

SG No. 128  $D_{4h}^6$   $P4/mnc$  [ tetragonal ]

\* generator :  $\{2_{001}|0\}$ ,  $\{4_{001}^+|0\}$ ,  $\{2_{010}|\frac{1}{2}\frac{1}{2}\frac{1}{2}\}$ ,  $\{-1|0\}$

\* symmetry operation + [0, 0, 0]

Table 1: Symmetry operations for 3d polar vector.

| No. | tag  | matrix (polar)   | det |
|-----|--|--|-----|
| 1   | $\{1 0\}$  | $\begin{bmatrix} 1 & 0 & 0 & 0 \\ 0 & 1 & 0 & 0 \\ 0 & 0 & 1 & 0 \end{bmatrix}$                                  | 1   |
| 2   | $\{2_{001} 0\}$  | $\begin{bmatrix} -1 & 0 & 0 & 0 \\ 0 & -1 & 0 & 0 \\ 0 & 0 & 1 & 0 \end{bmatrix}$                                | 1   |
| 3   | $\{4_{001}^+ 0\}$                                      | $\begin{bmatrix} 0 & -1 & 0 & 0 \\ 1 & 0 & 0 & 0 \\ 0 & 0 & 1 & 0 \end{bmatrix}$                                 | 1   |
| 4   | $\{4_{001}^- 0\}$                                      | $\begin{bmatrix} 0 & 1 & 0 & 0 \\ -1 & 0 & 0 & 0 \\ 0 & 0 & 1 & 0 \end{bmatrix}$                                 | 1   |
| 5   | $\{2_{010} \frac{1}{2}\frac{1}{2}\frac{1}{2}\}$        | $\begin{bmatrix} -1 & 0 & 0 & \frac{1}{2} \\ 0 & 1 & 0 & \frac{1}{2} \\ 0 & 0 & -1 & \frac{1}{2} \end{bmatrix}$  | 1   |
| 6   | $\{2_{100} \frac{1}{2}\frac{1}{2}\frac{1}{2}\}$        | $\begin{bmatrix} 1 & 0 & 0 & \frac{1}{2} \\ 0 & -1 & 0 & \frac{1}{2} \\ 0 & 0 & -1 & \frac{1}{2} \end{bmatrix}$  | 1   |
| 7   | $\{2_{110} \frac{1}{2}\frac{1}{2}\frac{1}{2}\}$        | $\begin{bmatrix} 0 & 1 & 0 & \frac{1}{2} \\ 1 & 0 & 0 & \frac{1}{2} \\ 0 & 0 & -1 & \frac{1}{2} \end{bmatrix}$   | 1   |
| 8   | $\{2_{1-10} \frac{1}{2}\frac{1}{2}\frac{1}{2}\}$       | $\begin{bmatrix} 0 & -1 & 0 & \frac{1}{2} \\ -1 & 0 & 0 & \frac{1}{2} \\ 0 & 0 & -1 & \frac{1}{2} \end{bmatrix}$ | 1   |
| 9   | $\{-1 0\}$   | $\begin{bmatrix} -1 & 0 & 0 & 0 \\ 0 & -1 & 0 & 0 \\ 0 & 0 & -1 & 0 \end{bmatrix}$                               | -1  |
| 10  | $\{\text{m}_{001} 0\}$                                 | $\begin{bmatrix} 1 & 0 & 0 & 0 \\ 0 & 1 & 0 & 0 \\ 0 & 0 & -1 & 0 \end{bmatrix}$                                 | -1  |
| 11  | $\{-4_{001}^+ 0\}$                                     | $\begin{bmatrix} 0 & 1 & 0 & 0 \\ -1 & 0 & 0 & 0 \\ 0 & 0 & -1 & 0 \end{bmatrix}$                                | -1  |
| 12  | $\{-4_{001}^- 0\}$                                     | $\begin{bmatrix} 0 & -1 & 0 & 0 \\ 1 & 0 & 0 & 0 \\ 0 & 0 & -1 & 0 \end{bmatrix}$                                | -1  |
| 13  | $\{\text{m}_{010} \frac{1}{2}\frac{1}{2}\frac{1}{2}\}$ | $\begin{bmatrix} 1 & 0 & 0 & \frac{1}{2} \\ 0 & -1 & 0 & \frac{1}{2} \\ 0 & 0 & 1 & \frac{1}{2} \end{bmatrix}$   | -1  |

*continued ...*

Table 1

| No. | tag  | matrix (polar)  | det |
|-----|--|---|-----|
| 14  | $\{m_{100}   \frac{1}{2} \frac{1}{2} \frac{1}{2}\}$  | $\begin{bmatrix} -1 & 0 & 0 & \frac{1}{2} \\ 0 & 1 & 0 & \frac{1}{2} \\ 0 & 0 & 1 & \frac{1}{2} \end{bmatrix}$  | -1  |
| 15  | $\{m_{110}   \frac{1}{2} \frac{1}{2} \frac{1}{2}\}$  | $\begin{bmatrix} 0 & -1 & 0 & \frac{1}{2} \\ -1 & 0 & 0 & \frac{1}{2} \\ 0 & 0 & 1 & \frac{1}{2} \end{bmatrix}$ | -1  |
| 16  | $\{m_{1-10}   \frac{1}{2} \frac{1}{2} \frac{1}{2}\}$ | $\begin{bmatrix} 0 & 1 & 0 & \frac{1}{2} \\ 1 & 0 & 0 & \frac{1}{2} \\ 0 & 0 & 1 & \frac{1}{2} \end{bmatrix}$   | -1  |