Polynomial Reduction — Solving Non — homogeneous Equations

For a non — homogeneous function, f(n) is not zero in the general equation. Hence, the characteristic non — homogeneous form can be expressed as follows:

$$a_0t_n + a_1t_{n-k} + \cdots + a_kt_{n-1} = b^np(n)$$

Here b is a constant and p(n) is a polynomial . The characteristic equation for this can be written as follows:

$$(a_0r^ka_1r^{k-1} + a_1r^{k-1} + \dots + a_k)(r-b)^{d+1} = 0$$

Here `d` is the degree of the polynomial.

The steps for solving a non - homogeneous equation are as follows:

1. Ignore f(n) and solve the homogoneous part assuming that f(n) = 0.

- 2. Restore f(n) and find a solution for the non -homogenous part that is rewritten as $(r-b)^{d+1}$ by ignoring the boundary conditions.
- 3. Form the general solution by considering all the roots obtained by performing steps 1 and 2.
- 4. Use boundary conditions to determine the specific solution for the given recurrence equation.
