

Problem 1

The tree before prune:

node 0

Top: 6,4, 0.97

Education Level gain = 0.125

Career gain = 0.125

Years of Experience gain = 0.020

Selected Attribute: Education

node 1

High School 4,1, 0.72

Career gain = 0.171

Years of Experience gain = 0.322

Selected Attribute: Years of Experience

node 3

More than 10

Career gain = 1.0

Selected attribute Career

node 8

Management

Class High

node 9

Service

Class Low

node 4

Less than 3

Class Low

node 5

3 to 10

ClassLow

node 2

College 3,2, 0.97

Career gain = 0.420

Years of Experience gain = 0.171

Selected Attribute: Career

node 6
Management
class High

node 7
Service 1,2, 0,91
Years of Experience gain = 0.918
selected attribute: Years of Experience

node 10
More than 10
Class Low

node 11
Less than 3
Class Low

node 12
3 to 10
Class High

puring the tree

for the 1 iteration:

node num: sum_of_total_wrong: wrong_count:

12	0	1
11	0	0
10	0	0
9	0	0
8	0	0
7	1	0

pruning node 7

for the 2 iteration:

node num: sum_of_total_wrong: wrong_count:

9	0	0
8	0	0
7	0	0

6	0	1
5	0	0
4	0	0
3	0	0
2	1	2
1	0	1
0	1	1

The final tree

node 0

Top: 6,4, 0.97

Education Level gain = 0.125

Career gain = 0.125

Years of Experience gain = 0.020

Selected Attribute: Education

node 1

High School 4,1, 0.72

Career gain = 0.171

Years of Experience gain = 0.322

Selected Attribute: Years of Experience

node 3

More than 10

Career gain = 1.0

Selected attribute Career

node 8

Management

Class High

node 9

Service

Class Low

node 4

Less than 3

Class Low

node 5

3 to 10

ClassLow

node 2

College 3,2, 0.97

Career gain = 0.420

Years of Experience gain = 0.171

Selected Attribute: Career

node 6

Management

class High

node 7

Service 1,2, 0.91

Years of Experience gain = 0.918

selected attribute: Years of Experience

Class Low

Problem2

The answer of this problem is also stored in “prob2.csv” file in result directory.

6.7,3.1,4.4,1.4,x1,versicolor,versicolor,versicolor,versicolor,versicolor
4.4,3.2,1.3,0.2,x2,setosa,setosa,setosa,setosa,setosa
5.3,3.7,1.5,0.2,x3,setosa,setosa,setosa,setosa,setosa
7.7,2.8,6.7,2.0,x10,virginica,virginica,virginica,virginica,virginica
5.1,3.5,1.4,0.2,x11,setosa,setosa,setosa,setosa,setosa
6.5,3.0,5.2,2.0,x12,setosa,virginica,virginica,virginica,virginica
7.1,3.0,5.9,2.1,x13,virginica,virginica,virginica,virginica,virginica
6.4,2.7,5.3,1.9,x14,virginica,virginica,virginica,virginica,virginica
5.2,2.7,3.9,1.4,x15,versicolor,versicolor,versicolor,versicolor,versicolor
7.0,3.2,4.7,1.4,x16,virginica,versicolor,versicolor,versicolor,versicolor
7.2,3.2,6.0,1.8,x17,virginica,virginica,virginica,virginica,virginica
5.4,3.7,1.5,0.2,x19,setosa,setosa,setosa,setosa,setosa
5.6,3.0,4.5,1.5,x20,versicolor,versicolor,versicolor,versicolor,versicolor
5.9,3.2,4.8,1.8,x21,versicolor,versicolor,versicolor,versicolor,versicolor
5.1,3.4,1.5,0.2,x22,setosa,setosa,setosa,setosa,setosa
6.9,3.1,4.9,1.5,x23,versicolor,versicolor,versicolor,versicolor,versicolor
6.0,2.2,4.0,1.0,x24,versicolor,versicolor,versicolor,versicolor,versicolor
4.7,3.2,1.6,0.2,x25,setosa,setosa,setosa,setosa,setosa
4.6,3.6,1.0,0.2,x27,setosa,setosa,setosa,setosa,setosa
5.6,3.0,4.1,1.3,x31,versicolor,versicolor,versicolor,versicolor,versicolor
5.5,3.5,1.3,0.2,x33,setosa,setosa,setosa,setosa,setosa
5.5,2.4,3.8,1.1,x34,versicolor,versicolor,versicolor,versicolor,versicolor
5.1,3.8,1.6,0.2,x35,setosa,setosa,setosa,setosa,setosa
6.3,3.3,4.7,1.6,x36,versicolor,versicolor,versicolor,versicolor,versicolor
6.6,2.9,4.6,1.3,x100,versicolor,versicolor,versicolor,versicolor,versicolor
7.7,3.0,6.1,2.3,x101,virginica,virginica,virginica,virginica,virginica
6.4,2.9,4.3,1.3,x102,versicolor,versicolor,versicolor,versicolor,versicolor
6.9,3.1,5.1,2.3,x103,virginica,virginica,virginica,virginica,virginica
6.7,3.0,5.0,1.7,x104,setosa,versicolor,versicolor,versicolor,versicolor
4.3,3.0,1.1,0.1,x105,setosa,setosa,setosa,setosa,setosa
7.7,2.6,6.9,2.3,x106,virginica,virginica,virginica,virginica,virginica
6.7,3.3,5.7,2.5,x107,virginica,virginica,virginica,virginica,virginica
6.7,2.5,5.8,1.8,x108,virginica,virginica,virginica,virginica,virginica
1.0,3.1,1.6,0.2,x109,setosa,setosa,setosa,setosa,setosa
5.7,4.4,1.5,0.4,x110,setosa,setosa,setosa,setosa,setosa
6.5,3.0,5.5,1.8,x111,setosa,virginica,virginica,virginica,virginica
6.1,3.0,4.9,1.8,x112,versicolor,versicolor,versicolor,versicolor,versicolor
5.4,3.4,1.7,0.2,x113,setosa,setosa,setosa,setosa,setosa

6.5,3.2,5.1,2.0,x114, virginica, virginica, virginica, virginica, virginica
5.2,3.4,1.4,0.2,x115, setosa, setosa, setosa, setosa, setosa
5.7,3.0,4.2,1.2,x116, versicolor, versicolor, versicolor, versicolor, versicolor
5.5,2.3,4.0,1.3,x117, versicolor, versicolor, versicolor, versicolor, versicolor
5.0,3.4,1.6,0.4,x118, setosa, setosa, setosa, setosa, setosa
5.8,2.7,5.1,1.9,x119, virginica, virginica, virginica, virginica, virginica
6.1,2.8,4.0,1.3,x120, versicolor, versicolor, versicolor, versicolor, versicolor
5.7,2.5,5.0,2.0,x121, virginica, virginica, virginica, virginica, virginica
6.3,2.9,5.6,1.8,x122, versicolor, virginica, virginica, virginica, virginica
4.9,3.1,1.5,0.1,x123, setosa, setosa, setosa, setosa, setosa
6.8,3.2,5.9,2.3,x124, virginica, virginica, virginica, virginica, virginica
6.9,3.2,5.7,2.3,x125, virginica, virginica, virginica, virginica, virginica
6.7,3.1,4.7,1.5,x126, versicolor, versicolor, versicolor, versicolor, versicolor
5.7,2.8,4.1,1.3,x127, versicolor, versicolor, versicolor, versicolor, versicolor
5.0,3.5,1.6,0.6,x128, setosa, setosa, setosa, setosa, setosa
5.4,3.9,1.7,0.4,x129, setosa, setosa, setosa, setosa, setosa
5.2,3.5,1.5,0.2,x130, setosa, setosa, setosa, setosa, setosa
6.1,2.8,4.7,1.2,x131, versicolor, versicolor, versicolor, versicolor, versicolor
5.7,2.9,4.2,1.3,x132, versicolor, versicolor, versicolor, versicolor, versicolor
5.8,2.7,3.9,1.2,x133, versicolor, versicolor, versicolor, versicolor, versicolor
5.0,3.3,1.4,0.2,x134, setosa, setosa, setosa, setosa, setosa
6.8,2.8,4.8,1.4,x135, versicolor, versicolor, versicolor, versicolor, versicolor
6.3,2.8,5.1,1.5,x136, versicolor, versicolor, versicolor, versicolor, versicolor
6.2,2.2,4.5,1.5,x137, virginica, versicolor, versicolor, versicolor, versicolor
6.0,3.0,4.8,1.8,x138, versicolor, versicolor, versicolor, versicolor, versicolor
5.1,3.5,1.4,0.3,x139, setosa, setosa, setosa, setosa, setosa
5.7,3.8,1.7,0.3,x140, setosa, setosa, setosa, setosa, setosa
6.1,3.0,4.6,1.4,x141, versicolor, versicolor, versicolor, versicolor, versicolor
5.8,4.0,1.2,0.2,x142, setosa, setosa, setosa, setosa, setosa
7.2,3.6,6.1,2.5,x143, virginica, virginica, virginica, virginica, virginica
6.1,2.6,5.6,1.4,x144, versicolor, versicolor, versicolor, versicolor, versicolor
5.5,2.5,4.0,1.3,x145, versicolor, versicolor, versicolor, versicolor, versicolor
7.3,2.9,6.3,1.8,x146, virginica, virginica, virginica, virginica, virginica
4.8,3.0,1.4,0.1,x147, setosa, setosa, setosa, setosa, setosa
7.6,3.0,6.6,2.1,x148, virginica, virginica, virginica, virginica, virginica
6.5,3.0,5.8,2.2,x149, virginica, virginica, virginica, virginica, virginica
5.1,3.3,1.7,0.5,x150, setosa, setosa, setosa, setosa, setosa

Problem 3

=====

poly-kernel

exponent = 1

result:

=== Confusion Matrix ===

a b <-- classified as

356 73 | a = car

56 361 | b = noncar

correct 717

incorect 129

=====

poly-kernel

exponent = 2

result:

=== Confusion Matrix ===

a b <-- classified as

408 21 | a = car

15 402 | b = noncar

correct 810

incorrect 36

=====

poly-kernel

exponent = 4

result:

=== Confusion Matrix ===

a b <-- classified as

401 28 | a = car

27 390 | b = noncar

correct 791

incorrect 55

=====

rbf kernel

gamma = 0.01

result:

=== Confusion Matrix ===

a b <-- classified as

267 162 | a = car

```
70 347 |    b = noncar
correct 614
incorrect 232
```

```
=====
rbf kernel
gamma = 1
result:
=== Confusion Matrix ===
a    b    <-- classified as
373  56 |    a = car
26 391 |    b = noncar
correct 764
incorrect 82
```

From the result, poly kernel, when exponent equals 2, the number of correct instances is greater than the number of correct instances when exponent equals to 1 and 4. For rbf kernel when gamma equals to 1 the number of correct instances is greater than the number of correct instances when gamma equals to 0.01

The kernel function map the original data set to a high dimension data set. If the higher dimension data set could be separated, the SVM would achieve a better result. So for the poly kernel, when exponent equals to 2 the mapped data is more separable than the mapped data when exponent equals to 1 and 4. For the same reason, when gamma eqs to 1 the mapped data is more separable than the mapped data when gamma eqs to 0.01

Problem 4

Let support $\Phi(x) = \Phi(x_1, x_2) = x_1 + e^{x^2}$, then $K(x, z) = K(x_1, x_2, z_1, z_2) = \Phi(x) * \Phi(z)$. From the definition of kernel we can see that $K(x, x) = \Phi(x)^2$. So that $K(x, z) = x_1 * z_1 + x_1 * e^{z^2} + z_1 * e^{x^2} + e^{x^2} + z_2$ is kernel.

Problem 5

Because $a_0 = -0.8$, $a_1 = 1$, $a_2 = 6.4$, $a_3 = -1.9$, so $[1,1,1]$ and $[1,1,0]$ are support vectors.

$$\mathbf{w} = \sum_{\mathbf{x}_i \in SV} \alpha_i y_i \mathbf{x}_i$$

Because , so that $\mathbf{w} = [5, 4, -1, -1]^T$, and according to

$$y_i(\mathbf{w}^T \mathbf{x}_i + b) = 1$$

, so $b = -4.4$.

To classify $[1, 0.8, 1]$, we apply the formula $\mathbf{w}^T * \mathbf{x} + b$, which equals to -0.8 . So we can conclude that even the tuple $[1, 0.8, 1]$ lies between the support vectors, it still closer to the negative class. $[1, 0.8, 1]$ is labeled with class -1.