

\* Harmonics for rank 0

$$\bar{Q}_0^{(2,2)}[q](A_1)$$

\*\* symmetry

$$1$$

\*\* expression

$$-\frac{\sqrt{5}Q_u(x^2+y^2-2z^2)}{10} + \frac{\sqrt{15}Q_v(x-y)(x+y)}{10} + \frac{\sqrt{15}Q_{xy}xy}{5} + \frac{\sqrt{15}Q_{xz}xz}{5} + \frac{\sqrt{15}Q_{yz}yz}{5}$$

\* Harmonics for rank 1

$$\bar{Q}_1^{(2,0)}[q](A_2)$$

\*\* symmetry

$$z$$

\*\* expression

$$\frac{\sqrt{10}Q_uz}{5} + \frac{\sqrt{30}Q_{xz}x}{10} + \frac{\sqrt{30}Q_{yz}y}{10}$$

$$\bar{Q}_1^{(2,2)}[q](A_2)$$

\*\* symmetry

$$z$$

\*\* expression

$$-\frac{3\sqrt{35}Q_uz(3x^2+3y^2-2z^2)}{70} + \frac{\sqrt{105}Q_vz(x-y)(x+y)}{14} + \frac{\sqrt{105}Q_{xy}xyz}{7} - \frac{\sqrt{105}Q_{xz}x(x^2+y^2-4z^2)}{35} - \frac{\sqrt{105}Q_{yz}y(x^2+y^2-4z^2)}{35}$$

$$\bar{Q}_{1,1}^{(2,0)}[q](E_1), \bar{Q}_{1,2}^{(2,0)}[q](E_1)$$

\*\* symmetry

$$x$$

$$y$$

\*\* expression

$$-\frac{\sqrt{10}Q_ux}{10} + \frac{\sqrt{30}Q_vx}{10} + \frac{\sqrt{30}Q_{xy}y}{10} + \frac{\sqrt{30}Q_{xz}z}{10}$$

$$-\frac{\sqrt{10}Q_uy}{10} - \frac{\sqrt{30}Q_vy}{10} + \frac{\sqrt{30}Q_{xy}x}{10} + \frac{\sqrt{30}Q_{yz}z}{10}$$

$$\bar{Q}_{1,1}^{(2,2)}[q](E_1), \bar{Q}_{1,2}^{(2,2)}[q](E_1)$$

\*\* symmetry

$$x$$

$$y$$

\*\* expression

$$-\frac{3\sqrt{35}Q_ux(x^2+y^2-4z^2)}{70} + \frac{\sqrt{105}Q_vx(3x^2-7y^2-2z^2)}{70} + \frac{\sqrt{105}Q_{xy}y(4x^2-y^2-z^2)}{35} + \frac{\sqrt{105}Q_{xz}z(4x^2-y^2-z^2)}{35} + \frac{\sqrt{105}Q_{yz}xyz}{7}$$

$$-\frac{3\sqrt{35}Q_uy(x^2+y^2-4z^2)}{70} + \frac{\sqrt{105}Q_vy(7x^2-3y^2+2z^2)}{70} - \frac{\sqrt{105}Q_{xy}x(x^2-4y^2+z^2)}{35} + \frac{\sqrt{105}Q_{xz}xyz}{7} - \frac{\sqrt{105}Q_{yz}z(x^2-4y^2+z^2)}{35}$$

\* Harmonics for rank 2

$$\bar{Q}_2^{(2,-2)}[q](A_1)$$

\*\* symmetry

$$-\frac{x^2}{2} - \frac{y^2}{2} + z^2$$

\*\* expression

$$Q_u$$

$$\bar{Q}_2^{(2,0)}[q](A_1)$$

\*\* symmetry

$$-\frac{x^2}{2} - \frac{y^2}{2} + z^2$$

\*\* expression

$$-\frac{\sqrt{14}Q_u(x^2+y^2-2z^2)}{14}-\frac{\sqrt{42}Q_v(x-y)(x+y)}{14}-\frac{\sqrt{42}Q_{xy}xy}{7}+\frac{\sqrt{42}Q_{xz}xz}{14}+\frac{\sqrt{42}Q_{yz}yz}{14}$$

$$\tilde{Q}_2^{(2,2)}[q](A_1)$$

\*\* symmetry

$$-\frac{x^2}{2}-\frac{y^2}{2}+z^2$$

\*\* expression

$$\frac{\sqrt{14}Q_u(3x^4+6x^2y^2-24x^2z^2+3y^4-24y^2z^2+8z^4)}{56}-\frac{5\sqrt{42}Q_v(x-y)(x+y)(x^2+y^2-6z^2)}{168}-\frac{5\sqrt{42}Q_{xy}xy(x^2+y^2-6z^2)}{84}-\frac{5\sqrt{42}Q_{xz}xz(3x^2+3y^2-4z^2)}{84}-\frac{5\sqrt{42}Q_{yz}yz(3x^2+3y^2-4z^2)}{84}$$

$$\tilde{Q}_{2,1}^{(2,-2)}[q](E_1), \tilde{Q}_{2,2}^{(2,-2)}[q](E_1)$$

\*\* symmetry

$$\sqrt{3}yz$$

$$-\sqrt{3}xz$$

\*\* expression

$$Q_{yz}$$

$$-Q_{xz}$$

$$\tilde{Q}_{2,1}^{(2,0)}[q](E_1), \tilde{Q}_{2,2}^{(2,0)}[q](E_1)$$

\*\* symmetry

$$\sqrt{3}yz$$

$$-\sqrt{3}xz$$

\*\* expression

$$\frac{\sqrt{42}Q_u yz}{14}-\frac{3\sqrt{14}Q_v yz}{14}+\frac{3\sqrt{14}Q_{xy}xz}{14}+\frac{3\sqrt{14}Q_{xz}xy}{14}-\frac{\sqrt{14}Q_{yz}(2x^2-y^2-z^2)}{14}$$

$$-\frac{\sqrt{42}Q_u xz}{14}-\frac{3\sqrt{14}Q_v xz}{14}-\frac{3\sqrt{14}Q_{xy}yz}{14}-\frac{\sqrt{14}Q_{xz}(x^2-2y^2+z^2)}{14}-\frac{3\sqrt{14}Q_{yz}xy}{14}$$

$$\tilde{Q}_{2,1}^{(2,2)}[q](E_1), \tilde{Q}_{2,2}^{(2,2)}[q](E_1)$$

\*\* symmetry

$$\sqrt{3}yz$$

$$-\sqrt{3}xz$$

\*\* expression

$$-\frac{5\sqrt{42}Q_u yz(3x^2+3y^2-4z^2)}{84}+\frac{5\sqrt{14}Q_v yz(9x^2-5y^2+2z^2)}{84}-\frac{5\sqrt{14}Q_{xy}xz(x^2-6y^2+z^2)}{42}$$

$$-\frac{5\sqrt{14}Q_{xz}xy(x^2+y^2-6z^2)}{42}+\frac{\sqrt{14}Q_{yz}(x^4-3x^2y^2-3x^2z^2-4y^4+27y^2z^2-4z^4)}{42}$$

$$\frac{5\sqrt{42}Q_u xz(3x^2+3y^2-4z^2)}{84}-\frac{5\sqrt{14}Q_v xz(5x^2-9y^2-2z^2)}{84}-\frac{5\sqrt{14}Q_{xy}yz(6x^2-y^2-z^2)}{42}$$

$$+\frac{\sqrt{14}Q_{xz}(4x^4+3x^2y^2-27x^2z^2-y^4+3y^2z^2+4z^4)}{42}+\frac{5\sqrt{14}Q_{yz}xy(x^2+y^2-6z^2)}{42}$$

$$\tilde{Q}_{2,1}^{(2,-2)}[q](E_2), \tilde{Q}_{2,2}^{(2,-2)}[q](E_2)$$

\*\* symmetry

$$\frac{\sqrt{3}(x-y)(x+y)}{2}$$

$$-\sqrt{3}xy$$

\*\* expression

$$Q_v$$

$$-Q_{xy}$$

$$\tilde{Q}_{2,1}^{(2,0)}[q](E_2), \tilde{Q}_{2,2}^{(2,0)}[q](E_2)$$

\*\* symmetry

$$\frac{\sqrt{3}(x-y)(x+y)}{2}$$

$$-\sqrt{3}xy$$

\*\* expression

$$-\frac{\sqrt{42}Q_u(x-y)(x+y)}{14} + \frac{\sqrt{14}Q_v(x^2+y^2-2z^2)}{14} + \frac{3\sqrt{14}Q_{xz}xz}{14} - \frac{3\sqrt{14}Q_{yz}yz}{14}$$

$$\frac{\sqrt{42}Q_u xy}{7} - \frac{\sqrt{14}Q_{xy}(x^2+y^2-2z^2)}{14} - \frac{3\sqrt{14}Q_{xz}yz}{14} - \frac{3\sqrt{14}Q_{yz}xz}{14}$$

$$\tilde{Q}_{2,1}^{(2,2)}[q](E_2), \tilde{Q}_{2,2}^{(2,2)}[q](E_2)$$

\*\* symmetry

$$\frac{\sqrt{3}(x-y)(x+y)}{2}$$

$$-\sqrt{3}xy$$

\*\* expression

$$-\frac{5\sqrt{42}Q_u(x-y)(x+y)(x^2+y^2-6z^2)}{168} + \frac{\sqrt{14}Q_v(19x^4-102x^2y^2-12x^2z^2+19y^4-12y^2z^2+4z^4)}{168}$$

$$+ \frac{5\sqrt{14}Q_{xy}xy(x-y)(x+y)}{12} + \frac{5\sqrt{14}Q_{xz}xz(5x^2-9y^2-2z^2)}{84} + \frac{5\sqrt{14}Q_{yz}yz(9x^2-5y^2+2z^2)}{84}$$

$$\frac{5\sqrt{42}Q_u xy(x^2+y^2-6z^2)}{84} - \frac{5\sqrt{14}Q_v xy(x-y)(x+y)}{12} + \frac{\sqrt{14}Q_{xy}(4x^4-27x^2y^2+3x^2z^2+4y^4+3y^2z^2-z^4)}{42}$$

$$- \frac{5\sqrt{14}Q_{xz}yz(6x^2-y^2-z^2)}{42} + \frac{5\sqrt{14}Q_{yz}xz(x^2-6y^2+z^2)}{42}$$

\* Harmonics for rank 3

$$\tilde{Q}_3^{(2,-2)}[q](A_2)$$

\*\* symmetry

$$-\frac{z(3x^2+3y^2-2z^2)}{2}$$

\*\* expression

$$\frac{\sqrt{15}Q_u z}{5} - \frac{\sqrt{5}Q_{xz}x}{5} - \frac{\sqrt{5}Q_{yz}y}{5}$$

$$\tilde{Q}_3^{(2,0)}[q](A_2)$$

\*\* symmetry

$$-\frac{z(3x^2+3y^2-2z^2)}{2}$$

\*\* expression

$$-\frac{\sqrt{15}Q_u z(3x^2+3y^2-2z^2)}{15} - \frac{\sqrt{5}Q_v z(x-y)(x+y)}{2} - \sqrt{5}Q_{xy}xyz - \frac{\sqrt{5}Q_{xz}x(x^2+y^2-4z^2)}{20} - \frac{\sqrt{5}Q_{yz}y(x^2+y^2-4z^2)}{20}$$

$$\tilde{Q}_3^{(2,2)}[q](A_2)$$

\*\* symmetry

$$-\frac{z(3x^2+3y^2-2z^2)}{2}$$

\*\* expression

$$\frac{\sqrt{330}Q_u z(15x^4+30x^2y^2-40x^2z^2+15y^4-40y^2z^2+8z^4)}{264} - \frac{7\sqrt{110}Q_v z(x-y)(x+y)(x^2+y^2-2z^2)}{88} - \frac{7\sqrt{110}Q_{xy}xyz(x^2+y^2-2z^2)}{44}$$

$$+ \frac{\sqrt{110}Q_{xz}x(x^4+2x^2y^2-12x^2z^2+y^4-12y^2z^2+8z^4)}{44} + \frac{\sqrt{110}Q_{yz}y(x^4+2x^2y^2-12x^2z^2+y^4-12y^2z^2+8z^4)}{44}$$

$$\bar{Q}_3^{(2,-2)}[q](B_1)$$

\*\* symmetry

$$\frac{\sqrt{10}y(3x^2 - y^2)}{4}$$

\*\* expression

$$\frac{\sqrt{2}Q_v y}{2} + \frac{\sqrt{2}Q_{xy} x}{2}$$

$$\bar{Q}_3^{(2,0)}[q](B_1)$$

\*\* symmetry

$$\frac{\sqrt{10}y(3x^2 - y^2)}{4}$$

\*\* expression

$$-\frac{5\sqrt{6}Q_u y(3x^2 - y^2)}{24} + \frac{\sqrt{2}Q_v y(x^2 + y^2 - 4z^2)}{8} + \frac{\sqrt{2}Q_{xy} x(x^2 + y^2 - 4z^2)}{8} + \frac{5\sqrt{2}Q_{xz}xyz}{4} + \frac{5\sqrt{2}Q_{yz}z(x - y)(x + y)}{8}$$

$$\bar{Q}_3^{(2,2)}[q](B_1)$$

\*\* symmetry

$$\frac{\sqrt{10}y(3x^2 - y^2)}{4}$$

\*\* expression

$$-\frac{7\sqrt{33}Q_u y(3x^2 - y^2)(x^2 + y^2 - 8z^2)}{264} + \frac{\sqrt{11}Q_v y(53x^4 - 104x^2y^2 - 6x^2z^2 + 11y^4 - 6y^2z^2 + 4z^4)}{88} \\ - \frac{\sqrt{11}Q_{xy} x(5x^4 - 53x^2y^2 + 3x^2z^2 + 26y^4 + 3y^2z^2 - 2z^4)}{44} + \frac{7\sqrt{11}Q_{xz}xyz(7x^2 - 5y^2 - 2z^2)}{44} - \frac{7\sqrt{11}Q_{yz}z(x^4 - 9x^2y^2 + x^2z^2 + 2y^4 - y^2z^2)}{44}$$

$$\bar{Q}_3^{(2,-2)}[q](B_2)$$

\*\* symmetry

$$\frac{\sqrt{10}x(x^2 - 3y^2)}{4}$$

\*\* expression

$$\frac{\sqrt{2}Q_v x}{2} - \frac{\sqrt{2}Q_{xy} y}{2}$$

$$\bar{Q}_3^{(2,0)}[q](B_2)$$

\*\* symmetry

$$\frac{\sqrt{10}x(x^2 - 3y^2)}{4}$$

\*\* expression

$$-\frac{5\sqrt{6}Q_u x(x^2 - 3y^2)}{24} + \frac{\sqrt{2}Q_v x(x^2 + y^2 - 4z^2)}{8} - \frac{\sqrt{2}Q_{xy} y(x^2 + y^2 - 4z^2)}{8} + \frac{5\sqrt{2}Q_{xz}z(x - y)(x + y)}{8} - \frac{5\sqrt{2}Q_{yz}xyz}{4}$$

$$\bar{Q}_3^{(2,2)}[q](B_2)$$

\*\* symmetry

$$\frac{\sqrt{10}x(x^2 - 3y^2)}{4}$$

\*\* expression

$$-\frac{7\sqrt{33}Q_u x(x^2 - 3y^2)(x^2 + y^2 - 8z^2)}{264} + \frac{\sqrt{11}Q_v x(11x^4 - 104x^2y^2 - 6x^2z^2 + 53y^4 - 6y^2z^2 + 4z^4)}{88} \\ + \frac{\sqrt{11}Q_{xy} y(26x^4 - 53x^2y^2 + 3x^2z^2 + 5y^4 + 3y^2z^2 - 2z^4)}{44} + \frac{7\sqrt{11}Q_{xz}z(2x^4 - 9x^2y^2 - x^2z^2 + y^4 + y^2z^2)}{44} + \frac{7\sqrt{11}Q_{yz}xyz(5x^2 - 7y^2 + 2z^2)}{44}$$

$$\bar{Q}_{3,1}^{(2,-2)}[q](E_1), \bar{Q}_{3,2}^{(2,-2)}[q](E_1)$$

\*\* symmetry

$$-\frac{\sqrt{6}x(x^2 + y^2 - 4z^2)}{4}$$

$$-\frac{\sqrt{6}y(x^2 + y^2 - 4z^2)}{4}$$

\*\* expression

$$\frac{\sqrt{10}Q_{ux}}{5} - \frac{\sqrt{30}Q_{vx}}{30} - \frac{\sqrt{30}Q_{xyy}}{30} + \frac{2\sqrt{30}Q_{xz}z}{15}$$

$$\frac{\sqrt{10}Q_{uy}}{5} + \frac{\sqrt{30}Q_{vy}}{30} - \frac{\sqrt{30}Q_{xyx}}{30} + \frac{2\sqrt{30}Q_{yz}z}{15}$$

$$\vec{Q}_{3,1}^{(2,0)}[q](E_1), \vec{Q}_{3,2}^{(2,0)}[q](E_1)$$

\*\* symmetry

$$-\frac{\sqrt{6}x(x^2+y^2-4z^2)}{4}$$

$$-\frac{\sqrt{6}y(x^2+y^2-4z^2)}{4}$$

\*\* expression

$$-\frac{3\sqrt{10}Q_{ux}(x^2+y^2-4z^2)}{40} - \frac{\sqrt{30}Q_{vx}(11x^2-9y^2-24z^2)}{120} - \frac{\sqrt{30}Q_{xyy}(21x^2+y^2-24z^2)}{120} + \frac{\sqrt{30}Q_{xz}z(9x^2-21y^2+4z^2)}{120} + \frac{\sqrt{30}Q_{yz}xyz}{4}$$

$$-\frac{3\sqrt{10}Q_{uy}(x^2+y^2-4z^2)}{40} - \frac{\sqrt{30}Q_{vy}(9x^2-11y^2+24z^2)}{120} - \frac{\sqrt{30}Q_{xyx}(x^2+21y^2-24z^2)}{120} + \frac{\sqrt{30}Q_{xz}xyz}{4} - \frac{\sqrt{30}Q_{yz}z(21x^2-9y^2-4z^2)}{120}$$

$$\vec{Q}_{3,1}^{(2,2)}[q](E_1), \vec{Q}_{3,2}^{(2,2)}[q](E_1)$$

\*\* symmetry

$$-\frac{\sqrt{6}x(x^2+y^2-4z^2)}{4}$$

$$-\frac{\sqrt{6}y(x^2+y^2-4z^2)}{4}$$

\*\* expression

$$\frac{3\sqrt{55}Q_{ux}(x^4+2x^2y^2-12x^2z^2+y^4-12y^2z^2+8z^4)}{88} - \frac{\sqrt{165}Q_{vx}(5x^4-4x^2y^2-46x^2z^2-9y^4+66y^2z^2+12z^4)}{264}$$

$$-\frac{\sqrt{165}Q_{xyy}(6x^4+5x^2y^2-51x^2z^2-y^4+5y^2z^2+6z^4)}{132}$$

$$-\frac{\sqrt{165}Q_{xzz}(18x^4+15x^2y^2-41x^2z^2-3y^4+y^2z^2+4z^4)}{132} - \frac{7\sqrt{165}Q_{yz}xyz(x^2+y^2-2z^2)}{44}$$

$$\frac{3\sqrt{55}Q_{uy}(x^4+2x^2y^2-12x^2z^2+y^4-12y^2z^2+8z^4)}{88} - \frac{\sqrt{165}Q_{vy}(9x^4+4x^2y^2-66x^2z^2-5y^4+46y^2z^2-12z^4)}{264}$$

$$+\frac{\sqrt{165}Q_{xyx}(x^4-5x^2y^2-5x^2z^2-6y^4+51y^2z^2-6z^4)}{132} - \frac{7\sqrt{165}Q_{xzx}xyz(x^2+y^2-2z^2)}{44}$$

$$+\frac{\sqrt{165}Q_{yzz}(3x^4-15x^2y^2-x^2z^2-18y^4+41y^2z^2-4z^4)}{132}$$

$$\vec{Q}_{3,1}^{(2,-2)}[q](E_2), \vec{Q}_{3,2}^{(2,-2)}[q](E_2)$$

\*\* symmetry

$$\sqrt{15}xyz$$

$$\frac{\sqrt{15}z(x-y)(x+y)}{2}$$

\*\* expression

$$\frac{\sqrt{3}Q_{xyz}}{3} + \frac{\sqrt{3}Q_{xzy}}{3} + \frac{\sqrt{3}Q_{yzx}}{3}$$

$$\frac{\sqrt{3}Q_{vz}}{3} + \frac{\sqrt{3}Q_{xzx}}{3} - \frac{\sqrt{3}Q_{yzy}}{3}$$

$$\vec{Q}_{3,1}^{(2,0)}[q](E_2), \vec{Q}_{3,2}^{(2,0)}[q](E_2)$$

\*\* symmetry

$$\sqrt{15}xyz$$

$$\frac{\sqrt{15}z(x-y)(x+y)}{2}$$

\*\* expression

$$\frac{\sqrt{3}Q_{xy}z(3x^2+3y^2-2z^2)}{6} + \frac{\sqrt{3}Q_{xz}y(3x^2-2y^2+3z^2)}{6} - \frac{\sqrt{3}Q_{yz}x(2x^2-3y^2-3z^2)}{6}$$

$$\frac{\sqrt{3}Q_vz(3x^2+3y^2-2z^2)}{6} + \frac{\sqrt{3}Q_{xz}y(x^2-9y^2+6z^2)}{12} + \frac{\sqrt{3}Q_{yz}y(9x^2-y^2-6z^2)}{12}$$

$$\tilde{\mathbb{Q}}_{3,1}^{(2,2)}[q](E_2), \tilde{\mathbb{Q}}_{3,2}^{(2,2)}[q](E_2)$$

\*\* symmetry

$$\sqrt{15}xyz$$

$$\frac{\sqrt{15}z(x-y)(x+y)}{2}$$

\*\* expression

$$-\frac{21\sqrt{22}Q_uxyz(x^2+y^2-2z^2)}{44} + \frac{21\sqrt{66}Q_vxyz(x-y)(x+y)}{44} - \frac{\sqrt{66}Q_{xy}z(6x^4-51x^2y^2+5x^2z^2+6y^4+5y^2z^2-z^4)}{66}$$

$$-\frac{\sqrt{66}Q_{xz}y(6x^4+5x^2y^2-51x^2z^2-y^4+5y^2z^2+6z^4)}{66} + \frac{\sqrt{66}Q_{yz}x(x^4-5x^2y^2-5x^2z^2-6y^4+51y^2z^2-6z^4)}{66}$$

$$-\frac{21\sqrt{22}Q_uz(x-y)(x+y)(x^2+y^2-2z^2)}{88} + \frac{\sqrt{66}Q_vz(39x^4-174x^2y^2-20x^2z^2+39y^4-20y^2z^2+4z^4)}{264} + \frac{21\sqrt{66}Q_{xy}xyz(x-y)(x+y)}{44}$$

$$-\frac{\sqrt{66}Q_{xz}x(5x^4-4x^2y^2-46x^2z^2-9y^4+66y^2z^2+12z^4)}{132} - \frac{\sqrt{66}Q_{yz}y(9x^4+4x^2y^2-66x^2z^2-5y^4+46y^2z^2-12z^4)}{132}$$

\* Harmonics for rank 4

$$\tilde{\mathbb{Q}}_4^{(2,-2)}[q](A_1)$$

\*\* symmetry

$$\frac{3x^4}{8} + \frac{3x^2y^2}{4} - 3x^2z^2 + \frac{3y^4}{8} - 3y^2z^2 + z^4$$

\*\* expression

$$-\frac{3\sqrt{70}Q_u(x^2+y^2-2z^2)}{70} + \frac{\sqrt{210}Q_v(x-y)(x+y)}{140} + \frac{\sqrt{210}Q_{xy}xy}{70} - \frac{2\sqrt{210}Q_{xz}xz}{35} - \frac{2\sqrt{210}Q_{yz}yz}{35}$$

$$\tilde{\mathbb{Q}}_4^{(2,0)}[q](A_1)$$

\*\* symmetry

$$\frac{3x^4}{8} + \frac{3x^2y^2}{4} - 3x^2z^2 + \frac{3y^4}{8} - 3y^2z^2 + z^4$$

\*\* expression

$$\frac{\sqrt{385}Q_u(3x^4+6x^2y^2-24x^2z^2+3y^4-24y^2z^2+8z^4)}{308} + \frac{3\sqrt{1155}Q_v(x-y)(x+y)(x^2+y^2-6z^2)}{308}$$

$$+ \frac{3\sqrt{1155}Q_{xy}xy(x^2+y^2-6z^2)}{154} - \frac{\sqrt{1155}Q_{xz}xz(3x^2+3y^2-4z^2)}{308} - \frac{\sqrt{1155}Q_{yz}yz(3x^2+3y^2-4z^2)}{308}$$

$$\tilde{\mathbb{Q}}_4^{(2,2)}[q](A_1)$$

\*\* symmetry

$$\frac{3x^4}{8} + \frac{3x^2y^2}{4} - 3x^2z^2 + \frac{3y^4}{8} - 3y^2z^2 + z^4$$

\*\* expression

$$-\frac{3\sqrt{715}Q_u(5x^6+15x^4y^2-90x^4z^2+15x^2y^4-180x^2y^2z^2+120x^2z^4+5y^6-90y^4z^2+120y^2z^4-16z^6)}{2288}$$

$$+ \frac{7\sqrt{2145}Q_v(x-y)(x+y)(x^4+2x^2y^2-16x^2z^2+y^4-16y^2z^2+16z^4)}{2288} + \frac{7\sqrt{2145}Q_{xy}xy(x^4+2x^2y^2-16x^2z^2+y^4-16y^2z^2+16z^4)}{1144}$$

$$+ \frac{7\sqrt{2145}Q_{xz}xz(5x^4+10x^2y^2-20x^2z^2+5y^4-20y^2z^2+8z^4)}{1144} + \frac{7\sqrt{2145}Q_{yz}yz(5x^4+10x^2y^2-20x^2z^2+5y^4-20y^2z^2+8z^4)}{1144}$$

$$\tilde{\mathbb{Q}}_4^{(2,-2)}[q](B_1)$$

\*\* symmetry

$$\frac{\sqrt{70}xz(x^2-3y^2)}{4}$$

\*\* expression

$$\frac{\sqrt{3}Q_vxz}{2} - \frac{\sqrt{3}Q_{xy}yz}{2} + \frac{\sqrt{3}Q_{xz}(x-y)(x+y)}{4} - \frac{\sqrt{3}Q_{yz}xy}{2}$$

$$\tilde{Q}_4^{(2,0)}[q](B_1)$$

\*\* symmetry

$$\frac{\sqrt{70}xz(x^2 - 3y^2)}{4}$$

\*\* expression

$$\begin{aligned} & -\frac{7\sqrt{22}Q_{uxz}(x^2 - 3y^2)}{88} + \frac{3\sqrt{66}Q_vxz(3x^2 + 3y^2 - 4z^2)}{88} - \frac{3\sqrt{66}Q_{xy}yz(3x^2 + 3y^2 - 4z^2)}{88} \\ & + \frac{\sqrt{66}Q_{xz}(x^4 - 21x^2y^2 + 15x^2z^2 + 6y^4 - 15y^2z^2)}{88} + \frac{\sqrt{66}Q_{yz}xy(19x^2 - 9y^2 - 30z^2)}{88} \end{aligned}$$

$$\tilde{Q}_4^{(2,2)}[q](B_1)$$

\*\* symmetry

$$\frac{\sqrt{70}xz(x^2 - 3y^2)}{4}$$

\*\* expression

$$\begin{aligned} & -\frac{9\sqrt{2002}Q_{uxz}(x^2 - 3y^2)(3x^2 + 3y^2 - 8z^2)}{1144} + \frac{\sqrt{6006}Q_vxz(19x^4 - 160x^2y^2 - 10x^2z^2 + 85y^4 - 10y^2z^2 + 4z^4)}{1144} \\ & + \frac{\sqrt{6006}Q_{xy}yz(40x^4 - 85x^2y^2 + 5x^2z^2 + 7y^4 + 5y^2z^2 - 2z^4)}{572} \\ & - \frac{\sqrt{6006}Q_{xz}(2x^6 - 7x^4y^2 - 23x^4z^2 - 8x^2y^4 + 90x^2y^2z^2 + 8x^2z^4 + y^6 - 7y^4z^2 - 8y^2z^4)}{572} \\ & - \frac{\sqrt{6006}Q_{yz}xy(5x^4 - 2x^2y^2 - 44x^2z^2 - 7y^4 + 76y^2z^2 - 16z^4)}{572} \end{aligned}$$

$$\tilde{Q}_4^{(2,-2)}[q](B_2)$$

\*\* symmetry

$$\frac{\sqrt{70}yz(3x^2 - y^2)}{4}$$

\*\* expression

$$\frac{\sqrt{3}Q_vyz}{2} + \frac{\sqrt{3}Q_{xy}xz}{2} + \frac{\sqrt{3}Q_{xz}xy}{2} + \frac{\sqrt{3}Q_{yz}(x - y)(x + y)}{4}$$

$$\tilde{Q}_4^{(2,0)}[q](B_2)$$

\*\* symmetry

$$\frac{\sqrt{70}yz(3x^2 - y^2)}{4}$$

\*\* expression

$$\begin{aligned} & -\frac{7\sqrt{22}Q_{uyz}(3x^2 - y^2)}{88} + \frac{3\sqrt{66}Q_vyz(3x^2 + 3y^2 - 4z^2)}{88} + \frac{3\sqrt{66}Q_{xy}xz(3x^2 + 3y^2 - 4z^2)}{88} \\ & + \frac{\sqrt{66}Q_{xz}xy(9x^2 - 19y^2 + 30z^2)}{88} - \frac{\sqrt{66}Q_{yz}(6x^4 - 21x^2y^2 - 15x^2z^2 + y^4 + 15y^2z^2)}{88} \end{aligned}$$

$$\tilde{Q}_4^{(2,2)}[q](B_2)$$

\*\* symmetry

$$\frac{\sqrt{70}yz(3x^2 - y^2)}{4}$$

\*\* expression

$$\begin{aligned} & -\frac{9\sqrt{2002}Q_{uyz}(3x^2 - y^2)(3x^2 + 3y^2 - 8z^2)}{1144} + \frac{\sqrt{6006}Q_vyz(85x^4 - 160x^2y^2 - 10x^2z^2 + 19y^4 - 10y^2z^2 + 4z^4)}{1144} \\ & - \frac{\sqrt{6006}Q_{xy}xz(7x^4 - 85x^2y^2 + 5x^2z^2 + 40y^4 + 5y^2z^2 - 2z^4)}{572} - \frac{\sqrt{6006}Q_{xz}xy(7x^4 + 2x^2y^2 - 76x^2z^2 - 5y^4 + 44y^2z^2 + 16z^4)}{572} \\ & + \frac{\sqrt{6006}Q_{yz}(x^6 - 8x^4y^2 - 7x^4z^2 - 7x^2y^4 + 90x^2y^2z^2 - 8x^2z^4 + 2y^6 - 23y^4z^2 + 8y^2z^4)}{572} \end{aligned}$$

$$\tilde{Q}_{4,1}^{(2,-2)}[q](E_1), \tilde{Q}_{4,2}^{(2,-2)}[q](E_1)$$

\*\* symmetry

$$-\frac{\sqrt{10}yz(3x^2 + 3y^2 - 4z^2)}{4}$$

$$\frac{\sqrt{10}xz(3x^2 + 3y^2 - 4z^2)}{4}$$

\*\* expression

$$\begin{aligned} & \frac{3\sqrt{7}Q_u yz}{7} + \frac{\sqrt{21}Q_v yz}{14} - \frac{\sqrt{21}Q_{xy}xz}{14} - \frac{\sqrt{21}Q_{xz}xy}{14} - \frac{\sqrt{21}Q_{yz}(x^2 + 3y^2 - 4z^2)}{28} \\ & - \frac{3\sqrt{7}Q_u xz}{7} + \frac{\sqrt{21}Q_v xz}{14} + \frac{\sqrt{21}Q_{xy}yz}{14} + \frac{\sqrt{21}Q_{xz}(3x^2 + y^2 - 4z^2)}{28} + \frac{\sqrt{21}Q_{yz}xy}{14} \end{aligned}$$

$$\tilde{\mathbb{Q}}_{4,1}^{(2,0)}[q](E_1), \tilde{\mathbb{Q}}_{4,2}^{(2,0)}[q](E_1)$$

\*\* symmetry

$$\begin{aligned} & - \frac{\sqrt{10}yz(3x^2 + 3y^2 - 4z^2)}{4} \\ & \frac{\sqrt{10}xz(3x^2 + 3y^2 - 4z^2)}{4} \end{aligned}$$

\*\* expression

$$\begin{aligned} & - \frac{17\sqrt{154}Q_u yz(3x^2 + 3y^2 - 4z^2)}{616} - \frac{\sqrt{462}Q_v yz(33x^2 - 51y^2 + 40z^2)}{616} - \frac{\sqrt{462}Q_{xy}xz(9x^2 + 93y^2 - 40z^2)}{616} \\ & - \frac{9\sqrt{462}Q_{xz}xy(x^2 + y^2 - 6z^2)}{616} + \frac{\sqrt{462}Q_{yz}(6x^4 + 3x^2y^2 - 39x^2z^2 - 3y^4 + 15y^2z^2 + 4z^4)}{616} \\ & \frac{17\sqrt{154}Q_u xz(3x^2 + 3y^2 - 4z^2)}{616} + \frac{\sqrt{462}Q_v xz(51x^2 - 33y^2 - 40z^2)}{616} + \frac{\sqrt{462}Q_{xy}yz(93x^2 + 9y^2 - 40z^2)}{616} \\ & + \frac{\sqrt{462}Q_{xz}(3x^4 - 3x^2y^2 - 15x^2z^2 - 6y^4 + 39y^2z^2 - 4z^4)}{616} + \frac{9\sqrt{462}Q_{yz}xy(x^2 + y^2 - 6z^2)}{616} \end{aligned}$$

$$\tilde{\mathbb{Q}}_{4,1}^{(2,2)}[q](E_1), \tilde{\mathbb{Q}}_{4,2}^{(2,2)}[q](E_1)$$

\*\* symmetry

$$\begin{aligned} & - \frac{\sqrt{10}yz(3x^2 + 3y^2 - 4z^2)}{4} \\ & \frac{\sqrt{10}xz(3x^2 + 3y^2 - 4z^2)}{4} \end{aligned}$$

\*\* expression

$$\begin{aligned} & \frac{21\sqrt{286}Q_u yz(5x^4 + 10x^2y^2 - 20x^2z^2 + 5y^4 - 20y^2z^2 + 8z^4)}{1144} - \frac{7\sqrt{858}Q_v yz(11x^4 + 4x^2y^2 - 26x^2z^2 - 7y^4 + 22y^2z^2 - 4z^4)}{1144} \\ & + \frac{7\sqrt{858}Q_{xy}xz(x^4 - 7x^2y^2 - x^2z^2 - 8y^4 + 23y^2z^2 - 2z^4)}{572} + \frac{7\sqrt{858}Q_{xz}xy(x^4 + 2x^2y^2 - 16x^2z^2 + y^4 - 16y^2z^2 + 16z^4)}{572} \\ & - \frac{\sqrt{858}Q_{yz}(x^6 - 4x^4y^2 - 11x^4z^2 - 11x^2y^4 + 90x^2y^2z^2 - 4x^2z^4 - 6y^6 + 101y^4z^2 - 116y^2z^4 + 8z^6)}{572} \\ & - \frac{21\sqrt{286}Q_u xz(5x^4 + 10x^2y^2 - 20x^2z^2 + 5y^4 - 20y^2z^2 + 8z^4)}{1144} \\ & + \frac{7\sqrt{858}Q_v xz(7x^4 - 4x^2y^2 - 22x^2z^2 - 11y^4 + 26y^2z^2 + 4z^4)}{1144} + \frac{7\sqrt{858}Q_{xy}yz(8x^4 + 7x^2y^2 - 23x^2z^2 - y^4 + y^2z^2 + 2z^4)}{572} \\ & - \frac{\sqrt{858}Q_{xz}(6x^6 + 11x^4y^2 - 101x^4z^2 + 4x^2y^4 - 90x^2y^2z^2 + 116x^2z^4 - y^6 + 11y^4z^2 + 4y^2z^4 - 8z^6)}{572} \\ & - \frac{7\sqrt{858}Q_{yz}xy(x^4 + 2x^2y^2 - 16x^2z^2 + y^4 - 16y^2z^2 + 16z^4)}{572} \end{aligned}$$

$$\tilde{\mathbb{Q}}_{4,1}^{(2,-2)}[q](E_2, 1), \tilde{\mathbb{Q}}_{4,2}^{(2,-2)}[q](E_2, 1)$$

\*\* symmetry

$$\begin{aligned} & \frac{\sqrt{35}(x^2 - 2xy - y^2)(x^2 + 2xy - y^2)}{8} \\ & \frac{\sqrt{35}xy(x - y)(x + y)}{2} \end{aligned}$$

\*\* expression

$$\begin{aligned} & \frac{\sqrt{6}Q_v(x - y)(x + y)}{4} - \frac{\sqrt{6}Q_{xy}xy}{2} \\ & \frac{\sqrt{6}Q_vxy}{2} + \frac{\sqrt{6}Q_{xy}(x - y)(x + y)}{4} \end{aligned}$$

$$\tilde{\mathbb{Q}}_{4,1}^{(2,-2)}[q](E_2, 2), \tilde{\mathbb{Q}}_{4,2}^{(2,-2)}[q](E_2, 2)$$



\*\* symmetry

$$-\frac{\sqrt{5}(x-y)(x+y)(x^2+y^2-6z^2)}{4}$$

$$\frac{\sqrt{5}xy(x^2+y^2-6z^2)}{2}$$

\*\* expression

$$\begin{aligned} & \frac{3\sqrt{14}Q_u(x-y)(x+y)}{28} - \frac{\sqrt{42}Q_v(x^2+y^2-2z^2)}{28} + \frac{\sqrt{42}Q_{xz}xz}{7} - \frac{\sqrt{42}Q_{yz}yz}{7} \\ & - \frac{3\sqrt{14}Q_{uxy}}{14} + \frac{\sqrt{42}Q_{xy}(x^2+y^2-2z^2)}{28} - \frac{\sqrt{42}Q_{xz}yz}{7} - \frac{\sqrt{42}Q_{yz}xz}{7} \end{aligned}$$

$$\tilde{\mathbb{Q}}_{4,1}^{(2,0)}[q](E_2, 1), \tilde{\mathbb{Q}}_{4,2}^{(2,0)}[q](E_2, 1)$$

\*\* symmetry

$$\frac{\sqrt{35}(x^2-2xy-y^2)(x^2+2xy-y^2)}{8}$$

$$\frac{\sqrt{35}xy(x-y)(x+y)}{2}$$

\*\* expression

$$\begin{aligned} & -\frac{7\sqrt{11}Q_u(x^2-2xy-y^2)(x^2+2xy-y^2)}{44} + \frac{\sqrt{33}Q_v(x-y)(x+y)(x^2+y^2-6z^2)}{44} \\ & - \frac{\sqrt{33}Q_{xy}xy(x^2+y^2-6z^2)}{22} + \frac{7\sqrt{33}Q_{xz}xz(x^2-3y^2)}{44} - \frac{7\sqrt{33}Q_{yz}yz(3x^2-y^2)}{44} \\ & - \frac{7\sqrt{11}Q_{uxy}(x-y)(x+y)}{11} + \frac{\sqrt{33}Q_{vxy}(x^2+y^2-6z^2)}{22} \\ & + \frac{\sqrt{33}Q_{xy}(x-y)(x+y)(x^2+y^2-6z^2)}{44} + \frac{7\sqrt{33}Q_{xz}yz(3x^2-y^2)}{44} + \frac{7\sqrt{33}Q_{yz}xz(x^2-3y^2)}{44} \end{aligned}$$

$$\tilde{\mathbb{Q}}_{4,1}^{(2,0)}[q](E_2, 2), \tilde{\mathbb{Q}}_{4,2}^{(2,0)}[q](E_2, 2)$$

\*\* symmetry

$$-\frac{\sqrt{5}(x-y)(x+y)(x^2+y^2-6z^2)}{4}$$

$$\frac{\sqrt{5}xy(x^2+y^2-6z^2)}{2}$$

\*\* expression

$$\begin{aligned} & -\frac{\sqrt{77}Q_u(x-y)(x+y)(x^2+y^2-6z^2)}{77} - \frac{\sqrt{231}Q_v(2x^4-3x^2y^2-9x^2z^2+2y^4-9y^2z^2+3z^4)}{77} \\ & - \frac{\sqrt{231}Q_{xy}xy(x-y)(x+y)}{22} + \frac{\sqrt{231}Q_{xz}xz(2x^2-3y^2+9z^2)}{154} + \frac{\sqrt{231}Q_{yz}yz(33x^2-2y^2-9z^2)}{154} \\ & \frac{2\sqrt{77}Q_{uxy}(x^2+y^2-6z^2)}{77} + \frac{\sqrt{231}Q_{vxy}(x-y)(x+y)}{22} + \frac{\sqrt{231}Q_{xy}(x^4+30x^2y^2-36x^2z^2+y^4-36y^2z^2+12z^4)}{308} \\ & - \frac{\sqrt{231}Q_{xz}yz(39x^2-31y^2+18z^2)}{308} + \frac{\sqrt{231}Q_{yz}xz(31x^2-39y^2-18z^2)}{308} \end{aligned}$$

$$\tilde{\mathbb{Q}}_{4,1}^{(2,2)}[q](E_2, 1), \tilde{\mathbb{Q}}_{4,2}^{(2,2)}[q](E_2, 1)$$

\*\* symmetry

$$\frac{\sqrt{35}(x^2-2xy-y^2)(x^2+2xy-y^2)}{8}$$

$$\frac{\sqrt{35}xy(x-y)(x+y)}{2}$$

\*\* expression

$$\begin{aligned} & -\frac{9\sqrt{1001}Q_u(x^2+y^2-10z^2)(x^2-2xy-y^2)(x^2+2xy-y^2)}{2288} + \frac{\sqrt{3003}Q_v(x-y)(x+y)(17x^4-230x^2y^2-8x^2z^2+17y^4-8y^2z^2+8z^4)}{2288} \\ & + \frac{\sqrt{3003}Q_{xy}xy(49x^4-166x^2y^2+8x^2z^2+49y^4+8y^2z^2-8z^4)}{1144} \\ & + \frac{3\sqrt{3003}Q_{xz}xz(7x^4-58x^2y^2-4x^2z^2+23y^4+12y^2z^2)}{1144} + \frac{3\sqrt{3003}Q_{yz}yz(23x^4-58x^2y^2+12x^2z^2+7y^4-4y^2z^2)}{1144} \end{aligned}$$

$$\begin{aligned}
& - \frac{9\sqrt{1001}Q_u xy (x-y) (x+y) (x^2 + y^2 - 10z^2)}{572} + \frac{\sqrt{3003}Q_v xy (25x^4 - 82x^2y^2 - 4x^2z^2 + 25y^4 - 4y^2z^2 + 4z^4)}{572} \\
& - \frac{\sqrt{3003}Q_{xy} (x-y) (x+y) (2x^4 - 29x^2y^2 + x^2z^2 + 2y^4 + y^2z^2 - z^4)}{286} \\
& + \frac{3\sqrt{3003}Q_{xz}yz (8x^4 - 13x^2y^2 - 3x^2z^2 + y^4 + y^2z^2)}{286} - \frac{3\sqrt{3003}Q_{yz}xz (x^4 - 13x^2y^2 + x^2z^2 + 8y^4 - 3y^2z^2)}{286}
\end{aligned}$$

$$\tilde{Q}_{4,1}^{(2,2)}[q](E_2, 2), \tilde{Q}_{4,2}^{(2,2)}[q](E_2, 2)$$

\*\* symmetry

$$- \frac{\sqrt{5} (x-y) (x+y) (x^2 + y^2 - 6z^2)}{4}$$

$$\frac{\sqrt{5}xy (x^2 + y^2 - 6z^2)}{2}$$

\*\* expression

$$\begin{aligned}
& \frac{21\sqrt{143}Q_u (x-y) (x+y) (x^4 + 2x^2y^2 - 16x^2z^2 + y^4 - 16y^2z^2 + 16z^4)}{1144} \\
& - \frac{\sqrt{429}Q_v (13x^6 - 45x^4y^2 - 150x^4z^2 - 45x^2y^4 + 540x^2y^2z^2 + 60x^2z^4 + 13y^6 - 150y^4z^2 + 60y^2z^4 - 8z^6)}{1144} \\
& - \frac{21\sqrt{429}Q_{xy}xy (x-y) (x+y) (x^2 + y^2 - 10z^2)}{572} - \frac{7\sqrt{429}Q_{xz}xz (7x^4 - 4x^2y^2 - 22x^2z^2 - 11y^4 + 26y^2z^2 + 4z^4)}{572} \\
& - \frac{7\sqrt{429}Q_{yz}yz (11x^4 + 4x^2y^2 - 26x^2z^2 - 7y^4 + 22y^2z^2 - 4z^4)}{572} \\
& - \frac{21\sqrt{143}Q_u xy (x^4 + 2x^2y^2 - 16x^2z^2 + y^4 - 16y^2z^2 + 16z^4)}{572} + \frac{21\sqrt{429}Q_v xy (x-y) (x+y) (x^2 + y^2 - 10z^2)}{572} \\
& - \frac{\sqrt{429}Q_{xy} (2x^6 - 15x^4y^2 - 15x^4z^2 - 15x^2y^4 + 180x^2y^2z^2 - 15x^2z^4 + 2y^6 - 15y^4z^2 - 15y^2z^4 + 2z^6)}{286} \\
& + \frac{7\sqrt{429}Q_{xz}yz (8x^4 + 7x^2y^2 - 23x^2z^2 - y^4 + y^2z^2 + 2z^4)}{286} - \frac{7\sqrt{429}Q_{yz}xz (x^4 - 7x^2y^2 - x^2z^2 - 8y^4 + 23y^2z^2 - 2z^4)}{286}
\end{aligned}$$