This is a part of SFQED-Loops script collection developed for calculating loop processes in Strong-Field Quantum Electrodynamics.

The scripts are available on https://github.com/ArsenyMironov/SFQED-Loops

If you use this script in your research, please, consider citing our papers:

- A. A. Mironov, S. Meuren, and A. M. Fedotov, PRD 102, 053005 (2020), https://doi.org/10.1103/PhysRevD.102.053005

If you have any questions, please, don't hesitate to contact me: mironov.hep@gmail.com

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Get["FeynCalc`"]
\$PrePrint = TraditionalForm

FeynCalc is already loaded! To reload it, please restart the kernel.

\$Aborted

TraditionalForm

```
kv[\alpha] = Pair[LorentzIndex[\alpha, D], Momentum[k, D]];
av[\alpha] = Pair[LorentzIndex[\alpha, D], Momentum[a, D]];
av2 = Contract[av[\alpha] av[\alpha]];
\mathsf{Ft}[\alpha_{-}, \beta_{-}] =
    TensorFunction[\{F, "A"\}, LorentzIndex[\alpha, D], LorentzIndex[\beta, D], Dimension \rightarrow D];
FFt[\alpha_{-}, \beta_{-}] = TensorFunction[\{FF, "S"\}, LorentzIndex[\alpha, D],
       LorentzIndex[\beta, D], Dimension \rightarrow D];
FDt[\alpha_{-}, \beta_{-}] = TensorFunction[\{FD, "A"\}, LorentzIndex[\alpha, D],
       LorentzIndex[\beta, D], Dimension \rightarrow D];
ScalarProduct[k, a] = 0;
ScalarProduct[k, k] = 0;
FieldSubstitutions = {Ft[\alpha_, \beta_] Ft[\beta_, \gamma_] Ft[\gamma_, \delta_] \rightarrow 0,
       \mathsf{Ft}[\alpha_-, \beta_-] \; \mathsf{Ft}[\beta_-, \varepsilon_-] \; \mathsf{Ft}[\delta_-, \varepsilon_-] \to 0, \; \mathsf{Ft}[\alpha_-, \beta_-] \; \mathsf{Ft}[\alpha_-, \gamma_-] \; \mathsf{Ft}[\gamma_-, \delta_-] \to 0,
       \mathsf{Ft}[\alpha_-, \beta_-] \; \mathsf{Ft}[\alpha_-, \varepsilon_-] \; \mathsf{Ft}[\delta_-, \varepsilon_-] \to 0, \; \mathsf{Ft}[\alpha_-, \beta_-] \; \mathsf{Ft}[\alpha_-, \beta_-] \to 0,
       \mathsf{FDt}[\alpha_-,\,\beta_-]\,\,\mathsf{FDt}[\beta_-,\,\gamma_-]\,\,\mathsf{FDt}[\gamma_-,\,\delta_-]\,\to\,0,\,\,\mathsf{FDt}[\alpha_-,\,\beta_-]\,\,\mathsf{FDt}[\beta_-,\,\epsilon_-]\,\,\mathsf{FDt}[\delta_-,\,\epsilon_-]\,\to\,0,
       FDt[\alpha_{-}, \beta_{-}] FDt[\alpha_{-}, \gamma_{-}] FDt[\gamma_{-}, \delta_{-}] \rightarrow 0
       FDt[\alpha_{-}, \beta_{-}] FDt[\alpha_{-}, \epsilon_{-}] FDt[\delta_{-}, \epsilon_{-}] \rightarrow 0, FDt[\alpha_{-}, \beta_{-}] FDt[\alpha_{-}, \beta_{-}] \rightarrow 0,
       FDt[\alpha_{-}, \beta_{-}] FDt[\beta_{-}, \gamma_{-}] \rightarrow Ft[\alpha, \beta] Ft[\beta, \gamma],
       FDt[\alpha_{-}, \beta_{-}] FDt[\alpha_{-}, \gamma_{-}] \rightarrow Ft[\alpha, \beta] Ft[\alpha, \gamma],
       Ft[\alpha_{-}, \beta_{-}] Ft[\beta_{-}, \gamma_{-}] \rightarrow FFt[\alpha, \gamma],
       Ft[\alpha_{-}, \beta_{-}] Ft[\alpha_{-}, \gamma_{-}] \rightarrow -FFt[\beta, \gamma],
       Ft[\alpha_{-}, \gamma_{-}] Ft[\beta_{-}, \gamma_{-}] \rightarrow -FFt[\alpha, \beta],
       Ft[\alpha_{-}, \beta_{-}] FDt[\beta_{-}, \gamma_{-}] \rightarrow 0,
       Ft[\alpha_{-}, \beta_{-}] FDt[\alpha_{-}, \gamma_{-}] \rightarrow 0,
       FDt[\alpha_{-}, \beta_{-}] Ft[\beta_{-}, \gamma_{-}] \rightarrow 0,
       FDt[\alpha_{-}, \beta_{-}] Ft[\alpha_{-}, \gamma_{-}] \rightarrow 0,
      Contract[FFt[\mu_, \nu_] FFt[\mu_, \nu_]] \rightarrow 0,
      Contract[FFt[\alpha_{-}, \nu_{-}] FFt[\beta_{-}, \nu_{-}]] \rightarrow 0,
      Contract[Ft[\mu_{-}, \nu] kv[\nu]] \rightarrow 0,
      Contract[FDt[\mu_{-}, \nu] kv[\nu]] \rightarrow 0,
      Contract[FFt[\mu_{-}, \nu] kv[\nu]] \rightarrow 0,
      Contract[FFt[\mu_{-}, \nu] av[\nu]] \rightarrow 0,
      Contract[Ft[\mu, \nu] av[\nu]] \rightarrow av2 kv[\mu],
      Contract[FFt[\mu, \nu] kv[\mu] kv[\nu]] \rightarrow 0};
FTensor[\alpha_{-}, \beta_{-}] = (kv[\alpha] av[\beta] - kv[\beta] av[\alpha])
FDTensor [\mu_{-}, \nu_{-}] = \text{Contract} [1/2 LC [\mu, \nu, \alpha, \beta] \text{ FTensor} [\alpha, \beta] / . \{D \rightarrow 4\}]
a^{\beta} k^{\alpha} - a^{\alpha} k^{\beta}
-\epsilon^{\mu\nu}\overline{a}\overline{k}
NewMomentum[p_] := Module[{},
    Print[Map[ToExpression,
         \{p <> v[\alpha] = Pair[LorentzIndex[\alpha,D],Momentum[" <> p <> ",D]]",
           p \leftrightarrow v2=Contract[" \leftrightarrow p \leftrightarrow v[\alpha]" \leftrightarrow p \leftrightarrow v[\alpha]]"
```

```
"k" <> p <>" =Contract[kv[\alpha]" <> p <> "v[\alpha]]",
      "F" <> p <> "v[\alpha_] = Pair[LorentzIndex[\alpha, D], Momentum[F" <math><> p <> ", D]]",
      "FF" <> p <> "v[\alpha] = Pair[LorentzIndex[\alpha, D], Momentum[FF" <> p <> ", D]]",
      "FD"<>p<>"v[α_] = Pair[LorentzIndex[α, D], Momentum[FD"<>p<>", D]]",
      "a" <> p <> "=Contract[av[\alpha]" <> p <> "v[<math>\alpha]]",
      "ScalarProduct[k, F" <> p <> "] = 0",
      "ScalarProduct[k, FF" <> p <> "] = 0",
      "ScalarProduct[a, FF" <> p <> "] = 0",
      "ScalarProduct[a, F"<>p<>"] = -av2 Contract[kv[\mu] "<>p<>"v[\mu]]",
      "ScalarProduct[k, FD" <> p <> "] = 0",
      "ScalarProduct[a, FD" <> p <> "] = 0",
      "ScalarProduct[F" <> p <> ", F" <> p <> "] = -x" <> p <> "^2*m^6/e^2",
      "ScalarProduct[FD" <> p <> ", FD" <> p <> "] = -x" <> p <> "^2*m^6/e^2",
      "ScalarProduct["<>p<>", FF"<>p<>"] = \chi"<>p<>"^2*m^6/e^2",
      "ScalarProduct["<>p<>", FD"<>p<>"] = 0",
      "ScalarProduct["<>p<>", F"<>p<>"] = 0",
      "ScalarProduct[F" <> p <> ", FD" <> p <> "] = 0",
      "ScalarProduct[FF" <> p <> ", FF" <> p <> "] = 0",
      "ScalarProduct[F" <> p <> ", FF" <> p <> "] = 0",
      "ScalarProduct[FD" <> p <> ", FF" <> p <> "] = 0"
    }]];
 FieldSubstitutions = Join[FieldSubstitutions,
    Map[ToExpression,
      {"Contract[Ft[\mu, \nu] "<> p <> "<math>\nu[\nu]] \rightarrow F"<> p <> "<math>\nu[\mu]",
       "Contract[FDt[\mu, \nu] "<>p<>"\nu[\nu]] \rightarrow FD"<>p<>"\nu[\mu]",
       "Contract[FFt[\mu, \nu] "\langle \rangle p\langle \rangle "\nu[\nu]] -> FF"\langle \rangle p\langle \rangle "\nu[\mu]",
       "Contract[Ft[\mu, \nu] F" \Leftrightarrow p \Leftrightarrow "\nu[\nu]] \rightarrow FF" \Leftrightarrow p \Leftrightarrow "\nu[\mu]",
       "Contract[FDt[\mu, \nu] FD" \Leftrightarrow p \Leftrightarrow "\nu[\nu]] \Rightarrow FF" \Leftrightarrow p \Leftrightarrow "\nu[\mu]",
       "FF" <> p <> "V[\mu] FF" <> p <> "V[v] -> \chi" <> p <> "^2*m^6/e^2 FFt[\mu, \nu]",
       "Contract[FFt[\alpha, \beta] "<>p<>"v[\alpha] "<>p<> "v[\beta]] -> \chi"<>p<> "^2*m^6/e^2",
       "Contract[FFt[\mu, \nu] FF" \langle \rangle p \langle \rangle "v[\nu]] -> 0",
       "Contract[FFt[\mu, \nu] "<>p<>"v[\mu] F"<>p<>"v[\nu]] -> 0",
       "Contract[FFt[\mu, \nu] "\langle \ranglep\langle \rangle"v[\mu] FF"\langle \ranglep\langle \rangle"v[\nu]] -> 0",
       "Contract[FDt[\mu_, \nu] F" <> p <> "\nu[\nu]] -> 0",
       "Contract[FDt[\mu, \nu] FF" \langle \rangle p \langle \rangle "\nu[\nu]] \rightarrow 0",
       "Contract[FFt[\mu, \nu] "<>p<>"\nu[\mu] k\nu[\nu]] -> 0",
       "Contract[Ft[\mu, \nu] FD" \langle \rangle p \langle \rangle "\nu[\nu]] \rightarrow 0",
       "Contract[FFt[\mu, \nu] FD" \langle \rangle p \langle \rangle "\nu[\nu]] -> 0",
       "Contract[FDt[\mu, \nu] F" \langle \rangle p \langle \rangle "\nu[\nu]] \rightarrow 0",
       "Contract[FDt[\mu, \nu] FF" \langle \rangle p \langle \rangle "\nu[\nu]] \rightarrow 0",
       "Contract[Ft[\mu, \nu] FF" \leftrightarrow p \leftrightarrow "\nu[\nu]] \rightarrow 0"}]
  ];
]
```

```
4 definitions.nb
```

```
NewCoordinate[x ] := Module[{},
  Print[Map[ToExpression,
      \{x <> v[\alpha] = Pair[LorentzIndex[\alpha,D],Momentum[" <> x <> ",D]]",
       x <> "v2 = Contract[" <> x <> "v[\alpha] " <> x <> "v[\alpha]]",
       "k" <> x <> " = Contract[kv[\alpha] " <> x <> "v[\alpha]]",
       "a" <> x <> " = Contract[av[\alpha] " <> x <> "v[\alpha]]",
       "F" <> x <> "v[\alpha] = Pair[LorentzIndex[\alpha, D], Momentum[F" <> x <> ", D]]",
       "FF" <> x <> "v[α_] = Pair[LorentzIndex[α, D], Momentum[FF" <> x <> ", D]]",
       "FD" <> x <> "v[\alpha] = Pair[LorentzIndex[\alpha, D], Momentum[FD" <> x <> ", D]]",
       "ScalarProduct[k, "<>x<>"] = k"<>x,
       "ScalarProduct[k, F" <> x <> "] = 0",
       "ScalarProduct[k, FF" <> x <> "] = 0",
       "ScalarProduct[a, FF" <> x <> "] = 0",
       "ScalarProduct[a, F"<>
        x \leftrightarrow "] = -av2 Contract[kv[\mu] " \leftrightarrow x \leftrightarrow "v[\mu]]",
       "ScalarProduct[k, FD" <> x <> "] = 0",
       "ScalarProduct[a, FD" <> x <> "] = 0",
       "ScalarProduct[F" <>
        x <> ", F" <> x <> "] = -\xi^2 k" <> x <> "^2*m^2/e^2",
       "ScalarProduct[FD" <> x <> ", FD" <> x <> "] = -\xi^2 k" <> x <> "^2*m^2/e^2",
       "ScalarProduct["<>x<>", FF"<>x<>"] = ξ^2 k"<>x<>"^2*m^2/e^2",
       "ScalarProduct["<>x<>", FD"<>x<>"] = 0",
       "ScalarProduct[" <> x <> ", F" <> x <> "] = 0",
       "ScalarProduct[F" <> x <> ", FD" <> x <> "] = 0",
       "ScalarProduct[FF" <> x <> ", FF" <> x <> "] = 0",
       "ScalarProduct[F" <> x <> ", FF" <> x <> "] = 0",
       "ScalarProduct[FD" <> x <> ", FF" <> x <> "] = 0"
     }]];
  FieldSubstitutions = Join[FieldSubstitutions,
     Map[ToExpression,
       {"Contract[Ft[\mu_{},\nu] "<> x <> "v[\nu]]\rightarrow F"<> x <> "v[\mu]",
        "Contract[FDt[\mu,\nu] "\langle \rangle X \langle \rangle "\nu[\nu]]\rightarrowFD" \langle \rangle X \langle \rangle "\nu[\mu]",
         "Contract[FFt[\mu_,\nu] "<> x <> "<math>\nu[\nu]]\rightarrowFF"<> x <> "<math>\nu[\mu]",
         "Contract[Ft[\mu,\nu] F" \langle \rangle x \langle \rangle "\nu[\nu]]\rightarrowFF" \langle \rangle x \langle \rangle "\nu[\mu]",
         "Contract[FDt[\mu,\nu] FD" <> x <> "\nu[\nu]] \rightarrow FF" <> x <> "\nu[\mu]",
        "FF" <> x <> "v[\mu] FF" <> x <> "v[v] \rightarrow \xi^2 k" <> x <> "^2 *m^2/e^2 FFt[\mu, v]",
        "Contract[FFt[\alpha,\beta] "<> x <> "v[<math>\alpha] "<> x <> "v[<math>\beta]] \rightarrow \xi^2 k" <> x <> "^2*m^2/e^2",
         "Contract[FFt[\mu,\nu] F" <> x <> "\nu[\nu]] \rightarrow0",
        "Contract[FFt[\mu,\nu] FF" \langle \rangle X \langle \rangle "\nu[\nu]] \rightarrow0",
         "Contract[FFt[\mu,\nu] "<> x <> "v[<math>\mu] F"<> x <> "v[<math>\nu]]\rightarrow 0",
         "Contract[FFt[\mu,\nu] "<> x <> "v[<math>\mu] FF"<> x <> "v[<math>\nu]] \rightarrow 0",
         "Contract[FDt[\mu,\nu] F" \langle \rangle x \langle \rangle "v[\nu]]\rightarrow0",
         "Contract[FDt[\mu,\nu] FF" \langle \rangle x \langle \rangle "\nu[\nu]]\rightarrow0",
```

```
"Contract[FFt[\mu,\nu] "<> x <> "v[<math>\mu] kv[\nu]]\rightarrow0",
                 "Contract[Ft[\mu,\nu] FD" \langle \rangle x \langle \rangle "\nu[\nu]]\rightarrow0",
                 "Contract[FFt[\mu_,\nu] FD" \langle \rangle x \langle \rangle "\nu[\nu]]\rightarrow0",
                 "Contract[FDt[\mu,\nu] F" \langle \rangle x \langle \rangle "v[\nu]]\rightarrow0",
                 "Contract[FDt[\mu,\nu] FF" \langle \rangle x \langle \rangle "\nu[\nu]]\rightarrow0",
                 "Contract[Ft[\mu_,\nu] FF" \langle \rangle x \langle \rangle "v[\nu]]\rightarrow0"}]];
   ]
(*Preparing symbolic substitutions for thriple \gamma-
   matrix combinations and recollecting F-tensors from vectors a[\mu] and k[\mu]*)
TripleGamma = {DiracGamma[Momentum[a_, D], D].
           DiracGamma[Momentum[b_, D], D].DiracGamma[Momentum[c_, D], D] →
        Contract[Pair[LorentzIndex[α1, D], Momentum[a, D]] Pair[LorentzIndex[α2, D],
                Momentum[b, D]] Pair[LorentzIndex[\alpha3, D], Momentum[c, D]] (MTD[\alpha1, \alpha2] GAD[\alpha3] +
                   \mathsf{MTD}[\alpha 2, \alpha 3] \; \mathsf{GAD}[\alpha 1] \; - \; \mathsf{MTD}[\alpha 1, \alpha 3] \; \mathsf{GAD}[\alpha 2] \; - \; \mathsf{i} \; \mathsf{LCD}[\beta, \alpha 1, \alpha 2, \alpha 3] \; \mathsf{GAD}[\beta] \; . \; \mathsf{GA}[5]) ] \}
EpsToF = \{Eps[LorentzIndex[\alpha_{p}, D], Momentum[a, D], Momentum[k, D], Momentum[V_{p}, D], Momentum[v_{p}
           Dimension \rightarrow D] \rightarrow -Contract[FDt[\alpha, \beta] Pair[LorentzIndex[\beta, D], Momentum[V, D]]],
     Eps[LorentzIndex[\alpha_{-}, D], Momentum[k, D], Momentum[a, D], Momentum[V_, D],
           Dimension → D] → Contract[FDt[\alpha, \beta] Pair[LorentzIndex[\beta, D], Momentum[V, D]]],
     Eps[LorentzIndex[α_, D], Momentum[V_, D], Momentum[a, D], Momentum[k, D],
           Dimension \rightarrow D] \rightarrow - Contract[FDt[\alpha, \beta] Pair[LorentzIndex[\beta, D], Momentum[V, D]]],
     Eps[LorentzIndex[\alpha_{-},D], Momentum[V_{-},D], Momentum[k,D], Momentum[a,D],\\
           Dimension → D] → Contract[FDt[α, β] Pair[LorentzIndex[β, D], Momentum[V, D]]],
     Eps[LorentzIndex[\alpha_, D], Momentum[a, D], Momentum[V_, D], Momentum[k, D],
           Dimension \rightarrow D] \rightarrow Contract[FDt[\alpha, \beta] Pair[LorentzIndex[\beta, D], Momentum[V, D]]],
     Eps[LorentzIndex[\alpha_{-}, D], Momentum[k, D], Momentum[V_, D], Momentum[a, D],
           Dimension → D] → -Contract[FDt[\alpha, \beta] Pair[LorentzIndex[\beta, D], Momentum[V, D]]]}
akToF = {DiracGamma[Momentum[k, D], D]    Pair[Momentum[a, D], Momentum[x, D]] -
           DiracGamma[Momentum[a, D], D] Pair[Momentum[k, D], Momentum[x, D]] →
        DiracGamma[Momentum[Fx, D], D],
      - DiracGamma[Momentum[k, D], D] Pair[Momentum[a, D], Momentum[x, D]] +
           DiracGamma[Momentum[a, D], D] Pair[Momentum[k, D], Momentum[x, D]] →
        -DiracGamma[Momentum[Fx, D], D],
     DiracGamma[Momentum[a, D], D].DiracGamma[Momentum[k, D], D] \rightarrow \pm/2 \sigma F,
     DiracGamma[Momentum[k, D], D].DiracGamma[Momentum[a, D], D] \rightarrow -i/2 \sigma F
\left\{ (\gamma \cdot \mathbf{a}_{-}).(\gamma \cdot \mathbf{b}_{-}).(\gamma \cdot \mathbf{c}_{-}) \rightarrow -i \, \gamma^{\beta}.\overline{\gamma}^{5} \, \epsilon^{\beta \, a \, b \, c} + (a \cdot b) \, \gamma \cdot c - (a \cdot c) \, \gamma \cdot b + \gamma \cdot a \, (b \cdot c) \right\}
\{\epsilon^{\alpha_-\,a\,k\,V_-}\to -\mathrm{FD}(\alpha,\ V),\ \epsilon^{\alpha_-\,k\,a\,V_-}\to \mathrm{FD}(\alpha,\ V),\ \epsilon^{\alpha_-\,V_-\,a\,k}\to -\mathrm{FD}(\alpha,\ V),
    \epsilon^{\alpha_{-}V_{-}ka} \to FD(\alpha, V), \epsilon^{\alpha_{-}aV_{-}k} \to FD(\alpha, V), \epsilon^{\alpha_{-}kV_{-}a} \to -FD(\alpha, V)
\left\{ (a \cdot x) \ \gamma \cdot k - \gamma \cdot a \ (k \cdot x) \rightarrow \gamma \cdot \operatorname{Fx}, \ \gamma \cdot a \ (k \cdot x) - (a \cdot x) \ \gamma \cdot k \rightarrow -(\gamma \cdot \operatorname{Fx}), \ (\gamma \cdot a).(\gamma \cdot k) \rightarrow \frac{\iota \ \sigma \operatorname{F}}{2}, \ (\gamma \cdot k).(\gamma \cdot a) \rightarrow -\frac{\iota \ \sigma \operatorname{F}}{2} \right\}
```

```
antiTripleGamma =
 \{DiracGamma[LorentzIndex[\beta_, D], D].DiracGamma[5] Eps[LorentzIndex[\beta_, D], \}
       Momentum[a_, D], Momentum[b_, D], Momentum[c_, D], Dimension \rightarrow D] \rightarrow
    -i Contract[Pair[LorentzIndex[α1, D], Momentum[a, D]]
        Pair[LorentzIndex[α2, D], Momentum[b, D]]
        Pair[LorentzIndex[\alpha3, D], Momentum[c, D]] (MTD[\alpha1, \alpha2] GAD[\alpha3] +
           MTD[\alpha 2, \alpha 3] GAD[\alpha 1] - MTD[\alpha 1, \alpha 3] GAD[\alpha 2] - DiracGamma[LorentzIndex[\alpha 1, D], D].
            DiracGamma[LorentzIndex[α2, D], D].DiracGamma[LorentzIndex[α3, D], D])]}
\left\{\gamma^{\beta_-}.\overline{\gamma^5}\,\epsilon^{\beta_-\,a_-\,b_-\,c_-}\rightarrow -i\left((a\cdot b)\,\gamma\cdot c-(a\cdot c)\,\gamma\cdot b+\gamma\cdot a\,(b\cdot c)-(\gamma\cdot a).(\gamma\cdot b).(\gamma\cdot c)\right)\right\}
Ep[z_, p_] := {
  1 - e/2/Pair[Momentum[k, D], Momentum[p, D]]
     Pair[Momentum[k, D], Momentum[z, D]] DiracSlash[k, a, Dimension → D],
  - Pair[Momentum[z, D], Momentum[p, D]] + e Pair[Momentum[a, D], Momentum[p, D]] / 2 /
       Pair[Momentum[k, D], Momentum[p, D]] (Pair[Momentum[k, D], Momentum[z, D]])^2+
    e^2 av2 / 6 / Pair [Momentum[k, D], Momentum[p, D]]
      (Pair[Momentum[k, D], Momentum[z, D]]) ^3
 }
EpC[z_, p_] := {
  1 - e / 2 / Pair [Momentum[k, D], Momentum[p, D]]
     Pair[Momentum[k, D], Momentum[z, D]] DiracSlash[a, k, Dimension → D],
  - (- Pair[Momentum[z, D], Momentum[p, D]] +
       e Pair[Momentum[a, D], Momentum[p, D]] / 2 / Pair[Momentum[k, D], Momentum[p, D]]
        (Pair[Momentum[k, D], Momentum[z, D]])^2+
      e^2 av2/6/Pair[Momentum[k, D], Momentum[p, D]]
        (Pair[Momentum[k, D], Momentum[z, D]]) ^3)
DiracElectronPropagatorXRepr[x_, X_, s_] := Module[{s1},
   {DiracSimplify[
       Contract[DotSimplify[(1/2/m/s1 GAD[\alpha]) (Pair[Momentum[x, D], LorentzIndex[
                     \alpha, D]] - s1 e (kv[\alpha] Pair[Momentum[a, D], Momentum[x, D]] -
                       av[α] Pair[Momentum[k, D], Momentum[x, D]]) +
                   s1^2/3 e^2 (-av2 Pair[Momentum[k, D], Momentum[x, D]] kv[\alpha]) + 1).
            (1 + e s1 DiracSlash[a, k, Dimension \rightarrow D]) /. {s1 \rightarrow s/m^2}]]],
     Exp[-IPi/2(D/2-1)] \Lambda^{(4-D)/2^{D/Pi^{(D/2)}} *m^{(D-1)/s^{(D/2)}},
     -s-m^2 Pair [Momentum[x, D], Momentum[x, D]] /4/s-
       s/12 e^2/m^2 Contract[Pair[Momentum[x, D], LorentzIndex[α, D]]
           FTensor[\alpha, \beta] FTensor[\beta, \gamma] Pair[Momentum[x, D], LorentzIndex[\gamma, D]]] +
       e Pair[Momentum[a, D], Momentum[x, D]] Pair[Momentum[k, D], Momentum[X, D]]
    \} /. \{av2 \rightarrow -m^2 \xi^2 / e^2\}
```

```
PhotonPropagator0[z_, t_, \mu_, \nu_] :=
 \{\mathsf{MTD}[\mu, \nu],
   - Exp[-IPi/2(D/2-1)] \Lambda^{(4-D)/2^{D/Pi^{(D/2)}} *m^{(D-2)/t^{(D/2)}},
   -m^2 Pair[Momentum[z, D], Momentum[z, D]] /4/t}
PhotonPropagatorExactXRepr[z_, t_, \mu_, \nu_] := Module[{TFzFz\mu\nu, TFDzFDz\mu\nu},
  TFzFz\mu\nu = Expand[Contract[
       \mathsf{Ft}[\mu, \alpha] \mathsf{Pair}[\mathsf{Momentum}[\mathsf{z}, \mathsf{D}], \mathsf{LorentzIndex}[\alpha, \mathsf{D}]] \mathsf{Ft}[\nu, \beta] \mathsf{Pair}[\mathsf{Momentum}[\mathsf{z}, \mathsf{D}],
           LorentzIndex[\beta, D]] /. {Ft[\alpha_, \beta_] \rightarrow kv[\alpha] av[\beta] - kv[\beta] av[\alpha]}
     11;
  TFDzFDz\mu\nu = Expand[Contract[
       -Pair[Momentum[z, D], Momentum[z, D]] FFt[\mu, \nu] + FFt[\mu, \alpha] Pair[Momentum[z, D],
             LorentzIndex[α, D]] Pair[Momentum[z, D], LorentzIndex[ν, D]] +
          FFt[ν, α] Pair[Momentum[z, D], LorentzIndex[α, D]] Pair[Momentum[z, D],
             LorentzIndex[\mu, D]] - TFzFz\mu\nu - Pair[Momentum[z, D], LorentzIndex[\alpha, D]]
           Pair[Momentum[z, D], LorentzIndex[\beta, D]] FFt[\alpha, \beta] MTD[\mu, \nu] /.
        \{Ft[\alpha_{-}, \beta_{-}] \rightarrow kv[\alpha] \text{ av}[\beta] - kv[\beta] \text{ av}[\alpha], FFt[\alpha_{-}, \beta_{-}] \rightarrow -\text{av2} \text{ kv}[\alpha] \text{ kv}[\beta]\}
        (*/.{av2\rightarrow -m^2 \xi^2/e^2}*)
     ]];
   \{MTD[\mu, \nu] * JO[m^{(-2)}t, \xi Pair[Momentum[k, D], Momentum[z, D]]/2/t] +
      (-2itkv[\mu]kv[\nu]/m^2/Pair[Momentum[z, D], Momentum[k, D]]^2+
          e^2 TFzFz\mu\nu/m^2/\xi^2/Pair[Momentum[z, D], Momentum[k, D]]^2
       J1[m^{(-2)}t, \xi Pair[Momentum[k, D], Momentum[z, D]]/2/t]+
      (-2itkv[\mu]kv[\nu]/m^2/Pair[Momentum[z, D], Momentum[k, D]]^2+
          e^2 TFDzFDz\mu\nu/m^2/\xi^2/Pair[Momentum[z, D], Momentum[k, D]]^2
       J2[m^{(-2)}t, \xi Pair[Momentum[k, D], Momentum[z, D]]/2/t],
    Exp[-IPi/2(D/2-2)] \Lambda^{(4-D)/2^{D/Pi^{(D/2)}} *m^{(D-2)/t^{(D/2)}/(2Pi)}
    -m^2 Pair[Momentum[z, D], Momentum[z, D]] /4/t}]
```

Uncomment to see examples

```
(*uncomment to see example*)
(*Contract[DiracGamma[LorentzIndex[\mu,D],D].GA[5]FDxv[\mu]/.
       \{FDxv[\mu] \rightarrow LCD[\mu, \alpha1, \alpha2, \alpha3]xv[\alpha1]kv[\alpha2]av[\alpha3]\}
    %/.antiTripleGamma
    %/.TripleGamma*)
(*NewMomentum["p"]
 NewCoordinate["x"]
 FieldSubstitutions
 Expand[Contract[Ft[\mu,\alpha]xv[\alpha]Ft[\nu,\beta]xv[\beta]]/.FieldSubstitutions/.
    \{Fxv[\alpha] \rightarrow kv[\alpha] \ ax-av[\alpha] \ kx\}\}
```

```
(*uncomment to see examples*)
(*NewCoordinate["o"]
NewCoordinate["0"]*)
(*Ep[x,p]
 EpC[y,q]*)
(*DiracElectronPropagatorXRepr[ov,Ov,s]
 DiracElectronPropagatorXRepr1[0,0,s]*)
(*{\tt PhotonPropagator0}\,[{\tt x}\,,{\tt t}\,,{\tt \lambda}\,,{\tt \delta}]\,*)
(*NewCoordinate["z"]
{\tt PhotonPropagatorExact[z,t,\mu,\nu]*)}
```