# Week 1: Simulating quantum advantage with trapped ions

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### Introduction

We put all the functions for the coding tasks in the script assignment. jl.

#### Task 1

In this task, we create a function getAmp2 to calculate the probability  $P(x) = |\langle x|\psi\rangle|^2$  of each bitstring x showing as a dot in the speckle pattern by taking the dot product between the bit-string and  $|\psi\rangle$  from the run function given in the script run\_random\_circuit.jl. In Fig. 1, we plot 16 different combinations of N and circuit depths, where N varies from 2 to 5, and the depths include 4, 16, 32, and 64. These patterns are plotted by the function speckles(). One can find that some bitstrings are much more likely to occur than others, especially when N is larger. The location x with highest probability seems to distribute randomly.

We also make a function studyBondDim to calculate the bond dimension in the bonus problem by using the built-in function maxlinkdim in ITensor. In Fig. 2, we plot the bond dimensions as a function of circuit depth at several values of N. The bond dimension saturates at a higher circuit depth when N is larger.

### Task 2

To consider a single random bit flip, we modified the given run function by adding an argument wbitflip. If wbitflip is True, we assign a bit flip at a random location bitloc in the modified run function. In the bitflipCompile function, we let wbitflip=True and plot 16 different speckle patterns generated from a single bit flip error of a single gate and collect them into a collage, as shown in Fig. 3.

### Task 3

In this task, we create a function cgfScalingSingle to calculate the cumulative distribution function (CDF) by numerically summing or integrating the probability distribution. Then we use the function cgfScaling to plot the CDF values with different depths and compare them with the theoretical value  $1 - e^{-2^N p}$ , as shown in Fig. 4

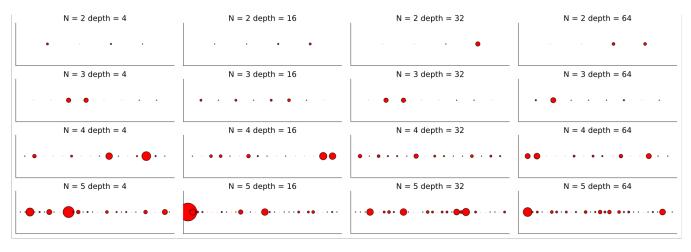


Figure 1: "Speckle patterns" displaying the probabilities of obtaining with N=2 to 5 and depths of 4, 16, 32, and 64.

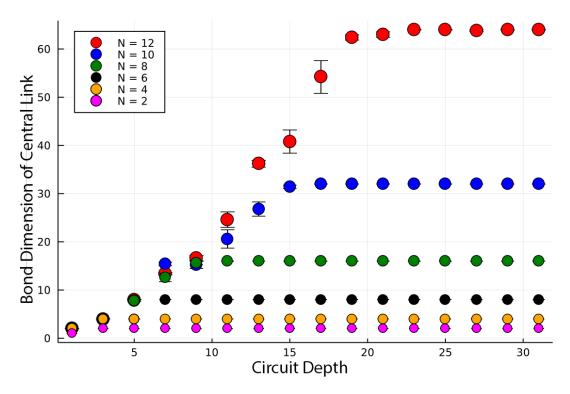


Figure 2: The bond dimensions of central links as a function of circuit depth at different numbers of qubits. At a

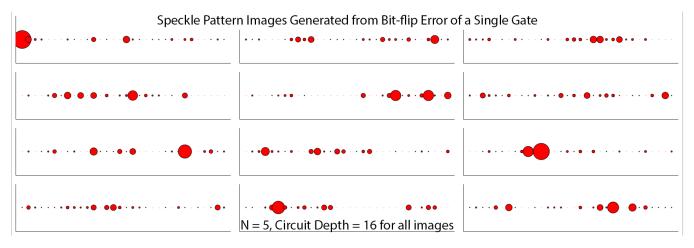


Figure 3: "Speckle patterns" displaying the probabilities of obtaining each of the 16 possible outcomes when sampling a 5-qubit circuit with a bit flip error occurred at a random location.

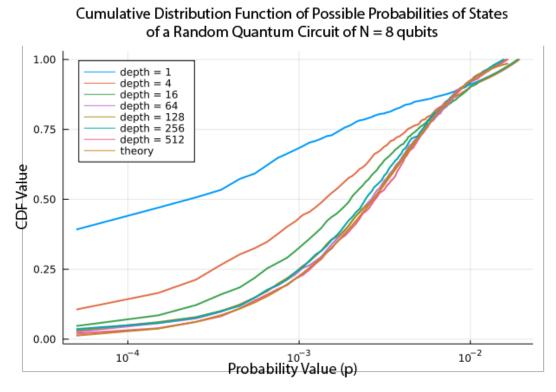


Figure 4: Calculated CDF as a function of the probability values p in log scale at different circuit depths in an 8-qubit circuit. When the depth is larger, the CDF converges toward the theoretical value  $1 - e^{-2^N p}$ .

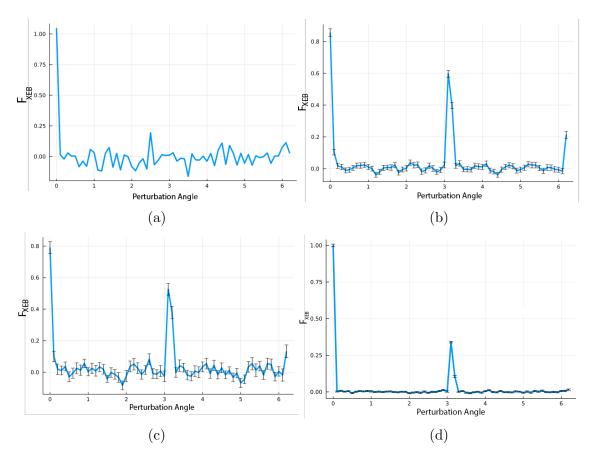


Figure 5: The crossed entropy benchmarking fidelity  $\mathcal{F}_{\text{XEB}}$  calculated as a function of the perturbation angle  $\Delta\Theta$  in a unit of radians at different numbers of qubit N, circuit depths d, and numbers of samples s. (a) N=8, d=512, without averaging; (b) N=4, d=128, s=200; (c) N=8, d=128, s=50; (d) N=10, d=128, s=50.

#### Task 4

In the function crossEntropyValue, we calculate the linear cross-entropy benchmarking (XEB) fidelity  $\mathcal{F}_{XEB}$ , defined in Eq. (1) of the instruction. In Fig. 5(a), the function crossEntropy assembles the results at different  $\Delta\Theta$  and plots the  $\mathcal{F}_{XEB}$  as a function of  $\Delta\Theta$ .

In the function crossEntropywDavg,  $\mathcal{F}_{XEB}$  is calculated by averaging over a certain number of samples s. In Figs. 5 (b) - (d), we calculate the XEB fidelity  $\mathcal{F}_{XEB}$  when performing the averages over a number of samples s. A peak occurs near  $\Delta\Theta = \pi$ .

## **Business Application**