

五、实验数据处理

实验 1. 激光双棱镜干涉

(1) 原始数据记录

i	1	2	3	4	5	6	7	8	9	10
x_i/mm	1.709	1.995	2.341	2.642	2.93	3.309	3.589	3.821	4.145	4.484
i	11	12	13	14	15	16	17	18	19	20
x_i/mm	4.711	5.071	5.312	5.641	5.957	6.245	6.534	6.841	7.155	7.438

	扩展光源	透镜成小像	透镜成大像
X/cm	129.4	66.45	99.71

	b/mm(小像)		b'/mm(大像)	
左	7.791	7.612	6.336	6.259
右	3.434	3.391	5.341	5.32

(2) 数据处理

用逐差法计算条纹间距 Δx :

$$\Delta x = \frac{\sum_{i=1}^{10} (x_{i+10} - x_i)}{10 \times 10} = 0.2994mm$$

计算波长 λ :

$$\bar{b} = \frac{b_{\text{正}} + b_{\text{反}}}{2} = \frac{(7.791 - 3.434) + (7.612 - 3.391)}{2} = 4.289$$

$$\bar{b}' = \frac{b'_{\text{正}} + b'_{\text{反}}}{2} = \frac{(6.336 - 5.341) + (6.259 - 5.32)}{2} = 0.967$$

$$S = 129.4 - 66.45 = 62.95cm$$

$$S' = 129.4 - 99.71 = 29.69cm$$

$$\lambda = \frac{\Delta \sqrt{\bar{b}\bar{b}'}}{S + S'} = 658.2nm$$

(3) 不确定度计算

Δx 的不确定度:

$10\Delta x$ 的 A 类不确定度:

$$u_a(10\Delta x) = \sqrt{\frac{\sum_{i=1}^{10} (10\Delta x_i - 10\bar{\Delta x})^2}{10 \times (10 - 1)}} = 4.372mm$$

$10\Delta x$ 的 B 类不确定度:

$$u_b(10\Delta x) = \frac{\Delta_{\text{仪}}}{\sqrt{3}} = \frac{0.01}{2 \times \sqrt{3}} = 0.00289mm$$

$10\Delta x$ 的不确定度:

$$u(10\Delta x) = \sqrt{u_a(10\Delta x)^2 + u_b(10\Delta x)^2} = 4.372mm$$

Δx 的不确定度:

$$\therefore u(\Delta x) = \frac{u(10\Delta x)}{10} = 0.4372mm$$

$$\frac{\Delta b}{b} = \frac{\Delta b'}{b} = 0.025$$

b 的不确定度:

$$u(b) = \frac{4.289 \times 0.025}{\sqrt{3}} = 0.06191$$

b' 的不确定度:

$$u(b') = \frac{0.967 \times 0.025}{\sqrt{3}} = 0.01396$$

S 的不确定度:

$$\Delta S = \Delta S' = 0.5cm$$

$$u(S + S') = \sqrt{2} \times 0.289 = 0.409cm$$

不确定度的合成:

$$\ln \lambda = \ln \Delta x + \frac{1}{2}(\ln b + \ln b') - \ln(S + S')$$

$$\frac{\ln \lambda}{\lambda} = \frac{\ln \Delta x}{\Delta x} + \frac{1}{2}\left(\frac{\ln b}{b} + \frac{\ln b'}{b'}\right) - \frac{\ln(S + S')}{S + S'}$$

$$\frac{u(\lambda)}{\lambda} = \sqrt{\left[\frac{u(\Delta x)}{\Delta x}\right]^2 + \frac{1}{4}\left[\frac{u(b)}{b}\right]^2 + \frac{1}{4}\left[\frac{u(b')}{b'}\right]^2 + \left[\frac{u(S + S')}{S + S'}\right]^2}$$