

MSG No. 162.73  $P\bar{3}1m$  [ Type I, trigonal ]

\* symmetry operation

Table 1: Symmetry operations for 3d polar vector.

| No. | tag                                 | matrix (polar)   | det | TR |
|-----|-------------------------------------|--|-----|----|
| 1   | {1 0}                               | $\begin{bmatrix} 1 & 0 & 0 & 0 \\ 0 & 1 & 0 & 0 \\ 0 & 0 & 1 & 0 \end{bmatrix}$    | 1   | 1  |
| 2   | {3 <sup>+</sup> <sub>001</sub>  0}  | $\begin{bmatrix} 0 & -1 & 0 & 0 \\ 1 & -1 & 0 & 0 \\ 0 & 0 & 1 & 0 \end{bmatrix}$  | 1   | 1  |
| 3   | {3 <sup>-</sup> <sub>001</sub>  0}  | $\begin{bmatrix} -1 & 1 & 0 & 0 \\ -1 & 0 & 0 & 0 \\ 0 & 0 & 1 & 0 \end{bmatrix}$  | 1   | 1  |
| 4   | {2 <sub>210</sub>  0}               | $\begin{bmatrix} 1 & 0 & 0 & 0 \\ 1 & -1 & 0 & 0 \\ 0 & 0 & -1 & 0 \end{bmatrix}$  | 1   | 1  |
| 5   | {2 <sub>120</sub>  0}               | $\begin{bmatrix} -1 & 1 & 0 & 0 \\ 0 & 1 & 0 & 0 \\ 0 & 0 & -1 & 0 \end{bmatrix}$  | 1   | 1  |
| 6   | {2 <sub>1-10</sub>  0}              | $\begin{bmatrix} 0 & -1 & 0 & 0 \\ -1 & 0 & 0 & 0 \\ 0 & 0 & -1 & 0 \end{bmatrix}$ | 1   | 1  |
| 7   | {-1 0}                              | $\begin{bmatrix} -1 & 0 & 0 & 0 \\ 0 & -1 & 0 & 0 \\ 0 & 0 & -1 & 0 \end{bmatrix}$ | -1  | 1  |
| 8   | {-3 <sup>+</sup> <sub>001</sub>  0} | $\begin{bmatrix} 0 & 1 & 0 & 0 \\ -1 & 1 & 0 & 0 \\ 0 & 0 & -1 & 0 \end{bmatrix}$  | -1  | 1  |
| 9   | {-3 <sup>-</sup> <sub>001</sub>  0} | $\begin{bmatrix} 1 & -1 & 0 & 0 \\ 1 & 0 & 0 & 0 \\ 0 & 0 & -1 & 0 \end{bmatrix}$  | -1  | 1  |
| 10  | {m <sub>210</sub>  0}               | $\begin{bmatrix} -1 & 0 & 0 & 0 \\ -1 & 1 & 0 & 0 \\ 0 & 0 & 1 & 0 \end{bmatrix}$  | -1  | 1  |
| 11  | {m <sub>120</sub>  0}               | $\begin{bmatrix} 1 & -1 & 0 & 0 \\ 0 & -1 & 0 & 0 \\ 0 & 0 & 1 & 0 \end{bmatrix}$  | -1  | 1  |
| 12  | {m <sub>1-10</sub>  0}              | $\begin{bmatrix} 0 & 1 & 0 & 0 \\ 1 & 0 & 0 & 0 \\ 0 & 0 & 1 & 0 \end{bmatrix}$    | -1  | 1  |