

Apêndice B. MATRIZ DE TRANSFORMAÇÃO T

A multiplicação das matrizes n matrizes de transformação homogênea resulta em

$$T_n^0 = \prod_{i=1}^n A_i = \begin{bmatrix} r_{11} & r_{12} & r_{13} & d_x \\ r_{21} & r_{22} & r_{23} & d_y \\ r_{31} & r_{22} & r_{33} & d_z \\ 0 & 0 & 0 & 1 \end{bmatrix} \quad (\text{B.1})$$

na qual os termos são

$$r_{11} = \left[\left[((-s_1 s_3 + c_1 c_2 c_3) c_4 + s_2 s_4 c_1) c_5 + (-s_1 c_3 - s_3 c_1 c_2) s_5 \right] c_6 + ((-s_1 s_3 + c_1 c_2 c_3) s_4 - s_2 c_1 c_4) s_6 \right] c_7 + \left[- \left[(-s_1 s_3 + c_1 c_2 c_3) c_4 + s_2 s_4 c_1 \right] s_5 + (-s_1 c_3 - s_3 c_1 c_2) c_5 \right] s_7 \quad (\text{B.2})$$

$$r_{12} = - \left[\left[((-s_1 s_3 + c_1 c_2 c_3) c_4 + s_2 s_4 c_1) c_5 + (-s_1 c_3 - s_3 c_1 c_2) s_5 \right] c_6 + ((-s_1 s_3 + c_1 c_2 c_3) s_4 - s_2 c_1 c_4) s_6 \right] s_7 + \left[- \left[(-s_1 s_3 + c_1 c_2 c_3) c_4 + s_2 s_4 c_1 \right] s_5 + (-s_1 c_3 - s_3 c_1 c_2) c_5 \right] c_7 \quad (\text{B.3})$$

$$r_{13} = \left[((-s_1 s_3 + c_1 c_2 c_3) c_4 + s_2 s_4 c_1) c_5 + (-s_1 c_3 - s_3 c_1 c_2) s_5 \right] s_6 - ((-s_1 s_3 + c_1 c_2 c_3) s_4 - s_2 c_1 c_4) c_6 \quad (\text{B.4})$$

$$r_{21} = \left[\left[((s_1 c_2 c_3 + s_3 c_1) c_4 + s_1 s_2 s_4) c_5 + (-s_1 s_3 c_2 + c_1 c_3) s_5 \right] c_6 + ((s_1 c_2 c_3 + s_3 c_1) s_4 - s_1 s_2 c_4) s_6 \right] c_7 + \left[- \left[(s_1 c_2 c_3 + s_3 c_1) c_4 + s_1 s_2 s_4 \right] s_5 + (-s_1 s_3 c_2 + c_1 c_3) c_5 \right] s_7 \quad (\text{B.5})$$

$$r_{22} = - \left[\left[((s_1 c_2 c_3 + s_3 c_1) c_4 + s_1 s_2 s_4) c_5 + (-s_1 s_3 c_2 + c_1 c_3) s_5 \right] c_6 + ((s_1 c_2 c_3 + s_3 c_1) s_4 - s_1 s_2 c_4) s_6 \right] s_7 + \left[- \left[(s_1 c_2 c_3 + s_3 c_1) c_4 + s_1 s_2 s_4 \right] s_5 + (-s_1 s_3 c_2 + c_1 c_3) c_5 \right] c_7 \quad (\text{B.6})$$

$$r_{23} = \left[\left[(s_1 c_2 c_3 + s_3 c_1) c_4 + s_1 s_2 s_4 \right] c_5 + (-s_1 s_3 c_2 + c_1 c_3) s_5 \right] s_6 - \left[(s_1 c_2 c_3 + s_3 c_1) s_4 - s_1 s_2 c_4 \right] c_6 \quad (\text{B.7})$$

$$r_{31} = \left[((-s_2 c_3 c_4 + s_4 c_2) c_5 + s_2 s_3 s_5) c_6 + (-s_2 s_4 c_3 - c_2 c_4) s_6 \right] c_7 + \left[- (-s_2 c_3 c_4 + s_4 c_2) s_5 + s_2 s_3 c_5 \right] s_7 \quad (\text{B.8})$$

$$r_{32} = - \left[((-s_2 c_3 c_4 + s_4 c_2) c_5 + s_2 s_3 s_5) c_6 + (-s_2 s_4 c_3 - c_2 c_4) s_6 \right] s_7 + \left[- (-s_2 c_3 c_4 + s_4 c_2) s_5 + s_2 s_3 c_5 \right] c_7 \quad (\text{B.9})$$

$$r_{33} = \left[(-s_2 c_3 c_4 + s_4 c_2) c_5 + s_2 s_3 s_5 \right] s_6 - (-s_2 s_4 c_3 - c_2 c_4) c_6 \quad (\text{B.10})$$

$$d_x = 90 \left[((-s_1 s_3 + c_1 c_2 c_3) c_4 + s_2 s_4 c_1) c_5 + (-s_1 c_3 - s_3 c_1 c_2) s_5 \right] s_6 - 90 \left[(-s_1 s_3 + c_1 c_2 c_3) s_4 - s_2 c_1 c_4 \right] c_6 - 400 (-s_1 s_3 + c_1 c_2 c_3) s_4 + 400 s_2 c_1 c_4 + 420 s_2 c_1 \quad (\text{B.11})$$

$$d_y = 90 \left[((s_1 c_2 c_3 + s_3 c_1) c_4 + s_1 s_2 s_4) c_5 + (-s_1 s_3 c_2 + c_1 c_3) s_5 \right] s_6 - 90 \left[(s_1 c_2 c_3 + s_3 c_1) s_4 - s_1 s_2 c_4 \right] c_6 - 400 (s_1 c_2 c_3 + s_3 c_1) s_4 + 400 s_1 s_2 c_4 + 420 s_1 s_2 \quad (\text{B.12})$$

$$d_z = 90 \left[(-s_2 c_3 c_4 + s_4 c_2) c_5 + s_2 s_3 s_5 \right] s_6 - 90 (-s_2 s_4 c_3 - c_2 c_4) c_6 + 400 s_2 s_4 c_3 + 400 c_2 c_4 + 420 c_2 + 360 \quad (\text{B.13})$$