

Let  $X_1, \ldots, X_m$  be a random sample from a normal distribution with variance  $\sigma_1^2$ , let  $Y_1, \ldots, Y_n$  be another random sample (independent of the  $X_i$ 's) from a normal distribution with variance  $\sigma_2^2$ , and let  $S_1^2$  and  $S_2^2$  denote the two sample

$$F = \frac{S_1^2/\sigma_1^2}{S_2^2/\sigma_2^2} \tag{9.9}$$

has an F distribution with  $v_1 = m - 1$  and  $v_2 = n - 1$ .

Null hypothesis:  $H_0$ :  $\sigma_1^2 = \sigma_2^2$ 

variances. Then the rv

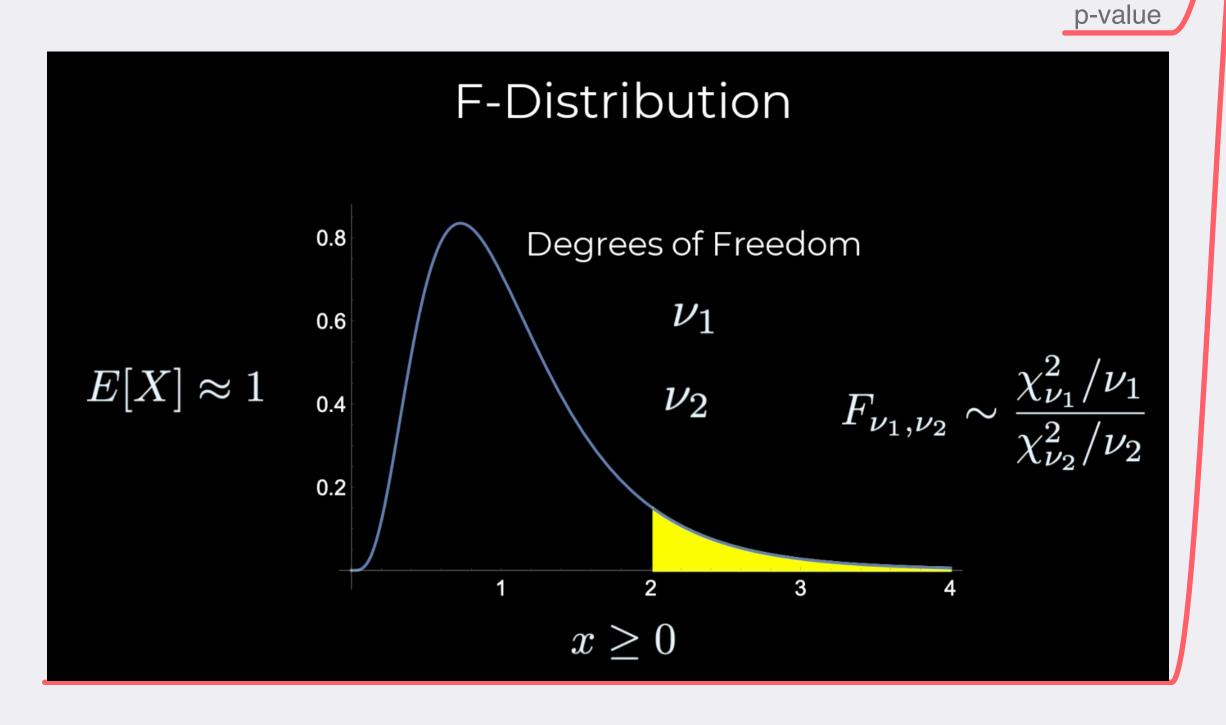
Test statistic value:  $f = s_1^2/s_2^2$ 

Alternative Hypothesis Rejection Region for a Level  $\alpha$  Test

 $egin{align} H_{\mathrm{a}}:\sigma_1^2>\sigma_2^2 & f\geq F_{lpha,m-1,n-1} \ H_{\mathrm{a}}:\sigma_1^2<\sigma_2^2 & f\leq F_{1-lpha,m-1,n-1} \ \end{array}$ 

 $H_a: \sigma_1^2 \neq \sigma_2^2$  either  $f \geq F_{\alpha/2, m-1, n-1}$  or  $f \leq F_{1-\alpha/2, m-1, n-1}$ 

Since critical values are tabled only for  $\alpha = .10, .05, .01$ , and .001, the two-tailed test can be performed only at levels .20, .10, .02, and .002. Other F critical values can be obtained from statistical software.



F stat: FINV(pvalue, df1, df2)

p-value: FDIST(fstat, df1, df2)

Excel

F distribution

Population variances

W09

