2\,\mathrm{vl}\,\gamma\cdot k\,(\,k\cdot x\,)^2}{2\,m^2\,\chi\mathrm{p}} + \frac{a^2\,e^2\,\mu\,\gamma\cdot k\,(\,k\cdot x\,)^2}{2\,m^2\,\chi\mathrm{p}} + \frac{a^2\,e^2\,\mu\,\gamma\cdot k\,(\,k\cdot x\,)^2}{2
                                               \frac{2\,a^{2}\,e^{2}\,\zeta\,\mathrm{tf}\,\gamma\cdot k\,(k\cdot p)}{m^{4}\,\chi\mathrm{p}^{2}}+\frac{a^{2}\,e^{2}\,\mathrm{v}2\,\gamma\cdot k\,(k\cdot p)}{m^{4}\,\chi\mathrm{p}^{2}}+\frac{i\,a^{2}\,e^{2}\,\zeta\,\mathrm{v}1\,(k\cdot p)\,(k\cdot x)}{2\,m^{3}\,\chi\mathrm{p}}+\frac{i\,a^{2}\,e^{2}\,\zeta\,\mathrm{v}1\,(k\cdot X)\,(p\cdot\gamma\mathrm{k}\gamma)}{m^{3}\,\chi\mathrm{p}}-\frac{i\,a^{2}\,e^{2}\,\zeta\,\mathrm{v}1\,(k\cdot y)\,(k\cdot x)}{m^{3}\,\chi\mathrm{p}}+\frac{i\,a^{2}\,e^{2}\,\zeta\,\mathrm{v}1\,(k\cdot y)\,(k\cdot y)\,(k\cdot y)}{m^{3}\,\chi\mathrm{p}}+\frac{i\,a^{2}\,e^{2}\,\zeta\,\mathrm{v}1\,(k\cdot y)\,(k\cdot y)\,(k\cdot y)\,(k\cdot y)}{m^{3}\,\chi\mathrm{p}}+\frac{i\,a^{2}\,e^{2}\,\zeta\,\mathrm{v}1\,(k\cdot y)\,(k\cdot y)\,(k\cdot y)\,(k\cdot y)}{m^{3}\,\chi\mathrm{p}}+\frac{i\,a^{2}\,e^{2}\,\chi\,\mathrm{v}1\,(k\cdot y)\,(k\cdot y)\,(k
                                               \frac{i\,a^{2}\,e^{2}\,\zeta\,\mathrm{v1}\,(k\cdot\,p)\,(k\cdot\,X)}{m^{3}\,\chi\mathrm{p}} - \frac{i\,a^{2}\,e^{2}\,\zeta\,\mathrm{sf}\,\gamma\cdot k\,(k\cdot\,x)}{2\,m^{2}\,\chi\mathrm{p}} + \frac{e\,\mathrm{v1}\,(a\cdot\,p)\,\gamma\cdot k\,(k\cdot\,X)}{k\cdot\,p} - e\,\mathrm{v1}\,\gamma\cdot a\,(k\cdot\,X) + \frac{e\,\mathrm{v1}\,(a\cdot\,p)
                                                   \frac{i\,e\zeta\,\mathrm{vl}\,(a\cdot p)\,(p\cdot\gamma\mathrm{k}\gamma)}{m^3\,\chi\mathrm{p}} + \frac{\mathrm{af}\,e(p\cdot\gamma\gamma5\mathrm{FD})}{m^2\,\chi\mathrm{p}} - \frac{i\,e\zeta\,\mathrm{vl}\,(k\cdot p)\,(p\cdot\gamma\mathrm{a}\gamma)}{m^3\,\chi\mathrm{p}} + \frac{i\,e\,m\,\mathrm{sf}\,\sigma\mathrm{F}\,(k\cdot x)}{4\,(k\cdot p)} - \frac{i\,e\,\omega\,\mathrm{vl}\,(k\cdot p)\,(p\cdot\gamma\mathrm{a}\gamma)}{m^3\,\omega\,\mathrm{vl}} + \frac{i\,e\,m\,\mathrm{sf}\,\sigma\mathrm{F}\,(k\cdot x)}{4\,(k\cdot p)} - \frac{i\,e\,\omega\,\mathrm{vl}\,(k\cdot p)\,(p\cdot\gamma\mathrm{a}\gamma)}{m^3\,\omega\,\mathrm{vl}} + \frac{i\,e\,\omega\,\mathrm{vl}\,(k\cdot p)\,(p\cdot\gamma\mathrm{a}\gamma)}{4\,(k\cdot p)\,(p\cdot\gamma\mathrm{a}\gamma)} - \frac{i\,e\,\omega\,\mathrm{vl}\,(k\cdot p)\,(p\cdot\gamma\mathrm{a}\gamma)}{m^3\,\omega\,\mathrm{vl}} + \frac{i\,e\,\omega\,\mathrm{vl}\,(k\cdot p)\,(p\cdot\gamma\mathrm{a}\gamma)}{m^3\,\omega\,\mathrm{vl}} - \frac{i\,e\,\omega\,\mathrm{vl}\,(k\cdot p)\,(p\cdot\gamma\mathrm{a}\gamma)}{m^3\,\omega\,\mathrm{vl}} + \frac{i\,e\,\omega\,\mathrm{vl}\,(k\cdot p)\,(p\cdot\gamma\mathrm{a}\gamma)}{m^3\,\omega\,\mathrm{vl}} - \frac{i\,e\,\omega\,\mathrm{vl}\,(k\cdot p)\,(p\cdot\gamma\mathrm{a}\gamma)}{m^3\,\omega\,\mathrm{vl}} + \frac{i\,e\,\omega\,\mathrm{vl}\,(k\cdot p)\,(p\cdot\gamma\mathrm{vl}\,(k\cdot p)\,
                                               \frac{i\,e\text{v1}\,(k\cdot x)\,(p\cdot\gamma\gamma5\text{FD})}{2\,(k\cdot p)} - \frac{e\,\zeta\,p^2\,\sigma\text{F}\,\text{v1}}{2\,m^3\,\chi\text{p}} + \frac{e\,\zeta\,\text{sf}\,(p\cdot\gamma\gamma5\text{FD})}{m^2\,\chi\text{p}} - \frac{e\,\sigma\text{F}\,\text{tf}}{m\,\chi\text{p}} + m\,\text{sf} - \text{v1}\,\gamma\cdot p
```

Expanding scalar products into components and changing variables

$$\begin{split} p &\to \left\{ p_- = 1 \; / \; 2 \; \left( p^0 \; - \; p^3 \right) \; \text{,} \; p_+ = p^0 \; + \; p^3 \; \text{,} \; p_\perp \right\} \\ p_- &= \; x_- \; / \; 2 \; s \\ p_+ &= \; \left( p^2 \; + \; p_\perp^2 \right) \; \middle/ \; 2 \; p_- \; = \; s \; \left( p^2 \; + \; p_\perp^2 \right) \; \middle/ \; x_- \end{split}$$

Integration measure

$$\int d^{\mathbf{D}} \mathbf{p} \cdot \cdot \cdot = \int \frac{ds}{2s} \, dp^2 \, d^{D-2} p_{\perp}$$

$$x_{-} = kx / m$$

$$p_{-} = kx / 2 m s$$

$$kp = mp_{-} = mxm/2s = kx/2s$$

$$ap = -atpt$$

$$\gamma p = \gamma_- p_+ + \gamma_+ p_- - \gamma_\perp p_\perp = Gm \frac{s}{x} \left( p^2 + p_\perp^2 \right) + Gp \frac{x_-}{2s} - Gt pt$$

$$\gamma k = \gamma_- k_+ = m Gm$$

$$kx = k_+ x_- = m xm$$

$$(\gamma F^*)^{\mu} \boldsymbol{\cdot} \gamma^5 \rightarrow \left\{ (\gamma F^*)_{-} \boldsymbol{\cdot} \gamma^5 = 0 \,, \quad (\gamma F^*)_{+} \boldsymbol{\cdot} \gamma^5 \,, \quad (\gamma F^*)_{\perp} \boldsymbol{\cdot} \gamma^5 \right\} = \left\{ 0 \,, \, \gamma \gamma 5 F D p \,, \, \gamma \gamma 5 F D t \right\}$$
 
$$(\gamma F^*)_{\mu} k^{\mu} = 0 \rightarrow (\gamma F^*)_{-} = 0$$

$$(\gamma F^*)_{\mu} a^{\mu} = 0 \rightarrow \gamma \gamma 5 FDt at = 0$$

$$(\gamma F^*)^{\mu} \cdot \gamma^5 p_{\mu} = \gamma \gamma 5 FDm * pp$$

$$\gamma k \gamma_{-} = (\gamma k)^{2} / m = 0$$

 $D[{xm/2/s, s(p2+pt2)/xm}, {{s, p2}}]$ 

Abs[Det[%]]

$$\begin{pmatrix}
-\frac{xm}{2 s^2} & 0 \\
\frac{p2+pt2}{xm} & \frac{s}{xm}
\end{pmatrix}$$

$$\frac{1}{2|s|}$$

```
Matrix5 = Collect[
                   Expand [Matrix4 /. {DiracGamma [Momentum[p, D], D] → Gp * pm + Gm * pp - Gt[i] * pt[i],
                                                                                   Pair[Momentum[a, D], Momentum[p, D]] → -at[i1] pt[i1],
                                                                                   Pair [Momentum[p, D], Momentum[γγ5FD, D]] → γγ5FDp * pm,
                                                                                  Pair[Momentum[p, D], Momentum[\gamma a \gamma, D]] \rightarrow
                                                                                           \gamma a \gamma p * pm + \gamma a \gamma m * pp - \gamma a \gamma t[i] * pt[i],
                                                                                   Pair[Momentum[p, D], Momentum[\gamma k \gamma, D]] \rightarrow \gamma k \gamma p * pm - \gamma k \gamma t[i] * pt[i],
                                                                                     (*av2→-at^2,*)
                                                                                   DiracGamma[Momentum[k, D], D] \rightarrow m Gm} /. {\chi k \chi m \rightarrow 0} /. {\chi p \rightarrow \xi k p / m^2} /.
                                                    \left\{ kp \rightarrow kx/2/s, pm \rightarrow xm/2/s \right\} /. \left\{ kx \rightarrow mxm \right\} /. \left\{ pp \rightarrow s \left( pv2 + pt[i2]^2 \right)/xm \right\} \right],
                    {v1, pt[i2] pt[i], pt[i2], pt[i_], pv2, \gamma\gamma5FDm, \gamma\gamma5FDp, \gamma\gamma5FDt[i],
                          ykym, ykyp, ykyt[i], yaym, yayp, yayt[i]}]
   Coefficient[Matrix5, ykyt[i]]
   Coeff5 = Coeff4/2/s
  Phase5 = Collect[
                   Expand [Phase4 /. {Pair [Momentum [p, D], Momentum [x, D]] \rightarrow pp xm + pm xp - pt * xt,
                                                                  kp \rightarrow mpm, Pair[Momentum[a, D], Momentum[p, D]] \rightarrow -at pt} /. \{kp \rightarrow kx/2/s,
                                                           pm \rightarrow xm/2/s /. \{pp \rightarrow s (pv2 + pt^2)/xm\} /. \{xm \rightarrow kx/m\}\}, \{pt, pp\}\}
{\rm v1}\left(\frac{a^2\,e^3\,\zeta\,s\,\sigma{\rm F}\,(\,k\cdot X\,)^2}{2\,m^2\,\xi\,{\rm xm}} + \frac{a^2\,e^2\,{\rm Gm}\,s\,(\,k\cdot X\,)^2}{{\rm xm}} + \right.
                                                \operatorname{pt}(i)\left(-\frac{2\,i\,a^2\,e^2\,\zeta\,s\,\gamma k \gamma \mathsf{t}(i)\,(k\cdot X)}{m^2\,\xi\,\mathrm{xm}} + \frac{2\,i\,e\,\zeta\,s\,\operatorname{at}(i1)\,\gamma k \gamma \mathsf{t}(i)\,\operatorname{pt}(i1)}{m^2\,\xi\,\mathrm{xm}} + \frac{i\,e\,\zeta\,\gamma a \gamma \mathsf{t}(i)}{m\,\xi} + \operatorname{Gt}(i)\right) - \frac{1}{m^2\,\xi\,\mathrm{xm}} + \frac{1}{m^2\,\xi\,\mathrm{
                                               \frac{a^{2} e^{3} \zeta s \sigma F xm}{8 \xi} - \frac{1}{4} a^{2} e^{2} Gm m^{2} s xm + \frac{i a^{2} \gamma k \gamma p e^{2} \zeta (k \cdot X)}{m^{2} \xi} - \frac{i a^{2} e^{2} \zeta (k \cdot X)}{m \xi} + \frac{i a^{2} e^{2} \zeta xm}{2 \xi} - \frac{i \alpha^{2} e^{2} \zeta (k \cdot X)}{m \xi} + \frac{i \alpha^{2} e^{2} \zeta xm}{2 \xi} - \frac{i \alpha^{2} e^{2} \zeta (k \cdot X)}{m \xi} + \frac{i \alpha^{2} e^{2} \zeta xm}{2 \xi} - \frac{i \gamma a \gamma m e \zeta s}{m \xi} + \frac{i \alpha^{2} e^{2} \zeta xm}{2 \xi} - \frac{i \gamma a \gamma m e \zeta s}{m \xi xm} + \frac{i \gamma a \gamma m e \zeta s}{m \xi xm} - \frac{i \gamma a \gamma m e \zeta s}{m \xi xm} - \frac{i \gamma a \gamma m e \zeta s}{m \xi xm} - \frac{i \gamma a \gamma m e \zeta s}{m \xi xm} - \frac{i \gamma a \gamma m e \zeta s}{m \xi xm} - \frac{i \gamma a \gamma m e \zeta s}{m \xi xm} - \frac{i \gamma a \gamma m e \zeta s}{m \xi xm} - \frac{i \gamma a \gamma m e \zeta s}{m \xi xm} - \frac{i \gamma a \gamma m e \zeta s}{m \xi xm} - \frac{i \gamma a \gamma m e \zeta s}{m \xi xm} - \frac{i \gamma a \gamma m e \zeta s}{m \xi xm} - \frac{i \gamma a \gamma m e \zeta s}{m \xi xm} - \frac{i \gamma a \gamma m e \zeta s}{m \xi xm} - \frac{i \gamma a \gamma m e \zeta s}{m \xi xm} - \frac{i \gamma a \gamma m e \zeta s}{m \xi xm} - \frac{i \gamma a \gamma m e \zeta s}{m \xi xm} - \frac{i \gamma a \gamma m e \zeta s}{m \xi xm} - \frac{i \gamma a \gamma m e \zeta s}{m \xi xm} - \frac{i \gamma a \gamma m e \zeta s}{m \xi xm} - \frac{i \gamma a \gamma m e \zeta s}{m \xi xm} - \frac{i \gamma a \gamma m e \zeta s}{m \xi xm} - \frac{i \gamma a \gamma m e \zeta s}{m \xi xm} - \frac{i \gamma a \gamma m e \zeta s}{m \xi xm} - \frac{i \gamma a \gamma m e \zeta s}{m \xi xm} - \frac{i \gamma a \gamma m e \zeta s}{m \xi xm} - \frac{i \gamma a \gamma m e \zeta s}{m \xi xm} - \frac{i \gamma a \gamma m e \zeta s}{m \xi xm} - \frac{i \gamma a \gamma m e \zeta s}{m \xi xm} - \frac{i \gamma a \gamma m e \zeta s}{m \xi xm} - \frac{i \gamma a \gamma m e \zeta s}{m \xi xm} - \frac{i \gamma a \gamma m e \zeta s}{m \xi xm} - \frac{i \gamma a \gamma m e \zeta s}{m \xi xm} - \frac{i \gamma a \gamma m e \zeta s}{m \xi xm} - \frac{i \gamma a \gamma m e \zeta s}{m \xi xm} - \frac{i \gamma a \gamma m e \zeta s}{m \xi xm} - \frac{i \gamma a \gamma m e \zeta s}{m \xi xm} - \frac{i \gamma a \gamma m e \zeta s}{m \xi xm} - \frac{i \gamma a \gamma m e \zeta s}{m \xi xm} - \frac{i \gamma a \gamma m e \zeta s}{m \xi xm} - \frac{i \gamma a \gamma m e \zeta s}{m \xi xm} - \frac{i \gamma a \gamma m e \zeta s}{m \xi xm} - \frac{i \gamma a \gamma m e \zeta s}{m \xi xm} - \frac{i \gamma a \gamma m e \zeta s}{m \xi xm} - \frac{i \gamma a \gamma m e \zeta s}{m \xi xm} - \frac{i \gamma a \gamma m e \zeta s}{m \xi xm} - \frac{i \gamma a \gamma m e \zeta s}{m \xi xm} - \frac{i \gamma a \gamma m e \zeta s}{m \xi xm} - \frac{i \gamma a \gamma m e \zeta s}{m \xi xm} - \frac{i \gamma a \gamma m e \zeta s}{m \xi xm} - \frac{i \gamma a \gamma m e \zeta s}{m \xi xm} - \frac{i \gamma a \gamma m e \zeta s}{m \xi xm} - \frac{i \gamma \alpha m e \zeta s}{m \xi xm} - \frac{i \gamma \alpha m e \zeta s}{m \xi xm} - \frac{i \gamma \alpha m e \zeta s}{m \xi xm} - \frac{i \gamma \alpha m e \zeta s}{m \xi xm} - \frac{i \gamma \alpha m e \zeta s}{m \xi xm} - \frac{i \gamma \alpha m e \zeta s}{m \xi xm} - \frac{i \gamma \alpha m e \zeta s
              \frac{i a^2 \operatorname{af} e^3 \zeta s \sigma F}{2 m \xi^2} - \frac{i a^2 \operatorname{af} e^2 \operatorname{Gm} m s}{\xi} - \frac{a^2 \operatorname{af} e^2 \zeta}{m \xi^2} + \frac{a^2 e^3 \zeta s \sigma F v 2}{m^2 \xi^3 \operatorname{xm}}
              \frac{i\,a^2\,e^2\,\zeta\,\mathrm{Gm}\,m\,s\,\mathrm{sf}}{\zeta}\,+
              \frac{2 a^2 e^2 \operatorname{Gm} \operatorname{s} \operatorname{v2}}{\xi^2 \operatorname{xm}} + \gamma \gamma 5 \operatorname{FDp} \left( \frac{\operatorname{af} e}{m \xi} + \frac{e \zeta \operatorname{sf}}{m \xi} \right) +
              \frac{1}{2}iemssf\sigma F - \frac{2es\sigma Ftf}{\xi xm} + msf
    2 i e \zeta s v1 at(i1) pt(i) pt(i1) 2 i a^2 e^2 \zeta s v1 pt(i) (k \cdot X)
                                                      m^2 \xi \text{ xm}
                                                                                                                                                                                                                   m^2 \xi xm
```

$$\frac{i \, 2^{-D-2} \, \pi^{-D} \, \Lambda^{4-D}}{s \, \mathrm{DdInv}(\zeta)}$$

$$\frac{1}{12} a^2 e^2 s (k \cdot x)^2 + a^2 e^2 s (k \cdot X)^2 + pt (xt - 2 \text{ at } e s (k \cdot X)) - \frac{xp (k \cdot x)}{2 m s} - p^2 s + pt^2 (-s)$$

## **Integration over**

$$\int \!\! d \!\! 1^{D-2} \, p_{\scriptscriptstyle \perp} \, \cdots$$

$$\begin{split} \mathbf{I}_0 &= \int \! d^{D-2} \; p_{_{\perp}} \; \mathsf{Exp} \left[ -\, \mathbf{I} \; A \; p_{_{\perp}}^2 \, + \, \mathbf{I} \; \left( \, \mathbf{J} \, . \, p_{_{\perp}} \right) \; \right] \; = \\ &= \; \mathsf{Exp} \; \left[ -\, \mathbf{I} \; \frac{\pi}{2} \; \frac{D-2}{2} \right] \; \pi^{\frac{D-2}{2}} (\, \mathsf{det} \; A)^{\, -\frac{1}{2}} \; \mathsf{Exp} \; \left[ \; \mathbf{I} \; \frac{1}{4} \; \, \mathsf{J} \, . \, A^{-1} \, . \, \, \mathsf{J} \; \right] \end{split}$$

$$I_{1i} = \int d^{D-2} p_{\perp} p_{\perp i} Exp[-IAp_{\perp}^{2} + I(J.p_{\perp})] =$$

$$= \frac{1}{2} (A^{-1}.J)_{i} I_{0}$$

$$\begin{split} \mathbf{I}_2 &= \int \! d^{D-2} \; p_{_{\perp}} \; p_{_{\perp}}^2 \; \mathsf{Exp} \left[ -\mathbf{I} \; \mathsf{A} \; p_{_{\perp}}^2 + \mathbf{I} \; \left( \mathsf{J.p}_{_{\perp}} \right) \; \right] \; = \\ &= \; \left[ - \, \dot{\mathbb{1}} \; \frac{1}{2} \; \mathsf{Tr} \; \mathsf{A}^{-1} \; + \; \left( \, \frac{1}{2} \; \mathsf{A}^{-1} \; . \; \mathsf{J} \right)^2 \; \right] \end{split}$$

$$I_{2 \, ij} = \int d^{D-2} \, p_{\perp} \, p_{\perp i} \, p_{\perp j} \, Exp \left[ -I \, A \, p_{\perp}^{2} + I \, (J.p_{\perp}) \, \right] =$$

$$= \left[ -i \, \frac{1}{2} \, A^{-1}_{ij} + \left( \frac{1}{2} \, A^{-1}.J \right)_{i} \, \left( \frac{1}{2} \, A^{-1}.J \right)_{j} \right] \, I_{0}$$

$$\begin{split} \mathbf{I}_{3\;i} &= -\,\dot{\mathbf{i}}\;\frac{\partial}{\partial \mathbf{J}_{i}}\,\mathbf{I}_{2} = \int\!\!d^{D-2}\;p_{\perp}\;p_{\perp}^{2}\;p_{\perp i}\;\mathsf{Exp}\left[\,-\,\mathbf{I}\;\mathsf{A}\;p_{\perp}^{2}\,+\,\mathbf{I}\;(\,\mathbf{J}\,.\,p_{\perp}^{})\;\right] \,= \\ &= \,\left\{\,\left[\,-\,\dot{\mathbf{i}}\;\frac{1}{2}\;\mathsf{Tr}\;\mathsf{A}^{-1}\,+\,\left(\,\frac{1}{2}\;\mathsf{A}^{-1}\,.\,\mathsf{J}\,\right)^{\,2}\,\right]\;\frac{1}{2}\;\left(\,\mathsf{A}^{-1}\,.\,\mathsf{J}\,\right)_{\,i}\,-\,\dot{\mathbf{i}}\;\frac{1}{2}\;\left(\,\mathsf{A}^{-1}\,^{\,T}\;\mathsf{A}^{-1}\,.\,\mathsf{J}\,\right)_{\,i}\;\right\}\;\mathbf{I}_{0} \,= \\ &= \,\left(\,\frac{1}{2}\;\mathsf{A}^{-1}\,.\,\mathsf{J}\,\right)_{\,i}\;\mathbf{I}_{2}\,-\,\dot{\mathbf{i}}\;\left(\,\mathsf{A}^{-1}\,^{\,T}\,\right)_{\,i\,\dot{\mathbf{j}}}\;\mathbf{I}_{1\,\dot{\mathbf{j}}} \end{split}$$

where

A = s,  
J = 
$$x_{\perp} - 2 ea_{\perp} s kX$$
,  
det A =  $s^{D-2}$ ,  
A<sup>-1</sup> = 1 / s

We perform integrations

Integrations changes the coefficient (Coeff) and phase

Then recollect some scalar products

$$a_{\perp}^{2} = -a^{2}$$
 $a_{\perp} x_{\perp} = -(ax)$ 
 $x_{\perp}^{2} = 2 x_{\perp} x_{\perp} - x^{2}$ 

```
Clear[J]
Amatr = -Coefficient[Phase5, pt^2]
J[i_] = Coefficient[Phase5, pt] /. \{at \rightarrow at[i], xt \rightarrow xt[i]\}
CIO = Exp[-IPi/2(D/2-1)]Pi^(D/2-1) / Amatr^(D/2-1)
s
xt(i) - 2 e s at(i) (k \cdot X)
e^{-\frac{1}{2}i\pi(\frac{D}{2}-1)}\pi^{\frac{D}{2}-1}s^{1-\frac{D}{2}}
Phase6 = Expand \left[ \left( \left( Phase5 / . \{pt \rightarrow 0\} \right) + 1 / 4 J[i] ^2 / Amatr \right) \right] / .
       {at[i]^2 \rightarrow -av2, at[i] xt[i] \rightarrow -ax, xt[i]^2 \rightarrow 2 xm xp -xv2} /. {xm \rightarrow kx/m}]
Coeff6 = Coeff5 * CIO
Expand[
   Expand[Matrix5] /.
          \{pt[i2_]^2 \neq [i1_] \rightarrow ((-I/2*(D-2)/Amatr+(1/2/Amatr*J[i2])^2)*
                  1/2/Amatr * J[i1] - I * 1/2/Amatr^2 * J[i1]) \} /. {pt[i_] pt[i1_]} \rightarrow
            (-I/2/Amatr \delta[i, i1] + (1/2/Amatr * J[i]) * (1/2/Amatr * J[i1]))} /.
       \{pt[i_{-}]^2 \rightarrow (-I/2*(D-2)/Amatr+(1/2/Amatr*J[i])^2)\}/.
     \{pt[i_] \rightarrow (1/2/Amatr * J[i])\}
% - Coefficient[%, \delta[i, i1]] \delta[i, i1] + (Coefficient[%, \delta[i, i1]] /. {i1 \rightarrow i});
Matrix6 =
  Collect[% /. \{\gamma\gamma 5FDt[i_] at[i_] \rightarrow 0 \} /. \{at[i_]^2 \rightarrow -av2\} /. \{at[i_] xt[i_] \rightarrow -ax\} /.
       \{xt[i]^2 \rightarrow 2xmxp - xv2\} /. \{at[i]axkXxt[i] \rightarrow -axaxkX\},
    {v1, pt[i2] pt[i], pt[i2], pt[i_], pv2, \gamma\gamma5FDm, \gamma\gamma5FDp,
     yy5FDt[i], ykym, ykyp, ykyt[i], yaym, yayp, yayt[i]}]
(*Matrix6=Collect[Expand[Expand[(Matrix5/.{pt[i_]→0})+
          Coefficient[Matrix5,pt]*1/2/Amatr*J+
          Coefficient[Matrix5,pt^2] * (-I/2*(D-2)/Amatr+(1/2/Amatr*J)^2) +
          Coefficient[Matrix5,pt<sup>3</sup>] ((-I/2*(D-2)/Amatr+(1/2/Amatr*J)^2)*1/2/Amatr*J+
               1/2/Amatr^2*J)]/.{\gamma\gamma5FDt at\rightarrow 0, at^4\rightarrow av^2,
        at^3\rightarrow -av2 at, at^2\rightarrow-av2,at xt\rightarrow -ax, xt^2\rightarrow 2xm xp -xv2}],
    \{p2,Gm,Gp,Gt,\gamma\gamma5FDm,\gamma\gamma5FDp,\gamma\gamma5FDt,\gamma k\gamma m,\gamma k\gamma p,\gamma k\gamma t,\gamma a\gamma m,\gamma a\gamma p,\gamma a\gamma t\}\}
\frac{1}{12} a^2 e^2 s (k \cdot x)^2 + e(a \cdot x) (k \cdot X) - p^2 s - \frac{x^2}{4 s}
\frac{i \, 2^{-D-2} \, e^{-\frac{1}{2} i \pi \left(\frac{D}{2}-1\right)} \pi^{-\frac{D}{2}-1} \, \Lambda^{4-D} \, s^{-D/2}}{}
```

$$\begin{split} & \text{v1} \left( \gamma \text{a} \gamma \text{m} \left( \frac{i \, a^2 \, e^3 \, \zeta \, s \, (k \cdot X)^2}{m \, \xi \, \text{xm}} - \frac{i \, e^2 \, \zeta \, (a \cdot x) \, (k \cdot X)}{m \, \xi \, \text{xm}} - \frac{D \, e \, \zeta}{2 \, m \, \xi \, \text{xm}} - \frac{i \, e \, \zeta \, \left( 2 \, \text{xm} \, \text{xp} - x^2 \right)}{4 \, m \, \xi \, \text{xm}} + \frac{e \, \zeta}{m \, \xi \, \text{xm}} \right) + \\ & \frac{a^2 \, e^3 \, \zeta \, s \, \sigma \, F \, (k \cdot X)^2}{2 \, m^2 \, \xi \, \text{xm}} + \gamma k \gamma t (i) \left( \frac{i \, e^2 \, \zeta \, \text{at} (i) \, (a \cdot x) \, (k \cdot X)}{m^2 \, \xi \, \text{xm}} - \frac{i \, e \, \zeta \, x t (i) \, (a \cdot x)}{2 \, m^2 \, \xi \, \text{xm}} + \frac{e \, \zeta \, \text{at} (i)}{m^2 \, \xi \, \text{xm}} \right) - \\ & \frac{a^2 \, e^3 \, \zeta \, s \, \sigma \, F \, \text{xm}}{8 \, \xi} - \frac{1}{4} \, a^2 \, e^2 \, \text{Gm} \, m^2 \, s \, \text{xm} - \frac{i \, a^2 \, e^2 \, \zeta \, (k \cdot X)}{m \, \xi} + \frac{i \, a^2 \, e^2 \, \zeta \, \chi m}{2 \, \xi} - \\ & e \, \gamma \cdot a \, (k \cdot X) + \frac{i \, \gamma k \gamma p \, e \, \zeta \, (a \cdot x)}{2 \, m^2 \, \xi \, s} + \gamma a \gamma t (i) \left( \frac{i \, e \, \zeta \, \text{xt} (i)}{2 \, m \, \xi \, s} - \frac{i \, e^2 \, \zeta \, \text{at} (i) \, (k \cdot X)}{m \, \xi} \right) - \\ & e \, at \, (i) \, \text{Gt} (i) \, (k \cdot X) + \frac{i \, D \, Gm}{2 \, xm} + p^2 \left( -\frac{e \, \zeta \, s \, \sigma \, F}{m^2 \, \xi \, xm} - \frac{i \, \gamma a \gamma m \, e \, \zeta \, s}{m \, \xi \, xm} - \frac{Gm \, s}{xm} \right) - \frac{i \, \gamma a \gamma p \, e \, \zeta \, xm}{2 \, m \, \xi \, s} - \\ & \frac{1}{2} \, i \, \gamma \gamma 5 \, \text{FDp} \, e \, xm - \frac{Gm \, \left( 2 \, xm \, xp - x^2 \right)}{4 \, s \, xm} - \frac{i \, Gm}{xm} - \frac{Gp \, xm}{m \, \xi \, xm} - \frac{Gm \, s}{xm} \right) - \frac{i \, \gamma a \gamma p \, e \, \zeta \, xm}{2 \, m \, \xi \, s} - \\ & \frac{i \, a^2 \, af \, e^3 \, \zeta \, s \, \sigma \, F}{2 \, Gm \, m \, s \, s} + \frac{i \, a^2 \, e^2 \, \zeta \, Gm \, s \, tf}{\xi} + \frac{4 \, a^2 \, e^2 \, \zeta \, Gm \, s \, tf}{\xi^2 \, xm} + \\ & \frac{4 \, a^2 \, e^2 \, \zeta \, Gm \, s \, tf}{\xi^2 \, xm} + \\ & \frac{2 \, a^2 \, e^2 \, Gm \, s \, v2}{\xi^2 \, xm} + \\ & \frac{2 \, a^2 \, e^2 \, Gm \, s \, v2}{\xi^2 \, xm} + \frac{2 \, e \, s \, \sigma \, F \, tf}{\xi^2 \, xm} + m \, sf + \\ & \frac{1}{2} \, i \, e \, m \, s \, s \, f \, \sigma \, F - \frac{2 \, e \, s \, \sigma \, F \, tf}{\xi \, xm} + m \, sf + \\ & \frac{1}{2} \, i \, e \, m \, s \, s \, f \, \sigma \, F - \frac{2 \, e \, s \, \sigma \, F \, tf}{\xi \, xm} + m \, sf + \\ & \frac{1}{2} \, i \, e \, m \, s \, s \, \sigma \, F - \frac{1}{2} \, e \, s \, \sigma \, F \, tf + \frac{1}{2} \, e \, s \, \sigma \, F \, tf + \frac{1}{2} \, e \, s \, \sigma \, F \, tf + \frac{1}{2} \, e \, s \, \sigma \, F \, tf + \frac{1}{2} \, e \, s \, \sigma \, F \, tf + \frac{1}{2} \, e \, s \, \sigma \, F \, tf + \frac{1}{2} \,$$

#### Next we substitute

$$\gamma_{\perp} a_{\perp} = -\gamma a$$

$$\gamma_{\perp} x_{\perp} = \gamma_{-} x_{+} + \gamma_{+} x_{-} - \gamma x$$

$$\gamma_{-} x_{-} = \frac{\gamma k}{m} x_{-}$$

$$x_{-} = kx / m$$

```
Matrix7 = Collect[
                     DiracSimplify[
                                  Expand[Matrix6] /. \{Gt[i_] at[i_] \rightarrow -Contract[GAD[\alpha] av[\alpha]],
                                                                                                    Gt[i] xt[i] \rightarrow Gm xp + Gp xm - Contract[GAD[\alpha] xv[\alpha]],
                                                                                                      (*γγ5FDt[i ] xt[i ] →γγ5FDp xm - DiracSlash[FDx,Dimension→D].GA[5],*)
                                                                                                   \gamma \gamma 5 FDp \rightarrow DiracSlash[FDx, Dimension \rightarrow D].GA[5] / xm,
                                                                                                   \gamma k \gamma t[i] \times t[i] \rightarrow -Pair[Momentum[x, D], Momentum[\gamma k \gamma, D]] + \gamma k \gamma p * x m,
                                                                                                   γkγt[i_] at[i_] → -Pair[Momentum[a, D], Momentum[γkγ, D]],
                                                                                                 \gamma a \gamma t[i_] x t[i_] \rightarrow - Pair[Momentum[x, D], Momentum[\gamma a \gamma, D]] + \gamma a \gamma p * xm + pair[Momentum[x, D], Momentum[y a \gamma, D]] + \gamma a \gamma p * xm + pair[Momentum[x, D], Momentum[y a \gamma, D]] + \gamma a \gamma p * xm + pair[Momentum[x, D], Momentum[y a \gamma, D]] + \gamma a \gamma p * xm + pair[Momentum[x, D], Momentum[y a \gamma, D]] + \gamma a \gamma p * xm + pair[Momentum[x, D], Momentum[y a \gamma, D]] + \gamma a \gamma p * xm + pair[Momentum[x, D], Momentum[y a \gamma, D]] + \gamma a \gamma p * xm + pair[Momentum[x, D], Momentum[y a \gamma, D]] + \gamma a \gamma p * xm + pair[Momentum[x, D], Momentum[x, D], Momentum[x, D]] + \gamma a \gamma p * xm + pair[Momentum[x, D], Momentum[x, D]] + \gamma a \gamma p * xm + pair[Momentum[x, D], Momentum[x, D]] + \gamma a \gamma p * xm + pair[Momentum[x, D], Momentum[x, D]] + \gamma a \gamma p * xm + pair[Momentum[x, D], Momentum[x, D]] + \gamma a \gamma p * xm + pair[Momentum[x, D], Momentum[x, D]] + \gamma a \gamma p * xm + pair[Momentum[x, D], Momentum[x, D]] + \gamma a \gamma p * xm + pair[Momentum[x, D], Momentum[x, D]] + \gamma a \gamma p * xm + pair[Momentum[x, D], Momentum[x, D]] + \gamma a \gamma p * xm + pair[Momentum[x, D], Momentum[x, D]] + \gamma a \gamma p * xm + pair[Momentum[x, D], Momentum[x, D]] + \gamma a \gamma p * xm + pair[Momentum[x, D], Momentum[x, D]] + \gamma a \gamma p * xm + pair[Momentum[x, D], Momentum[x, D]] + \gamma a \gamma p * xm + pair[Momentum[x, D], Momentum[x, D]] + \gamma a \gamma p * xm + pair[Momentum[x, D], Momentum[x, D]] + \gamma a \gamma p * xm + pair[Momentum[x, D], Momentum[x, D]] + \gamma a \gamma p * xm + pair[Momentum[x, D], Momentum[x, D]] + \gamma a \gamma p * xm + pair[Momentum[x, D], Momentum[x, D]] + \gamma a \gamma p * xm + pair[Momentum[x, D], Momentum[x, D]] + \gamma a \gamma p * xm + pair[Momentum[x, D], Momentum[x, D]] + \gamma a \gamma p * xm + pair[Momentum[x, D], Momentum[x, D]] + \gamma a \gamma p * xm + pair[Momentum[x, D], Momentum[x, D]] + \gamma a \gamma p * xm + pair[Momentum[x, D], Momentum[x, D]] + \gamma a \gamma p * xm + pair[Momentum[x, D], Momentum[x, D], Momen
                                                                                                                         \gamma a \gamma m * x p, \gamma a \gamma t [i_] a t [i_] \rightarrow - Pair[Momentum[a, D], Momentum[<math>\gamma a \gamma, D]]} /.
                                                                                \{Gm \rightarrow DiracGamma[Momentum[k, D], D]/m\}/. \{\gamma k \gamma m \rightarrow 0\}/.
                                                         {\gam → DiracGamma[Momentum[a, D], D].DiracGamma[Momentum[k, D], D]/m}
                                            /. \{xm \rightarrow kx/m\}
                     ],
                        \{v1, p2, Gm, Gp, Gt, \gamma\gamma 5FDm, \gamma\gamma 5FDp, \gamma\gamma 5FDt, \gamma k\gamma m, \gamma k\gamma p, \gamma k\gamma t, \gamma a\gamma m, \gamma a\gamma p, \gamma a\gamma t\}
Coeff7 = Coeff6
 Phase7 = Phase6
         -\frac{i\operatorname{af} s\,\zeta\,\sigma\operatorname{F}\,a^{2}\,e^{3}}{2\,m\,\xi^{2}}+\frac{s\,v2\,\zeta\,\sigma\operatorname{F}\,a^{2}\,e^{3}}{m\,\xi^{3}\,(k\cdot x)}-\frac{i\operatorname{af} s\,\gamma\cdot k\,a^{2}\,e^{2}}{\xi}-\frac{i\,s\operatorname{sf}\,\zeta\,\gamma\cdot k\,a^{2}\,e^{2}}{\xi}-\frac{\operatorname{af}\,\zeta\,a^{2}\,e^{2}}{m\,\xi^{2}}+\frac{2\,s\,v2\,\gamma\cdot k\,a^{2}\,e^{2}}{\xi^{2}\,(k\cdot x)}+\frac{2\,s\,v2\,\gamma\cdot k
            \frac{4 \operatorname{stf} \zeta \gamma \cdot k \, a^2 \, e^2}{\xi^2 \, (k \cdot x)} + \frac{1}{2} i \, m \, s \, \text{sf} \, \sigma \\ F \, e - \frac{2 \, m \, s \, \text{tf} \, \sigma \\ F \, e}{\xi \, (k \cdot x)} + \frac{\operatorname{af} \, (\gamma \cdot FDx) \cdot \overline{\gamma}^5 \, e}{\xi \, (k \cdot x)} + \frac{\operatorname{sf} \, \zeta \, (\gamma \cdot FDx) \cdot \overline{\gamma}^5 \, e}{\xi \, (k \cdot x)} + m \, \text{sf} + v \cdot \left( \frac{s \, \zeta \, \sigma \\ F \, a^2 \, (k \cdot X)^2 \, e^3}{2 \, m \, \xi \, (k \cdot X)} + \frac{i \, s \, \zeta \, (\gamma \cdot a) \cdot (\gamma \cdot k) \, a^2 \, (k \cdot X)^2 \, e^3}{m \, \xi \, (k \cdot X)} - \frac{s \, \zeta \, \sigma \\ F \, a^2 \, (k \cdot x) \, e^3}{8 \, m \, \xi} - \frac{1}{4} \, s \, \gamma \cdot k \, a^2 \, (k \cdot x) \, e^2 + v \cdot \left( \frac{s \, \zeta \, \sigma \\ F \, a^2 \, (k \cdot x) \, e^3}{2 \, m \, \xi \, (k \cdot x)} + \frac{s \, \zeta \, (\gamma \cdot a) \cdot (\gamma \cdot k) \, a^2 \, (k \cdot x)^2 \, e^3}{2 \, m \, \xi \, (k \cdot x)} - \frac{s \, \zeta \, \sigma \\ F \, a^2 \, (k \cdot x) \, e^3}{2 \, m \, \xi \, (k \cdot x)} + \frac{s \, \zeta \, (\gamma \cdot a) \cdot (\gamma \cdot k) \, a^2 \, (k \cdot x)^2 \, e^3}{2 \, m \, \xi \, (k \cdot x)} - \frac{s \, \zeta \, \sigma \\ F \, a^2 \, (k \cdot x) \, e^3}{2 \, m \, \xi \, (k \cdot x)} + \frac{s \, \zeta \, (\gamma \cdot a) \cdot (\gamma \cdot k) \, a^2 \, (k \cdot x)^2 \, e^3}{2 \, m \, \xi \, (k \cdot x)} - \frac{s \, \zeta \, \sigma \\ F \, a^2 \, (k \cdot x) \, e^3}{2 \, m \, \xi \, (k \cdot x)} + \frac{s \, \zeta \, (\gamma \cdot a) \cdot (\gamma \cdot k) \, a^2 \, (k \cdot x)^2 \, e^3}{2 \, m \, \xi \, (k \cdot x)} - \frac{s \, \zeta \, \sigma \\ F \, a^2 \, (k \cdot x) \, e^3}{2 \, m \, \xi \, (k \cdot x)} + \frac{s \, \zeta \, (\gamma \cdot a) \cdot (\gamma \cdot k) \, a^2 \, (k \cdot x)^2 \, e^3}{2 \, m \, \xi \, (k \cdot x)} - \frac{s \, \zeta \, \sigma \\ F \, a^2 \, (k \cdot x) \, e^3}{2 \, m \, \xi \, (k \cdot x)} + \frac{s \, \zeta \, (\gamma \cdot a) \cdot (\gamma \cdot k) \, a^2 \, (k \cdot x)^2 \, e^3}{2 \, m \, \xi \, (k \cdot x)^2 \, e^3} - \frac{s \, \zeta \, \sigma \, F \, a^2 \, (k \cdot x) \, e^3}{2 \, m \, \xi \, (k \cdot x)^2 \, e^3} - \frac{s \, \zeta \, \sigma \, F \, a^2 \, (k \cdot x) \, e^3}{2 \, m \, \xi \, (k \cdot x)^2 \, e^3} - \frac{s \, \zeta \, \sigma \, F \, a^2 \, (k \cdot x) \, e^3}{2 \, m \, \xi \, (k \cdot x)^2 \, e^3} - \frac{s \, \zeta \, \sigma \, F \, a^2 \, (k \cdot x) \, e^3}{2 \, m \, \xi \, (k \cdot x)^2 \, e^3} - \frac{s \, \zeta \, \sigma \, F \, a^2 \, (k \cdot x) \, e^3}{2 \, m \, \xi \, (k \cdot x)^2 \, e^3} - \frac{s \, \zeta \, \sigma \, F \, a^2 \, (k \cdot x) \, e^3}{2 \, m \, \xi \, (k \cdot x)^2 \, e^3} - \frac{s \, \zeta \, \sigma \, F \, a^2 \, (k \cdot x) \, e^3}{2 \, m \, \xi \, (k \cdot x)^2 \, e^3} - \frac{s \, \zeta \, \sigma \, F \, a^2 \, (k \cdot x) \, e^3}{2 \, m \, \xi \, (k \cdot x)^2 \, e^3} - \frac{s \, \zeta \, (k \cdot x) \, e^3}{2 \, m \, \xi \, (k \cdot x)^2 \, e^3} - \frac{s \, \zeta \, (k \cdot x) \, e^3}{2 \, m \, \xi \, (k \cdot x)^2 \, e^3} - \frac{s \, \zeta \, (k \cdot x) \, e^3}{2 \, m \, \xi 
                                                                  \frac{i\,\zeta\,a^{2}\left(k\cdot x\right)\,e^{2}}{2\,m\,\xi}-\frac{i\,\zeta\,a^{2}\left(k\cdot X\right)\,e^{2}}{m\,\xi}+\frac{i\,\zeta\left(a\cdot\gamma a\gamma\right)\left(k\cdot X\right)\,e^{2}}{m\,\xi}-\frac{i\,\zeta\left(\gamma\cdot a\right).\left(\gamma\cdot k\right)\left(a\cdot x\right)\left(k\cdot X\right)\,e^{2}}{m\,\xi\left(k\cdot x\right)}
                                                                    \frac{i\,\zeta\left(a\cdot x\right)\left(a\cdot\gamma k\gamma\right)\left(k\cdot X\right)\,e^{2}}{m\,\varepsilon\left(k\cdot x\right)}-\frac{1}{2}\,i\,(\gamma\cdot\mathrm{FDx}).\overline{\gamma}^{5}\,e-\frac{s\,\zeta\,\sigma\mathrm{F}\,p^{2}\,e}{m\,\varepsilon\left(k\cdot x\right)}-\frac{i\,s\,\zeta\left(\gamma\cdot a\right).(\gamma\cdot k)\,p^{2}\,e}{m\,\varepsilon\left(k\cdot x\right)}+
                                                                 \frac{i\,\zeta\,(\gamma\cdot a).(\gamma\cdot k)\,x^2\,e}{4\,m\,s\,\xi\,(k\cdot x)} - \frac{i\,\zeta\,(x\cdot\gamma a\gamma)\,e}{2\,m\,s\,\xi} + \frac{i\,\zeta\,(a\cdot x)\,(x\cdot\gamma k\gamma)\,e}{2\,m\,s\,\xi\,(k\cdot x)} - \frac{D\,\zeta\,(\gamma\cdot a).(\gamma\cdot k)\,e}{2\,m\,\xi\,(k\cdot x)} + \frac{\zeta\,(\gamma\cdot a).(\gamma\cdot k)\,e}{m\,\xi\,(k\cdot x)} - \frac{\gamma\cdot x}{2\,s} - \frac{s\,\gamma\cdot k\,p^2}{k\cdot x} + \frac{\gamma\cdot k\,x^2}{4\,s\,(k\cdot x)} + \frac{i\,D\,\gamma\cdot k}{2\,(k\cdot x)} - \frac{i\,\gamma\cdot k}{k\cdot x}\right)
 i \, 2^{-D-2} \, e^{-\frac{1}{2} i \, \pi \left(\frac{D}{2}-1\right)} \pi^{-\frac{D}{2}-1} \, \Lambda^{4-D} \, s^{-D/2}
\frac{1}{12}a^2e^2s(k\cdot x)^2 + e(a\cdot x)(k\cdot X) - p^2s - \frac{x^2}{4s}
```

```
Matrix8 = Collect[
      Expand [
         DiracSimplify[
                     Matrix7 /.
                        \{Pair[Momentum[x, D], Momentum[\gamma k \gamma, D]] \rightarrow
                              DiracGamma[Momentum[k, D], D].DiracGamma[Momentum[x, D], D],
                          Pair [Momentum [a, D], Momentum [\gamma k \gamma, D]] \rightarrow
                             DiracGamma[Momentum[k, D], D].DiracGamma[Momentum[a, D], D],
                           Pair [Momentum [x, D], Momentum [\gamma a \gamma, D]] \rightarrow
                             DiracGamma[Momentum[a, D], D].DiracGamma[Momentum[x, D], D],
                           Pair [Momentum[a, D], Momentum[γaγ, D]] →
                             DiracGamma[Momentum[a, D], D].DiracGamma[Momentum[a, D], D]}
                  ] /. FieldSubstitutions /. akToF /. \{av2 \rightarrow -\xi^2 m^2 / e^2\}
       {sf, v1, v2, tf, af, ζ, σF}]
 Coeff8 = Coeff7
 Phase8 = Phase7 /. \{av2 \rightarrow -\xi^2 m^2 / e^4 \}
v1\left(-\frac{1}{2}ie(\gamma \cdot FDx).\overline{\gamma}^{5} + \zeta\left(\frac{ie(a \cdot x)(\gamma \cdot k).(\gamma \cdot x)}{2m\xi s(k \cdot x)} - \frac{ie(\gamma \cdot a).(\gamma \cdot x)}{2m\xi s} + \sigma F\right)\right)
                                  \left(-\frac{i\,D\,e}{4\,m\,\xi\,(k\cdot x)} - \frac{e\,p^2\,s}{2\,m\,\xi\,(k\cdot x)} + \frac{1}{8}\,e\,m\,\xi\,s\,(k\cdot x) - \frac{e\,x^2}{8\,m\,\xi\,s\,(k\cdot x)} + \frac{i\,e}{m\,\xi\,(k\cdot x)}\right) - \frac{1}{2}\,i\,m\,\xi\,(k\cdot x)\right) + \frac{1}{2}\,m\,\xi\,(k\cdot x)
                  \frac{i D \gamma \cdot k}{2 (k \cdot x)} + \frac{1}{4} m^2 \xi^2 s \gamma \cdot k (k \cdot x) - \frac{p^2 s \gamma \cdot k}{k \cdot x} + \frac{x^2 \gamma \cdot k}{4 s (k \cdot x)} - \frac{i \gamma \cdot k}{k \cdot x} - \frac{\gamma \cdot x}{2 s} + \frac{y \cdot x}{2 s}
    \operatorname{af}\left(\frac{e\left(\gamma\cdot\operatorname{FDx}\right).\overline{\gamma}^{\flat}}{\mathcal{E}\left(k\cdot x\right)} + \zeta\left(m + \frac{1}{2}i\,e\,m\,s\,\sigma\operatorname{F}\right) + i\,m^{2}\,\xi\,s\,\gamma\cdot k\right) +
    \operatorname{sf}\left(\zeta\left(\frac{e\left(\gamma\cdot\operatorname{FDx}\right).\overline{\gamma}^{5}}{\xi\left(k\cdot x\right)}+i\ m^{2}\xi\,s\,\gamma\cdot k\right)+\frac{1}{2}\,i\ e\ m\ s\ \sigma\operatorname{F}+m\right)+
   \operatorname{tf}\left(-\frac{2\,e\,m\,s\,\sigma F}{\xi\,(k\cdot x)}-\frac{4\,\zeta\,m^2\,s\,\gamma\cdot k}{k\cdot x}\right)+
    v2\left(-\frac{e\zeta m s \sigma F}{\xi (k \cdot x)} - \frac{2 m^2 s \gamma \cdot k}{k \cdot x}\right)
 i \, 2^{-D-2} \, e^{-\frac{1}{2} i \, \pi \left(\frac{D}{2}-1\right)} \pi^{-\frac{D}{2}-1} \, \Lambda^{4-D} \, s^{-D/2}
-\frac{1}{12}m^2\xi^2 s(k \cdot x)^2 + e(a \cdot x)(k \cdot X) - p^2 s - \frac{x^2}{4a^2}
 (*a small test*) Expand [ ((Matrix8 /. {sf \rightarrow 1, v1 \rightarrow -1, v2 \rightarrow 0, tf \rightarrow 0, af \rightarrow 0, \mathcal{E} \rightarrow 1}) +
             (Matrix8 /. {sf \rightarrow 1, v1 \rightarrow -1, v2 \rightarrow 0, tf \rightarrow 0, af \rightarrow 0, \zeta \rightarrow -1}))/2
\frac{1}{2} i e(\gamma \cdot \text{FDx}) \cdot \overline{\gamma}^5 - \frac{i D \gamma \cdot k}{2(k \cdot x)} + \frac{1}{2} i e m s \sigma F - \frac{1}{4} m^2 \xi^2 s \gamma \cdot k(k \cdot x) + \frac{p^2 s \gamma \cdot k}{k \cdot x} - \frac{x^2 \gamma \cdot k}{4 s(k \cdot x)} + \frac{i \gamma \cdot k}{k \cdot x} + m + \frac{\gamma \cdot x}{2 s}
```

```
DiracSimplify[
    DiracGamma[Momentum[Fx, D], D].DiracGamma[Momentum[x, D], D] /. FxToak]
 DiracSimplify[
    I DiracGamma[Momentum[FDx, D], D].DiracGamma[5].DiracGamma[Momentum[x, D], D] /.
             FxToEps /. FxToak /. Gamma5toTrippleGammax]
(a \cdot x) (\gamma \cdot k) \cdot (\gamma \cdot x) - (k \cdot x) (\gamma \cdot a) \cdot (\gamma \cdot x)
(a \cdot x) (\gamma \cdot k) \cdot (\gamma \cdot x) - (k \cdot x) (\gamma \cdot a) \cdot (\gamma \cdot x) + x^2 (\gamma \cdot a) \cdot (\gamma \cdot k)
 Matrix9 = Collect[
       Expand [
          Matrix8 /. {ax DiracGamma[Momentum[k, D], D].DiracGamma[Momentum[x, D], D] →
                      I DiracGamma[Momentum[FDx, D], D].DiracGamma[5].DiracGamma[Momentum[x, D],
                                   D] + kx DiracGamma[Momentum[a, D], D].DiracGamma[Momentum[x, D], D] -
                          ( xv2 DiracGamma[Momentum[a, D], D].DiracGamma[Momentum[k, D], D] /. akToF),
                    DiracGamma[Momentum[k, D], D] \rightarrow - DiracGamma[Momentum[FFx, D], D] / av2 / kx\} /.
             \{av2 \rightarrow -\xi^2 m^2/e^2\}
       1,
       {sf, v1, v2, tf, af, \xi, e \sigmaF/m/\xi/kx, \sigmaF,
          e^2 DiracGamma [Momentum[FFx, D], D] / m^2/\xi^2/kx^2]
 Coeff9 = Coeff8
 Phase9 = Phase8
\operatorname{v1}\left[\zeta\left(-\frac{e\left(\gamma\cdot\operatorname{FDx}\right).\overline{\gamma}^{5}.\left(\gamma\cdot x\right)}{2\ m\xi\ s\left(k\cdot x\right)} + \frac{e\ \sigma\operatorname{F}\left(-\frac{i\ D}{4} - \frac{p\ s}{2} + \frac{x}{8\ s} + i\right)}{m\xi\left(k\cdot x\right)} + \frac{1}{8}\ e\ m\xi\ s\ \sigma\operatorname{F}\left(k\cdot x\right) - \frac{1}{2}\ i\ m\xi\left(k\cdot x\right)\right] - \frac{1}{2}\ m\xi\left(k\cdot x\right)\right] - \frac{1}{2}\ m\xi\left(k\cdot x\right)
                  \frac{1}{2}i e(\gamma \cdot \text{FDx}).\overline{\gamma}^5 + \frac{e^2 \gamma \cdot \text{FFx}\left(\frac{i D}{2} - p^2 s + \frac{x^2}{4 s} - i\right)}{m^2 \xi^2 (k \cdot x)^2} + \frac{1}{4}e^2 s \gamma \cdot \text{FFx} - \frac{\gamma \cdot x}{2 s} + \frac{1}{4}e^2 s \gamma \cdot \text{FFx} - \frac{\gamma \cdot x}{2 s}
    \operatorname{af}\left(\frac{e\left(\gamma\cdot\operatorname{FDx}\right).\overline{\gamma}^{5}}{\varepsilon\left(k\cdot x\right)}+\frac{i\,e^{2}\,s\,\gamma\cdot\operatorname{FFx}}{\varepsilon\left(k\cdot x\right)}+\zeta\left(m+\frac{1}{2}\,i\,e\,m\,s\,\sigma\operatorname{F}\right)\right)+
    \operatorname{sf}\left(\zeta\left(\frac{e\left(\gamma\cdot\operatorname{FDx}\right).\overline{\gamma}^{b}}{\xi\left(k\cdot x\right)} + \frac{i\,e^{2}\,s\,\gamma\cdot\operatorname{FFx}}{\xi\left(k\cdot x\right)}\right) + \frac{1}{2}\,i\,e\,m\,s\,\sigma\operatorname{F} + m\right) +
     \mathrm{tf}\left(-\frac{4\,e^{2}\,\zeta\,s\,\gamma\cdot\mathrm{FFx}}{\xi^{2}\,(\,k\cdot x\,)^{2}}-\frac{2\,e\,m\,s\,\sigma\mathrm{F}}{\xi\,(k\cdot x)}\right)+\,\mathrm{v2}\left(-\frac{2\,e^{2}\,s\,\gamma\cdot\mathrm{FFx}}{\xi^{2}\,(\,k\cdot x\,)^{2}}-\frac{e\,\zeta\,m\,s\,\sigma\mathrm{F}}{\xi\,(k\cdot x)}\right)
 \frac{i \, 2^{-D-2} \, e^{-\frac{1}{2} i \pi \left(\frac{D}{2}-1\right)} \pi^{-\frac{D}{2}-1} \, \Lambda^{4-D} \, s^{-D/2}}{2^{-D-2} \, e^{-\frac{1}{2} i \pi \left(\frac{D}{2}-1\right)} \pi^{-\frac{D}{2}-1} \, \Lambda^{4-D} \, s^{-D/2}}
-\frac{1}{12}m^2\xi^2 s(k \cdot x)^2 + e(a \cdot x)(k \cdot X) - p^2 s - \frac{x^2}{4s}
```

 $Collect[Expand[Simplify[D[Coeff8 s f[\chi[s]] Exp[I Phase8], s]/Exp[I Phase8]/Coeff8]],$ f[x[s]]

pv2Sol = pv2 /. Solve[% == dfds, pv2][[1]]

$$s \, \chi'(s) \, f'(\chi(s)) + f(\chi(s)) \left( -\frac{1}{12} \, i \, m^2 \, \xi^2 \, s \, (k \cdot x)^2 - \frac{D}{2} - i \, p^2 \, s + \frac{i \, x^2}{4 \, s} + 1 \right)$$

$$\frac{1}{12 \, s^2 f(\chi(s))} \left( -m^2 \, \xi^2 \, s^2 f(\chi(s)) \, (\, k \cdot x \,)^2 + 6 \, i \left( D \, s \, f(\chi(s)) + 2 \, \text{dfds} \, s - 2 \, s^2 \, \chi'(s) \, f'(\chi(s)) - 2 \, s \, f(\chi(s)) \right) + 3 \, x^2 \, f(\chi(s)) \right)$$

Let

$$f\left(\zeta, p^2, \chi(s)\right) = v_1\left(p^2, \chi(s)\right) D_{\zeta}^{-1}\left(p^2, \chi(s)\right)$$

```
Matrix9pv2 =
         Coefficient[Matrix9, pv2] /. \{v1 \rightarrow f[\xi, pv2, \chi[s]]\} /. \{\chi[s] \rightarrow \xi kx/2/m^2/s\}
  CoeffNoD = Coeff9 * DdInv[g]
   PhaseNopv2 = Phase9 - Coefficient[Phase9, pv2] pv2
   Collect[
         Expand[
                Simplify [
                        -ID[Matrix9pv2 * CoeffNoD * Exp[I PhaseNopv2], s] / (CoeffNoD * Exp[I PhaseNopv2])
        ],
          \{f[g, pv2, \xi kx/2/m^2/s]\}\]
   Matrix91 = Coefficient[%, f[\xi, pv2, \xi kx/2/m<sup>2</sup>/s]] v1
 Matrix92 = % - Matrix91 / v1 * f[g, pv2, g kx / 2 / m^2 / s]
  -\frac{e^2\,s\,\gamma\cdot\operatorname{FFx}\,f\big(\zeta,\,\,p^2,\,\,\frac{\xi(k\cdot x)}{2\,m^2\,s}\big)}{m^2\,\xi^2\,(\,\,k\cdot x\,)^2}-\frac{e\,\zeta\,s\,\sigma\operatorname{F}\,f\big(\zeta,\,\,p^2,\,\,\frac{\xi(k\cdot x)}{2\,m^2\,s}\big)}{2\,m\,\xi\,(k\cdot x)}
 i 2^{-D-2} e^{-\frac{1}{2}i\pi(\frac{D}{2}-1)} \pi^{-\frac{D}{2}-1} \Lambda^{4-D} s^{-D/2}
-\frac{1}{12}m^2\xi^2 s(k\cdot x)^2 + e(a\cdot x)(k\cdot X) - \frac{x^2}{4s}
f\left(\zeta, p^2, \frac{\xi(k \cdot x)}{2 m^2 s}\right) \left(-\frac{i D e^2 \gamma \cdot FFx}{2 m^2 \xi^2 (k \cdot x)^2} - \frac{e^2 x^2 \gamma \cdot FFx}{4 m^2 \xi^2 s (k \cdot x)^2} + \frac{i e^2 \gamma \cdot FFx}{m^2 \xi^2 (k \cdot x)^2} - \frac{e^2 x^2 \gamma \cdot FFx}{4 m^2 \xi^2 s (k \cdot x)^2} + \frac{i e^2 \gamma \cdot FFx}{m^2 \xi^2 (k \cdot x)^2} - \frac{e^2 x^2 \gamma \cdot FFx}{4 m^2 \xi^2 s (k \cdot x)^2} + \frac{i e^2 \gamma \cdot FFx}{m^2 \xi^2 (k \cdot x)^2} - \frac{e^2 x^2 \gamma \cdot FFx}{4 m^2 \xi^2 s (k \cdot x)^2} + \frac{i e^2 \gamma \cdot FFx}{m^2 \xi^2 (k \cdot x)^2} - \frac{e^2 x^2 \gamma \cdot FFx}{4 m^2 \xi^2 s (k \cdot x)^2} + \frac{i e^2 \gamma \cdot FFx}{m^2 \xi^2 (k \cdot x)^2} - \frac{e^2 x^2 \gamma \cdot FFx}{4 m^2 \xi^2 s (k \cdot x)^2} + \frac{i e^2 \gamma \cdot FFx}{m^2 \xi^2 (k \cdot x)^2} - \frac{e^2 x^2 \gamma \cdot FFx}{4 m^2 \xi^2 s (k \cdot x)^2} + \frac{i e^2 \gamma \cdot FFx}{m^2 \xi^2 (k \cdot x)^2} - \frac{e^2 x^2 \gamma \cdot FFx}{4 m^2 \xi^2 s (k \cdot x)^2} + \frac{i e^2 \gamma \cdot FFx}{m^2 \xi^2 (k \cdot x)^2} - \frac{e^2 x^2 \gamma \cdot FFx}{4 m^2 \xi^2 s (k \cdot x)^2} + \frac{i e^2 \gamma \cdot FFx}{m^2 \xi^2 (k \cdot x)^2} - \frac{e^2 x^2 \gamma \cdot FFx}{4 m^2 \xi^2 s (k \cdot x)^2} + \frac{i e^2 \gamma \cdot FFx}{m^2 \xi^2 (k \cdot x)^2} - \frac{e^2 x^2 \gamma \cdot FFx}{4 m^2 \xi^2 s (k \cdot x)^2} + \frac{i e^2 \gamma \cdot FFx}{m^2 \xi^2 (k \cdot x)^2} - \frac{e^2 x^2 \gamma \cdot FFx}{4 m^2 \xi^2 s (k \cdot x)^2} + \frac{i e^2 \gamma \cdot FFx}{m^2 \xi^2 (k \cdot x)^2} - \frac{e^2 x^2 \gamma \cdot FFx}{4 m^2 \xi^2 s (k \cdot x)^2} + \frac{i e^2 \gamma \cdot FFx}{m^2 \xi^2 (k \cdot x)^2} - \frac{e^2 x^2 \gamma \cdot FFx}{4 m^2 \xi^2 s (k \cdot x)^2} + \frac{i e^2 \gamma \cdot FFx}{m^2 \xi^2 (k \cdot x)^2} - \frac{e^2 x^2 \gamma \cdot FFx}{4 m^2 \xi^2 s (k \cdot x)^2} + \frac{i e^2 \gamma \cdot FFx}{m^2 \xi^2 (k \cdot x)^2} - \frac{e^2 x^2 \gamma \cdot FFx}{4 m^2 \xi^2 s (k \cdot x)^2} + \frac{i e^2 \gamma \cdot FFx}{m^2 \xi^2 (k \cdot x)^2} - \frac{e^2 x^2 \gamma \cdot FFx}{4 m^2 \xi^2 s (k \cdot x)^2} + \frac{i e^2 \gamma \cdot FFx}{m^2 \xi^2 s (k \cdot x)^2} - \frac{e^2 x^2 \gamma \cdot FFx}{4 m^2 \xi^2 s (k \cdot x)^2} + \frac{i e^2 \gamma \cdot FFx}{m^2 \xi^2 s (k \cdot x)^2} - \frac{e^2 x^2 \gamma \cdot FFx}{m^2 \xi^2 s (k \cdot x)^2} + \frac{i e^2 \gamma \cdot FFx}{m^2 \xi^2 s (k \cdot x)^2} + \frac{i e^2 \gamma \cdot FFx}{m^2 \xi^2 s (k \cdot x)^2} + \frac{i e^2 \gamma \cdot FFx}{m^2 \xi^2 s (k \cdot x)^2} + \frac{i e^2 \gamma \cdot FFx}{m^2 \xi^2 s (k \cdot x)^2} + \frac{i e^2 \gamma \cdot FFx}{m^2 \xi^2 s (k \cdot x)^2} + \frac{i e^2 \gamma \cdot FFx}{m^2 \xi^2 s (k \cdot x)^2} + \frac{i e^2 \gamma \cdot FFx}{m^2 \xi^2 s (k \cdot x)^2} + \frac{i e^2 \gamma \cdot FFx}{m^2 \xi^2 s (k \cdot x)^2} + \frac{i e^2 \gamma \cdot FFx}{m^2 \xi^2 s (k \cdot x)^2} + \frac{i e^2 \gamma \cdot FFx}{m^2 \xi^2 s (k \cdot x)^2} + \frac{i e^2 \gamma \cdot FFx}{m^2 \xi^2 s (k \cdot x)^2} + \frac{i
                                              \frac{i D e \zeta \sigma F}{4 m \xi (k \cdot x)} + \frac{1}{12} e^2 s \gamma \cdot FFx + \frac{1}{24} e \zeta m \xi s \sigma F(k \cdot x) - \frac{e \zeta \sigma F x^2}{8 m \xi s (k \cdot x)} + \frac{i e \zeta \sigma F}{2 m \xi (k \cdot x)} - \frac{e \zeta \sigma F}{2 m \xi (k \cdot x)}
             \frac{i \, e^2 \, \gamma \cdot \text{FFx} \, f^{(0,0,1)} \left(\zeta, \, p^2, \, \frac{\xi(k \cdot x)}{2 \, m^2 \, s}\right)}{2 \, m^2 \, s} - \frac{i \, e \, \zeta \, \sigma \text{F} \, f^{(0,0,1)} \left(\zeta, \, p^2, \, \frac{\xi(k \cdot x)}{2 \, m^2 \, s}\right)}{2 \, m^2 \, s}
v1 \left( -\frac{i\,D\,e^2\,\gamma \cdot FFx}{2\,m^2\,\xi^2\,(\,k \cdot x\,)^2} - \frac{e^2\,x^2\,\gamma \cdot FFx}{4\,m^2\,\xi^2\,s\,(\,k \cdot x\,)^2} + \frac{i\,e^2\,\gamma \cdot FFx}{m^2\,\xi^2\,(\,k \cdot x\,)^2} - \right.
                                    \frac{i D e \zeta \sigma F}{4 m \mathcal{E}(k \cdot x)} + \frac{1}{12} e^2 s \gamma \cdot FFx + \frac{1}{24} e \zeta m \mathcal{E} s \sigma F(k \cdot x) - \frac{e \zeta \sigma F x^2}{8 m \mathcal{E} s(k \cdot x)} + \frac{i e \zeta \sigma F}{2 m \mathcal{E}(k \cdot x)}
      -\frac{i\,e^2\,\gamma\cdot {\rm FFx}\,f^{(0,0,1)}\big(\zeta,\,\,p^2,\,\,\frac{\xi\,(k\,\cdot\,x)}{2\,m^2\,s}\big)}{2\,m^4\,\xi\,s\,(k\,\cdot\,x)}-\frac{i\,e\,\zeta\,\sigma {\rm F}\,f^{(0,0,1)}\big(\zeta,\,\,p^2,\,\,\frac{\xi\,(k\,\cdot\,x)}{2\,m^2\,s}\big)}{4\,m^3\,s}
```

```
Matrix101 = Collect[
                 (Expand[Matrix9] - Coefficient[Matrix9, pv2] pv2 + Matrix91) / m,
                 {sf, v1, v2, tf, af, g, \sigma F, DiracGamma[Momentum[FFx, D], D],
                       DiracGamma[Momentum[x, D], D], DiracGamma[Momentum[FDx, D], D]}, Simplify]
  Matrix102 = Expand[Matrix92/m]
   (*Matrix101=Collect[Matrix9/m,{sf,v1,v2,tf,af,g,σF, DiracGamma[Momentum[FFx,D],D],
                                      DiracGamma[Momentum[x,D],D],DiracGamma[Momentum[FDx,D],D]},Simplify]
                       Matrix102=0*)
Coeff10 = Coeff9 * m
  Phase10 = Phase9
\operatorname{af}\left(\frac{e\left(\gamma\cdot\operatorname{FDx}\right).\overline{\gamma}^{5}}{m\,\varepsilon\left(k\cdot x\right)} + \frac{i\,e^{2}\,s\,\gamma\cdot\operatorname{FFx}}{m\,\varepsilon\left(k\cdot x\right)} + \zeta\left(1 + \frac{1}{2}\,i\,e\,s\,\sigma\operatorname{F}\right)\right) +
          v1\left(\zeta\left(-\frac{e\left(\gamma\cdot\text{FDx}\right).\overline{\gamma}^{5}.(\gamma\cdot x)}{2\ m^{2}\ \xi\ s\ (k\cdot x)}+\sigma\text{F}\left(\frac{1}{6}\ e\ \xi\ s\ (k\cdot x)-\frac{i\ (D-3)\ e}{2\ m^{2}\ \xi\ (k\cdot x)}\right)-\frac{1}{2}\ i\ \xi\ (k\cdot x)\right)-\frac{1}{2}\ i\ \xi\ (k\cdot x)\right)-\frac{1}{2}\ i\ \xi\ (k\cdot x)
                                              \frac{i e(\gamma \cdot \text{FDx}) \cdot \overline{\gamma}^5}{2 m} + \frac{e^2 s \gamma \cdot \text{FFx}}{3 m} - \frac{\gamma \cdot x}{2 m s} + \text{sf} \left( \zeta \left( \frac{e(\gamma \cdot \text{FDx}) \cdot \overline{\gamma}^5}{m \varepsilon (k \cdot x)} + \frac{i e^2 s \gamma \cdot \text{FFx}}{m \varepsilon (k \cdot x)} \right) + \frac{1}{2} i e s \sigma F + 1 \right) + \frac{1}{2} i e s \sigma F + 1 + \frac{1}{2} i e s \sigma F + 1 + \frac{1}{2} i e s \sigma F + 1 + \frac{1}{2} i e s \sigma F + 1 + \frac{1}{2} i e s \sigma F + 1 + \frac{1}{2} i e s \sigma F + 1 + \frac{1}{2} i e s \sigma F + 1 + \frac{1}{2} i e s \sigma F + 1 + \frac{1}{2} i e s \sigma F + 1 + \frac{1}{2} i e s \sigma F + 1 + \frac{1}{2} i e s \sigma F + \frac{
         \operatorname{tf}\left(-\frac{4\ e^{2}\ \zeta\ s\ \gamma\cdot \operatorname{FFx}}{m\ \varepsilon^{2}\ (\ k\cdot\ x)^{2}} - \frac{2\ e\ s\ \sigma\operatorname{F}}{\varepsilon\ (k\cdot\ x)}\right) + \operatorname{v2}\left(-\frac{2\ e^{2}\ s\ \gamma\cdot \operatorname{FFx}}{m\ \varepsilon^{2}\ (\ k\cdot\ x)^{2}} - \frac{e\ \zeta\ s\ \sigma\operatorname{F}}{\varepsilon\ (k\cdot\ x)}\right)
    -\frac{i\,e^2\,\gamma\cdot\text{FFx}\,f^{(0,0,1)}\!\!\left(\zeta,\,\,p^2,\,\,\frac{\xi(k\cdot x)}{2\,m^2\,s}\right)}{2\,m^5\,\xi\,s\,(k\cdot x)}-\frac{i\,e\,\zeta\,\sigma\text{F}\,f^{(0,0,1)}\!\!\left(\zeta,\,\,p^2,\,\,\frac{\xi(k\cdot x)}{2\,m^2\,s}\right)}{4\,\,m^4\,s}
  i \, 2^{-D-2} \, e^{-\frac{1}{2} i \pi \left(\frac{D}{2}-1\right)} \pi^{-\frac{D}{2}-1} \, m \, \Lambda^{4-D} \, s^{-D/2}
-\frac{1}{12}m^2\xi^2 s(k \cdot x)^2 + e(a \cdot x)(k \cdot X) - p^2 s - \frac{x^2}{4s}
```

Matrix101 // StandardForm;

#### Matrix10 =

Collect[Expand[Matrix101 + Matrix102], {e^2 DiracGamma[Momentum[FFx, D], D], e DiracGamma [Momentum [FDx, D], D].DiracGamma [5], e DiracGamma [Momentum [FDx, D], D].DiracGamma [5].DiracGamma [Momentum [x, D], D],  $\sigma$ F, DiracGamma[Momentum[x, D], D], sf, v1, v2, tf, af,  $\xi$ }]  $e(\gamma \cdot \mathrm{FDx}).\overline{\gamma}^5 \left( \frac{\mathrm{af}}{m \, \xi \, (k \cdot x)} + \frac{\zeta \, \mathrm{sf}}{m \, \xi \, (k \cdot x)} - \frac{i \, \mathrm{v1}}{2 \, m} \right) - \frac{e \, \zeta \, \mathrm{v1} \, (\gamma \cdot \mathrm{FDx}).\overline{\gamma}^5.(\gamma \cdot x)}{2 \, m^2 \, \xi \, s \, (k \cdot x)} + \frac{e \, \zeta \, \mathrm{v2}}{2 \, m^2 \, \xi \, s \, (k \cdot x)} + \frac{e \, \zeta \, \mathrm{v2}}{2 \, m^2 \, \xi \, s \, (k \cdot x)} + \frac{e \, \zeta \, \mathrm{v2}}{2 \, m^2 \, \xi \, s \, (k \cdot x)} + \frac{e \, \zeta \, \mathrm{v2}}{2 \, m^2 \, \xi \, s \, (k \cdot x)} + \frac{e \, \zeta \, \mathrm{v2}}{2 \, m^2 \, \xi \, s \, (k \cdot x)} + \frac{e \, \zeta \, \mathrm{v2}}{2 \, m^2 \, \xi \, s \, (k \cdot x)} + \frac{e \, \zeta \, \mathrm{v2}}{2 \, m^2 \, \xi \, s \, (k \cdot x)} + \frac{e \, \zeta \, \mathrm{v2}}{2 \, m^2 \, \xi \, s \, (k \cdot x)} + \frac{e \, \zeta \, \mathrm{v2}}{2 \, m^2 \, \xi \, s \, (k \cdot x)} + \frac{e \, \zeta \, \mathrm{v2}}{2 \, m^2 \, \xi \, s \, (k \cdot x)} + \frac{e \, \zeta \, \mathrm{v2}}{2 \, m^2 \, \xi \, s \, (k \cdot x)} + \frac{e \, \zeta \, \mathrm{v2}}{2 \, m^2 \, \xi \, s \, (k \cdot x)} + \frac{e \, \zeta \, \mathrm{v2}}{2 \, m^2 \, \xi \, s \, (k \cdot x)} + \frac{e \, \zeta \, \mathrm{v2}}{2 \, m^2 \, \xi \, s \, (k \cdot x)} + \frac{e \, \zeta \, \mathrm{v2}}{2 \, m^2 \, \xi \, s \, (k \cdot x)} + \frac{e \, \zeta \, \mathrm{v2}}{2 \, m^2 \, \xi \, s \, (k \cdot x)} + \frac{e \, \zeta \, \mathrm{v2}}{2 \, m^2 \, \xi \, s \, (k \cdot x)} + \frac{e \, \zeta \, \mathrm{v2}}{2 \, m^2 \, \xi \, s \, (k \cdot x)} + \frac{e \, \zeta \, \mathrm{v2}}{2 \, m^2 \, \xi \, s \, (k \cdot x)} + \frac{e \, \zeta \, \mathrm{v2}}{2 \, m^2 \, \xi \, s \, (k \cdot x)} + \frac{e \, \zeta \, \mathrm{v2}}{2 \, m^2 \, \xi \, s \, (k \cdot x)} + \frac{e \, \zeta \, \mathrm{v2}}{2 \, m^2 \, \xi \, s \, (k \cdot x)} + \frac{e \, \zeta \, \mathrm{v2}}{2 \, m^2 \, \xi \, s \, (k \cdot x)} + \frac{e \, \zeta \, \mathrm{v2}}{2 \, m^2 \, \xi \, s \, (k \cdot x)} + \frac{e \, \zeta \, \mathrm{v2}}{2 \, m^2 \, \xi \, s \, (k \cdot x)} + \frac{e \, \zeta \, \mathrm{v2}}{2 \, m^2 \, \xi \, s \, (k \cdot x)} + \frac{e \, \zeta \, \mathrm{v2}}{2 \, m^2 \, \xi \, s \, (k \cdot x)} + \frac{e \, \zeta \, \mathrm{v2}}{2 \, m^2 \, \xi \, s \, (k \cdot x)} + \frac{e \, \zeta \, \mathrm{v2}}{2 \, m^2 \, \xi \, s \, (k \cdot x)} + \frac{e \, \zeta \, \mathrm{v2}}{2 \, m^2 \, \xi \, s \, (k \cdot x)} + \frac{e \, \zeta \, \mathrm{v2}}{2 \, m^2 \, \xi \, s \, (k \cdot x)} + \frac{e \, \zeta \, \mathrm{v2}}{2 \, m^2 \, \xi \, s \, (k \cdot x)} + \frac{e \, \zeta \, \mathrm{v2}}{2 \, m^2 \, \xi \, s \, (k \cdot x)} + \frac{e \, \zeta \, \mathrm{v2}}{2 \, m^2 \, \xi \, s \, (k \cdot x)} + \frac{e \, \zeta \, \mathrm{v2}}{2 \, m^2 \, \xi \, s \, (k \cdot x)} + \frac{e \, \zeta \, \mathrm{v2}}{2 \, m^2 \, \xi \, s \, (k \cdot x)} + \frac{e \, \zeta \, \mathrm{v2}}{2 \, m^2 \, \xi \, s \, (k \cdot x)} + \frac{e \, \zeta \, \mathrm{v2}}{2 \, m^2 \, \xi \, s \, (k \cdot x)} + \frac{e \, \zeta \, \mathrm{v2}}{2 \, m^2 \, \xi \, s \, (k \cdot x)} + \frac{e \, \zeta \, \mathrm{v2}}{2 \, m^2 \, \xi \, s \, (k \cdot x)} + \frac{e \, \zeta \, \mathrm{v2}}{2$  $\sigma F \left( -\frac{i e \zeta f^{(0,0,1)} \left( \zeta, p^2, \frac{\xi(k \cdot x)}{2 m^2 s} \right)}{4 m^4 s} + \frac{1}{2} i \text{ af } e \zeta s + \zeta v 1 \left( -\frac{i D e}{2 m^2 \xi(k \cdot x)} + \frac{3 i e}{2 m^2 \xi(k \cdot x)} + \frac{1}{6} e \xi s(k \cdot x) \right) - \frac{1}{2 m^2 \xi(k \cdot x)} + \frac{1}{6 k^2 \xi($  $\frac{2 e s tf}{\xi(k \cdot x)} - \frac{e \zeta s v2}{\xi(k \cdot x)} + \frac{1}{2} i e s sf + af \zeta - \frac{1}{2} i \zeta \xi v1 (k \cdot x) - \frac{v1 \gamma \cdot x}{2 m s} + sf$ 

```
Matrix10ReorderPart1 =
            Collect[Coefficient[Matrix10, e^2 DiracGamma[Momentum[FFx, D], D]] *
                                 m^1 \xi^2 (kx)^2, \{sf, v1, v2, tf, af, \xi\}, Simplify
                       e^2 DiracGamma [Momentum[FFx, D], D] / (m^1 \xi^2 (kx)^2) +
                 Collect Coefficient [Matrix10, e DiracGamma [Momentum [FDx, D], D].DiracGamma [5]] *
                                 m \xi (kx), {sf, v1, v2, tf, af, \xi}, Simplify] e
                      DiracGamma[Momentum[FDx, D], D].DiracGamma[5] / (m \xi (kx)) +
                 Collect[Coefficient[Matrix10, e \sigma F] * 2 m^0 \xi (kx) /\xi,
                             {sf, v1, v2, tf, af, \xi}, Simplify] e \sigma F / (2 m^0 \xi (kx) / \xi) +
                 Coefficient[Matrix10, e DiracGamma[Momentum[FDx, D], D].
                                       DiracGamma[5].DiracGamma[Momentum[x, D], D]] e
                      DiracGamma[Momentum[FDx, D], D].DiracGamma[5].DiracGamma[Momentum[x, D], D] +
                 Coefficient[Matrix10, DiracGamma[Momentum[x, D], D]]
                       DiracGamma[Momentum[x, D], D];
Matrix10Reorder = Matrix10ReorderPart1 + Expand[Matrix10 - Matrix10ReorderPart1] /.
             \{1/\zeta\to\zeta\}
 Coeff10
 Phase10
 \frac{e\left(\gamma\cdot\mathrm{FDx}\right).\overline{\gamma}^{5}\left(\mathrm{af}-\frac{1}{2}\,i\,\xi\,\mathrm{v1}\left(k\cdot x\right)+\zeta\,\mathrm{sf}\right)}{m\,\xi\left(k\cdot x\right)}-\frac{e\,\zeta\,\mathrm{v1}\left(\gamma\cdot\mathrm{FDx}\right).\overline{\gamma}^{5}.(\gamma\cdot x)}{2\,m^{2}\,\xi\,s\left(k\cdot x\right)}+
       \frac{1}{2\,\xi\,(k\cdot x)}\,e\,\zeta\,\sigma F\left(-\frac{i\,\xi\,(k\cdot x)\,f^{(0,0,1)}\!\left(\zeta,\,p^2,\,\frac{\xi\,(k\cdot x)}{2\,m^2\,s}\right)}{2\,m^4\,s}+\frac{{\rm v1}\left(m^2\,\xi^2\,s\,(\,k\cdot x\,)^2-3\,i\,D+9\,i\right)}{3\,m^2}+\right.
                                       i \operatorname{af} \xi s (k \cdot x) + i \zeta \xi s \operatorname{sf} (k \cdot x) - 4 \zeta s \operatorname{tf} - 2 s \operatorname{v2} + \frac{1}{m \xi^2 (k \cdot x)^2} e^2 \gamma \cdot \operatorname{FFx}
                       \left(-\frac{i\,\xi\,(k\cdot x)\,f^{(0,0,1)}\!\left(\zeta,\,\,p^2,\,\,\frac{\xi\,(k\cdot x)}{2\,m^2\,s}\right)}{2\,m^4\,s} + \frac{1}{3}\,\xi^2\,s\,v\,l\,\left(\,k\cdot x\,\right)^2 + i\,af\,\xi\,s\,(k\cdot x) + i\,\zeta\,\xi\,s\,sf\,(k\cdot x) - 4\,\zeta\,s\,tf - 2\,s\,v\,2\right) + \frac{1}{3}\,\xi^2\,s\,v\,l\,\left(\,k\cdot x\,\right)^2 + i\,af\,\xi\,s\,(k\cdot x) + i\,\zeta\,\xi\,s\,sf\,(k\cdot x) - 4\,\zeta\,s\,tf - 2\,s\,v\,2\right) + \frac{1}{3}\,\xi^2\,s\,v\,l\,\left(\,k\cdot x\,\right)^2 + i\,af\,\xi\,s\,(k\cdot x) + i\,\zeta\,\xi\,s\,sf\,(k\cdot x) - 4\,\zeta\,s\,tf - 2\,s\,v\,2\right) + \frac{1}{3}\,\xi^2\,s\,v\,l\,\left(\,k\cdot x\,\right)^2 + i\,af\,\xi\,s\,(k\cdot x) + i\,\zeta\,\xi\,s\,sf\,(k\cdot x) - 4\,\zeta\,s\,tf - 2\,s\,v\,2\right) + \frac{1}{3}\,\xi^2\,s\,v\,l\,\left(\,k\cdot x\,\right)^2 + i\,af\,\xi\,s\,(k\cdot x) + i\,\zeta\,\xi\,s\,sf\,(k\cdot x) - 4\,\zeta\,s\,tf - 2\,s\,v\,2\right) + \frac{1}{3}\,\xi^2\,s\,v\,l\,\left(\,k\cdot x\,\right)^2 + i\,af\,\xi\,s\,(k\cdot x) + i\,\zeta\,\xi\,s\,sf\,(k\cdot x) - 4\,\zeta\,s\,tf - 2\,s\,v\,2\right) + \frac{1}{3}\,\xi^2\,s\,v\,l\,\left(\,k\cdot x\,\right)^2 + i\,af\,\xi\,s\,(k\cdot x) + i\,\zeta\,\xi\,s\,sf\,(k\cdot x) - 4\,\zeta\,s\,tf - 2\,s\,v\,2\right) + \frac{1}{3}\,\xi^2\,s\,v\,l\,\left(\,k\cdot x\,\right)^2 + i\,af\,\xi\,s\,(k\cdot x) + i\,\zeta\,\xi\,s\,sf\,(k\cdot x) - 4\,\zeta\,s\,tf - 2\,s\,v\,2\right) + \frac{1}{3}\,\xi^2\,s\,v\,l\,\left(\,k\cdot x\,\right)^2 + i\,af\,\xi\,s\,(k\cdot x) + i\,\zeta\,\xi\,s\,sf\,(k\cdot x) - 4\,\zeta\,s\,tf - 2\,s\,v\,2\right) + \frac{1}{3}\,\xi^2\,s\,v\,l\,\left(\,k\cdot x\,\right)^2 + i\,af\,\xi\,s\,(k\cdot x) + i\,\zeta\,\xi\,s\,sf\,(k\cdot x) + i\,\zeta\,\xi\,s\,sf\,(
        \operatorname{af} \zeta - \frac{1}{2} i \zeta \xi \operatorname{vl} (k \cdot x) - \frac{\operatorname{vl} \gamma \cdot x}{2 m s} + \operatorname{sf}
\frac{i \, 2^{-D-2} \, e^{-\frac{1}{2} i \pi \left(\frac{D}{2}-1\right)} \pi^{-\frac{D}{2}-1} \, m \, \Lambda^{4-D} \, s^{-D/2}}{\text{DdInv}(\mathcal{L})}
-\frac{1}{12}m^2\xi^2 s(k \cdot x)^2 + e(a \cdot x)(k \cdot X) - p^2 s - \frac{x^2}{4s}
```

Matrix10 without removing p^2 with integration by parts

$$sf + af \, \mathcal{E} - \frac{\text{vi DiracGamma}[\mathsf{Momentum}[x,D],D]}{2\,\,\text{ms}} - \left(\text{evi}\,\mathcal{E}\right)$$

$$DiracGamma[\mathsf{Momentum}[\mathsf{FDX},D],D].DiracGamma[\mathsf{S}].DiracGamma[\mathsf{Momentum}[x,D],D] / \left(2\,\,\text{m}^2\,\,\text{s}\,\,\mathcal{E}\,\,\text{Pair}[\mathsf{Momentum}[k,D],\mathsf{Momentum}[x,D]]\right) - \frac{1}{2}\,\,\text{ivi}\,\,\mathcal{E}\,\,\mathcal{E}$$

$$Pair[\mathsf{Momentum}[k,D],\mathsf{Momentum}[x,D]] + \left(\text{e DiracGamma}[\mathsf{Momentum}[k,D],\mathsf{Momentum}[x,D])\right) / \left(\text{m}\,\,\mathcal{E}\,\,\text{Pair}[\mathsf{Momentum}[k,D],\mathsf{Momentum}[x,D]\right) + \left(\text{e }\,\,\mathcal{E}\,\,\text{or}\,\,\mathcal{E}\,\,\mathcal{E}\,\,\text{Pair}[\mathsf{Momentum}[k,D],\mathsf{Momentum}[x,D])\right) / \left(\text{m}\,\,\mathcal{E}\,\,\text{Pair}[\mathsf{Momentum}[k,D],\mathsf{Momentum}[x,D]\right) + \frac{1}{4\,\,\text{m}^2\,\,\text{s}}\,\,\text{vi}\,\,(8\,\,\text{si}\,\,\text{s}\,\,\text{-}\,\,2\,\,\text{iD}\,\,\text{s}\,\,\text{+}\,\,\text{inf}\,\,\text{s}\,\,\mathcal{E}\,\,\text{Pair}[\mathsf{Momentum}[x,D]\right) + \frac{1}{4\,\,\text{m}^2\,\,\text{s}}\,\,\text{vi}\,\,(8\,\,\text{si}\,\,\text{s}\,\,\text{-}\,\,2\,\,\text{s}\,\,\text{D}\,\,\text{s}\,\,\text{s}\,\,\text{momentum}[x,D]\right) + \frac{1}{4\,\,\text{m}^2\,\,\text{s}}\,\,\text{vi}\,\,(8\,\,\text{si}\,\,\text{s}\,\,\text{-}\,\,2\,\,\text{s}\,\,\text{D}\,\,\text{s}\,\,\text{s}\,\,\text{momentum}[x,D]\right) + \frac{1}{4\,\,\text{m}^2\,\,\text{s}}\,\,\text{vi}\,\,(8\,\,\text{si}\,\,\text{s}\,\,\text{-}\,\,2\,\,\text{s}\,\,\text{D}\,\,\text{s}\,\,\text{s}\,\,\text{momentum}[x,D]\right) / \left(2\,\,\mathcal{E}\,\,\text{Pair}[\mathsf{Momentum}[k,D],\mathsf{Momentum}[x,D],\mathsf{Momentum}[x,D]\right) + \frac{1}{4\,\,\text{m}^2\,\,\text{s}}\,\,\text{vi}\,\,(3\,\,\text{s}\,\,\text{s}\,\,\text{s}\,\,\text{s}\,\,\text{e}\,\,\text{pair}[\mathsf{Momentum}[k,D],\mathsf{Momentum}[x,D]\right) + \frac{1}{4\,\,\text{m}^2\,\,\text{s}}\,\,\text{vi}\,\,(1-4\,\,\text{s}\,\,\text{s}\,\,\text{s}\,\,\text{e}\,\,\text{pair}[\mathsf{Momentum}[x,D],\mathsf{Momentum}[x,D]\right) + \frac{1}{4\,\,\text{m}^2\,\,\text{s}}\,\,\text{vi}\,\,(1-4\,\,\text{s}\,\,\text{s}\,\,\text{s}\,\,\text{e}\,\,\text{e}\,\,\text{pair}[\mathsf{Momentum}[k,D],\mathsf{Momentum}[x,D]\right) / \left(m\,\,\mathcal{E}^2\,\,\text{Pair}[\mathsf{Momentum}[x,D],\mathsf{Momentum}[x,D]\right) + \frac{1}{4\,\,\text{m}^2\,\,\text{s}}\,\,\text{vi}\,\,(1-4\,\,\text{s}\,\,\text{s}\,\,\text{s}\,\,\text{e}\,\,\text{s}\,\,\text{e}\,\,\text{s}\,\,\text{o}\,\,\text{s}\,\,\text{o}\,\,\text{s}\,\,\text{o}\,\,\text{o}\,\,\text{o}\,\,\text{o}\,\,\text{o}\,\,\text{o}\,\,\text{o}\,\,\text{o}\,\,\text{o}\,\,\text{o}\,\,\text{o}\,\,\text{o}\,\,\text{o}\,\,\text{o}\,\,\text{o}\,\,\text{o}\,\,\text{o}\,\,\text{o}\,\,\text{o}\,\,\text{o}\,\,\text{o}\,\,\text{o}\,\,\text{o}\,\,\text{o}\,\,\text{o}\,\,\text{o}\,\,\text{o}\,\,\text{o}\,\,\text{o}\,\,\text{o}\,\,\text{o}\,\,\text{o}\,\,\text{o}\,\,\text{o}\,\,\text{o}\,\,\text{o}\,\,\text{o}\,\,\text{o}\,\,\text{o}\,\,\text{o}\,\,\text{o}\,\,\text{o}\,\,\text{o}\,\,\text{o}\,\,\text{o}\,\,\text{o}\,\,\text{o}\,\,\text{o}\,\,\text{o}\,\,\text{o}\,\,\text{o}\,\,\text{o}\,\,\text{o}\,\,\text{o}\,\,\text{o}\,\,\text{o}\,\,\text{o}\,\,\text{o}\,\,\text{o}\,\,\text{o}\,\,\text{o}\,\,\text{o}\,\,\text{o}\,\,\text{o}\,\,\text{o}\,\,\text{o}\,\,\text{o}\,\,\text{o}\,\,\text{o}\,\,\text{o}\,\,\text{o}\,\,\text{o}\,\,\text{o}\,\,\text{o}\,\,\text{o}\,\,\text{o}\,\,\text{o}\,\,\text{o}\,\,\text{o}\,\,\text{o}\,$$

Matrix111 = Collect[

DiracOrder[DiracSimplify[Expand[Matrix101] /. FxToEps /. FxToak /. Gamma5toTrippleGammax /.  $\{av2 \rightarrow -\xi^2 m^2 / e^2\}$ ],

{sf, v1, v2, tf, af, \( \gamma \)}, Simplify

 $-\frac{1}{12}m^2\xi^2 s(k\cdot x)^2 + e(a\cdot x)(k\cdot X) - p^2 s - \frac{x^2}{4s}$ 

Matrix112 = Expand[Matrix102 /. FxToEps /. FxToak /. Gamma5toTrippleGammax] Coeff10

Phase10

$$\begin{aligned} & \text{v1} \left( \frac{1}{6 \, m \, s} \left( s \left( y \cdot k \left( 2 \, m^2 \, \xi^2 \, s \left( k \cdot x \right) - 3 \, e \left( a \cdot x \right) \right) + 3 \, e \, \gamma \cdot a \, \left( k \cdot x \right) - 3 \, e \left( \gamma \cdot a \right) . \left( \gamma \cdot k \right) . \left( \gamma \cdot x \right) \right) - 3 \, \gamma \cdot x \right) - \\ & \quad \left( i \, \zeta \left( e \left( \gamma \cdot a \right) . \left( \gamma \cdot k \right) \left( 2 \, m^2 \, \xi^2 \, s^2 \left( \, k \cdot x \right)^2 - 6 \, i \, \left( D - 3 \right) \, s - 3 \, x^2 \right) + \\ & \quad 3 \, \left( k \cdot x \right) \left( e \left( \gamma \cdot a \right) . \left( \gamma \cdot k \right) + m^2 \, \xi^2 \, s \, \left( k \cdot x \right) \right) - 3 \, e \left( a \cdot x \right) \left( \gamma \cdot k \right) . \left( \gamma \cdot x \right) \right) \right) / \left( 6 \, m^2 \, \xi \, s \, \left( k \cdot x \right) \right) \right) + \\ & \quad 4 \, \left( \left\{ \zeta \left( e \, s \left( \gamma \cdot a \right) . \left( \gamma \cdot k \right) + 1 \right) + \frac{1}{m \, \xi \left( k \cdot x \right)} \, i \, \left( \gamma \cdot k \left( m^2 \, \xi^2 \, s \, \left( k \cdot x \right) - e \left( a \cdot x \right) \right) + e \, \gamma \cdot a \, \left( k \cdot x \right) - e \left( \gamma \cdot a \right) . \left( \gamma \cdot k \right) . \left( \gamma \cdot x \right) \right) \right) + \\ & \quad 5 \, \left( \left\{ \frac{1}{m \, \xi \left( k \cdot x \right)} \, i \, \zeta \left( \gamma \cdot k \left( m^2 \, \xi^2 \, s \, \left( k \cdot x \right) - e \left( a \cdot x \right) \right) + e \, \gamma \cdot a \, \left( k \cdot x \right) - e \left( \gamma \cdot a \right) . \left( \gamma \cdot k \right) . \left( \gamma \cdot x \right) \right) + e \, s \, \left( \gamma \cdot a \right) . \left( \gamma \cdot k \right) \left( \gamma \cdot k \right) \right) \right) + \\ & \quad 1 \, \left\{ \left\{ \left\{ \frac{4 \, \zeta \, m \, s \, \gamma \cdot k}{k \cdot x} + \frac{4 \, i \, e \, s \, \left( \gamma \cdot a \right) . \left( \gamma \cdot k \right)}{\xi \left( k \cdot x \right)} \right) + e \, \gamma \cdot k \, f^{(0,0,1)} \left( \zeta , \, p^2, \, \frac{\xi \left( k \cdot x \right)}{2 \, m^2 \, s} \right) \right) \right\} \\ & \quad 2 \, \left\{ \frac{2 \, m \, s \, \gamma \cdot k}{k \cdot x} + \frac{2 \, i \, e \, \zeta \, s \, \left( \gamma \cdot a \right) . \left( \gamma \cdot k \right)}{\xi \left( k \cdot x \right)} \right) \right\} \\ & \quad 2 \, m^4 \, s + \frac{1 \, a^2 \, e^2 \, \gamma \cdot k \, f^{(0,0,1)} \left( \zeta , \, p^2, \, \frac{\xi \left( k \cdot x \right)}{2 \, m^2 \, s} \right)}{2 \, m^5 \, \xi \, s} \right) \\ & \quad 1 \, 2 \, m^5 \, \xi \, s + \frac{1 \, a^2 \, e^2 \, \gamma \cdot k \, f^{(0,0,1)} \left( \zeta , \, p^2, \, \frac{\xi \left( k \cdot x \right)}{2 \, m^2 \, s} \right)}{2 \, m^5 \, \xi \, s} \right) \\ & \quad 1 \, 2 \, m^{-D-2} \, e^{-\frac{1}{2} \, i \, \pi \left( \frac{D}{2} - 1 \right) \, \pi^{-\frac{D}{2} - 1} \, m \, \Lambda^{4-D} \, s^{-D/2}}{2 \, m^2 \, s} \right) \\ & \quad 1 \, 2 \, m^{-D-1} \, \left\{ \left\{ \frac{D}{2} \, m^2 \, s \right\} \right\} \right\} \right)$$

```
Collect[Expand[Matrix111],
                 DiracGamma[Momentum[x, D], D],
                 DiracGamma[Momentum[k, D], D],
                 DiracGamma[Momentum[a, D], D],
                 DiracGamma[Momentum[a, D], D].DiracGamma[Momentum[k, D], D],
                  DiracGamma[Momentum[a, D], D].DiracGamma[Momentum[x, D], D],
                 DiracGamma[Momentum[k, D], D].DiracGamma[Momentum[x, D], D],
                 DiracGamma[Momentum[a, D], D].
                          DiracGamma[Momentum[k, D], D].DiracGamma[Momentum[x, D], D],
                  sf, v1, v2, tf, af, \(\gamma\)}]
(\gamma \cdot a).(\gamma \cdot k)
                         \left(\operatorname{af} e\zeta s + \zeta v \operatorname{1} \left( -\frac{De}{m^2 \varepsilon(k \cdot x)} + \frac{i e x^2}{2 m^2 \varepsilon s(k \cdot x)} + \frac{3e}{m^2 \varepsilon(k \cdot x)} - \frac{1}{3} i e \xi s(k \cdot x) \right) + \frac{4 i e s \operatorname{tf}}{\varepsilon(k \cdot x)} + \frac{2 i e \zeta s v 2}{\varepsilon(k \cdot x)} + e s \operatorname{sf} \right) +
           \gamma \cdot k \left( \operatorname{af} \left( i \, m \, \xi \, s - \frac{i \, e \, (a \cdot x)}{m \, \xi \, (k \cdot x)} \right) + \zeta \operatorname{sf} \left( i \, m \, \xi \, s - \frac{i \, e \, (a \cdot x)}{m \, \xi \, (k \cdot x)} \right) + \operatorname{v1} \left( \frac{1}{3} \, m \, \xi^2 \, s \, (k \cdot x) - \frac{e \, (a \cdot x)}{2 \, m} \right) - 
                                                     \frac{4 \zeta m s tf}{k \cdot x} - \frac{2 m s v2}{k \cdot x} + (\gamma \cdot a) \cdot (\gamma \cdot k) \cdot (\gamma \cdot x) \left( -\frac{i af e}{m \xi (k \cdot x)} - \frac{i e \zeta sf}{m \xi (k \cdot x)} - \frac{e v1}{2 m} \right) +
           \gamma \cdot a \left( \frac{i \text{ af } e}{m \, \xi} + \frac{e \, \text{v1} \, (k \cdot x)}{2 \, m} + \frac{i \, e \, \zeta \, \text{sf}}{m \, \xi} \right) + \frac{i \, e \, \zeta \, \text{v1} \, (a \cdot x) \, (\gamma \cdot k).(\gamma \cdot x)}{2 \, m^2 \, \xi \, s \, (k \cdot x)} - \frac{i \, e \, \zeta \, \text{v1} \, (\gamma \cdot a).(\gamma \cdot x)}{2 \, m^2 \, \xi \, s} + \frac{i \, e \, \zeta \, \text{v1} \, (a \cdot x) \, (\gamma \cdot k).(\gamma \cdot x)}{2 \, m^2 \, \xi \, s} + \frac{i \, e \, \zeta \, \text{v1} \, (a \cdot x) \, (\gamma \cdot k).(\gamma \cdot x)}{2 \, m^2 \, \xi \, s} + \frac{i \, e \, \zeta \, \text{v1} \, (a \cdot x) \, (\gamma \cdot k).(\gamma \cdot x)}{2 \, m^2 \, \xi \, s} + \frac{i \, e \, \zeta \, \text{v1} \, (a \cdot x) \, (\gamma \cdot k).(\gamma \cdot x)}{2 \, m^2 \, \xi \, s} + \frac{i \, e \, \zeta \, \text{v1} \, (a \cdot x) \, (\alpha \cdot x) \, (\alpha \cdot x) \, (\alpha \cdot x) \, (\alpha \cdot x)}{2 \, m^2 \, \xi \, s} + \frac{i \, e \, \zeta \, \text{v2} \, (\alpha \cdot x) \, (\alpha \cdot x)}{2 \, m^2 \, \xi \, s} + \frac{i \, e \, \zeta \, \text{v2} \, (\alpha \cdot x) \, (\alpha \cdot x) \, (\alpha \cdot x) \, (\alpha \cdot x) \, (\alpha \cdot x)}{2 \, m^2 \, \xi \, s} + \frac{i \, e \, \zeta \, \text{v2} \, (\alpha \cdot x) \, (\alpha \cdot x
            \operatorname{af} \zeta - \frac{1}{2} i \zeta \xi \operatorname{vl} (k \cdot x) - \frac{\operatorname{vl} \gamma \cdot x}{2 - \cdots} + \operatorname{sf}
```

# Final result for the electron propagator in a CCF

$$\begin{split} S^{c}\left(x_{2},\,x_{1}\right) &= \Lambda^{4-D} \int \frac{\mathrm{d}^{D}p}{\left(2\,\pi\right)^{\,D}}\,E_{p}\left(x_{2}\right) \\ &= \sum_{\mathcal{E}=+-}\frac{\frac{\mathrm{i}}{2}\left[m\,s\,\left(p^{2}\,,\,\chi_{p}\right)\,-\,\left(\gamma p\right)\,\,v_{1}\left(p^{2}\,,\,\chi_{p}\right)\,-\,\frac{e^{2}\,\left(\gamma F^{2}\,p\right)}{m^{4}}\,\,v_{2}\left(p^{2}\,,\,\chi_{p}\right)\,-\,\frac{e\,\sigma F}{m}\,t\,\left(p^{2}\,,\,\chi_{p}\right)\,+\,\frac{e\,\left(\gamma F^{*}\,p\right)\,\gamma^{5}}{m^{2}}\,a_{s}\left(p^{2}\,,\,\chi_{p}\right)\,\left]\,\frac{1\,+\,\mathcal{E}\,\gamma \varepsilon^{\,(2)}\,\gamma^{5}}{D_{\mathcal{E}}\left(p^{2}\,,\,\chi_{p}\right)}\,E_{p}^{bar}\left(x_{1}\right)\,=\\ &= e^{-\mathrm{i}\,\frac{\pi}{2}\,\left(\frac{D}{2}-2\right)}\,\frac{m\,\Lambda^{4-D}}{2^{D+2}\,\pi^{D/2+1}}\,e^{\mathrm{i}\,\eta}\,\sum_{\mathcal{E}=+-}\int_{0}^{\infty}\frac{\mathrm{d}\,S}{s^{D/2}}\left(\int_{0}^{\infty}\frac{\mathrm{d}\,p^{2}}{D_{\mathcal{E}}\left(p^{2}\,,\,\chi_{p}\left(s\right)\right)}\,e^{-\mathrm{i}\,sp^{2}-\mathrm{i}\,\frac{\chi^{2}}{4\,s}+\mathrm{i}\,\frac{s}{12}\,e^{2}\left(Fx\right)^{2}}\,\times\\ &\left\{\,s\,\left(p^{2}\,,\,\chi_{p}\left(s\right)\right)\,\right[\\ &= 1\,+\,\frac{1}{2}\,\,\mathrm{i}\,\,s\,e\,\,\sigma F\,+\,\mathcal{E}\,\left(\frac{\mathrm{i}\,\,e^{2}\,s\,\left(\gamma\,FFx\right)}{m\,\mathcal{E}\left(kx\right)}\,+\,\frac{e\,F_{\alpha\beta}^{*}\,x^{\beta}\,\gamma^{\alpha}\,\gamma^{5}}{m\,\mathcal{E}\left(kx\right)}\,\right)\\ &+ v_{1}\,\left(p^{2}\,,\,\chi_{p}\left(s\right)\right)\left[\,-\,\frac{\left(\gamma x\right)}{2\,m\,s}\,+\,\frac{e^{2}\,s\,\left(\gamma\,FFx\right)}{3\,m}\,-\,\frac{\mathrm{i}\,\,e\,F_{\alpha\beta}^{*}\,x^{\beta}\,\gamma^{\alpha}\,\gamma^{5}}{2\,m}\,\right] \end{split}$$

$$\begin{split} + \mathcal{E}\left(-\frac{1}{2} \ i \ \mathcal{E} \ (kx) - \frac{e \ \sigma F}{2 \ m^2 \ \mathcal{E} \ (kx)}\right) \\ & \left(i \ (D-3) - \frac{1}{3} \ m^2 \ s \ \mathcal{E}^2 \ (kx)^2\right) - \frac{e \ (\gamma F^* \ x) \ \gamma^5 \ (\gamma X)}{2 \ m^2 \ \mathcal{E} \ s \ (kx)}\right) \Big] \\ & + v_2 \ (p^2, \ \chi_p \ (s)) \Big[ - \frac{2 \ s \ e^2 \ (\gamma \ FFx)}{m \ \mathcal{E}^2 \ (kx)^2} - \mathcal{E} \frac{s \ e^3 \ \mathcal{E}}{\mathcal{E} \ (kx)} \Big] \\ & + t \ (p^2, \ \chi_p \ (s)) \Big[ - \frac{2 \ s \ e^3 \ (\gamma \ FFx)}{m \ \mathcal{E}^2 \ (kx)} - \mathcal{E} \frac{s \ e^3 \ \mathcal{E}}{\mathcal{E} \ (kx)} \Big] \\ & + t \ (p^2, \ \chi_p \ (s)) \Big[ - \frac{2 \ s \ e^3 \ (r \ FFx)}{\mathcal{E} \ (kx)} - \mathcal{E} \frac{s \ e^3 \ (r \ FFx)}{\mathcal{E} \ (kx)^2} \Big] \\ & + t \ (p^2, \ \chi_p \ (s)) \Big[ - \frac{2 \ s \ e^3 \ (r \ FFx)}{\mathcal{E} \ (kx)} - \mathcal{E} \frac{s^2 \ (r \ FFx)}{\mathcal{E} \ (kx)^2} \Big] \\ & + t \ (p^2, \ \chi_p \ (s)) \Big[ - \frac{2 \ s \ e^3 \ (r \ FFx)}{\mathcal{E} \ (kx)} - \mathcal{E} \frac{s^2 \ (r \ FFx)}{m \ \mathcal{E}^2 \ (kx)^2} \Big] \\ & + t \ (p^2, \ \chi_p \ (s)) \Big[ - \frac{1}{2} \ i \ s \ e^3 \ (r^2 \ FFx) \Big] \\ & + t \ (p^2, \ \chi_p \ (s)) \Big[ - \frac{1}{2} \ i \ s \ e^3 \ (r^2 \ FFx) \Big] \\ & + t \ (p^2, \ \chi_p \ (s)) \Big[ - \frac{1}{2} \ i \ s \ e^3 \ (r^2 \ FFx) \Big] \\ & + t \ (p^2, \ \chi_p \ (s)) \Big[ - \frac{1}{2} \ i \ s \ e^3 \ (r^2 \ FFx) \Big] \\ & + t \ (p^2, \ \chi_p \ (s)) \Big[ - \frac{1}{2} \ i \ e^3 \ e^3 \ (r^2 \ FFx) \Big] \\ & + t \ (p^2, \ \chi_p \ (s)) \Big[ - \frac{1}{2} \ i \ e^3 \ e^3 \ (r^2 \ FFx) \Big] \\ & + t \ (p^2, \ \chi_p \ (s)) \Big[ - \frac{1}{2} \ i \ e^3 \ e^3 \ (r^2 \ FFx) \Big] \\ & + t \ (p^2, \ \chi_p \ (s)) \Big[ - \frac{1}{2} \ i \ e^3 \ e^3 \ (r^2 \ FFx) \Big] \\ & + t \ (p^2, \ \chi_p \ (s)) \Big[ - \frac{1}{2} \ i \ e^3 \ e^3 \ (r^2 \ FFx) \Big] \\ & + t \ (p^2, \ \chi_p \ (s)) \Big[ - \frac{1}{2} \ i \ e^3 \ e^3 \ e^3 \ (r^2 \ FFx) \Big] \\ & + t \ (p^2, \ \chi_p \ (s)) \Big[ - \frac{1}{2} \ i \ e^3 \ e^3 \ (r^2 \ i \ i \ e^3 \$$

$$\begin{split} &m^2 \Big[ \text{i} \ \xi \ \xi \ (kx) \ s \ s \ (p) + \frac{1}{3} \, s \ \xi^2 \ (kx)^2 \, v_1 \ (p) - 2 \, s \, v_2 \ (p) - 4 \, \xi \, s \, t \ (p) + \\ & \text{i} \ \xi \, s \ (kx) \ a \ (p) - \frac{\text{i} \ \xi \ (kx)}{2 \, m^4 \, s} \ D_\xi \left( p^2, \ \chi_p \ (s) \right) \frac{\partial}{\partial \chi_p} \left( \frac{v_1 \left( p^2, \chi_p \right)}{D_\xi \left( p^2, \chi_p \right)} \right) \Big] \\ & + \xi \, \frac{e \, \sigma F}{m^2 \, \xi \ (kx)} \, m^2 \Big[ \text{i} \ \xi \, \xi \ (kx) \, s \, s \ (p) + \left( \frac{1}{3} \, s \, \xi^2 \ (kx)^2 - \frac{\text{i} \ (D-3)}{m^2} \right) \\ & \quad v_1 \ (p) - 2 \, s \, v_2 \ (p) - 4 \, \xi \, s \, t \ (p) + \text{i} \ \xi \, s \ (kx) \ a \ (p) - \\ & \quad \frac{\text{i} \ \xi \ (kx)}{2 \, m^4 \, s} \, D_\xi \left( p^2, \chi_p \ (s) \right) \frac{\partial}{\partial \chi_p} \left( \frac{v_1 \left( p^2, \chi_p \right)}{p^2 \left( p^2, \chi_p \right)} \right) \Big] \\ & \quad + \frac{e \ (\gamma F^* \, x) \, \gamma^5}{m \, \xi \ (kx)} \Big[ \xi \, s \ (p) - \frac{\text{i}}{2} \, \xi \ (kx) \, v_1 \ (p) + a \ (p) \Big] \\ & \quad - \xi \, \frac{e \ (\gamma F^* \, x) \, \gamma^5}{2 \, m^2 \, s} \, \xi \ (kx) \\ & \quad - \frac{e \ (\gamma F^* \, x) \, \gamma^5}{2 \, m^2 \, s} \, \xi \ (kx) \\ & \quad - \frac{e \ (\gamma F^* \, x) \, \gamma^5}{2 \, m^2 \, s} \, \xi \ (kx) \\ & \quad - \frac{e \ (\gamma F^* \, x) \, \gamma^5}{2 \, m^2 \, s} \, \xi \ (kx) \\ & \quad - \frac{e \ (\gamma F^* \, x) \, \gamma^5}{2 \, m^2 \, s} \, \xi \ (kx) \\ & \quad - \frac{e \ (\gamma F^* \, x) \, \gamma^5}{2 \, m^2 \, s} \, \xi \ (kx) \\ & \quad - \frac{e \ (\gamma F^* \, x) \, \gamma^5}{2 \, m^2 \, s} \, \xi \ (kx) \\ & \quad - \frac{e \ (\gamma F^* \, x) \, \gamma^5}{2 \, m^2 \, s} \, \xi \ (kx) \\ & \quad - \frac{e \ (\gamma F^* \, x) \, \gamma^5}{2 \, m^2 \, s} \, \xi \ (kx) \\ & \quad - \frac{e \ (\gamma F^* \, x) \, \gamma^5}{2 \, m^2 \, s} \, \xi \ (kx) \\ & \quad - \frac{e \ (\gamma F^* \, x) \, \gamma^5}{2 \, m^2 \, s} \, \xi \ (kx) \\ & \quad - \frac{e \ (\gamma F^* \, x) \, \gamma^5}{2 \, m^2 \, s} \, \xi \ (kx) \\ & \quad - \frac{e \ (\gamma F^* \, x) \, \gamma^5}{2 \, m^2 \, s} \, \xi \ (kx) \\ & \quad - \frac{e \ (\gamma F^* \, x) \, \gamma^5}{2 \, m^2 \, s} \, \xi \ (kx) \\ & \quad - \frac{e \ (\gamma F^* \, x) \, \gamma^5}{2 \, m^2 \, s} \, \xi \ (kx) \\ & \quad - \frac{e \ (\gamma F^* \, x) \, \gamma^5}{2 \, m^2 \, s} \, \xi \ (kx) \\ & \quad - \frac{e \ (\gamma F^* \, x) \, \gamma^5}{2 \, m^2 \, s} \, \xi \ (kx) \\ & \quad - \frac{e \ (\gamma F^* \, x) \, \gamma^5}{2 \, m^2 \, s} \, \xi \ (kx) \\ & \quad - \frac{e \ (\gamma F^* \, x) \, \gamma^5}{2 \, m^2 \, s} \, \xi \ (kx) \\ & \quad - \frac{e \ (\gamma F^* \, x) \, \gamma^5}{2 \, m^2 \, s} \, \xi \ (kx) \\ & \quad - \frac{e \ (\gamma F^* \, x) \, \gamma^5}{2 \, m^2 \, s} \, \xi \ (kx) \ (kx) \\ & \quad - \frac{e \ (\gamma F^* \, x) \, \gamma^5}{2 \, m^2 \, s} \, \xi \ (kx) \ (kx) \\ & \quad - \frac{e \$$