

# 1 Standard errors

Total covariance matrix

$$\mathbf{K} = \sum_{i=0}^{K-1} a_i \mathbf{K}_i \quad (1)$$

Total variance

$$\sigma^2 = \text{var}(\mathbf{K}) = \frac{1}{N-1} \text{tr}(\mathbf{P}^T \mathbf{K} \mathbf{P}) = \sum_{i=0}^{K-1} a_i \frac{1}{N-1} \text{tr}(\mathbf{P}^T \mathbf{K}_i \mathbf{P}) = \sum_{i=0}^{K-1} a_i \text{var}(\mathbf{K}_i) \quad (2)$$

Fractions of total variance

$$h_i = \frac{a_i \text{var}(\mathbf{K}_i)}{\sigma^2} \quad (3)$$

Change of coordinate

$$\begin{cases} a_k = \frac{h_k \sigma^2}{\text{var}(\mathbf{K}_k)} \\ a_{K-1} = \frac{(1 - \sum_{j=0}^{K-2} h_j) \sigma^2}{\text{var}(\mathbf{K}_{K-1})} \end{cases} \quad (4)$$

Jacobian

$$\mathbf{J} = \left( \frac{\partial(a_0, \dots, a_{K-1})}{\partial(\sigma^2, h_0, \dots, h_{K-2})} \right) = \begin{pmatrix} \frac{h_0}{\text{var}(\mathbf{K}_0)} & \frac{\sigma^2}{\text{var}(\mathbf{K}_0)} & \dots & 0 \\ \vdots & 0 & \ddots & 0 \\ \frac{h_{K-2}}{\text{var}(\mathbf{K}_{K-2})} & 0 & \dots & \frac{\sigma^2}{\text{var}(\mathbf{K}_{K-2})} \\ \frac{h_{K-1}}{\text{var}(\mathbf{K}_{K-1})} & -\frac{\sigma^2}{\text{var}(\mathbf{K}_{K-1})} & \dots & -\frac{\sigma^2}{\text{var}(\mathbf{K}_{K-1})} \end{pmatrix} \quad (5)$$

Transformation of expected fisher information  $\mathbf{F}$ :

$$\mathbf{F}^{(\text{new})} = \mathbf{J}^T \mathbf{F} \mathbf{J} \quad (6)$$