

32 Point Groups

No. 1 C_1 1 [triclinic] tag = "C1"

* generator : 1

* conjugacy class

$$[1] = 1$$

* symmetry operation

$$\textcircled{1} \quad 1$$

* product table

		1
1	1	1

No. 2 C_i -1 [triclinic] tag = "Ci"

* generator : -1

* conjugacy class

$$\begin{bmatrix} 1 \end{bmatrix} = 1$$

$$\begin{bmatrix} -1 \end{bmatrix} = -1$$

* symmetry operation

$$\textcircled{1} \quad 1 \quad \textcircled{2} \quad -1$$

* product table

	1	-1
1	1	-1
-1	-1	1

No. 3 C_2 2 (b-axis setting) [monoclinic] tag = "C2"

* generator : 2_{010}

* conjugacy class

$$[1] = 1$$

$$[2_{010}] = 2_{010}$$

* symmetry operation

$$\textcircled{1} \quad 1 \quad \textcircled{2} \quad 2_{010}$$

* product table

			1	2_{010}	
1	1	2_{010}			
2_{010}	2_{010}	1			

No. 4 C_s m (b-axis setting) [monoclinic] tag = "Cs"

* generator : m_{010}

* conjugacy class

$$[1] = 1$$

$$[m_{010}] = m_{010}$$

* symmetry operation

$$\textcircled{1} \quad 1 \quad \textcircled{2} \quad m_{010}$$

* product table

	1	m_{010}
1	1	m_{010}
m_{010}	m_{010}	1

No. 5 C_{2h} $2/m$ (b-axis setting) [monoclinic] tag = "C2h"

* generator : 2_{010} , -1

* conjugacy class

$$[1] = 1$$

$$[2_{010}] = 2_{010}$$

$$[-1] = -1$$

$$[m_{010}] = m_{010}$$

* symmetry operation

$$\textcircled{1} \quad 1 \quad \textcircled{2} \quad 2_{010} \quad \textcircled{3} \quad -1 \quad \textcircled{4} \quad m_{010}$$

* product table

	1	2_{010}	-1	m_{010}
1	1	2_{010}	-1	m_{010}
2_{010}	2_{010}	1	m_{010}	-1
-1	-1	m_{010}	1	2_{010}
m_{010}	m_{010}	-1	2_{010}	1

No. 6 D_2 222 [orthorhombic] tag = "D2"

* generator : 2_{001} , 2_{010}

* conjugacy class

$$[1] = 1$$

$$[2_{001}] = 2_{001}$$

$$[2_{010}] = 2_{010}$$

$$[2_{100}] = 2_{100}$$

* symmetry operation

$$\textcircled{1} \quad 1 \quad \textcircled{2} \quad 2_{001} \quad \textcircled{3} \quad 2_{010} \quad \textcircled{4} \quad 2_{100}$$

* product table

	1	2_{001}	2_{010}	2_{100}
1	1	2_{001}	2_{010}	2_{100}
2_{001}	2_{001}	1	2_{100}	2_{010}
2_{010}	2_{010}	2_{100}	1	2_{001}
2_{100}	2_{100}	2_{010}	2_{001}	1

No. 7 C_{2v} $mm2$ [orthorhombic] tag = "C2v"

* generator : 2_{001} , m_{010}

* conjugacy class

$$[1] = 1$$

$$[2_{001}] = 2_{001}$$

$$[m_{010}] = m_{010}$$

$$[m_{100}] = m_{100}$$

* symmetry operation

$$\textcircled{1} \quad 1 \quad \textcircled{2} \quad 2_{001} \quad \textcircled{3} \quad m_{010} \quad \textcircled{4} \quad m_{100}$$

* product table

	1	2_{001}	m_{010}	m_{100}
1	1	2_{001}	m_{010}	m_{100}
2_{001}	2_{001}	1	m_{100}	m_{010}
m_{010}	m_{010}	m_{100}	1	2_{001}
m_{100}	m_{100}	m_{010}	2_{001}	1

No. 8 D_{2h} mmm [orthorhombic] tag = "D2h"

* generator : 2_{001} , 2_{010} , -1

* conjugacy class

$$\begin{aligned} [1] &= 1 \\ [2_{001}] &= 2_{001} \\ [2_{010}] &= 2_{010} \\ [2_{100}] &= 2_{100} \\ [-1] &= -1 \\ [m_{001}] &= m_{001} \\ [m_{010}] &= m_{010} \\ [m_{100}] &= m_{100} \end{aligned}$$

* symmetry operation

$$\textcircled{1} \quad 1 \quad \textcircled{2} \quad 2_{001} \quad \textcircled{3} \quad 2_{010} \quad \textcircled{4} \quad 2_{100} \quad \textcircled{5} \quad -1 \quad \textcircled{6} \quad m_{001} \quad \textcircled{7} \quad m_{010} \quad \textcircled{8} \quad m_{100}$$

* product table

	1	2_{001}	2_{010}	2_{100}	-1	m_{001}	m_{010}	m_{100}
1	1	2_{001}	2_{010}	2_{100}	-1	m_{001}	m_{010}	m_{100}
2_{001}	2_{001}	1	2_{100}	2_{010}	m_{001}	-1	m_{100}	m_{010}
2_{010}	2_{010}	2_{100}	1	2_{001}	m_{010}	m_{100}	-1	m_{001}
2_{100}	2_{100}	2_{010}	2_{001}	1	m_{100}	m_{010}	m_{001}	-1
-1	-1	m_{001}	m_{010}	m_{100}	1	2_{001}	2_{010}	2_{100}
m_{001}	m_{001}	-1	m_{100}	m_{010}	2_{001}	1	2_{100}	2_{010}
m_{010}	m_{010}	m_{100}	-1	m_{001}	2_{010}	2_{100}	1	2_{001}
m_{100}	m_{100}	m_{010}	m_{001}	-1	2_{100}	2_{010}	2_{001}	1

No. 9 C_4 4 [tetragonal] tag = "C4"

* generator : 2_{001} , 4_{001}^+

* conjugacy class

$$[1] = 1$$

$$[2_{001}] = 2_{001}$$

$$[4_{001}^+] = 4_{001}^+$$

$$[4_{001}^-] = 4_{001}^-$$

* symmetry operation

$$\textcircled{1} \quad 1 \quad \textcircled{2} \quad 2_{001} \quad \textcircled{3} \quad 4_{001}^+ \quad \textcircled{4} \quad 4_{001}^-$$

* product table

	1	2_{001}	4_{001}^+	4_{001}^-
1	1	2_{001}	4_{001}^+	4_{001}^-
2_{001}	2_{001}	1	4_{001}^-	4_{001}^+
4_{001}^+	4_{001}^+	4_{001}^-	2_{001}	1
4_{001}^-	4_{001}^-	4_{001}^+	1	2_{001}

No. 10 S_4 -4 [tetragonal] tag = "S4"

* generator : 2_{001} , -4_{001}^+

* conjugacy class

$$[1] = 1$$

$$[2_{001}] = 2_{001}$$

$$[-4_{001}^+] = -4_{001}^+$$

$$[-4_{001}^-] = -4_{001}^-$$

* symmetry operation

$$\textcircled{1} \quad 1 \quad \textcircled{2} \quad 2_{001} \quad \textcircled{3} \quad -4_{001}^+ \quad \textcircled{4} \quad -4_{001}^-$$

* product table

	1	2_{001}	-4_{001}^+	-4_{001}^-
1	1	2_{001}	-4_{001}^+	-4_{001}^-
2_{001}	2_{001}	1	-4_{001}^-	-4_{001}^+
-4_{001}^+	-4_{001}^+	-4_{001}^-	2_{001}	1
-4_{001}^-	-4_{001}^-	-4_{001}^+	1	2_{001}

No. 11 C_{4h} $4/m$ [tetragonal] tag = "C4h"

* generator : 2_{001} , 4_{001}^+ , -1

* conjugacy class

$$\begin{aligned}
 [1] &= 1 \\
 [2_{001}] &= 2_{001} \\
 [4_{001}^+] &= 4_{001}^+ \\
 [4_{001}^-] &= 4_{001}^- \\
 [-1] &= -1 \\
 [m_{001}] &= m_{001} \\
 [-4_{001}^+] &= -4_{001}^+ \\
 [-4_{001}^-] &= -4_{001}^-
 \end{aligned}$$

* symmetry operation

$$\textcircled{1} \quad 1 \quad \textcircled{2} \quad 2_{001} \quad \textcircled{3} \quad 4_{001}^+ \quad \textcircled{4} \quad 4_{001}^- \quad \textcircled{5} \quad -1 \quad \textcircled{6} \quad m_{001} \quad \textcircled{7} \quad -4_{001}^+ \quad \textcircled{8} \quad -4_{001}^-$$

* product table

	1	2_{001}	4_{001}^+	4_{001}^-	-1	m_{001}	-4_{001}^+	-4_{001}^-
1	1	2_{001}	4_{001}^+	4_{001}^-	-1	m_{001}	-4_{001}^+	-4_{001}^-
2_{001}	2_{001}	1	4_{001}^-	4_{001}^+	m_{001}	-1	-4_{001}^-	-4_{001}^+
4_{001}^+	4_{001}^+	4_{001}^-	2_{001}	1	-4_{001}^+	-4_{001}^-	m_{001}	-1
4_{001}^-	4_{001}^-	4_{001}^+	1	2_{001}	-4_{001}^-	-4_{001}^+	-1	m_{001}
-1	-1	m_{001}	-4_{001}^+	-4_{001}^-	1	2_{001}	4_{001}^+	4_{001}^-
m_{001}	m_{001}	-1	-4_{001}^-	-4_{001}^+	2_{001}	1	4_{001}^-	4_{001}^+
-4_{001}^+	-4_{001}^+	-4_{001}^-	m_{001}	-1	4_{001}^+	4_{001}^-	2_{001}	1
-4_{001}^-	-4_{001}^-	-4_{001}^+	-1	m_{001}	4_{001}^-	4_{001}^+	1	2_{001}

No. 12 D_4 422 [tetragonal] tag = "D4"

* generator : 2_{001} , 4_{001}^+ , 2_{010}

* conjugacy class

$$\begin{aligned} [1] &= 1 \\ [2_{001}] &= 2_{001} \\ [2_{100}] &= 2_{100}, 2_{010} \\ [2_{110}] &= 2_{110}, 2_{1-10} \\ [4_{001}^+] &= 4_{001}^+, 4_{001}^- \end{aligned}$$

* symmetry operation

$$\textcircled{1} \quad 1 \quad \textcircled{2} \quad 2_{001} \quad \textcircled{3} \quad 2_{100} \quad \textcircled{4} \quad 2_{010} \quad \textcircled{5} \quad 2_{110} \quad \textcircled{6} \quad 2_{1-10} \quad \textcircled{7} \quad 4_{001}^+ \quad \textcircled{8} \quad 4_{001}^-$$

* product table

	1	2_{001}	2_{100}	2_{010}	2_{110}	2_{1-10}	4_{001}^+	4_{001}^-
1	1	2_{001}	2_{100}	2_{010}	2_{110}	2_{1-10}	4_{001}^+	4_{001}^-
2_{001}	2_{001}	1	2_{010}	2_{100}	2_{1-10}	2_{110}	4_{001}^-	4_{001}^+
2_{100}	2_{100}	2_{010}	1	2_{001}	4_{001}^-	4_{001}^+	2_{1-10}	2_{110}
2_{010}	2_{010}	2_{100}	2_{001}	1	4_{001}^+	4_{001}^-	2_{110}	2_{1-10}
2_{110}	2_{110}	2_{1-10}	4_{001}^+	4_{001}^-	1	2_{001}	2_{100}	2_{010}
2_{1-10}	2_{1-10}	2_{110}	4_{001}^-	4_{001}^+	2_{001}	1	2_{010}	2_{100}
4_{001}^+	4_{001}^+	4_{001}^-	2_{110}	2_{1-10}	2_{010}	2_{100}	2_{001}	1
4_{001}^-	4_{001}^-	4_{001}^+	2_{1-10}	2_{110}	2_{100}	2_{010}	1	2_{001}

No. 13 C_{4v} $4mm$ [tetragonal] tag = "C4v"

* generator : 2_{001} , 4_{001}^+ , m_{010}

* conjugacy class

$$\begin{aligned} [1] &= 1 \\ [2_{001}] &= 2_{001} \\ [4_{001}^+] &= 4_{001}^+, 4_{001}^- \\ [m_{100}] &= m_{100}, m_{010} \\ [m_{110}] &= m_{110}, m_{1-10} \end{aligned}$$

* symmetry operation

$$\textcircled{1} \quad 1 \quad \textcircled{2} \quad 2_{001} \quad \textcircled{3} \quad 4_{001}^+ \quad \textcircled{4} \quad 4_{001}^- \quad \textcircled{5} \quad m_{100} \quad \textcircled{6} \quad m_{010} \quad \textcircled{7} \quad m_{110} \quad \textcircled{8} \quad m_{1-10}$$

* product table

	1	2_{001}	4_{001}^+	4_{001}^-	m_{100}	m_{010}	m_{110}	m_{1-10}
1	1	2_{001}	4_{001}^+	4_{001}^-	m_{100}	m_{010}	m_{110}	m_{1-10}
2_{001}	2_{001}	1	4_{001}^-	4_{001}^+	m_{010}	m_{100}	m_{1-10}	m_{110}
4_{001}^+	4_{001}^+	4_{001}^-	2_{001}	1	m_{110}	m_{1-10}	m_{010}	m_{100}
4_{001}^-	4_{001}^-	4_{001}^+	1	2_{001}	m_{1-10}	m_{110}	m_{100}	m_{010}
m_{100}	m_{100}	m_{010}	m_{1-10}	m_{110}	1	2_{001}	4_{001}^-	4_{001}^+
m_{010}	m_{010}	m_{100}	m_{110}	m_{1-10}	2_{001}	1	4_{001}^+	4_{001}^-
m_{110}	m_{110}	m_{1-10}	m_{100}	m_{010}	4_{001}^+	4_{001}^-	1	2_{001}
m_{1-10}	m_{1-10}	m_{110}	m_{010}	m_{100}	4_{001}^-	4_{001}^+	2_{001}	1

No. 14 D_{2d} $-42m$ ($-42m$ setting) [tetragonal] tag = "D2d"

* generator : 2_{001} , -4_{001}^+ , 2_{010}

* conjugacy class

$$\begin{aligned} [1] &= 1 \\ [2_{001}] &= 2_{001} \\ [2_{100}] &= 2_{100}, 2_{010} \\ [m_{110}] &= m_{110}, m_{1-10} \\ [-4_{001}^+] &= -4_{001}^+, -4_{001}^- \end{aligned}$$

* symmetry operation

$$\textcircled{1} \quad 1 \quad \textcircled{2} \quad 2_{001} \quad \textcircled{3} \quad 2_{100} \quad \textcircled{4} \quad 2_{010} \quad \textcircled{5} \quad m_{110} \quad \textcircled{6} \quad m_{1-10} \quad \textcircled{7} \quad -4_{001}^+ \quad \textcircled{8} \quad -4_{001}^-$$

* product table

	1	2_{001}	2_{100}	2_{010}	m_{110}	m_{1-10}	-4_{001}^+	-4_{001}^-
1	1	2_{001}	2_{100}	2_{010}	m_{110}	m_{1-10}	-4_{001}^+	-4_{001}^-
2_{001}	2_{001}	1	2_{010}	2_{100}	m_{1-10}	m_{110}	-4_{001}^-	-4_{001}^+
2_{100}	2_{100}	2_{010}	1	2_{001}	-4_{001}^-	-4_{001}^+	m_{1-10}	m_{110}
2_{010}	2_{010}	2_{100}	2_{001}	1	-4_{001}^+	-4_{001}^-	m_{110}	m_{1-10}
m_{110}	m_{110}	m_{1-10}	-4_{001}^+	-4_{001}^-	1	2_{001}	2_{100}	2_{010}
m_{1-10}	m_{1-10}	m_{110}	-4_{001}^-	-4_{001}^+	2_{001}	1	2_{010}	2_{100}
-4_{001}^+	-4_{001}^+	-4_{001}^-	m_{110}	m_{1-10}	2_{010}	2_{100}	2_{001}	1
-4_{001}^-	-4_{001}^-	-4_{001}^+	m_{1-10}	m_{110}	2_{100}	2_{010}	1	2_{001}

No. 14 $D_{2d} - 1$ $-4m2$ ($-4m2$ setting) [tetragonal] tag = "D2d-1"

* generator : 2_{001} , -4_{001}^+ , m_{010}

* conjugacy class

$$\begin{aligned} [1] &= 1 \\ [2_{001}] &= 2_{001} \\ [2_{110}] &= 2_{110}, 2_{1-10} \\ [m_{100}] &= m_{100}, m_{010} \\ [-4_{001}^+] &= -4_{001}^+, -4_{001}^- \end{aligned}$$

* symmetry operation

$$\textcircled{1} \quad 1 \quad \textcircled{2} \quad 2_{001} \quad \textcircled{3} \quad 2_{110} \quad \textcircled{4} \quad 2_{1-10} \quad \textcircled{5} \quad m_{100} \quad \textcircled{6} \quad m_{010} \quad \textcircled{7} \quad -4_{001}^+ \quad \textcircled{8} \quad -4_{001}^-$$

* product table

	1	2_{001}	2_{110}	2_{1-10}	m_{100}	m_{010}	-4_{001}^+	-4_{001}^-
1	1	2_{001}	2_{110}	2_{1-10}	m_{100}	m_{010}	-4_{001}^+	-4_{001}^-
2_{001}	2_{001}	1	2_{1-10}	2_{110}	m_{010}	m_{100}	-4_{001}^-	-4_{001}^+
2_{110}	2_{110}	2_{1-10}	1	2_{001}	-4_{001}^+	-4_{001}^-	m_{100}	m_{010}
2_{1-10}	2_{1-10}	2_{110}	2_{001}	1	-4_{001}^-	-4_{001}^+	m_{010}	m_{100}
m_{100}	m_{100}	m_{010}	-4_{001}^-	-4_{001}^+	1	2_{001}	2_{1-10}	2_{110}
m_{010}	m_{010}	m_{100}	-4_{001}^+	-4_{001}^-	2_{001}	1	2_{110}	2_{1-10}
-4_{001}^+	-4_{001}^+	-4_{001}^-	m_{010}	m_{100}	2_{110}	2_{1-10}	2_{001}	1
-4_{001}^-	-4_{001}^-	-4_{001}^+	m_{100}	m_{010}	2_{1-10}	2_{110}	1	2_{001}

No. 15 D_{4h} $4/mmm$ [tetragonal] tag = "D4h"

* generator : 2_{001} , 4_{001}^+ , 2_{010} , -1

* conjugacy class

$$\begin{aligned}
 [1] &= 1 \\
 [2_{001}] &= 2_{001} \\
 [2_{100}] &= 2_{100}, 2_{010} \\
 [2_{110}] &= 2_{110}, 2_{1-10} \\
 [4_{001}^+] &= 4_{001}^+, 4_{001}^- \\
 [-1] &= -1 \\
 [m_{001}] &= m_{001} \\
 [m_{100}] &= m_{100}, m_{010} \\
 [m_{110}] &= m_{110}, m_{1-10} \\
 [-4_{001}^+] &= -4_{001}^+, -4_{001}^-
 \end{aligned}$$

* symmetry operation

$$\begin{array}{cccccccccccc}
 \textcircled{1} & 1 & \textcircled{2} & 2_{001} & \textcircled{3} & 2_{100} & \textcircled{4} & 2_{010} & \textcircled{5} & 2_{110} & \textcircled{6} & 2_{1-10} & \textcircled{7} & 4_{001}^+ & \textcircled{8} & 4_{001}^- & \textcircled{9} & -1 & \textcircled{10} & m_{001} \\
 \textcircled{11} & m_{100} & \textcircled{12} & m_{010} & \textcircled{13} & m_{110} & \textcircled{14} & m_{1-10} & \textcircled{15} & -4_{001}^+ & \textcircled{16} & -4_{001}^- & & & & & & & &
 \end{array}$$

* product table

	1	2 ₀₀₁	2 ₁₀₀	2 ₀₁₀	2 ₁₁₀	2 ₁₋₁₀	4 ₀₀₁ ⁺	4 ₀₀₁ ⁻	-1	m ₀₀₁	m ₁₀₀	m ₀₁₀	m ₁₁₀	m ₁₋₁₀	-4 ₀₀₁ ⁺	-4 ₀₀₁ ⁻
1	1	2 ₀₀₁	2 ₁₀₀	2 ₀₁₀	2 ₁₁₀	2 ₁₋₁₀	4 ₀₀₁ ⁺	4 ₀₀₁ ⁻	-1	m ₀₀₁	m ₁₀₀	m ₀₁₀	m ₁₁₀	m ₁₋₁₀	-4 ₀₀₁ ⁺	-4 ₀₀₁ ⁻
2 ₀₀₁	2 ₀₀₁	1	2 ₀₁₀	2 ₁₀₀	2 ₁₋₁₀	2 ₁₁₀	4 ₀₀₁ ⁻	4 ₀₀₁ ⁺	m ₀₀₁	-1	m ₀₁₀	m ₁₀₀	m ₁₋₁₀	m ₁₁₀	-4 ₀₀₁ ⁻	-4 ₀₀₁ ⁺
2 ₁₀₀	2 ₁₀₀	2 ₀₁₀	1	2 ₀₀₁	4 ₀₀₁ ⁻	4 ₀₀₁ ⁺	2 ₁₋₁₀	2 ₁₁₀	m ₁₀₀	m ₀₁₀	-1	m ₀₀₁	-4 ₀₀₁ ⁻	-4 ₀₀₁ ⁺	m ₁₋₁₀	m ₁₁₀
2 ₀₁₀	2 ₀₁₀	2 ₁₀₀	2 ₀₀₁	1	4 ₀₀₁ ⁺	4 ₀₀₁ ⁻	2 ₁₁₀	2 ₁₋₁₀	m ₀₁₀	m ₁₀₀	m ₀₀₁	-1	-4 ₀₀₁ ⁺	-4 ₀₀₁ ⁻	m ₁₁₀	m ₁₋₁₀
2 ₁₁₀	2 ₁₁₀	2 ₁₋₁₀	4 ₀₀₁ ⁺	4 ₀₀₁ ⁻	1	2 ₀₀₁	2 ₁₀₀	2 ₀₁₀	m ₁₁₀	m ₁₋₁₀	-4 ₀₀₁ ⁺	-4 ₀₀₁ ⁻	-1	m ₀₀₁	m ₁₀₀	m ₀₁₀
2 ₁₋₁₀	2 ₁₋₁₀	2 ₁₁₀	4 ₀₀₁ ⁻	4 ₀₀₁ ⁺	2 ₀₀₁	1	2 ₀₁₀	2 ₁₀₀	m ₁₋₁₀	m ₁₁₀	-4 ₀₀₁ ⁻	-4 ₀₀₁ ⁺	m ₀₀₁	-1	m ₀₁₀	m ₁₀₀
4 ₀₀₁ ⁺	4 ₀₀₁ ⁺	4 ₀₀₁ ⁻	2 ₁₁₀	2 ₁₋₁₀	2 ₀₁₀	2 ₁₀₀	2 ₀₀₁	1	-4 ₀₀₁ ⁺	-4 ₀₀₁ ⁻	m ₁₁₀	m ₁₋₁₀	m ₀₁₀	m ₁₀₀	m ₀₀₁	-1
4 ₀₀₁ ⁻	4 ₀₀₁ ⁻	4 ₀₀₁ ⁺	2 ₁₋₁₀	2 ₁₁₀	2 ₁₀₀	2 ₀₁₀	1	2 ₀₀₁	-4 ₀₀₁ ⁻	-4 ₀₀₁ ⁺	m ₁₋₁₀	m ₁₁₀	m ₁₀₀	m ₀₁₀	-1	m ₀₀₁
-1	-1	m ₀₀₁	m ₁₀₀	m ₀₁₀	m ₁₁₀	m ₁₋₁₀	-4 ₀₀₁ ⁺	-4 ₀₀₁ ⁻	1	2 ₀₀₁	2 ₁₀₀	2 ₀₁₀	2 ₁₁₀	2 ₁₋₁₀	4 ₀₀₁ ⁺	4 ₀₀₁ ⁻
m ₀₀₁	m ₀₀₁	-1	m ₀₁₀	m ₁₀₀	m ₁₋₁₀	m ₁₁₀	-4 ₀₀₁ ⁻	-4 ₀₀₁ ⁺	2 ₀₀₁	1	2 ₀₁₀	2 ₁₀₀	2 ₁₋₁₀	2 ₁₁₀	4 ₀₀₁ ⁻	4 ₀₀₁ ⁺
m ₁₀₀	m ₁₀₀	m ₀₁₀	-1	m ₀₀₁	-4 ₀₀₁ ⁻	-4 ₀₀₁ ⁺	m ₁₋₁₀	m ₁₁₀	2 ₁₀₀	2 ₀₁₀	1	2 ₀₀₁	4 ₀₀₁ ⁻	4 ₀₀₁ ⁺	2 ₁₋₁₀	2 ₁₁₀
m ₀₁₀	m ₀₁₀	m ₁₀₀	m ₀₀₁	-1	-4 ₀₀₁ ⁺	-4 ₀₀₁ ⁻	m ₁₁₀	m ₁₋₁₀	2 ₀₁₀	2 ₁₀₀	2 ₀₀₁	1	4 ₀₀₁ ⁺	4 ₀₀₁ ⁻	2 ₁₁₀	2 ₁₋₁₀
m ₁₁₀	m ₁₁₀	m ₁₋₁₀	-4 ₀₀₁ ⁺	-4 ₀₀₁ ⁻	-1	m ₀₀₁	m ₁₀₀	m ₀₁₀	2 ₁₁₀	2 ₁₋₁₀	4 ₀₀₁ ⁺	4 ₀₀₁ ⁻	1	2 ₀₀₁	2 ₁₀₀	2 ₀₁₀
m ₁₋₁₀	m ₁₋₁₀	m ₁₁₀	-4 ₀₀₁ ⁻	-4 ₀₀₁ ⁺	m ₀₀₁	-1	m ₀₁₀	m ₁₀₀	2 ₁₋₁₀	2 ₁₁₀	4 ₀₀₁ ⁻	4 ₀₀₁ ⁺	2 ₀₀₁	1	2 ₀₁₀	2 ₁₀₀
-4 ₀₀₁ ⁺	-4 ₀₀₁ ⁺	-4 ₀₀₁ ⁻	m ₁₁₀	m ₁₋₁₀	m ₀₁₀	m ₁₀₀	m ₀₀₁	-1	4 ₀₀₁ ⁺	4 ₀₀₁ ⁻	2 ₁₁₀	2 ₁₋₁₀	2 ₀₁₀	2 ₁₀₀	2 ₀₀₁	1
-4 ₀₀₁ ⁻	-4 ₀₀₁ ⁻	-4 ₀₀₁ ⁺	m ₁₋₁₀	m ₁₁₀	m ₁₀₀	m ₀₁₀	-1	m ₀₀₁	4 ₀₀₁ ⁻	4 ₀₀₁ ⁺	2 ₁₋₁₀	2 ₁₁₀	2 ₁₀₀	2 ₀₁₀	1	2 ₀₀₁

No. 16 C_3 3 [trigonal] tag = "C3"

* generator : 3_{001}^+

* conjugacy class

$$[1] = 1$$

$$[3_{001}^+] = 3_{001}^+$$

$$[3_{001}^-] = 3_{001}^-$$

* symmetry operation

$$\textcircled{1} \quad 1 \quad \textcircled{2} \quad 3_{001}^+ \quad \textcircled{3} \quad 3_{001}^-$$

* product table

	1	3_{001}^+	3_{001}^-
1	1	3_{001}^+	3_{001}^-
3_{001}^+	3_{001}^+	3_{001}^-	1
3_{001}^-	3_{001}^-	1	3_{001}^+

No. 17 C_{3i} -3 [trigonal] tag = "C3i"

* generator : 3_{001}^+ , -1

* conjugacy class

$$\begin{aligned} [1] &= 1 \\ [3_{001}^+] &= 3_{001}^+ \\ [3_{001}^-] &= 3_{001}^- \\ [-1] &= -1 \\ [-3_{001}^+] &= -3_{001}^+ \\ [-3_{001}^-] &= -3_{001}^- \end{aligned}$$

* symmetry operation

$$\textcircled{1} \quad 1 \quad \textcircled{2} \quad 3_{001}^+ \quad \textcircled{3} \quad 3_{001}^- \quad \textcircled{4} \quad -1 \quad \textcircled{5} \quad -3_{001}^+ \quad \textcircled{6} \quad -3_{001}^-$$

* product table

	1	3_{001}^+	3_{001}^-	-1	-3_{001}^+	-3_{001}^-
1	1	3_{001}^+	3_{001}^-	-1	-3_{001}^+	-3_{001}^-
3_{001}^+	3_{001}^+	3_{001}^-	1	-3_{001}^+	-3_{001}^-	-1
3_{001}^-	3_{001}^-	1	3_{001}^+	-3_{001}^-	-1	-3_{001}^+
-1	-1	-3_{001}^+	-3_{001}^-	1	3_{001}^+	3_{001}^-
-3_{001}^+	-3_{001}^+	-3_{001}^-	-1	3_{001}^+	3_{001}^-	1
-3_{001}^-	-3_{001}^-	-1	-3_{001}^+	3_{001}^-	1	3_{001}^+

No. 18 D_3 312 (312 setting) [trigonal] tag = "D3"

* generator : 3_{001}^+ , 2_{1-10}

* conjugacy class

$$[1] = 1$$

$$[2_{120}] = 2_{120}, 2_{210}, 2_{1-10}$$

$$[3_{001}^+] = 3_{001}^+, 3_{001}^-$$

* symmetry operation

$$\textcircled{1} \quad 1 \quad \textcircled{2} \quad 2_{120} \quad \textcircled{3} \quad 2_{210} \quad \textcircled{4} \quad 2_{1-10} \quad \textcircled{5} \quad 3_{001}^+ \quad \textcircled{6} \quad 3_{001}^-$$

* product table

	1	2_{120}	2_{210}	2_{1-10}	3_{001}^+	3_{001}^-
1	1	2_{120}	2_{210}	2_{1-10}	3_{001}^+	3_{001}^-
2_{120}	2_{120}	1	3_{001}^+	3_{001}^-	2_{210}	2_{1-10}
2_{210}	2_{210}	3_{001}^-	1	3_{001}^+	2_{1-10}	2_{120}
2_{1-10}	2_{1-10}	3_{001}^+	3_{001}^-	1	2_{120}	2_{210}
3_{001}^+	3_{001}^+	2_{1-10}	2_{120}	2_{210}	3_{001}^-	1
3_{001}^-	3_{001}^-	2_{210}	2_{1-10}	2_{120}	1	3_{001}^+

No. 18 $D_3 - 1$ 321 (321 setting) [trigonal] tag = "D3-1"

* generator : 3_{001}^+ , 2_{110}

* conjugacy class

$$[1] = 1$$

$$[2_{100}] = 2_{100}, 2_{010}, 2_{110}$$

$$[3_{001}^+] = 3_{001}^+, 3_{001}^-$$

* symmetry operation

$$\textcircled{1} \quad 1 \quad \textcircled{2} \quad 2_{100} \quad \textcircled{3} \quad 2_{010} \quad \textcircled{4} \quad 2_{110} \quad \textcircled{5} \quad 3_{001}^+ \quad \textcircled{6} \quad 3_{001}^-$$

* product table

	1	2_{100}	2_{010}	2_{110}	3_{001}^+	3_{001}^-
1	1	2_{100}	2_{010}	2_{110}	3_{001}^+	3_{001}^-
2_{100}	2_{100}	1	3_{001}^+	3_{001}^-	2_{010}	2_{110}
2_{010}	2_{010}	3_{001}^-	1	3_{001}^+	2_{110}	2_{100}
2_{110}	2_{110}	3_{001}^+	3_{001}^-	1	2_{100}	2_{010}
3_{001}^+	3_{001}^+	2_{110}	2_{100}	2_{010}	3_{001}^-	1
3_{001}^-	3_{001}^-	2_{010}	2_{110}	2_{100}	1	3_{001}^+

No. 19 C_{3v} $3m1$ (3m1 setting) [trigonal] tag = "C3v"

* generator : 3_{001}^+ , m_{110}

* conjugacy class

$$[1] = 1$$

$$[3_{001}^+] = 3_{001}^+, 3_{001}^-$$

$$[m_{100}] = m_{100}, m_{010}, m_{110}$$

* symmetry operation

$$\textcircled{1} \quad 1 \quad \textcircled{2} \quad 3_{001}^+ \quad \textcircled{3} \quad 3_{001}^- \quad \textcircled{4} \quad m_{100} \quad \textcircled{5} \quad m_{010} \quad \textcircled{6} \quad m_{110}$$

* product table

	1	3_{001}^+	3_{001}^-	m_{100}	m_{010}	m_{110}
1	1	3_{001}^+	3_{001}^-	m_{100}	m_{010}	m_{110}
3_{001}^+	3_{001}^+	3_{001}^-	1	m_{110}	m_{100}	m_{010}
3_{001}^-	3_{001}^-	1	3_{001}^+	m_{010}	m_{110}	m_{100}
m_{100}	m_{100}	m_{010}	m_{110}	1	3_{001}^+	3_{001}^-
m_{010}	m_{010}	m_{110}	m_{100}	3_{001}^-	1	3_{001}^+
m_{110}	m_{110}	m_{100}	m_{010}	3_{001}^+	3_{001}^-	1

No. 19 $C_{3v} - 1$ $31m$ (31m setting) [trigonal] tag = "C3v-1"

* generator : 3_{001}^+ , m_{1-10}

* conjugacy class

$$[1] = 1$$

$$[3_{001}^+] = 3_{001}^+, 3_{001}^-$$

$$[m_{120}] = m_{120}, m_{210}, m_{1-10}$$

* symmetry operation

$$\textcircled{1} \quad 1 \quad \textcircled{2} \quad 3_{001}^+ \quad \textcircled{3} \quad 3_{001}^- \quad \textcircled{4} \quad m_{120} \quad \textcircled{5} \quad m_{210} \quad \textcircled{6} \quad m_{1-10}$$

* product table

	1	3_{001}^+	3_{001}^-	m_{120}	m_{210}	m_{1-10}
1	1	3_{001}^+	3_{001}^-	m_{120}	m_{210}	m_{1-10}
3_{001}^+	3_{001}^+	3_{001}^-	1	m_{1-10}	m_{120}	m_{210}
3_{001}^-	3_{001}^-	1	3_{001}^+	m_{210}	m_{1-10}	m_{120}
m_{120}	m_{120}	m_{210}	m_{1-10}	1	3_{001}^+	3_{001}^-
m_{210}	m_{210}	m_{1-10}	m_{120}	3_{001}^-	1	3_{001}^+
m_{1-10}	m_{1-10}	m_{120}	m_{210}	3_{001}^+	3_{001}^-	1

No. 20 D_{3d} $-31m$ ($-31m$ setting) [trigonal] tag = "D3d"

* generator : 3_{001}^+ , 2_{1-10} , -1

* conjugacy class

$$[1] = 1$$

$$[2_{120}] = 2_{120}, 2_{210}, 2_{1-10}$$

$$[3_{001}^+] = 3_{001}^+, 3_{001}^-$$

$$[-1] = -1$$

$$[m_{120}] = m_{120}, m_{210}, m_{1-10}$$

$$[-3_{001}^+] = -3_{001}^+, -3_{001}^-$$

* symmetry operation

$$\begin{array}{cccccccccccc} \textcircled{1} & 1 & \textcircled{2} & 2_{120} & \textcircled{3} & 2_{210} & \textcircled{4} & 2_{1-10} & \textcircled{5} & 3_{001}^+ & \textcircled{6} & 3_{001}^- & \textcircled{7} & -1 & \textcircled{8} & m_{120} & \textcircled{9} & m_{210} & \textcircled{10} & m_{1-10} \\ \textcircled{11} & -3_{001}^+ & \textcircled{12} & -3_{001}^- & & & & & & & & & & & & & & & & & \end{array}$$

* product table

	1	2_{120}	2_{210}	2_{1-10}	3_{001}^+	3_{001}^-	-1	m_{120}	m_{210}	m_{1-10}	-3_{001}^+	-3_{001}^-
1	1	2_{120}	2_{210}	2_{1-10}	3_{001}^+	3_{001}^-	-1	m_{120}	m_{210}	m_{1-10}	-3_{001}^+	-3_{001}^-
2_{120}	2_{120}	1	3_{001}^+	3_{001}^-	2_{210}	2_{1-10}	m_{120}	-1	-3_{001}^+	-3_{001}^-	m_{210}	m_{1-10}
2_{210}	2_{210}	3_{001}^-	1	3_{001}^+	2_{1-10}	2_{120}	m_{210}	-3_{001}^-	-1	-3_{001}^+	m_{1-10}	m_{120}
2_{1-10}	2_{1-10}	3_{001}^+	3_{001}^-	1	2_{120}	2_{210}	m_{1-10}	-3_{001}^+	-3_{001}^-	-1	m_{120}	m_{210}
3_{001}^+	3_{001}^+	2_{1-10}	2_{120}	2_{210}	3_{001}^-	1	-3_{001}^+	m_{1-10}	m_{120}	m_{210}	-3_{001}^-	-1
3_{001}^-	3_{001}^-	2_{210}	2_{1-10}	2_{120}	1	3_{001}^+	-3_{001}^-	m_{210}	m_{1-10}	m_{120}	-1	-3_{001}^+
-1	-1	m_{120}	m_{210}	m_{1-10}	-3_{001}^+	-3_{001}^-	1	2_{120}	2_{210}	2_{1-10}	3_{001}^+	3_{001}^-
m_{120}	m_{120}	-1	-3_{001}^+	-3_{001}^-	m_{210}	m_{1-10}	2_{120}	1	3_{001}^+	3_{001}^-	2_{210}	2_{1-10}
m_{210}	m_{210}	-3_{001}^-	-1	-3_{001}^+	m_{1-10}	m_{120}	2_{210}	3_{001}^-	1	3_{001}^+	2_{1-10}	2_{120}
m_{1-10}	m_{1-10}	-3_{001}^+	-3_{001}^-	-1	m_{120}	m_{210}	2_{1-10}	3_{001}^+	3_{001}^-	1	2_{120}	2_{210}
-3_{001}^+	-3_{001}^+	m_{1-10}	m_{120}	m_{210}	-3_{001}^-	-1	3_{001}^+	2_{1-10}	2_{120}	2_{210}	3_{001}^-	1
-3_{001}^-	-3_{001}^-	m_{210}	m_{1-10}	m_{120}	-1	-3_{001}^+	3_{001}^-	2_{210}	2_{1-10}	2_{120}	1	3_{001}^+

No. 20 $D_{3d} - 1 - 3m1$ (-3m1 setting) [trigonal] tag = "D3d-1"

* generator : 3_{001}^+ , 2_{110} , -1

* conjugacy class

$$[1] = 1$$

$$[2_{100}] = 2_{100}, 2_{010}, 2_{110}$$

$$[3_{001}^+] = 3_{001}^+, 3_{001}^-$$

$$[-1] = -1$$

$$[m_{100}] = m_{100}, m_{010}, m_{110}$$

$$[-3_{001}^+] = -3_{001}^+, -3_{001}^-$$

* symmetry operation

$$\begin{array}{cccccccccccc} \textcircled{1} & 1 & \textcircled{2} & 2_{100} & \textcircled{3} & 2_{010} & \textcircled{4} & 2_{110} & \textcircled{5} & 3_{001}^+ & \textcircled{6} & 3_{001}^- & \textcircled{7} & -1 & \textcircled{8} & m_{100} & \textcircled{9} & m_{010} & \textcircled{10} & m_{110} \\ \textcircled{11} & -3_{001}^+ & \textcircled{12} & -3_{001}^- & & & & & & & & & & & & & & & & & \end{array}$$

* product table

	1	2_{100}	2_{010}	2_{110}	3_{001}^+	3_{001}^-	-1	m_{100}	m_{010}	m_{110}	-3_{001}^+	-3_{001}^-
1	1	2_{100}	2_{010}	2_{110}	3_{001}^+	3_{001}^-	-1	m_{100}	m_{010}	m_{110}	-3_{001}^+	-3_{001}^-
2_{100}	2_{100}	1	3_{001}^+	3_{001}^-	2_{010}	2_{110}	m_{100}	-1	-3_{001}^+	-3_{001}^-	m_{010}	m_{110}
2_{010}	2_{010}	3_{001}^-	1	3_{001}^+	2_{110}	2_{100}	m_{010}	-3_{001}^-	-1	-3_{001}^+	m_{110}	m_{100}
2_{110}	2_{110}	3_{001}^+	3_{001}^-	1	2_{100}	2_{010}	m_{110}	-3_{001}^+	-3_{001}^-	-1	m_{100}	m_{010}
3_{001}^+	3_{001}^+	2_{110}	2_{100}	2_{010}	3_{001}^-	1	-3_{001}^+	m_{110}	m_{100}	m_{010}	-3_{001}^-	-1
3_{001}^-	3_{001}^-	2_{010}	2_{110}	2_{100}	1	3_{001}^+	-3_{001}^-	m_{010}	m_{110}	m_{100}	-1	-3_{001}^+
-1	-1	m_{100}	m_{010}	m_{110}	-3_{001}^+	-3_{001}^-	1	2_{100}	2_{010}	2_{110}	3_{001}^+	3_{001}^-
m_{100}	m_{100}	-1	-3_{001}^+	-3_{001}^-	m_{010}	m_{110}	2_{100}	1	3_{001}^+	3_{001}^-	2_{010}	2_{110}
m_{010}	m_{010}	-3_{001}^-	-1	-3_{001}^+	m_{110}	m_{100}	2_{010}	3_{001}^-	1	3_{001}^+	2_{110}	2_{100}
m_{110}	m_{110}	-3_{001}^+	-3_{001}^-	-1	m_{100}	m_{010}	2_{110}	3_{001}^+	3_{001}^-	1	2_{100}	2_{010}
-3_{001}^+	-3_{001}^+	m_{110}	m_{100}	m_{010}	-3_{001}^-	-1	3_{001}^+	2_{110}	2_{100}	2_{010}	3_{001}^-	1
-3_{001}^-	-3_{001}^-	m_{010}	m_{110}	m_{100}	-1	-3_{001}^+	3_{001}^-	2_{010}	2_{110}	2_{100}	1	3_{001}^+

No. 21 C_6 6 [hexagonal] tag = "C6"

* generator : 3_{001}^+ , 2_{001}

* conjugacy class

$$\begin{aligned} [1] &= 1 \\ [2_{001}] &= 2_{001} \\ [3_{001}^+] &= 3_{001}^+ \\ [3_{001}^-] &= 3_{001}^- \\ [6_{001}^+] &= 6_{001}^+ \\ [6_{001}^-] &= 6_{001}^- \end{aligned}$$

* symmetry operation

$$\textcircled{1} \quad 1 \quad \textcircled{2} \quad 2_{001} \quad \textcircled{3} \quad 3_{001}^+ \quad \textcircled{4} \quad 3_{001}^- \quad \textcircled{5} \quad 6_{001}^+ \quad \textcircled{6} \quad 6_{001}^-$$

* product table

	1	2_{001}	3_{001}^+	3_{001}^-	6_{001}^+	6_{001}^-
1	1	2_{001}	3_{001}^+	3_{001}^-	6_{001}^+	6_{001}^-
2_{001}	2_{001}	1	6_{001}^-	6_{001}^+	3_{001}^-	3_{001}^+
3_{001}^+	3_{001}^+	6_{001}^-	3_{001}^-	1	2_{001}	6_{001}^+
3_{001}^-	3_{001}^-	6_{001}^+	1	3_{001}^+	6_{001}^-	2_{001}
6_{001}^+	6_{001}^+	3_{001}^-	2_{001}	6_{001}^-	3_{001}^+	1
6_{001}^-	6_{001}^-	3_{001}^+	6_{001}^+	2_{001}	1	3_{001}^-

No. 22 C_{3h} -6 [hexagonal] tag = "C3h"

* generator : 3_{001}^+ , m_{001}

* conjugacy class

$$\begin{aligned} [1] &= 1 \\ [3_{001}^+] &= 3_{001}^+ \\ [3_{001}^-] &= 3_{001}^- \\ [m_{001}] &= m_{001} \\ [-6_{001}^+] &= -6_{001}^+ \\ [-6_{001}^-] &= -6_{001}^- \end{aligned}$$

* symmetry operation

$$\textcircled{1} \quad 1 \quad \textcircled{2} \quad 3_{001}^+ \quad \textcircled{3} \quad 3_{001}^- \quad \textcircled{4} \quad m_{001} \quad \textcircled{5} \quad -6_{001}^+ \quad \textcircled{6} \quad -6_{001}^-$$

* product table

	1	3_{001}^+	3_{001}^-	m_{001}	-6_{001}^+	-6_{001}^-
1	1	3_{001}^+	3_{001}^-	m_{001}	-6_{001}^+	-6_{001}^-
3_{001}^+	3_{001}^+	3_{001}^-	1	-6_{001}^-	m_{001}	-6_{001}^+
3_{001}^-	3_{001}^-	1	3_{001}^+	-6_{001}^+	-6_{001}^-	m_{001}
m_{001}	m_{001}	-6_{001}^-	-6_{001}^+	1	3_{001}^-	3_{001}^+
-6_{001}^+	-6_{001}^+	m_{001}	-6_{001}^-	3_{001}^-	3_{001}^+	1
-6_{001}^-	-6_{001}^-	-6_{001}^+	m_{001}	3_{001}^+	1	3_{001}^-

No. 23 C_{6h} $6/m$ [hexagonal] tag = "C6h"

* generator : 3_{001}^+ , 2_{001} , -1

* conjugacy class

$$\begin{aligned}
 [1] &= 1 \\
 [2_{001}] &= 2_{001} \\
 [3_{001}^+] &= 3_{001}^+ \\
 [3_{001}^-] &= 3_{001}^- \\
 [6_{001}^+] &= 6_{001}^+ \\
 [6_{001}^-] &= 6_{001}^- \\
 [-1] &= -1 \\
 [m_{001}] &= m_{001} \\
 [-3_{001}^+] &= -3_{001}^+ \\
 [-3_{001}^-] &= -3_{001}^- \\
 [-6_{001}^+] &= -6_{001}^+ \\
 [-6_{001}^-] &= -6_{001}^-
 \end{aligned}$$

* symmetry operation

$$\begin{array}{cccccccccccc}
 \textcircled{1} & 1 & \textcircled{2} & 2_{001} & \textcircled{3} & 3_{001}^+ & \textcircled{4} & 3_{001}^- & \textcircled{5} & 6_{001}^+ & \textcircled{6} & 6_{001}^- & \textcircled{7} & -1 & \textcircled{8} & m_{001} & \textcircled{9} & -3_{001}^+ & \textcircled{10} & -3_{001}^- \\
 \textcircled{11} & -6_{001}^+ & \textcircled{12} & -6_{001}^- & & & & & & & & & & & & & & & & &
 \end{array}$$

* product table

	1	2_{001}	3_{001}^+	3_{001}^-	6_{001}^+	6_{001}^-	-1	m_{001}	-3_{001}^+	-3_{001}^-	-6_{001}^+	-6_{001}^-
1	1	2_{001}	3_{001}^+	3_{001}^-	6_{001}^+	6_{001}^-	-1	m_{001}	-3_{001}^+	-3_{001}^-	-6_{001}^+	-6_{001}^-
2_{001}	2_{001}	1	6_{001}^-	6_{001}^+	3_{001}^-	3_{001}^+	m_{001}	-1	-6_{001}^-	-6_{001}^+	-3_{001}^-	-3_{001}^+
3_{001}^+	3_{001}^+	6_{001}^-	3_{001}^-	1	2_{001}	6_{001}^+	-3_{001}^+	-6_{001}^-	-3_{001}^-	-1	m_{001}	-6_{001}^+
3_{001}^-	3_{001}^-	6_{001}^+	1	3_{001}^+	6_{001}^-	2_{001}	-3_{001}^-	-6_{001}^+	-1	-3_{001}^+	-6_{001}^-	m_{001}
6_{001}^+	6_{001}^+	3_{001}^-	2_{001}	6_{001}^-	3_{001}^+	1	-6_{001}^+	-3_{001}^-	m_{001}	-6_{001}^-	-3_{001}^+	-1
6_{001}^-	6_{001}^-	3_{001}^+	6_{001}^+	2_{001}	1	3_{001}^-	-6_{001}^-	-3_{001}^+	-6_{001}^+	m_{001}	-1	-3_{001}^-
-1	-1	m_{001}	-3_{001}^+	-3_{001}^-	-6_{001}^+	-6_{001}^-	1	2_{001}	3_{001}^+	3_{001}^-	6_{001}^+	6_{001}^-
m_{001}	m_{001}	-1	-6_{001}^-	-6_{001}^+	-3_{001}^-	-3_{001}^+	2_{001}	1	6_{001}^-	6_{001}^+	3_{001}^-	3_{001}^+
-3_{001}^+	-3_{001}^+	-6_{001}^-	-3_{001}^-	-1	m_{001}	-6_{001}^+	3_{001}^+	6_{001}^-	3_{001}^-	1	2_{001}	6_{001}^+
-3_{001}^-	-3_{001}^-	-6_{001}^+	-1	-3_{001}^+	-6_{001}^-	m_{001}	3_{001}^-	6_{001}^+	1	3_{001}^+	6_{001}^-	2_{001}
-6_{001}^+	-6_{001}^+	-3_{001}^-	m_{001}	-6_{001}^-	-3_{001}^+	-1	6_{001}^+	3_{001}^-	2_{001}	6_{001}^-	3_{001}^+	1
-6_{001}^-	-6_{001}^-	-3_{001}^+	-6_{001}^+	m_{001}	-1	-3_{001}^-	6_{001}^-	3_{001}^+	6_{001}^+	2_{001}	1	3_{001}^-

No. 24 D_6 622 [hexagonal] tag = "D6"

* generator : 3_{001}^+ , 2_{001} , 2_{110}

* conjugacy class

$$[1] = 1$$

$$[2_{001}] = 2_{001}$$

$$[2_{100}] = 2_{100}, 2_{010}, 2_{110}$$

$$[2_{120}] = 2_{120}, 2_{210}, 2_{1-10}$$

$$[3_{001}^+] = 3_{001}^+, 3_{001}^-$$

$$[6_{001}^+] = 6_{001}^+, 6_{001}^-$$

* symmetry operation

$$\begin{array}{cccccccccccc} \textcircled{1} & 1 & \textcircled{2} & 2_{001} & \textcircled{3} & 2_{100} & \textcircled{4} & 2_{010} & \textcircled{5} & 2_{110} & \textcircled{6} & 2_{120} & \textcircled{7} & 2_{210} & \textcircled{8} & 2_{1-10} & \textcircled{9} & 3_{001}^+ & \textcircled{10} & 3_{001}^- \\ \textcircled{11} & 6_{001}^+ & \textcircled{12} & 6_{001}^- & & & & & & & & & & & & & & & & & \end{array}$$

* product table

	1	2_{001}	2_{100}	2_{010}	2_{110}	2_{120}	2_{210}	2_{1-10}	3_{001}^+	3_{001}^-	6_{001}^+	6_{001}^-
1	1	2_{001}	2_{100}	2_{010}	2_{110}	2_{120}	2_{210}	2_{1-10}	3_{001}^+	3_{001}^-	6_{001}^+	6_{001}^-
2_{001}	2_{001}	1	2_{120}	2_{210}	2_{1-10}	2_{100}	2_{010}	2_{110}	6_{001}^-	6_{001}^+	3_{001}^-	3_{001}^+
2_{100}	2_{100}	2_{120}	1	3_{001}^+	3_{001}^-	2_{001}	6_{001}^-	6_{001}^+	2_{010}	2_{110}	2_{1-10}	2_{210}
2_{010}	2_{010}	2_{210}	3_{001}^-	1	3_{001}^+	6_{001}^+	2_{001}	6_{001}^-	2_{110}	2_{100}	2_{120}	2_{1-10}
2_{110}	2_{110}	2_{1-10}	3_{001}^+	3_{001}^-	1	6_{001}^-	6_{001}^+	2_{001}	2_{100}	2_{010}	2_{210}	2_{120}
2_{120}	2_{120}	2_{100}	2_{001}	6_{001}^-	6_{001}^+	1	3_{001}^+	3_{001}^-	2_{210}	2_{1-10}	2_{110}	2_{010}
2_{210}	2_{210}	2_{010}	6_{001}^+	2_{001}	6_{001}^-	3_{001}^-	1	3_{001}^+	2_{1-10}	2_{120}	2_{100}	2_{110}
2_{1-10}	2_{1-10}	2_{110}	6_{001}^-	6_{001}^+	2_{001}	3_{001}^+	3_{001}^-	1	2_{120}	2_{210}	2_{010}	2_{100}
3_{001}^+	3_{001}^+	6_{001}^-	2_{110}	2_{100}	2_{010}	2_{1-10}	2_{120}	2_{210}	3_{001}^-	1	2_{001}	6_{001}^+
3_{001}^-	3_{001}^-	6_{001}^+	2_{010}	2_{110}	2_{100}	2_{210}	2_{1-10}	2_{120}	1	3_{001}^+	6_{001}^-	2_{001}
6_{001}^+	6_{001}^+	3_{001}^-	2_{210}	2_{1-10}	2_{120}	2_{010}	2_{110}	2_{100}	2_{001}	6_{001}^-	3_{001}^+	1
6_{001}^-	6_{001}^-	3_{001}^+	2_{1-10}	2_{120}	2_{210}	2_{110}	2_{100}	2_{010}	6_{001}^+	2_{001}	1	3_{001}^-

No. 25 C_{6v} $6mm$ [hexagonal] tag = "C6v"

* generator : 3_{001}^+ , 2_{001} , m_{110}

* conjugacy class

$$[1] = 1$$

$$[2_{001}] = 2_{001}$$

$$[3_{001}^+] = 3_{001}^+, 3_{001}^-$$

$$[6_{001}^+] = 6_{001}^+, 6_{001}^-$$

$$[m_{100}] = m_{100}, m_{010}, m_{110}$$

$$[m_{120}] = m_{120}, m_{210}, m_{1-10}$$

* symmetry operation

$$\begin{array}{cccccccccccc} \textcircled{1} & 1 & \textcircled{2} & 2_{001} & \textcircled{3} & 3_{001}^+ & \textcircled{4} & 3_{001}^- & \textcircled{5} & 6_{001}^+ & \textcircled{6} & 6_{001}^- & \textcircled{7} & m_{100} & \textcircled{8} & m_{010} & \textcircled{9} & m_{110} & \textcircled{10} & m_{120} \\ \textcircled{11} & m_{210} & \textcircled{12} & m_{1-10} & & & & & & & & & & & & & & & & & \end{array}$$

* product table

	1	2 ₀₀₁	3 ⁺ ₀₀₁	3 ⁻ ₀₀₁	6 ⁺ ₀₀₁	6 ⁻ ₀₀₁	m ₁₀₀	m ₀₁₀	m ₁₁₀	m ₁₂₀	m ₂₁₀	m ₁₋₁₀
1	1	2 ₀₀₁	3 ⁺ ₀₀₁	3 ⁻ ₀₀₁	6 ⁺ ₀₀₁	6 ⁻ ₀₀₁	m ₁₀₀	m ₀₁₀	m ₁₁₀	m ₁₂₀	m ₂₁₀	m ₁₋₁₀
2 ₀₀₁	2 ₀₀₁	1	6 ⁻ ₀₀₁	6 ⁺ ₀₀₁	3 ⁻ ₀₀₁	3 ⁺ ₀₀₁	m ₁₂₀	m ₂₁₀	m ₁₋₁₀	m ₁₀₀	m ₀₁₀	m ₁₁₀
3 ⁺ ₀₀₁	3 ⁺ ₀₀₁	6 ⁻ ₀₀₁	3 ⁻ ₀₀₁	1	2 ₀₀₁	6 ⁺ ₀₀₁	m ₁₁₀	m ₁₀₀	m ₀₁₀	m ₁₋₁₀	m ₁₂₀	m ₂₁₀
3 ⁻ ₀₀₁	3 ⁻ ₀₀₁	6 ⁺ ₀₀₁	1	3 ⁺ ₀₀₁	6 ⁻ ₀₀₁	2 ₀₀₁	m ₀₁₀	m ₁₁₀	m ₁₀₀	m ₂₁₀	m ₁₋₁₀	m ₁₂₀
6 ⁺ ₀₀₁	6 ⁺ ₀₀₁	3 ⁻ ₀₀₁	2 ₀₀₁	6 ⁻ ₀₀₁	3 ⁺ ₀₀₁	1	m ₂₁₀	m ₁₋₁₀	m ₁₂₀	m ₀₁₀	m ₁₁₀	m ₁₀₀
6 ⁻ ₀₀₁	6 ⁻ ₀₀₁	3 ⁺ ₀₀₁	6 ⁺ ₀₀₁	2 ₀₀₁	1	3 ⁻ ₀₀₁	m ₁₋₁₀	m ₁₂₀	m ₂₁₀	m ₁₁₀	m ₁₀₀	m ₀₁₀
m ₁₀₀	m ₁₀₀	m ₁₂₀	m ₀₁₀	m ₁₁₀	m ₁₋₁₀	m ₂₁₀	1	3 ⁺ ₀₀₁	3 ⁻ ₀₀₁	2 ₀₀₁	6 ⁻ ₀₀₁	6 ⁺ ₀₀₁
m ₀₁₀	m ₀₁₀	m ₂₁₀	m ₁₁₀	m ₁₀₀	m ₁₂₀	m ₁₋₁₀	3 ⁻ ₀₀₁	1	3 ⁺ ₀₀₁	6 ⁺ ₀₀₁	2 ₀₀₁	6 ⁻ ₀₀₁
m ₁₁₀	m ₁₁₀	m ₁₋₁₀	m ₁₀₀	m ₀₁₀	m ₂₁₀	m ₁₂₀	3 ⁺ ₀₀₁	3 ⁻ ₀₀₁	1	6 ⁻ ₀₀₁	6 ⁺ ₀₀₁	2 ₀₀₁
m ₁₂₀	m ₁₂₀	m ₁₀₀	m ₂₁₀	m ₁₋₁₀	m ₁₁₀	m ₀₁₀	2 ₀₀₁	6 ⁻ ₀₀₁	6 ⁺ ₀₀₁	1	3 ⁺ ₀₀₁	3 ⁻ ₀₀₁
m ₂₁₀	m ₂₁₀	m ₀₁₀	m ₁₋₁₀	m ₁₂₀	m ₁₀₀	m ₁₁₀	6 ⁺ ₀₀₁	2 ₀₀₁	6 ⁻ ₀₀₁	3 ⁻ ₀₀₁	1	3 ⁺ ₀₀₁
m ₁₋₁₀	m ₁₋₁₀	m ₁₁₀	m ₁₂₀	m ₂₁₀	m ₀₁₀	m ₁₀₀	6 ⁻ ₀₀₁	6 ⁺ ₀₀₁	2 ₀₀₁	3 ⁺ ₀₀₁	3 ⁻ ₀₀₁	1

No. 26 D_{3h} $-6m2$ ($-6m2$ setting) [hexagonal] tag = "D3h"

* generator : 3_{001}^+ , m_{001} , m_{110}

* conjugacy class

$$[1] = 1$$

$$[2_{120}] = 2_{120}, 2_{210}, 2_{1-10}$$

$$[3_{001}^+] = 3_{001}^+, 3_{001}^-$$

$$[m_{100}] = m_{100}, m_{010}, m_{110}$$

$$[m_{001}] = m_{001}$$

$$[-6_{001}^+] = -6_{001}^+, -6_{001}^-$$

* symmetry operation

$$\begin{array}{cccccccccccc} \textcircled{1} & 1 & \textcircled{2} & 2_{120} & \textcircled{3} & 2_{210} & \textcircled{4} & 2_{1-10} & \textcircled{5} & 3_{001}^+ & \textcircled{6} & 3_{001}^- & \textcircled{7} & m_{100} & \textcircled{8} & m_{010} & \textcircled{9} & m_{110} & \textcircled{10} & m_{001} \\ \textcircled{11} & -6_{001}^+ & \textcircled{12} & -6_{001}^- & & & & & & & & & & & & & & & & & \end{array}$$

* product table

	1	2_{120}	2_{210}	2_{1-10}	3_{001}^+	3_{001}^-	m_{100}	m_{010}	m_{110}	m_{001}	-6_{001}^+	-6_{001}^-
1	1	2_{120}	2_{210}	2_{1-10}	3_{001}^+	3_{001}^-	m_{100}	m_{010}	m_{110}	m_{001}	-6_{001}^+	-6_{001}^-
2_{120}	2_{120}	1	3_{001}^+	3_{001}^-	2_{210}	2_{1-10}	m_{001}	-6_{001}^-	-6_{001}^+	m_{100}	m_{110}	m_{010}
2_{210}	2_{210}	3_{001}^-	1	3_{001}^+	2_{1-10}	2_{120}	-6_{001}^+	m_{001}	-6_{001}^-	m_{010}	m_{100}	m_{110}
2_{1-10}	2_{1-10}	3_{001}^+	3_{001}^-	1	2_{120}	2_{210}	-6_{001}^-	-6_{001}^+	m_{001}	m_{110}	m_{010}	m_{100}
3_{001}^+	3_{001}^+	2_{1-10}	2_{120}	2_{210}	3_{001}^-	1	m_{110}	m_{100}	m_{010}	-6_{001}^-	m_{001}	-6_{001}^+
3_{001}^-	3_{001}^-	2_{210}	2_{1-10}	2_{120}	1	3_{001}^+	m_{010}	m_{110}	m_{100}	-6_{001}^+	-6_{001}^-	m_{001}
m_{100}	m_{100}	m_{001}	-6_{001}^-	-6_{001}^+	m_{010}	m_{110}	1	3_{001}^+	3_{001}^-	2_{120}	2_{1-10}	2_{210}
m_{010}	m_{010}	-6_{001}^+	m_{001}	-6_{001}^-	m_{110}	m_{100}	3_{001}^-	1	3_{001}^+	2_{210}	2_{120}	2_{1-10}
m_{110}	m_{110}	-6_{001}^-	-6_{001}^+	m_{001}	m_{100}	m_{010}	3_{001}^+	3_{001}^-	1	2_{1-10}	2_{210}	2_{120}
m_{001}	m_{001}	m_{100}	m_{010}	m_{110}	-6_{001}^-	-6_{001}^+	2_{120}	2_{210}	2_{1-10}	1	3_{001}^-	3_{001}^+
-6_{001}^+	-6_{001}^+	m_{010}	m_{110}	m_{100}	m_{001}	-6_{001}^-	2_{210}	2_{1-10}	2_{120}	3_{001}^-	3_{001}^+	1
-6_{001}^-	-6_{001}^-	m_{110}	m_{100}	m_{010}	-6_{001}^+	m_{001}	2_{1-10}	2_{120}	2_{210}	3_{001}^+	1	3_{001}^-

No. 26 $D_{3h} - 1$ $-62m$ (-62m setting) [hexagonal] tag = "D3h-1"

* generator : 3_{001}^+ , m_{001} , 2_{110}

* conjugacy class

$$[1] = 1$$

$$[2_{100}] = 2_{100}, 2_{010}, 2_{110}$$

$$[3_{001}^+] = 3_{001}^+, 3_{001}^-$$

$$[m_{001}] = m_{001}$$

$$[m_{120}] = m_{120}, m_{210}, m_{1-10}$$

$$[-6_{001}^+] = -6_{001}^+, -6_{001}^-$$

* symmetry operation

$$\begin{array}{cccccccccccc} \textcircled{1} & 1 & \textcircled{2} & 2_{100} & \textcircled{3} & 2_{010} & \textcircled{4} & 2_{110} & \textcircled{5} & 3_{001}^+ & \textcircled{6} & 3_{001}^- & \textcircled{7} & m_{001} & \textcircled{8} & m_{120} & \textcircled{9} & m_{210} & \textcircled{10} & m_{1-10} \\ \textcircled{11} & -6_{001}^+ & \textcircled{12} & -6_{001}^- & & & & & & & & & & & & & & & & & \end{array}$$

* product table

	1	2_{100}	2_{010}	2_{110}	3_{001}^+	3_{001}^-	m_{001}	m_{120}	m_{210}	m_{1-10}	-6_{001}^+	-6_{001}^-
1	1	2_{100}	2_{010}	2_{110}	3_{001}^+	3_{001}^-	m_{001}	m_{120}	m_{210}	m_{1-10}	-6_{001}^+	-6_{001}^-
2_{100}	2_{100}	1	3_{001}^+	3_{001}^-	2_{010}	2_{110}	m_{120}	m_{001}	-6_{001}^-	-6_{001}^+	m_{1-10}	m_{210}
2_{010}	2_{010}	3_{001}^-	1	3_{001}^+	2_{110}	2_{100}	m_{210}	-6_{001}^+	m_{001}	-6_{001}^-	m_{120}	m_{1-10}
2_{110}	2_{110}	3_{001}^+	3_{001}^-	1	2_{100}	2_{010}	m_{1-10}	-6_{001}^-	-6_{001}^+	m_{001}	m_{210}	m_{120}
3_{001}^+	3_{001}^+	2_{110}	2_{100}	2_{010}	3_{001}^-	1	-6_{001}^-	m_{1-10}	m_{120}	m_{210}	m_{001}	-6_{001}^+
3_{001}^-	3_{001}^-	2_{010}	2_{110}	2_{100}	1	3_{001}^+	-6_{001}^+	m_{210}	m_{1-10}	m_{120}	-6_{001}^-	m_{001}
m_{001}	m_{001}	m_{120}	m_{210}	m_{1-10}	-6_{001}^-	-6_{001}^+	1	2_{100}	2_{010}	2_{110}	3_{001}^-	3_{001}^+
m_{120}	m_{120}	m_{001}	-6_{001}^-	-6_{001}^+	m_{210}	m_{1-10}	2_{100}	1	3_{001}^+	3_{001}^-	2_{110}	2_{010}
m_{210}	m_{210}	-6_{001}^+	m_{001}	-6_{001}^-	m_{1-10}	m_{120}	2_{010}	3_{001}^-	1	3_{001}^+	2_{100}	2_{110}
m_{1-10}	m_{1-10}	-6_{001}^-	-6_{001}^+	m_{001}	m_{120}	m_{210}	2_{110}	3_{001}^+	3_{001}^-	1	2_{010}	2_{100}
-6_{001}^+	-6_{001}^+	m_{210}	m_{1-10}	m_{120}	m_{001}	-6_{001}^-	3_{001}^-	2_{010}	2_{110}	2_{100}	3_{001}^+	1
-6_{001}^-	-6_{001}^-	m_{1-10}	m_{120}	m_{210}	-6_{001}^+	m_{001}	3_{001}^+	2_{110}	2_{100}	2_{010}	1	3_{001}^-

No. 27 D_{6h} $6/mmm$ [hexagonal] tag = "D6h"

* generator : 3_{001}^+ , 2_{001} , 2_{110} , -1

* conjugacy class

$$\begin{aligned}
[1] &= 1 \\
[2_{001}] &= 2_{001} \\
[2_{100}] &= 2_{100}, 2_{010}, 2_{110} \\
[2_{120}] &= 2_{120}, 2_{210}, 2_{1-10} \\
[3_{001}^+] &= 3_{001}^+, 3_{001}^- \\
[6_{001}^+] &= 6_{001}^+, 6_{001}^- \\
[-1] &= -1 \\
[m_{100}] &= m_{100}, m_{010}, m_{110} \\
[m_{001}] &= m_{001} \\
[m_{120}] &= m_{120}, m_{210}, m_{1-10} \\
[-3_{001}^+] &= -3_{001}^+, -3_{001}^- \\
[-6_{001}^+] &= -6_{001}^+, -6_{001}^-
\end{aligned}$$

* symmetry operation

①	1	②	2_{001}	③	2_{100}	④	2_{010}	⑤	2_{110}	⑥	2_{120}	⑦	2_{210}	⑧	2_{1-10}	⑨	3_{001}^+	⑩	3_{001}^-
⑪	6_{001}^+	⑫	6_{001}^-	⑬	-1	⑭	m_{100}	⑮	m_{010}	⑯	m_{110}	⑰	m_{001}	⑱	m_{120}	⑲	m_{210}	⑳	m_{1-10}
㉑	-3_{001}^+	㉒	-3_{001}^-	㉓	-6_{001}^+	㉔	-6_{001}^-												

* product table omitted because of large table.

No. 28 T 23 [cubic] tag = "T"

* generator : 2_{001} , 2_{010} , 3_{111}^+

* conjugacy class

$$[1] = 1$$

$$[2_{001}] = 2_{001}, 2_{100}, 2_{010}$$

$$[3_{111}^+] = 3_{111}^+, 3_{1-1-1}^+, 3_{-11-1}^+, 3_{-1-11}^+$$

$$[3_{111}^-] = 3_{111}^-, 3_{1-1-1}^-, 3_{-11-1}^-, 3_{-1-11}^-$$

* symmetry operation

$$\begin{array}{cccccccccccc} \textcircled{1} & 1 & \textcircled{2} & 2_{001} & \textcircled{3} & 2_{100} & \textcircled{4} & 2_{010} & \textcircled{5} & 3_{111}^+ & \textcircled{6} & 3_{1-1-1}^+ & \textcircled{7} & 3_{-11-1}^+ & \textcircled{8} & 3_{-1-11}^+ & \textcircled{9} & 3_{111}^- & \textcircled{10} & 3_{1-1-1}^- \\ \textcircled{11} & 3_{-11-1}^- & \textcircled{12} & 3_{-1-11}^- & & & & & & & & & & & & & & & & & \end{array}$$

* product table

	1	2_{001}	2_{100}	2_{010}	3_{111}^+	3_{1-1-1}^+	3_{-11-1}^+	3_{-1-11}^+	3_{111}^-	3_{1-1-1}^-	3_{-11-1}^-	3_{-1-11}^-
1	1	2_{001}	2_{100}	2_{010}	3_{111}^+	3_{1-1-1}^+	3_{-11-1}^+	3_{-1-11}^+	3_{111}^-	3_{1-1-1}^-	3_{-11-1}^-	3_{-1-11}^-
2_{001}	2_{001}	1	2_{010}	2_{100}	3_{1-1-1}^+	3_{111}^+	3_{-1-11}^+	3_{-11-1}^+	3_{-11-1}^-	3_{-1-11}^-	3_{111}^-	3_{1-1-1}^-
2_{100}	2_{100}	2_{010}	1	2_{001}	3_{-11-1}^+	3_{-1-11}^+	3_{111}^+	3_{1-1-1}^+	3_{-1-11}^-	3_{-11-1}^-	3_{1-1-1}^-	3_{111}^-
2_{010}	2_{010}	2_{100}	2_{001}	1	3_{-1-11}^+	3_{-11-1}^+	3_{1-1-1}^+	3_{111}^+	3_{1-1-1}^-	3_{111}^-	3_{-1-11}^-	3_{-11-1}^-
3_{111}^+	3_{111}^+	3_{-11-1}^+	3_{-1-11}^+	3_{1-1-1}^+	3_{111}^-	3_{-1-11}^-	3_{1-1-1}^-	3_{-11-1}^-	1	2_{001}	2_{100}	2_{010}
3_{1-1-1}^+	3_{1-1-1}^+	3_{-1-11}^+	3_{-11-1}^+	3_{111}^+	3_{-11-1}^-	3_{1-1-1}^-	3_{-1-11}^-	3_{111}^-	2_{001}	1	2_{010}	2_{100}
3_{-11-1}^+	3_{-11-1}^+	3_{111}^+	3_{1-1-1}^+	3_{-1-11}^+	3_{-1-11}^-	3_{111}^-	3_{-11-1}^-	3_{1-1-1}^-	2_{100}	2_{010}	1	2_{001}
3_{-1-11}^+	3_{-1-11}^+	3_{1-1-1}^+	3_{111}^+	3_{-11-1}^+	3_{1-1-1}^-	3_{-11-1}^-	3_{111}^-	3_{-1-11}^-	2_{010}	2_{100}	2_{001}	1
3_{111}^-	3_{111}^-	3_{1-1-1}^-	3_{-11-1}^-	3_{-1-11}^-	1	2_{010}	2_{001}	2_{100}	3_{111}^+	3_{-11-1}^+	3_{-1-11}^+	3_{1-1-1}^+
3_{1-1-1}^-	3_{1-1-1}^-	3_{111}^-	3_{-1-11}^-	3_{-11-1}^-	2_{010}	1	2_{100}	2_{001}	3_{-1-11}^+	3_{1-1-1}^+	3_{111}^+	3_{-11-1}^+
3_{-11-1}^-	3_{-11-1}^-	3_{-1-11}^-	3_{111}^-	3_{1-1-1}^-	2_{001}	2_{100}	1	2_{010}	3_{1-1-1}^+	3_{-1-11}^+	3_{-11-1}^+	3_{111}^+
3_{-1-11}^-	3_{-1-11}^-	3_{-11-1}^-	3_{1-1-1}^-	3_{111}^-	2_{100}	2_{001}	2_{010}	1	3_{-11-1}^+	3_{111}^+	3_{1-1-1}^+	3_{-1-11}^+

No. 29 T_h $m-3$ [cubic] tag = "Th"

* generator : 2_{001} , 2_{010} , 3_{111}^+ , -1

* conjugacy class

$$\begin{aligned}
 [1] &= 1 \\
 [2_{001}] &= 2_{001}, 2_{100}, 2_{010} \\
 [3_{111}^+] &= 3_{111}^+, 3_{1-1-1}^+, 3_{-11-1}^+, 3_{-1-11}^+ \\
 [3_{111}^-] &= 3_{111}^-, 3_{1-1-1}^-, 3_{-11-1}^-, 3_{-1-11}^- \\
 [-1] &= -1 \\
 [m_{001}] &= m_{001}, m_{100}, m_{010} \\
 [-3_{111}^+] &= -3_{111}^+, -3_{1-1-1}^+, -3_{-11-1}^+, -3_{-1-11}^+ \\
 [-3_{111}^-] &= -3_{111}^-, -3_{1-1-1}^-, -3_{-11-1}^-, -3_{-1-11}^-
 \end{aligned}$$

* symmetry operation

① 1	② 2_{001}	③ 2_{100}	④ 2_{010}	⑤ 3_{111}^+	⑥ 3_{1-1-1}^+	⑦ 3_{-11-1}^+	⑧ 3_{-1-11}^+	⑨ 3_{111}^-	⑩ 3_{1-1-1}^-
⑪ 3_{-11-1}^-	⑫ 3_{-1-11}^-	⑬ -1	⑭ m_{001}	⑮ m_{100}	⑯ m_{010}	⑰ -3_{111}^+	⑱ -3_{1-1-1}^+	⑲ -3_{-11-1}^+	⑳ -3_{-1-11}^+
㉑ -3_{111}^-	㉒ -3_{1-1-1}^-	㉓ -3_{-11-1}^-	㉔ -3_{-1-11}^-						

* product table omitted because of large table.

No. 30 O 432 [cubic] tag = "0"

* generator : $2_{001}, 2_{010}, 3_{111}^+, 2_{110}$

* conjugacy class

$$[1] = 1$$

$$[2_{001}] = 2_{001}, 2_{100}, 2_{010}$$

$$[2_{110}] = 2_{110}, 2_{101}, 2_{011}, 2_{1-10}, 2_{-101}, 2_{01-1}$$

$$[3_{111}^+] = 3_{111}^+, 3_{1-1-1}^+, 3_{-11-1}^+, 3_{-1-11}^+, 3_{111}^-, 3_{1-1-1}^-, 3_{-11-1}^-, 3_{-1-11}^-$$

$$[4_{001}^+] = 4_{001}^+, 4_{100}^+, 4_{010}^+, 4_{001}^-, 4_{100}^-, 4_{010}^-$$

* symmetry operation

① 1	② 2_{001}	③ 2_{100}	④ 2_{010}	⑤ 2_{110}	⑥ 2_{101}	⑦ 2_{011}	⑧ 2_{1-10}	⑨ 2_{-101}	⑩ 2_{01-1}
⑪ 3_{111}^+	⑫ 3_{1-1-1}^+	⑬ 3_{-11-1}^+	⑭ 3_{-1-11}^+	⑮ 3_{111}^-	⑯ 3_{1-1-1}^-	⑰ 3_{-11-1}^-	⑱ 3_{-1-11}^-	⑲ 4_{001}^+	⑳ 4_{100}^+
㉑ 4_{010}^+	㉒ 4_{-001}^-	㉓ 4_{100}^-	㉔ 4_{010}^-						

* product table omitted because of large table.

No. 31 T_d $-43m$ [cubic] tag = "Td"

* generator : 2_{001} , 2_{010} , 3_{111}^+ , m_{1-10}

* conjugacy class

$$\begin{aligned}
 [1] &= 1 \\
 [2_{001}] &= 2_{001}, 2_{100}, 2_{010} \\
 [3_{111}^+] &= 3_{111}^+, 3_{1-1-1}^+, 3_{-11-1}^+, 3_{-1-11}^+, 3_{111}^-, 3_{1-1-1}^-, 3_{-11-1}^-, 3_{-1-11}^- \\
 [m_{110}] &= m_{110}, m_{101}, m_{011}, m_{1-10}, m_{-101}, m_{01-1} \\
 [-4_{001}^+] &= -4_{001}^+, -4_{100}^+, -4_{010}^+, -4_{001}^-, -4_{100}^-, -4_{010}^-
 \end{aligned}$$

* symmetry operation

$$\begin{array}{llllllllll}
 \textcircled{1} & 1 & \textcircled{2} & 2_{001} & \textcircled{3} & 2_{100} & \textcircled{4} & 2_{010} & \textcircled{5} & 3_{111}^+ & \textcircled{6} & 3_{1-1-1}^+ & \textcircled{7} & 3_{-11-1}^+ & \textcircled{8} & 3_{-1-11}^+ & \textcircled{9} & 3_{111}^- & \textcircled{10} & 3_{1-1-1}^- \\
 \textcircled{11} & 3_{-11-1}^- & \textcircled{12} & 3_{-1-11}^- & \textcircled{13} & m_{110} & \textcircled{14} & m_{101} & \textcircled{15} & m_{011} & \textcircled{16} & m_{1-10} & \textcircled{17} & m_{-101} & \textcircled{18} & m_{01-1} & \textcircled{19} & -4_{001}^+ & \textcircled{20} & -4_{100}^+ \\
 \textcircled{21} & -4_{010}^+ & \textcircled{22} & -4_{001}^- & \textcircled{23} & -4_{100}^- & \textcircled{24} & -4_{010}^- & & & & & & & & & & & & &
 \end{array}$$

* product table omitted because of large table.

No. 32 O_h $m - 3m$ [cubic] tag = "0h"

* generator : $2_{001}, 2_{010}, 3_{111}^+, 2_{110}, -1$

* conjugacy class

$$\begin{aligned}
[1] &= 1 \\
[2_{001}] &= 2_{001}, 2_{100}, 2_{010} \\
[2_{110}] &= 2_{110}, 2_{101}, 2_{011}, 2_{1-10}, 2_{-101}, 2_{01-1} \\
[3_{111}^+] &= 3_{111}^+, 3_{1-1-1}^+, 3_{-11-1}^+, 3_{-1-11}^+, 3_{111}^-, 3_{1-1-1}^-, 3_{-11-1}^-, 3_{-1-11}^- \\
[4_{001}^+] &= 4_{001}^+, 4_{100}^+, 4_{010}^+, 4_{001}^-, 4_{100}^-, 4_{010}^- \\
[-1] &= -1 \\
[m_{001}] &= m_{001}, m_{100}, m_{010} \\
[m_{110}] &= m_{110}, m_{101}, m_{011}, m_{1-10}, m_{-101}, m_{01-1} \\
[-3_{111}^+] &= -3_{111}^+, -3_{1-1-1}^+, -3_{-11-1}^+, -3_{-1-11}^+, -3_{111}^-, -3_{1-1-1}^-, -3_{-11-1}^-, -3_{-1-11}^- \\
[-4_{001}^+] &= -4_{001}^+, -4_{100}^+, -4_{010}^+, -4_{001}^-, -4_{100}^-, -4_{010}^-
\end{aligned}$$

* symmetry operation

① 1	② 2_{001}	③ 2_{100}	④ 2_{010}	⑤ 2_{110}	⑥ 2_{101}	⑦ 2_{011}	⑧ 2_{1-10}	⑨ 2_{-101}	⑩ 2_{01-1}
⑪ 3_{111}^+	⑫ 3_{1-1-1}^+	⑬ 3_{-11-1}^+	⑭ 3_{-1-11}^+	⑮ 3_{111}^-	⑯ 3_{1-1-1}^-	⑰ 3_{-11-1}^-	⑱ 3_{-1-11}^-	⑲ 4_{001}^+	⑳ 4_{100}^+
㉑ 4_{010}^+	㉒ 4_{001}^-	㉓ 4_{100}^-	㉔ 4_{010}^-	㉕ -1	㉖ m_{001}	㉗ m_{100}	㉘ m_{010}	㉙ m_{110}	㉚ m_{101}
㉛ m_{011}	㉜ m_{1-10}	㉝ m_{-101}	㉞ m_{01-1}	㉟ -3_{111}^+	㊱ -3_{1-1-1}^+	㊲ -3_{-11-1}^+	㊳ -3_{-1-11}^+	㊴ -3_{111}^-	㊵ -3_{1-1-1}^-
㊶ -3_{-11-1}^-	㊷ -3_{-1-11}^-	㊸ -4_{001}^+	㊹ -4_{100}^+	㊺ -4_{010}^+	㊻ -4_{001}^-	㊼ -4_{100}^-	㊽ -4_{010}^-		

* product table omitted because of large table.