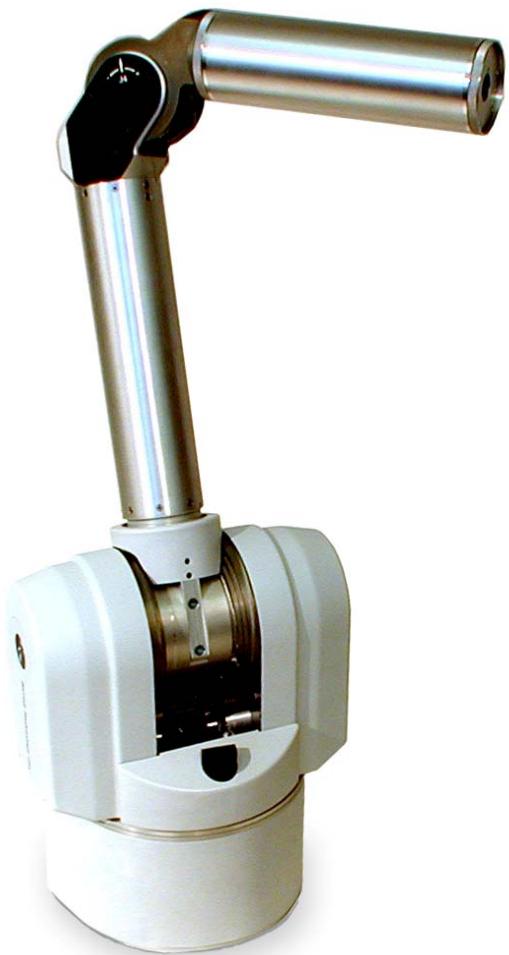


WAM™ Arm

Inertial Specifications



Barrett Technology® Inc.

Inertial Data for the WAM arm.

This document presents the inertial data for the WAM robotic arm (both the 4- and 7-dof version) in support of computed-torque control techniques. This draft document is a work in progress and not ready to be released for general use. Critical feedback is encouraged.

Relevance and Approximation of “Reflected Inertia.”

Except for (generally impractical) direct-drive robotic arms, all multi-serial-link robotic arms have drive inertias whose main effect may be approximated as “reflected” inertias. Reflected inertias are only approximations because of the assumption that there is no cross-product interaction between the spinning drive components and the (generally rotating) frames in which they are embedded. Reflected inertias are amplified by the square of the drive-reduction-ratios which generally range from 30 – 1,000 for practical robotic arms, so the reflected inertias generally range from 1,000 – 1,000,000, easily contributing most of the inertia of a robot. It is interesting to note that most text books on robotics deemphasize or dismiss the contributions of reflected inertias even though they generally overwhelm the inertias of the moving links. The WAM is unique is that its ratios were selected to balance the two inertia sources for optimal backdrivability and so both inertia sources are important.

Relevance and Treatment of “Differential” Mechanisms.

Also, many, if not most, robotic arms minimize moving inertia through the use of drive mechanisms called “differentials” which allow a pair of motors to be placed on one side of two perpendicular, intersecting axes, such as at shoulders and wrists, thereby minimizing the moving inertia of those motors. However, differentials also require special treatment when applying the approximation of “reflected” inertias because of the 2x2 motor-joint couplings, especially in the case of a high-backdrivability robot like the WAM. The couplings are given by the middle 2x2 transformations of Equation 1 for the shoulder, where $n_3 = 1.6800$, and Equation 2 for the wrist, where $n_6 = 1.0000$. For any pair of computed Joint torques the kinematically equivalent Motor torques are easily calculated as the sum of 2 polynomials with constant coefficients.

$$\begin{pmatrix} M\tau_1 \\ M\tau_2 \\ M\tau_3 \\ M\tau_4 \end{pmatrix} = \begin{pmatrix} -1/N_1 & 0 & 0 & 0 \\ 0 & 1/(2N_2) & -n_3/(2N_2) & 0 \\ 0 & -1/(2N_2) & -n_3/(2N_2) & 0 \\ 0 & 0 & 0 & -1/N_4 \end{pmatrix} \begin{pmatrix} J\tau_1 \\ J\tau_2 \\ J\tau_3 \\ J\tau_4 \end{pmatrix}$$

$$\begin{pmatrix} M\tau_5 \\ M\tau_6 \\ M\tau_7 \end{pmatrix} = \begin{pmatrix} 1/(2N_5) & -n_6/(2N_5) & 0 \\ 1/(2N_5) & n_6/(2N_5) & 0 \\ 0 & 0 & -1/N_7 \end{pmatrix} \begin{pmatrix} J\tau_5 \\ J\tau_6 \\ J\tau_7 \end{pmatrix}$$

Equation 2 - Wrist Joint-to-Motor torque transformations

Equation 1: Arm Joint-to-Motor torque transformations

The inertial data are calculated and employed separately for Frames and Drives:

1. Link (or Frame) inertias that are associated by Coordinate Frame number (0-7).
2. Drive inertias that are associated by Motor number (1-7).

How to Use the Inertia Data

Generally, motor torques are calculated in the following sequence:

1. Use the Frame inertias in the generalized robot equation. Apply either LaGrange or numerical Newton-Euler methods to translate desired robot forces and torques described in world Cartesian coordinates into equivalent, computed, joint torques.
2. For axes driven by differentials at the shoulder and wrist, apply the 2x2 torque transformations to translate the computed joint torques into the kinematically equivalent ideal motor torques.
3. For each ideal motor torque, calculate an adjusted motor torque required to provide the appropriate additional motor-output torque that overcomes the drive inertias.

Frame Inertias (and Related Mass Data)

See the data in Table 2 through Table 11 that correspond to the model graphics in Figure 4 through Figure 13. Some of the data in the tables is not necessary for most computed-torque calculations. All units are in kilograms and meters unless otherwise indicated. Generally, 13 values are important:

- Mass.
- X, Y, Z location of the Center of Mass.
- I_{xx} through I_{zz} (9 inertia-tensor values).

Drive Inertias

The motor-drive inertias are reported in Table 1. The data is derived from model geometries shown in Figure 14 through Figure 24. In these models, roller and ball bearings are generally separated into their stationary and moving components. The geometric information from these models is summarized in Table 23 along with the associated cable diameters and resulting intermediate and total drive ratios. The inertial data from these models, in which only one inertia tensor (bolded and underlined) value is relevant are given in Table 12 through Table 22. The additional inertia data can, for example, quantify corrections in the “reflected”-inertia assumptions though it is believed that these errors are well under 1%. Table 24 calculates the lumped pinion+cable inertia for each drive body and gives its equivalent inertia at the rotor end of the drive. Table 25 then combines the various drive-components for each motor-drive number.

Table 1 -- Drive Inertias for all WAM DOFs.

| Motor Drive Number | Total Drive Inertia at Rotor ($\text{kg}\cdot\text{m}^2$) | Drive Ratios | Total Reflected Inertia at Output ($\text{kg}\cdot\text{m}^2$) |
|--------------------|---|--------------|--|
| M1 | 0.00011631 | 42.00 | 0.205190 |
| M2 | 0.00011831 | 28.25 | 0.094428 |
| M3 | 0.00011831 | 28.25 | 0.094428 |
| M4 | 0.00010686 | 18.00 | 0.034628 |
| M5 | 0.00001685 | 9.48 | 0.001584 |
| M6 | 0.00001745 | 9.48 | 0.001641 |
| M7 | 0.00000142 | 14.93 | 0.000318 |

There are several one-page graphics that show an assembly (rigid body) with its associated coordinate frame and reports of mass parameters (mass, CG, and inertia tensor). Many of the components of the assembly are rendered as transparent to make clear what components are and are not included in the assembly. The numerical data is reported with the screen-shot graphic (to prevent any possibility of associating data to the wrong model). However the data is then repeated as text on the page following each graphic to allow easy copy-and-paste to a user's program.

Figure 1 shows the relationships between pulleys throughout the WAM. The present-day WAM has changed little since this artist's sketch was produced in 1987. In modern WAMs there are twin cables in each 2nd stage where the illustration shows only one cable, and the base motor has flipped orientation for better compactness. Figure 2 helps clarify the operation of the differential. It should be noted that the rotations of both differential-input pulleys are totally independent of the structure that supports them and (therefore) independent of the orientation of motor 4. One depends on the rotation of the M2 rotor and the other on the M3 rotor.

Figure 14 through Figure 16 are rigid-models required to calculate the "reflected" inertia of each of the 1st four DOFs of the WAM. In cases where there are sets of ball or roller bearings supporting a spinning body, we deleted ½ of the bearings as an approximation. For the elbow pulley-pinion, we can take an average of the case with all bearings installed (Figure 17) and the case of no bearings installed.

Cable, pinion, and pulley diameter/radius geometric data given in Table 23 enable calculation of all transmission ratios including intermediate ratios required to associate the "grenades" of Figure 15 and elbow-pulley-pinion set of Figure 17 with their associated joint inertias. The only ratio not given in this table (but given in this sentence) is the 1.68:1 ratio between the differential-input-pulley radii and the output pulley radius for calculating the J3 reflected inertias.

The (unreflected) motor rotor inertia (I_{zz} only) of Figure 14 is identical for each motor of the 1st four DOFs of the WAM = 0.00010569 kg·m². Also for all 4 DOFs, this rotor drives a pair of identical Stage-1 cables (Sava Cable Part Number SN2047 in Table 23) that have a mass of 0.013 kg each, or 0.026 kg total. The radius to the centerline of these cables where they are wrapped onto the scalloped pinion of the rotor is 0.009 m (9 mm), and since the entire length of cable translates as the same velocity one can lump the both cable masses at the 9-mm radius. In this case the inertia of the cables is (0.026 kg)*(0.009 m)² = 0.00000178 kg·m², adding <2% to the rotor inertia. The combined inertia is then = 0.00010747 kg·m².

At least for the 1st three WAM motor drives, the 1st and 2nd stages are coupled through a pair of “grenades” (Figure 15) that have an 11-mm radius pinion at one end driven by a stage-1 cable and a 33-mm-radius pulley at the other that drives a pair of stage-2 cables.

Cautions:

While the robot inertias are given here, several modeling errors are known to exist:

1. Machining, plastics, and composite-layup tolerances, especially important with thin (WAM) structures.
2. Ceramic, anodize/Teflon-surface-coating densities not accounted for.
3. Density variances from (allowed) tolerances in alloy contents, plastics, ceramics, and composites.
4. Inability to model (especially stranded) wires and cables in any practical manner, especially their paths as they flex.
5. Lack of knowledge of the proprietary assembly of components, such as bearings, wires, electrical cable assemblies, connectors, etc.
6. Treating ball and roller bearings as if they had only an inner and an outer race, when, in fact the balls themselves belong to neither, have individual (unmodelled) spins, and their CGs travel neither with the inner race nor the outer race. Ball retainers also move at the average ball velocity and not with either race.
7. Ball bearings in the WAM model are modeled as single parts, not as assemblies of races, balls, retainers, shields, and lubricants.
8. Modeling most threaded holes as if only the tap drill (but not the tap) has been applied.
9. Adhesives not modeled.
10. Lubricants not modeled and not clear how to associate velocities.

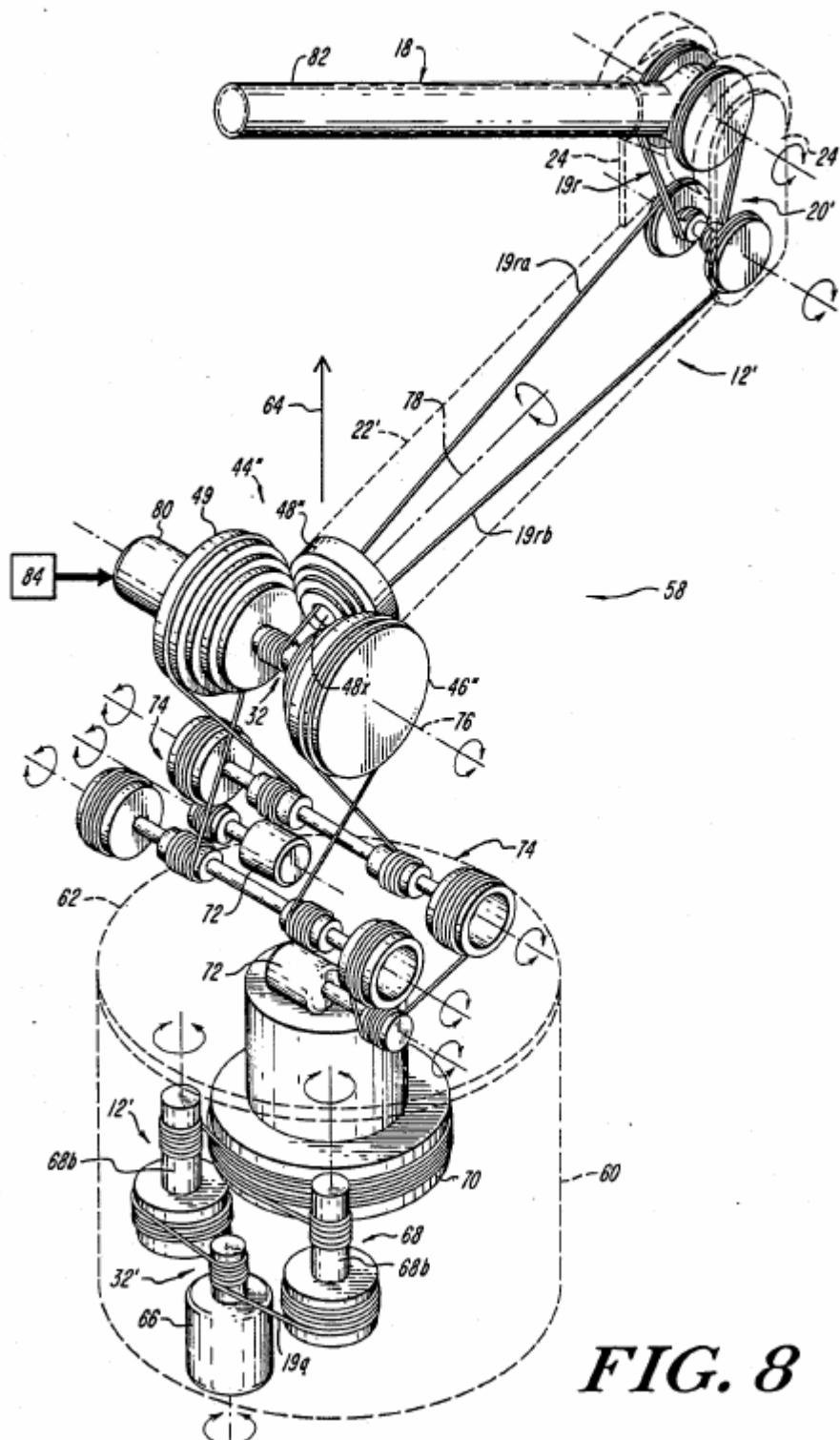
Background

Historical analysis of robotic arms (Paul, Craig, Spong, etc.) assumes a set of kinematically linked rigid bodies that can be assigned coordinate frames consistent with DH parameters. The analysis holds strictly only for direct-drive robots in which the rotor is integral with one rigid body and the stator is integral with an adjacent rigid body.

While direct-drive motors have outstanding inherent backdrivability with unity transmission ratios ($N=1$) they are far too massive and power-inefficient for the joint-torque demands of practical robots. So virtually all conventional robots use geared speed reducers in the form of harmonic drives with transmission ratios of $40 < N < 400$ to match the power capability (which varies as N^2) of practical motors with the speed and torque requirements of robotic arms. DH-kinematic analysis is not equipped to account for the spinning motor rotors, which impart significant momentum effects because of the amplified speeds involved.

It has been long proposed to treat the fast-spinning backdriven motor-rotor inertias as “reflected” inertias. However, it should be said that, while the “robot math” used to calculate computed

torques is precise for a direct-drive robot, even the precise calculation of reflected inertias does not and cannot account for some inertial interactions between fast spinning rotors and the velocities of the motor bodies containing those rotors. We are not aware of published analyses that have explored these errors.

U.S. Patent**Feb. 27, 1990****Sheet 5 of 5****4,903,536****FIG. 8****Figure 1 -- Artist's sketch of WAM cable drives.**

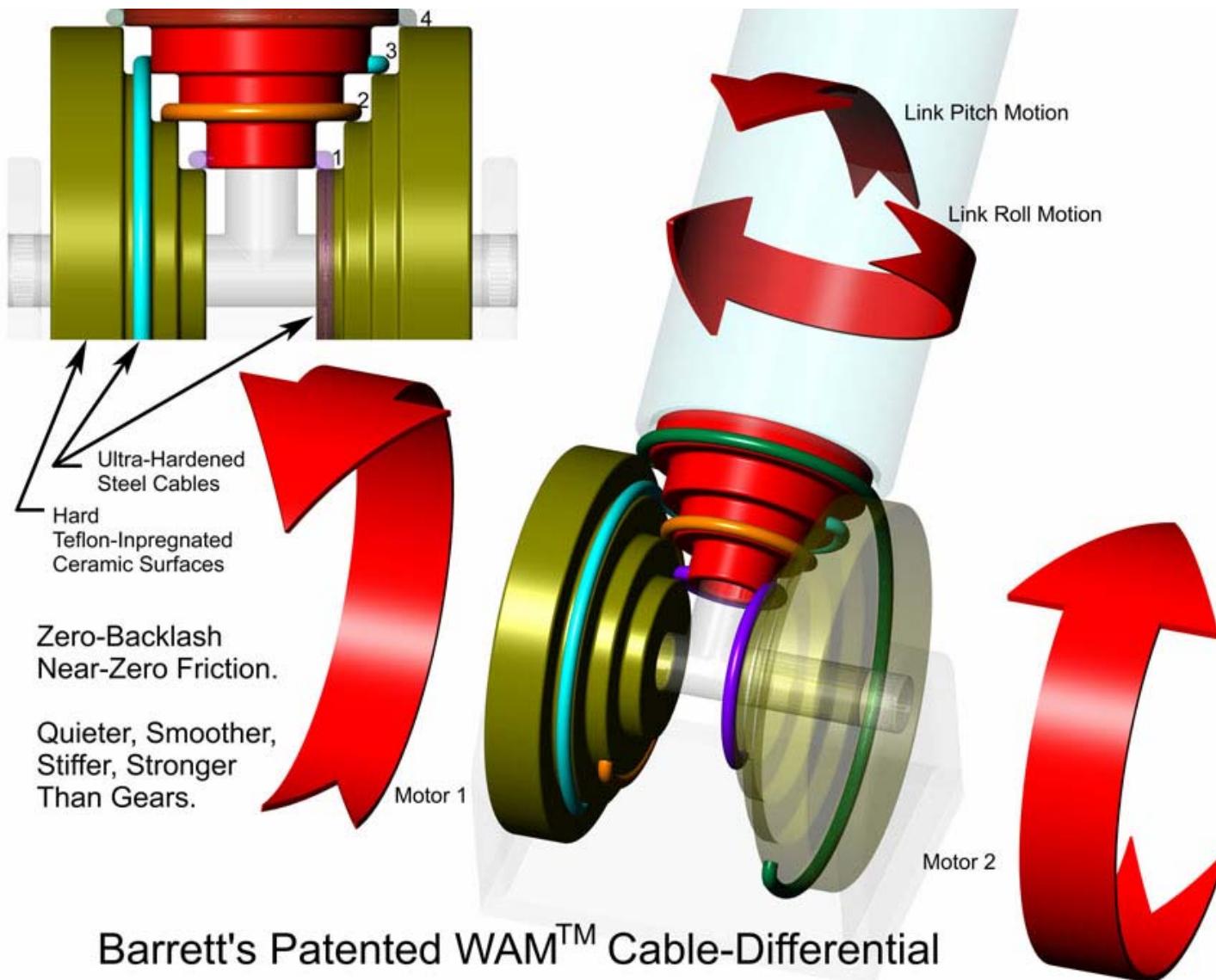


Figure 2 – Basic operation of the cabled differential mechanism used in the WAM shoulder. The WAM wrist differential operates similarly.

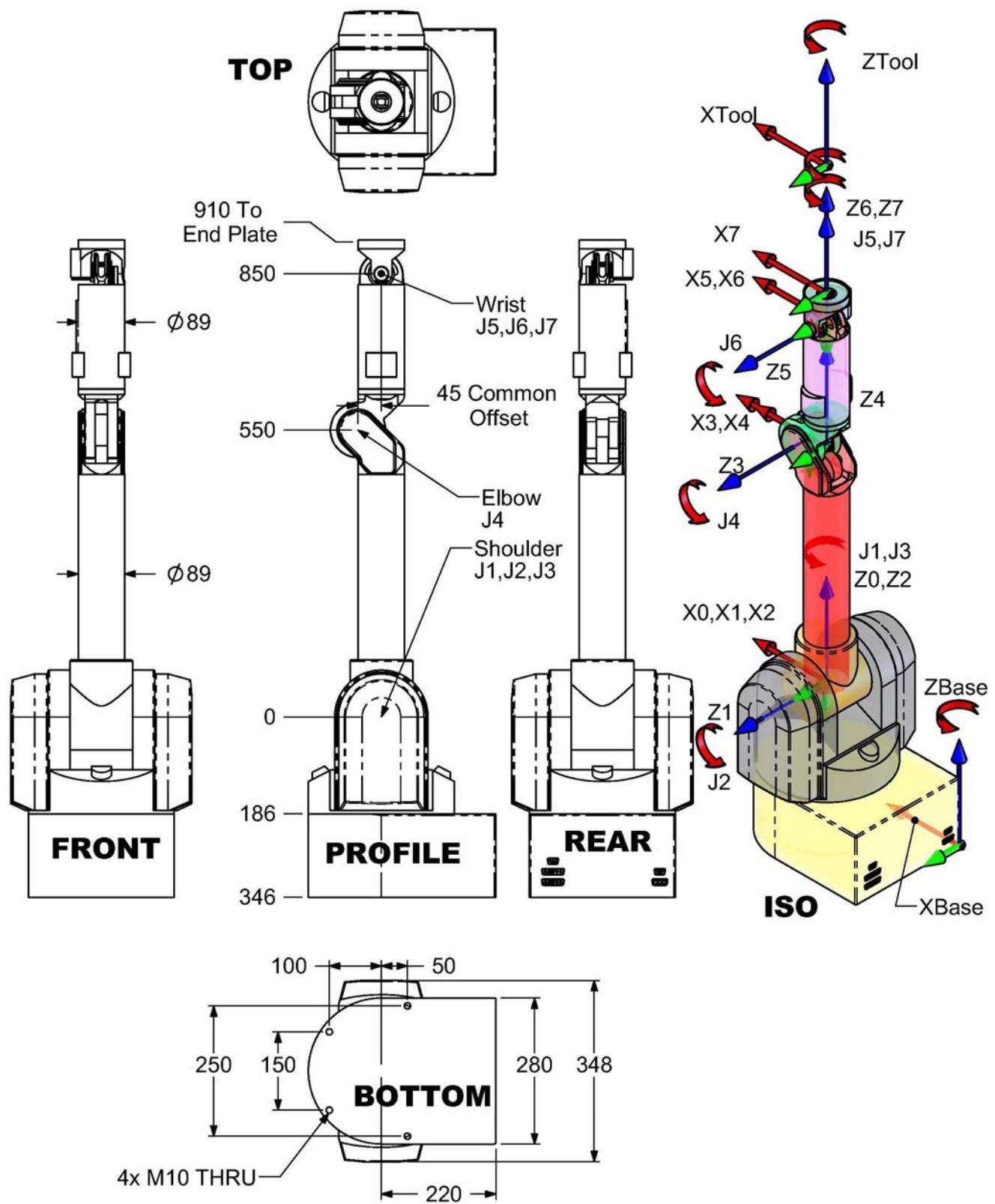


Figure 3 -- WAM Coordinate Frames.

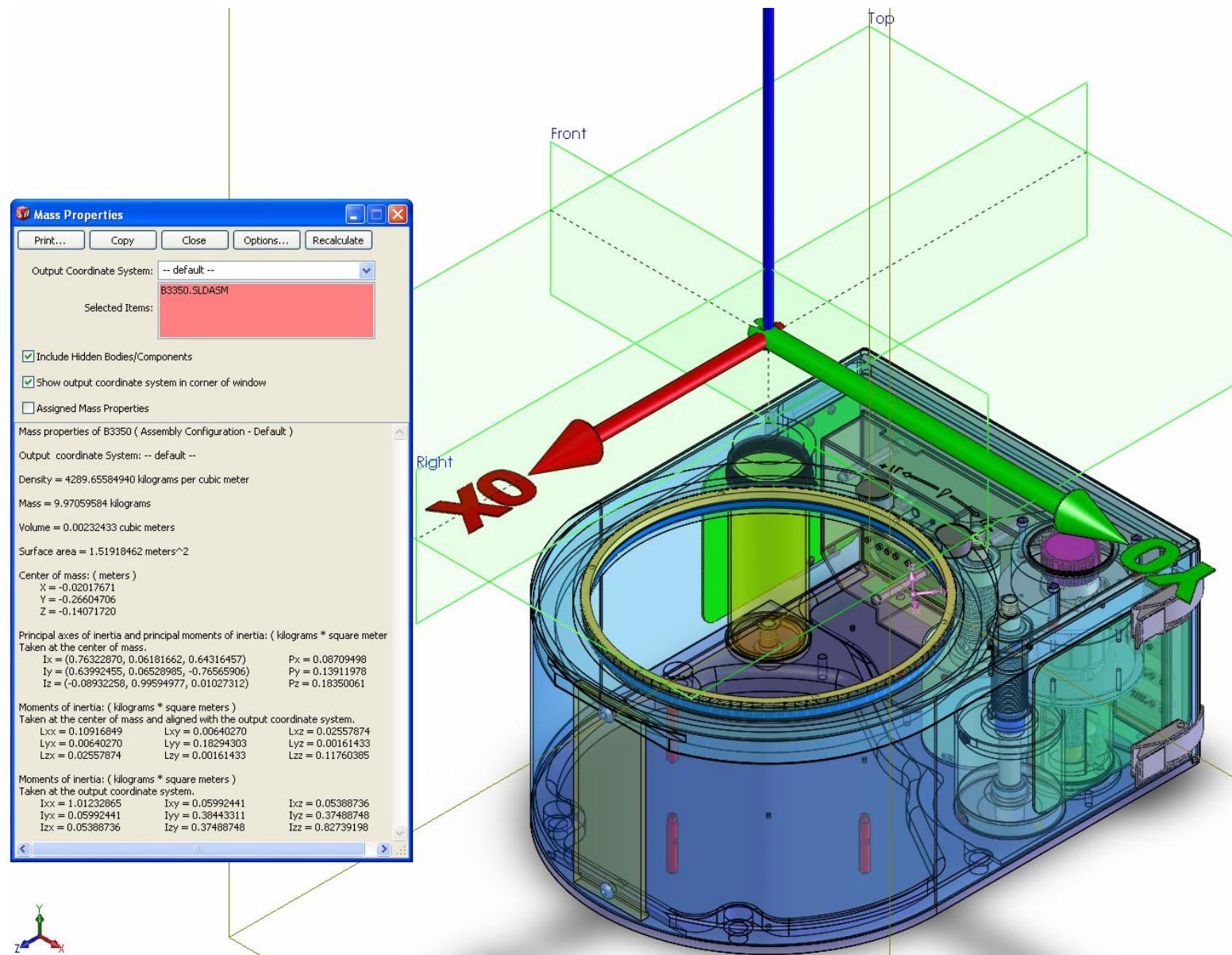


Figure 4 -- Frame 0 Inertia

Table 2 --Frame-0 Mass properties of B3350 (Assembly Configuration - Default)

Density = 4289.65584940 kilograms per cubic meter

Mass = 9.97059584 kilograms

Volume = 0.00232433 cubic meters

Surface area = 1.51918462 meters²

Center of mass: (meters)

$$X = -0.02017671$$

$$Y = -0.26604706$$

$$Z = -0.14071720$$

Principal axes of inertia and principal moments of inertia: (kilograms * square meters)

Taken at the center of mass.

$$I_x = (0.76322870, 0.06181662, 0.64316457) \quad P_x = 0.08709498$$

$$I_y = (0.63992455, 0.06528985, -0.76565906) \quad P_y = 0.13911978$$

$$I_z = (-0.08932258, 0.99594977, 0.01027312) \quad P_z = 0.18350061$$

Moments of inertia: (kilograms * square meters)

Taken at the center of mass and aligned with the output coordinate system.

$$L_{xx} = 0.10916849 \quad L_{xy} = 0.00640270 \quad L_{xz} = 0.02557874$$

$$L_{yx} = 0.00640270 \quad L_{yy} = 0.18294303 \quad L_{yz} = 0.00161433$$

$$L_{zx} = 0.02557874 \quad L_{zy} = 0.00161433 \quad L_{zz} = 0.11760385$$

Moments of inertia: (kilograms * square meters)

Taken at the output coordinate system.

$$I_{xx} = 1.01232865 \quad I_{xy} = 0.05992441 \quad I_{xz} = 0.05388736$$

$$I_{yx} = 0.05992441 \quad I_{yy} = 0.38443311 \quad I_{yz} = 0.37488748$$

$$I_{zx} = 0.05388736 \quad I_{zy} = 0.37488748 \quad I_{zz} = 0.82739198$$

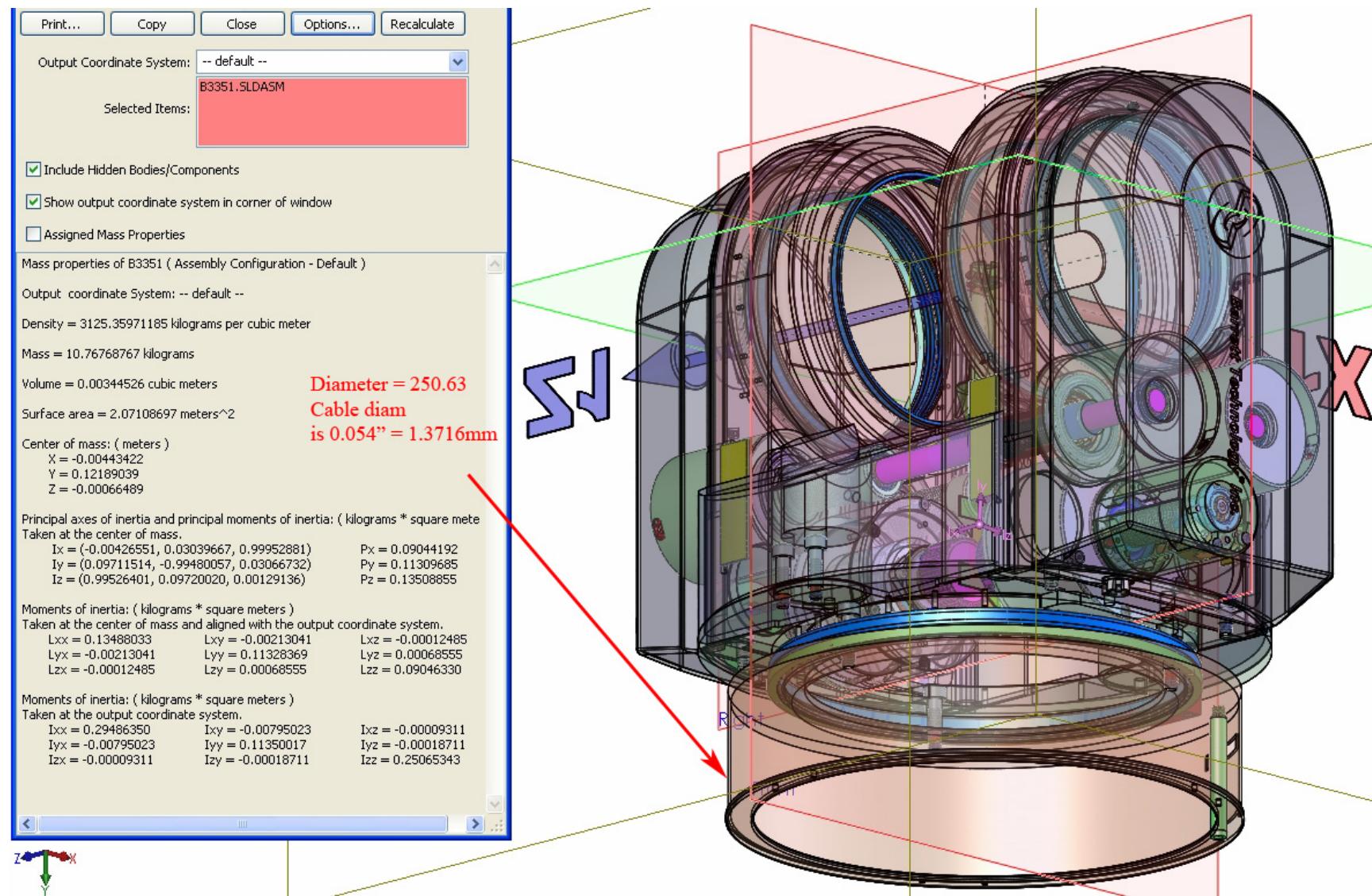


Figure 5 -- Frame-1 Inertia.

Table 3 --Frame-1 Mass properties of B3351 (Assembly Configuration - Default)

Density = 3125.35971185 kilograms per cubic meter

Mass = 10.76768767 kilograms

Volume = 0.00344526 cubic meters

Surface area = 2.07108697 meters²

Center of mass: (meters)

$$X = -0.00443422$$

$$Y = 0.12189039$$

$$Z = -0.00066489$$

Principal axes of inertia and principal moments of inertia: (kilograms * square meters)

Taken at the center of mass.

$$I_x = (-0.00426551, 0.03039667, 0.99952881) \quad P_x = 0.09044192$$

$$I_y = (0.09711514, -0.99480057, 0.03066732) \quad P_y = 0.11309685$$

$$I_z = (0.99526401, 0.09720020, 0.00129136) \quad P_z = 0.13508855$$

Moments of inertia: (kilograms * square meters)

Taken at the center of mass and aligned with the output coordinate system.

$$L_{xx} = 0.13488033 \quad L_{xy} = -0.00213041 \quad L_{xz} = -0.00012485$$

$$L_{yx} = -0.00213041 \quad L_{yy} = 0.11328369 \quad L_{yz} = 0.00068555$$

$$L_{zx} = -0.00012485 \quad L_{zy} = 0.00068555 \quad L_{zz} = 0.09046330$$

Moments of inertia: (kilograms * square meters)

Taken at the output coordinate system.

$$I_{xx} = 0.29486350 \quad I_{xy} = -0.00795023 \quad I_{xz} = -0.00009311$$

$$I_{yx} = -0.00795023 \quad I_{yy} = 0.11350017 \quad I_{yz} = -0.00018711$$

$$I_{zx} = -0.00009311 \quad I_{zy} = -0.00018711 \quad I_{zz} = 0.25065343$$

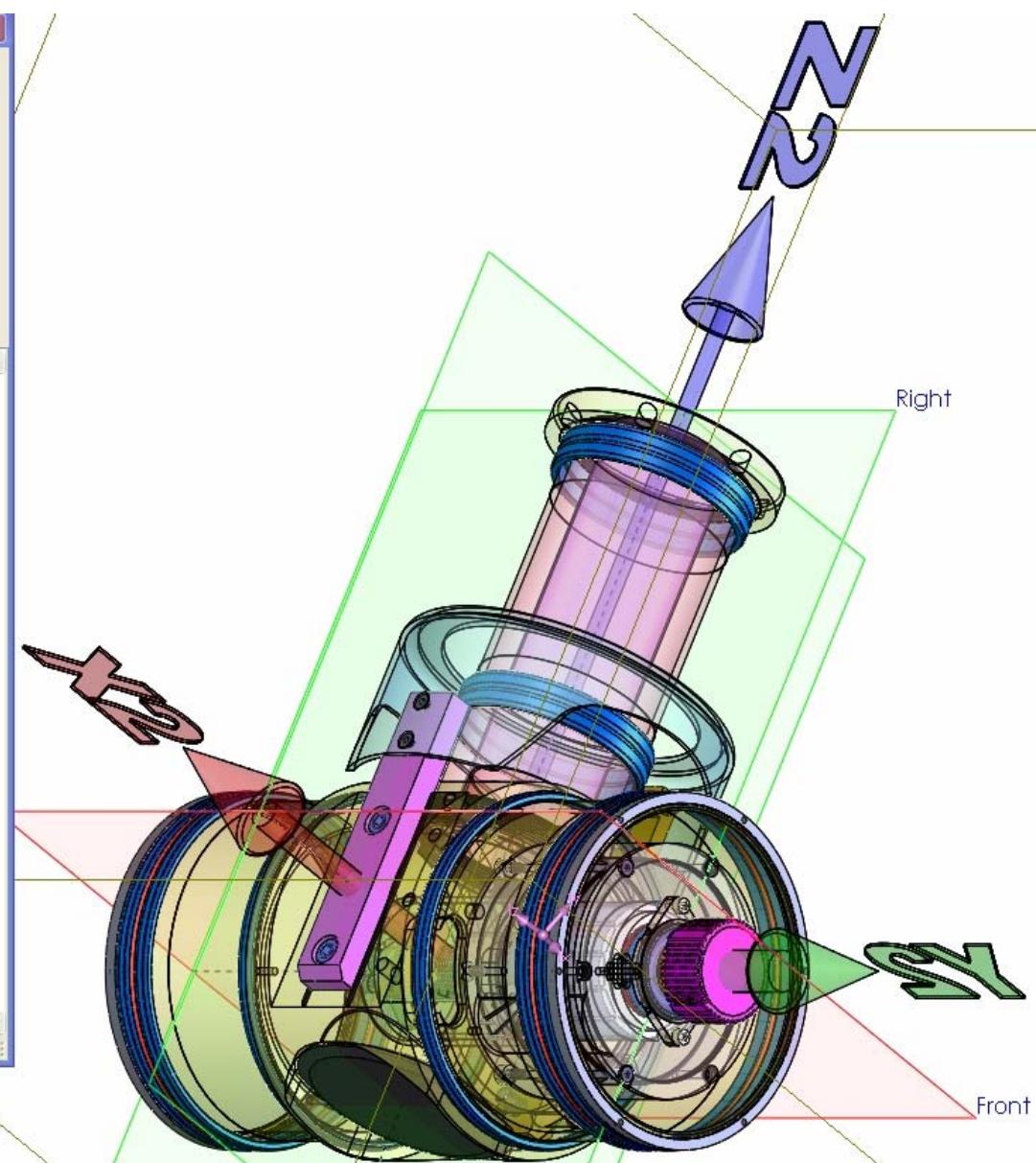
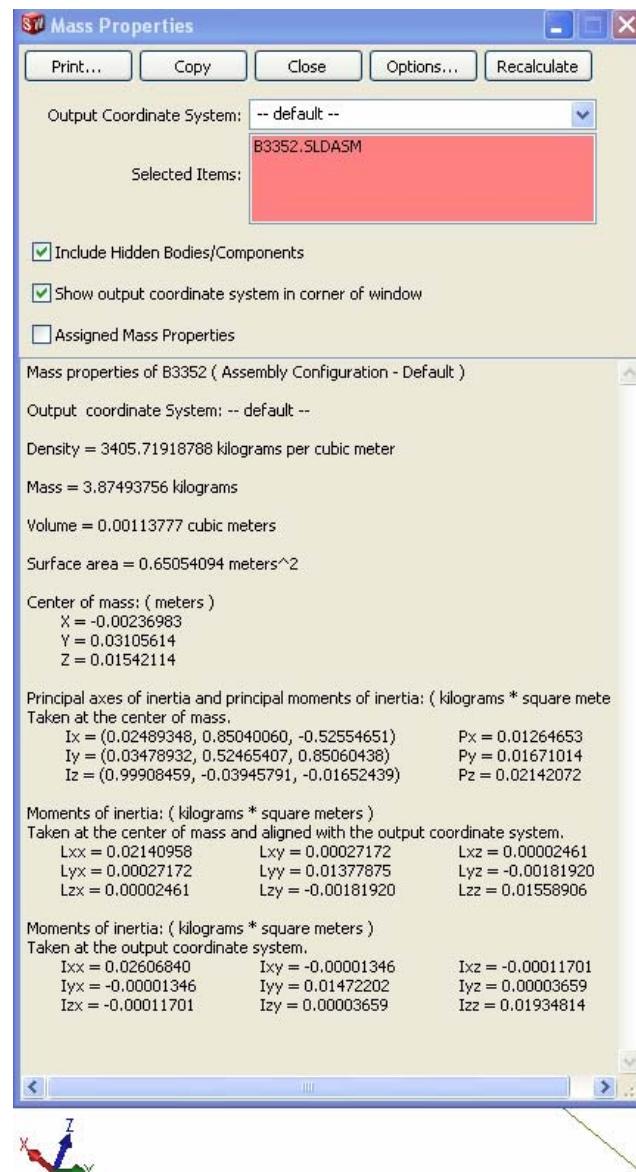


Figure 6 -- Frame-2 Inertia.

Table 4 --Frame-2 Mass properties of B3352 (Assembly Configuration - Default)

Mass = 3.87493756 kilograms

Volume = 0.00113777 cubic meters

Surface area = 0.65054094 meters²

Center of mass: (meters)

$$X = -0.00236983$$

$$Y = 0.03105614$$

$$Z = 0.01542114$$

Principal axes of inertia and principal moments of inertia: (kilograms * square meters)

Taken at the center of mass.

$$I_x = (0.02489348, 0.85040060, -0.52554651) \quad P_x = 0.01264653$$

$$I_y = (0.03478932, 0.52465407, 0.85060438) \quad P_y = 0.01671014$$

$$I_z = (0.99908459, -0.03945791, -0.01652439) \quad P_z = 0.02142072$$

Moments of inertia: (kilograms * square meters)

Taken at the center of mass and aligned with the output coordinate system.

$$L_{xx} = 0.02140958 \quad L_{xy} = 0.00027172 \quad L_{xz} = 0.00002461$$

$$L_{yx} = 0.00027172 \quad L_{yy} = 0.01377875 \quad L_{yz} = -0.00181920$$

$$L_{zx} = 0.00002461 \quad L_{zy} = -0.00181920 \quad L_{zz} = 0.01558906$$

Moments of inertia: (kilograms * square meters)

Taken at the output coordinate system.

$$I_{xx} = 0.02606840 \quad I_{xy} = -0.00001346 \quad I_{xz} = -0.00011701$$

$$I_{yx} = -0.00001346 \quad I_{yy} = 0.01472202 \quad I_{yz} = 0.00003659$$

$$I_{zx} = -0.00011701 \quad I_{zy} = 0.00003659 \quad I_{zz} = 0.01934814$$

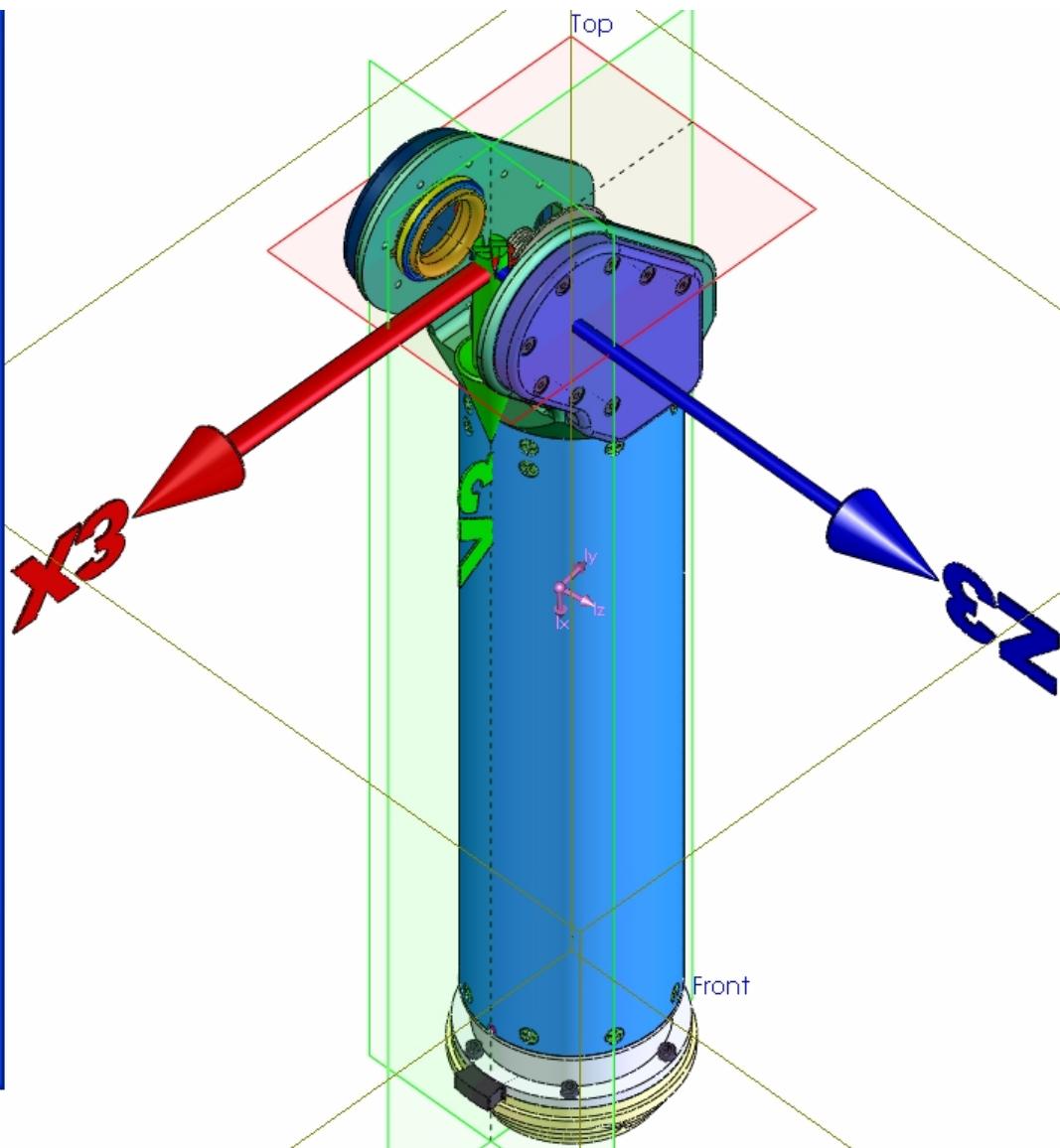
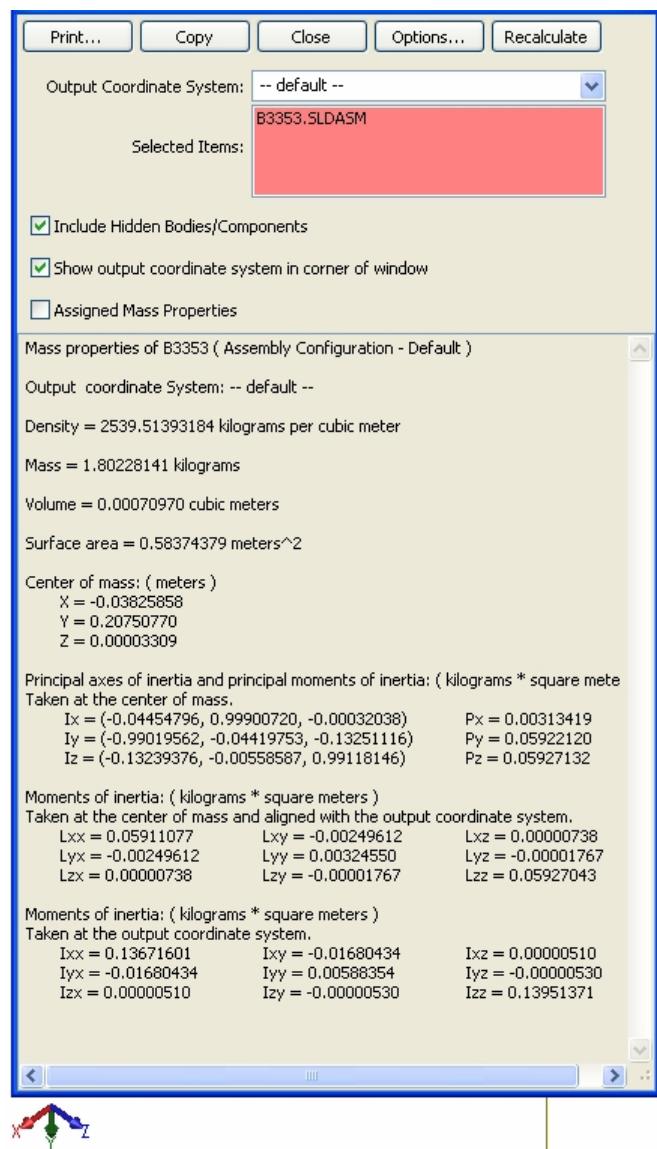
**Figure 7 -- Frame-3 Inertia.**

Table 5 --Frame-3 Mass properties of B3353 (Assembly Configuration - Default)

Density = 2539.51393184 kilograms per cubic meter

Mass = 1.80228141 kilograms

Volume = 0.00070970 cubic meters

Surface area = 0.58374379 meters²

Center of mass: (meters)

$$X = -0.03825858$$

$$Y = 0.20750770$$

$$Z = 0.00003309$$

Principal axes of inertia and principal moments of inertia: (kilograms * square meters)

Taken at the center of mass.

$$I_x = (-0.04454796, 0.99900720, -0.00032038) \quad P_x = 0.00313419$$

$$I_y = (-0.99019562, -0.04419753, -0.13251116) \quad P_y = 0.05922120$$

$$I_z = (-0.13239376, -0.00558587, 0.99118146) \quad P_z = 0.05927132$$

Moments of inertia: (kilograms * square meters)

Taken at the center of mass and aligned with the output coordinate system.

$$L_{xx} = 0.05911077 \quad L_{xy} = -0.00249612 \quad L_{xz} = 0.00000738$$

$$L_{yx} = -0.00249612 \quad L_{yy} = 0.00324550 \quad L_{yz} = -0.00001767$$

$$L_{zx} = 0.00000738 \quad L_{zy} = -0.00001767 \quad L_{zz} = 0.05927043$$

Moments of inertia: (kilograms * square meters)

Taken at the output coordinate system.

$$I_{xx} = 0.13671601 \quad I_{xy} = -0.01680434 \quad I_{xz} = 0.00000510$$

$$I_{yx} = -0.01680434 \quad I_{yy} = 0.00588354 \quad I_{yz} = -0.00000530$$

$$I_{zx} = 0.00000510 \quad I_{zy} = -0.00000530 \quad I_{zz} = 0.13951371$$

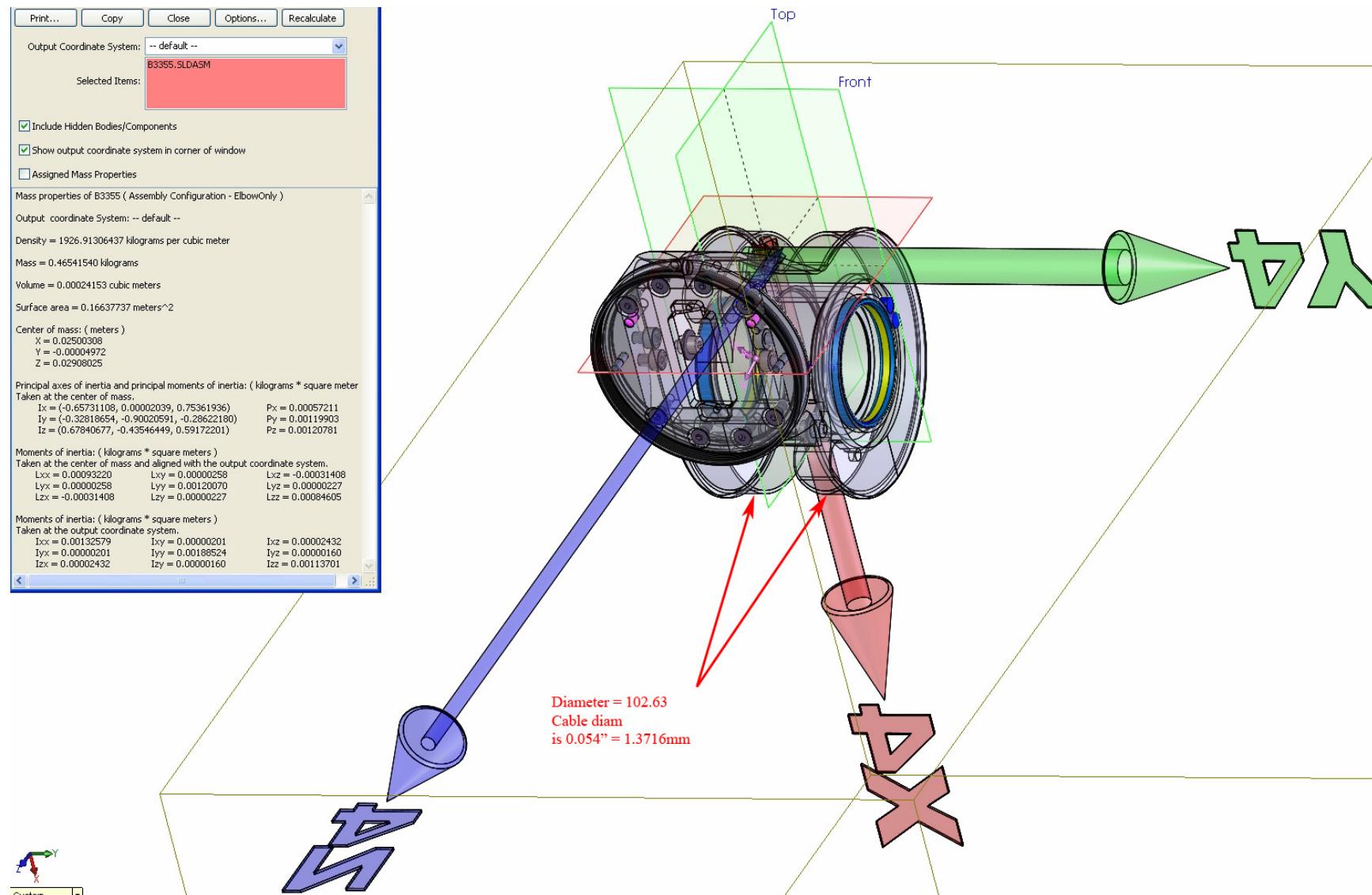


Figure 8 -- Frame-4 Inertia (without any attachment)

Table 6 --Frame-4 Mass properties of B3355 (Assembly Configuration - ElbowOnly)

Density = 1926.91306437 kilograms per cubic meter

Mass = 0.46541540 kilograms

Volume = 0.00024153 cubic meters

Surface area = 0.16637737 meters²

Center of mass: (meters)

$$X = 0.02500308$$

$$Y = -0.00004972$$

$$Z = 0.02908025$$

Principal axes of inertia and principal moments of inertia: (kilograms * square meters)

Taken at the center of mass.

$$I_x = (-0.65731108, 0.00002039, 0.75361936) \quad P_x = 0.00057211$$

$$I_y = (-0.32818654, -0.90020591, -0.28622180) \quad P_y = 0.00119903$$

$$I_z = (0.67840677, -0.43546449, 0.59172201) \quad P_z = 0.00120781$$

Moments of inertia: (kilograms * square meters)

Taken at the center of mass and aligned with the output coordinate system.

$$L_{xx} = 0.00093220 \quad L_{xy} = 0.00000258 \quad L_{xz} = -0.00031408$$

$$L_{yx} = 0.00000258 \quad L_{yy} = 0.00120070 \quad L_{yz} = 0.00000227$$

$$L_{zx} = -0.00031408 \quad L_{zy} = 0.00000227 \quad L_{zz} = 0.00084605$$

Moments of inertia: (kilograms * square meters)

Taken at the output coordinate system.

$$I_{xx} = 0.00132579 \quad I_{xy} = 0.00000201 \quad I_{xz} = 0.00002432$$

$$I_{yx} = 0.00000201 \quad I_{yy} = 0.00188524 \quad I_{yz} = 0.00000160$$

$$I_{zx} = 0.00002432 \quad I_{zy} = 0.00000160 \quad I_{zz} = 0.00113701$$

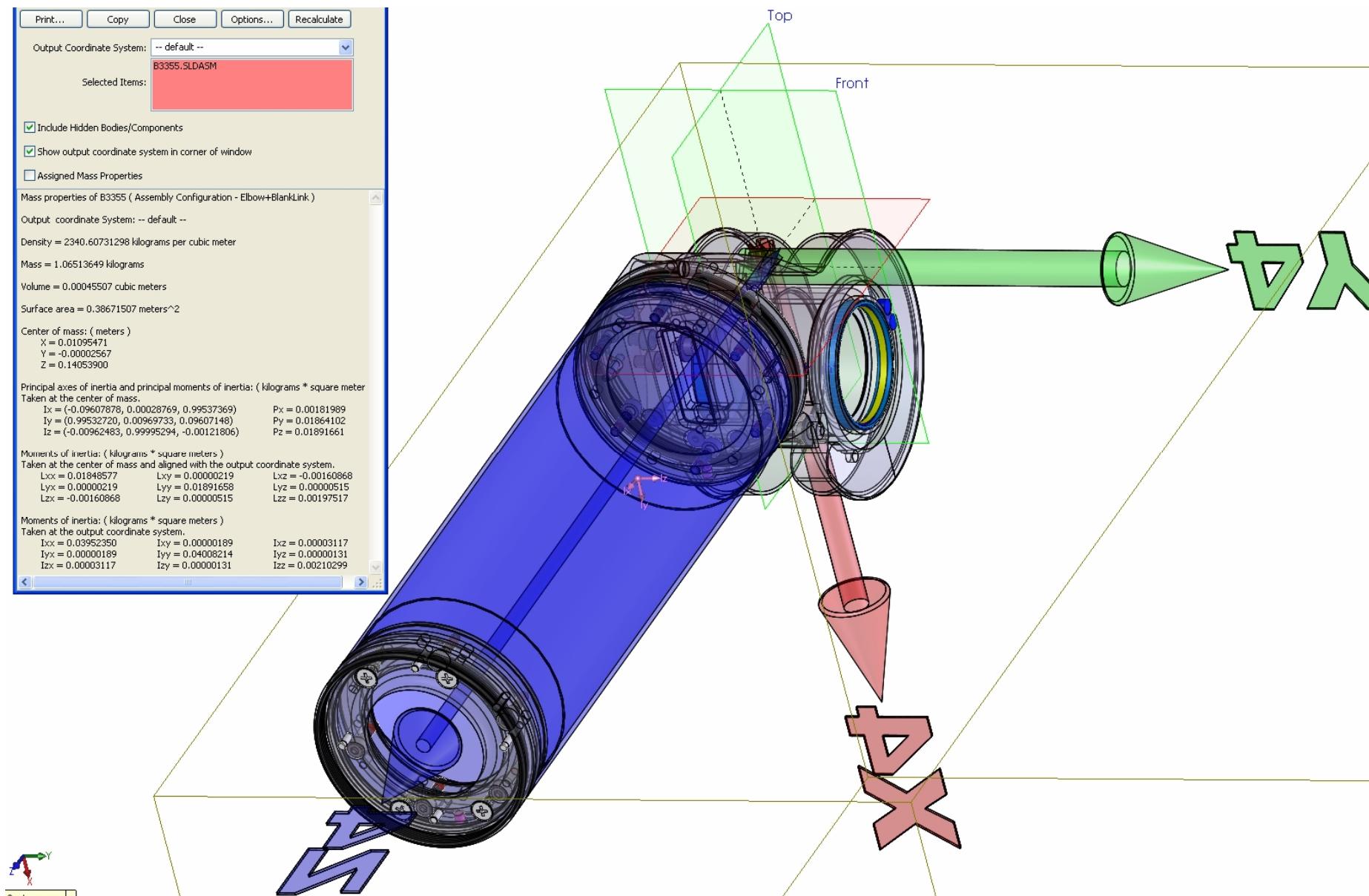
**Figure 9 -- Frame-4 Inertia (with 4-DOF forearm attached).**

Table 7 --Frame-4 Mass properties of B3355 (Assembly Configuration - Elbow+BlankLink)

Density = 2340.60731298 kilograms per cubic meter

Mass = 1.06513649 kilograms

Volume = 0.00045507 cubic meters

Surface area = 0.38671507 meters²

Center of mass: (meters)

$$X = 0.01095471$$

$$Y = -0.00002567$$

$$Z = 0.14053900$$

Principal axes of inertia and principal moments of inertia: (kilograms * square meters)

Taken at the center of mass.

$$I_x = (-0.09607878, 0.00028769, 0.99537369) \quad P_x = 0.00181989$$

$$I_y = (0.99532720, 0.00969733, 0.09607148) \quad P_y = 0.01864102$$

$$I_z = (-0.00962483, 0.99995294, -0.00121806) \quad P_z = 0.01891661$$

Moments of inertia: (kilograms * square meters)

Taken at the center of mass and aligned with the output coordinate system.

$$L_{xx} = 0.01848577 \quad L_{xy} = 0.00000219 \quad L_{xz} = -0.00160868$$

$$L_{yx} = 0.00000219 \quad L_{yy} = 0.01891658 \quad L_{yz} = 0.00000515$$

$$L_{zx} = -0.00160868 \quad L_{zy} = 0.00000515 \quad L_{zz} = 0.00197517$$

Moments of inertia: (kilograms * square meters)

Taken at the output coordinate system.

$$I_{xx} = 0.03952350 \quad I_{xy} = 0.00000189 \quad I_{xz} = 0.00003117$$

$$I_{yx} = 0.00000189 \quad I_{yy} = 0.04008214 \quad I_{yz} = 0.00000131$$

$$I_{zx} = 0.00003117 \quad I_{zy} = 0.00000131 \quad I_{zz} = 0.00210299$$

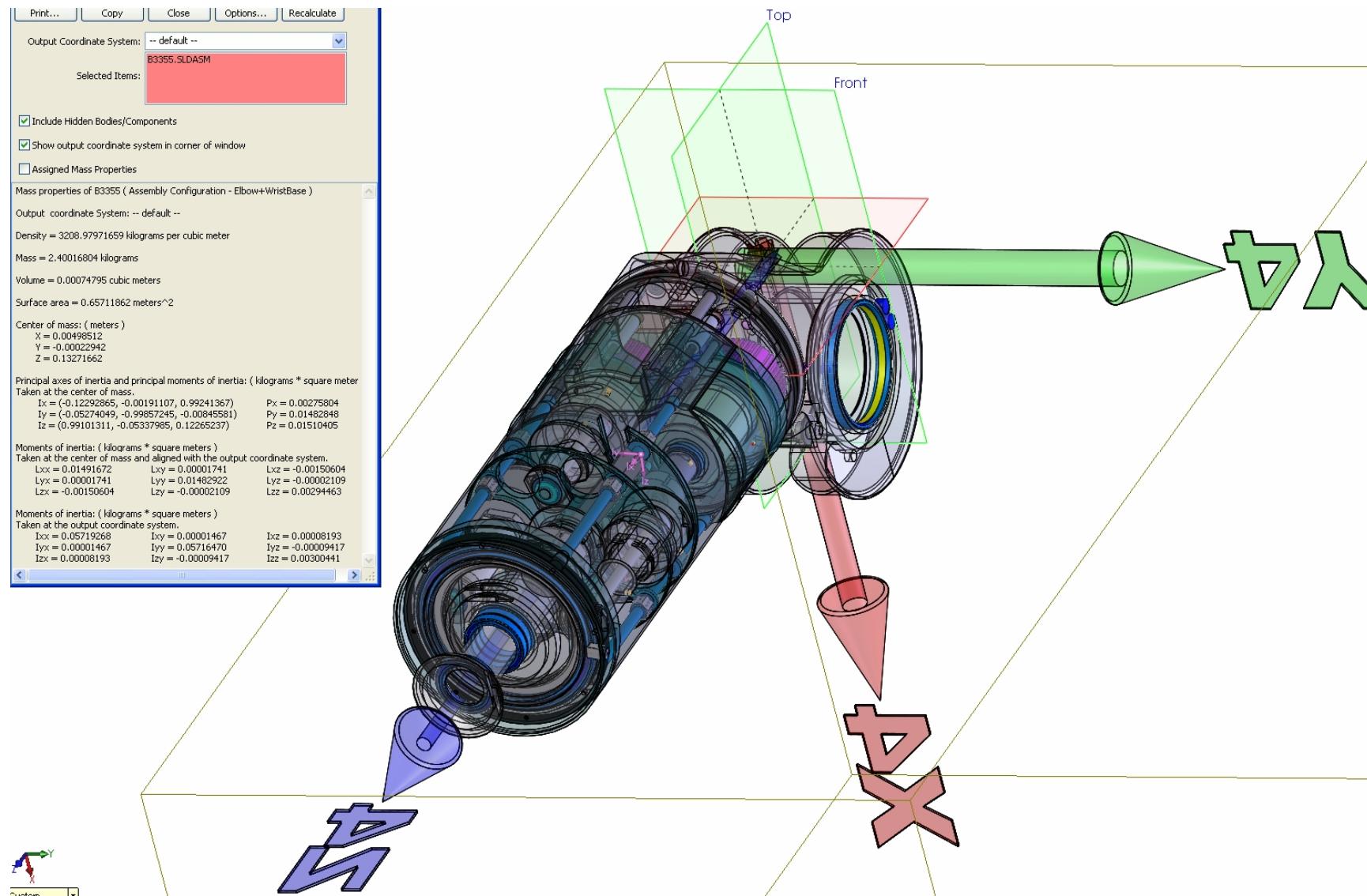
**Figure 10 -- Frame-4 Inertia (with base of wrist attached).**

Table 8 --Frame-4 Mass properties of B3355 (Assembly Configuration - Elbow+WristBase)

Density = 3208.97971659 kilograms per cubic meter

Mass = 2.40016804 kilograms

Volume = 0.00074795 cubic meters

Surface area = 0.65711862 meters²

Center of mass: (meters)

$$X = 0.00498512$$

$$Y = -0.00022942$$

$$Z = 0.13271662$$

Principal axes of inertia and principal moments of inertia: (kilograms * square meters)

Taken at the center of mass.

$$I_x = (-0.12292865, -0.00191107, 0.99241367) \quad P_x = 0.00275804$$

$$I_y = (-0.05274049, -0.99857245, -0.00845581) \quad P_y = 0.01482848$$

$$I_z = (0.99101311, -0.05337985, 0.12265237) \quad P_z = 0.01510405$$

Moments of inertia: (kilograms * square meters)

Taken at the center of mass and aligned with the output coordinate system.

$$L_{xx} = 0.01491672 \quad L_{xy} = 0.00001741 \quad L_{xz} = -0.00150604$$

$$L_{yx} = 0.00001741 \quad L_{yy} = 0.01482922 \quad L_{yz} = -0.00002109$$

$$L_{zx} = -0.00150604 \quad L_{zy} = -0.00002109 \quad L_{zz} = 0.00294463$$

Moments of inertia: (kilograms * square meters)

Taken at the output coordinate system.

$$I_{xx} = 0.05719268 \quad I_{xy} = 0.00001467 \quad I_{xz} = 0.00008193$$

$$I_{yx} = 0.00001467 \quad I_{yy} = 0.05716470 \quad I_{yz} = -0.00009417$$

$$I_{zx} = 0.00008193 \quad I_{zy} = -0.00009417 \quad I_{zz} = 0.00300441$$

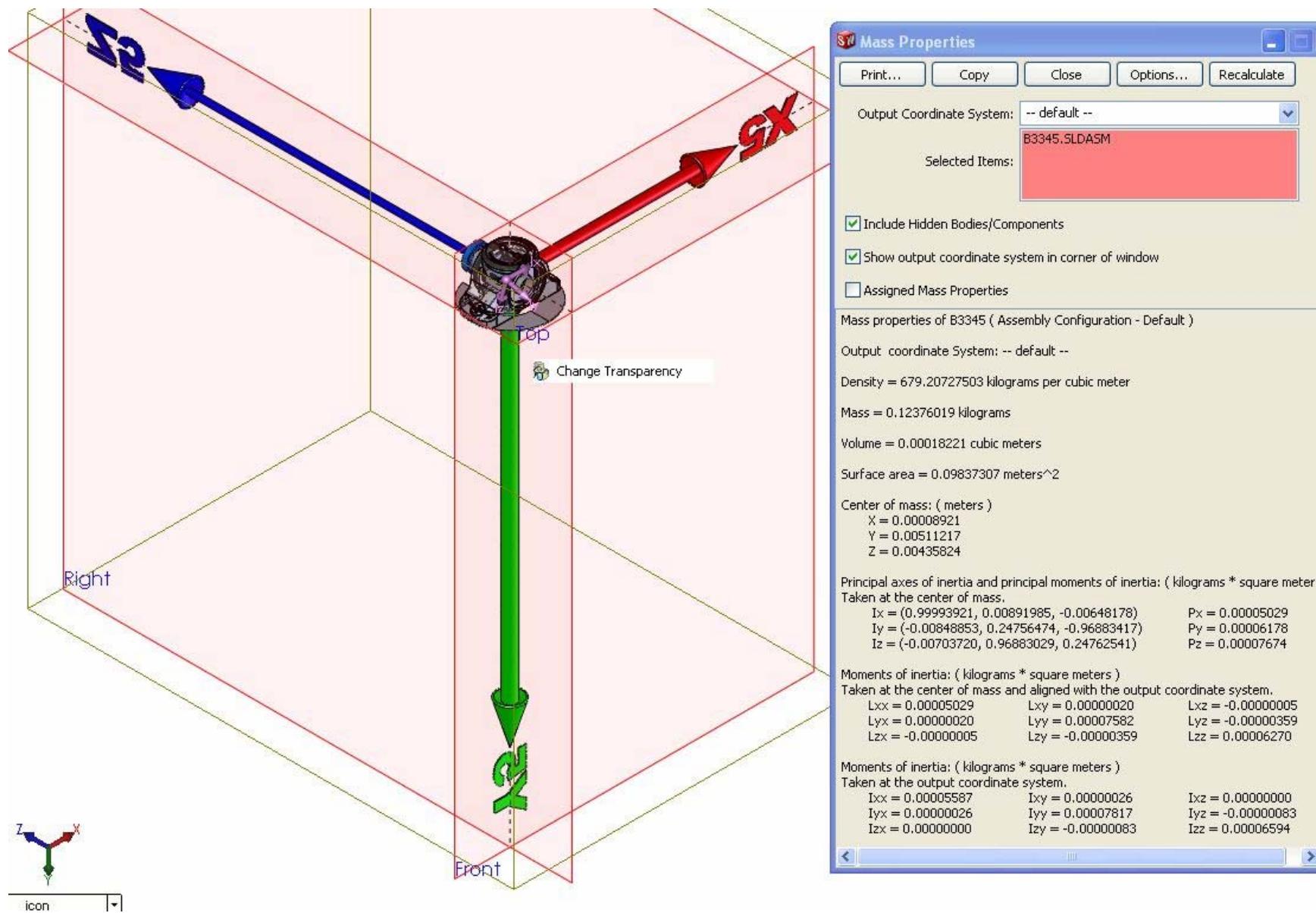


Figure 11 – Frame-5 Inertia

Table 9 --Frame-5 Mass properties of B3345 (Assembly Configuration - Default)

Density = 679.20727503 kilograms per cubic meter

Mass = 0.12376019 kilograms

Volume = 0.00018221 cubic meters

Surface area = 0.09837307 meters²

Center of mass: (meters)

$$X = 0.00008921$$

$$Y = 0.00511217$$

$$Z = 0.00435824$$

Principal axes of inertia and principal moments of inertia: (kilograms * square meters)

Taken at the center of mass.

$$I_x = (0.99993921, 0.00891985, -0.00648178) \quad P_x = 0.00005029$$

$$I_y = (-0.00848853, 0.24756474, -0.96883417) \quad P_y = 0.00006178$$

$$I_z = (-0.00703720, 0.96883029, 0.24762541) \quad P_z = 0.00007674$$

Moments of inertia: (kilograms * square meters)

Taken at the center of mass and aligned with the output coordinate system.

$$L_{xx} = 0.00005029 \quad L_{xy} = 0.00000020 \quad L_{xz} = -0.00000005$$

$$L_{yx} = 0.00000020 \quad L_{yy} = 0.00007582 \quad L_{yz} = -0.00000359$$

$$L_{zx} = -0.00000005 \quad L_{zy} = -0.00000359 \quad L_{zz} = 0.00006270$$

Moments of inertia: (kilograms * square meters)

Taken at the output coordinate system.

$$I_{xx} = 0.00005587 \quad I_{xy} = 0.00000026 \quad I_{xz} = 0.00000000$$

$$I_{yx} = 0.00000026 \quad I_{yy} = 0.00007817 \quad I_{yz} = -0.00000083$$

$$I_{zx} = 0.00000000 \quad I_{zy} = -0.00000083 \quad I_{zz} = 0.00006594$$

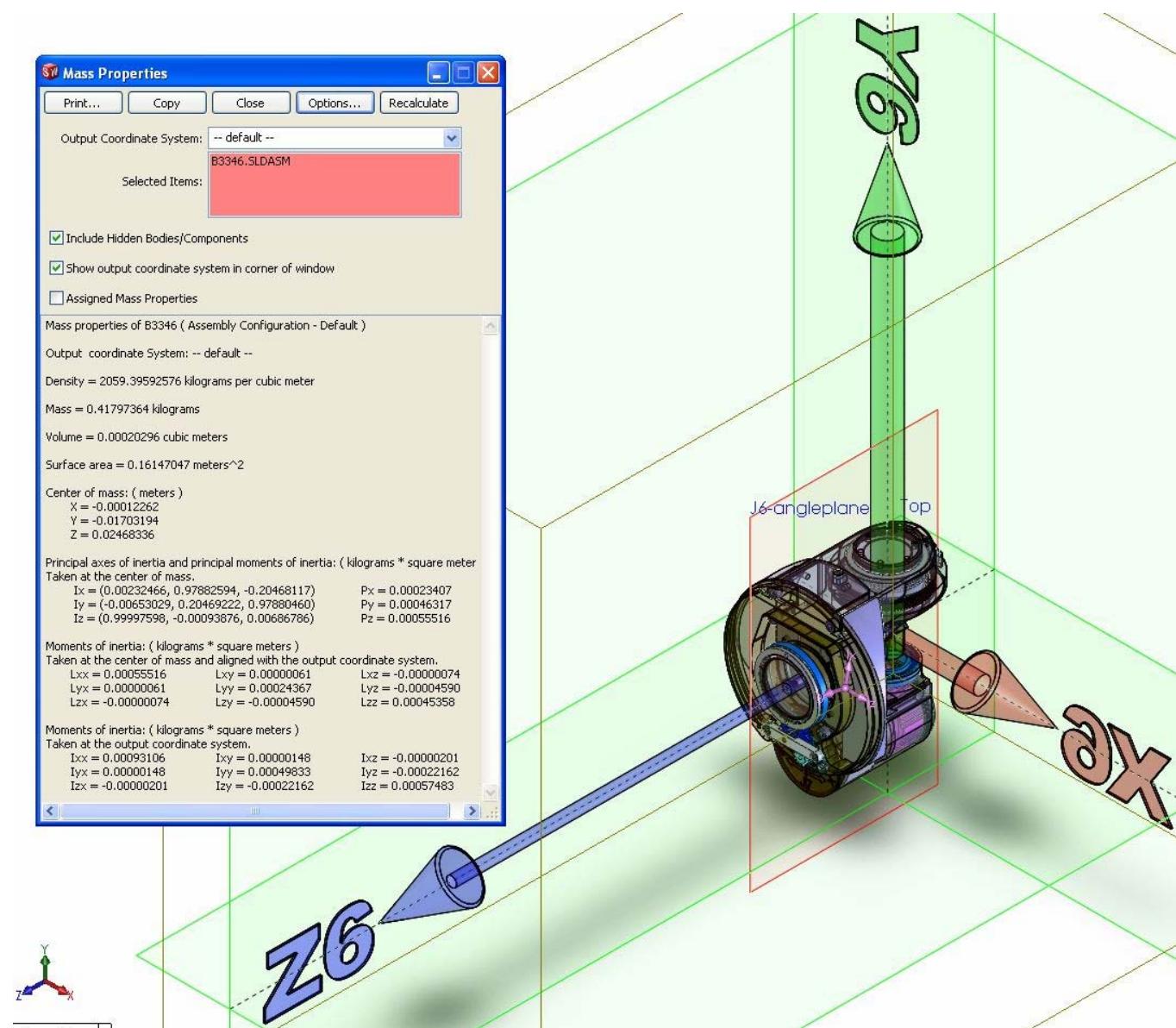


Figure 12 -- Frame-6 Inertia.

Table 10 --Frame-6 Mass properties of B3346 (Assembly Configuration - Default)

Density = 2059.39592576 kilograms per cubic meter

Mass = 0.41797364 kilograms

Volume = 0.00020296 cubic meters

Surface area = 0.16147047 meters²

Center of mass: (meters)

$$X = -0.00012262$$

$$Y = -0.01703194$$

$$Z = 0.02468336$$

Principal axes of inertia and principal moments of inertia: (kilograms * square meters)

Taken at the center of mass.

$$I_x = (0.00232466, 0.97882594, -0.20468117) \quad P_x = 0.00023407$$

$$I_y = (-0.00653029, 0.20469222, 0.97880460) \quad P_y = 0.00046317$$

$$I_z = (0.99997598, -0.00093876, 0.00686786) \quad P_z = 0.00055516$$

Moments of inertia: (kilograms * square meters)

Taken at the center of mass and aligned with the output coordinate system.

$$L_{xx} = 0.00055516 \quad L_{xy} = 0.00000061 \quad L_{xz} = -0.00000074$$

$$L_{yx} = 0.00000061 \quad L_{yy} = 0.00024367 \quad L_{yz} = -0.00004590$$

$$L_{zx} = -0.00000074 \quad L_{zy} = -0.00004590 \quad L_{zz} = 0.00045358$$

Moments of inertia: (kilograms * square meters)

Taken at the output coordinate system.

$$I_{xx} = 0.00093106 \quad I_{xy} = 0.00000148 \quad I_{xz} = -0.00000201$$

$$I_{yx} = 0.00000148 \quad I_{yy} = 0.00049833 \quad I_{yz} = -0.00022162$$

$$I_{zx} = -0.00000201 \quad I_{zy} = -0.00022162 \quad I_{zz} = 0.00057483$$

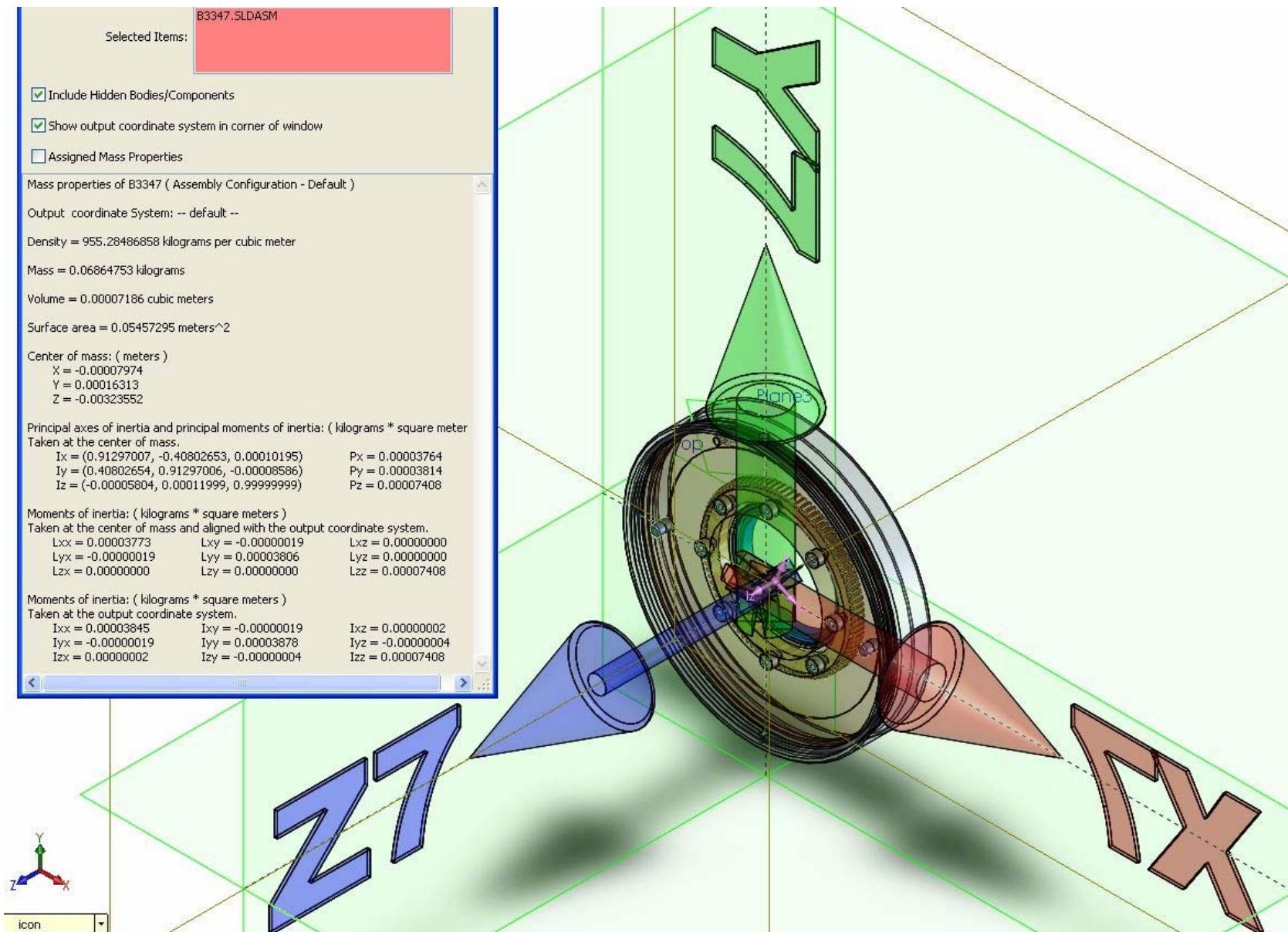


Figure 13 -- Frame-7 Inertia.

Table 11 --Frame-7 Mass properties of B3347 (Assembly Configuration - Default)

Density = 955.28486858 kilograms per cubic meter

Mass = 0.06864753 kilograms

Volume = 0.00007186 cubic meters

Surface area = 0.05457295 meters²

Center of mass: (meters)

$$X = -0.00007974$$

$$Y = 0.00016313$$

$$Z = -0.00323552$$

Principal axes of inertia and principal moments of inertia: (kilograms * square meters)

Taken at the center of mass.

$$I_x = (0.91297007, -0.40802653, 0.00010195) \quad P_x = 0.00003764$$

$$I_y = (0.40802654, 0.91297006, -0.00008586) \quad P_y = 0.00003814$$

$$I_z = (-0.00005804, 0.00011999, 0.99999999) \quad P_z = 0.00007408$$

Moments of inertia: (kilograms * square meters)

Taken at the center of mass and aligned with the output coordinate system.

$$L_{xx} = 0.00003773 \quad L_{xy} = -0.00000019 \quad L_{xz} = 0.00000000$$

$$L_{yx} = -0.00000019 \quad L_{yy} = 0.00003806 \quad L_{yz} = 0.00000000$$

$$L_{zx} = 0.00000000 \quad L_{zy} = 0.00000000 \quad L_{zz} = 0.00007408$$

Moments of inertia: (kilograms * square meters)

Taken at the output coordinate system.

$$I_{xx} = 0.00003845 \quad I_{xy} = -0.00000019 \quad I_{xz} = 0.00000002$$

$$I_{yx} = -0.00000019 \quad I_{yy} = 0.00003878 \quad I_{yz} = -0.00000004$$

$$I_{zx} = 0.00000002 \quad I_{zy} = -0.00000004 \quad I_{zz} = 0.00007408$$

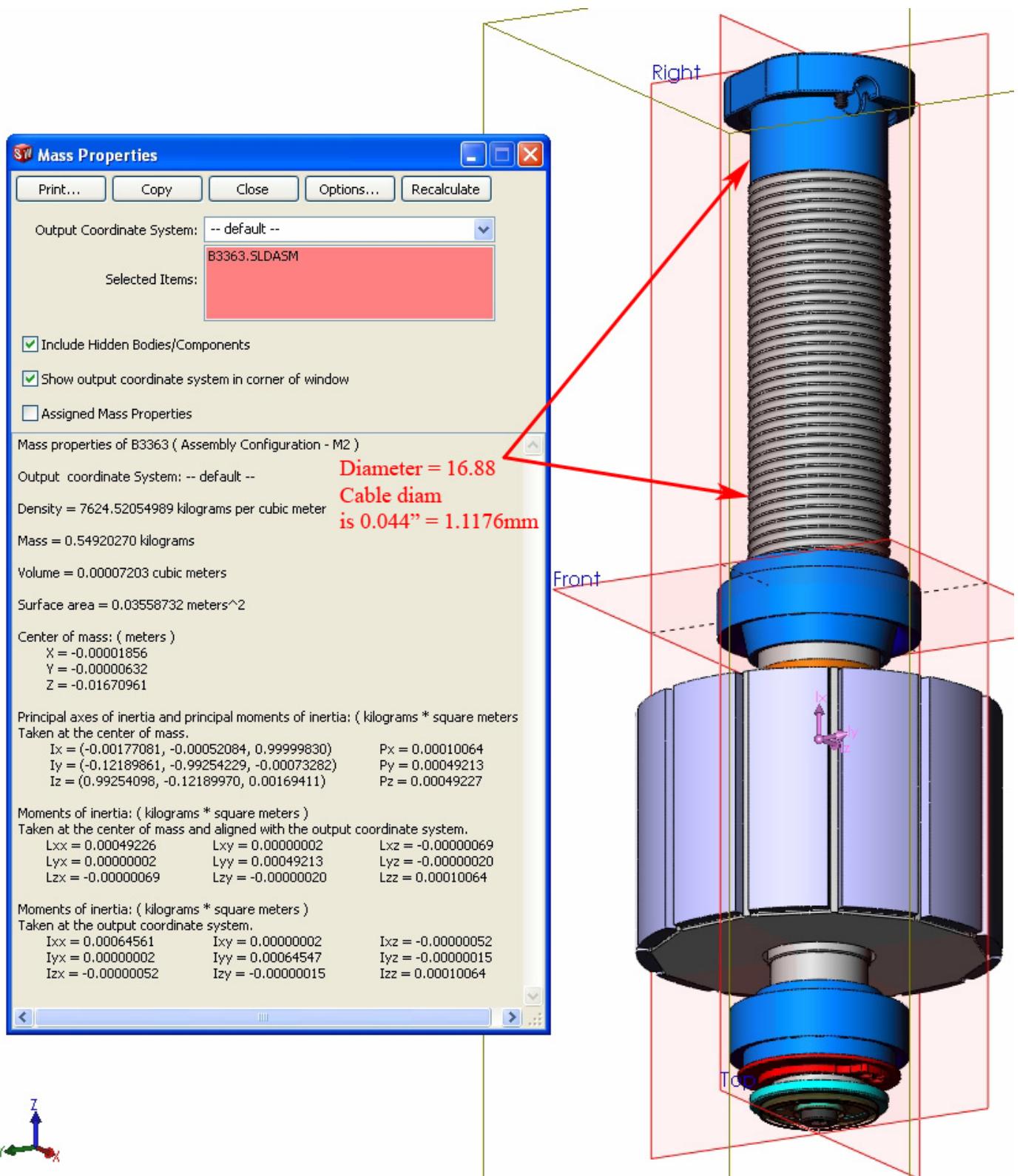


Figure 14 -- Motor Rotor for the 1st Four DOFs of the WAM.

Table 12 --Mass properties of B3363 (Assembly Configuration - M2)

Density = 7624.52054989 kilograms per cubic meter

Mass = 0.54920270 kilograms

Volume = 0.00007203 cubic meters

Surface area = 0.03558732 meters²

Center of mass: (meters)

$$X = -0.00001856$$

$$Y = -0.00000632$$

$$Z = -0.01670961$$

Principal axes of inertia and principal moments of inertia: (kilograms * square meters)

Taken at the center of mass.

$$I_x = (-0.00177081, -0.00052084, 0.99999830) \quad P_x = 0.00010064$$

$$I_y = (-0.12189861, -0.99254229, -0.00073282) \quad P_y = 0.00049213$$

$$I_z = (0.99254098, -0.12189970, 0.00169411) \quad P_z = 0.00049227$$

Moments of inertia: (kilograms * square meters)

Taken at the center of mass and aligned with the output coordinate system.

$$L_{xx} = 0.00049226 \quad L_{xy} = 0.00000002 \quad L_{xz} = -0.00000069$$

$$L_{yx} = 0.00000002 \quad L_{yy} = 0.00049213 \quad L_{yz} = -0.00000020$$

$$L_{zx} = -0.00000069 \quad L_{zy} = -0.00000020 \quad L_{zz} = 0.00010064$$

Moments of inertia: (kilograms * square meters)

Taken at the output coordinate system.

$$I_{xx} = 0.00064561 \quad I_{xy} = 0.00000002 \quad I_{xz} = -0.00000052$$

$$I_{yx} = 0.00000002 \quad I_{yy} = 0.00064547 \quad I_{yz} = -0.00000015$$

$$I_{zx} = -0.00000052 \quad I_{zy} = -0.00000015 \quad \underline{I_{zz} = 0.00010064}$$

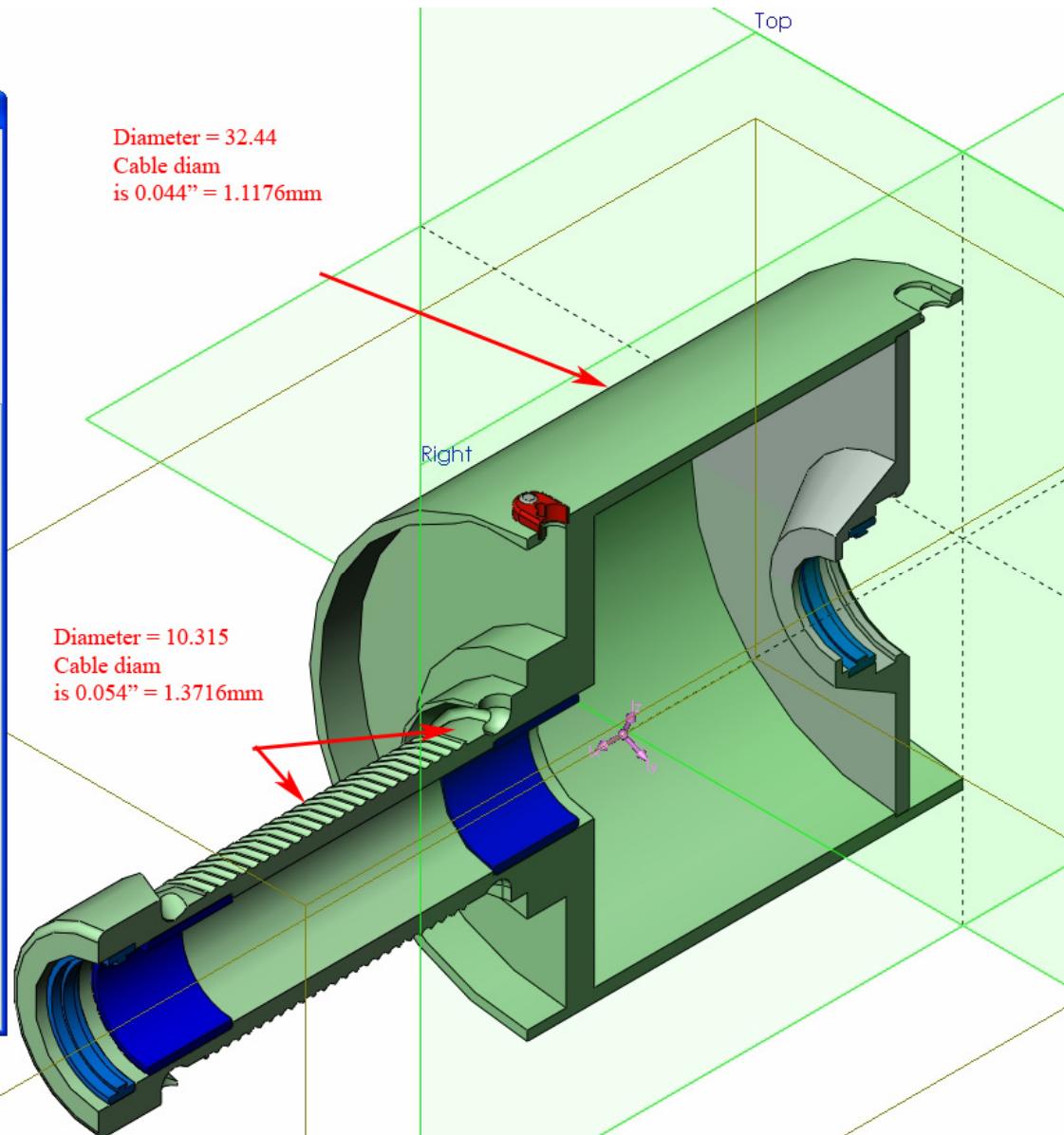
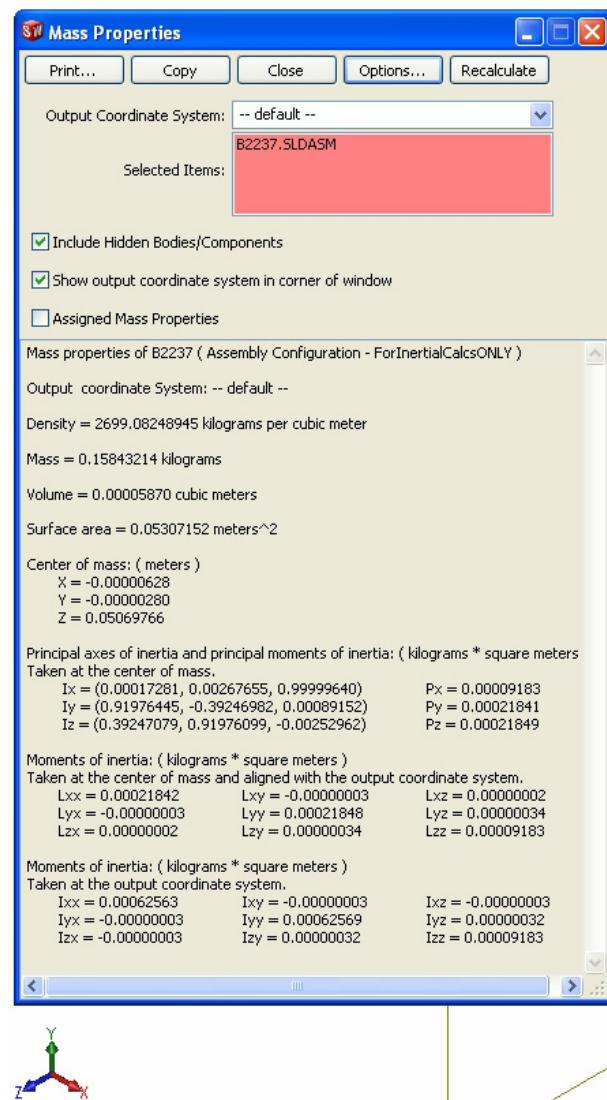


Figure 15 -- "Grenade" that couples 1st and 2nd stages of the 1st three DOFs of the WAM.

Table 13 --Mass properties of B2237 (Assembly Configuration - ForInertialCalcsONLY)

Density = 2699.08248945 kilograms per cubic meter

Mass = 0.15843214 kilograms

Volume = 0.00005870 cubic meters

Surface area = 0.05307152 meters²

Center of mass: (meters)

X = -0.00000628

Y = -0.00000280

Z = 0.05069766

Principal axes of inertia and principal moments of inertia: (kilograms * square meters)

Taken at the center of mass.

Ix = (0.00017281, 0.00267655, 0.99999640) Px = 0.00009183

Iy = (0.91976445, -0.39246982, 0.00089152) Py = 0.00021841

Iz = (0.39247079, 0.91976099, -0.00252962) Pz = 0.00021849

Moments of inertia: (kilograms * square meters)

Taken at the center of mass and aligned with the output coordinate system.

Lxx = 0.00021842 Lxy = -0.00000003 Lxz = 0.00000002

Lyx = -0.00000003 Lyy = 0.00021848 Lyz = 0.00000034

Lzx = 0.00000002 Lzy = 0.00000034 Lzz = 0.00009183

Moments of inertia: (kilograms * square meters)

Taken at the output coordinate system.

Ixx = 0.00062563 Ixy = -0.00000003 Ixz = -0.00000003

Iyx = -0.00000003 Iyy = 0.00062569 Iyz = 0.00000032

Izx = -0.00000003 Izy = 0.00000032 **Izz = 0.00009183**

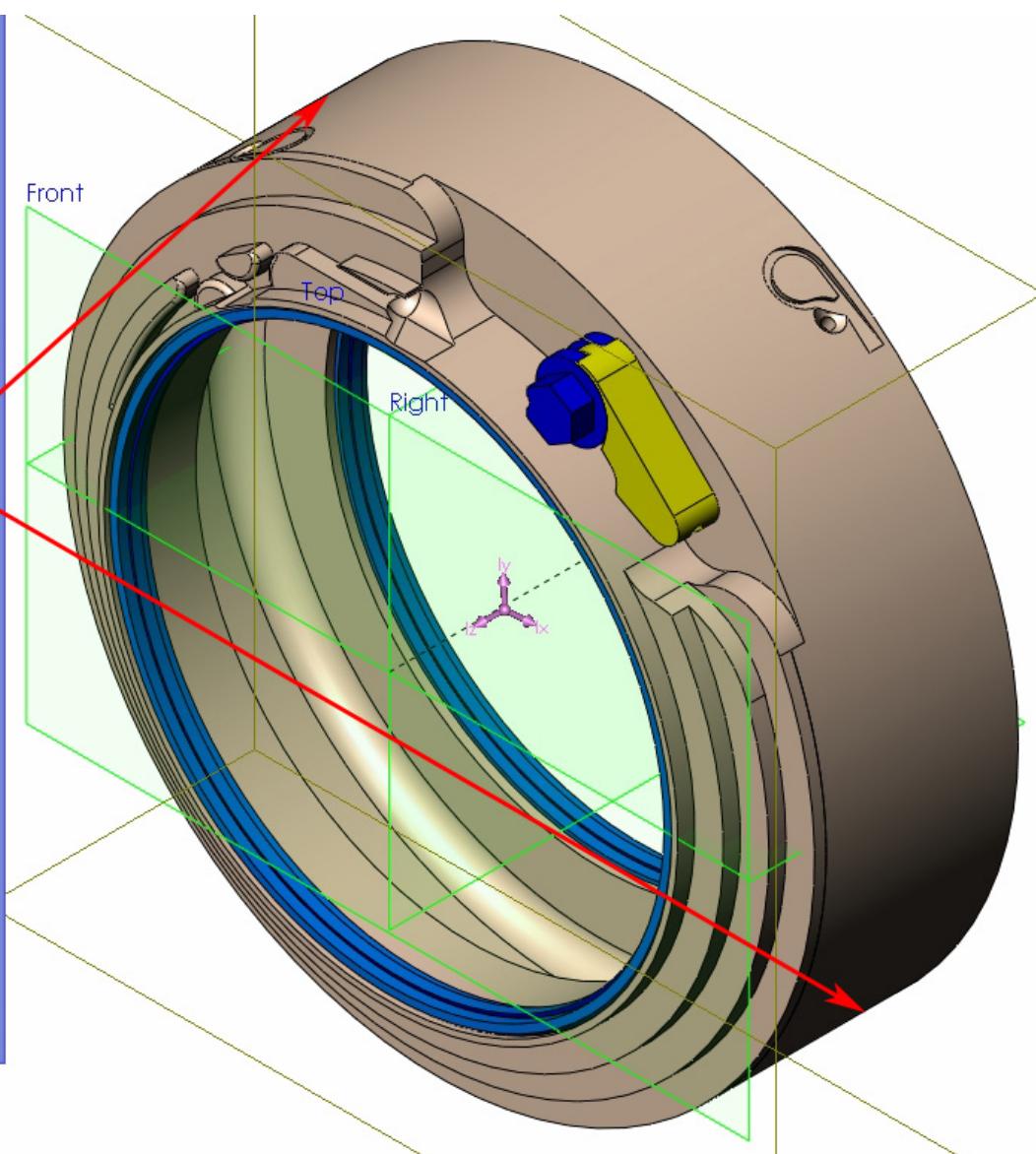
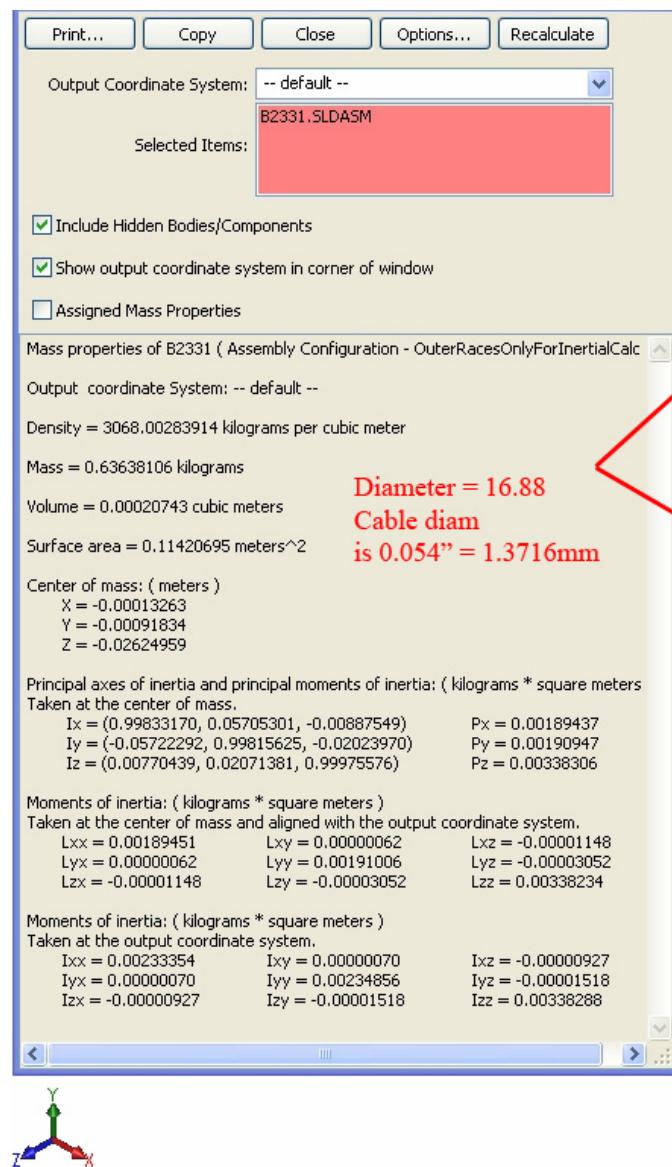


Figure 16 -- Differential-Input Pulley.

Table 14 --Mass properties of B2331 (Assembly Configuration - OuterRacesOnlyForInertialCales)

Density = 3068.00283914 kilograms per cubic meter

Mass = 0.63638106 kilograms

Volume = 0.00020743 cubic meters

Surface area = 0.11420695 meters²

Center of mass: (meters)

X = -0.00013263

Y = -0.00091834

Z = -0.02624959

Principal axes of inertia and principal moments of inertia: (kilograms * square meters)

Taken at the center of mass.

Ix = (0.99833170, 0.05705301, -0.00887549) Px = 0.00189437

Iy = (-0.05722292, 0.99815625, -0.02023970) Py = 0.00190947

Iz = (0.00770439, 0.02071381, 0.99975576) Pz = 0.00338306

Moments of inertia: (kilograms * square meters)

Taken at the center of mass and aligned with the output coordinate system.

Lxx = 0.00189451 Lxy = 0.00000062 Lxz = -0.00001148

Lyx = 0.00000062 Lyy = 0.00191006 Lyz = -0.00003052

Lzx = -0.00001148 Lzy = -0.00003052 Lzz = 0.00338234

Moments of inertia: (kilograms * square meters)

Taken at the output coordinate system.

Ixx = 0.00233354 Ixy = 0.00000070 Ixz = -0.00000927

Iyx = 0.00000070 Iyy = 0.00234856 Iyz = -0.00001518

Izx = -0.00000927 Izy = -0.00001518 **Izz = 0.00338288**

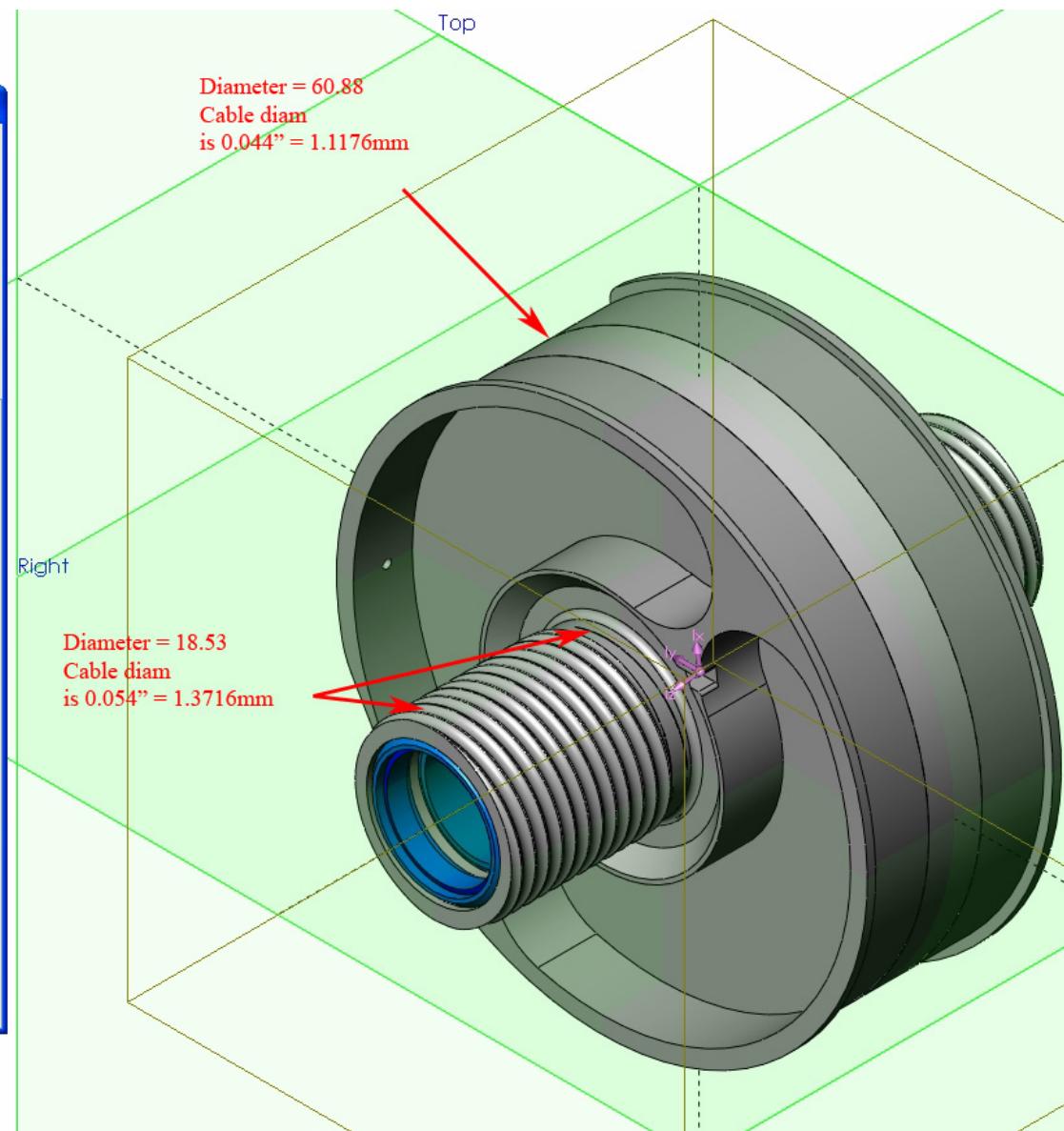
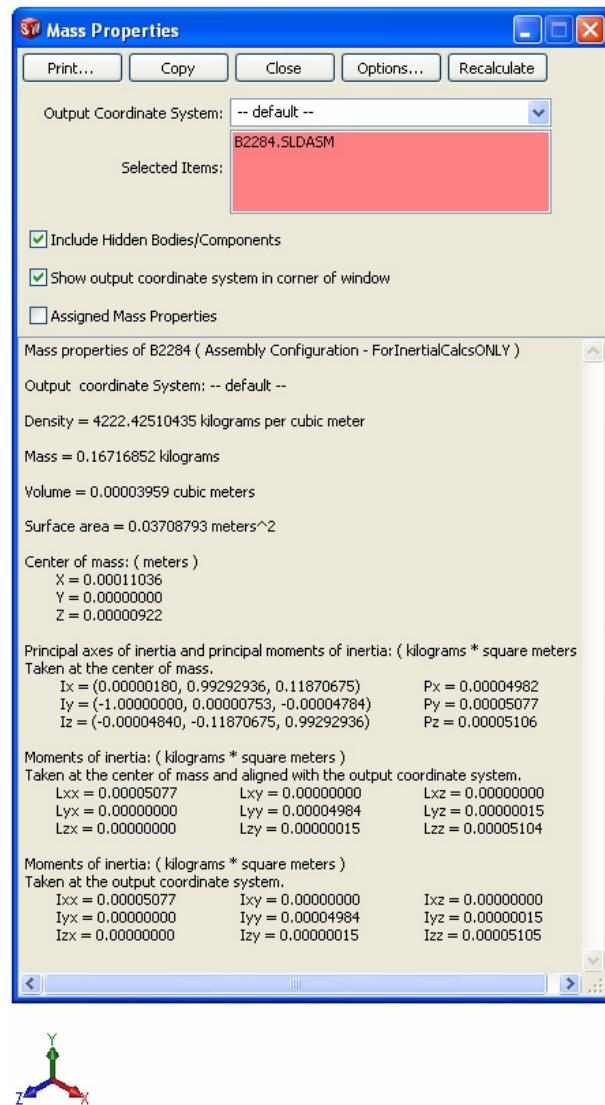


Figure 17 -- Elbow Pulley-Pinion with all bearings that couples the 1st & 2nd stages of J4.

Table 15 --Mass properties of B2284 (Assembly Configuration - ForInertialCalcsONLY)

Density = 4222.42510435 kilograms per cubic meter

Mass = 0.16716852 kilograms

Volume = 0.00003959 cubic meters

Surface area = 0.03708793 meters²

Center of mass: (meters)

$$X = 0.00011036$$

$$Y = 0.00000000$$

$$Z = 0.00000922$$

Principal axes of inertia and principal moments of inertia: (kilograms * square meters)

Taken at the center of mass.

$$I_x = (0.00000180, 0.99292936, 0.11870675) \quad P_x = 0.00004982$$

$$I_y = (-1.00000000, 0.00000753, -0.00004784) \quad P_y = 0.00005077$$

$$I_z = (-0.00004840, -0.11870675, 0.99292936) \quad P_z = 0.00005106$$

Moments of inertia: (kilograms * square meters)

Taken at the center of mass and aligned with the output coordinate system.

$$L_{xx} = 0.00005077 \quad L_{xy} = 0.00000000 \quad L_{xz} = 0.00000000$$

$$L_{yx} = 0.00000000 \quad L_{yy} = 0.00004984 \quad L_{yz} = 0.00000015$$

$$L_{zx} = 0.00000000 \quad L_{zy} = 0.00000015 \quad L_{zz} = 0.00005104$$

Moments of inertia: (kilograms * square meters)

Taken at the output coordinate system.

$$I_{xx} = 0.00005077 \quad I_{xy} = 0.00000000 \quad I_{xz} = 0.00000000$$

$$I_{yx} = 0.00000000 \quad I_{yy} = 0.00004984 \quad I_{yz} = 0.00000015$$

$$I_{zx} = 0.00000000 \quad I_{zy} = 0.00000015 \quad \underline{I_{zz} = 0.00005105}$$

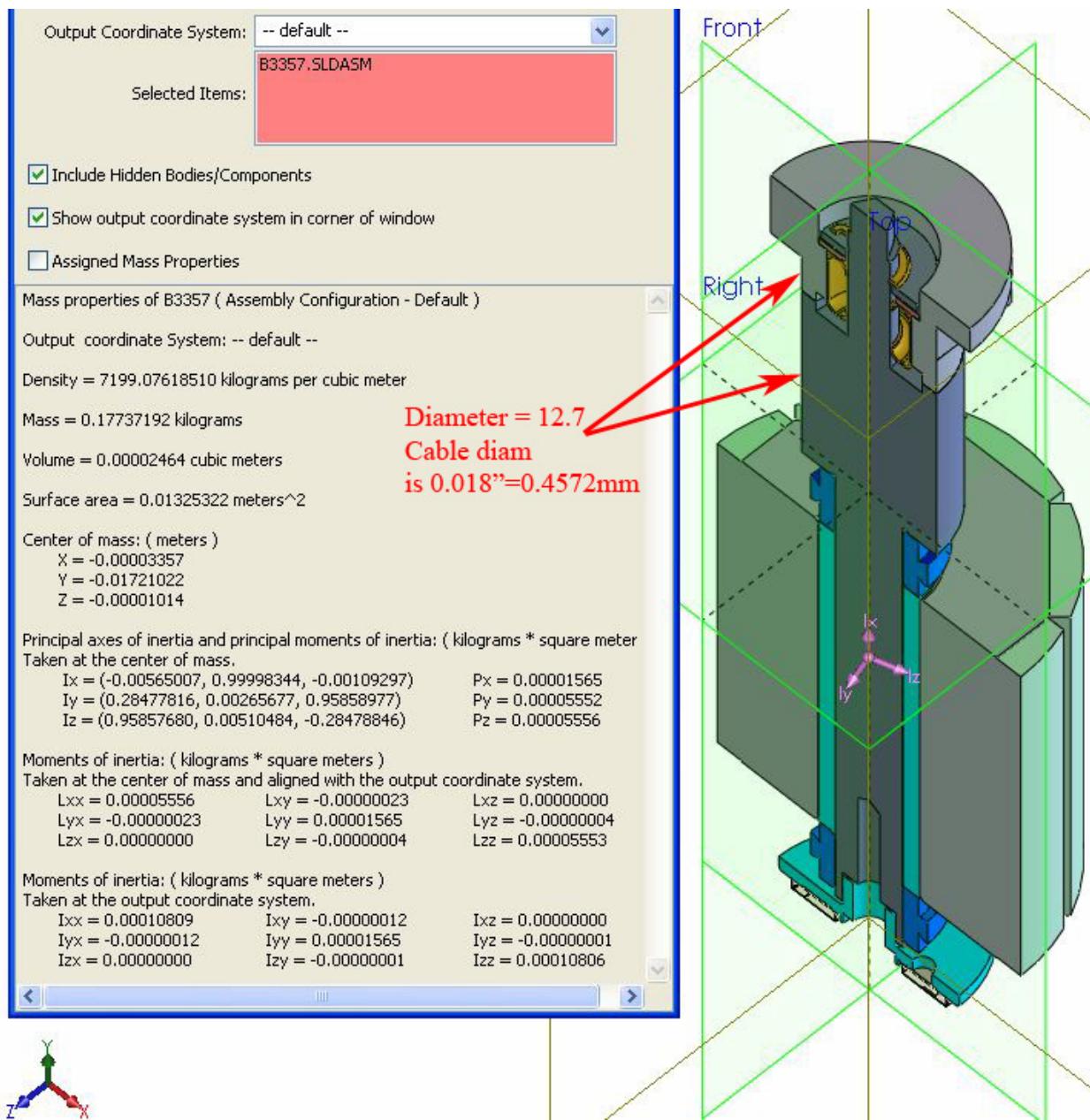


Figure 18 -- M5/M6 Motor Inertia.

Table 16 --Mass properties of B3357 (Assembly Configuration - Default)

Density = 7199.07618510 kilograms per cubic meter

Mass = 0.17737192 kilograms

Volume = 0.00002464 cubic meters

Surface area = 0.01325322 meters²

Center of mass: (meters)

X = -0.00003357

Y = -0.01721022

Z = -0.00001014

Principal axes of inertia and principal moments of inertia: (kilograms * square meters)

Taken at the center of mass.

Ix = (-0.00565007, 0.99998344, -0.00109297) Px = 0.00001565

Iy = (0.28477816, 0.00265677, 0.95858977) Py = 0.00005552

Iz = (0.95857680, 0.00510484, -0.28478846) Pz = 0.00005556

Moments of inertia: (kilograms * square meters)

Taken at the center of mass and aligned with the output coordinate system.

Lxx = 0.00005556 Lxy = -0.00000023 Lxz = 0.00000000

Lyx = -0.00000023 Lyy = 0.00001565 Lyz = -0.00000004

Lzx = 0.00000000 Lzy = -0.00000004 Lzz = 0.00005553

Moments of inertia: (kilograms * square meters)

Taken at the output coordinate system.

Ixx = 0.00010809 Ixy = -0.00000012 Ixz = 0.00000000

Iyx = -0.00000012 **Iyy = 0.00001565** Iyz = -0.00000001

Izx = 0.00000000 Izy = -0.00000001 Izz = 0.00010806

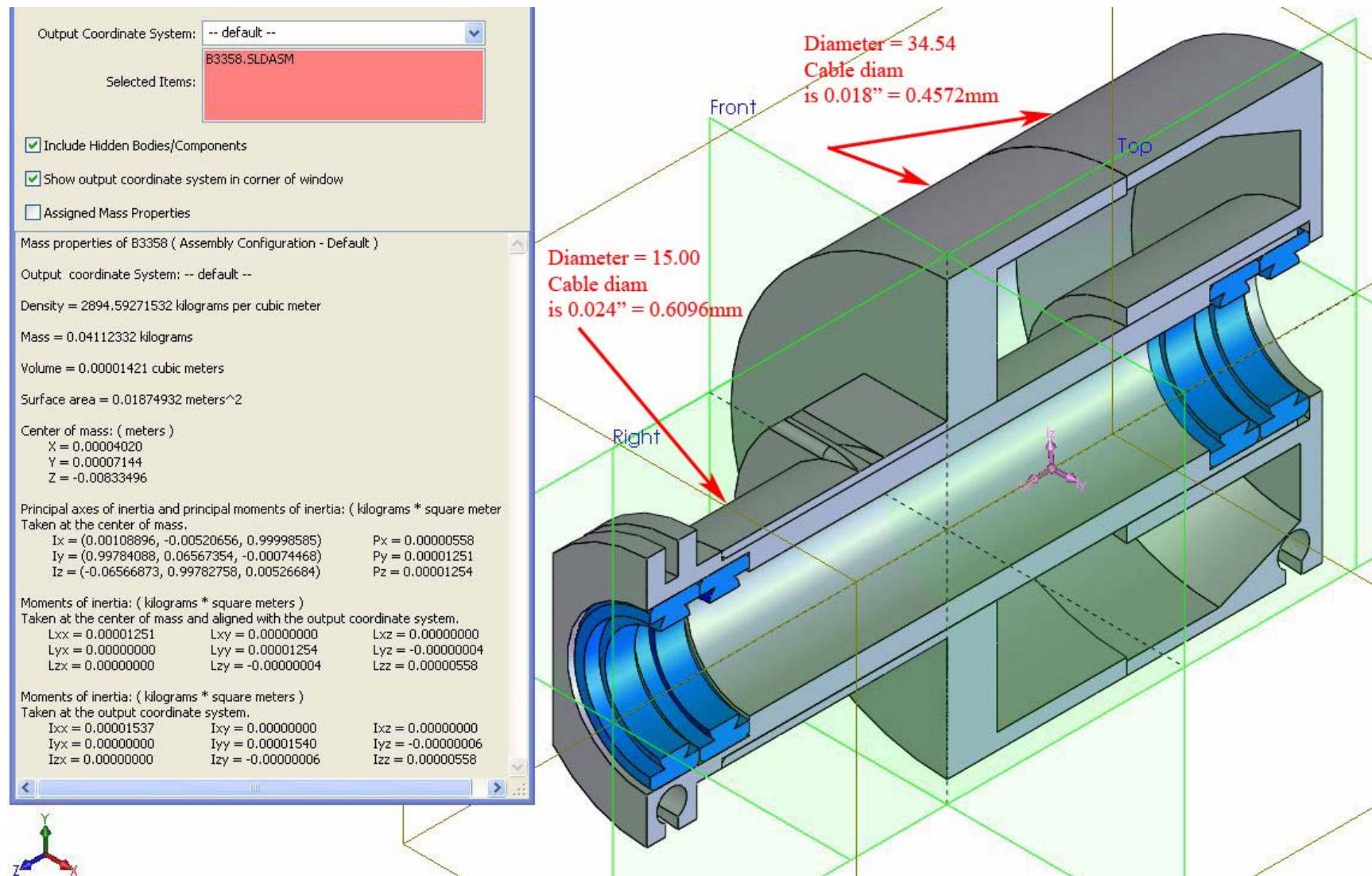


Figure 19 -- Stage-1-2 PulleyPinion.

Table 17 --Mass properties of B3358 (Assembly Configuration - Default)

Density = 2894.59271532 kilograms per cubic meter

Mass = 0.04112332 kilograms

Volume = 0.00001421 cubic meters

Surface area = 0.01874932 meters²

Center of mass: (meters)

$$X = 0.00004020$$

$$Y = 0.00007144$$

$$Z = -0.00833496$$

Principal axes of inertia and principal moments of inertia: (kilograms * square meters)

Taken at the center of mass.

$$I_x = (0.00108896, -0.00520656, 0.99998585) \quad P_x = 0.00000558$$

$$I_y = (0.99784088, 0.06567354, -0.00074468) \quad P_y = 0.00001251$$

$$I_z = (-0.06566873, 0.99782758, 0.00526684) \quad P_z = 0.00001254$$

Moments of inertia: (kilograms * square meters)

Taken at the center of mass and aligned with the output coordinate system.

$$L_{xx} = 0.00001251 \quad L_{xy} = 0.00000000 \quad L_{xz} = 0.00000000$$

$$L_{yx} = 0.00000000 \quad L_{yy} = 0.00001254 \quad L_{yz} = -0.00000004$$

$$L_{zx} = 0.00000000 \quad L_{zy} = -0.00000004 \quad L_{zz} = 0.00000558$$

Moments of inertia: (kilograms * square meters)

Taken at the output coordinate system.

$$I_{xx} = 0.00001537 \quad I_{xy} = 0.00000000 \quad I_{xz} = 0.00000000$$

$$I_{yx} = 0.00000000 \quad I_{yy} = 0.00001540 \quad I_{yz} = -0.00000006$$

$$I_{zx} = 0.00000000 \quad I_{zy} = -0.00000006 \quad \underline{I_{zz} = 0.00000558}$$

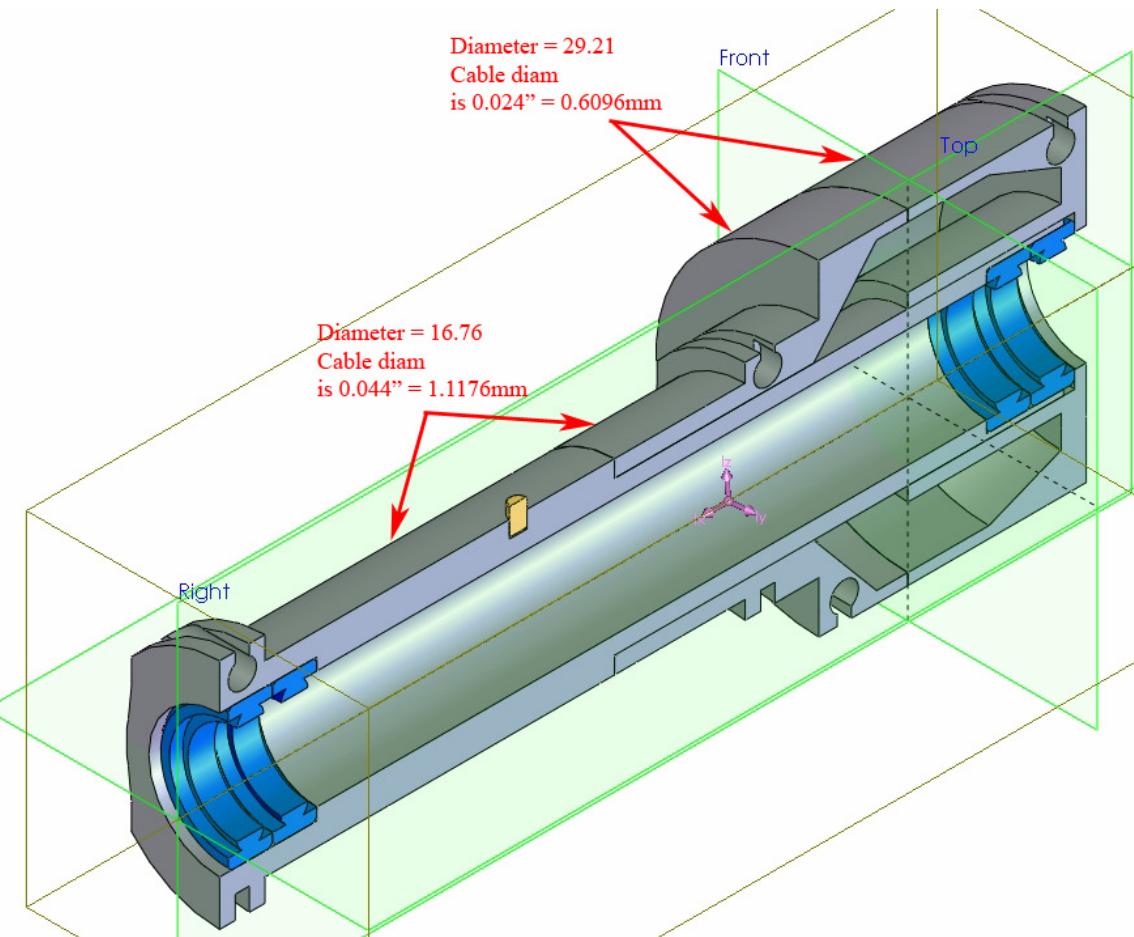
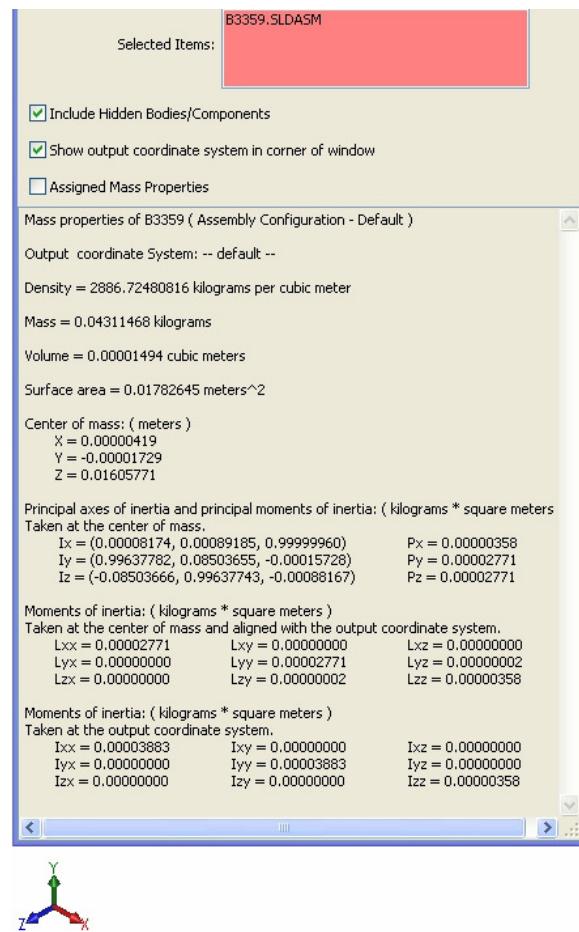


Figure 20 –Stage2-3 PulleyPinion.

Table 18 --Mass properties of B3359 (Assembly Configuration - Default)

Density = 2886.72480816 kilograms per cubic meter

Mass = 0.04311468 kilograms

Volume = 0.00001494 cubic meters

Surface area = 0.01782645 meters²

Center of mass: (meters)

$$X = 0.00000419$$

$$Y = -0.00001729$$

$$Z = 0.01605771$$

Principal axes of inertia and principal moments of inertia: (kilograms * square meters)

Taken at the center of mass.

$$I_x = (0.00008174, 0.00089185, 0.99999960) \quad P_x = 0.00000358$$

$$I_y = (0.99637782, 0.08503655, -0.00015728) \quad P_y = 0.00002771$$

$$I_z = (-0.08503666, 0.99637743, -0.00088167) \quad P_z = 0.00002771$$

Moments of inertia: (kilograms * square meters)

Taken at the center of mass and aligned with the output coordinate system.

$$L_{xx} = 0.00002771 \quad L_{xy} = 0.00000000 \quad L_{xz} = 0.00000000$$

$$L_{yx} = 0.00000000 \quad L_{yy} = 0.00002771 \quad L_{yz} = 0.00000002$$

$$L_{zx} = 0.00000000 \quad L_{zy} = 0.00000002 \quad L_{zz} = 0.00000358$$

Moments of inertia: (kilograms * square meters)

Taken at the output coordinate system.

$$I_{xx} = 0.00003883 \quad I_{xy} = 0.00000000 \quad I_{xz} = 0.00000000$$

$$I_{yx} = 0.00000000 \quad I_{yy} = 0.00003883 \quad I_{yz} = 0.00000000$$

$$I_{zx} = 0.00000000 \quad I_{zy} = 0.00000000 \quad \underline{I_{zz} = 0.00000358}$$

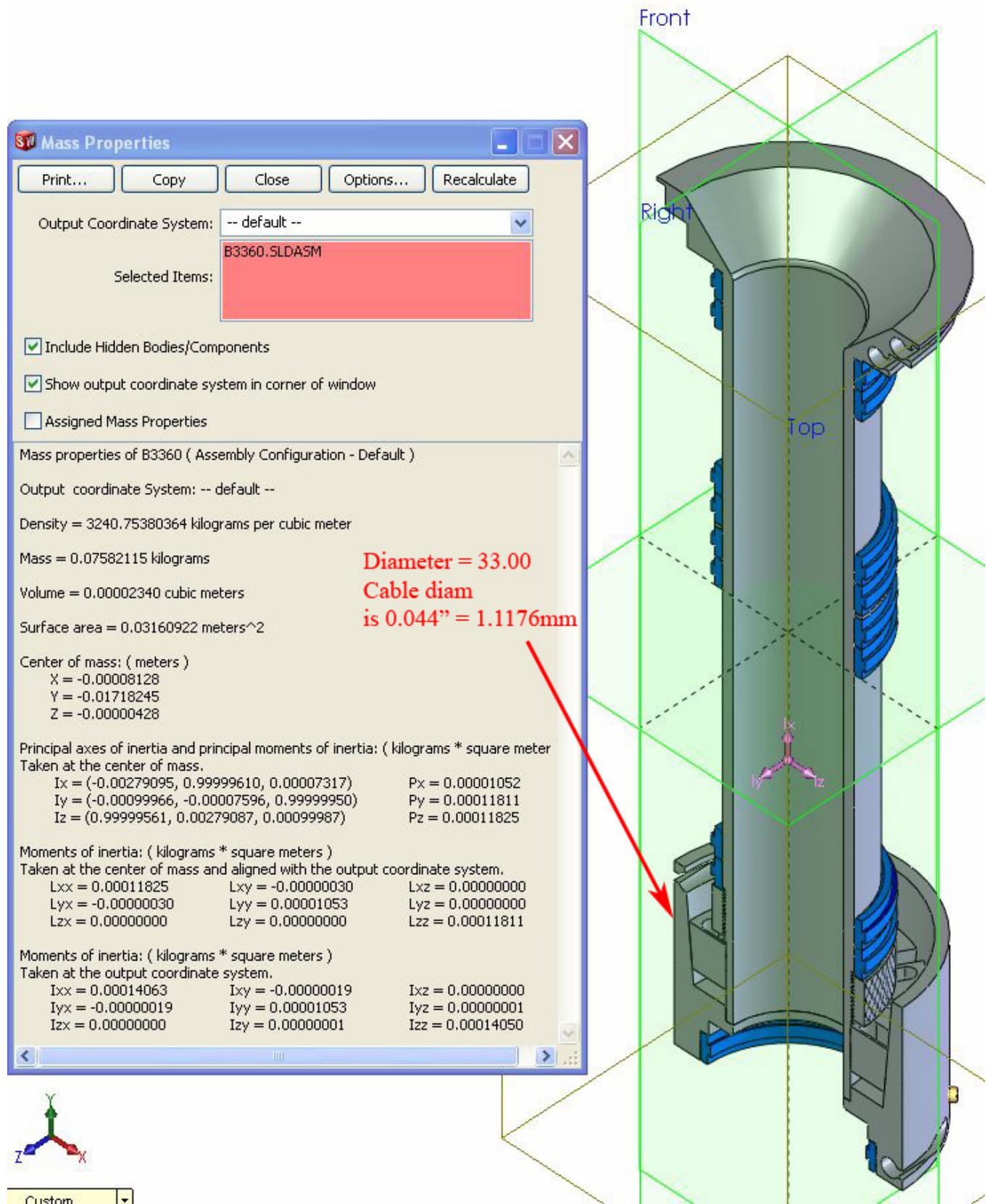


Figure 21 -- Wrist differential outer input-pulley pair driven by Motor 5.

Table 19 -- Mass properties of B3360 (Assembly Configuration - Default)

Density = 3240.75380364 kilograms per cubic meter

Mass = 0.07582115 kilograms

Volume = 0.00002340 cubic meters

Surface area = 0.03160922 meters²

Center of mass: (meters)

X = -0.00008128

Y = -0.01718245

Z = -0.00000428

Principal axes of inertia and principal moments of inertia: (kilograms * square meters)

Taken at the center of mass.

I_x = (-0.00279095, 0.99999610, 0.00007317) P_x = 0.00001052

I_y = (-0.00099966, -0.00007596, 0.99999950) P_y = 0.00011811

I_z = (0.99999561, 0.00279087, 0.00099987) P_z = 0.00011825

Moments of inertia: (kilograms * square meters)

Taken at the center of mass and aligned with the output coordinate system.

L_{xx} = 0.00011825 L_{xy} = -0.00000030 L_{xz} = 0.00000000

L_{yx} = -0.00000030 L_{yy} = 0.00001053 L_{yz} = 0.00000000

L_{zx} = 0.00000000 L_{zy} = 0.00000000 L_{zz} = 0.00011811

Moments of inertia: (kilograms * square meters)

Taken at the output coordinate system.

I_{xx} = 0.00014063 I_{xy} = -0.00000019 I_{xz} = 0.00000000

I_{yx} = -0.00000019 **I_{yy} = 0.00001053** I_{yz} = 0.00000001

I_{xz} = 0.00000000 I_{zy} = 0.00000001 I_{zz} = 0.00014050

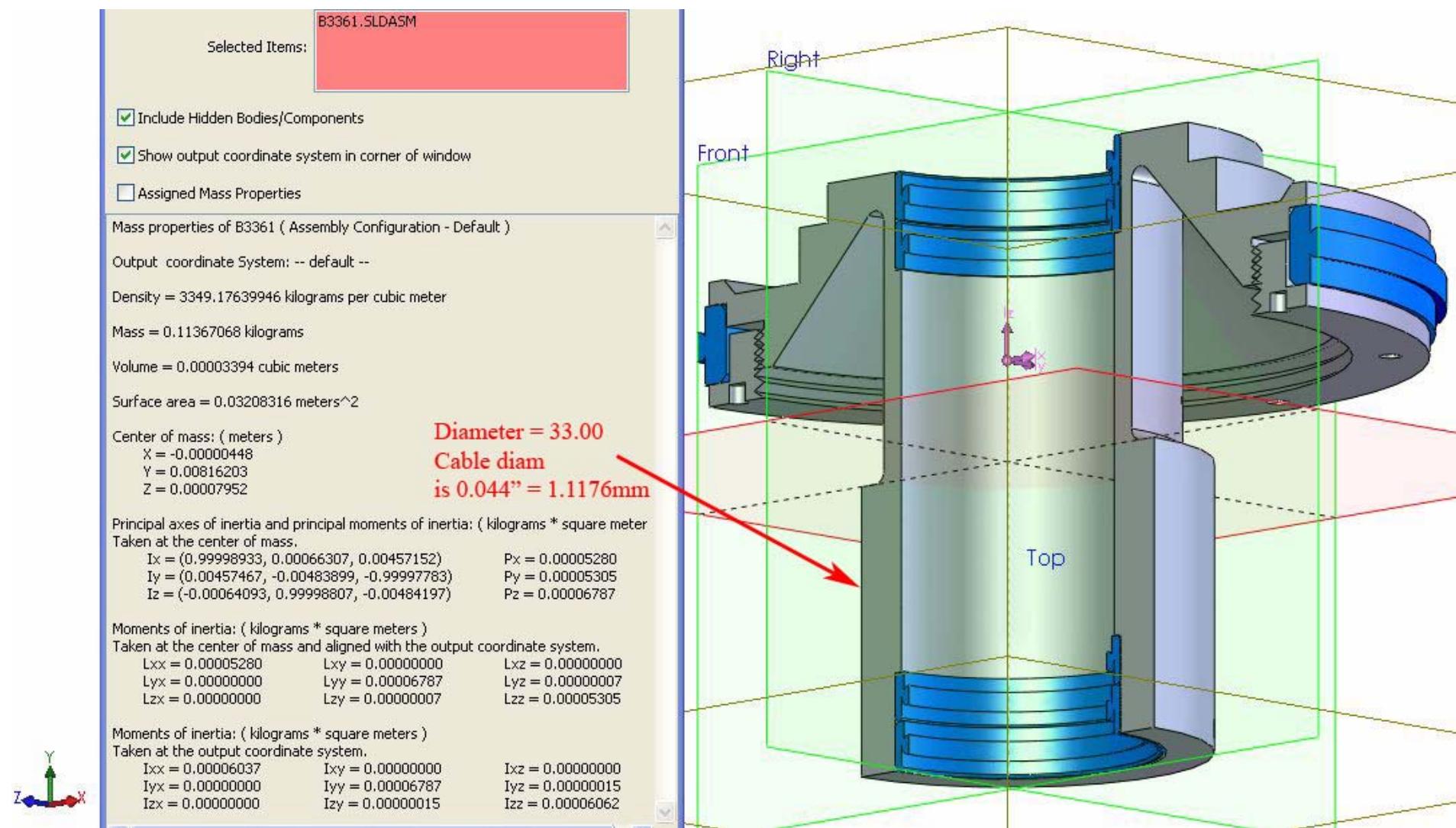


Figure 22 -- Wrist differential inner input-pulley pair driven by Motor 6.

Table 20 -- Mass properties of B3361 (Assembly Configuration - Default)

Density = 3349.17639946 kilograms per cubic meter

Mass = 0.11367068 kilograms

Volume = 0.00003394 cubic meters

Surface area = 0.03208316 meters²

Center of mass: (meters)

$$X = -0.00000448$$

$$Y = 0.00816203$$

$$Z = 0.00007952$$

Principal axes of inertia and principal moments of inertia: (kilograms * square meters)

Taken at the center of mass.

$$I_x = (0.99998933, 0.00066307, 0.00457152) \quad P_x = 0.00005280$$

$$I_y = (0.00457467, -0.00483899, -0.99997783) \quad P_y = 0.00005305$$

$$I_z = (-0.00064093, 0.99998807, -0.00484197) \quad P_z = 0.00006787$$

Moments of inertia: (kilograms * square meters)

Taken at the center of mass and aligned with the output coordinate system.

$$L_{xx} = 0.00005280 \quad L_{xy} = 0.00000000 \quad L_{xz} = 0.00000000$$

$$L_{yx} = 0.00000000 \quad L_{yy} = 0.00006787 \quad L_{yz} = 0.00000007$$

$$L_{zx} = 0.00000000 \quad L_{zy} = 0.00000007 \quad L_{zz} = 0.00005305$$

Moments of inertia: (kilograms * square meters)

Taken at the output coordinate system.

$$I_{xx} = 0.00006037 \quad I_{xy} = 0.00000000 \quad I_{xz} = 0.00000000$$

$$I_{yx} = 0.00000000 \quad \underline{I_{yy} = 0.00006787} \quad I_{yz} = 0.00000015$$

$$I_{zx} = 0.00000000 \quad I_{zy} = 0.00000015 \quad I_{zz} = 0.00006062$$

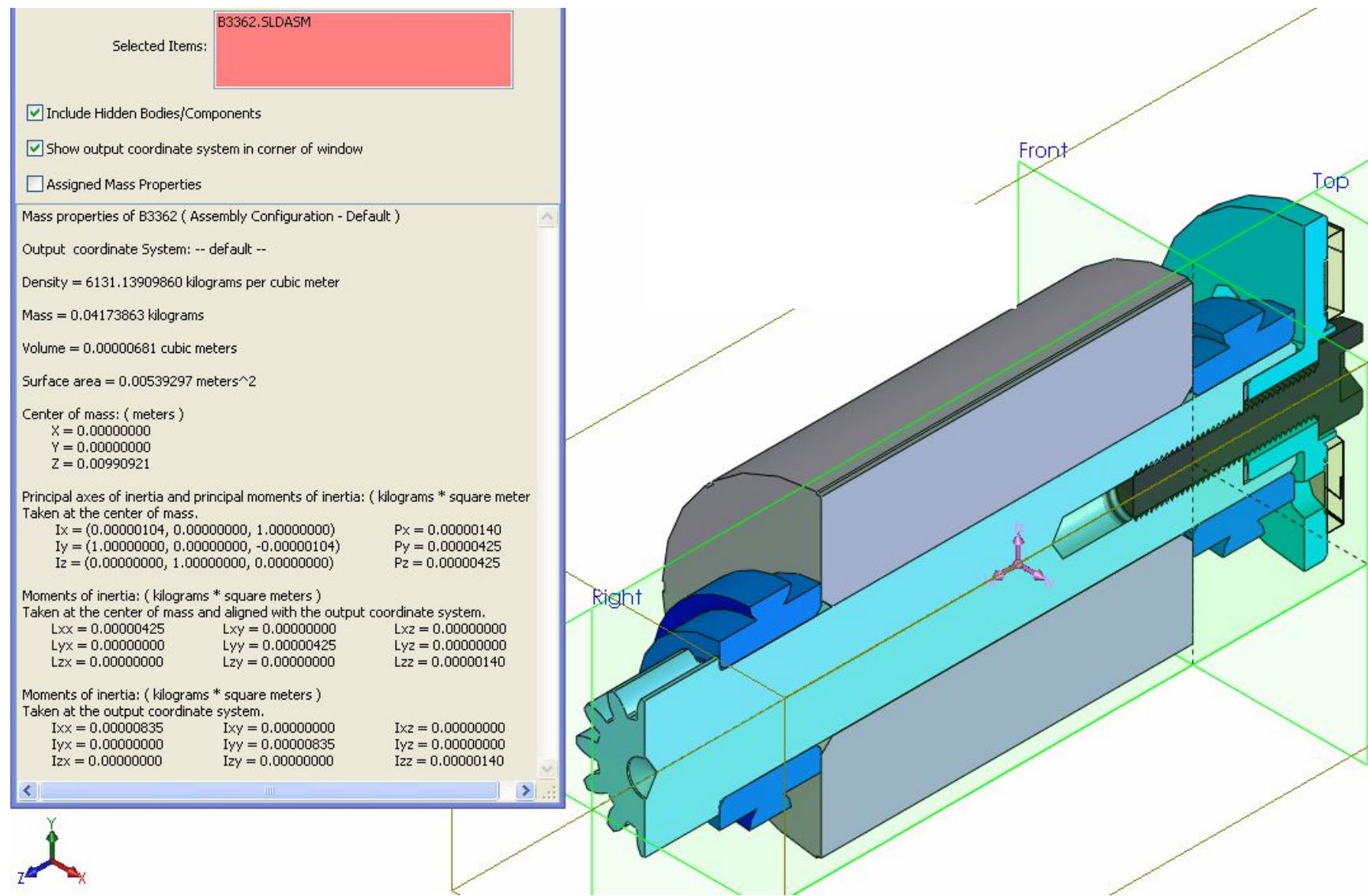


Figure 23 -- Motor-7 Inertia.

Table 21 --Mass properties of B3362 (Assembly Configuration - Default)

Density = 6131.13909860 kilograms per cubic meter

Mass = 0.04173863 kilograms

Volume = 0.00000681 cubic meters

Surface area = 0.00539297 meters²

Center of mass: (meters)

$$X = 0.00000000$$

$$Y = 0.00000000$$

$$Z = 0.00990921$$

Principal axes of inertia and principal moments of inertia: (kilograms * square meters)

Taken at the center of mass.

$$I_x = (0.00000104, 0.00000000, 1.00000000) \quad P_x = 0.00000140$$

$$I_y = (1.00000000, 0.00000000, -0.00000104) \quad P_y = 0.00000425$$

$$I_z = (0.00000000, 1.00000000, 0.00000000) \quad P_z = 0.00000425$$

Moments of inertia: (kilograms * square meters)

Taken at the center of mass and aligned with the output coordinate system.

$$L_{xx} = 0.00000425 \quad L_{xy} = 0.00000000 \quad L_{xz} = 0.00000000$$

$$L_{yx} = 0.00000000 \quad L_{yy} = 0.00000425 \quad L_{yz} = 0.00000000$$

$$L_{zx} = 0.00000000 \quad L_{zy} = 0.00000000 \quad L_{zz} = 0.00000140$$

Moments of inertia: (kilograms * square meters)

Taken at the output coordinate system.

$$I_{xx} = 0.00000835 \quad I_{xy} = 0.00000000 \quad I_{xz} = 0.00000000$$

$$I_{yx} = 0.00000000 \quad I_{yy} = 0.00000835 \quad I_{yz} = 0.00000000$$

$$I_{zx} = 0.00000000 \quad I_{zy} = 0.00000000 \quad \underline{\underline{I_{zz} = 0.00000140}}$$

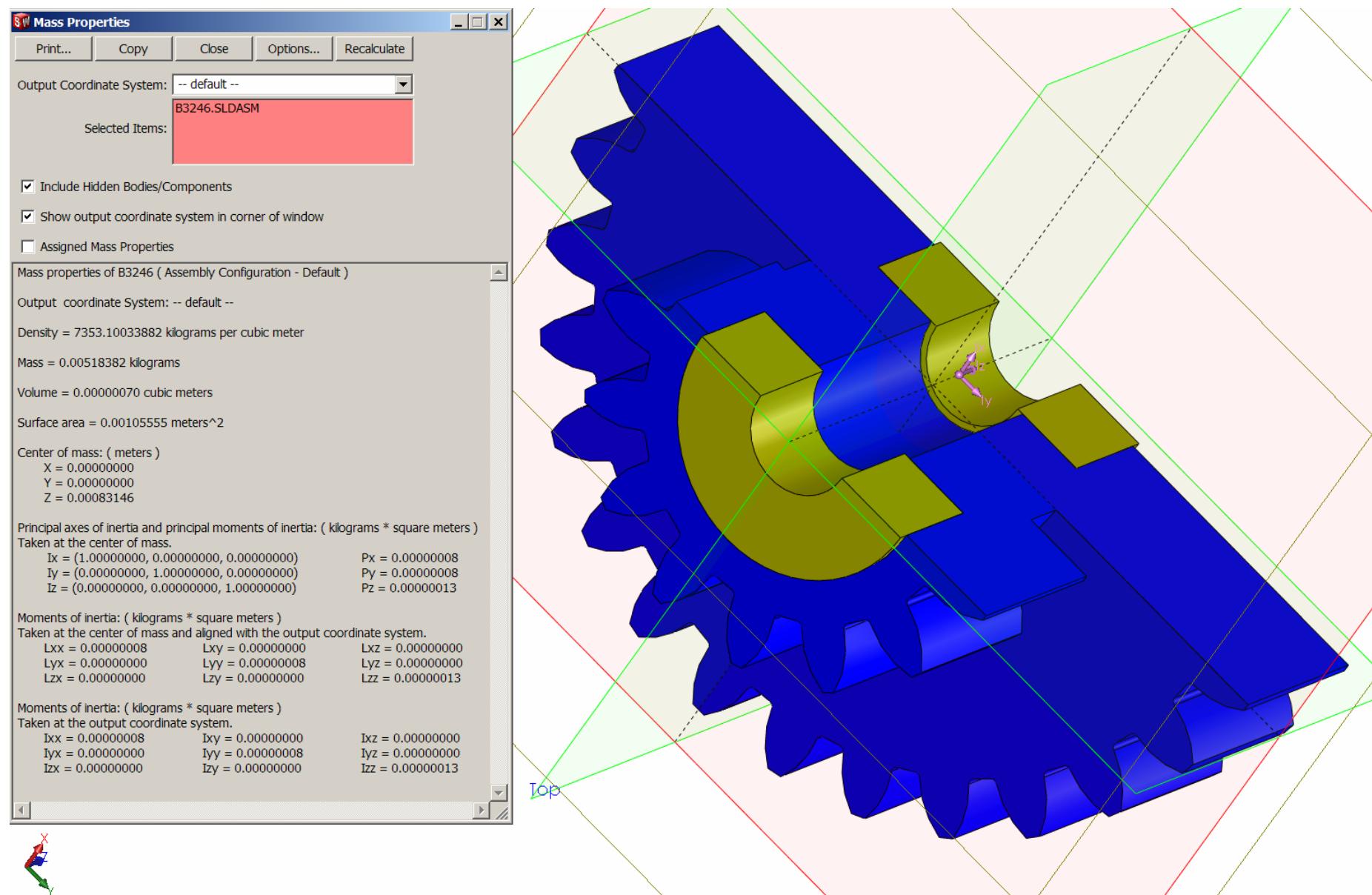
**Figure 24 -- Geared 28/15 reducer.**

Table 22 --Mass properties of B3246 (Assembly Configuration - Default)

Density = 7353.10033882 kilograms per cubic meter

Mass = 0.00518382 kilograms

Volume = 0.00000070 cubic meters

Surface area = 0.00105555 meters²

Center of mass: (meters)

X = 0.00000000

Y = 0.00000000

Z = 0.00083146

Principal axes of inertia and principal moments of inertia: (kilograms * square meters)

Taken at the center of mass.

I_x = (1.00000000, 0.00000000, 0.00000000) P_x = 0.00000008

I_y = (0.00000000, 1.00000000, 0.00000000) P_y = 0.00000008

I_z = (0.00000000, 0.00000000, 1.00000000) P_z = 0.00000013

Moments of inertia: (kilograms * square meters)

Taken at the center of mass and aligned with the output coordinate system.

L_{xx} = 0.00000008 L_{xy} = 0.00000000 L_{xz} = 0.00000000

L_{yx} = 0.00000000 L_{yy} = 0.00000008 L_{yz} = 0.00000000

L_{zx} = 0.00000000 L_{zy} = 0.00000000 L_{zz} = 0.00000013

Moments of inertia: (kilograms * square meters)

Taken at the output coordinate system.

I_{xx} = 0.00000008 I_{xy} = 0.00000000 I_{xz} = 0.00000000

I_{yx} = 0.00000000 I_{yy} = 0.00000008 I_{yz} = 0.00000000

I_{zx} = 0.00000000 I_{zy} = 0.00000000 **I_{zz} = 0.00000013**

Table 23 -- Geometric drive data and transmission ratios.

| | SAVA PN | in | CabDia | Radius Definitions | BT PN | Radii | Dia | AdjDia | Radius | Ratios | | |
|-----------------|--------------------|-----------|---------------|-------------------------------|--------------|--------------|------------|---------------|---------------|-------------------------------|----------------|--------------------|
| | | | mm | | | | mm | mm | mm | | | |
| M1 | SN2047 | 0.044 | 1.1176 | Pinion of Motor Rotor | B2072 | r_m | 16.88 | 18.00 | 9.00 | N_s1 | 3.6670 | |
| | SN2047 | 0.044 | 1.1176 | Pulley of Grenade | B2198 | R_pp | 64.88 | 66.00 | 33.00 | | | |
| | SN2054 | 0.054 | 1.3716 | Pinion of Grenade | B2198 | r_pp | 20.63 | 22.00 | 11.00 | N_s2 | 11.4538 | |
| | SN2054 | 0.054 | 1.3716 | BasePulley | B1898 | R_base | 250.63 | 252.00 | 126.00 | | | |
| | | | | | | | | | | N = N_s1 * N_s2 | 42.0013 | M1 |
| M2&3 | SN2047 | 0.044 | 1.1176 | Pinion of Motor Rotor | B2072 | r_m | 16.88 | 18.00 | 9.00 | N_s1 | 3.6670 | |
| | SN2047 | 0.044 | 1.1176 | Pulley of Grenade | B2198 | R_pp | 64.88 | 66.00 | 33.00 | | | |
| | SN2054 | 0.054 | 1.3716 | Pinion of Grenade | B2198 | r_pp | 20.63 | 22.00 | 11.00 | N_s2 | 7.7041 | |
| | SN2054 | 0.054 | 1.3716 | Pulley of Differential Inputs | B1910 | R_diff | 168.13 | 169.50 | 84.75 | | | |
| | | | | | | | | | | N = N_s1 * N_s2 | 28.2510 | M1 & M2 |
| M4 | SN2047 | 0.044 | 1.1176 | Pinion of Motor Rotor | B2072 | r_m | 16.88 | 18.00 | 9.00 | N_s1 | 3.4448 | |
| | SN2047 | 0.044 | 1.1176 | Pulley of ElbowPulleyPinion | B2196 | R_pp | 60.88 | 62.00 | 31.00 | | | |
| | SN2054 | 0.054 | 1.3716 | Pinion of ElbowPulleyPinion | B2196 | r_pp | 18.53 | 19.90 | 9.95 | N_s2 | 5.2258 | |
| | SN2054 | 0.054 | 1.3716 | ElbowOutputHalfPulleys | B2186/7 | R_diff | 102.63 | 104.00 | 52.00 | | | |
| | | | | | | | | | | N = N_s1 * N_s2 | 18.0016 | M4 |
| M5&6 | SN2019 | 0.018 | 0.4572 | Pinion of Motor Rotor | B3357 | r_m | 12.70 | 13.16 | 6.58 | N_s1 | 2.6599 | |
| | SN2019 | 0.018 | 0.4572 | Pulley of Stage1-2 PP | B3358 | R_pp12 | 34.54 | 35.00 | 17.50 | | | |
| | SN2024 | 0.024 | 0.6096 | Pinion of Stage1-2 PP | B3358 | r_pp12 | 15.00 | 15.61 | 7.80 | N_s2 | 1.9103 | |
| | SN2024 | 0.024 | 0.6096 | Pulley of Stage2-3 PP | B3359 | R_pp23 | 29.21 | 29.82 | 14.91 | | | |
| | SN2047 | 0.044 | 1.1176 | Pinion of Stage2-3 PP | B3359 | r_pp23 | 16.76 | 17.88 | 8.94 | N_s3 | 1.9084 | |
| | SN2047 | 0.044 | 1.1176 | Pulley of Differential Inputs | B3360/1 | R_diff | 33.00 | 34.12 | 17.06 | | | |
| | | | | | | | | | | N = N_s1 * N_s2 * N_s3 | 9.6973 | M5&6 |
| M7 | N/A | | | Pinion of Motor Rotor | B3362 | r_m | 12 | | | N_s1 | 2.3333 | |
| | N/A | | | Idler Gear | B3246 | R_pp | 28 | | | | | |
| | N/A | | | Pinion of Idler Gear | B3246 | r_pp | 15 | | | N_s2 | 6.4000 | |
| | N/A | | | Output Gear | B3347 | R_out | 96 | | | | | |
| | | | | | | | | | | | 14.9333 | M7 |

Table 24 – Inertia of discrete drive components translated to the equivalent inertias (reflected) at each rotor.

| | | BTech | part inertia | cbl masses | cbl radius | inertia w/cbls | stg1 | stg2 | stg3 | inertia@rotor |
|--------------|---------------------------|-------|--------------|------------|------------|----------------|------|-------|------|---------------|
| | | PN | kg-m^2 | kg | m | kg-m^2 | | | | kg-m^2 |
| m1234 | rotor | B3363 | 0.00010064 | 0.011 | 0.009 | 0.00010242 | 1.00 | 1.00 | 1.00 | 0.00010242 |
| m123 | grenade-pp X2 | B2237 | 0.00009183 | 0.013 | 0.011 | 0.00018681 | 3.67 | 1.00 | 1.00 | 0.00001389 |
| m2/3 | diff input | B2331 | 0.00338288 | 0.013 | 0.075 | 0.00352913 | 3.67 | 11.45 | 1.00 | 0.00000200 |
| m4 | elbow pp | B2284 | 0.00005105 | 0.008 | 0.010 | 0.00005263 | 3.44 | 1.00 | 1.00 | 0.00000444 |
| m56 | rotor | B3357 | 0.00001565 | 0.001 | 0.007 | 0.00001574 | 1.00 | 1.00 | 1.00 | 0.00001574 |
| m56a | S12-pp | B3358 | 0.00000558 | 0.002 | 0.008 | 0.00000582 | 2.66 | 1.00 | 1.00 | 0.00000082 |
| m56b | S23-pp | B3359 | 0.00000358 | 0.003 | 0.009 | 0.00000406 | 2.66 | 1.91 | 1.00 | 0.00000016 |
| m5 | diff input (outer) | B3360 | 0.00001053 | 0.003 | 0.018 | 0.00001247 | 2.66 | 1.91 | 1.91 | 0.00000013 |
| m6 | diff input (inner) | B3361 | 0.00006787 | 0.003 | 0.013 | 0.00006888 | 2.66 | 1.91 | 1.91 | 0.00000073 |
| m7 | rotor | B3362 | 0.00000140 | 0.000 | 0 | 0.00000140 | 1.00 | 1.00 | 1.00 | 0.00000140 |
| m7i | rotor | B3246 | 0.00000013 | 0.000 | 0 | 0.00000013 | 2.33 | 1 | 1.00 | 0.00000002 |

Table 25 – Combined total drive inertias by motor number reported both at the motor rotor and at the drive output.

| Drive Number | Summed Components from Previous Table | Inertia@Rotor | Drive Ratio | Inertia@Output |
|--------------|---------------------------------------|---------------|-------------|----------------|
| | | kg-m^2 | | kg-m^2 |
| M1 | m1234 + m123 | 0.00011631 | 42.00 | 0.20518962 |
| M2 | m1234 + m123 + m2/3 | 0.00011831 | 28.25 | 0.09442836 |
| M3 | m1234 + m123 + m2/3 | 0.00011831 | 28.25 | 0.09442836 |
| M4 | m1234 + m4 | 0.00010686 | 18.00 | 0.03462804 |
| M5 | m56 + m56a + m56b + m5 | 0.00001685 | 9.70 | 0.00158448 |
| M6 | m56 + m56a + m56b + m6 | 0.00001745 | 9.70 | 0.00164089 |
| M7 | m7+m7i | 0.00000142 | 14.93 | 0.00031753 |