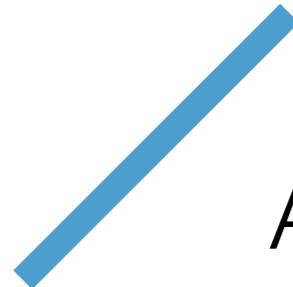


Redes Complejas

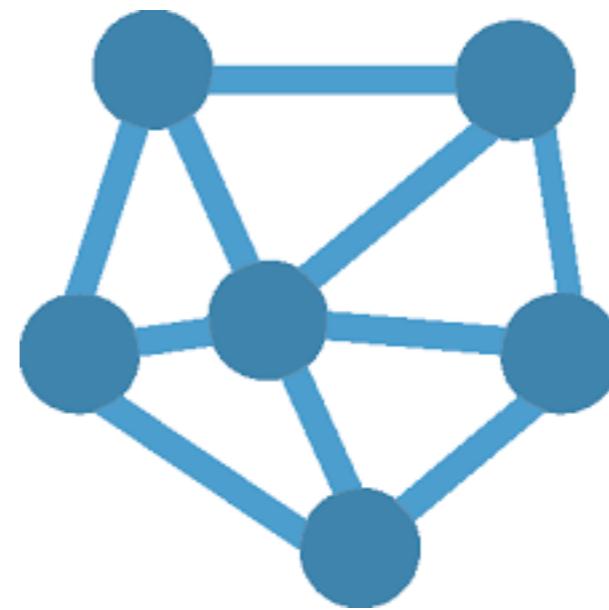
Redes - Grafos



Vértices (*Nodes*)



Aristas (*Edges*)

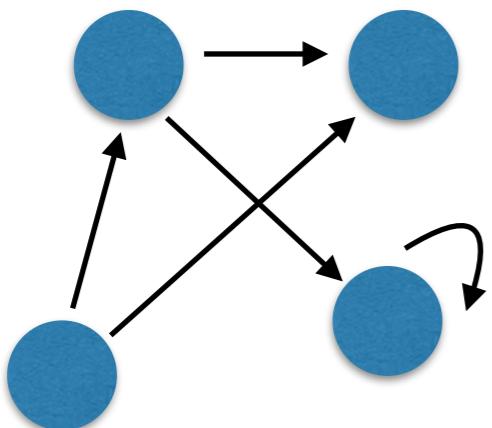


Red

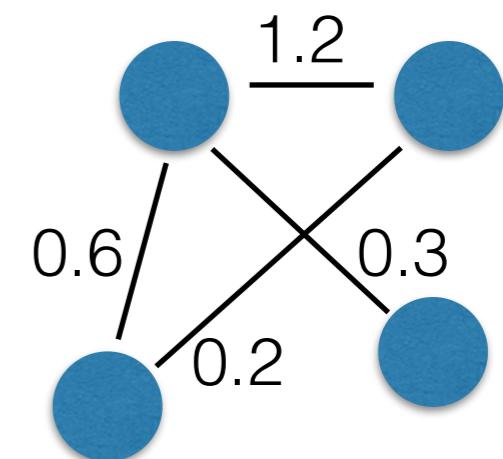
Traveling salesman, Erdös, Dijkstra, ...

Tipos de grafos

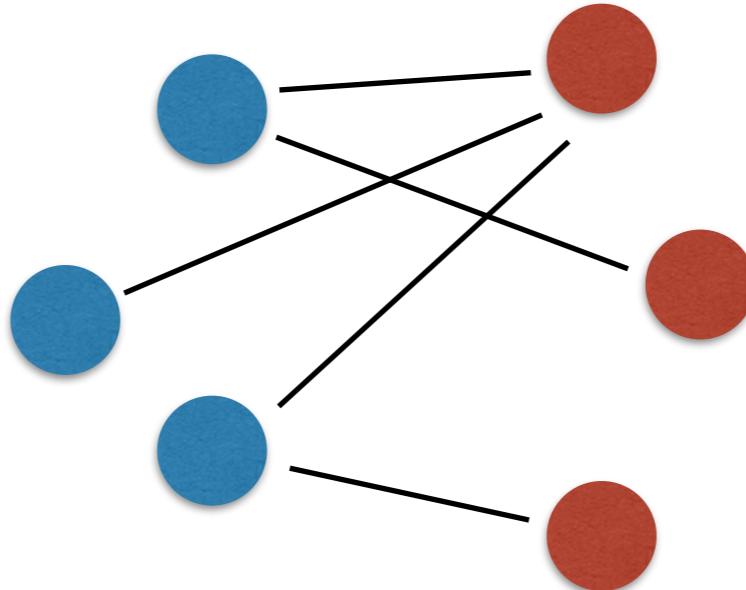
Dirigidos



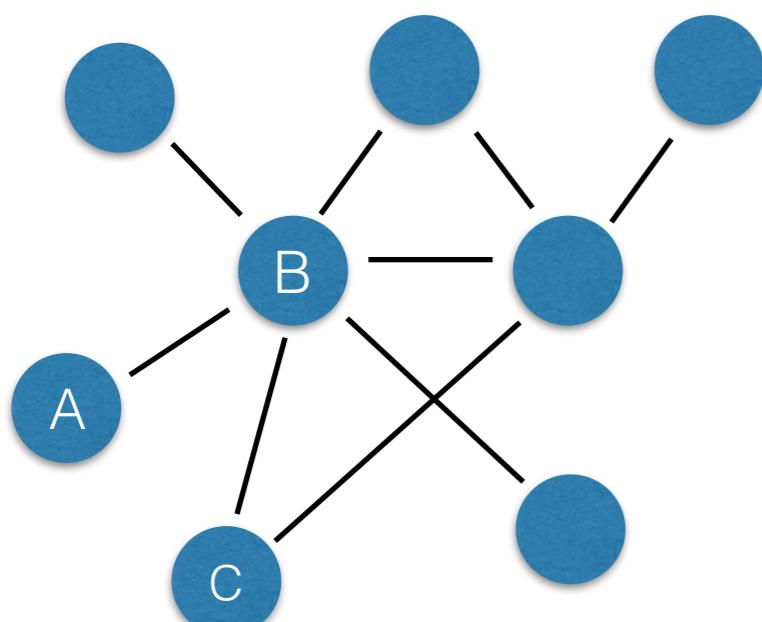
Pesados



Bipartitos



Representando Grafos

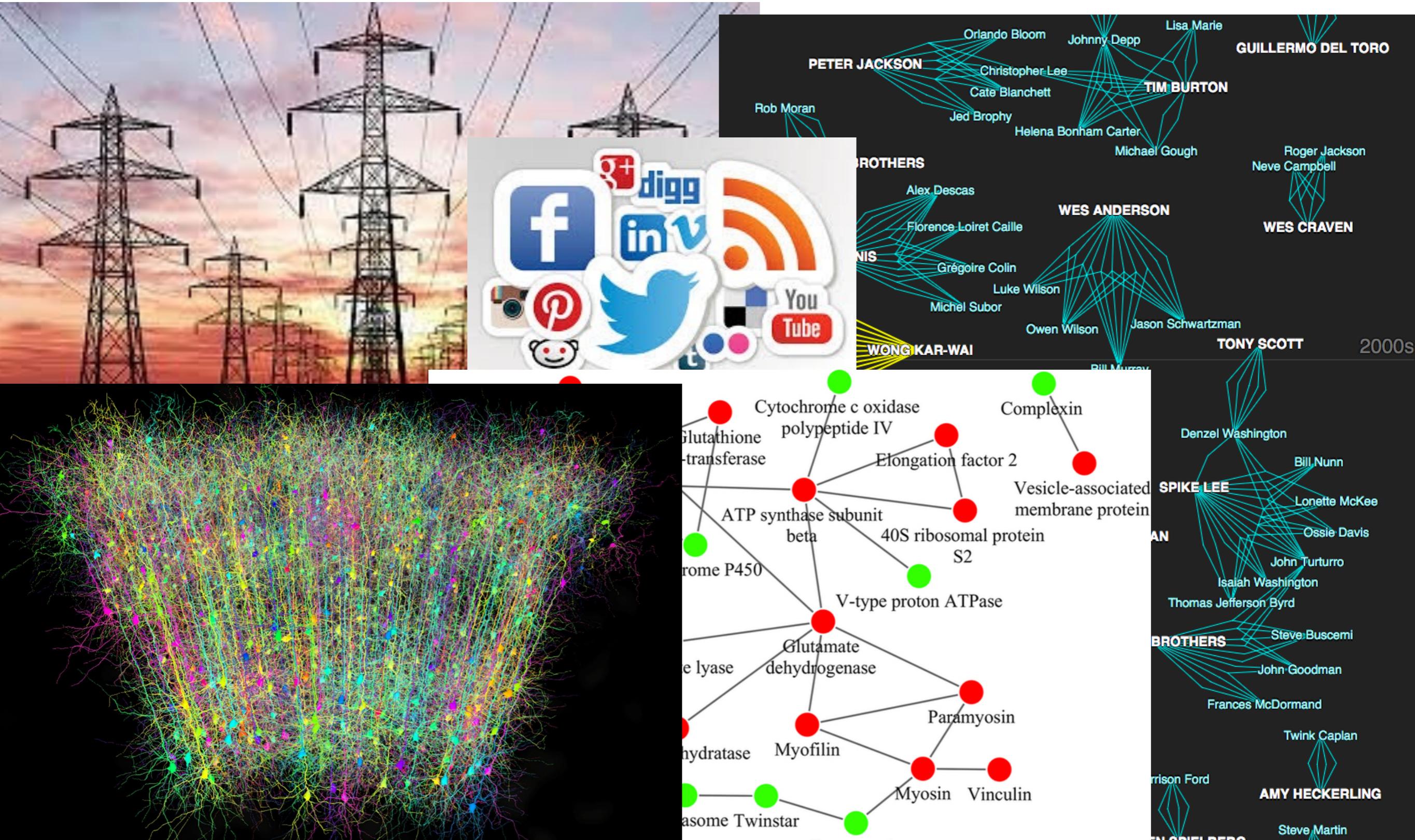


Matriz de adyacencia

Lista de aristas
(A,B), (B,C), ...

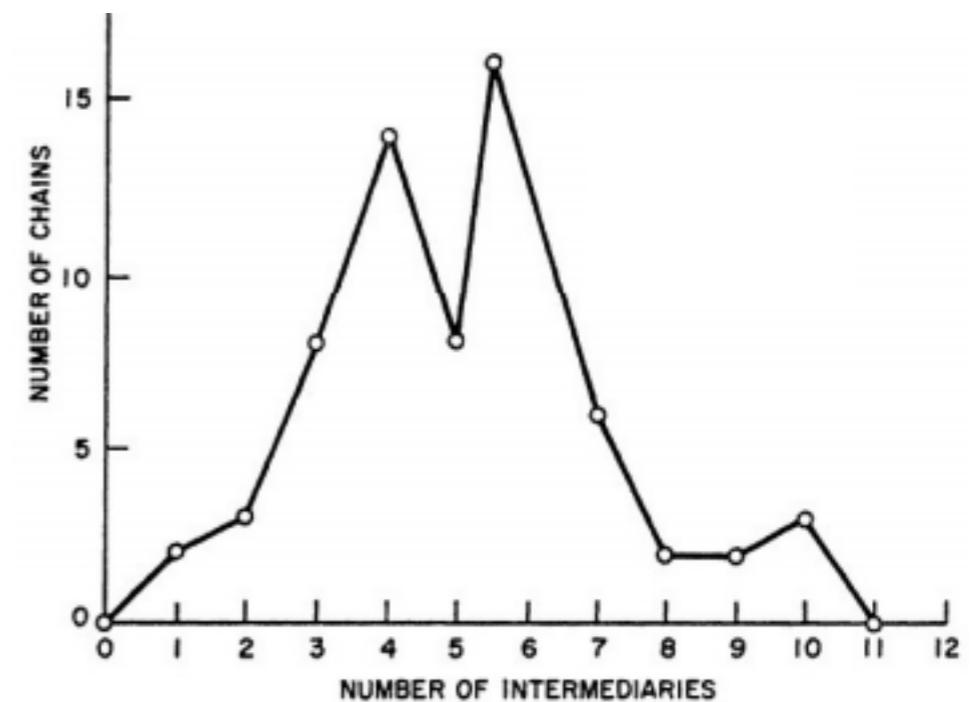
Nodos	A	B	C
A	0	1	0
B	1	0	1
C	0	1	0

Redes en el mundo



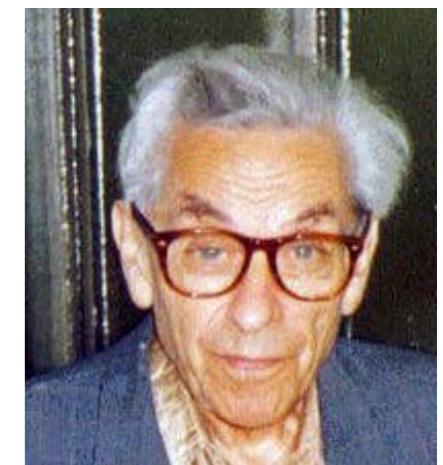
Seis grados de separación: El experimento de Milgram (1967)

- 300 personas al azar en ciertas ciudades de EE.UU.
- Se les pedía que le hagan llegar una carta a un agente de bolsa en Boston, pero sólo mandándola a amigos/concidos
- Se midió cuántos pasos eran necesarios para llegar



Seis grados de separación

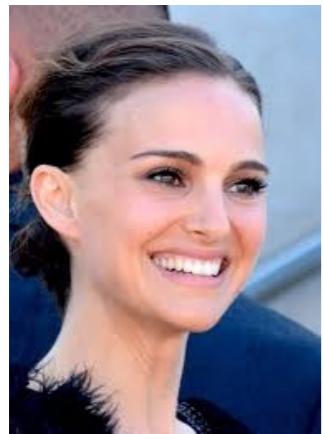
Número de Erdös (1969): número de pasos hasta llegar Erdös via coautoría de artículos



Número de Bacon: número de pasos hasta llegar Kevin Bacon via coparticipación en películas



Número de Erdös-Bacon: suma de ambos



Mundos Pequeños

- Cada persona conectada con 100 amigos
- A dos pasos, llegamos a $100 \times 100 = 10000$ personas
- A 5 pasos, 10^5 personas.. ¡todo el mundo!

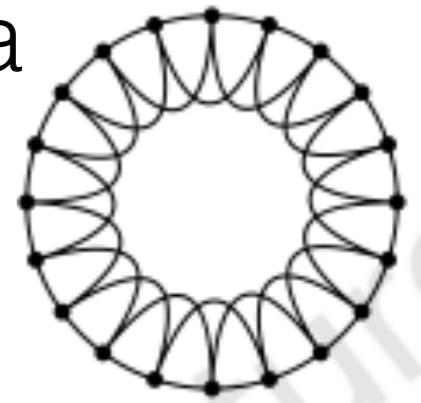
...pero qué está mal?

¡Los amigos de mis amigos son amigos entre sí!

No tan aleatoria...



sino más ordenada



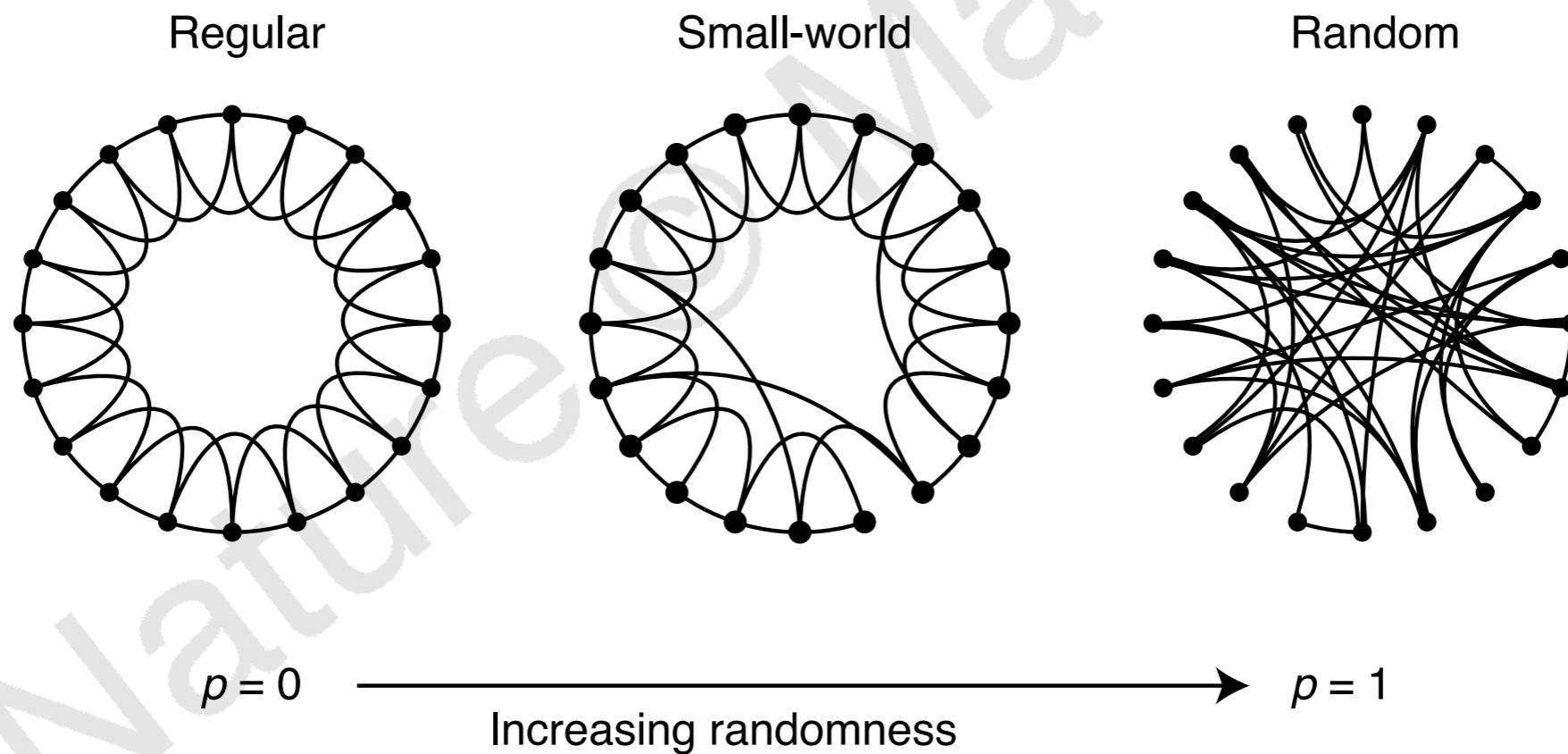
Mundos Pequeños

1998

Collective dynamics of 'small-world' networks

Duncan J. Watts* & Steven H. Strogatz

Department of Theoretical and Applied Mechanics, Kimball Hall,
Cornell University, Ithaca, New York 14853, USA



Mundos Pequeños

Clustering y Longitud de camino medio

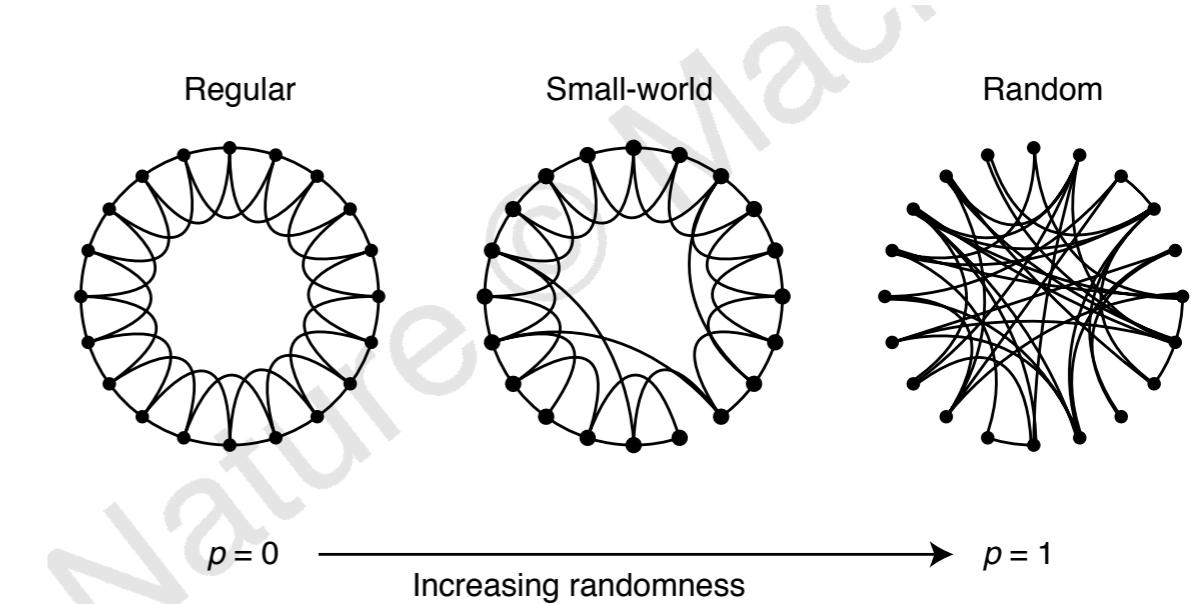
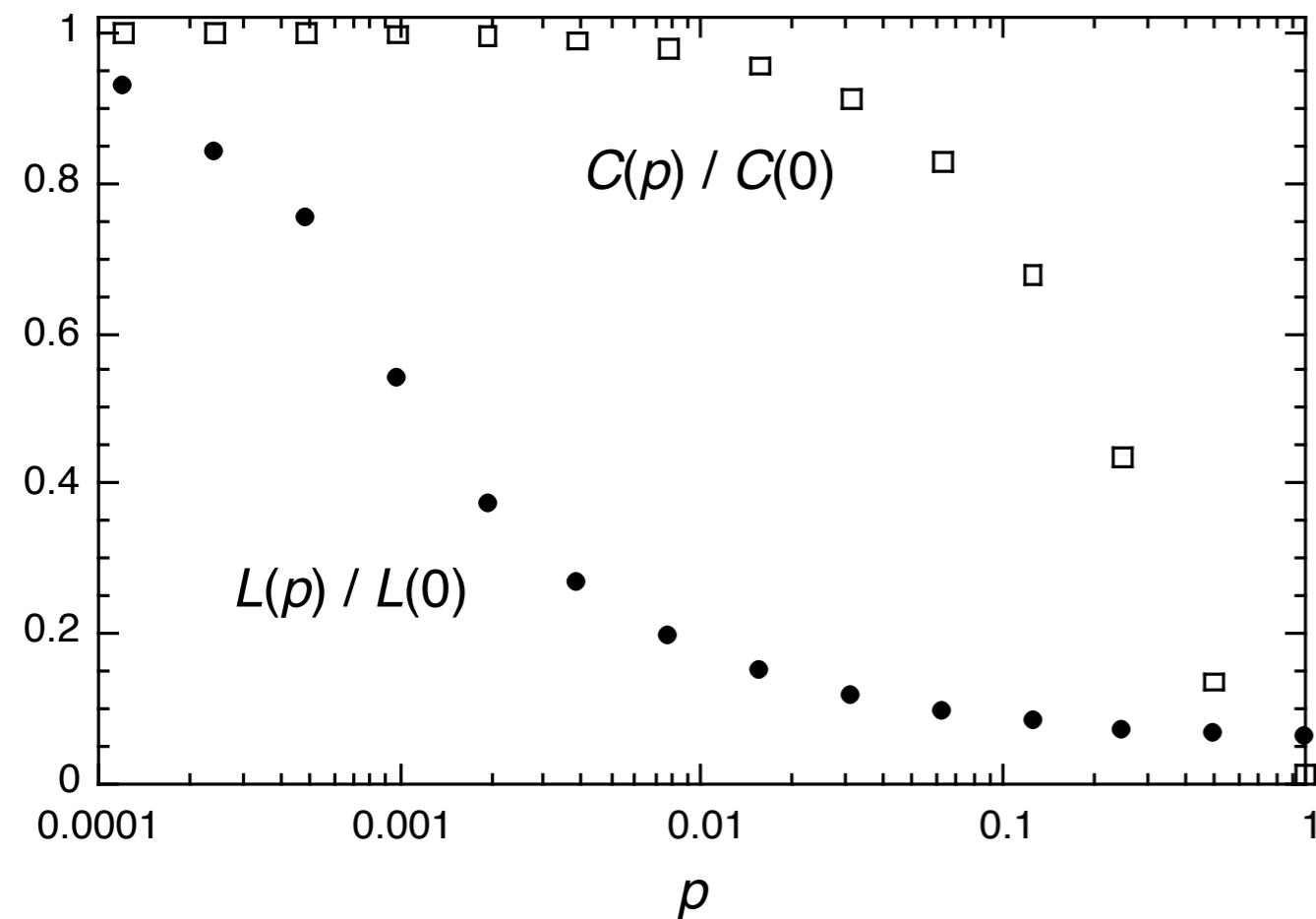
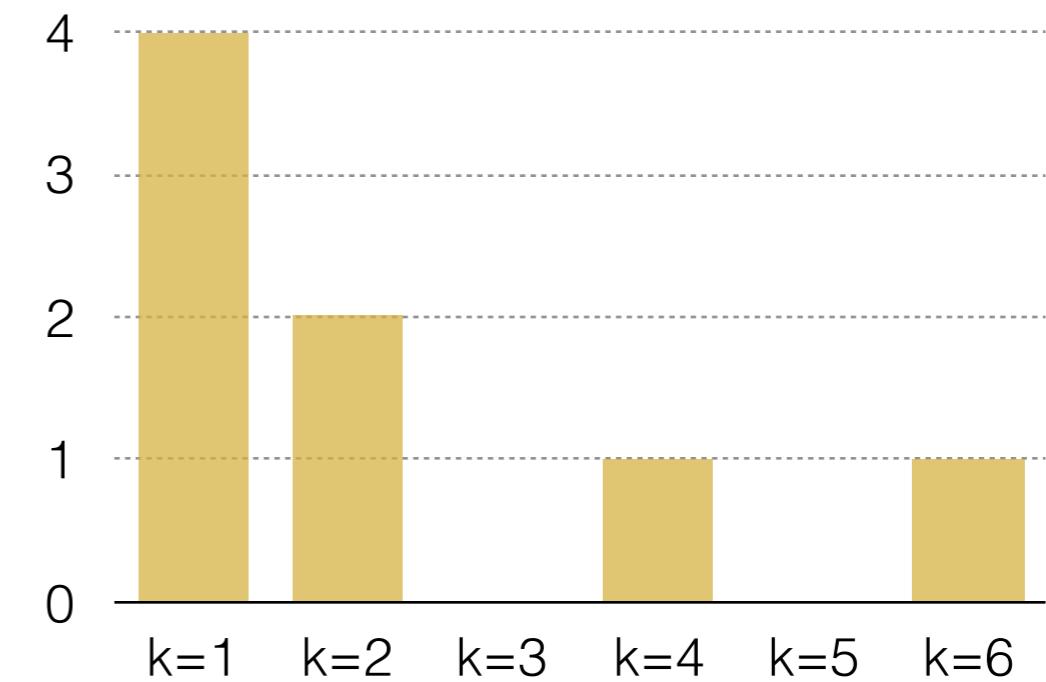
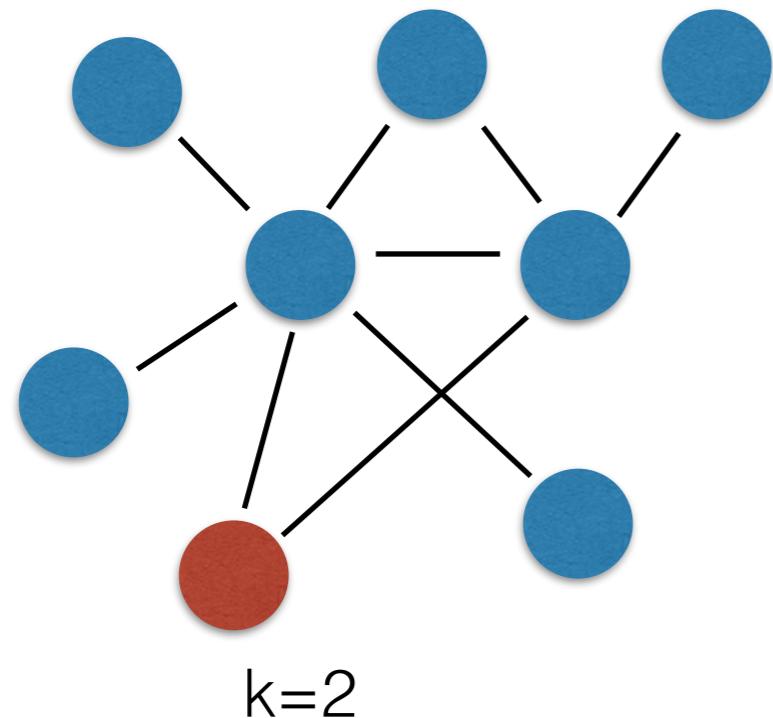


Table 1 Empirical examples of small-world networks

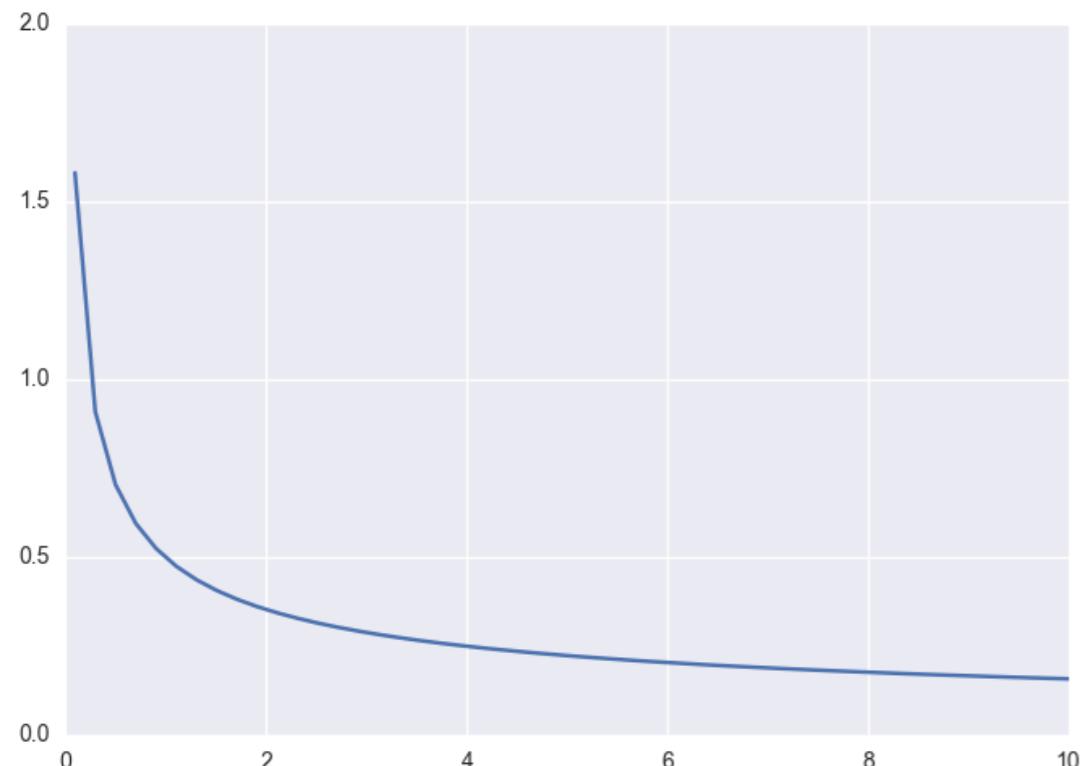
	L_{actual}	L_{random}	C_{actual}	C_{random}
Film actors	3.65	2.99	0.79	0.00027
Power grid	18.7	12.4	0.080	0.005
<i>C. elegans</i>	2.65	2.25	0.28	0.05

Distribución de grado

“Número de vecinos”

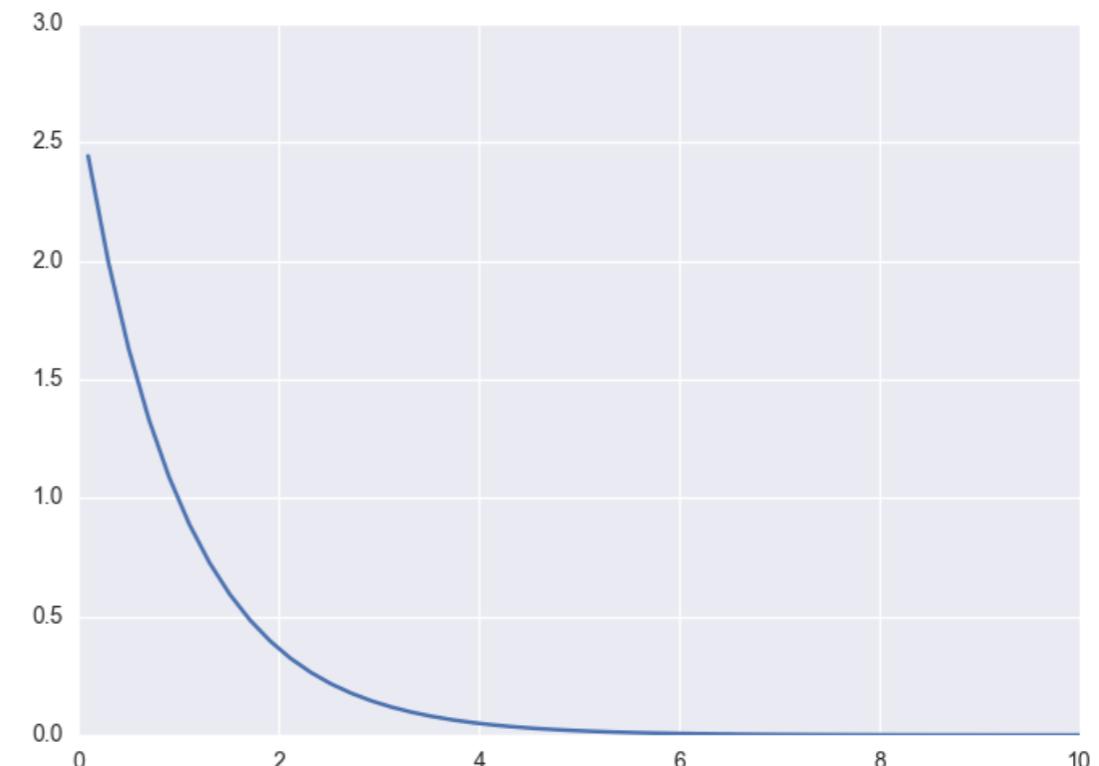


Distribuciones frecuentes



Ley de potencias

$$f(x) = Ax^{-b}$$

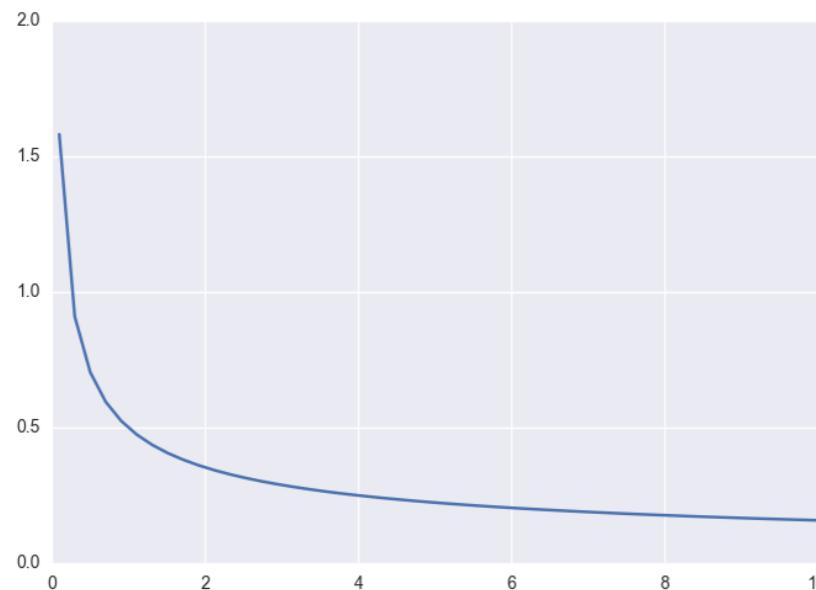


Exponencial

$$f(x) = Ae^{-bx}$$

Gráficos Log-Log y Semilog

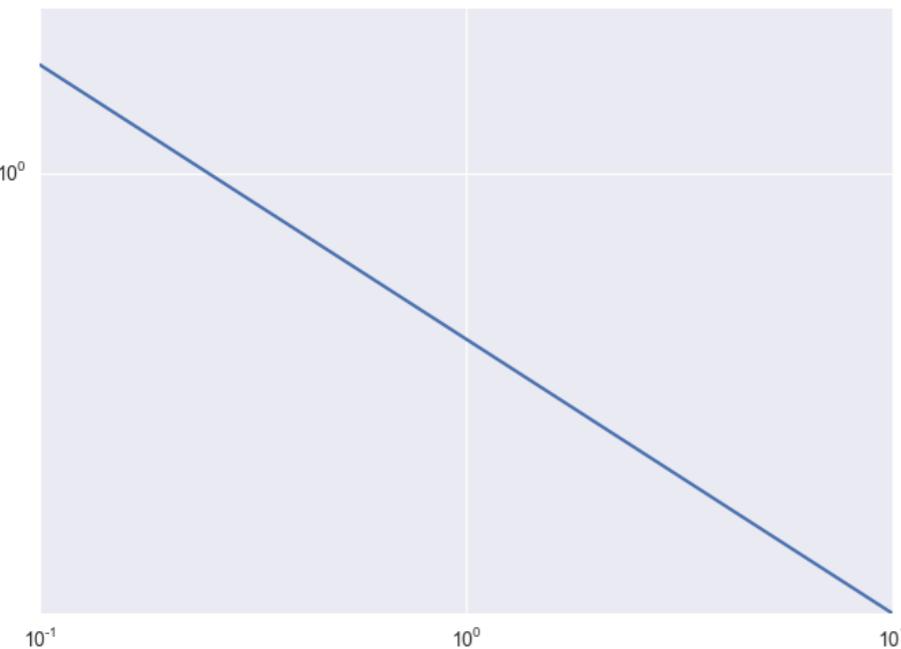
Ley de potencias



`plt.loglog()`

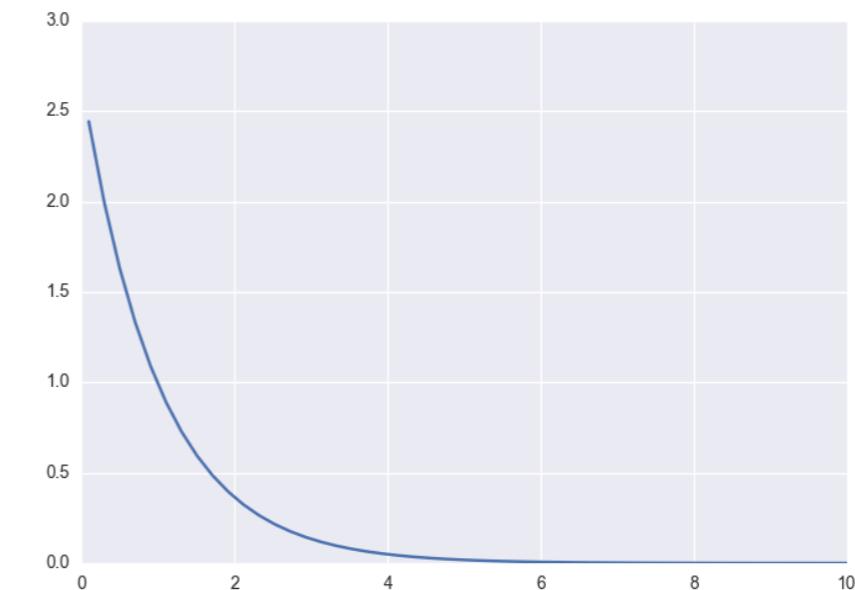


Log



Log

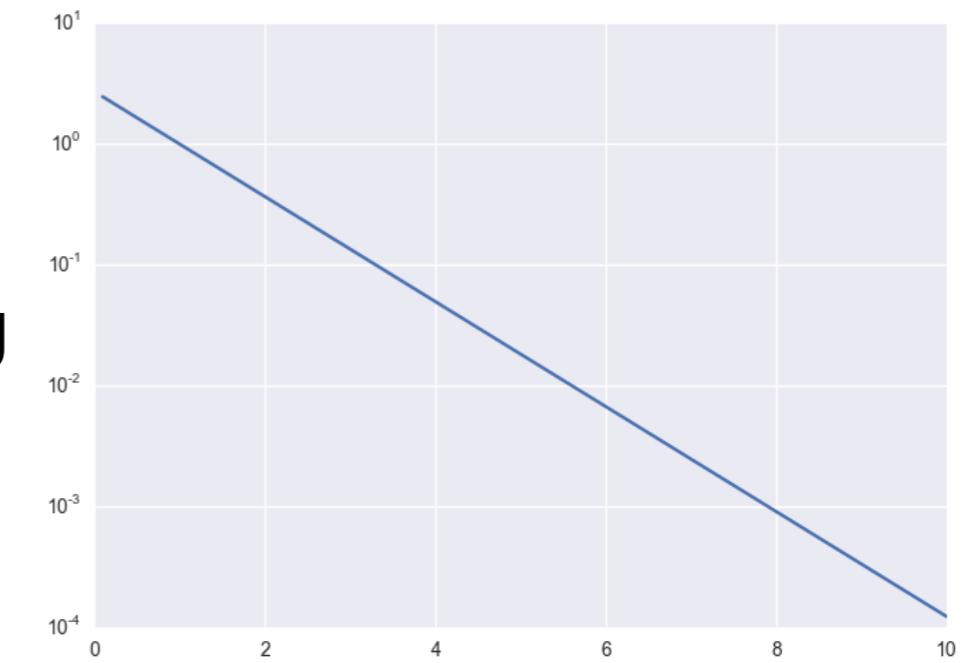
Exponencial



`plt.semilogy()`



Log



Lin

Redes Libres de Escala

1999

Emergence of Scaling in Random Networks

Albert-László Barabási* and Réka Albert

Systems as diverse as genetic networks or the World Wide Web are best described as networks with complex topology. A common property of many large networks is that the vertex connectivities follow a scale-free power-law distribution. This feature was found to be a consequence of two generic mechanisms: (i) networks expand continuously by the addition of new vertices, and (ii) new vertices attach preferentially to sites that are already well connected. A model based on these two ingredients reproduces the observed stationary scale-free distributions, which indicates that the development of large networks is governed by robust self-organizing phenomena that go beyond the particulars of the individual systems.

- Las redes se expanden a través de la adición de nuevos vértices
- Los nuevos vértices se ligan preferentemente a sitios bien conectados (*preferential attachment*)

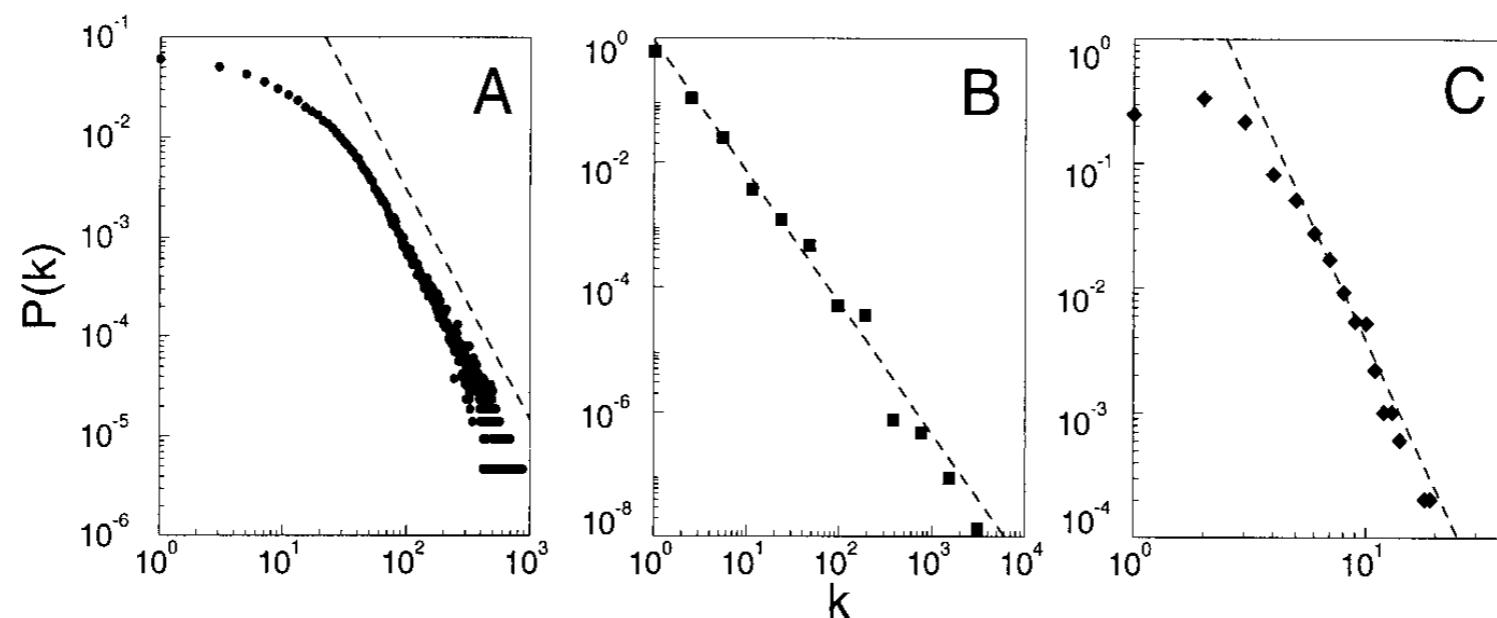
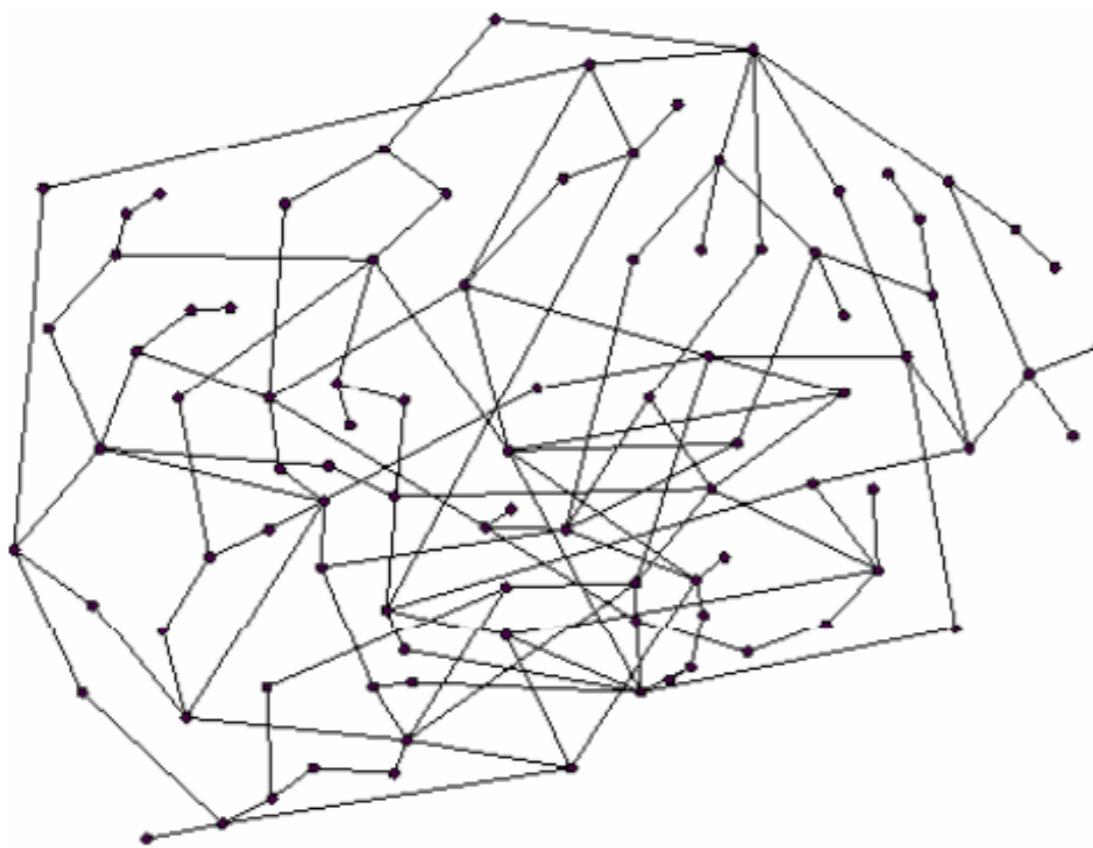


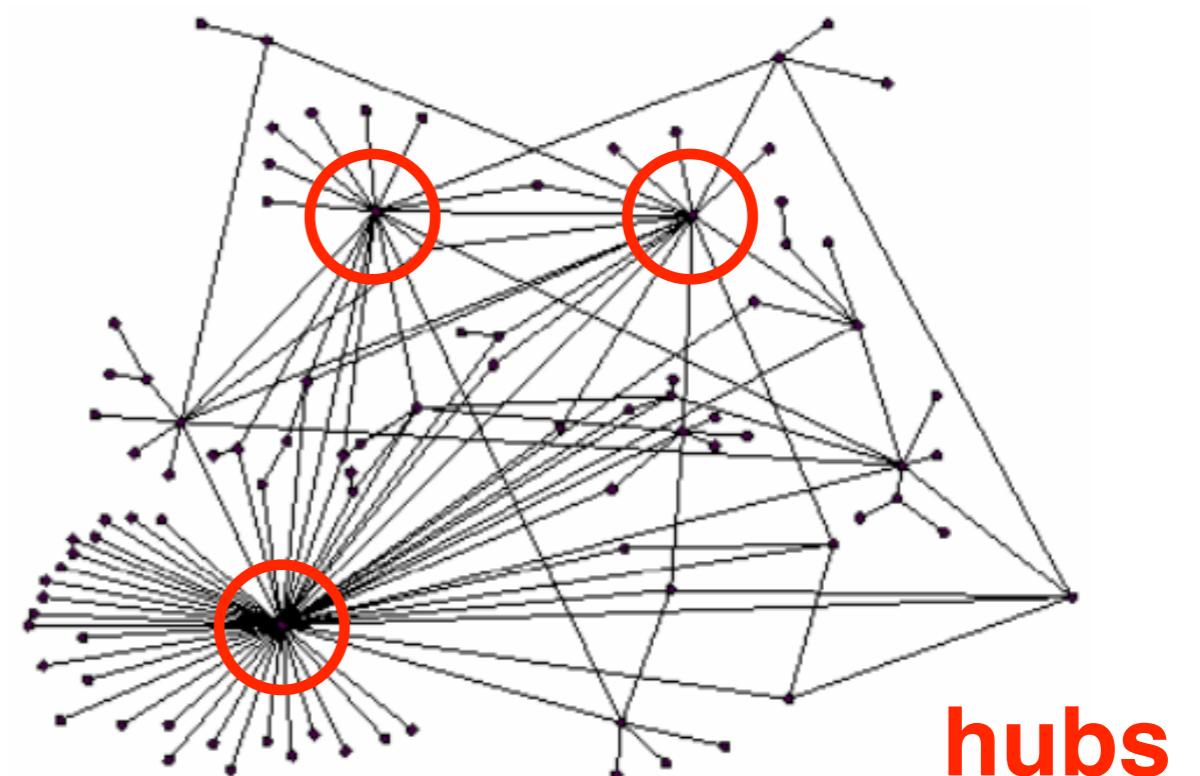
Fig. 1. The distribution function of connectivities for various large networks. (A) Actor collaboration graph with $N = 212,250$ vertices and average connectivity $\langle k \rangle = 28.78$. (B) WWW, $N = 325,729$, $\langle k \rangle = 5.46$ (6). (C) Power grid data, $N = 4941$, $\langle k \rangle = 2.67$. The dashed lines have slopes (A) $\gamma_{\text{actor}} = 2.3$, (B) $\gamma_{\text{www}} = 2.1$ and (C) $\gamma_{\text{power}} = 4$.

Redes Libres de Escala

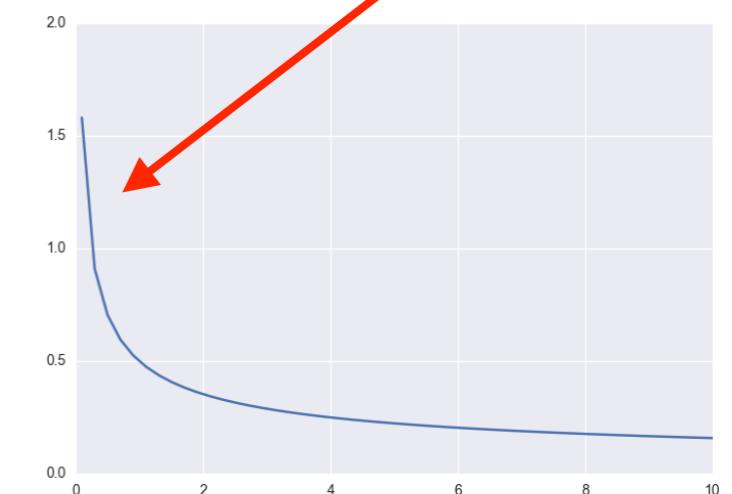
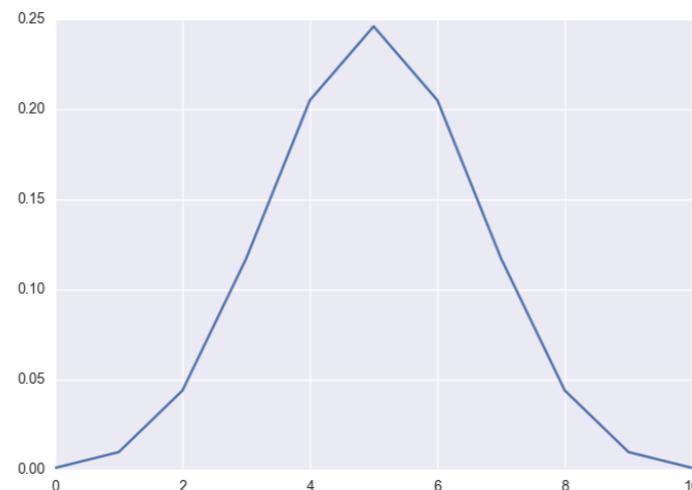
Red aleatoria (Erdös)



Red scale-free



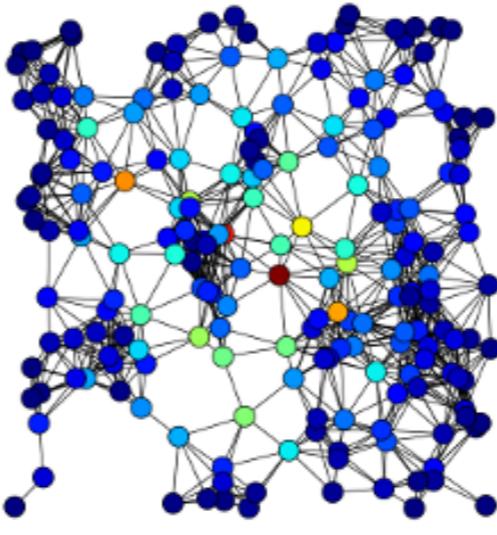
Distribución
de grado:



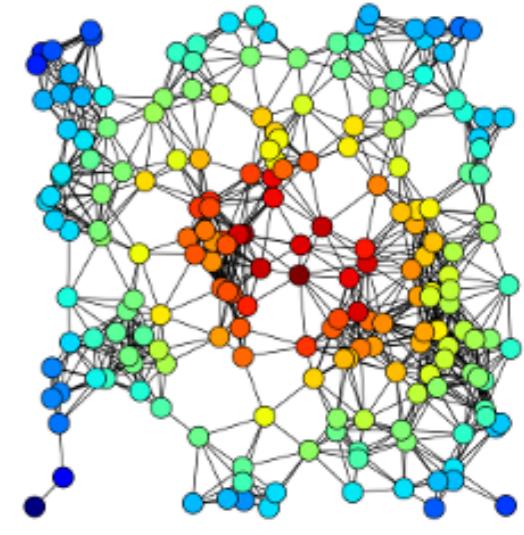
hubs

Centrality

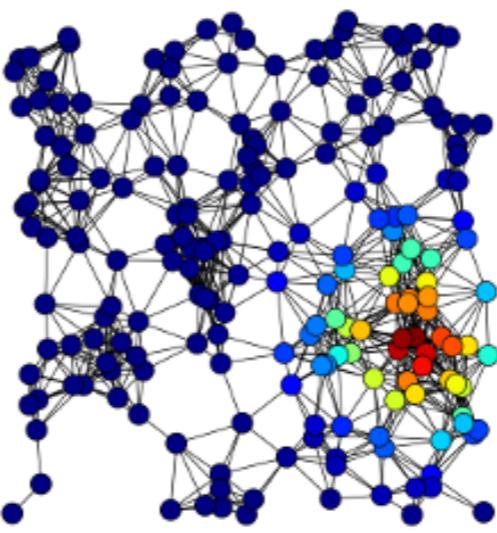
- A. Betweenness
- B. Closeness
- C. Eigenvector
- D. Degree
- E. Harmonic
- F. Katz



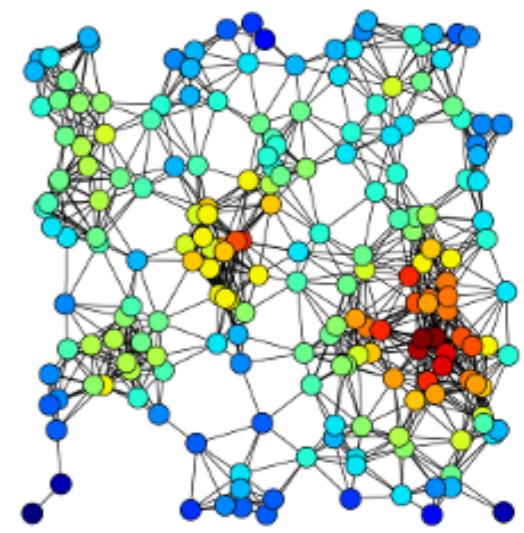
A



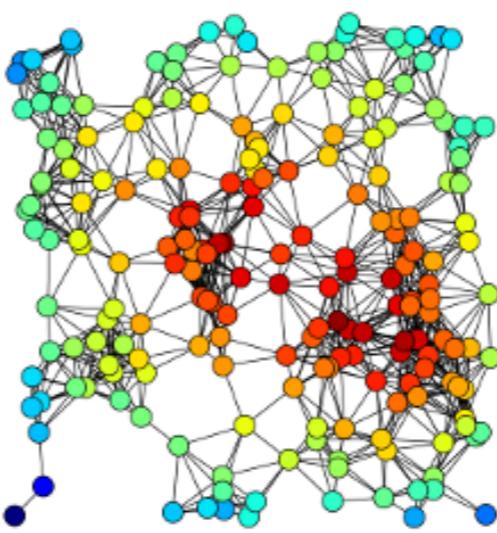
B



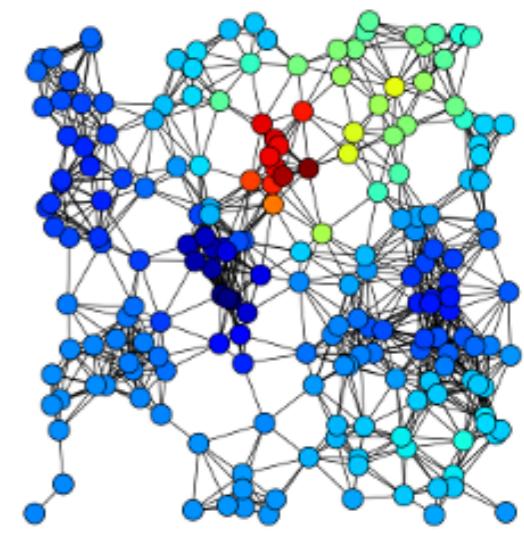
C



D

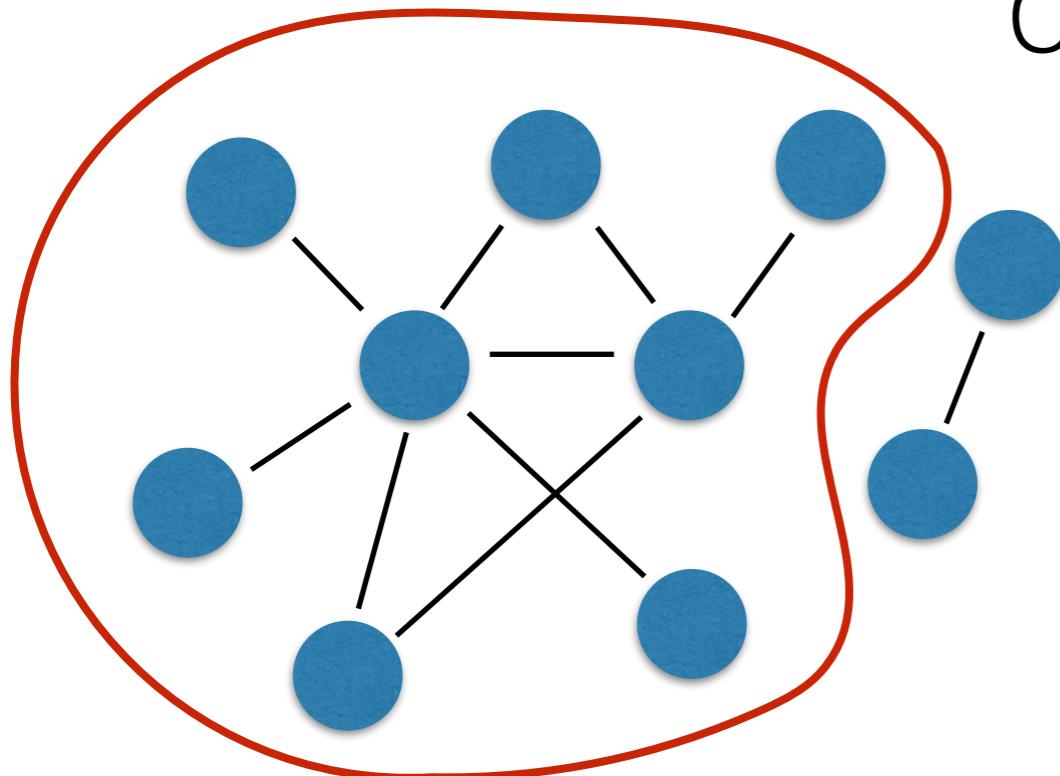


E

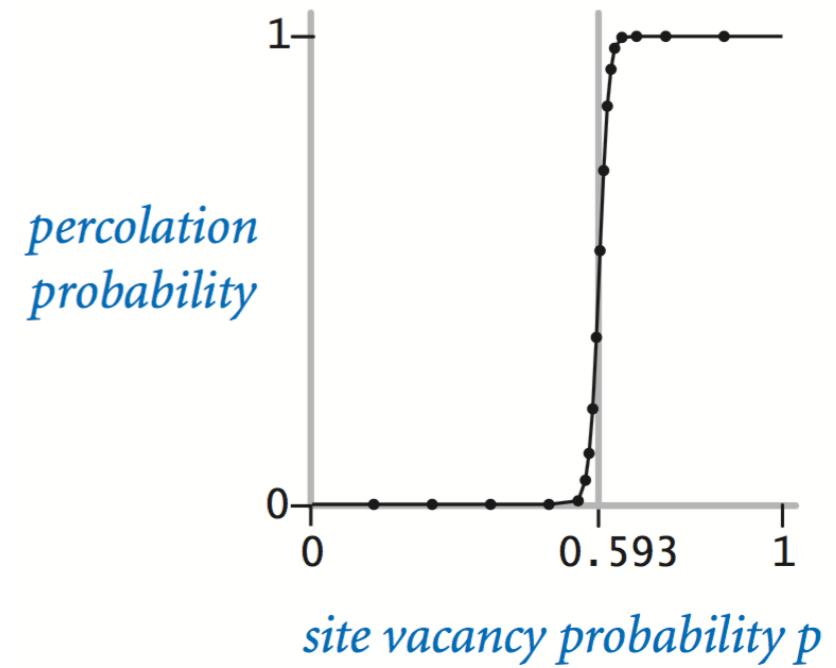


F

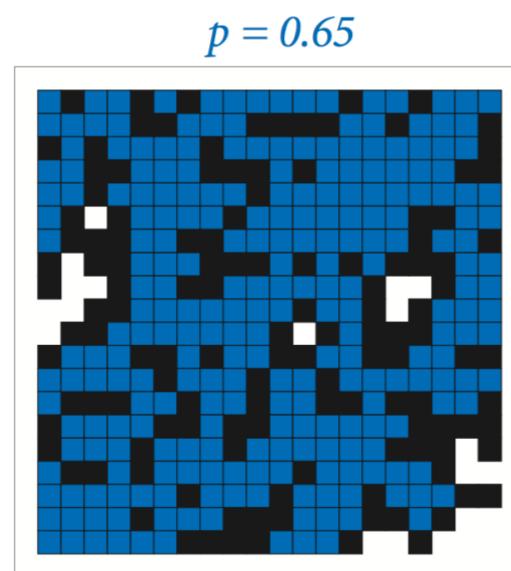
Componentes Conexas



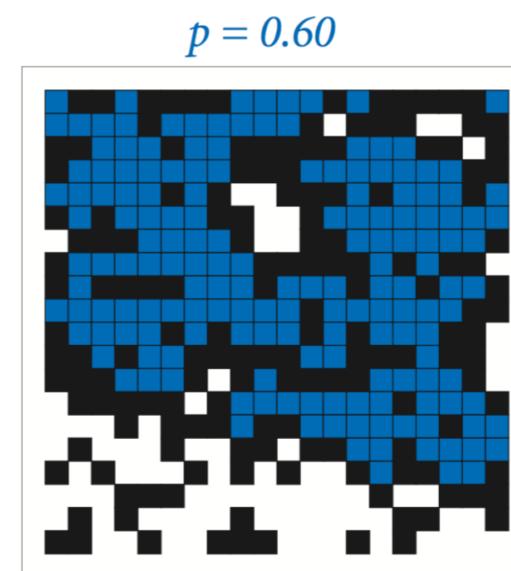
Componente
“gigante”



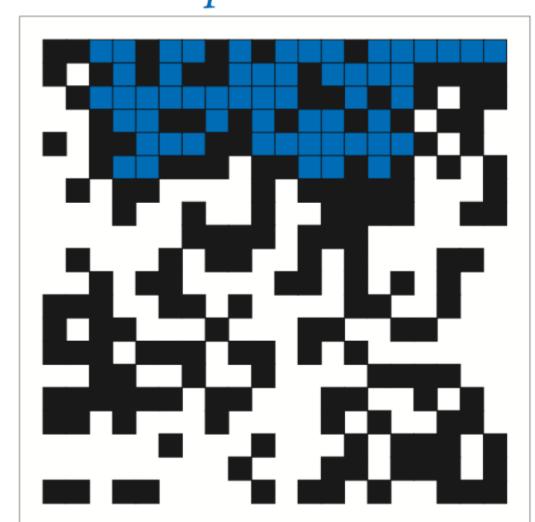
Percolación



$p = 0.65$



$p = 0.60$

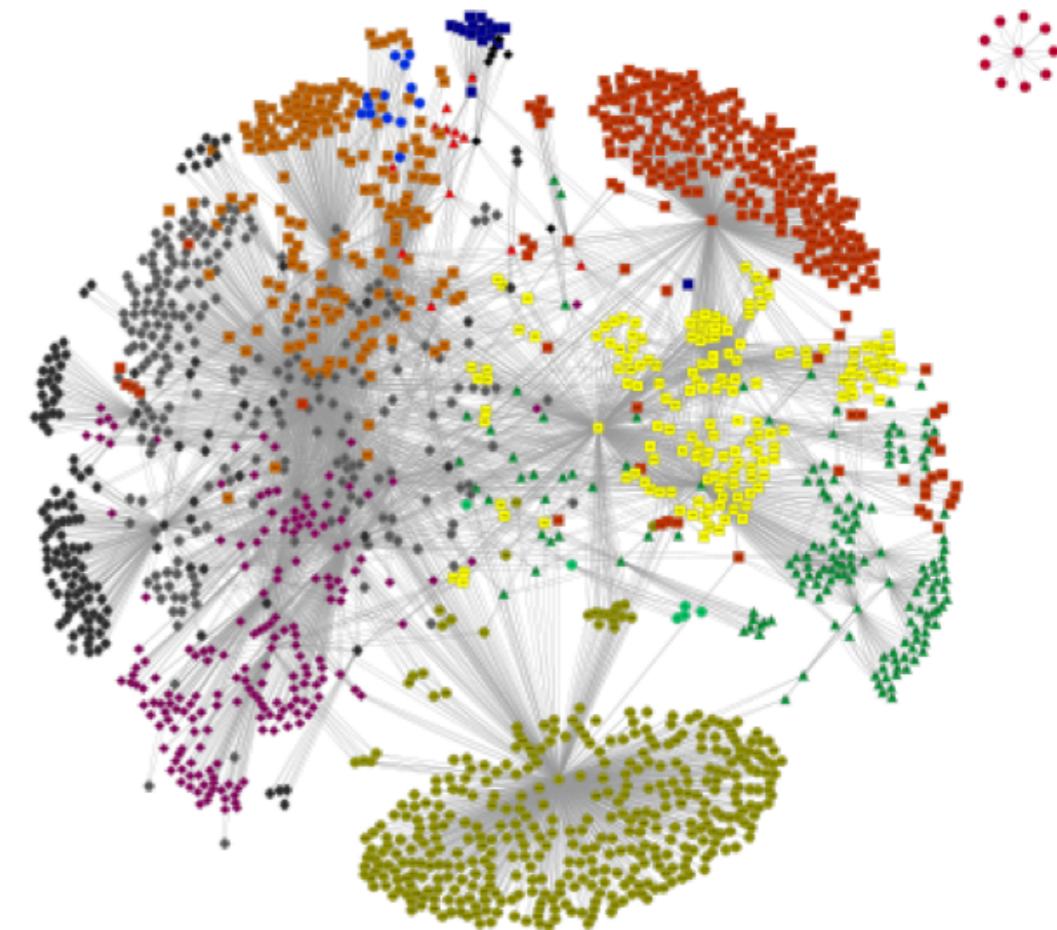


$p = 0.55$

Comunidades

Algoritmo de Girvan-Newman

1. Calcular betweenness de todas las **aristas**
2. Eliminar la arista con mayor betweenness
3. Recalcular betweenness de aristas afectadas
4. Iterar hasta que no haya aristas

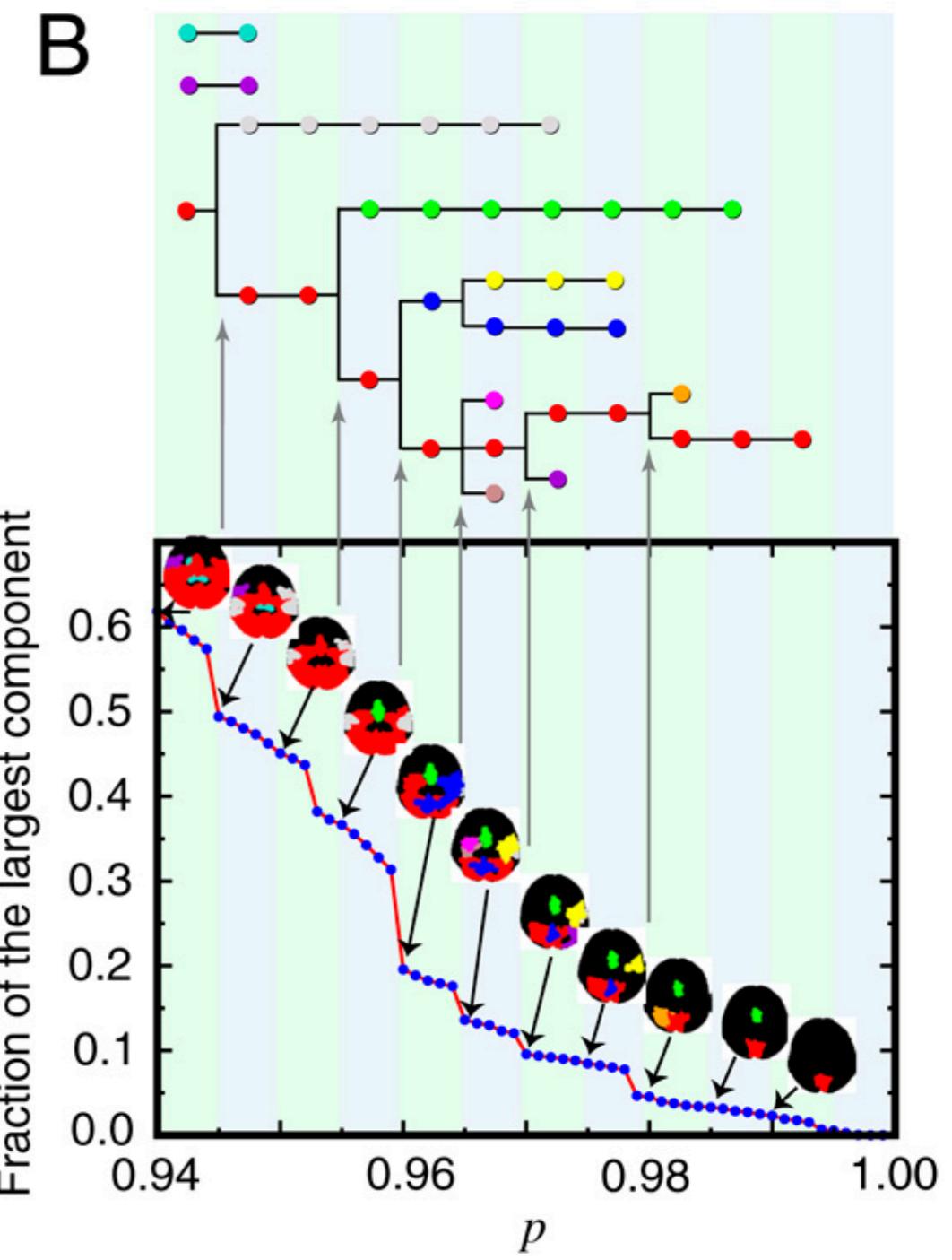
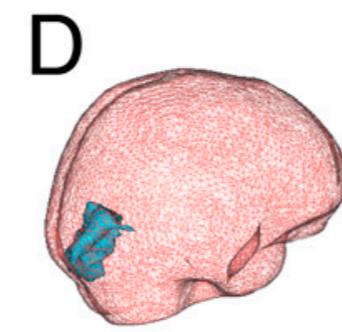
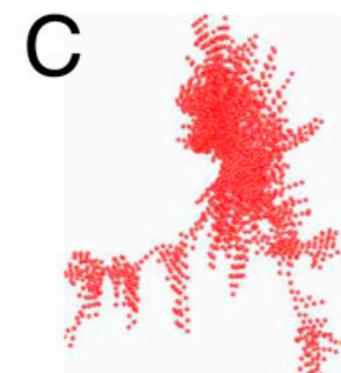
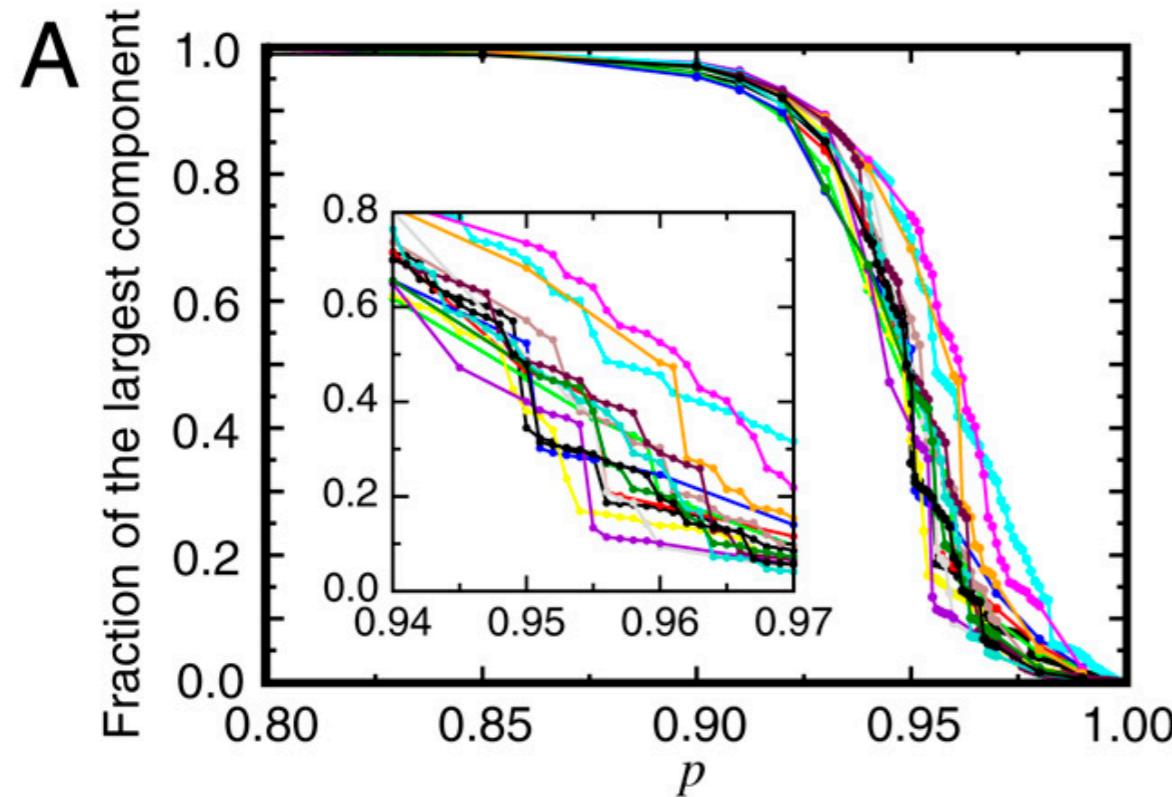


Salida: *Dendrograma*

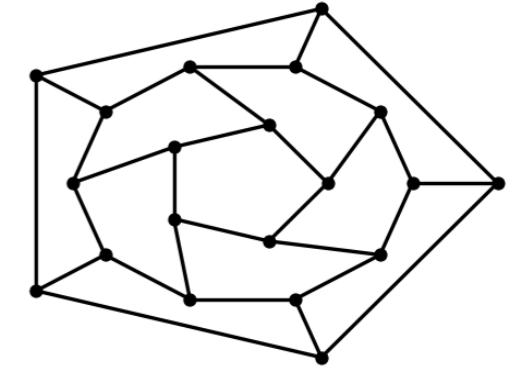
Redes del Cerebro: Modularidad

A small world of weak ties provides optimal global integration of self-similar modules in functional brain networks

Lazaros K. Gallos^a, Hernán A. Makse^{a,b,1}, and Mariano Sigman^b



networkx



- <https://networkx.github.io/>
- Grafos dirigidos, pesados, multigrafos, ...
- ```
import networkx as nx
G = nx.Graph()
G.add_edges_from([(1, 2), (1, 3)])
```
- pero también:  

```
ws = nx.watts_strogatz_graph(30, 3, 0.1)
nx.algorithms.centrality.betweenness_centrality()
```