

MSG No. 139.531 $I4/mmm$ [Type I, tetragonal]

Table 1: Wyckoff site: 2a, site symmetry: 4/mmm

| No. | position | mapping |
|-----|---|--|
| 1 | [0, 0, 0] | [1, 2, 3, 4, 5, 6, 7, 8, 9, 10, 11, 12, 13, 14, 15, 16] |
| 2 | [\frac{1}{2}, \frac{1}{2}, \frac{1}{2}] | [17, 18, 19, 20, 21, 22, 23, 24, 25, 26, 27, 28, 29, 30, 31, 32] |

Table 2: Wyckoff site: 2b, site symmetry: 4/mmm

| No. | position | mapping |
|-----|-------------------------------|--|
| 1 | [0, 0, \frac{1}{2}] | [1, 2, 3, 4, 5, 6, 7, 8, 9, 10, 11, 12, 13, 14, 15, 16] |
| 2 | [\frac{1}{2}, \frac{1}{2}, 0] | [17, 18, 19, 20, 21, 22, 23, 24, 25, 26, 27, 28, 29, 30, 31, 32] |

Table 3: Wyckoff site: 4c, site symmetry: mmm.

| No. | position | mapping |
|-----|-------------------------------|----------------------------------|
| 1 | [0, \frac{1}{2}, 0] | [1, 4, 5, 6, 9, 12, 13, 14] |
| 2 | [\frac{1}{2}, 0, 0] | [2, 3, 7, 8, 10, 11, 15, 16] |
| 3 | [\frac{1}{2}, 0, \frac{1}{2}] | [17, 20, 21, 22, 25, 28, 29, 30] |
| 4 | [0, \frac{1}{2}, \frac{1}{2}] | [18, 19, 23, 24, 26, 27, 31, 32] |

Table 4: Wyckoff site: 4d, site symmetry: -4m2

| No. | position | mapping |
|-----|-------------------------------|--------------------------------|
| 1 | [0, \frac{1}{2}, \frac{1}{4}] | [1, 6, 12, 13, 23, 24, 26, 27] |
| 2 | [\frac{1}{2}, 0, \frac{1}{4}] | [2, 3, 15, 16, 20, 21, 25, 30] |
| 3 | [0, \frac{1}{2}, \frac{3}{4}] | [4, 5, 9, 14, 18, 19, 31, 32] |
| 4 | [\frac{1}{2}, 0, \frac{3}{4}] | [7, 8, 10, 11, 17, 22, 28, 29] |

Table 5: Wyckoff site: 4e, site symmetry: 4mm

| No. | position | mapping |
|-----|---|----------------------------------|
| 1 | [0, 0, z] | [1, 2, 3, 6, 12, 13, 15, 16] |
| 2 | [0, 0, -z] | [4, 5, 7, 8, 9, 10, 11, 14] |
| 3 | [\frac{1}{2}, \frac{1}{2}, z + \frac{1}{2}] | [17, 18, 19, 22, 28, 29, 31, 32] |
| 4 | [\frac{1}{2}, \frac{1}{2}, \frac{1}{2} - z] | [20, 21, 23, 24, 25, 26, 27, 30] |

Table 6: Wyckoff site: 8f, site symmetry: $\ldots 2/\text{m}$

| No. | position | mapping |
|-----|---|-----------------|
| 1 | $[\frac{1}{4}, \frac{1}{4}, \frac{1}{4}]$ | [1, 16, 24, 25] |
| 2 | $[\frac{3}{4}, \frac{1}{4}, \frac{1}{4}]$ | [2, 12, 20, 26] |
| 3 | $[\frac{1}{4}, \frac{3}{4}, \frac{1}{4}]$ | [3, 13, 21, 27] |
| 4 | $[\frac{1}{4}, \frac{3}{4}, \frac{3}{4}]$ | [4, 10, 18, 28] |
| 5 | $[\frac{3}{4}, \frac{1}{4}, \frac{3}{4}]$ | [5, 11, 19, 29] |
| 6 | $[\frac{3}{4}, \frac{3}{4}, \frac{1}{4}]$ | [6, 15, 23, 30] |
| 7 | $[\frac{1}{4}, \frac{1}{4}, \frac{3}{4}]$ | [7, 14, 22, 31] |
| 8 | $[\frac{3}{4}, \frac{3}{4}, \frac{3}{4}]$ | [8, 9, 17, 32] |

Table 7: Wyckoff site: 8g, site symmetry: 2mm .

| No. | position | mapping |
|-----|-------------------------------------|------------------|
| 1 | $[0, \frac{1}{2}, z]$ | [1, 6, 12, 13] |
| 2 | $[\frac{1}{2}, 0, z]$ | [2, 3, 15, 16] |
| 3 | $[0, \frac{1}{2}, -z]$ | [4, 5, 9, 14] |
| 4 | $[\frac{1}{2}, 0, -z]$ | [7, 8, 10, 11] |
| 5 | $[\frac{1}{2}, 0, z + \frac{1}{2}]$ | [17, 22, 28, 29] |
| 6 | $[0, \frac{1}{2}, z + \frac{1}{2}]$ | [18, 19, 31, 32] |
| 7 | $[\frac{1}{2}, 0, \frac{1}{2} - z]$ | [20, 21, 25, 30] |
| 8 | $[0, \frac{1}{2}, \frac{1}{2} - z]$ | [23, 24, 26, 27] |

Table 8: Wyckoff site: 8h, site symmetry: $\text{m}.2\text{m}$

| No. | position | mapping |
|-----|---|------------------|
| 1 | $[x, x, 0]$ | [1, 7, 14, 16] |
| 2 | $[-x, x, 0]$ | [2, 5, 11, 12] |
| 3 | $[x, -x, 0]$ | [3, 4, 10, 13] |
| 4 | $[-x, -x, 0]$ | [6, 8, 9, 15] |
| 5 | $[x + \frac{1}{2}, x + \frac{1}{2}, \frac{1}{2}]$ | [17, 23, 30, 32] |
| 6 | $[\frac{1}{2} - x, x + \frac{1}{2}, \frac{1}{2}]$ | [18, 21, 27, 28] |
| 7 | $[x + \frac{1}{2}, \frac{1}{2} - x, \frac{1}{2}]$ | [19, 20, 26, 29] |
| 8 | $[\frac{1}{2} - x, \frac{1}{2} - x, \frac{1}{2}]$ | [22, 24, 25, 31] |

Table 9: Wyckoff site: 8i, site symmetry: $\text{m}2\text{m}$.

| No. | position | mapping |
|-----|--------------|----------------|
| 1 | $[x, 0, 0]$ | [1, 4, 13, 14] |
| 2 | $[0, x, 0]$ | [2, 7, 11, 16] |
| 3 | $[0, -x, 0]$ | [3, 8, 10, 15] |

continued ...

Table 9

| No. | position | mapping |
|-----|---|---------------|
| 4 | $[-x, 0, 0]$ | [5,6,9,12] |
| 5 | $[x + \frac{1}{2}, \frac{1}{2}, \frac{1}{2}]$ | [17,20,29,30] |
| 6 | $[\frac{1}{2}, x + \frac{1}{2}, \frac{1}{2}]$ | [18,23,27,32] |
| 7 | $[\frac{1}{2}, \frac{1}{2} - x, \frac{1}{2}]$ | [19,24,26,31] |
| 8 | $[\frac{1}{2} - x, \frac{1}{2}, \frac{1}{2}]$ | [21,22,25,28] |

Table 10: Wyckoff site: 8j, site symmetry: $m\bar{2}m$.

| No. | position | mapping |
|-----|-------------------------------------|---------------|
| 1 | $[x, \frac{1}{2}, 0]$ | [1,4,13,14] |
| 2 | $[\frac{1}{2}, x, 0]$ | [2,7,11,16] |
| 3 | $[\frac{1}{2}, -x, 0]$ | [3,8,10,15] |
| 4 | $[-x, \frac{1}{2}, 0]$ | [5,6,9,12] |
| 5 | $[x + \frac{1}{2}, 0, \frac{1}{2}]$ | [17,20,29,30] |
| 6 | $[0, x + \frac{1}{2}, \frac{1}{2}]$ | [18,23,27,32] |
| 7 | $[0, \frac{1}{2} - x, \frac{1}{2}]$ | [19,24,26,31] |
| 8 | $[\frac{1}{2} - x, 0, \frac{1}{2}]$ | [21,22,25,28] |

Table 11: Wyckoff site: 16k, site symmetry: $\dots 2$

| No. | position | mapping |
|-----|--------------------------------------|---------|
| 1 | $[x, x + \frac{1}{2}, \frac{1}{4}]$ | [1,23] |
| 2 | $[\frac{1}{2} - x, x, \frac{1}{4}]$ | [2,21] |
| 3 | $[x + \frac{1}{2}, -x, \frac{1}{4}]$ | [3,20] |
| 4 | $[x, \frac{1}{2} - x, \frac{3}{4}]$ | [4,19] |
| 5 | $[-x, x + \frac{1}{2}, \frac{3}{4}]$ | [5,18] |
| 6 | $[-x, \frac{1}{2} - x, \frac{1}{4}]$ | [6,24] |
| 7 | $[x + \frac{1}{2}, x, \frac{3}{4}]$ | [7,17] |
| 8 | $[\frac{1}{2} - x, -x, \frac{3}{4}]$ | [8,22] |
| 9 | $[-x, \frac{1}{2} - x, \frac{3}{4}]$ | [9,31] |
| 10 | $[x + \frac{1}{2}, -x, \frac{3}{4}]$ | [10,29] |
| 11 | $[\frac{1}{2} - x, x, \frac{3}{4}]$ | [11,28] |
| 12 | $[-x, x + \frac{1}{2}, \frac{1}{4}]$ | [12,27] |
| 13 | $[x, \frac{1}{2} - x, \frac{1}{4}]$ | [13,26] |
| 14 | $[x, x + \frac{1}{2}, \frac{3}{4}]$ | [14,32] |
| 15 | $[\frac{1}{2} - x, -x, \frac{1}{4}]$ | [15,25] |
| 16 | $[x + \frac{1}{2}, x, \frac{1}{4}]$ | [16,30] |

Table 12: Wyckoff site: 161, site symmetry: m..

| No. | position | mapping |
|-----|---|---------|
| 1 | $[x, y, 0]$ | [1,14] |
| 2 | $[-y, x, 0]$ | [2,11] |
| 3 | $[y, -x, 0]$ | [3,10] |
| 4 | $[x, -y, 0]$ | [4,13] |
| 5 | $[-x, y, 0]$ | [5,12] |
| 6 | $[-x, -y, 0]$ | [6,9] |
| 7 | $[y, x, 0]$ | [7,16] |
| 8 | $[-y, -x, 0]$ | [8,15] |
| 9 | $[x + \frac{1}{2}, y + \frac{1}{2}, \frac{1}{2}]$ | [17,30] |
| 10 | $[\frac{1}{2} - y, x + \frac{1}{2}, \frac{1}{2}]$ | [18,27] |
| 11 | $[y + \frac{1}{2}, \frac{1}{2} - x, \frac{1}{2}]$ | [19,26] |
| 12 | $[x + \frac{1}{2}, \frac{1}{2} - y, \frac{1}{2}]$ | [20,29] |
| 13 | $[\frac{1}{2} - x, y + \frac{1}{2}, \frac{1}{2}]$ | [21,28] |
| 14 | $[\frac{1}{2} - x, \frac{1}{2} - y, \frac{1}{2}]$ | [22,25] |
| 15 | $[y + \frac{1}{2}, x + \frac{1}{2}, \frac{1}{2}]$ | [23,32] |
| 16 | $[\frac{1}{2} - y, \frac{1}{2} - x, \frac{1}{2}]$ | [24,31] |

Table 13: Wyckoff site: 16m, site symmetry: ..m

| No. | position | mapping |
|-----|---|---------|
| 1 | $[x, x, z]$ | [1,16] |
| 2 | $[-x, x, z]$ | [2,12] |
| 3 | $[x, -x, z]$ | [3,13] |
| 4 | $[x, -x, -z]$ | [4,10] |
| 5 | $[-x, x, -z]$ | [5,11] |
| 6 | $[-x, -x, z]$ | [6,15] |
| 7 | $[x, x, -z]$ | [7,14] |
| 8 | $[-x, -x, -z]$ | [8,9] |
| 9 | $[x + \frac{1}{2}, x + \frac{1}{2}, z + \frac{1}{2}]$ | [17,32] |
| 10 | $[\frac{1}{2} - x, x + \frac{1}{2}, z + \frac{1}{2}]$ | [18,28] |
| 11 | $[x + \frac{1}{2}, \frac{1}{2} - x, z + \frac{1}{2}]$ | [19,29] |
| 12 | $[x + \frac{1}{2}, \frac{1}{2} - x, \frac{1}{2} - z]$ | [20,26] |
| 13 | $[\frac{1}{2} - x, x + \frac{1}{2}, \frac{1}{2} - z]$ | [21,27] |
| 14 | $[\frac{1}{2} - x, \frac{1}{2} - x, z + \frac{1}{2}]$ | [22,31] |
| 15 | $[x + \frac{1}{2}, x + \frac{1}{2}, \frac{1}{2} - z]$ | [23,30] |
| 16 | $[\frac{1}{2} - x, \frac{1}{2} - x, \frac{1}{2} - z]$ | [24,25] |

Table 14: Wyckoff site: 16n, site symmetry: ..m..

| No. | position | mapping |
|-----|-------------|---------|
| 1 | $[0, y, z]$ | [1,12] |

continued ...

Table 14

| No. | position | mapping |
|-----|---|---------|
| 2 | $[-y, 0, z]$ | [2,15] |
| 3 | $[y, 0, z]$ | [3,16] |
| 4 | $[0, -y, -z]$ | [4,9] |
| 5 | $[0, y, -z]$ | [5,14] |
| 6 | $[0, -y, z]$ | [6,13] |
| 7 | $[y, 0, -z]$ | [7,10] |
| 8 | $[-y, 0, -z]$ | [8,11] |
| 9 | $[\frac{1}{2}, y + \frac{1}{2}, z + \frac{1}{2}]$ | [17,28] |
| 10 | $[\frac{1}{2} - y, \frac{1}{2}, z + \frac{1}{2}]$ | [18,31] |
| 11 | $[y + \frac{1}{2}, \frac{1}{2}, z + \frac{1}{2}]$ | [19,32] |
| 12 | $[\frac{1}{2}, \frac{1}{2} - y, \frac{1}{2} - z]$ | [20,25] |
| 13 | $[\frac{1}{2}, y + \frac{1}{2}, \frac{1}{2} - z]$ | [21,30] |
| 14 | $[\frac{1}{2}, \frac{1}{2} - y, z + \frac{1}{2}]$ | [22,29] |
| 15 | $[y + \frac{1}{2}, \frac{1}{2}, \frac{1}{2} - z]$ | [23,26] |
| 16 | $[\frac{1}{2} - y, \frac{1}{2}, \frac{1}{2} - z]$ | [24,27] |

Table 15: Wyckoff site: 32o, site symmetry: 1

| No. | position | mapping |
|-----|---|---------|
| 1 | $[x, y, z]$ | [1] |
| 2 | $[-y, x, z]$ | [2] |
| 3 | $[y, -x, z]$ | [3] |
| 4 | $[x, -y, -z]$ | [4] |
| 5 | $[-x, y, -z]$ | [5] |
| 6 | $[-x, -y, z]$ | [6] |
| 7 | $[y, x, -z]$ | [7] |
| 8 | $[-y, -x, -z]$ | [8] |
| 9 | $[-x, -y, -z]$ | [9] |
| 10 | $[y, -x, -z]$ | [10] |
| 11 | $[-y, x, -z]$ | [11] |
| 12 | $[-x, y, z]$ | [12] |
| 13 | $[x, -y, z]$ | [13] |
| 14 | $[x, y, -z]$ | [14] |
| 15 | $[-y, -x, z]$ | [15] |
| 16 | $[y, x, z]$ | [16] |
| 17 | $[x + \frac{1}{2}, y + \frac{1}{2}, z + \frac{1}{2}]$ | [17] |
| 18 | $[\frac{1}{2} - y, x + \frac{1}{2}, z + \frac{1}{2}]$ | [18] |
| 19 | $[y + \frac{1}{2}, \frac{1}{2} - x, z + \frac{1}{2}]$ | [19] |
| 20 | $[x + \frac{1}{2}, \frac{1}{2} - y, \frac{1}{2} - z]$ | [20] |
| 21 | $[\frac{1}{2} - x, y + \frac{1}{2}, \frac{1}{2} - z]$ | [21] |
| 22 | $[\frac{1}{2} - x, \frac{1}{2} - y, z + \frac{1}{2}]$ | [22] |
| 23 | $[y + \frac{1}{2}, x + \frac{1}{2}, \frac{1}{2} - z]$ | [23] |
| 24 | $[\frac{1}{2} - y, \frac{1}{2} - x, \frac{1}{2} - z]$ | [24] |
| 25 | $[\frac{1}{2} - x, \frac{1}{2} - y, \frac{1}{2} - z]$ | [25] |

continued ...

Table 15

| No. | position | mapping |
|-----|---|---------|
| 26 | $[y + \frac{1}{2}, \frac{1}{2} - x, \frac{1}{2} - z]$ | [26] |
| 27 | $[\frac{1}{2} - y, x + \frac{1}{2}, \frac{1}{2} - z]$ | [27] |
| 28 | $[\frac{1}{2} - x, y + \frac{1}{2}, z + \frac{1}{2}]$ | [28] |
| 29 | $[x + \frac{1}{2}, \frac{1}{2} - y, z + \frac{1}{2}]$ | [29] |
| 30 | $[x + \frac{1}{2}, y + \frac{1}{2}, \frac{1}{2} - z]$ | [30] |
| 31 | $[\frac{1}{2} - y, \frac{1}{2} - x, z + \frac{1}{2}]$ | [31] |
| 32 | $[y + \frac{1}{2}, x + \frac{1}{2}, z + \frac{1}{2}]$ | [32] |