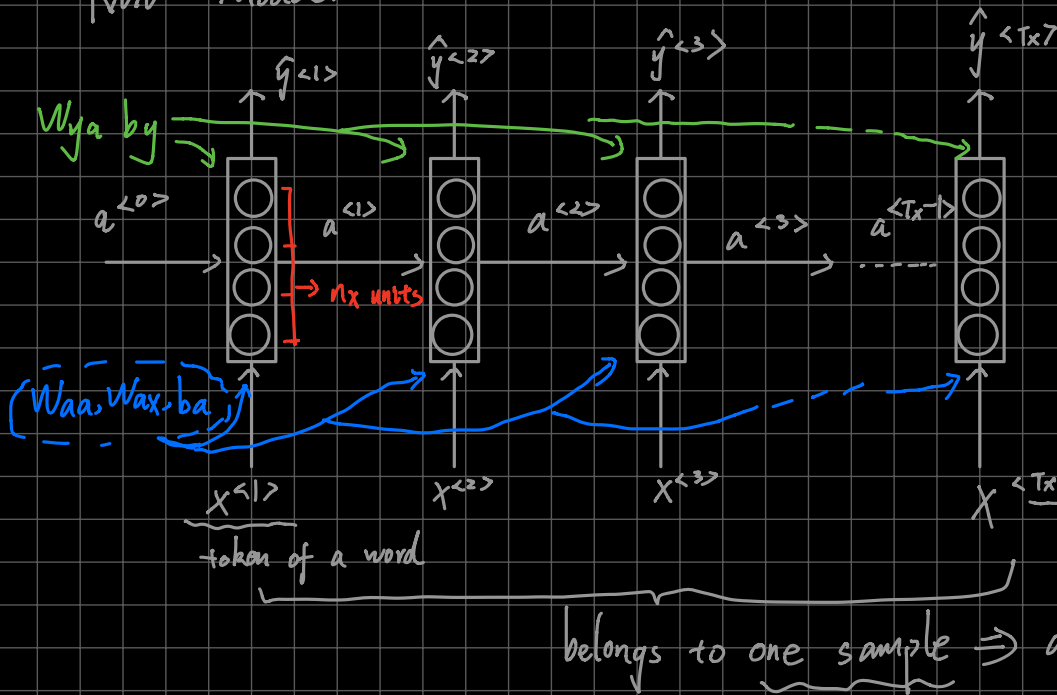


Sequence Model

RNN Model:

Notation:

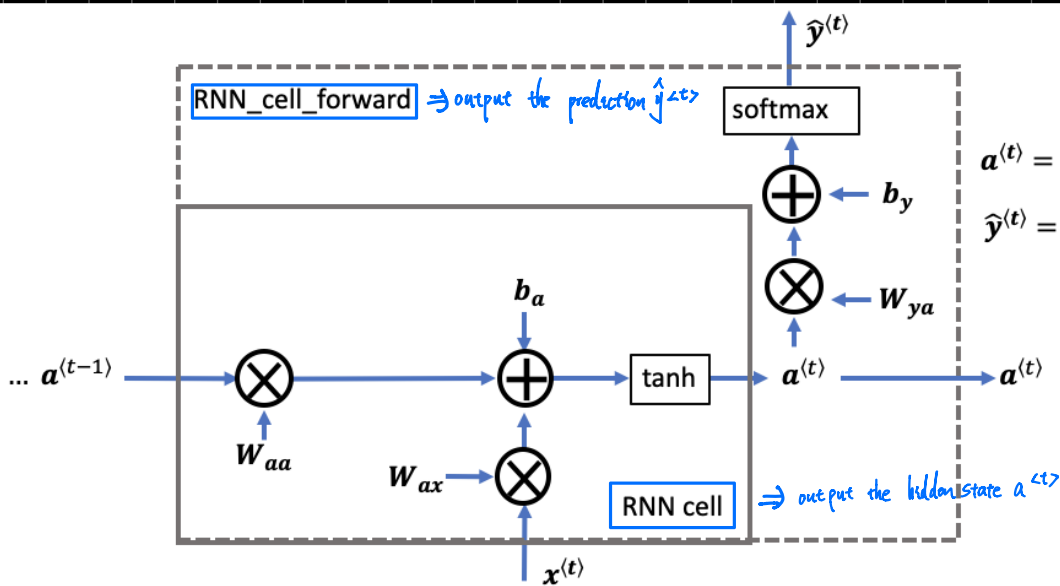


(2) [3] <4>
 a_5
 sample 2, RNN layer 3,
 timestep 4, unit 5.

length of a sequences

- Δ There is only one $W_{aa}, W_{ax}, b_a, W_{ya}, b_y$.
- Δ $n_x = \text{vocabulary size} = x^{(1)}[1] \dots x^{(j)}[n_x]$'s size

Forward propagation:



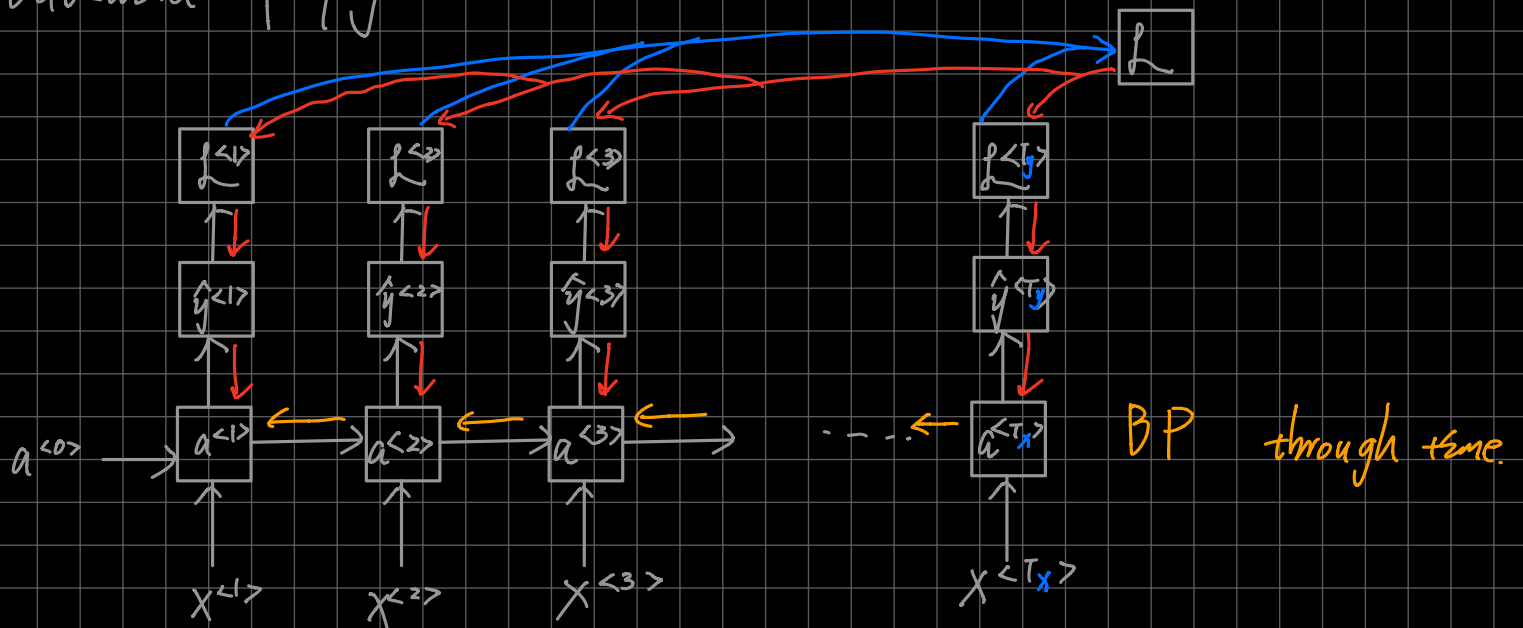
$$a^{(t)} = \tanh(W_{ax} x^{(t)} + W_{aa} a^{(t-1)} + b_a)$$

$$\hat{y}^{(t)} = \text{softmax}(W_{ya} a^{(t)} + b_y)$$

or relu
 or sigmoid

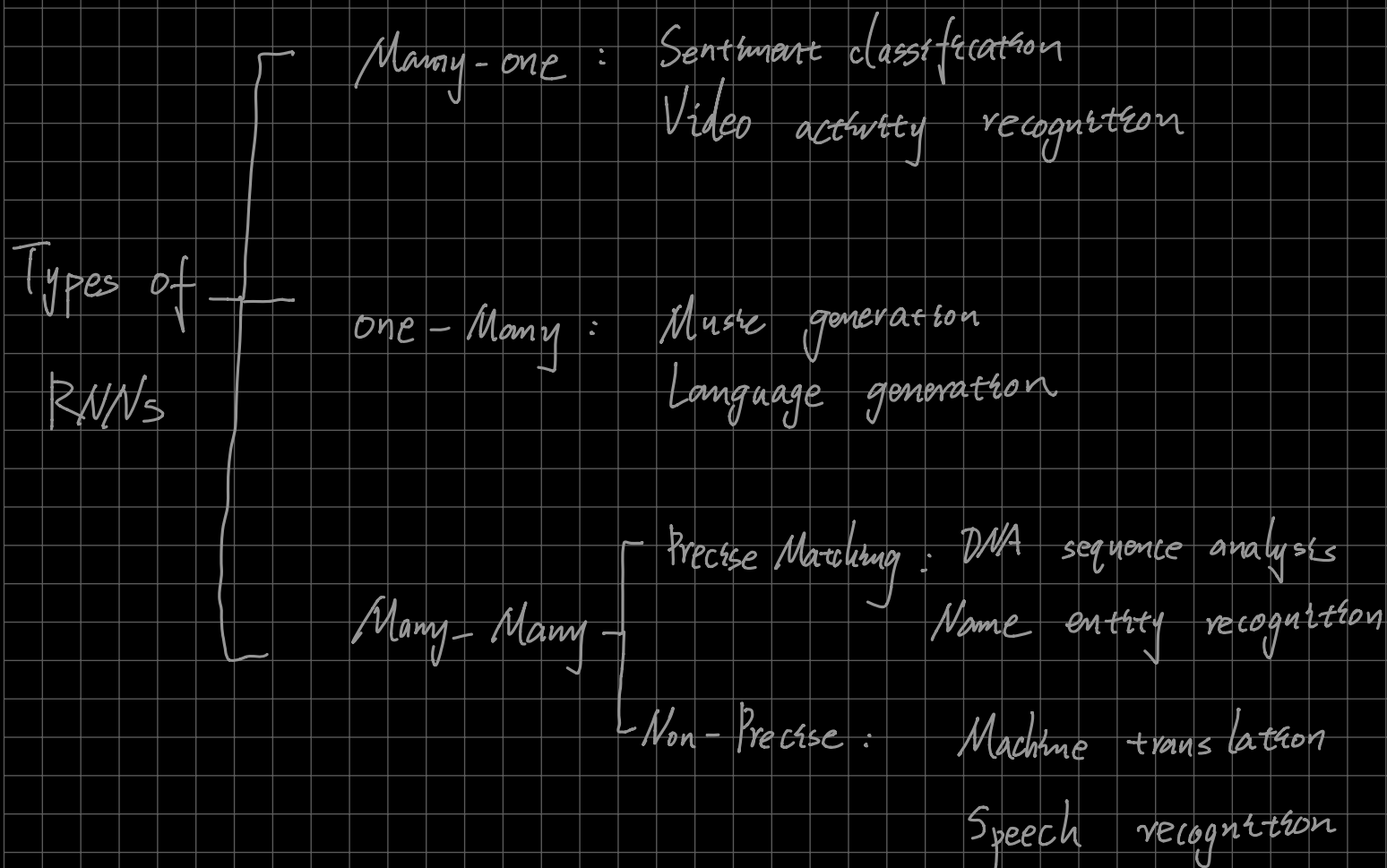
$$\begin{cases} a^{(t)} = g_1(W_{aa} a^{(t-1)} + W_{ax} x^{(t)} + b_a) \\ \hat{y}^{(t)} = g_2(W_{ya} a^{(t)} + b_y) \end{cases}$$

Backward propagation:

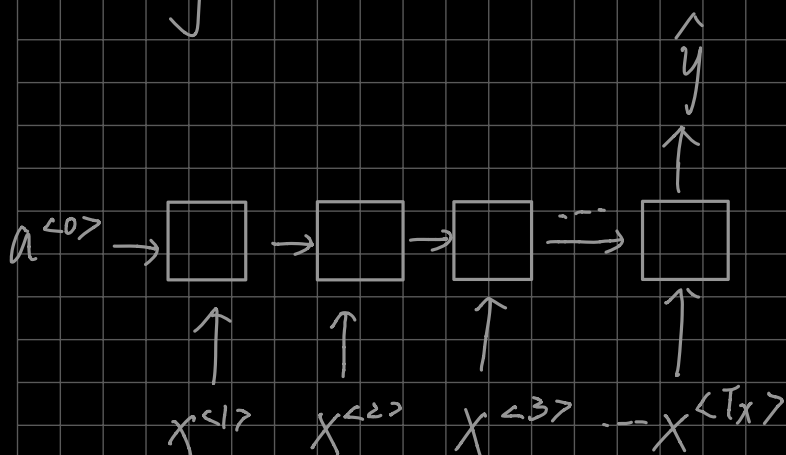


$$L^{<i>} = - (y^{<i>} \cdot \log \hat{y}^{<i>} + (1 - y^{<i>}) \cdot \log(1 - \hat{y}^{<i>}))$$

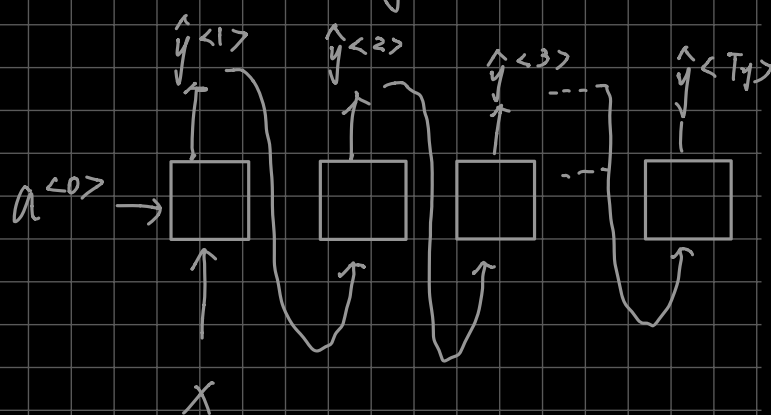
$$L = \sum_{i=1}^{T_x} L^{<i>} (\hat{y}^{<i>}, y^{<i>})$$



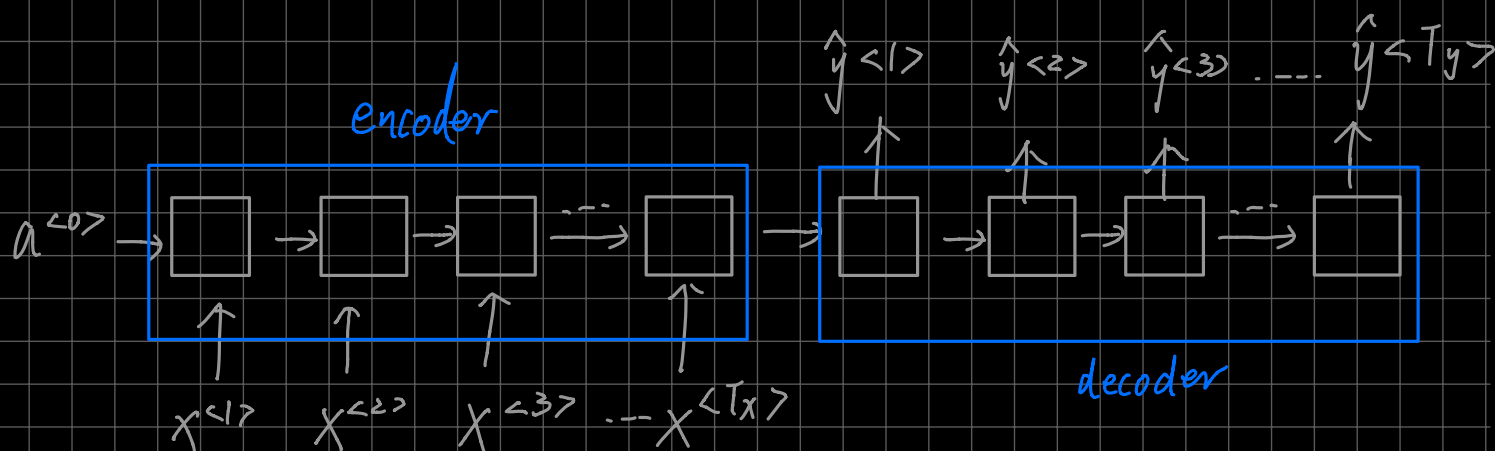
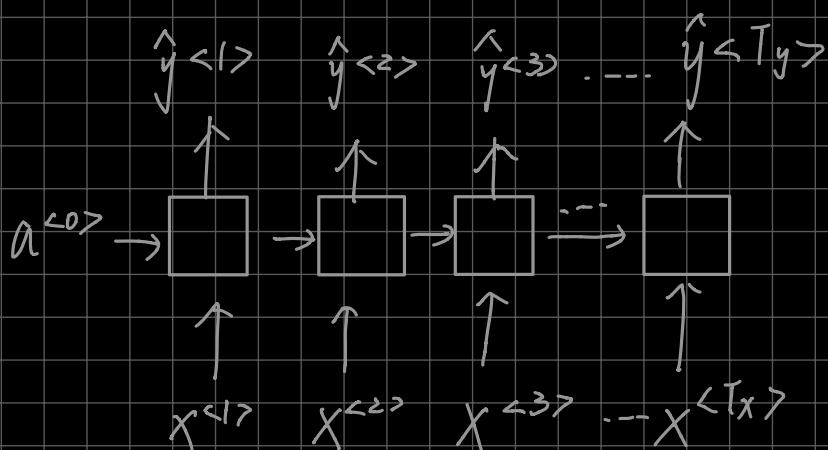
Many to one:



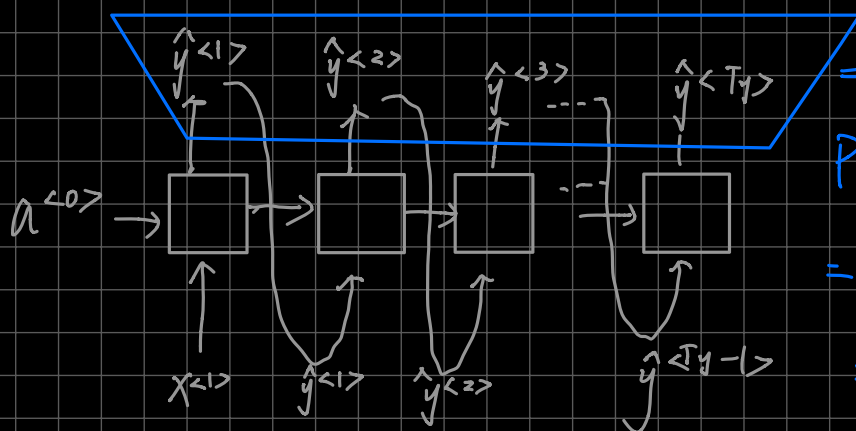
One to Many:



Many to many:



Sampling from a trained RNN:



Sampling sequence

$$P(y^{<1>}, y^{<2>}, \dots, y^{<T_y>})$$

$$= P(y^{<1>}) \cdot P(y^{<2>} | y^{<1>}) \cdot P(y^{<3>} | y^{<1>}, y^{<2>}) \cdot \dots$$

条件概率公式

RNN input's shape: $X = (\underbrace{n_x}_{\text{number of units}}, \underbrace{m}_{\text{batch size}}, \underbrace{T_x}_{\text{Time step}})$

TimeStep input's shape: $X^{<t>} = (\underbrace{n_x}_\text{each timestep, we input a batch of data}, m)$

Hidden state's shape: $a^{<t>} = (\underbrace{n_a}_\text{batch of data}, m)$

Prediction: $\hat{y} = (n_y, m, T_y)$
 $\hat{y}^{<t>} = (n_y, m)$