

* Rank 0 tensor.

$$[Q]$$

$$Q = Q_s^{(1)}$$

* Rank 1 tensor.

$$[0 \quad 0 \quad Q_z]$$

$$Q_z = Q_{pz}^{(1)}$$

* Rank 2 tensor (s).

$$\begin{bmatrix} Q_{xx} & 0 & 0 \\ 0 & Q_{xx} & 0 \\ 0 & 0 & Q_{zz} \end{bmatrix}$$

$$Q_{xx} = -Q_{du}^{(1)} + Q_s^{(1)}$$

$$Q_{zz} = 2Q_{du}^{(1)} + Q_s^{(1)}$$

* Rank 2 tensor (a).

$$\begin{bmatrix} 0 & Q_{xy} & 0 \\ -Q_{xy} & 0 & 0 \\ 0 & 0 & 0 \end{bmatrix}$$

$$Q_{xy} = G_{pz}^{(1)}$$

* Rank 3 tensor (s).

$$\begin{bmatrix} Q_{xxx} & Q_{xxy} & Q_{xxz} \\ -Q_{xxx} & -Q_{xxy} & Q_{xxz} \\ 0 & 0 & Q_{zzz} \\ Q_{yzx} & Q_{yyz} & 0 \\ Q_{yzy} & -Q_{yzx} & 0 \\ Q_{xyy} & -Q_{xxx} & 0 \end{bmatrix}$$

$$Q_{xxx} = Q_{f2}^{(1)}$$

$$Q_{xxy} = Q_{f1}^{(1)}$$

$$Q_{xxz} = -Q_{faz}^{(1)} + Q_{pz}^{(1)}$$

$$Q_{zzz} = 2Q_{faz}^{(1)} + Q_{pz}^{(1)} + 2Q_{pz}^{(2)}$$

$$Q_{yzx} = -3G_{du}^{(1)}$$

$$Q_{yzy} = -Q_{faz}^{(1)} + Q_{pz}^{(2)}$$

* Rank 3 tensor (a).

$$\begin{bmatrix} Q_{yzx} & Q_{yzy} & 0 \\ -Q_{yzy} & Q_{yzx} & 0 \\ 0 & 0 & Q_{xyz} \end{bmatrix}$$

$$Q_{yzx} = -G_{du}^{(2)} + G_s^{(1)}$$

$$Q_{yzy} = Q_{pz}^{(3)}$$

$$Q_{xyz} = 2G_{du}^{(2)} + G_s^{(1)}$$

* Rank 4 tensor (sss).

$$\begin{bmatrix} Q_{xxxx} & Q_{xxyy} & Q_{xxzz} & Q_{xxyz} & Q_{xxzx} & 0 \\ Q_{xxyy} & Q_{xxxx} & Q_{xxzz} & -Q_{xxyz} & -Q_{xxzx} & 0 \\ Q_{xxzz} & Q_{xxzz} & Q_{zzzz} & 0 & 0 & 0 \\ Q_{xxyz} & -Q_{xxyz} & 0 & Q_{yzyz} & 0 & -Q_{xxzx} \\ Q_{xxzx} & -Q_{xxzx} & 0 & 0 & Q_{yzyz} & Q_{xxyz} \\ 0 & 0 & 0 & -Q_{xxzx} & Q_{xxyz} & \frac{Q_{xxxx}}{2} - \frac{Q_{xxyy}}{2} \end{bmatrix}$$

$$Q_{xxxx} = -2Q_{du}^{(1)} - 4Q_{du}^{(2)} + 3Q_{g0}^{(1)} + Q_s^{(1)} + 2Q_s^{(2)}$$

$$Q_{xxyy} = -2Q_{du}^{(1)} + Q_{g0}^{(1)} + Q_s^{(1)}$$

$$Q_{xxzz} = Q_{du}^{(1)} - 4Q_{g0}^{(1)} + Q_s^{(1)}$$

$$Q_{xxyz} = Q_{gb}^{(1)}$$

$$Q_{xxzx} = Q_{ga}^{(1)}$$

$$Q_{zzzz} = 4Q_{du}^{(1)} + 8Q_{du}^{(2)} + 8Q_{g0}^{(1)} + Q_s^{(1)} + 2Q_s^{(2)}$$

$$Q_{yzyz} = Q_{du}^{(2)} - 4Q_{g0}^{(1)} + Q_s^{(2)}$$

* Rank 4 tensor (ssa).

$$\begin{bmatrix} 0 & 0 & Q_{xxzz} & Q_{xxyz} & Q_{xxzx} & Q_{xxyy} \\ 0 & 0 & Q_{xxzz} & -Q_{xxyz} & -Q_{xxzx} & -Q_{xxyy} \\ -Q_{xxzz} & -Q_{xxzz} & 0 & 0 & 0 & 0 \\ -Q_{xxyz} & Q_{xxyz} & 0 & 0 & Q_{yzzx} & Q_{xxzx} \\ -Q_{xxzx} & Q_{xxzx} & 0 & -Q_{yzzx} & 0 & -Q_{xxyz} \\ -Q_{xxyy} & Q_{xxyy} & 0 & -Q_{xxzx} & Q_{xxyz} & 0 \end{bmatrix}$$

$$Q_{xxzz} = 3Q_{du}^{(3)}$$

$$Q_{xxyz} = 2G_{f2}^{(1)}$$

$$Q_{xxzx} = -2G_{f1}^{(1)}$$

$$Q_{xxyy} = -2G_{faz}^{(1)} + 2G_{pz}^{(1)}$$

$$Q_{yzzx} = -4G_{faz}^{(1)} - G_{pz}^{(1)}$$

* Rank 4 tensor (aas).

$$\begin{bmatrix} Q_{yzyz} & 0 & 0 \\ 0 & Q_{yzyz} & 0 \\ 0 & 0 & Q_{xyxy} \end{bmatrix}$$

$$Q_{yzyz} = -2Q_{du}^{(4)} + Q_s^{(3)}$$

$$Q_{xyxy} = 4Q_{du}^{(4)} + Q_s^{(3)}$$

* Rank 4 tensor (aaa).

$$\begin{bmatrix} 0 & Q_{yzzx} & 0 \\ -Q_{yzzx} & 0 & 0 \\ 0 & 0 & 0 \end{bmatrix}$$

$$Q_{yzzx} = -G_{pz}^{(2)}$$

* Rank 4 tensor (sa).

$$\begin{bmatrix} Q_{xxyz} & Q_{xxzx} & Q_{xxyy} \\ -Q_{xxyz} & -Q_{xxzx} & Q_{xxyy} \\ 0 & 0 & Q_{zzxy} \\ Q_{yzyz} & Q_{yzzx} & 0 \\ Q_{yzzx} & -Q_{yzyz} & 0 \\ Q_{xxzx} & -Q_{xxyz} & 0 \end{bmatrix}$$

$$\begin{aligned}
Q_{xxyz} &= G_{f2}^{(2)} \\
Q_{xxzx} &= G_{f1}^{(2)} \\
Q_{xxxy} &= -G_{faz}^{(2)} + G_{pz}^{(3)} \\
Q_{zzxy} &= 2G_{faz}^{(2)} + G_{pz}^{(3)} + 2G_{pz}^{(4)} \\
Q_{yzyz} &= -3Q_{du}^{(5)} \\
Q_{yzzx} &= -G_{faz}^{(2)} + G_{pz}^{(4)}
\end{aligned}$$

* Rank 4 tensor (as).

$$\begin{bmatrix}
Q_{yzxx} & -Q_{yzxx} & 0 & Q_{yzyz} & Q_{yzzx} & Q_{yzxy} \\
Q_{yzxy} & -Q_{yzxy} & 0 & Q_{yzzx} & -Q_{yzyz} & -Q_{yzzx} \\
Q_{xyxx} & Q_{xyxx} & Q_{xyyz} & 0 & 0 & 0
\end{bmatrix}$$

$$\begin{aligned}
Q_{yzxx} &= G_{f2}^{(3)} \\
Q_{yzyz} &= -3Q_{du}^{(6)} \\
Q_{yzzx} &= -G_{faz}^{(3)} + G_{pz}^{(6)} \\
Q_{yzxy} &= G_{f1}^{(3)} \\
Q_{xyxx} &= -G_{faz}^{(3)} + G_{pz}^{(5)} \\
Q_{xyyz} &= 2G_{faz}^{(3)} + G_{pz}^{(5)} + 2G_{pz}^{(6)}
\end{aligned}$$

* Rank 4 tensor (s).

$$\begin{bmatrix}
Q_{xxxx} & Q_{xxyy} & Q_{xxzz} & Q_{xxyz} & Q_{xxzx} & Q_{xxxy} & Q_{xxzy} & Q_{xxxz} & Q_{xxyx} \\
Q_{xxyy} & Q_{xxxx} & Q_{xxzz} & -Q_{xxyz} & -Q_{xxzx} & -Q_{xxyx} & -Q_{xxzy} & -Q_{xxxz} & -Q_{xxyx} \\
Q_{zzxx} & Q_{zzxx} & Q_{zzzz} & 0 & 0 & Q_{zzxy} & 0 & 0 & -Q_{zzxy} \\
Q_{yzxx} & -Q_{yzxx} & 0 & Q_{yzyz} & Q_{yzzx} & Q_{yzyx} & Q_{yzyy} & Q_{yzzx} & Q_{yzyx} \\
-Q_{yzyx} & Q_{yzyx} & 0 & -Q_{yzzx} & Q_{yzyy} & Q_{yzzx} & -Q_{yzyx} & Q_{yzyx} & Q_{yzzx} \\
-\frac{Q_{xxxxy}}{2} - \frac{Q_{xxxxy}}{2} & \frac{Q_{xxxxy}}{2} + \frac{Q_{xxxxy}}{2} & 0 & -Q_{xxxz} & Q_{xxzy} & \frac{Q_{xxxz}}{2} - \frac{Q_{xxxxy}}{2} & -Q_{xxxz} & Q_{xxzy} & \frac{Q_{xxxz}}{2} - \frac{Q_{xxxxy}}{2}
\end{bmatrix}$$

$$\begin{aligned}
Q_{xxxx} &= -2Q_{du}^{(1)} - 4Q_{du}^{(2)} + 3Q_{g0}^{(1)} + Q_s^{(1)} + 2Q_s^{(2)} \\
Q_{xxyy} &= -2Q_{du}^{(1)} + Q_{g0}^{(1)} + Q_s^{(1)} \\
Q_{xxzz} &= Q_{du}^{(1)} + 3Q_{du}^{(3)} - 4Q_{g0}^{(1)} + Q_s^{(1)} \\
Q_{xxyz} &= 2G_{f2}^{(1)} + G_{f2}^{(2)} + Q_{gb}^{(1)} \\
Q_{xxzx} &= -2G_{f1}^{(1)} + G_{f1}^{(2)} + Q_{ga}^{(1)} \\
Q_{xxxy} &= -2G_{faz}^{(1)} - G_{faz}^{(2)} + 2G_{pz}^{(1)} + G_{pz}^{(3)} \\
Q_{xxzy} &= 2G_{f2}^{(1)} - G_{f2}^{(2)} + Q_{gb}^{(1)} \\
Q_{xxxz} &= -2G_{f1}^{(1)} - G_{f1}^{(2)} + Q_{ga}^{(1)} \\
Q_{xxyx} &= -2G_{faz}^{(1)} + G_{faz}^{(2)} + 2G_{pz}^{(1)} - G_{pz}^{(3)} \\
Q_{zzxx} &= Q_{du}^{(1)} - 3Q_{du}^{(3)} - 4Q_{g0}^{(1)} + Q_s^{(1)} \\
Q_{zzzz} &= 4Q_{du}^{(1)} + 8Q_{du}^{(2)} + 8Q_{g0}^{(1)} + Q_s^{(1)} + 2Q_s^{(2)} \\
Q_{zzxy} &= 2G_{faz}^{(2)} + G_{pz}^{(3)} + 2G_{pz}^{(4)} \\
Q_{yzxx} &= -2G_{f2}^{(1)} + Q_{gb}^{(1)} \\
Q_{yzyz} &= Q_{du}^{(2)} - 3Q_{du}^{(5)} - 4Q_{g0}^{(1)} + Q_s^{(2)} \\
Q_{yzzx} &= -4G_{faz}^{(1)} - G_{faz}^{(2)} - G_{pz}^{(1)} + G_{pz}^{(4)} \\
Q_{yzxy} &= -2G_{f1}^{(1)} - Q_{ga}^{(1)} \\
Q_{yzzy} &= Q_{du}^{(2)} + 3Q_{du}^{(5)} - 4Q_{g0}^{(1)} + Q_s^{(2)} \\
Q_{yzzx} &= -4G_{faz}^{(1)} + G_{faz}^{(2)} - G_{pz}^{(1)} - G_{pz}^{(4)}
\end{aligned}$$

* Rank 4 tensor (a).

$$\begin{bmatrix} Q_{yzxx} & -Q_{yzxx} & 0 & Q_{yzyz} & Q_{yzzx} & Q_{yzxy} & Q_{yzzz} & Q_{yzxz} & Q_{yzxy} \\ Q_{yzxy} & -Q_{yzxy} & 0 & Q_{yzxz} & -Q_{yzzz} & -Q_{yzxx} & Q_{yzzx} & -Q_{yzyz} & -Q_{yzzx} \\ Q_{xyxx} & Q_{xyxx} & Q_{xyzz} & 0 & 0 & Q_{xyxy} & 0 & 0 & -Q_{xyxy} \end{bmatrix}$$

$$\begin{aligned} Q_{yzxx} &= G_{f2}^{(3)} \\ Q_{yzyz} &= -2Q_{du}^{(4)} - 3Q_{du}^{(6)} + Q_s^{(3)} \\ Q_{yzzx} &= -G_{faz}^{(3)} - G_{pz}^{(2)} + G_{pz}^{(6)} \\ Q_{yzxy} &= G_{f1}^{(3)} \\ Q_{yzzz} &= 2Q_{du}^{(4)} - 3Q_{du}^{(6)} - Q_s^{(3)} \\ Q_{yzzx} &= -G_{faz}^{(3)} + G_{pz}^{(2)} + G_{pz}^{(6)} \\ Q_{xyxx} &= -G_{faz}^{(3)} + G_{pz}^{(5)} \\ Q_{xyzz} &= 2G_{faz}^{(3)} + G_{pz}^{(5)} + 2G_{pz}^{(6)} \\ Q_{xyxy} &= 4Q_{du}^{(4)} + Q_s^{(3)} \end{aligned}$$

* Rank 4 tensor (t).

$$\begin{bmatrix} Q_{xxxx} & 0 & Q_{xxxx} \\ 0 & Q_{xxxx} & Q_{yyyy} \\ 0 & 0 & Q_{zzzz} \\ -Q_{xxxx} & Q_{yyyy} & Q_{yyzz} \\ Q_{zzxx} & 0 & 0 \\ 0 & Q_{xyxy} & -Q_{yyyz} \\ 0 & Q_{yzzz} & 0 \\ Q_{xxzz} & -Q_{yyyz} & -\frac{Q_{xxxx}}{2} + \frac{3Q_{xyyy}}{2} + Q_{yyzz} - Q_{yzzz} + Q_{zzxx} \\ \frac{Q_{xxxx}}{2} - \frac{Q_{xyyy}}{2} & 0 & -Q_{xxzz} \\ -Q_{yyyz} & -Q_{xxzz} & 0 \end{bmatrix}$$

$$\begin{aligned} Q_{xxxx} &= -2Q_{du}^{(1)} - 4Q_{du}^{(2)} + 3Q_{g0}^{(1)} + 3Q_s^{(1)} \\ Q_{xxzz} &= Q_{ga}^{(1)} \\ Q_{yyyy} &= -Q_{gb}^{(1)} \\ Q_{zzzz} &= 4Q_{du}^{(1)} + 8Q_{du}^{(2)} + 8Q_{g0}^{(1)} + 3Q_s^{(1)} \\ Q_{yyzz} &= Q_{du}^{(1)} + 3Q_{du}^{(3)} - 4Q_{g0}^{(1)} + Q_s^{(1)} \\ Q_{zzxx} &= Q_{du}^{(1)} - 3Q_{du}^{(3)} - 4Q_{g0}^{(1)} + Q_s^{(1)} \\ Q_{xyyy} &= -2Q_{du}^{(1)} + Q_{g0}^{(1)} + Q_s^{(1)} \\ Q_{yzzz} &= Q_{du}^{(2)} + 3Q_{du}^{(5)} - 4Q_{g0}^{(1)} + Q_s^{(1)} \end{aligned}$$