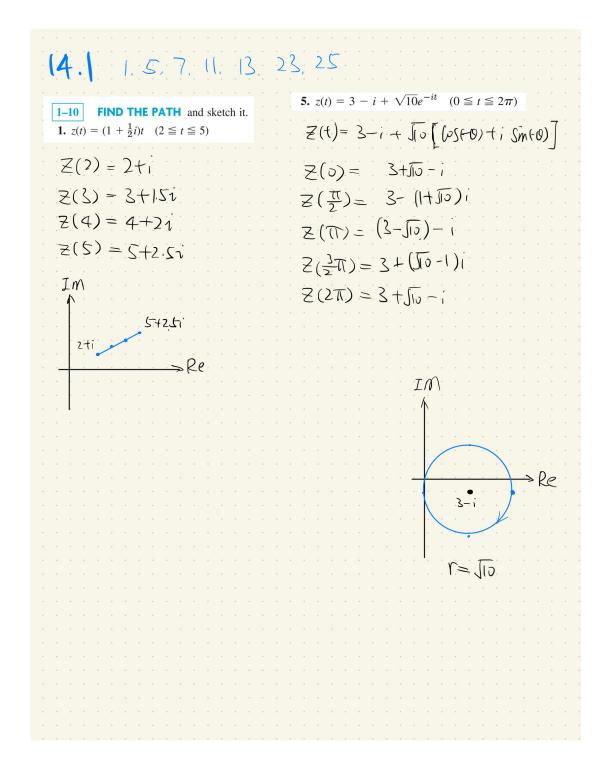
# **Chapter 14 - Complex Integration**

## **Selected Problem set 14.1**



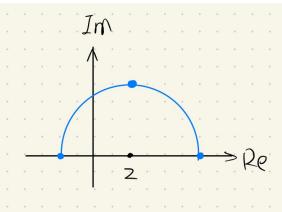
7. 
$$z(t) = 2 + 4e^{\pi i t/2}$$
  $(0 \le t \le 2)$ 

$$e^{\frac{\pi t}{2}} = \cos(\frac{\pi t}{2}t) + i \sin(\frac{\pi t}{2}t)$$

$$Z(0) = 2 + 4((+0)) = 6$$

$$z_{i}(t) = 2t + 4(0 + i) = 2t + 4i$$

$$Z(2) = 2 + 4(-1) + 0i) = -2$$



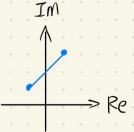
### 11-20

#### FIND A PARAMETRIC REPRESENTATION

and sketch the path.

**11.** Segment from (-1, 1) to (1, 3)

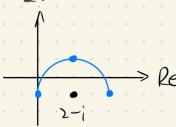
$$M = \frac{3-1}{1-(-1)} = 1$$
  
 $(-1+t, 1+t)$   $0 \le t \le 2$ 



**13.** Upper half of 
$$|z - 2 + i| = 2$$
 from  $(4, -1)$  to  $(0, -1)$ 

$$Z(t) = 2 - i + 2e^{it} \qquad 0 \le t \le \pi$$

$$Im$$



### 21–30 INTEGRATION

Integrate by the first method or state why it does not apply and use the second method. Show the details.

23.  $\int_C e^z dz$ , C the shortest path from  $\pi i$  to  $2\pi i$ 

$$C \cdot Z(t) = t \cdot \pi$$

$$\dot{Z}(t) = \tau \cdot \pi$$

$$\int_{1}^{2} e^{t\pi i} \pi i dt$$

$$= \pi i \int_{1}^{2} [\cos(t\pi) + i \sin(t\pi)] dt$$

$$= \pi_{i} \left( 0 + - \frac{2}{\pi} \pi_{i} \right)$$

$$= 2$$

**25.**  $\int_C z \exp(z^2) dz$ , C from 1 along the axes to i

$$C_1 : Z_1(t) = 1 - t$$
  $0 \le t \le 1$   
 $Z_1(t) = -1$   
 $C_2 : Z_1(t) = ti$   $0 \le t \le 1$   
 $Z_2(t) = i$ 

