# Project1 Documentation

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August 24, 2015

#### 1 Model

Neurons are modeled as conductance-based leaky integrate-and-fire units. The membrane potential  $V_i^{\alpha}$  of the *i*-th neuron  $(i=1,\cdots,N_{\alpha})$  from population  $\alpha=E,I,X$  (excitatory, inhibitory and external population, respectively) evolves according to

$$C_m \frac{dV_i^{\alpha}}{dt} = -g_L(V_i^{\alpha} - V_L) + I_{i,syn}^{\alpha}(t) + I_{i,app}^{\alpha}(t), \text{ if } V_i^{\alpha} < V_{th}$$

$$\tag{1.1}$$

When neurons reach the threshold  $V_{th}$ , a spike is emitted and they are reset to  $V_{rt}$  for an absolute refractory period  $\tau_{ref}$ . The spike times  $t_i^{\alpha}$  are recorded. The synaptic currents received by a neuron are given by

$$I_{i,syn}^{\alpha}(t) = \sum_{\beta=1}^{P} I_{i}^{\alpha\beta}(t)$$
(1.2)

$$= \sum_{\beta=1}^{P} \left[ -g_i^{\alpha\beta} (V_i^{\alpha} - V_{rev}^{\beta}) \right] \tag{1.3}$$

$$= \sum_{\beta=1}^{P} \{ -[\sum_{i=1}^{N_{\beta}} a_{ij}^{\alpha\beta} g_{ij}^{\alpha\beta} s_{ij}^{\alpha\beta}(t)] (V_i^{\alpha} - V_{rev}^{\beta}) \}$$
 (1.4)

where  $V_{rev}^{\beta}$  is the reversal potential of the corresponding current  $I_i^{\alpha\beta}$  induced by pre-synaptic population  $\beta$  and mathematically models the excitatory/inhibitory nature of it.  $a_{ij}^{\alpha\beta}$  is a binary variable which determines the existence of synapse from the j-th neuron in population  $\beta$  to the i-th neuron in population  $\alpha$ , while  $g_{ij}^{\alpha\beta}$  reflects the (maximal) strength of the synaptic conductance. The gating variable  $s_{ij}^{\alpha\beta}(t)$  models the instananeous value of synaptic conductance in terms of the fraction of open channels, described by

| $\alpha$                           | $\mathbf{E}$ | I   |
|------------------------------------|--------------|-----|
| $\tau_r^{\alpha} \text{ (ms)}$     | 1            | 1   |
| $\tau_d^{\alpha} \; (\mathrm{ms})$ | 5            | 3   |
| $V_{rev}^{\alpha}$ (mV)            | 0            | -80 |
| $\tau_{ref} \; (\mathrm{ms})$      | 2            |     |
| $C_m$ (nF)                         | 0.25         |     |
| $g_L \; (\mu { m S})$              | 0.0167       |     |
| $V_L (\mathrm{mV})$                | -70          |     |
| $V_{rt} (\mathrm{mV})$             | -60          |     |
| $\theta (\mathrm{mV})$             | -50          |     |

Table 1: Model constants

$$\frac{ds_{ij}^{\alpha\beta}}{dt} = -\frac{s_{ij}^{\alpha\beta}}{\tau_d^{\beta}} + \sum_{t_j^{\beta}} h^{\beta} (t - t_j^{\beta} - d_{ij}^{\alpha\beta}) (1 - s_{ij}^{\alpha\beta}) \tag{1.5}$$

where h models the concentration time-course of the channel-opening neurotransmitters, arrived with a conduction delay  $d_{ij}^{\alpha\beta}$  after the pre-synaptic spike time  $t_j^{\beta}$ . The  $(1-s_{ij}^{\alpha\beta})$  term introduces saturation effect. Following the simplification in [1], a rectangular pulse with unitary area is used for h

$$h(t) = \begin{cases} 1/\tau_r, & \text{if } 0 \le t \le \tau_r \\ 0, & \text{otherwise} \end{cases}$$
 (1.6)

The default parameters are summarized in Table 1. All numerical values are in consistant units unless mentioned otherwise (ms for time, mV for voltage, nA for current, nF for capacitance and  $\mu$ S for conductance). Numerical integration is performed using Euler method with a time-step of 0.1 ms [2].

# 2 Input File Format

The input files are text files. The default input filename is "input\_filename.ygin". It is advised that synapse definitions always be given in a separate file. The default synapse definition filename is "input\_filename.ygin\_syn". Non-default synapse definition file path and name can be specified by "SYNF001" command. Input data format is as following.

```
> INIT001 # number of neurons in each population N1, N2, ...,
```

```
> INIT003 # random initial distributions for V
        p_fire_pop1 (range (0,1]), ..., p_fire_popN,
> INIT004 # external Gaussian currents
        pop_ind, mean (nA), std (nA),
> INIT005 # external Poissonian spikes
        pop_ind, type_ext, K_ext (\muS), Num_ext, ia, ib,
        \verb|rate_1| (\verb|Hz|), \verb|rate_2|, \ldots, \verb|rate_step_tot|
> INIT006 # chemical connection definition
        type, pop_ind_pre, pop_ind_post,
        I (row vector),
        J (row vector),
        K (row vector),
        D (row vector),
> SYNF001 # non-default synapse definition file name
        path/to/file_name (no comma!)
> KILL001 # runaway killer setting
        pop_ind, min_ms, runaway_Hz, Hz_ms,
> PARA001 # non-default neuron population parameter
        pop_ind, number_of_parameters,
        parameter_name1, value1,
        parameter_name2, value2,
> PARA002 # non-default synapse parameter
        number_of_parameters,
        parameter_name1, value1,
        parameter_name2, value2,
> SAMP001 # neuron data sampling
        pop_ind,
        data_type (logical vector),
        ind1, ind2, ..., indX, (sample neuron indices)
        1, 1, 0, 0, ..., (1-by-step_tot logical values)
        # Note that data_type specifies sample data types
        # and it must correspond to
        # [V,I_leak,I_AMPA,I_GABA,I_NMDA,I_GJ,I_ext]
> SAMP002 # synapse data sampling
        pop_ind_pre, pop_ind_post, syn_type,
        ind1, ind2, ..., indX, (post-synaptic sample neuron indices)
        1, 1, 0, 0, ..., (1-by-step_tot logical values)
```

> SAMP003 # neuron population statistical data record

```
pop_ind,
```

> SAMP004 # synaptic currents statistical data record
 pop\_ind\_pre, pop\_ind\_post, syn\_type,

### 3 Output File Format

The output files are text files. The default output filename is "input\_filename-time\_stamp.ygout". For data completeness, the corresponding input file will be attached to the output file. The output data format is as following.

```
> KILL002 # step at which runaway activity is killed
        step_killed,
> POPD001 # spike history of neuron population
        pop_ind,
        spike_neuron_ind (row vector),
        num_spikes_t (1-by-step_tot row vector),
        num_ref_t (1-by-step_tot row vector),
> POPD002 # neuron parameters in the population
        pop_ind, number_of_parameters,
        parameter_name1, value1,
        parameter_name2, value2,
> POPD003 # neuron population statistical data
        pop_ind,
        V_mean_t1, V_mean_t2, ... (1-by-step_tot)
        V_std_t1, V_std_t2, ... (1-by-step_tot)
        I_input_mean_t1, I_input_mean_t2, ... (1-by-step_tot)
        I\_input\_std\_t1\,,\ I\_input\_std\_t2\,,\ \dots\ (1-by-step\_tot)
> POPD004 # sampled neuron data
        pop_ind, number_of_sample_neurons,
        data_name1, ..., data_nameX,
        data_1 (sampled_neurons-by-sampled_steps matrix),
        data_2 (sampled_neurons-by-sampled_steps matrix),
        data_X (sampled_neurons-by-sampled_steps matrix),
> POPD005 # time average of input currents for each neuron
        pop_ind,
        I_{input_avg_1}, I_{input_avg_2}, ... (1-by-N),
> SYND001 # synaptic connection parameters
        number_of_parameters,
        parameter_name1, value1,
```

#### References

- [1] Alain Destexhe, Zachary F Mainen, and Terrence J Sejnowski. An efficient method for computing synaptic conductances based on a kinetic model of receptor binding. *Neural Computation*, 6(1):14–18, 1994.
- [2] Ashok Litwin-Kumar and Brent Doiron. Slow dynamics and high variability in balanced cortical networks with clustered connections. *Nature neuroscience*, 15(11):1498–1505, 2012.