## SAMB for "C3h"

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• Generation condition

model type: tight\_bindingtime-reversal type: electric

irrep: [A']spinful

• Kets: dimension = 32

Table 1: Hilbert space for full matrix.

No.	ket	No.	ket	No.	ket	No.	ket	No.	ket
1	$(s,\uparrow)$ @H1 <sub>1</sub>	2	$(s,\downarrow)$ @H1 <sub>1</sub>	3	$(p_x,\uparrow)$ @O <sub>1</sub>	4	$(p_x,\downarrow)$ @O <sub>1</sub>	5	$(p_y,\uparrow)$ @O <sub>1</sub>
6	$(p_y,\downarrow)$ @O <sub>1</sub>	7	$(p_z,\uparrow)$ @ $\mathcal{O}_1$	8	$(p_z,\downarrow)$ @O <sub>1</sub>				

• Sites in (primitive) unit cell:

Table 2: Site-clusters.

	site	position	mapping
$S_1$	$H1_1$	$\begin{pmatrix} 0 & 0 & 0 \end{pmatrix}$	[1,2,3,4,5,6]
$S_2$	$O_1$	$\begin{pmatrix} \frac{1}{3} & 0 & 0 \end{pmatrix}$	[1,4]
	$O_2$	$\left(0  \frac{1}{3}  0\right)$	[2,6]
	$O_3$	$\left( -\frac{1}{3}  -\frac{1}{3}  0 \right)$	[3,5]

Table 2

	site	position	mapping
$S_3$	$H2_1$	$\begin{pmatrix} \frac{1}{2} & \frac{1}{6} & 0 \end{pmatrix}$	[1,4]
	$H2_2$	$\begin{pmatrix} -\frac{1}{6} & \frac{1}{3} & 0 \end{pmatrix}$	[2,6]
	$H2_3$	$\begin{pmatrix} -\frac{1}{3} & -\frac{1}{2} & 0 \end{pmatrix}$	[3,5]

• Bonds in (primitive) unit cell:

Table 3: Bond-clusters.

	bond	tail	head	n	#	b@c	mapping
$\mathrm{B}_1$	$b_1$	$H1_1$	$O_1$	1	1	$\begin{pmatrix} \frac{1}{3} & 0 & 0 \end{pmatrix} @ \begin{pmatrix} \frac{1}{6} & 0 & 0 \end{pmatrix}$	[1,4]
	$b_2$	$H1_1$	$O_2$	1	1	$\left(0  \frac{1}{3}  0\right) @ \left(0  \frac{1}{6}  0\right)$	[2,6]
	$b_3$	H1 <sub>1</sub>	$O_3$	1	1	$\left( -\frac{1}{3}  -\frac{1}{3}  0 \right) @ \left( -\frac{1}{6}  -\frac{1}{6}  0 \right)$	[3,5]
$B_2$	$b_4$	$O_1$	$H2_1$	1	1	$\begin{pmatrix} \frac{1}{6} & \frac{1}{6} & 0 \end{pmatrix} @ \begin{pmatrix} \frac{5}{12} & \frac{1}{12} & 0 \end{pmatrix}$	[1,4]
	$b_5$	$O_2$	$H2_2$	1	1	$ \begin{pmatrix} -\frac{1}{6} & 0 & 0 \end{pmatrix} @ \begin{pmatrix} -\frac{1}{12} & \frac{1}{3} & 0 \end{pmatrix} $	[2,6]
	$b_6$	$O_3$	$H2_3$	1	1	$\begin{pmatrix} 0 & -\frac{1}{6} & 0 \end{pmatrix} @ \begin{pmatrix} -\frac{1}{3} & -\frac{5}{12} & 0 \end{pmatrix}$	[3,5]

• SAMB:

No. 1 
$$\hat{\mathbb{Q}}_0^{(A')}$$
 [M<sub>1</sub>, S<sub>1</sub>]

$$\hat{\mathbb{Z}}_1 = \mathbb{X}_1[\mathbb{Q}_0^{(a,A')}] \otimes \mathbb{U}_1[\mathbb{Q}_0^{(s,A')}]$$

No. 2 
$$\hat{\mathbb{Q}}_0^{(A')}$$
 [M<sub>1</sub>, S<sub>2</sub>]

$$\hat{\mathbb{Z}}_2 = \mathbb{X}_1[\mathbb{Q}_0^{(a,A')}] \otimes \mathbb{U}_2[\mathbb{Q}_0^{(s,A')}]$$

No. 3 
$$\hat{\mathbb{Q}}_0^{(A')}$$
 [M<sub>2</sub>, S<sub>2</sub>]

$$\hat{\mathbb{Z}}_3 = \frac{\sqrt{2}\mathbb{X}_3[\mathbb{Q}_{1,0}^{(a,E')}] \otimes \mathbb{U}_3[\mathbb{Q}_{1,0}^{(s,E')}]}{2} + \frac{\sqrt{2}\mathbb{X}_4[\mathbb{Q}_{1,1}^{(a,E')}] \otimes \mathbb{U}_4[\mathbb{Q}_{1,1}^{(s,E')}]}{2}$$

No. 4 
$$\hat{\mathbb{G}}_1^{(A')}$$
 [M<sub>2</sub>, S<sub>2</sub>]

$$\hat{\mathbb{Z}}_4 = \frac{\sqrt{2}\mathbb{X}_3[\mathbb{Q}_{1,0}^{(a,E')}] \otimes \mathbb{U}_4[\mathbb{Q}_{1,1}^{(s,E')}]}{2} - \frac{\sqrt{2}\mathbb{X}_4[\mathbb{Q}_{1,1}^{(a,E')}] \otimes \mathbb{U}_3[\mathbb{Q}_{1,0}^{(s,E')}]}{2}$$

No. 5 
$$\hat{\mathbb{Q}}_0^{(A')}(1,0) [M_2, S_2]$$

$$\hat{\mathbb{Z}}_5 = \frac{\sqrt{2}\mathbb{X}_5[\mathbb{Q}_{1,0}^{(a,E')}(1,0)] \otimes \mathbb{U}_3[\mathbb{Q}_{1,0}^{(s,E')}]}{2} + \frac{\sqrt{2}\mathbb{X}_6[\mathbb{Q}_{1,1}^{(a,E')}(1,0)] \otimes \mathbb{U}_4[\mathbb{Q}_{1,1}^{(s,E')}]}{2}$$

No. 6 
$$\hat{\mathbb{G}}_1^{(A')}(1,0) [M_2, S_2]$$

$$\hat{\mathbb{Z}}_6 = \frac{\sqrt{2}\mathbb{X}_5[\mathbb{Q}_{1,0}^{(a,E')}(1,0)] \otimes \mathbb{U}_4[\mathbb{Q}_{1,1}^{(s,E')}]}{2} - \frac{\sqrt{2}\mathbb{X}_6[\mathbb{Q}_{1,1}^{(a,E')}(1,0)] \otimes \mathbb{U}_3[\mathbb{Q}_{1,0}^{(s,E')}]}{2}$$

No. 7 
$$\hat{\mathbb{Q}}_0^{(A')}$$
 [M<sub>3</sub>, S<sub>2</sub>]

$$\hat{\mathbb{Z}}_7 = \mathbb{X}_9[\mathbb{Q}_0^{(a,A')}] \otimes \mathbb{U}_2[\mathbb{Q}_0^{(s,A')}]$$

No. 8 
$$\hat{\mathbb{Q}}_2^{(A')}$$
 [M<sub>3</sub>, S<sub>2</sub>]

$$\hat{\mathbb{Z}}_8 = \mathbb{X}_{10}[\mathbb{Q}_2^{(a,A')}] \otimes \mathbb{U}_2[\mathbb{Q}_0^{(s,A')}]$$

No. 9 
$$\hat{\mathbb{Q}}_3^{(A',1)}$$
 [M<sub>3</sub>, S<sub>2</sub>]

$$\hat{\mathbb{Z}}_9 = \frac{\sqrt{2}\mathbb{X}_{14}[\mathbb{Q}_{2,0}^{(a,E')}] \otimes \mathbb{U}_4[\mathbb{Q}_{1,1}^{(s,E')}]}{2} - \frac{\sqrt{2}\mathbb{X}_{15}[\mathbb{Q}_{2,1}^{(a,E')}] \otimes \mathbb{U}_3[\mathbb{Q}_{1,0}^{(s,E')}]}{2}$$

No. 10 
$$\hat{\mathbb{Q}}_3^{(A',2)}$$
 [M<sub>3</sub>, S<sub>2</sub>]

$$\hat{\mathbb{Z}}_{10} = \frac{\sqrt{2}\mathbb{X}_{14}[\mathbb{Q}_{2,0}^{(a,E')}] \otimes \mathbb{U}_{3}[\mathbb{Q}_{1,0}^{(s,E')}]}{2} + \frac{\sqrt{2}\mathbb{X}_{15}[\mathbb{Q}_{2,1}^{(a,E')}] \otimes \mathbb{U}_{4}[\mathbb{Q}_{1,1}^{(s,E')}]}{2}$$

No. 11 
$$\hat{\mathbb{Q}}_0^{(A')}(1,1)$$
 [M<sub>3</sub>, S<sub>2</sub>]

$$\hat{\mathbb{Z}}_{11} = \mathbb{X}_{11}[\mathbb{Q}_0^{(a,A')}(1,1)] \otimes \mathbb{U}_2[\mathbb{Q}_0^{(s,A')}]$$

No. 12 
$$\hat{\mathbb{Q}}_2^{(A')}(1,-1)$$
 [M<sub>3</sub>, S<sub>2</sub>]

$$\hat{\mathbb{Z}}_{12} = \mathbb{X}_{12}[\mathbb{Q}_2^{(a,A')}(1,-1)] \otimes \mathbb{U}_2[\mathbb{Q}_0^{(s,A')}]$$

No. 13 
$$\hat{\mathbb{Q}}_3^{(A',1)}(1,-1)$$
 [M<sub>3</sub>, S<sub>2</sub>]

$$\hat{\mathbb{Z}}_{13} = \frac{\sqrt{2}\mathbb{X}_{16}[\mathbb{Q}_{2,0}^{(a,E')}(1,-1)] \otimes \mathbb{U}_{4}[\mathbb{Q}_{1,1}^{(s,E')}]}{2} - \frac{\sqrt{2}\mathbb{X}_{17}[\mathbb{Q}_{2,1}^{(a,E')}(1,-1)] \otimes \mathbb{U}_{3}[\mathbb{Q}_{1,0}^{(s,E')}]}{2}$$

No. 14 
$$\hat{\mathbb{Q}}_3^{(A',2)}(1,-1)$$
 [M<sub>3</sub>, S<sub>2</sub>]

$$\hat{\mathbb{Z}}_{14} = \frac{\sqrt{2}\mathbb{X}_{16}[\mathbb{Q}_{2,0}^{(a,E')}(1,-1)] \otimes \mathbb{U}_{3}[\mathbb{Q}_{1,0}^{(s,E')}]}{2} + \frac{\sqrt{2}\mathbb{X}_{17}[\mathbb{Q}_{2,1}^{(a,E')}(1,-1)] \otimes \mathbb{U}_{4}[\mathbb{Q}_{1,1}^{(s,E')}]}{2}$$

No. 15 
$$\hat{\mathbb{G}}_1^{(A')}(1,0) [M_3, S_2]$$

$$\hat{\mathbb{Z}}_{15} = \mathbb{X}_{13}[\mathbb{G}_1^{(a,A')}(1,0)] \otimes \mathbb{U}_2[\mathbb{Q}_0^{(s,A')}]$$

No. 16 
$$\hat{\mathbb{Q}}_0^{(A')}$$
 [M<sub>1</sub>, S<sub>3</sub>]

$$\hat{\mathbb{Z}}_{16} = \mathbb{X}_1[\mathbb{Q}_0^{(a,A')}] \otimes \mathbb{U}_5[\mathbb{Q}_0^{(s,A')}]$$

No. 17 
$$\hat{\mathbb{Q}}_0^{(A')}$$
 [M<sub>1</sub>, B<sub>1</sub>]

$$\hat{\mathbb{Z}}_{17} = \mathbb{X}_1[\mathbb{Q}_0^{(a,A')}] \otimes \mathbb{U}_6[\mathbb{Q}_0^{(u,A')}]$$

No. 18 
$$\hat{\mathbb{G}}_{1}^{(A')}(1,-1) [M_{1},B_{1}]$$

$$\hat{\mathbb{Z}}_{18} = \mathbb{X}_2[\mathbb{M}_1^{(a,A')}(1,-1)] \otimes \mathbb{U}_9[\mathbb{T}_0^{(u,A')}]$$

No. 19 
$$\hat{\mathbb{Q}}_0^{(A')}$$
 [M<sub>2</sub>, B<sub>1</sub>]

$$\hat{\mathbb{Z}}_{19} = \frac{\sqrt{2}\mathbb{X}_{3}[\mathbb{Q}_{1,0}^{(a,E')}] \otimes \mathbb{U}_{7}[\mathbb{Q}_{1,0}^{(u,E')}]}{2} + \frac{\sqrt{2}\mathbb{X}_{4}[\mathbb{Q}_{1,1}^{(a,E')}] \otimes \mathbb{U}_{8}[\mathbb{Q}_{1,1}^{(u,E')}]}{2}$$

No. 20 
$$\hat{\mathbb{G}}_1^{(A')}$$
 [M<sub>2</sub>, B<sub>1</sub>]

$$\hat{\mathbb{Z}}_{20} = \frac{\sqrt{2}\mathbb{X}_{3}[\mathbb{Q}_{1,0}^{(a,E')}] \otimes \mathbb{U}_{8}[\mathbb{Q}_{1,1}^{(u,E')}]}{2} - \frac{\sqrt{2}\mathbb{X}_{4}[\mathbb{Q}_{1,1}^{(a,E')}] \otimes \mathbb{U}_{7}[\mathbb{Q}_{1,0}^{(u,E')}]}{2}$$

No. 21 
$$\hat{\mathbb{Q}}_0^{(A')}(1,0)$$
 [M<sub>2</sub>, B<sub>1</sub>]

$$\hat{\mathbb{Z}}_{21} = \frac{\sqrt{2}\mathbb{X}_{5}[\mathbb{Q}_{1,0}^{(a,E')}(1,0)] \otimes \mathbb{U}_{7}[\mathbb{Q}_{1,0}^{(u,E')}]}{2} + \frac{\sqrt{2}\mathbb{X}_{6}[\mathbb{Q}_{1,1}^{(a,E')}(1,0)] \otimes \mathbb{U}_{8}[\mathbb{Q}_{1,1}^{(u,E')}]}{2}$$

No. 22 
$$\hat{\mathbb{G}}_{1}^{(A')}(1,0)$$
 [M<sub>2</sub>, B<sub>1</sub>]

$$\hat{\mathbb{Z}}_{22} = \frac{\sqrt{2}\mathbb{X}_{5}[\mathbb{Q}_{1,0}^{(a,E')}(1,0)] \otimes \mathbb{U}_{8}[\mathbb{Q}_{1,1}^{(u,E')}]}{2} - \frac{\sqrt{2}\mathbb{X}_{6}[\mathbb{Q}_{1,1}^{(a,E')}(1,0)] \otimes \mathbb{U}_{7}[\mathbb{Q}_{1,0}^{(u,E')}]}{2}$$

No. 23 
$$\hat{\mathbb{G}}_{1}^{(A')}(1,-1)$$
 [M<sub>2</sub>, B<sub>1</sub>]

$$\hat{\mathbb{Z}}_{23} = \frac{\sqrt{2}\mathbb{X}_{7}[\mathbb{M}_{2,0}^{(a,E')}(1,-1)] \otimes \mathbb{U}_{10}[\mathbb{T}_{1,0}^{(u,E')}]}{2} + \frac{\sqrt{2}\mathbb{X}_{8}[\mathbb{M}_{2,1}^{(a,E')}(1,-1)] \otimes \mathbb{U}_{11}[\mathbb{T}_{1,1}^{(u,E')}]}{2}$$

No. 24 
$$\hat{\mathbb{Q}}_2^{(A')}(1,-1)$$
 [M<sub>2</sub>, B<sub>1</sub>]

$$\hat{\mathbb{Z}}_{24} = \frac{\sqrt{2}\mathbb{X}_{7}[\mathbb{M}_{2,0}^{(a,E')}(1,-1)] \otimes \mathbb{U}_{11}[\mathbb{T}_{1,1}^{(u,E')}]}{2} - \frac{\sqrt{2}\mathbb{X}_{8}[\mathbb{M}_{2,1}^{(a,E')}(1,-1)] \otimes \mathbb{U}_{10}[\mathbb{T}_{1,0}^{(u,E')}]}{2}$$

No. 25 
$$\hat{\mathbb{Q}}_0^{(A')}$$
 [M<sub>1</sub>, B<sub>2</sub>]

$$\hat{\mathbb{Z}}_{25} = \mathbb{X}_1[\mathbb{Q}_0^{(a,A')}] \otimes \mathbb{U}_{12}[\mathbb{Q}_0^{(u,A')}]$$

No. 26 
$$\hat{\mathbb{G}}_1^{(A')}(1,-1)$$
 [M<sub>1</sub>, B<sub>2</sub>]

$$\hat{\mathbb{Z}}_{26} = \mathbb{X}_2[\mathbb{M}_1^{(a,A')}(1,-1)] \otimes \mathbb{U}_{15}[\mathbb{T}_0^{(u,A')}]$$

No. 27 
$$\hat{\mathbb{Q}}_0^{(A')}$$
 [M<sub>4</sub>, B<sub>2</sub>]

$$\hat{\mathbb{Z}}_{27} = \frac{\sqrt{2}\mathbb{X}_{18}[\mathbb{Q}_{1,0}^{(a,E')}] \otimes \mathbb{U}_{13}[\mathbb{Q}_{1,0}^{(u,E')}]}{2} + \frac{\sqrt{2}\mathbb{X}_{19}[\mathbb{Q}_{1,1}^{(a,E')}] \otimes \mathbb{U}_{14}[\mathbb{Q}_{1,1}^{(u,E')}]}{2}$$

No. 28 
$$\hat{\mathbb{G}}_{1}^{(A')}$$
 [M<sub>4</sub>, B<sub>2</sub>]

$$\hat{\mathbb{Z}}_{28} = \frac{\sqrt{2}\mathbb{X}_{18}[\mathbb{Q}_{1,0}^{(a,E')}] \otimes \mathbb{U}_{14}[\mathbb{Q}_{1,1}^{(u,E')}]}{2} - \frac{\sqrt{2}\mathbb{X}_{19}[\mathbb{Q}_{1,1}^{(a,E')}] \otimes \mathbb{U}_{13}[\mathbb{Q}_{1,0}^{(u,E')}]}{2}$$

No. 29 
$$\hat{\mathbb{Q}}_0^{(A')}(1,0)$$
 [M<sub>4</sub>, B<sub>2</sub>]

$$\hat{\mathbb{Z}}_{29} = \frac{\sqrt{2}\mathbb{X}_{20}[\mathbb{Q}_{1,0}^{(a,E')}(1,0)] \otimes \mathbb{U}_{13}[\mathbb{Q}_{1,0}^{(u,E')}]}{2} + \frac{\sqrt{2}\mathbb{X}_{21}[\mathbb{Q}_{1,1}^{(a,E')}(1,0)] \otimes \mathbb{U}_{14}[\mathbb{Q}_{1,1}^{(u,E')}]}{2}$$

No. 30 
$$\hat{\mathbb{G}}_{1}^{(A')}(1,0)$$
 [M<sub>4</sub>, B<sub>2</sub>]

$$\hat{\mathbb{Z}}_{30} = \frac{\sqrt{2}\mathbb{X}_{20}[\mathbb{Q}_{1,0}^{(a,E')}(1,0)] \otimes \mathbb{U}_{14}[\mathbb{Q}_{1,1}^{(u,E')}]}{2} - \frac{\sqrt{2}\mathbb{X}_{21}[\mathbb{Q}_{1,1}^{(a,E')}(1,0)] \otimes \mathbb{U}_{13}[\mathbb{Q}_{1,0}^{(u,E')}]}{2}$$

No. 31 
$$\hat{\mathbb{G}}_{1}^{(A')}(1,-1)$$
 [M<sub>4</sub>, B<sub>2</sub>]

$$\hat{\mathbb{Z}}_{31} = \frac{\sqrt{2}\mathbb{X}_{22}[\mathbb{M}_{2,0}^{(a,E')}(1,-1)] \otimes \mathbb{U}_{16}[\mathbb{T}_{1,0}^{(u,E')}]}{2} + \frac{\sqrt{2}\mathbb{X}_{23}[\mathbb{M}_{2,1}^{(a,E')}(1,-1)] \otimes \mathbb{U}_{17}[\mathbb{T}_{1,1}^{(u,E')}]}{2}$$

No. 32 
$$\hat{\mathbb{Q}}_2^{(A')}(1,-1)$$
 [M<sub>4</sub>, B<sub>2</sub>]

$$\hat{\mathbb{Z}}_{32} = \frac{\sqrt{2}\mathbb{X}_{22}[\mathbb{M}_{2,0}^{(a,E')}(1,-1)] \otimes \mathbb{U}_{17}[\mathbb{T}_{1,1}^{(u,E')}]}{2} - \frac{\sqrt{2}\mathbb{X}_{23}[\mathbb{M}_{2,1}^{(a,E')}(1,-1)] \otimes \mathbb{U}_{16}[\mathbb{T}_{1,0}^{(u,E')}]}{2}$$

Table 4: Atomic SAMB group.

group	bra	ket
$M_1$	$(s,\uparrow),(s,\downarrow)$	$(s,\uparrow),(s,\downarrow)$
$M_2$	$(s,\uparrow),(s,\downarrow)$	$(p_x,\uparrow),(p_x,\downarrow),(p_y,\uparrow),(p_y,\downarrow),(p_z,\uparrow),(p_z,\downarrow)$
$M_3$	$(p_x,\uparrow),(p_x,\downarrow),(p_y,\uparrow),(p_y,\downarrow),(p_z,\uparrow),(p_z,\downarrow)$	$(p_x,\uparrow),(p_x,\downarrow),(p_y,\uparrow),(p_y,\downarrow),(p_z,\uparrow),(p_z,\downarrow)$
$M_4$	$(p_x,\uparrow),(p_x,\downarrow),(p_y,\uparrow),(p_y,\downarrow),(p_z,\uparrow),(p_z,\downarrow)$	$(s,\uparrow),(s,\downarrow)$

Table 5: Atomic SAMB.

symbol	type	group	form
$\mathbb{X}_1$	$\mathbb{Q}_0^{(a,A')}$	$M_1$	$\begin{pmatrix} \frac{\sqrt{2}}{2} & 0 \\ 0 & \frac{\sqrt{2}}{2} \end{pmatrix}$
$\mathbb{X}_2$	$\mathbb{M}_1^{(a,A')}(1,-1)$	$M_1$	$\begin{pmatrix} \frac{\sqrt{2}}{2} & 0 \\ 0 & -\frac{\sqrt{2}}{2} \end{pmatrix}$
$\mathbb{X}_3$	$\mathbb{Q}_{1,0}^{(a,E')}$	$M_2$	$\begin{pmatrix} \frac{\sqrt{2}}{2} & 0 & 0 & 0 & 0 & 0 \\ 0 & \frac{\sqrt{2}}{2} & 0 & 0 & 0 & 0 \end{pmatrix}$ $\begin{pmatrix} 0 & 0 & \frac{\sqrt{2}}{2} & 0 & 0 & 0 \\ 0 & 0 & 0 & \frac{\sqrt{2}}{2} & 0 & 0 \end{pmatrix}$
$\mathbb{X}_4$	$\mathbb{Q}_{1,1}^{(a,E')}$	$M_2$	$\begin{pmatrix} 0 & 0 & \frac{\sqrt{2}}{2} & 0 & 0 & 0 \\ 0 & 0 & 0 & \frac{\sqrt{2}}{2} & 0 & 0 \end{pmatrix}$
$\mathbb{X}_5$	$\mathbb{Q}_{1,0}^{(a,E')}(1,0)$	$M_2$	$ \begin{pmatrix} 0 & 0 & -\frac{i}{2} & 0 & 0 & \frac{i}{2} \\ 0 & 0 & 0 & \frac{i}{2} & -\frac{1}{2} & 0 \end{pmatrix} $
$\mathbb{X}_6$	$\mathbb{Q}_{1,1}^{(a,E')}(1,0)$	$M_2$	$\begin{pmatrix} \frac{i}{2} & 0 & 0 & 0 & 0 & -\frac{i}{2} \\ 0 & -\frac{i}{2} & 0 & 0 & -\frac{i}{2} & 0 \end{pmatrix}$
$\mathbb{X}_7$	$\mathbb{M}_{2,0}^{(a,E')}(1,-1)$	$M_2$	$ \begin{pmatrix} \frac{1}{2} & 0 & 0 & 0 & 0 & \frac{1}{2} \\ 0 & -\frac{1}{2} & 0 & 0 & \frac{1}{2} & 0 \end{pmatrix} $
$\mathbb{X}_8$	$\mathbb{M}_{2,1}^{(a,E')}(1,-1)$	$M_2$	$\begin{pmatrix} 0 & 0 & 0 & -\frac{1}{2} & \frac{i}{2} & 0 \end{pmatrix}$
$\mathbb{X}_9$	$\mathbb{Q}_0^{(a,A')}$	$ m M_3$	$\begin{pmatrix} \frac{\sqrt{6}}{6} & 0 & 0 & 0 & 0 & 0 \\ 0 & \frac{\sqrt{6}}{6} & 0 & 0 & 0 & 0 \\ 0 & 0 & \frac{\sqrt{6}}{6} & 0 & 0 & 0 \\ 0 & 0 & 0 & \frac{\sqrt{6}}{6} & 0 & 0 \\ 0 & 0 & 0 & 0 & \frac{\sqrt{6}}{6} & 0 \\ 0 & 0 & 0 & 0 & 0 & \frac{\sqrt{6}}{6} \end{pmatrix}$
X <sub>10</sub>	$\mathbb{Q}_2^{(a,A')}$	$ m M_3$	$\begin{pmatrix} -\frac{\sqrt{3}}{6} & 0 & 0 & 0 & 0 & 0 \\ 0 & -\frac{\sqrt{3}}{6} & 0 & 0 & 0 & 0 \\ 0 & 0 & -\frac{\sqrt{3}}{6} & 0 & 0 & 0 \\ 0 & 0 & 0 & -\frac{\sqrt{3}}{6} & 0 & 0 \\ 0 & 0 & 0 & 0 & \frac{\sqrt{3}}{3} & 0 \\ 0 & 0 & 0 & 0 & 0 & \frac{\sqrt{3}}{3} \end{pmatrix}$

Table 5

Table 5			
symbol	type	group	form
$\mathbb{X}_{11}$	$\mathbb{Q}_0^{(a,A')}(1,1)$	$ m M_3$	$ \begin{pmatrix} 0 & 0 & -\frac{\sqrt{3}i}{6} & 0 & 0 & \frac{\sqrt{3}}{6} \\ 0 & 0 & 0 & \frac{\sqrt{3}i}{6} & -\frac{\sqrt{3}}{6} & 0 \\ \frac{\sqrt{3}i}{6} & 0 & 0 & 0 & 0 & -\frac{\sqrt{3}i}{6} \\ 0 & -\frac{\sqrt{3}i}{6} & 0 & 0 & -\frac{\sqrt{3}i}{6} & 0 \\ 0 & -\frac{\sqrt{3}}{6} & 0 & \frac{\sqrt{3}i}{6} & 0 & 0 \\ \frac{\sqrt{3}}{6} & 0 & \frac{\sqrt{3}i}{6} & 0 & 0 & 0 \end{pmatrix} $ $ \begin{pmatrix} 0 & 0 & -\frac{\sqrt{6}i}{6} & 0 & 0 & -\frac{\sqrt{6}}{12} \\ 0 & 0 & 0 & \frac{\sqrt{6}i}{6} & \frac{\sqrt{6}i}{12} & 0 \end{pmatrix} $
$\mathbb{X}_{12}$	$\mathbb{Q}_2^{(a,A')}(1,-1)$	$ m M_3$	$ \begin{pmatrix} 0 & 0 & -\frac{\sqrt{6}i}{6} & 0 & 0 & -\frac{\sqrt{6}}{12} \\ 0 & 0 & 0 & \frac{\sqrt{6}i}{6} & \frac{\sqrt{6}}{12} & 0 \\ \frac{\sqrt{6}i}{6} & 0 & 0 & 0 & 0 & \frac{\sqrt{6}i}{12} \\ 0 & -\frac{\sqrt{6}i}{6} & 0 & 0 & \frac{\sqrt{6}i}{12} & 0 \\ 0 & \frac{\sqrt{6}}{12} & 0 & -\frac{\sqrt{6}i}{12} & 0 & 0 \\ -\frac{\sqrt{6}}{12} & 0 & -\frac{\sqrt{6}i}{12} & 0 & 0 & 0 \end{pmatrix} $
$\mathbb{X}_{13}$	$\mathbb{G}_{1}^{(a,A')}(1,0)$	$ m M_3$	$ \begin{pmatrix} 0 & 0 & 0 & 0 & 0 & \frac{\sqrt{2}i}{4} \\ 0 & 0 & 0 & 0 & \frac{\sqrt{2}i}{4} & 0 \\ 0 & 0 & 0 & 0 & 0 & \frac{\sqrt{2}}{4} \\ 0 & 0 & 0 & 0 & -\frac{\sqrt{2}}{4} & 0 \\ 0 & -\frac{\sqrt{2}i}{4} & 0 & -\frac{\sqrt{2}}{4} & 0 & 0 \\ -\frac{\sqrt{2}i}{4} & 0 & \frac{\sqrt{2}}{4} & 0 & 0 \end{pmatrix} $
$\mathbb{X}_{14}$	$\mathbb{Q}_{2,0}^{(a,E')}$	$ m M_3$	$\begin{pmatrix} \frac{1}{2} & 0 & 0 & 0 & 0 & 0 \\ 0 & \frac{1}{2} & 0 & 0 & 0 & 0 \\ 0 & 0 & -\frac{1}{2} & 0 & 0 & 0 \\ 0 & 0 & 0 & -\frac{1}{2} & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 &$
$\mathbb{X}_{15}$	$\mathbb{Q}_{2,1}^{(a,E')}$	$ m M_3$	$\begin{pmatrix} 0 & 0 & -\frac{1}{2} & 0 & 0 & 0 \\ 0 & 0 & 0 & -\frac{1}{2} & 0 & 0 \\ -\frac{1}{2} & 0 & 0 & 0 & 0 & 0 \\ 0 & -\frac{1}{2} & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0$

continued ...

Table 5

symbol	type	group	form
X16	$\mathbb{Q}_{2,0}^{(a,E')}(1,-1)$	М3	$\begin{pmatrix} 0 & 0 & 0 & 0 & 0 & -\frac{\sqrt{2}}{4} \\ 0 & 0 & 0 & 0 & \frac{\sqrt{2}}{4} & 0 \\ 0 & 0 & 0 & 0 & 0 & -\frac{\sqrt{2}i}{4} \\ 0 & 0 & 0 & 0 & -\frac{\sqrt{2}i}{4} & 0 \\ 0 & \frac{\sqrt{2}}{4} & 0 & \frac{\sqrt{2}i}{4} & 0 & 0 \\ -\frac{\sqrt{2}}{4} & 0 & \frac{\sqrt{2}i}{4} & 0 & 0 & 0 \end{pmatrix}$
$\mathbb{X}_{17}$	$\mathbb{Q}_{2,1}^{(a,E')}(1,-1)$	$ m M_3$	$\begin{pmatrix} 0 & 0 & 0 & 0 & 0 & -\frac{\sqrt{2}i}{4} \\ 0 & 0 & 0 & 0 & -\frac{\sqrt{2}i}{4} & 0 \\ 0 & 0 & 0 & 0 & 0 & \frac{\sqrt{2}}{4} \\ 0 & 0 & 0 & 0 & -\frac{\sqrt{2}}{4} & 0 \\ 0 & \frac{\sqrt{2}i}{4} & 0 & -\frac{\sqrt{2}}{4} & 0 & 0 \\ \sqrt{2}i & 0 & \sqrt{2} & 0 & 0 & 0 \end{pmatrix}$
$\mathbb{X}_{18}$	$\mathbb{Q}_{1,0}^{(a,E')}$	$ m M_4$	$ \begin{pmatrix} \frac{\sqrt{2}}{4} & 0 & \frac{\sqrt{2}}{4} & 0 & 0 & 0 \end{pmatrix} $ $ \begin{pmatrix} \frac{\sqrt{2}}{2} & 0 \\ 0 & \frac{\sqrt{2}}{2} \\ 0 & 0 \\ 0 & 0 \\ 0 & 0 \\ 0 & 0 \end{pmatrix} $
$\mathbb{X}_{19}$	$\mathbb{Q}_{1,1}^{(a,E')}$	$ m M_4$	$\begin{pmatrix} 0 & 0 \\ 0 & 0 \\ \frac{\sqrt{2}}{2} & 0 \\ 0 & \frac{\sqrt{2}}{2} \\ 0 & 0 \\ 0 & 0 \end{pmatrix}$
$\mathbb{X}_{20}$	$\mathbb{Q}_{1,0}^{(a,E')}(1,0)$	$ m M_4$	$\begin{pmatrix} 0 & 0 \\ 0 & 0 \\ \frac{i}{2} & 0 \\ 0 & -\frac{i}{2} \\ 0 & -\frac{1}{2} \\ \frac{1}{2} & 0 \end{pmatrix}$

Table 5

Table 5			
symbol	type	group	form
$\mathbb{X}_{21}$	$\mathbb{Q}_{1,1}^{(a,E')}(1,0)$	$ m M_4$	$\begin{pmatrix} -\frac{i}{2} & 0\\ 0 & \frac{i}{2}\\ 0 & 0\\ 0 & 0\\ 0 & \frac{i}{2}\\ \frac{i}{2} & 0 \end{pmatrix}$
$\mathbb{X}_{22}$	$\mathbb{M}_{2,0}^{(a,E')}(1,-1)$	$ m M_4$	$\begin{pmatrix} \frac{1}{2} & 0 \\ 0 & -\frac{1}{2} \\ 0 & 0 \\ 0 & 0 \\ 0 & \frac{1}{2} \\ \frac{1}{2} & 0 \end{pmatrix}$
$\mathbb{X}_{23}$	$\mathbb{M}_{2,1}^{(a,E')}(1,-1)$	$ m M_4$	$\begin{pmatrix} 0 & 0 \\ 0 & 0 \\ \frac{1}{2} & 0 \\ 0 & -\frac{1}{2} \\ 0 & -\frac{i}{2} \\ \frac{i}{2} & 0 \end{pmatrix}$

Table 6: Uniform SAMB.

symbol	type	cluster	form					
			(1 0 0 0 0 0 0)					
		$S_1$				0 0 0 0 0 0 0		
	$\mathbb{Q}_0^{(s,A')}$		0 0 0 0 0 0 0					
$\mathbb{U}_1$			$S_1$	$S_1$	$S_1$	$S_1$	$S_1$	0 0 0 0 0 0 0
			0 0 0 0 0 0 0					
			0 0 0 0 0 0					
			(0 0 0 0 0 0 0)					

Table 6

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symbol	type	cluster	form
пт	$\mathbb{Q}_0^{(s,A')}$	g	$\begin{pmatrix} 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & \frac{\sqrt{3}}{3} & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & \frac{\sqrt{3}}{3} & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0$
$\mathbb{U}_2$	Qò '	$S_2$	$\begin{bmatrix} 0 & 0 & 0 & \frac{\sqrt{3}}{3} & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0$
$\mathbb{U}_3$	$\mathbb{Q}_{1,0}^{(s,E')}$	$\mathrm{S}_2$	$\begin{pmatrix} 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & -\frac{\sqrt{6}}{6} & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & \frac{\sqrt{6}}{3} & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & -\frac{\sqrt{6}}{6} & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0$
$\mathbb{U}_4$	$\mathbb{Q}_{1,1}^{(s,E')}$	$\mathrm{S}_2$	$\begin{pmatrix} 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & -\frac{\sqrt{2}}{2} & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0$
$\mathbb{U}_5$	$\mathbb{Q}_0^{(s,A')}$	$\mathrm{S}_3$	$\begin{pmatrix} 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 &$

Table 6

symbol	type	cluster	form
symbol	туре	cluster	/ / / / / / / / / / / / / / / / / / / /
			$\begin{pmatrix} 0 & \frac{\sqrt{6}}{6} & \frac{\sqrt{6}}{6} & \frac{\sqrt{6}}{6} & 0 & 0 & 0 \\ \frac{\sqrt{6}}{6} & 0 & 0 & 0 & 0 & 0 \end{pmatrix}$
			$\begin{bmatrix} \frac{\sqrt{6}}{6} & 0 & 0 & 0 & 0 & 0 \end{bmatrix}$
	a(u,A')	_	$\left[\begin{array}{cccccccccccccccccccccccccccccccccccc$
$\mathbb{U}_6$	$\mathbb{Q}_0^{(u,A')}$	$B_1$	$ \begin{pmatrix} 0 & \frac{\sqrt{6}}{6} & \frac{\sqrt{6}}{6} & \frac{\sqrt{6}}{6} & 0 & 0 & 0 \\ \frac{\sqrt{6}}{6} & 0 & 0 & 0 & 0 & 0 & 0 \\ \frac{\sqrt{6}}{6} & 0 & 0 & 0 & 0 & 0 & 0 \\ \frac{\sqrt{6}}{6} & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0$
			$\begin{pmatrix} 0 & -\frac{\sqrt{3}}{6} & \frac{\sqrt{3}}{3} & -\frac{\sqrt{3}}{6} & 0 & 0 \end{pmatrix}$
			$\left[ \begin{array}{cccccccccccccccccccccccccccccccccccc$
	. ,.		$\left[\begin{array}{cccccccccccccccccccccccccccccccccccc$
$\mathbb{U}_7$	$\mathbb{Q}_{1,0}^{(u,E')}$	$\mathrm{B}_1$	$\begin{bmatrix} -\frac{\sqrt{3}}{6} & 0 & 0 & 0 & 0 & 0 & 0 \\ \frac{\sqrt{3}}{3} & 0 & 0 & 0 & 0 & 0 & 0 \\ -\frac{\sqrt{3}}{6} & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0$
	,		0 0 0 0 0 0 0
			$\begin{pmatrix} 0 & -\frac{1}{2} & 0 & \frac{1}{2} & 0 & 0 & 0 \end{pmatrix}$
			$\left( \begin{array}{cccccccccccccccccccccccccccccccccccc$
	$\mathbb{Q}_{1,1}^{(u,E')}$		0 0 0 0 0 0 0
$\mathbb{U}_8$		$B_1$	$ \left  \begin{array}{cccccccccccccccccccccccccccccccccccc$
			$\begin{pmatrix} 0 & \frac{\sqrt{6}i}{6} & \frac{\sqrt{6}i}{6} & 0 & 0 & 0 \end{pmatrix}$
			$\left[ \begin{array}{cccccccccccccccccccccccccccccccccccc$
			$\begin{bmatrix} \frac{6}{-\sqrt{6}i} & 0 & 0 & 0 & 0 & 0 \end{bmatrix}$
$\mathbb{U}_9$	$\mathbb{T}_0^{(u,A')}$	$_{ m B_1}$	$\begin{bmatrix} -\frac{\sqrt{6}i}{6} & 0 & 0 & 0 & 0 & 0 & 0 \\ -\frac{\sqrt{6}i}{6} & 0 & 0 & 0 & 0 & 0 & 0 \\ -\frac{\sqrt{6}i}{6} & 0 & 0 & 0 & 0 & 0 & 0 \end{bmatrix}$
~ y	-0		$\begin{bmatrix} -\frac{6}{6} & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0$

Table 6

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symbol	type	cluster	form $\sqrt{3}i$ $\sqrt{3}i$ $\sqrt{3}i$ $\sqrt{3}i$
$\mathbb{U}_{10}$	$\mathbb{T}_{1,0}^{(u,E')}$	$\mathrm{B}_1$	$ \begin{pmatrix} 0 & -\frac{\sqrt{3}i}{6} & \frac{\sqrt{3}i}{3} & -\frac{\sqrt{3}i}{6} & 0 & 0 & 0 \\ \frac{\sqrt{3}i}{6} & 0 & 0 & 0 & 0 & 0 & 0 \\ -\frac{\sqrt{3}i}{3} & 0 & 0 & 0 & 0 & 0 & 0 \\ \frac{\sqrt{3}i}{6} & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0$
$\mathbb{U}_{11}$	$\mathbb{T}_{1,1}^{(u,E')}$	$\mathrm{B}_1$	$\begin{pmatrix} 0 & -\frac{i}{2} & 0 & \frac{i}{2} & 0 & 0 & 0 \\ \frac{i}{2} & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0$
$\mathbb{U}_{12}$	$\mathbb{Q}_0^{(u,A')}$	$\mathrm{B}_2$	$\begin{pmatrix} 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 &$
$\mathbb{U}_{13}$	$\mathbb{Q}_{1,0}^{(u,E')}$	$\mathrm{B}_2$	$ \begin{pmatrix} 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 &$

Table 6

symbol	type	cluster	form
$\mathbb{U}_{14}$	$\mathbb{Q}_{1,1}^{(u,E')}$	$\mathrm{B}_2$	$\begin{pmatrix} 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 &$
$\mathbb{U}_{15}$	$\mathbb{T}_0^{(u,A')}$	$\mathrm{B}_2$	$ \begin{pmatrix} 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 &$
$\mathbb{U}_{16}$	$\mathbb{T}_{1,0}^{(u,E')}$	$\mathrm{B}_2$	$ \left( \begin{array}{cccccccccccccccccccccccccccccccccccc$
$\mathbb{U}_{17}$	$\mathbb{T}_{1,1}^{(u,E')}$	$\mathrm{B}_2$	$\begin{pmatrix} 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 &$

Table 7: Polar harmonics.

No.	symbol	rank	irrep.	mul.	comp.	form
1	$\mathbb{Q}_0^{(A')}$	0	A'	_	_	1
2	$\mathbb{Q}_{1,0}^{(E')}$	1	E'	_	0	x
3	$\mathbb{Q}_{1,1}^{(E')}$	1	E'	_	1	y
4	$\mathbb{Q}_2^{(A')}$	2	A'	_	_	$-\frac{x^2}{2} - \frac{y^2}{2} + z^2$
5	$\mathbb{Q}_{2,0}^{(E')}$	2	E'	_	0	$\frac{\sqrt{3}(x^2-y^2)}{2}$
6	$\mathbb{Q}_{2,1}^{(E')}$	2	E'	_	1	$-\sqrt{3}xy$

Table 8: Axial harmonics.

No.	symbol	rank	irrep.	mul.	comp.	form
1	$\mathbb{G}_1^{(A')}$	1	A'	_	_	Z
2	$\mathbb{G}_{2,0}^{(E')}$	2	E'	_	0	$\sqrt{3}XZ$
3	$\mathbb{G}_{2,1}^{(E')}$	2	E'	_	1	$\sqrt{3}YZ$

• Group info.: Generator =  $3^+_{001}$ ,  $m_{001}$ 

Table 9: Conjugacy class.

rep. SO	symmetry operations
1	1
3 <sup>+</sup> <sub>001</sub>	3 <sup>+</sup> <sub>001</sub>
3-001	3_001
m <sub>001</sub>	m <sub>001</sub>
$-6^{+}_{001}$	$-6^{+}_{001}$

Table 9

rep. SO	symmetry operations
$-6^{-}_{001}$	$-6^{-}_{001}$

Table 10: Symmetry operations.

No.	SO	No.	SO	No.	SO	No.	SO	No.	SO
1	1	2	3 <sup>+</sup> <sub>001</sub>	3	3-001	4	$m_{001}$	5	$-6^{+}_{001}$
6	$-6^{-}_{001}$								

Table 11: Character table.

	1	$3^{+}_{001}$	$3^{-}_{001}$	$m_{001}$	$-6^{+}_{001}$	$-6^{-}_{001}$
A'	1	1	1	1	1	1
$A^{\prime\prime}$	1	1	1	-1	-1	-1
$E'^{(a)}$	1	$\omega^*$	$\omega$	1	$\omega$	$\omega^*$
$E'^{(b)}$	1	$\omega$	$\omega^*$	1	$\omega^*$	$\omega$
$E^{\prime\prime(a)}$	1	$\omega^*$	$\omega$	-1	$-\omega$	$-\omega^*$
$E^{\prime\prime(b)}$	1	$\omega$	$\omega^*$	-1	$-\omega^*$	$-\omega$

Table 12: Parity conversion.

$\leftrightarrow$	$\leftrightarrow$	$\leftrightarrow$	$\leftrightarrow$	$\leftrightarrow$
A'(A'')	A''(A')	$E^{\prime\prime(a)}\ (E^{\prime(a)})$	$E^{\prime\prime(b)}\ (E^{\prime(b)})$	$E^{\prime(a)}\ (E^{\prime\prime(a)})$
$E'^{(b)}$ $(E''^{(b)})$	$A^{\prime\prime} (A^{\prime})$	$E^{\prime\prime\prime}(u)$ $(E^{\prime\prime}(u))$	$E^{\prime\prime\prime}(0)$ $(E^{\prime\prime}(0))$	1

Table 13: Symmetric product,  $[\Gamma \otimes \Gamma']_+$ .

	A'	$A^{\prime\prime}$	$E'^{(a)}$	$E'^{(b)}$	$E^{\prime\prime(a)}$	$E^{\prime\prime(b)}$
A'	A'	$A^{\prime\prime}$	$E'^{(a)}$	$E'^{(b)}$	$E^{\prime\prime(a)}$	$E^{\prime\prime(b)}$
$A^{\prime\prime}$		A'	$E^{\prime\prime(a)}$	$E^{\prime\prime(b)}$	$E'^{(a)}$	$E'^{(b)}$
$E'^{(a)}$			$E'^{(b)}$	A'	$E^{\prime\prime(b)}$	$A^{\prime\prime}$
$E'^{(b)}$				$E'^{(a)}$	$A^{\prime\prime}$	$E^{\prime\prime(a)}$
$E^{\prime\prime(a)}$					$E'^{(b)}$	A'
$E^{\prime\prime(b)}$						$E'^{(a)}$

Table 14: Anti-symmetric product,  $[\Gamma \otimes \Gamma]_-$ .

$\overline{A'}$	$A^{\prime\prime}$	$E'^{(a)}$	$E'^{(b)}$	$E^{\prime\prime(a)}$	$E^{\prime\prime(b)}$
	_	_	_	_	_

Table 15: Virtual-cluster sites.

No.	position	No.	position	No.	position	No.	position
1	$\begin{pmatrix} -1 & -1 & 1 \end{pmatrix}$	2	$\begin{pmatrix} 1 & 0 & 1 \end{pmatrix}$	3	$\begin{pmatrix} 0 & 1 & 1 \end{pmatrix}$	4	(-1  -1  -1)
5	$\begin{pmatrix} 0 & 1 & -1 \end{pmatrix}$	6	$\begin{pmatrix} 1 & 0 & -1 \end{pmatrix}$				

Table 16: Virtual-cluster basis.

symbol	1	2	3	4	5	6
$\mathbb{Q}_0^{(A')}$	$\frac{\sqrt{6}}{6}$	$\frac{\sqrt{6}}{6}$	$\frac{\sqrt{6}}{6}$	$\frac{\sqrt{6}}{6}$	$\frac{\sqrt{6}}{6}$	$\frac{\sqrt{6}}{6}$

Table 16

symbol	1	2	3	4	5	6
$\mathbb{Q}_1^{(A^{\prime\prime})}$	$\frac{\sqrt{6}}{6}$	$\frac{\sqrt{6}}{6}$	$\frac{\sqrt{6}}{6}$	$-\frac{\sqrt{6}}{6}$	$-\frac{\sqrt{6}}{6}$	$-\frac{\sqrt{6}}{6}$
$\mathbb{Q}_{1,0}^{(E')}$	$-\frac{\sqrt{3}}{6}$	$\frac{\sqrt{3}}{3}$	$-\frac{\sqrt{3}}{6}$	$-\frac{\sqrt{3}}{6}$	$-\frac{\sqrt{3}}{6}$	$\frac{\sqrt{3}}{3}$
$\mathbb{Q}_{1,1}^{(E')}$	$-\frac{1}{2}$	0	$\frac{1}{2}$	$-\frac{1}{2}$	$\frac{1}{2}$	0
$\mathbb{Q}_{2,0}^{(E'')}$	$-\frac{\sqrt{3}}{6}$	$\frac{\sqrt{3}}{3}$	$-\frac{\sqrt{3}}{6}$	$\frac{\sqrt{3}}{6}$	$\frac{\sqrt{3}}{6}$	$-\frac{\sqrt{3}}{3}$
$\mathbb{Q}_{2,1}^{(E^{\prime\prime})}$	$-\frac{1}{2}$	0	$\frac{1}{2}$	$\frac{1}{2}$	$-\frac{1}{2}$	0