

PG No. 2 C_1 $\bar{1}$ [triclinic] (polar, internal axial dipole)

* Harmonics for rank 0

* Harmonics for rank 1

$$\bar{Q}_1^{(1,0)}[g](A_u, 1)$$

** symmetry

$$x$$

** expression

$$\frac{\sqrt{2}G_y z}{2} - \frac{\sqrt{2}G_z y}{2}$$

$$\bar{Q}_1^{(1,0)}[g](A_u, 2)$$

** symmetry

$$y$$

** expression

$$-\frac{\sqrt{2}G_x z}{2} + \frac{\sqrt{2}G_z x}{2}$$

$$\bar{Q}_1^{(1,0)}[g](A_u, 3)$$

** symmetry

$$z$$

** expression

$$\frac{\sqrt{2}G_x y}{2} - \frac{\sqrt{2}G_y x}{2}$$

* Harmonics for rank 2

$$\bar{Q}_2^{(1,0)}[g](A_g, 1)$$

** symmetry

$$-\frac{x^2}{2} - \frac{y^2}{2} + z^2$$

** expression

$$\frac{\sqrt{6}G_x y z}{2} - \frac{\sqrt{6}G_y x z}{2}$$

$$\bar{Q}_2^{(1,0)}[g](A_g, 2)$$

** symmetry

$$\frac{\sqrt{3}(x-y)(x+y)}{2}$$

** expression

$$\frac{\sqrt{2}G_x y z}{2} + \frac{\sqrt{2}G_y x z}{2} - \sqrt{2}G_z x y$$

$$\bar{Q}_2^{(1,0)}[g](A_g, 3)$$

** symmetry

$$\sqrt{3}y z$$

** expression

$$\frac{\sqrt{2}G_x (y-z)(y+z)}{2} - \frac{\sqrt{2}G_y x y}{2} + \frac{\sqrt{2}G_z x z}{2}$$

$$\bar{Q}_2^{(1,0)}[g](A_g, 4)$$

** symmetry

$$\sqrt{3}x z$$

** expression

$$\frac{\sqrt{2}G_x x y}{2} - \frac{\sqrt{2}G_y (x-z)(x+z)}{2} - \frac{\sqrt{2}G_z y z}{2}$$

$$\bar{Q}_2^{(1,0)}[g](A_g, 5)$$

** symmetry

$$\sqrt{3}x y$$

** expression

$$-\frac{\sqrt{2}G_{xx}z}{2} + \frac{\sqrt{2}G_{yy}z}{2} + \frac{\sqrt{2}G_z(x-y)(x+y)}{2}$$

* Harmonics for rank 3

$$\tilde{\mathbb{Q}}_3^{(1,0)}[g](A_u, 1)$$

** symmetry

$$\sqrt{15}xyz$$

** expression

$$\frac{\sqrt{5}G_{xx}(y-z)(y+z)}{2} - \frac{\sqrt{5}G_{yy}(x-z)(x+z)}{2} + \frac{\sqrt{5}G_z(x-y)(x+y)}{2}$$

$$\tilde{\mathbb{Q}}_3^{(1,0)}[g](A_u, 2)$$

** symmetry

$$\frac{x(2x^2 - 3y^2 - 3z^2)}{2}$$

** expression

$$\frac{\sqrt{3}G_{yz}(4x^2 - y^2 - z^2)}{4} - \frac{\sqrt{3}G_{zy}(4x^2 - y^2 - z^2)}{4}$$

$$\tilde{\mathbb{Q}}_3^{(1,0)}[g](A_u, 3)$$

** symmetry

$$-\frac{y(3x^2 - 2y^2 + 3z^2)}{2}$$

** expression

$$\frac{\sqrt{3}G_{xz}(x^2 - 4y^2 + z^2)}{4} - \frac{\sqrt{3}G_{zx}(x^2 - 4y^2 + z^2)}{4}$$

$$\tilde{\mathbb{Q}}_3^{(1,0)}[g](A_u, 4)$$

** symmetry

$$-\frac{z(3x^2 + 3y^2 - 2z^2)}{2}$$

** expression

$$-\frac{\sqrt{3}G_{xy}(x^2 + y^2 - 4z^2)}{4} + \frac{\sqrt{3}G_{yx}(x^2 + y^2 - 4z^2)}{4}$$

$$\tilde{\mathbb{Q}}_3^{(1,0)}[g](A_u, 5)$$

** symmetry

$$\frac{\sqrt{15}x(y-z)(y+z)}{2}$$

** expression

$$-\sqrt{5}G_{xx}yz + \frac{\sqrt{5}G_{yz}(2x^2 + y^2 - z^2)}{4} + \frac{\sqrt{5}G_{zy}(2x^2 - y^2 + z^2)}{4}$$

$$\tilde{\mathbb{Q}}_3^{(1,0)}[g](A_u, 6)$$

** symmetry

$$-\frac{\sqrt{15}y(x-z)(x+z)}{2}$$

** expression

$$\frac{\sqrt{5}G_{xz}(x^2 + 2y^2 - z^2)}{4} - \sqrt{5}G_{yx}yz - \frac{\sqrt{5}G_{zx}(x^2 - 2y^2 - z^2)}{4}$$

$$\tilde{\mathbb{Q}}_3^{(1,0)}[g](A_u, 7)$$

** symmetry

$$\frac{\sqrt{15}z(x-y)(x+y)}{2}$$

** expression

$$\frac{\sqrt{5}G_{xy}(x^2 - y^2 + 2z^2)}{4} - \frac{\sqrt{5}G_{yx}(x^2 - y^2 - 2z^2)}{4} - \sqrt{5}G_{zxyz}$$

* Harmonics for rank 4

$$\bar{\mathbb{Q}}_4^{(1,0)}[g](A_g, 1)$$

** symmetry

$$\frac{\sqrt{21} (x^4 - 3x^2y^2 - 3x^2z^2 + y^4 - 3y^2z^2 + z^4)}{6}$$

** expression

$$-\frac{\sqrt{105}G_x yz (y-z)(y+z)}{6} + \frac{\sqrt{105}G_y xz (x-z)(x+z)}{6} - \frac{\sqrt{105}G_z xy (x-y)(x+y)}{6}$$

$$\bar{\mathbb{Q}}_4^{(1,0)}[g](A_g, 2)$$

** symmetry

$$-\frac{\sqrt{15} (x^4 - 12x^2y^2 + 6x^2z^2 + y^4 + 6y^2z^2 - 2z^4)}{12}$$

** expression

$$-\frac{\sqrt{3}G_x yz (9x^2 + 2y^2 - 5z^2)}{6} + \frac{\sqrt{3}G_y xz (2x^2 + 9y^2 - 5z^2)}{6} + \frac{7\sqrt{3}G_z xy (x-y)(x+y)}{6}$$

$$\bar{\mathbb{Q}}_4^{(1,0)}[g](A_g, 3)$$

** symmetry

$$\frac{\sqrt{5} (x-y)(x+y)(x^2 + y^2 - 6z^2)}{4}$$

** expression

$$-\frac{G_x yz (3x^2 - 4y^2 + 3z^2)}{2} + \frac{G_y xz (4x^2 - 3y^2 - 3z^2)}{2} - \frac{G_z xy (x^2 + y^2 - 6z^2)}{2}$$

$$\bar{\mathbb{Q}}_4^{(1,0)}[g](A_g, 4)$$

** symmetry

$$\frac{\sqrt{35} yz (y-z)(y+z)}{2}$$

** expression

$$\frac{\sqrt{7}G_x (y^2 - 2yz - z^2)(y^2 + 2yz - z^2)}{4} - \frac{\sqrt{7}G_y xy (y^2 - 3z^2)}{4} + \frac{\sqrt{7}G_z xz (3y^2 - z^2)}{4}$$

$$\bar{\mathbb{Q}}_4^{(1,0)}[g](A_g, 5)$$

** symmetry

$$-\frac{\sqrt{35} xz (x-z)(x+z)}{2}$$

** expression

$$-\frac{\sqrt{7}G_x xy (x^2 - 3z^2)}{4} + \frac{\sqrt{7}G_y (x^2 - 2xz - z^2)(x^2 + 2xz - z^2)}{4} + \frac{\sqrt{7}G_z yz (3x^2 - z^2)}{4}$$

$$\bar{\mathbb{Q}}_4^{(1,0)}[g](A_g, 6)$$

** symmetry

$$\frac{\sqrt{35} xy (x-y)(x+y)}{2}$$

** expression

$$-\frac{\sqrt{7}G_x xz (x^2 - 3y^2)}{4} + \frac{\sqrt{7}G_y yz (3x^2 - y^2)}{4} + \frac{\sqrt{7}G_z (x^2 - 2xy - y^2)(x^2 + 2xy - y^2)}{4}$$

$$\bar{\mathbb{Q}}_4^{(1,0)}[g](A_g, 7)$$

** symmetry

$$\frac{\sqrt{5} yz (6x^2 - y^2 - z^2)}{2}$$

** expression

$$\frac{G_x (y-z)(y+z)(6x^2 - y^2 - z^2)}{4} - \frac{G_y xy (6x^2 - y^2 - 15z^2)}{4} + \frac{G_z xz (6x^2 - 15y^2 - z^2)}{4}$$

$$\bar{\mathbb{Q}}_4^{(1,0)}[g](A_g, 8)$$

** symmetry

$$-\frac{\sqrt{5} xz (x^2 - 6y^2 + z^2)}{2}$$

** expression

$$-\frac{G_xxy\left(x^2-6y^2+15z^2\right)}{4}+\frac{G_y\left(x-z\right)\left(x+z\right)\left(x^2-6y^2+z^2\right)}{4}+\frac{G_zyz\left(15x^2-6y^2+z^2\right)}{4}$$

$$\vec{\mathbb{Q}}_4^{(1,0)}[g](A_g,9)$$

** symmetry

$$-\frac{\sqrt{5}xy\left(x^2+y^2-6z^2\right)}{2}$$

** expression

$$\frac{G_xxz\left(x^2+15y^2-6z^2\right)}{4}-\frac{G_yyz\left(15x^2+y^2-6z^2\right)}{4}-\frac{G_z\left(x-y\right)\left(x+y\right)\left(x^2+y^2-6z^2\right)}{4}$$