B.B.14. Transformation

Sometimes recurrences cannot be solved using the aforemetioned methods. For example, consider the following problem:

$$T(n) = T(\sqrt{n}) + n$$

$$T(n) = T\left(\frac{n}{2}\right) + n$$

In this problem, many recurrences may involve terms that are not in the fixed range of n. That is, the recurrence equation may have powers, square roots, ceilings, floor or logarithms.

Mostly non — linear recurrence equations involve powers.

It is necessary to convert a recurrence equation into a familiar form so that it can be solved. By applying some transformations involving logarithms, multiplicative terms, or other algebraic manipulations to a recurrence equation, it can be converted into the standard form.

The non — linear recurrence equations that are amenable to these kinds of transformations are called pseudo — nonlinear recurrences.
