SAMB for "SnTe"

- Group: No. 31 C_{2v}^{7} $Pmn2_1$ [orthorhombic]
- Associated point group: No. 7 C_{2v} $mm2$ [orthorhombic]

- Generation condition
    - model type: `tight_binding`
    - time-reversal type: `electric`
    - irrep: `[A1]`
    - `spinful`

- Unit cell:
    $a = 4.559,\ b = 6.0,\ c = 4.57,\ \alpha = 90.0,\ \beta = 90.0,\ \gamma = 90.0$
- Lattice vectors:
    $\boldsymbol{a}_1 = \begin{pmatrix} 4.559 & 0 & 0 \end{pmatrix}$
    $\boldsymbol{a}_2 = \begin{pmatrix} 0 & 6.0 & 0 \end{pmatrix}$
    $\boldsymbol{a}_3 = \begin{pmatrix} 0 & 0 & 4.57 \end{pmatrix}$

Table 1: High-symmetry line: Γ-X.

symbol	position	symbol	position
Γ	$\begin{pmatrix} 0 & 0 & 0 \end{pmatrix}$	X	$\begin{pmatrix} \frac{1}{2} & 0 & 0 \end{pmatrix}$

- Kets: dimension = 24

Table 2: Hilbert space for full matrix.

No.	ket	No.	ket	No.	ket	No.	ket	No.	ket
1	$(p_x,\uparrow)$@Sn_1	2	$(p_x,\downarrow)$@Sn_1	3	$(p_y,\uparrow)$@Sn_1	4	$(p_y,\downarrow)$@Sn_1	5	$(p_z,\uparrow)$@Sn_1
6	$(p_z,\downarrow)$@Sn_1	7	$(p_x,\uparrow)$@Sn_2	8	$(p_x,\downarrow)$@Sn_2	9	$(p_y,\uparrow)$@Sn_2	10	$(p_y,\downarrow)$@Sn_2
11	$(p_z,\uparrow)$@Sn_2	12	$(p_z,\downarrow)$@Sn_2	13	$(p_x,\uparrow)$@Te_1	14	$(p_x,\downarrow)$@Te_1	15	$(p_y,\uparrow)$@Te_1
16	$(p_y,\downarrow)$@Te_1	17	$(p_z,\uparrow)$@Te_1	18	$(p_z,\downarrow)$@Te_1	19	$(p_x,\uparrow)$@Te_2	20	$(p_x,\downarrow)$@Te_2
21	$(p_y,\uparrow)$@Te_2	22	$(p_y,\downarrow)$@Te_2	23	$(p_z,\uparrow)$@Te_2	24	$(p_z,\downarrow)$@Te_2		

- Sites in (primitive) unit cell:

Table 3: Site-clusters.

	site	position	mapping
S_1 [2a: m..]	Sn_1	$\begin{pmatrix} \frac{1}{2} & \frac{3}{5} & \frac{3}{5} \end{pmatrix}$	[1,4]
	Sn_2	$\begin{pmatrix} 0 & \frac{2}{5} & \frac{1}{10} \end{pmatrix}$	[2,3]
S_2 [2a: m..]	Te_1	$\begin{pmatrix} \frac{1}{2} & \frac{7}{20} & \frac{2}{5} \end{pmatrix}$	[1,4]
	Te_2	$\begin{pmatrix} 0 & \frac{13}{20} & \frac{9}{10} \end{pmatrix}$	[2,3]

- Bonds in (primitive) unit cell:

Table 4: Bond-clusters.

	bond	tail	head	n	#	$\boldsymbol{b}$@$\boldsymbol{c}$	mapping
B_1 [2a: m..]	b_1	Te_1	Sn_1	1	1	$\begin{pmatrix} 0 & -\frac{1}{4} & -\frac{1}{5} \end{pmatrix}$@$\begin{pmatrix} \frac{1}{2} & \frac{19}{40} & \frac{1}{2} \end{pmatrix}$	[1,4]
	b_2	Te_2	Sn_2	1	1	$\begin{pmatrix} 0 & \frac{1}{4} & -\frac{1}{5} \end{pmatrix}$@$\begin{pmatrix} 0 & \frac{21}{40} & 0 \end{pmatrix}$	[2,3]
B_2 [4b: 1]	b_3	Te_2	Sn_1	2	1	$\begin{pmatrix} -\frac{1}{2} & \frac{1}{20} & \frac{3}{10} \end{pmatrix}$@$\begin{pmatrix} \frac{1}{4} & \frac{5}{8} & \frac{3}{4} \end{pmatrix}$	[1]
	b_4	Te_1	Sn_2	2	1	$\begin{pmatrix} \frac{1}{2} & -\frac{1}{20} & \frac{3}{10} \end{pmatrix}$@$\begin{pmatrix} \frac{1}{4} & \frac{3}{8} & \frac{1}{4} \end{pmatrix}$	[2]
	b_5	Te_1	Sn_2	2	1	$\begin{pmatrix} -\frac{1}{2} & -\frac{1}{20} & \frac{3}{10} \end{pmatrix}$@$\begin{pmatrix} \frac{3}{4} & \frac{3}{8} & \frac{1}{4} \end{pmatrix}$	[3]

continued …

Table 4

	bond	tail	head	n	#	$\boldsymbol{b}@\boldsymbol{c}$		mapping
	b_6	Te_2	Sn_1	2	1	$\left(\frac{1}{2} \quad \frac{1}{20} \quad \frac{3}{10}\right)$ @ $\left(\frac{3}{4} \quad \frac{5}{8} \quad \frac{3}{4}\right)$		[4]
B_3 [4b: 1]	b_7	Sn_2	Sn_1	1	1	$\left(-\frac{1}{2} \quad -\frac{1}{5} \quad -\frac{1}{2}\right)$ @ $\left(\frac{1}{4} \quad \frac{1}{2} \quad \frac{7}{20}\right)$		[1]
	b_8	Sn_2	Sn_1	1	1	$\left(-\frac{1}{2} \quad -\frac{1}{5} \quad \frac{1}{2}\right)$ @ $\left(\frac{1}{4} \quad \frac{1}{2} \quad \frac{17}{20}\right)$		[-2]
	b_9	Sn_2	Sn_1	1	1	$\left(\frac{1}{2} \quad -\frac{1}{5} \quad \frac{1}{2}\right)$ @ $\left(\frac{3}{4} \quad \frac{1}{2} \quad \frac{17}{20}\right)$		[-3]
	b_{10}	Sn_2	Sn_1	1	1	$\left(\frac{1}{2} \quad -\frac{1}{5} \quad -\frac{1}{2}\right)$ @ $\left(\frac{3}{4} \quad \frac{1}{2} \quad \frac{7}{20}\right)$		[4]
B_4 [4b: 1]	b_{11}	Te_2	Te_1	1	1	$\left(-\frac{1}{2} \quad \frac{3}{10} \quad -\frac{1}{2}\right)$ @ $\left(\frac{1}{4} \quad \frac{1}{2} \quad \frac{3}{20}\right)$		[1]
	b_{12}	Te_2	Te_1	1	1	$\left(-\frac{1}{2} \quad \frac{3}{10} \quad \frac{1}{2}\right)$ @ $\left(\frac{1}{4} \quad \frac{1}{2} \quad \frac{13}{20}\right)$		[-2]
	b_{13}	Te_2	Te_1	1	1	$\left(\frac{1}{2} \quad \frac{3}{10} \quad \frac{1}{2}\right)$ @ $\left(\frac{3}{4} \quad \frac{1}{2} \quad \frac{13}{20}\right)$		[-3]
	b_{14}	Te_2	Te_1	1	1	$\left(\frac{1}{2} \quad \frac{3}{10} \quad -\frac{1}{2}\right)$ @ $\left(\frac{3}{4} \quad \frac{1}{2} \quad \frac{3}{20}\right)$		[4]

- SAMB:

No. 1 $\hat{\mathbb{Q}}_0^{(A_1)}$ $[M_1, S_1]$

$\hat{\mathbb{Z}}_1 = \mathbb{X}_1[\mathbb{Q}_0^{(a,A_1)}] \otimes \mathbb{Y}_1[\mathbb{Q}_0^{(s,A_1)}]$

No. 2 $\hat{\mathbb{Q}}_2^{(A_1,1)}$ $[M_1, S_1]$

$\hat{\mathbb{Z}}_2 = \mathbb{X}_2[\mathbb{Q}_2^{(a,A_1,1)}] \otimes \mathbb{Y}_1[\mathbb{Q}_0^{(s,A_1)}]$

No. 3 $\hat{\mathbb{Q}}_2^{(A_1,2)}$ $[M_1, S_1]$

$\hat{\mathbb{Z}}_3 = \mathbb{X}_3[\mathbb{Q}_2^{(a,A_1,2)}] \otimes \mathbb{Y}_1[\mathbb{Q}_0^{(s,A_1)}]$

No. 4 $\hat{\mathbb{Q}}_1^{(A_1)}$ $[M_1, S_1]$

$\hat{\mathbb{Z}}_4 = \mathbb{X}_9[\mathbb{Q}_2^{(a,B_2)}] \otimes \mathbb{Y}_2[\mathbb{Q}_1^{(s,B_2)}]$

No. 5 $\hat{\mathbb{Q}}_0^{(A_1)}(1,1)$ $[M_1, S_1]$

$\hat{\mathbb{Z}}_5 = \mathbb{X}_4[\mathbb{Q}_0^{(a,A_1)}(1,1)] \otimes \mathbb{Y}_1[\mathbb{Q}_0^{(s,A_1)}]$

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No. 6 $\hat{\mathbb{Q}}_2^{(A_1,1)}(1,-1)$ $[\mathrm{M}_1,\mathrm{S}_1]$

$\hat{\mathbb{Z}}_6 = \mathbb{X}_5[\mathbb{Q}_2^{(a,A_1,1)}(1,-1)] \otimes \mathbb{Y}_1[\mathbb{Q}_0^{(s,A_1)}]$

No. 7 $\hat{\mathbb{Q}}_2^{(A_1,2)}(1,-1)$ $[\mathrm{M}_1,\mathrm{S}_1]$

$\hat{\mathbb{Z}}_7 = \mathbb{X}_6[\mathbb{Q}_2^{(a,A_1,2)}(1,-1)] \otimes \mathbb{Y}_1[\mathbb{Q}_0^{(s,A_1)}]$

No. 8 $\hat{\mathbb{Q}}_1^{(A_1)}(1,-1)$ $[\mathrm{M}_1,\mathrm{S}_1]$

$\hat{\mathbb{Z}}_8 = \mathbb{X}_{14}[\mathbb{Q}_2^{(a,B_2)}(1,-1)] \otimes \mathbb{Y}_2[\mathbb{Q}_1^{(s,B_2)}]$

No. 9 $\hat{\mathbb{Q}}_1^{(A_1)}(1,0)$ $[\mathrm{M}_1,\mathrm{S}_1]$

$\hat{\mathbb{Z}}_9 = \mathbb{X}_{15}[\mathbb{G}_1^{(a,B_2)}(1,0)] \otimes \mathbb{Y}_2[\mathbb{Q}_1^{(s,B_2)}]$

No. 10 $\hat{\mathbb{Q}}_0^{(A_1)}$ $[\mathrm{M}_1,\mathrm{S}_2]$

$\hat{\mathbb{Z}}_{10} = \mathbb{X}_1[\mathbb{Q}_0^{(a,A_1)}] \otimes \mathbb{Y}_3[\mathbb{Q}_0^{(s,A_1)}]$

No. 11 $\hat{\mathbb{Q}}_2^{(A_1,1)}$ $[\mathrm{M}_1,\mathrm{S}_2]$

$\hat{\mathbb{Z}}_{11} = \mathbb{X}_2[\mathbb{Q}_2^{(a,A_1,1)}] \otimes \mathbb{Y}_3[\mathbb{Q}_0^{(s,A_1)}]$

No. 12 $\hat{\mathbb{Q}}_2^{(A_1,2)}$ $[\mathrm{M}_1,\mathrm{S}_2]$

$\hat{\mathbb{Z}}_{12} = \mathbb{X}_3[\mathbb{Q}_2^{(a,A_1,2)}] \otimes \mathbb{Y}_3[\mathbb{Q}_0^{(s,A_1)}]$

No. 13 $\hat{\mathbb{Q}}_1^{(A_1)}$ $[\mathrm{M}_1,\mathrm{S}_2]$

$\hat{\mathbb{Z}}_{13} = \mathbb{X}_9[\mathbb{Q}_2^{(a,B_2)}] \otimes \mathbb{Y}_4[\mathbb{Q}_1^{(s,B_2)}]$

No. 14 $\hat{\mathbb{Q}}_0^{(A_1)}(1,1)$ $[\mathrm{M}_1,\mathrm{S}_2]$

$\hat{\mathbb{Z}}_{14} = \mathbb{X}_4[\mathbb{Q}_0^{(a,A_1)}(1,1)] \otimes \mathbb{Y}_3[\mathbb{Q}_0^{(s,A_1)}]$

No. 15 $\hat{\mathbb{Q}}_2^{(A_1,1)}(1,-1)$ $[M_1, S_2]$

$$\hat{\mathbb{Z}}_{15} = \mathbb{X}_5[\mathbb{Q}_2^{(a,A_1,1)}(1,-1)] \otimes \mathbb{Y}_3[\mathbb{Q}_0^{(s,A_1)}]$$

No. 16 $\hat{\mathbb{Q}}_2^{(A_1,2)}(1,-1)$ $[M_1, S_2]$

$$\hat{\mathbb{Z}}_{16} = \mathbb{X}_6[\mathbb{Q}_2^{(a,A_1,2)}(1,-1)] \otimes \mathbb{Y}_3[\mathbb{Q}_0^{(s,A_1)}]$$

No. 17 $\hat{\mathbb{Q}}_1^{(A_1)}(1,-1)$ $[M_1, S_2]$

$$\hat{\mathbb{Z}}_{17} = \mathbb{X}_{14}[\mathbb{Q}_2^{(a,B_2)}(1,-1)] \otimes \mathbb{Y}_4[\mathbb{Q}_1^{(s,B_2)}]$$

No. 18 $\hat{\mathbb{Q}}_1^{(A_1)}(1,0)$ $[M_1, S_2]$

$$\hat{\mathbb{Z}}_{18} = \mathbb{X}_{15}[\mathbb{G}_1^{(a,B_2)}(1,0)] \otimes \mathbb{Y}_4[\mathbb{Q}_1^{(s,B_2)}]$$

No. 19 $\hat{\mathbb{Q}}_0^{(A_1)}$ $[M_1, B_1]$

$$\hat{\mathbb{Z}}_{19} = \mathbb{X}_1[\mathbb{Q}_0^{(a,A_1)}] \otimes \mathbb{Y}_5[\mathbb{Q}_0^{(b,A_1)}]$$

No. 20 $\hat{\mathbb{Q}}_2^{(A_1,1)}$ $[M_1, B_1]$

$$\hat{\mathbb{Z}}_{20} = \mathbb{X}_2[\mathbb{Q}_2^{(a,A_1,1)}] \otimes \mathbb{Y}_5[\mathbb{Q}_0^{(b,A_1)}]$$

No. 21 $\hat{\mathbb{Q}}_2^{(A_1,2)}$ $[M_1, B_1]$

$$\hat{\mathbb{Z}}_{21} = \mathbb{X}_3[\mathbb{Q}_2^{(a,A_1,2)}] \otimes \mathbb{Y}_5[\mathbb{Q}_0^{(b,A_1)}]$$

No. 22 $\hat{\mathbb{Q}}_1^{(A_1)}$ $[M_1, B_1]$

$$\hat{\mathbb{Z}}_{22} = \mathbb{X}_9[\mathbb{Q}_2^{(a,B_2)}] \otimes \mathbb{Y}_6[\mathbb{Q}_1^{(b,B_2)}]$$

No. 23 $\hat{\mathbb{Q}}_0^{(A_1)}(1,1)$ $[M_1, B_1]$

$$\hat{\mathbb{Z}}_{23} = \mathbb{X}_4[\mathbb{Q}_0^{(a,A_1)}(1,1)] \otimes \mathbb{Y}_5[\mathbb{Q}_0^{(b,A_1)}]$$

$\boxed{\text{No. 24}}$ $\hat{\mathbb{Q}}_2^{(A_1,1)}(1,-1)$ $[\text{M}_1,\text{B}_1]$

$\hat{\mathbb{Z}}_{24} = \mathbb{X}_5[\mathbb{Q}_2^{(a,A_1,1)}(1,-1)] \otimes \mathbb{Y}_5[\mathbb{Q}_0^{(b,A_1)}]$

$\boxed{\text{No. 25}}$ $\hat{\mathbb{Q}}_2^{(A_1,2)}(1,-1)$ $[\text{M}_1,\text{B}_1]$

$\hat{\mathbb{Z}}_{25} = \mathbb{X}_6[\mathbb{Q}_2^{(a,A_1,2)}(1,-1)] \otimes \mathbb{Y}_5[\mathbb{Q}_0^{(b,A_1)}]$

$\boxed{\text{No. 26}}$ $\hat{\mathbb{Q}}_1^{(A_1)}(1,-1)$ $[\text{M}_1,\text{B}_1]$

$\hat{\mathbb{Z}}_{26} = \mathbb{X}_{14}[\mathbb{Q}_2^{(a,B_2)}(1,-1)] \otimes \mathbb{Y}_6[\mathbb{Q}_1^{(b,B_2)}]$

$\boxed{\text{No. 27}}$ $\hat{\mathbb{Q}}_1^{(A_1)}(1,0)$ $[\text{M}_1,\text{B}_1]$

$\hat{\mathbb{Z}}_{27} = \mathbb{X}_{15}[\mathbb{G}_1^{(a,B_2)}(1,0)] \otimes \mathbb{Y}_6[\mathbb{Q}_1^{(b,B_2)}]$

$\boxed{\text{No. 28}}$ $\hat{\mathbb{Q}}_1^{(A_1)}$ $[\text{M}_1,\text{B}_1]$

$\hat{\mathbb{Z}}_{28} = \mathbb{X}_{18}[\mathbb{M}_1^{(a,B_2)}] \otimes \mathbb{Y}_8[\mathbb{T}_1^{(b,B_2)}]$

$\boxed{\text{No. 29}}$ $\hat{\mathbb{Q}}_1^{(A_1)}(1,1)$ $[\text{M}_1,\text{B}_1]$

$\hat{\mathbb{Z}}_{29} = \mathbb{X}_{29}[\mathbb{M}_1^{(a,B_2)}(1,1)] \otimes \mathbb{Y}_8[\mathbb{T}_1^{(b,B_2)}]$

$\boxed{\text{No. 30}}$ $\hat{\mathbb{Q}}_1^{(A_1)}(1,-1)$ $[\text{M}_1,\text{B}_1]$

$\hat{\mathbb{Z}}_{30} = \mathbb{X}_{30}[\mathbb{M}_1^{(a,B_2)}(1,-1)] \otimes \mathbb{Y}_8[\mathbb{T}_1^{(b,B_2)}]$

$\boxed{\text{No. 31}}$ $\hat{\mathbb{G}}_3^{(A_1)}(1,-1)$ $[\text{M}_1,\text{B}_1]$

$\hat{\mathbb{Z}}_{31} = \mathbb{X}_{34}[\mathbb{M}_3^{(a,A_1)}(1,-1)] \otimes \mathbb{Y}_7[\mathbb{T}_0^{(b,A_1)}]$

$\boxed{\text{No. 32}}$ $\hat{\mathbb{G}}_2^{(A_1)}(1,-1)$ $[\text{M}_1,\text{B}_1]$

$\hat{\mathbb{Z}}_{32} = -\dfrac{\sqrt{6}\mathbb{X}_{31}[\mathbb{M}_3^{(a,B_2,1)}(1,-1)] \otimes \mathbb{Y}_8[\mathbb{T}_1^{(b,B_2)}]}{4} + \dfrac{\sqrt{10}\mathbb{X}_{32}[\mathbb{M}_3^{(a,B_2,2)}(1,-1)] \otimes \mathbb{Y}_8[\mathbb{T}_1^{(b,B_2)}]}{4}$

No. 33 $\hat{\mathbb{Q}}_3^{(A_1,1)}(1,-1)\ [\mathrm{M}_1,\mathrm{B}_1]$

$$\hat{\mathbb{Z}}_{33} = -\frac{\sqrt{10}\mathbb{X}_{31}[\mathbb{M}_3^{(a,B_2,1)}(1,-1)] \otimes \mathbb{Y}_8[\mathbb{T}_1^{(b,B_2)}]}{4} - \frac{\sqrt{6}\mathbb{X}_{32}[\mathbb{M}_3^{(a,B_2,2)}(1,-1)] \otimes \mathbb{Y}_8[\mathbb{T}_1^{(b,B_2)}]}{4}$$

No. 34 $\hat{\mathbb{Q}}_2^{(A_1,1)}(1,0)\ [\mathrm{M}_1,\mathrm{B}_1]$

$$\hat{\mathbb{Z}}_{34} = \mathbb{X}_{35}[\mathbb{T}_2^{(a,A_1,1)}(1,0)] \otimes \mathbb{Y}_7[\mathbb{T}_0^{(b,A_1)}]$$

No. 35 $\hat{\mathbb{Q}}_2^{(A_1,2)}(1,0)\ [\mathrm{M}_1,\mathrm{B}_1]$

$$\hat{\mathbb{Z}}_{35} = \mathbb{X}_{36}[\mathbb{T}_2^{(a,A_1,2)}(1,0)] \otimes \mathbb{Y}_7[\mathbb{T}_0^{(b,A_1)}]$$

No. 36 $\hat{\mathbb{Q}}_1^{(A_1)}(1,0)\ [\mathrm{M}_1,\mathrm{B}_1]$

$$\hat{\mathbb{Z}}_{36} = \mathbb{X}_{33}[\mathbb{T}_2^{(a,B_2)}(1,0)] \otimes \mathbb{Y}_8[\mathbb{T}_1^{(b,B_2)}]$$

No. 37 $\hat{\mathbb{Q}}_0^{(A_1)}\ [\mathrm{M}_1,\mathrm{B}_2]$

$$\hat{\mathbb{Z}}_{37} = \mathbb{X}_1[\mathbb{Q}_0^{(a,A_1)}] \otimes \mathbb{Y}_9[\mathbb{Q}_0^{(b,A_1)}]$$

No. 38 $\hat{\mathbb{Q}}_2^{(A_1,1)}\ [\mathrm{M}_1,\mathrm{B}_2]$

$$\hat{\mathbb{Z}}_{38} = \mathbb{X}_2[\mathbb{Q}_2^{(a,A_1,1)}] \otimes \mathbb{Y}_9[\mathbb{Q}_0^{(b,A_1)}]$$

No. 39 $\hat{\mathbb{Q}}_2^{(A_1,2)}\ [\mathrm{M}_1,\mathrm{B}_2]$

$$\hat{\mathbb{Z}}_{39} = \mathbb{X}_3[\mathbb{Q}_2^{(a,A_1,2)}] \otimes \mathbb{Y}_9[\mathbb{Q}_0^{(b,A_1)}]$$

No. 40 $\hat{\mathbb{Q}}_1^{(A_1)}\ [\mathrm{M}_1,\mathrm{B}_2]$

$$\hat{\mathbb{Z}}_{40} = \frac{\sqrt{2}\mathbb{X}_8[\mathbb{Q}_2^{(a,B_1)}] \otimes \mathbb{Y}_{10}[\mathbb{Q}_1^{(b,B_1)}]}{2} + \frac{\sqrt{2}\mathbb{X}_9[\mathbb{Q}_2^{(a,B_2)}] \otimes \mathbb{Y}_{11}[\mathbb{Q}_1^{(b,B_2)}]}{2}$$

No. 41 $\hat{\mathbb{G}}_2^{(A_1)}\ [\mathrm{M}_1,\mathrm{B}_2]$

$$\hat{\mathbb{Z}}_{41} = \frac{\sqrt{2}\mathbb{X}_8[\mathbb{Q}_2^{(a,B_1)}] \otimes \mathbb{Y}_{10}[\mathbb{Q}_1^{(b,B_1)}]}{2} - \frac{\sqrt{2}\mathbb{X}_9[\mathbb{Q}_2^{(a,B_2)}] \otimes \mathbb{Y}_{11}[\mathbb{Q}_1^{(b,B_2)}]}{2}$$

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$\boxed{\text{No. 42}}$ $\hat{\mathbb{Q}}_0^{(A_1)}[\text{M}_1, \text{B}_2]$

$\hat{\mathbb{Z}}_{42} = \mathbb{X}_7[\mathbb{Q}_2^{(a,A_2)}] \otimes \mathbb{Y}_{12}[\mathbb{Q}_2^{(b,A_2)}]$

$\boxed{\text{No. 43}}$ $\hat{\mathbb{Q}}_0^{(A_1)}(1,1)[\text{M}_1, \text{B}_2]$

$\hat{\mathbb{Z}}_{43} = \mathbb{X}_4[\mathbb{Q}_0^{(a,A_1)}(1,1)] \otimes \mathbb{Y}_9[\mathbb{Q}_0^{(b,A_1)}]$

$\boxed{\text{No. 44}}$ $\hat{\mathbb{Q}}_2^{(A_1,1)}(1,-1)[\text{M}_1, \text{B}_2]$

$\hat{\mathbb{Z}}_{44} = \mathbb{X}_5[\mathbb{Q}_2^{(a,A_1,1)}(1,-1)] \otimes \mathbb{Y}_9[\mathbb{Q}_0^{(b,A_1)}]$

$\boxed{\text{No. 45}}$ $\hat{\mathbb{Q}}_2^{(A_1,2)}(1,-1)[\text{M}_1, \text{B}_2]$

$\hat{\mathbb{Z}}_{45} = \mathbb{X}_6[\mathbb{Q}_2^{(a,A_1,2)}(1,-1)] \otimes \mathbb{Y}_9[\mathbb{Q}_0^{(b,A_1)}]$

$\boxed{\text{No. 46}}$ $\hat{\mathbb{Q}}_1^{(A_1)}(1,-1)[\text{M}_1, \text{B}_2]$

$\hat{\mathbb{Z}}_{46} = \dfrac{\sqrt{2}\mathbb{X}_{12}[\mathbb{Q}_2^{(a,B_1)}(1,-1)] \otimes \mathbb{Y}_{10}[\mathbb{Q}_1^{(b,B_1)}]}{2} + \dfrac{\sqrt{2}\mathbb{X}_{14}[\mathbb{Q}_2^{(a,B_2)}(1,-1)] \otimes \mathbb{Y}_{11}[\mathbb{Q}_1^{(b,B_2)}]}{2}$

$\boxed{\text{No. 47}}$ $\hat{\mathbb{G}}_2^{(A_1)}(1,-1)[\text{M}_1, \text{B}_2]$

$\hat{\mathbb{Z}}_{47} = \dfrac{\sqrt{2}\mathbb{X}_{12}[\mathbb{Q}_2^{(a,B_1)}(1,-1)] \otimes \mathbb{Y}_{10}[\mathbb{Q}_1^{(b,B_1)}]}{2} - \dfrac{\sqrt{2}\mathbb{X}_{14}[\mathbb{Q}_2^{(a,B_2)}(1,-1)] \otimes \mathbb{Y}_{11}[\mathbb{Q}_1^{(b,B_2)}]}{2}$

$\boxed{\text{No. 48}}$ $\hat{\mathbb{Q}}_0^{(A_1)}(1,-1)[\text{M}_1, \text{B}_2]$

$\hat{\mathbb{Z}}_{48} = \mathbb{X}_{10}[\mathbb{Q}_2^{(a,A_2)}(1,-1)] \otimes \mathbb{Y}_{12}[\mathbb{Q}_2^{(b,A_2)}]$

$\boxed{\text{No. 49}}$ $\hat{\mathbb{Q}}_1^{(A_1)}(1,0)[\text{M}_1, \text{B}_2]$

$\hat{\mathbb{Z}}_{49} = -\dfrac{\sqrt{2}\mathbb{X}_{13}[\mathbb{G}_1^{(a,B_1)}(1,0)] \otimes \mathbb{Y}_{10}[\mathbb{Q}_1^{(b,B_1)}]}{2} + \dfrac{\sqrt{2}\mathbb{X}_{15}[\mathbb{G}_1^{(a,B_2)}(1,0)] \otimes \mathbb{Y}_{11}[\mathbb{Q}_1^{(b,B_2)}]}{2}$

$\boxed{\text{No. 50}}$ $\hat{\mathbb{G}}_2^{(A_1)}(1,0)[\text{M}_1, \text{B}_2]$

$\hat{\mathbb{Z}}_{50} = \dfrac{\sqrt{2}\mathbb{X}_{13}[\mathbb{G}_1^{(a,B_1)}(1,0)] \otimes \mathbb{Y}_{10}[\mathbb{Q}_1^{(b,B_1)}]}{2} + \dfrac{\sqrt{2}\mathbb{X}_{15}[\mathbb{G}_1^{(a,B_2)}(1,0)] \otimes \mathbb{Y}_{11}[\mathbb{Q}_1^{(b,B_2)}]}{2}$

No. 51 $\quad \hat{\mathbb{Q}}_2^{(A_1,2)}(1,0)\ [M_1, B_2]$

$\hat{\mathbb{Z}}_{51} = -\mathbb{X}_{11}[\mathbb{G}_1^{(a,A_2)}(1,0)] \otimes \mathbb{Y}_{12}[\mathbb{Q}_2^{(b,A_2)}]$

No. 52 $\quad \hat{\mathbb{Q}}_1^{(A_1)}\ [M_1, B_2]$

$\hat{\mathbb{Z}}_{52} = -\dfrac{\sqrt{2}\mathbb{X}_{17}[\mathbb{M}_1^{(a,B_1)}] \otimes \mathbb{Y}_{14}[\mathbb{T}_1^{(b,B_1)}]}{2} + \dfrac{\sqrt{2}\mathbb{X}_{18}[\mathbb{M}_1^{(a,B_2)}] \otimes \mathbb{Y}_{15}[\mathbb{T}_1^{(b,B_2)}]}{2}$

No. 53 $\quad \hat{\mathbb{G}}_2^{(A_1)}\ [M_1, B_2]$

$\hat{\mathbb{Z}}_{53} = \dfrac{\sqrt{2}\mathbb{X}_{17}[\mathbb{M}_1^{(a,B_1)}] \otimes \mathbb{Y}_{14}[\mathbb{T}_1^{(b,B_1)}]}{2} + \dfrac{\sqrt{2}\mathbb{X}_{18}[\mathbb{M}_1^{(a,B_2)}] \otimes \mathbb{Y}_{15}[\mathbb{T}_1^{(b,B_2)}]}{2}$

No. 54 $\quad \hat{\mathbb{Q}}_2^{(A_1,2)}\ [M_1, B_2]$

$\hat{\mathbb{Z}}_{54} = -\mathbb{X}_{16}[\mathbb{M}_1^{(a,A_2)}] \otimes \mathbb{Y}_{16}[\mathbb{T}_2^{(b,A_2)}]$

No. 55 $\quad \hat{\mathbb{Q}}_1^{(A_1)}(1,1)\ [M_1, B_2]$

$\hat{\mathbb{Z}}_{55} = -\dfrac{\sqrt{2}\mathbb{X}_{24}[\mathbb{M}_1^{(a,B_1)}(1,1)] \otimes \mathbb{Y}_{14}[\mathbb{T}_1^{(b,B_1)}]}{2} + \dfrac{\sqrt{2}\mathbb{X}_{29}[\mathbb{M}_1^{(a,B_2)}(1,1)] \otimes \mathbb{Y}_{15}[\mathbb{T}_1^{(b,B_2)}]}{2}$

No. 56 $\quad \hat{\mathbb{G}}_2^{(A_1)}(1,1)\ [M_1, B_2]$

$\hat{\mathbb{Z}}_{56} = \dfrac{\sqrt{2}\mathbb{X}_{24}[\mathbb{M}_1^{(a,B_1)}(1,1)] \otimes \mathbb{Y}_{14}[\mathbb{T}_1^{(b,B_1)}]}{2} + \dfrac{\sqrt{2}\mathbb{X}_{29}[\mathbb{M}_1^{(a,B_2)}(1,1)] \otimes \mathbb{Y}_{15}[\mathbb{T}_1^{(b,B_2)}]}{2}$

No. 57 $\quad \hat{\mathbb{Q}}_2^{(A_1,2)}(1,1)\ [M_1, B_2]$

$\hat{\mathbb{Z}}_{57} = -\mathbb{X}_{19}[\mathbb{M}_1^{(a,A_2)}(1,1)] \otimes \mathbb{Y}_{16}[\mathbb{T}_2^{(b,A_2)}]$

No. 58 $\quad \hat{\mathbb{Q}}_1^{(A_1)}(1,-1)\ [M_1, B_2]$

$\hat{\mathbb{Z}}_{58} = -\dfrac{\sqrt{2}\mathbb{X}_{25}[\mathbb{M}_1^{(a,B_1)}(1,-1)] \otimes \mathbb{Y}_{14}[\mathbb{T}_1^{(b,B_1)}]}{2} + \dfrac{\sqrt{2}\mathbb{X}_{30}[\mathbb{M}_1^{(a,B_2)}(1,-1)] \otimes \mathbb{Y}_{15}[\mathbb{T}_1^{(b,B_2)}]}{2}$

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No. 59 $\hat{\mathbb{G}}_2^{(A_1)}(1,-1)$ $[\mathrm{M}_1, \mathrm{B}_2]$

$$\hat{\mathbb{Z}}_{59} = \frac{\sqrt{2}\mathbb{X}_{25}[\mathbb{M}_1^{(a,B_1)}(1,-1)] \otimes \mathbb{Y}_{14}[\mathbb{T}_1^{(b,B_1)}]}{2} + \frac{\sqrt{2}\mathbb{X}_{30}[\mathbb{M}_1^{(a,B_2)}(1,-1)] \otimes \mathbb{Y}_{15}[\mathbb{T}_1^{(b,B_2)}]}{2}$$

No. 60 $\hat{\mathbb{Q}}_2^{(A_1,2)}(1,-1)$ $[\mathrm{M}_1, \mathrm{B}_2]$

$$\hat{\mathbb{Z}}_{60} = -\mathbb{X}_{20}[\mathbb{M}_1^{(a,A_2)}(1,-1)] \otimes \mathbb{Y}_{16}[\mathbb{T}_2^{(b,A_2)}]$$

No. 61 $\hat{\mathbb{G}}_3^{(A_1)}(1,-1)$ $[\mathrm{M}_1, \mathrm{B}_2]$

$$\hat{\mathbb{Z}}_{61} = \mathbb{X}_{34}[\mathbb{M}_3^{(a,A_1)}(1,-1)] \otimes \mathbb{Y}_{13}[\mathbb{T}_0^{(b,A_1)}]$$

No. 62 $\hat{\mathbb{G}}_2^{(A_1)}(1,-1)$ $[\mathrm{M}_1, \mathrm{B}_2]$

$$\hat{\mathbb{Z}}_{62} = -\frac{\sqrt{3}\mathbb{X}_{26}[\mathbb{M}_3^{(a,B_1,1)}(1,-1)] \otimes \mathbb{Y}_{14}[\mathbb{T}_1^{(b,B_1)}]}{4} - \frac{\sqrt{5}\mathbb{X}_{27}[\mathbb{M}_3^{(a,B_1,2)}(1,-1)] \otimes \mathbb{Y}_{14}[\mathbb{T}_1^{(b,B_1)}]}{4}$$
$$- \frac{\sqrt{3}\mathbb{X}_{31}[\mathbb{M}_3^{(a,B_2,1)}(1,-1)] \otimes \mathbb{Y}_{15}[\mathbb{T}_1^{(b,B_2)}]}{4} + \frac{\sqrt{5}\mathbb{X}_{32}[\mathbb{M}_3^{(a,B_2,2)}(1,-1)] \otimes \mathbb{Y}_{15}[\mathbb{T}_1^{(b,B_2)}]}{4}$$

No. 63 $\hat{\mathbb{Q}}_3^{(A_1,1)}(1,-1)$ $[\mathrm{M}_1, \mathrm{B}_2]$

$$\hat{\mathbb{Z}}_{63} = \frac{\sqrt{3}\mathbb{X}_{26}[\mathbb{M}_3^{(a,B_1,1)}(1,-1)] \otimes \mathbb{Y}_{14}[\mathbb{T}_1^{(b,B_1)}]}{4} - \frac{\sqrt{5}\mathbb{X}_{27}[\mathbb{M}_3^{(a,B_1,2)}(1,-1)] \otimes \mathbb{Y}_{14}[\mathbb{T}_1^{(b,B_1)}]}{4}$$
$$- \frac{\sqrt{3}\mathbb{X}_{31}[\mathbb{M}_3^{(a,B_2,1)}(1,-1)] \otimes \mathbb{Y}_{15}[\mathbb{T}_1^{(b,B_2)}]}{4} - \frac{\sqrt{5}\mathbb{X}_{32}[\mathbb{M}_3^{(a,B_2,2)}(1,-1)] \otimes \mathbb{Y}_{15}[\mathbb{T}_1^{(b,B_2)}]}{4}$$

No. 64 $\hat{\mathbb{Q}}_3^{(A_1,2)}(1,-1)$ $[\mathrm{M}_1, \mathrm{B}_2]$

$$\hat{\mathbb{Z}}_{64} = \frac{\sqrt{5}\mathbb{X}_{26}[\mathbb{M}_3^{(a,B_1,1)}(1,-1)] \otimes \mathbb{Y}_{14}[\mathbb{T}_1^{(b,B_1)}]}{4} - \frac{\sqrt{3}\mathbb{X}_{27}[\mathbb{M}_3^{(a,B_1,2)}(1,-1)] \otimes \mathbb{Y}_{14}[\mathbb{T}_1^{(b,B_1)}]}{4}$$
$$+ \frac{\sqrt{5}\mathbb{X}_{31}[\mathbb{M}_3^{(a,B_2,1)}(1,-1)] \otimes \mathbb{Y}_{15}[\mathbb{T}_1^{(b,B_2)}]}{4} + \frac{\sqrt{3}\mathbb{X}_{32}[\mathbb{M}_3^{(a,B_2,2)}(1,-1)] \otimes \mathbb{Y}_{15}[\mathbb{T}_1^{(b,B_2)}]}{4}$$

No. 65 $\hat{\mathbb{G}}_4^{(A_1,1)}(1,-1)$ $[\mathrm{M}_1, \mathrm{B}_2]$

$$\hat{\mathbb{Z}}_{65} = -\frac{\sqrt{5}\mathbb{X}_{26}[\mathbb{M}_3^{(a,B_1,1)}(1,-1)] \otimes \mathbb{Y}_{14}[\mathbb{T}_1^{(b,B_1)}]}{4} - \frac{\sqrt{3}\mathbb{X}_{27}[\mathbb{M}_3^{(a,B_1,2)}(1,-1)] \otimes \mathbb{Y}_{14}[\mathbb{T}_1^{(b,B_1)}]}{4}$$
$$+ \frac{\sqrt{5}\mathbb{X}_{31}[\mathbb{M}_3^{(a,B_2,1)}(1,-1)] \otimes \mathbb{Y}_{15}[\mathbb{T}_1^{(b,B_2)}]}{4} - \frac{\sqrt{3}\mathbb{X}_{32}[\mathbb{M}_3^{(a,B_2,2)}(1,-1)] \otimes \mathbb{Y}_{15}[\mathbb{T}_1^{(b,B_2)}]}{4}$$

No. 66 $\hat{\mathbb{Q}}_2^{(A_1,1)}(1,-1)\ [\mathrm{M}_1,\mathrm{B}_2]$

$\hat{\mathbb{Z}}_{66} = \mathbb{X}_{22}[\mathbb{M}_3^{(a,A_2,2)}(1,-1)] \otimes \mathbb{Y}_{16}[\mathbb{T}_2^{(b,A_2)}]$

No. 67 $\hat{\mathbb{Q}}_2^{(A_1,2)}(1,-1)\ [\mathrm{M}_1,\mathrm{B}_2]$

$\hat{\mathbb{Z}}_{67} = \mathbb{X}_{21}[\mathbb{M}_3^{(a,A_2,1)}(1,-1)] \otimes \mathbb{Y}_{16}[\mathbb{T}_2^{(b,A_2)}]$

No. 68 $\hat{\mathbb{Q}}_2^{(A_1,1)}(1,0)\ [\mathrm{M}_1,\mathrm{B}_2]$

$\hat{\mathbb{Z}}_{68} = \mathbb{X}_{35}[\mathbb{T}_2^{(a,A_1,1)}(1,0)] \otimes \mathbb{Y}_{13}[\mathbb{T}_0^{(b,A_1)}]$

No. 69 $\hat{\mathbb{Q}}_2^{(A_1,2)}(1,0)\ [\mathrm{M}_1,\mathrm{B}_2]$

$\hat{\mathbb{Z}}_{69} = \mathbb{X}_{36}[\mathbb{T}_2^{(a,A_1,2)}(1,0)] \otimes \mathbb{Y}_{13}[\mathbb{T}_0^{(b,A_1)}]$

No. 70 $\hat{\mathbb{Q}}_1^{(A_1)}(1,0)\ [\mathrm{M}_1,\mathrm{B}_2]$

$\hat{\mathbb{Z}}_{70} = \dfrac{\sqrt{2}\mathbb{X}_{28}[\mathbb{T}_2^{(a,B_1)}(1,0)] \otimes \mathbb{Y}_{14}[\mathbb{T}_1^{(b,B_1)}]}{2} + \dfrac{\sqrt{2}\mathbb{X}_{33}[\mathbb{T}_2^{(a,B_2)}(1,0)] \otimes \mathbb{Y}_{15}[\mathbb{T}_1^{(b,B_2)}]}{2}$

No. 71 $\hat{\mathbb{G}}_2^{(A_1)}(1,0)\ [\mathrm{M}_1,\mathrm{B}_2]$

$\hat{\mathbb{Z}}_{71} = \dfrac{\sqrt{2}\mathbb{X}_{28}[\mathbb{T}_2^{(a,B_1)}(1,0)] \otimes \mathbb{Y}_{14}[\mathbb{T}_1^{(b,B_1)}]}{2} - \dfrac{\sqrt{2}\mathbb{X}_{33}[\mathbb{T}_2^{(a,B_2)}(1,0)] \otimes \mathbb{Y}_{15}[\mathbb{T}_1^{(b,B_2)}]}{2}$

No. 72 $\hat{\mathbb{Q}}_0^{(A_1)}(1,0)\ [\mathrm{M}_1,\mathrm{B}_2]$

$\hat{\mathbb{Z}}_{72} = \mathbb{X}_{23}[\mathbb{T}_2^{(a,A_2)}(1,0)] \otimes \mathbb{Y}_{16}[\mathbb{T}_2^{(b,A_2)}]$

No. 73 $\hat{\mathbb{Q}}_0^{(A_1)}\ [\mathrm{M}_1,\mathrm{B}_3]$

$\hat{\mathbb{Z}}_{73} = \mathbb{X}_1[\mathbb{Q}_0^{(a,A_1)}] \otimes \mathbb{Y}_{17}[\mathbb{Q}_0^{(b,A_1)}]$

No. 74 $\hat{\mathbb{Q}}_2^{(A_1,1)}\ [\mathrm{M}_1,\mathrm{B}_3]$

$\hat{\mathbb{Z}}_{74} = \mathbb{X}_2[\mathbb{Q}_2^{(a,A_1,1)}] \otimes \mathbb{Y}_{17}[\mathbb{Q}_0^{(b,A_1)}]$

No. 75 $\hat{\mathbb{Q}}_2^{(A_1,2)}$ [M_1, B_3]

$$\hat{\mathbb{Z}}_{75} = \mathbb{X}_3[\mathbb{Q}_2^{(a,A_1,2)}] \otimes \mathbb{Y}_{17}[\mathbb{Q}_0^{(b,A_1)}]$$

No. 76 $\hat{\mathbb{Q}}_1^{(A_1)}$ [M_1, B_3]

$$\hat{\mathbb{Z}}_{76} = \frac{\sqrt{2}\mathbb{X}_8[\mathbb{Q}_2^{(a,B_1)}] \otimes \mathbb{Y}_{18}[\mathbb{Q}_1^{(b,B_1)}]}{2} + \frac{\sqrt{2}\mathbb{X}_9[\mathbb{Q}_2^{(a,B_2)}] \otimes \mathbb{Y}_{19}[\mathbb{Q}_1^{(b,B_2)}]}{2}$$

No. 77 $\hat{\mathbb{G}}_2^{(A_1)}$ [M_1, B_3]

$$\hat{\mathbb{Z}}_{77} = \frac{\sqrt{2}\mathbb{X}_8[\mathbb{Q}_2^{(a,B_1)}] \otimes \mathbb{Y}_{18}[\mathbb{Q}_1^{(b,B_1)}]}{2} - \frac{\sqrt{2}\mathbb{X}_9[\mathbb{Q}_2^{(a,B_2)}] \otimes \mathbb{Y}_{19}[\mathbb{Q}_1^{(b,B_2)}]}{2}$$

No. 78 $\hat{\mathbb{Q}}_0^{(A_1)}$ [M_1, B_3]

$$\hat{\mathbb{Z}}_{78} = \mathbb{X}_7[\mathbb{Q}_2^{(a,A_2)}] \otimes \mathbb{Y}_{20}[\mathbb{Q}_2^{(b,A_2)}]$$

No. 79 $\hat{\mathbb{Q}}_0^{(A_1)}(1,1)$ [M_1, B_3]

$$\hat{\mathbb{Z}}_{79} = \mathbb{X}_4[\mathbb{Q}_0^{(a,A_1)}(1,1)] \otimes \mathbb{Y}_{17}[\mathbb{Q}_0^{(b,A_1)}]$$

No. 80 $\hat{\mathbb{Q}}_2^{(A_1,1)}(1,-1)$ [M_1, B_3]

$$\hat{\mathbb{Z}}_{80} = \mathbb{X}_5[\mathbb{Q}_2^{(a,A_1,1)}(1,-1)] \otimes \mathbb{Y}_{17}[\mathbb{Q}_0^{(b,A_1)}]$$

No. 81 $\hat{\mathbb{Q}}_2^{(A_1,2)}(1,-1)$ [M_1, B_3]

$$\hat{\mathbb{Z}}_{81} = \mathbb{X}_6[\mathbb{Q}_2^{(a,A_1,2)}(1,-1)] \otimes \mathbb{Y}_{17}[\mathbb{Q}_0^{(b,A_1)}]$$

No. 82 $\hat{\mathbb{Q}}_1^{(A_1)}(1,-1)$ [M_1, B_3]

$$\hat{\mathbb{Z}}_{82} = \frac{\sqrt{2}\mathbb{X}_{12}[\mathbb{Q}_2^{(a,B_1)}(1,-1)] \otimes \mathbb{Y}_{18}[\mathbb{Q}_1^{(b,B_1)}]}{2} + \frac{\sqrt{2}\mathbb{X}_{14}[\mathbb{Q}_2^{(a,B_2)}(1,-1)] \otimes \mathbb{Y}_{19}[\mathbb{Q}_1^{(b,B_2)}]}{2}$$

No. 83 $\hat{\mathbb{G}}_2^{(A_1)}(1,-1)$ [M_1, B_3]

$$\hat{\mathbb{Z}}_{83} = \frac{\sqrt{2}\mathbb{X}_{12}[\mathbb{Q}_2^{(a,B_1)}(1,-1)] \otimes \mathbb{Y}_{18}[\mathbb{Q}_1^{(b,B_1)}]}{2} - \frac{\sqrt{2}\mathbb{X}_{14}[\mathbb{Q}_2^{(a,B_2)}(1,-1)] \otimes \mathbb{Y}_{19}[\mathbb{Q}_1^{(b,B_2)}]}{2}$$

No. 84 | $\hat{\mathbb{Q}}_0^{(A_1)}(1,-1)$ $[\mathrm{M}_1, \mathrm{B}_3]$

$$\hat{\mathbb{Z}}_{84} = \mathbb{X}_{10}[\mathbb{Q}_2^{(a,A_2)}(1,-1)] \otimes \mathbb{Y}_{20}[\mathbb{Q}_2^{(b,A_2)}]$$

No. 85 | $\hat{\mathbb{Q}}_1^{(A_1)}(1,0)$ $[\mathrm{M}_1, \mathrm{B}_3]$

$$\hat{\mathbb{Z}}_{85} = -\frac{\sqrt{2}\mathbb{X}_{13}[\mathbb{G}_1^{(a,B_1)}(1,0)] \otimes \mathbb{Y}_{18}[\mathbb{Q}_1^{(b,B_1)}]}{2} + \frac{\sqrt{2}\mathbb{X}_{15}[\mathbb{G}_1^{(a,B_2)}(1,0)] \otimes \mathbb{Y}_{19}[\mathbb{Q}_1^{(b,B_2)}]}{2}$$

No. 86 | $\hat{\mathbb{G}}_2^{(A_1)}(1,0)$ $[\mathrm{M}_1, \mathrm{B}_3]$

$$\hat{\mathbb{Z}}_{86} = \frac{\sqrt{2}\mathbb{X}_{13}[\mathbb{G}_1^{(a,B_1)}(1,0)] \otimes \mathbb{Y}_{18}[\mathbb{Q}_1^{(b,B_1)}]}{2} + \frac{\sqrt{2}\mathbb{X}_{15}[\mathbb{G}_1^{(a,B_2)}(1,0)] \otimes \mathbb{Y}_{19}[\mathbb{Q}_1^{(b,B_2)}]}{2}$$

No. 87 | $\hat{\mathbb{Q}}_2^{(A_1,2)}(1,0)$ $[\mathrm{M}_1, \mathrm{B}_3]$

$$\hat{\mathbb{Z}}_{87} = -\mathbb{X}_{11}[\mathbb{G}_1^{(a,A_2)}(1,0)] \otimes \mathbb{Y}_{20}[\mathbb{Q}_2^{(b,A_2)}]$$

No. 88 | $\hat{\mathbb{Q}}_1^{(A_1)}$ $[\mathrm{M}_1, \mathrm{B}_3]$

$$\hat{\mathbb{Z}}_{88} = -\frac{\sqrt{2}\mathbb{X}_{17}[\mathbb{M}_1^{(a,B_1)}] \otimes \mathbb{Y}_{22}[\mathbb{T}_1^{(b,B_1)}]}{2} + \frac{\sqrt{2}\mathbb{X}_{18}[\mathbb{M}_1^{(a,B_2)}] \otimes \mathbb{Y}_{23}[\mathbb{T}_1^{(b,B_2)}]}{2}$$

No. 89 | $\hat{\mathbb{G}}_2^{(A_1)}$ $[\mathrm{M}_1, \mathrm{B}_3]$

$$\hat{\mathbb{Z}}_{89} = \frac{\sqrt{2}\mathbb{X}_{17}[\mathbb{M}_1^{(a,B_1)}] \otimes \mathbb{Y}_{22}[\mathbb{T}_1^{(b,B_1)}]}{2} + \frac{\sqrt{2}\mathbb{X}_{18}[\mathbb{M}_1^{(a,B_2)}] \otimes \mathbb{Y}_{23}[\mathbb{T}_1^{(b,B_2)}]}{2}$$

No. 90 | $\hat{\mathbb{Q}}_2^{(A_1,2)}$ $[\mathrm{M}_1, \mathrm{B}_3]$

$$\hat{\mathbb{Z}}_{90} = -\mathbb{X}_{16}[\mathbb{M}_1^{(a,A_2)}] \otimes \mathbb{Y}_{24}[\mathbb{T}_2^{(b,A_2)}]$$

No. 91 | $\hat{\mathbb{Q}}_1^{(A_1)}(1,1)$ $[\mathrm{M}_1, \mathrm{B}_3]$

$$\hat{\mathbb{Z}}_{91} = -\frac{\sqrt{2}\mathbb{X}_{24}[\mathbb{M}_1^{(a,B_1)}(1,1)] \otimes \mathbb{Y}_{22}[\mathbb{T}_1^{(b,B_1)}]}{2} + \frac{\sqrt{2}\mathbb{X}_{29}[\mathbb{M}_1^{(a,B_2)}(1,1)] \otimes \mathbb{Y}_{23}[\mathbb{T}_1^{(b,B_2)}]}{2}$$

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No. 92 $\hat{\mathbb{G}}_2^{(A_1)}(1,1)\ [\mathrm{M_1,B_3}]$

$$\hat{\mathbb{Z}}_{92} = \frac{\sqrt{2}\mathbb{X}_{24}[\mathbb{M}_1^{(a,B_1)}(1,1)] \otimes \mathbb{Y}_{22}[\mathbb{T}_1^{(b,B_1)}]}{2} + \frac{\sqrt{2}\mathbb{X}_{29}[\mathbb{M}_1^{(a,B_2)}(1,1)] \otimes \mathbb{Y}_{23}[\mathbb{T}_1^{(b,B_2)}]}{2}$$

No. 93 $\hat{\mathbb{Q}}_2^{(A_1,2)}(1,1)\ [\mathrm{M_1,B_3}]$

$$\hat{\mathbb{Z}}_{93} = -\mathbb{X}_{19}[\mathbb{M}_1^{(a,A_2)}(1,1)] \otimes \mathbb{Y}_{24}[\mathbb{T}_2^{(b,A_2)}]$$

No. 94 $\hat{\mathbb{Q}}_1^{(A_1)}(1,-1)\ [\mathrm{M_1,B_3}]$

$$\hat{\mathbb{Z}}_{94} = -\frac{\sqrt{2}\mathbb{X}_{25}[\mathbb{M}_1^{(a,B_1)}(1,-1)] \otimes \mathbb{Y}_{22}[\mathbb{T}_1^{(b,B_1)}]}{2} + \frac{\sqrt{2}\mathbb{X}_{30}[\mathbb{M}_1^{(a,B_2)}(1,-1)] \otimes \mathbb{Y}_{23}[\mathbb{T}_1^{(b,B_2)}]}{2}$$

No. 95 $\hat{\mathbb{G}}_2^{(A_1)}(1,-1)\ [\mathrm{M_1,B_3}]$

$$\hat{\mathbb{Z}}_{95} = \frac{\sqrt{2}\mathbb{X}_{25}[\mathbb{M}_1^{(a,B_1)}(1,-1)] \otimes \mathbb{Y}_{22}[\mathbb{T}_1^{(b,B_1)}]}{2} + \frac{\sqrt{2}\mathbb{X}_{30}[\mathbb{M}_1^{(a,B_2)}(1,-1)] \otimes \mathbb{Y}_{23}[\mathbb{T}_1^{(b,B_2)}]}{2}$$

No. 96 $\hat{\mathbb{Q}}_2^{(A_1,2)}(1,-1)\ [\mathrm{M_1,B_3}]$

$$\hat{\mathbb{Z}}_{96} = -\mathbb{X}_{20}[\mathbb{M}_1^{(a,A_2)}(1,-1)] \otimes \mathbb{Y}_{24}[\mathbb{T}_2^{(b,A_2)}]$$

No. 97 $\hat{\mathbb{G}}_3^{(A_1)}(1,-1)\ [\mathrm{M_1,B_3}]$

$$\hat{\mathbb{Z}}_{97} = \mathbb{X}_{34}[\mathbb{M}_3^{(a,A_1)}(1,-1)] \otimes \mathbb{Y}_{21}[\mathbb{T}_0^{(b,A_1)}]$$

No. 98 $\hat{\mathbb{G}}_2^{(A_1)}(1,-1)\ [\mathrm{M_1,B_3}]$

$$\hat{\mathbb{Z}}_{98} = -\frac{\sqrt{3}\mathbb{X}_{26}[\mathbb{M}_3^{(a,B_1,1)}(1,-1)] \otimes \mathbb{Y}_{22}[\mathbb{T}_1^{(b,B_1)}]}{4} - \frac{\sqrt{5}\mathbb{X}_{27}[\mathbb{M}_3^{(a,B_1,2)}(1,-1)] \otimes \mathbb{Y}_{22}[\mathbb{T}_1^{(b,B_1)}]}{4}$$
$$- \frac{\sqrt{3}\mathbb{X}_{31}[\mathbb{M}_3^{(a,B_2,1)}(1,-1)] \otimes \mathbb{Y}_{23}[\mathbb{T}_1^{(b,B_2)}]}{4} + \frac{\sqrt{5}\mathbb{X}_{32}[\mathbb{M}_3^{(a,B_2,2)}(1,-1)] \otimes \mathbb{Y}_{23}[\mathbb{T}_1^{(b,B_2)}]}{4}$$

No. 99 $\hat{\mathbb{Q}}_3^{(A_1,1)}(1,-1)\ [\mathrm{M_1,B_3}]$

$$\hat{\mathbb{Z}}_{99} = \frac{\sqrt{3}\mathbb{X}_{26}[\mathbb{M}_3^{(a,B_1,1)}(1,-1)] \otimes \mathbb{Y}_{22}[\mathbb{T}_1^{(b,B_1)}]}{4} - \frac{\sqrt{5}\mathbb{X}_{27}[\mathbb{M}_3^{(a,B_1,2)}(1,-1)] \otimes \mathbb{Y}_{22}[\mathbb{T}_1^{(b,B_1)}]}{4}$$
$$- \frac{\sqrt{3}\mathbb{X}_{31}[\mathbb{M}_3^{(a,B_2,1)}(1,-1)] \otimes \mathbb{Y}_{23}[\mathbb{T}_1^{(b,B_2)}]}{4} - \frac{\sqrt{5}\mathbb{X}_{32}[\mathbb{M}_3^{(a,B_2,2)}(1,-1)] \otimes \mathbb{Y}_{23}[\mathbb{T}_1^{(b,B_2)}]}{4}$$

No. 100 $\hat{\mathbb{Q}}_3^{(A_1,2)}(1,-1)$ $[\mathrm{M}_1,\mathrm{B}_3]$

$$\hat{\mathbb{Z}}_{100} = \frac{\sqrt{5}\mathbb{X}_{26}[\mathbb{M}_3^{(a,B_1,1)}(1,-1)] \otimes \mathbb{Y}_{22}[\mathbb{T}_1^{(b,B_1)}]}{4} - \frac{\sqrt{3}\mathbb{X}_{27}[\mathbb{M}_3^{(a,B_1,2)}(1,-1)] \otimes \mathbb{Y}_{22}[\mathbb{T}_1^{(b,B_1)}]}{4}$$
$$+ \frac{\sqrt{5}\mathbb{X}_{31}[\mathbb{M}_3^{(a,B_2,1)}(1,-1)] \otimes \mathbb{Y}_{23}[\mathbb{T}_1^{(b,B_2)}]}{4} + \frac{\sqrt{3}\mathbb{X}_{32}[\mathbb{M}_3^{(a,B_2,2)}(1,-1)] \otimes \mathbb{Y}_{23}[\mathbb{T}_1^{(b,B_2)}]}{4}$$

No. 101 $\hat{\mathbb{G}}_4^{(A_1,1)}(1,-1)$ $[\mathrm{M}_1,\mathrm{B}_3]$

$$\hat{\mathbb{Z}}_{101} = -\frac{\sqrt{5}\mathbb{X}_{26}[\mathbb{M}_3^{(a,B_1,1)}(1,-1)] \otimes \mathbb{Y}_{22}[\mathbb{T}_1^{(b,B_1)}]}{4} - \frac{\sqrt{3}\mathbb{X}_{27}[\mathbb{M}_3^{(a,B_1,2)}(1,-1)] \otimes \mathbb{Y}_{22}[\mathbb{T}_1^{(b,B_1)}]}{4}$$
$$+ \frac{\sqrt{5}\mathbb{X}_{31}[\mathbb{M}_3^{(a,B_2,1)}(1,-1)] \otimes \mathbb{Y}_{23}[\mathbb{T}_1^{(b,B_2)}]}{4} - \frac{\sqrt{3}\mathbb{X}_{32}[\mathbb{M}_3^{(a,B_2,2)}(1,-1)] \otimes \mathbb{Y}_{23}[\mathbb{T}_1^{(b,B_2)}]}{4}$$

No. 102 $\hat{\mathbb{Q}}_2^{(A_1,1)}(1,-1)$ $[\mathrm{M}_1,\mathrm{B}_3]$

$$\hat{\mathbb{Z}}_{102} = \mathbb{X}_{22}[\mathbb{M}_3^{(a,A_2,2)}(1,-1)] \otimes \mathbb{Y}_{24}[\mathbb{T}_2^{(b,A_2)}]$$

No. 103 $\hat{\mathbb{Q}}_2^{(A_1,2)}(1,-1)$ $[\mathrm{M}_1,\mathrm{B}_3]$

$$\hat{\mathbb{Z}}_{103} = \mathbb{X}_{21}[\mathbb{M}_3^{(a,A_2,1)}(1,-1)] \otimes \mathbb{Y}_{24}[\mathbb{T}_2^{(b,A_2)}]$$

No. 104 $\hat{\mathbb{Q}}_2^{(A_1,1)}(1,0)$ $[\mathrm{M}_1,\mathrm{B}_3]$

$$\hat{\mathbb{Z}}_{104} = \mathbb{X}_{35}[\mathbb{T}_2^{(a,A_1,1)}(1,0)] \otimes \mathbb{Y}_{21}[\mathbb{T}_0^{(b,A_1)}]$$

No. 105 $\hat{\mathbb{Q}}_2^{(A_1,2)}(1,0)$ $[\mathrm{M}_1,\mathrm{B}_3]$

$$\hat{\mathbb{Z}}_{105} = \mathbb{X}_{36}[\mathbb{T}_2^{(a,A_1,2)}(1,0)] \otimes \mathbb{Y}_{21}[\mathbb{T}_0^{(b,A_1)}]$$

No. 106 $\hat{\mathbb{Q}}_1^{(A_1)}(1,0)$ $[\mathrm{M}_1,\mathrm{B}_3]$

$$\hat{\mathbb{Z}}_{106} = \frac{\sqrt{2}\mathbb{X}_{28}[\mathbb{T}_2^{(a,B_1)}(1,0)] \otimes \mathbb{Y}_{22}[\mathbb{T}_1^{(b,B_1)}]}{2} + \frac{\sqrt{2}\mathbb{X}_{33}[\mathbb{T}_2^{(a,B_2)}(1,0)] \otimes \mathbb{Y}_{23}[\mathbb{T}_1^{(b,B_2)}]}{2}$$

No. 107 $\hat{\mathbb{G}}_2^{(A_1)}(1,0)$ $[\mathrm{M}_1,\mathrm{B}_3]$

$$\hat{\mathbb{Z}}_{107} = \frac{\sqrt{2}\mathbb{X}_{28}[\mathbb{T}_2^{(a,B_1)}(1,0)] \otimes \mathbb{Y}_{22}[\mathbb{T}_1^{(b,B_1)}]}{2} - \frac{\sqrt{2}\mathbb{X}_{33}[\mathbb{T}_2^{(a,B_2)}(1,0)] \otimes \mathbb{Y}_{23}[\mathbb{T}_1^{(b,B_2)}]}{2}$$

No. 108 $\hat{\mathbb{Q}}_0^{(A_1)}(1,0)$ $[\text{M}_1, \text{B}_3]$

$$\hat{\mathbb{Z}}_{108} = \mathbb{X}_{23}[\mathbb{T}_2^{(a,A_2)}(1,0)] \otimes \mathbb{Y}_{24}[\mathbb{T}_2^{(b,A_2)}]$$

No. 109 $\hat{\mathbb{Q}}_0^{(A_1)}$ $[\text{M}_1, \text{B}_4]$

$$\hat{\mathbb{Z}}_{109} = \mathbb{X}_1[\mathbb{Q}_0^{(a,A_1)}] \otimes \mathbb{Y}_{25}[\mathbb{Q}_0^{(b,A_1)}]$$

No. 110 $\hat{\mathbb{Q}}_2^{(A_1,1)}$ $[\text{M}_1, \text{B}_4]$

$$\hat{\mathbb{Z}}_{110} = \mathbb{X}_2[\mathbb{Q}_2^{(a,A_1,1)}] \otimes \mathbb{Y}_{25}[\mathbb{Q}_0^{(b,A_1)}]$$

No. 111 $\hat{\mathbb{Q}}_2^{(A_1,2)}$ $[\text{M}_1, \text{B}_4]$

$$\hat{\mathbb{Z}}_{111} = \mathbb{X}_3[\mathbb{Q}_2^{(a,A_1,2)}] \otimes \mathbb{Y}_{25}[\mathbb{Q}_0^{(b,A_1)}]$$

No. 112 $\hat{\mathbb{Q}}_1^{(A_1)}$ $[\text{M}_1, \text{B}_4]$

$$\hat{\mathbb{Z}}_{112} = \frac{\sqrt{2}\mathbb{X}_8[\mathbb{Q}_2^{(a,B_1)}] \otimes \mathbb{Y}_{26}[\mathbb{Q}_1^{(b,B_1)}]}{2} + \frac{\sqrt{2}\mathbb{X}_9[\mathbb{Q}_2^{(a,B_2)}] \otimes \mathbb{Y}_{27}[\mathbb{Q}_1^{(b,B_2)}]}{2}$$

No. 113 $\hat{\mathbb{G}}_2^{(A_1)}$ $[\text{M}_1, \text{B}_4]$

$$\hat{\mathbb{Z}}_{113} = \frac{\sqrt{2}\mathbb{X}_8[\mathbb{Q}_2^{(a,B_1)}] \otimes \mathbb{Y}_{26}[\mathbb{Q}_1^{(b,B_1)}]}{2} - \frac{\sqrt{2}\mathbb{X}_9[\mathbb{Q}_2^{(a,B_2)}] \otimes \mathbb{Y}_{27}[\mathbb{Q}_1^{(b,B_2)}]}{2}$$

No. 114 $\hat{\mathbb{Q}}_0^{(A_1)}$ $[\text{M}_1, \text{B}_4]$

$$\hat{\mathbb{Z}}_{114} = \mathbb{X}_7[\mathbb{Q}_2^{(a,A_2)}] \otimes \mathbb{Y}_{28}[\mathbb{Q}_2^{(b,A_2)}]$$

No. 115 $\hat{\mathbb{Q}}_0^{(A_1)}(1,1)$ $[\text{M}_1, \text{B}_4]$

$$\hat{\mathbb{Z}}_{115} = \mathbb{X}_4[\mathbb{Q}_0^{(a,A_1)}(1,1)] \otimes \mathbb{Y}_{25}[\mathbb{Q}_0^{(b,A_1)}]$$

No. 116 $\hat{\mathbb{Q}}_2^{(A_1,1)}(1,-1)$ $[\text{M}_1, \text{B}_4]$

$$\hat{\mathbb{Z}}_{116} = \mathbb{X}_5[\mathbb{Q}_2^{(a,A_1,1)}(1,-1)] \otimes \mathbb{Y}_{25}[\mathbb{Q}_0^{(b,A_1)}]$$

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No. 117 $\hat{\mathbb{Q}}_2^{(A_1,2)}(1,-1)$ $[\text{M}_1,\text{B}_4]$

$$\hat{\mathbb{Z}}_{117} = \mathbb{X}_6[\mathbb{Q}_2^{(a,A_1,2)}(1,-1)] \otimes \mathbb{Y}_{25}[\mathbb{Q}_0^{(b,A_1)}]$$

No. 118 $\hat{\mathbb{Q}}_1^{(A_1)}(1,-1)$ $[\text{M}_1,\text{B}_4]$

$$\hat{\mathbb{Z}}_{118} = \frac{\sqrt{2}\mathbb{X}_{12}[\mathbb{Q}_2^{(a,B_1)}(1,-1)] \otimes \mathbb{Y}_{26}[\mathbb{Q}_1^{(b,B_1)}]}{2} + \frac{\sqrt{2}\mathbb{X}_{14}[\mathbb{Q}_2^{(a,B_2)}(1,-1)] \otimes \mathbb{Y}_{27}[\mathbb{Q}_1^{(b,B_2)}]}{2}$$

No. 119 $\hat{\mathbb{G}}_2^{(A_1)}(1,-1)$ $[\text{M}_1,\text{B}_4]$

$$\hat{\mathbb{Z}}_{119} = \frac{\sqrt{2}\mathbb{X}_{12}[\mathbb{Q}_2^{(a,B_1)}(1,-1)] \otimes \mathbb{Y}_{26}[\mathbb{Q}_1^{(b,B_1)}]}{2} - \frac{\sqrt{2}\mathbb{X}_{14}[\mathbb{Q}_2^{(a,B_2)}(1,-1)] \otimes \mathbb{Y}_{27}[\mathbb{Q}_1^{(b,B_2)}]}{2}$$

No. 120 $\hat{\mathbb{Q}}_0^{(A_1)}(1,-1)$ $[\text{M}_1,\text{B}_4]$

$$\hat{\mathbb{Z}}_{120} = \mathbb{X}_{10}[\mathbb{Q}_2^{(a,A_2)}(1,-1)] \otimes \mathbb{Y}_{28}[\mathbb{Q}_2^{(b,A_2)}]$$

No. 121 $\hat{\mathbb{Q}}_1^{(A_1)}(1,0)$ $[\text{M}_1,\text{B}_4]$

$$\hat{\mathbb{Z}}_{121} = -\frac{\sqrt{2}\mathbb{X}_{13}[\mathbb{G}_1^{(a,B_1)}(1,0)] \otimes \mathbb{Y}_{26}[\mathbb{Q}_1^{(b,B_1)}]}{2} + \frac{\sqrt{2}\mathbb{X}_{15}[\mathbb{G}_1^{(a,B_2)}(1,0)] \otimes \mathbb{Y}_{27}[\mathbb{Q}_1^{(b,B_2)}]}{2}$$

No. 122 $\hat{\mathbb{G}}_2^{(A_1)}(1,0)$ $[\text{M}_1,\text{B}_4]$

$$\hat{\mathbb{Z}}_{122} = \frac{\sqrt{2}\mathbb{X}_{13}[\mathbb{G}_1^{(a,B_1)}(1,0)] \otimes \mathbb{Y}_{26}[\mathbb{Q}_1^{(b,B_1)}]}{2} + \frac{\sqrt{2}\mathbb{X}_{15}[\mathbb{G}_1^{(a,B_2)}(1,0)] \otimes \mathbb{Y}_{27}[\mathbb{Q}_1^{(b,B_2)}]}{2}$$

No. 123 $\hat{\mathbb{Q}}_2^{(A_1,2)}(1,0)$ $[\text{M}_1,\text{B}_4]$

$$\hat{\mathbb{Z}}_{123} = -\mathbb{X}_{11}[\mathbb{G}_1^{(a,A_2)}(1,0)] \otimes \mathbb{Y}_{28}[\mathbb{Q}_2^{(b,A_2)}]$$

No. 124 $\hat{\mathbb{Q}}_1^{(A_1)}$ $[\text{M}_1,\text{B}_4]$

$$\hat{\mathbb{Z}}_{124} = -\frac{\sqrt{2}\mathbb{X}_{17}[\mathbb{M}_1^{(a,B_1)}] \otimes \mathbb{Y}_{30}[\mathbb{T}_1^{(b,B_1)}]}{2} + \frac{\sqrt{2}\mathbb{X}_{18}[\mathbb{M}_1^{(a,B_2)}] \otimes \mathbb{Y}_{31}[\mathbb{T}_1^{(b,B_2)}]}{2}$$

No. 125 $\hat{\mathbb{G}}_2^{(A_1)}$ [M$_1$, B$_4$]

$$\hat{\mathbb{Z}}_{125} = \frac{\sqrt{2}\mathbb{X}_{17}[\mathbb{M}_1^{(a,B_1)}] \otimes \mathbb{Y}_{30}[\mathbb{T}_1^{(b,B_1)}]}{2} + \frac{\sqrt{2}\mathbb{X}_{18}[\mathbb{M}_1^{(a,B_2)}] \otimes \mathbb{Y}_{31}[\mathbb{T}_1^{(b,B_2)}]}{2}$$

No. 126 $\hat{\mathbb{Q}}_2^{(A_1,2)}$ [M$_1$, B$_4$]

$$\hat{\mathbb{Z}}_{126} = -\mathbb{X}_{16}[\mathbb{M}_1^{(a,A_2)}] \otimes \mathbb{Y}_{32}[\mathbb{T}_2^{(b,A_2)}]$$

No. 127 $\hat{\mathbb{Q}}_1^{(A_1)}(1,1)$ [M$_1$, B$_4$]

$$\hat{\mathbb{Z}}_{127} = -\frac{\sqrt{2}\mathbb{X}_{24}[\mathbb{M}_1^{(a,B_1)}(1,1)] \otimes \mathbb{Y}_{30}[\mathbb{T}_1^{(b,B_1)}]}{2} + \frac{\sqrt{2}\mathbb{X}_{29}[\mathbb{M}_1^{(a,B_2)}(1,1)] \otimes \mathbb{Y}_{31}[\mathbb{T}_1^{(b,B_2)}]}{2}$$

No. 128 $\hat{\mathbb{G}}_2^{(A_1)}(1,1)$ [M$_1$, B$_4$]

$$\hat{\mathbb{Z}}_{128} = \frac{\sqrt{2}\mathbb{X}_{24}[\mathbb{M}_1^{(a,B_1)}(1,1)] \otimes \mathbb{Y}_{30}[\mathbb{T}_1^{(b,B_1)}]}{2} + \frac{\sqrt{2}\mathbb{X}_{29}[\mathbb{M}_1^{(a,B_2)}(1,1)] \otimes \mathbb{Y}_{31}[\mathbb{T}_1^{(b,B_2)}]}{2}$$

No. 129 $\hat{\mathbb{Q}}_2^{(A_1,2)}(1,1)$ [M$_1$, B$_4$]

$$\hat{\mathbb{Z}}_{129} = -\mathbb{X}_{19}[\mathbb{M}_1^{(a,A_2)}(1,1)] \otimes \mathbb{Y}_{32}[\mathbb{T}_2^{(b,A_2)}]$$

No. 130 $\hat{\mathbb{Q}}_1^{(A_1)}(1,-1)$ [M$_1$, B$_4$]

$$\hat{\mathbb{Z}}_{130} = -\frac{\sqrt{2}\mathbb{X}_{25}[\mathbb{M}_1^{(a,B_1)}(1,-1)] \otimes \mathbb{Y}_{30}[\mathbb{T}_1^{(b,B_1)}]}{2} + \frac{\sqrt{2}\mathbb{X}_{30}[\mathbb{M}_1^{(a,B_2)}(1,-1)] \otimes \mathbb{Y}_{31}[\mathbb{T}_1^{(b,B_2)}]}{2}$$

No. 131 $\hat{\mathbb{G}}_2^{(A_1)}(1,-1)$ [M$_1$, B$_4$]

$$\hat{\mathbb{Z}}_{131} = \frac{\sqrt{2}\mathbb{X}_{25}[\mathbb{M}_1^{(a,B_1)}(1,-1)] \otimes \mathbb{Y}_{30}[\mathbb{T}_1^{(b,B_1)}]}{2} + \frac{\sqrt{2}\mathbb{X}_{30}[\mathbb{M}_1^{(a,B_2)}(1,-1)] \otimes \mathbb{Y}_{31}[\mathbb{T}_1^{(b,B_2)}]}{2}$$

No. 132 $\hat{\mathbb{Q}}_2^{(A_1,2)}(1,-1)$ [M$_1$, B$_4$]

$$\hat{\mathbb{Z}}_{132} = -\mathbb{X}_{20}[\mathbb{M}_1^{(a,A_2)}(1,-1)] \otimes \mathbb{Y}_{32}[\mathbb{T}_2^{(b,A_2)}]$$

No. 133 | $\hat{\mathbb{G}}_3^{(A_1)}(1,-1)$ $[\mathrm{M}_1, \mathrm{B}_4]$

$\hat{\mathbb{Z}}_{133} = \mathbb{X}_{34}[\mathbb{M}_3^{(a,A_1)}(1,-1)] \otimes \mathbb{Y}_{29}[\mathbb{T}_0^{(b,A_1)}]$

No. 134 | $\hat{\mathbb{G}}_2^{(A_1)}(1,-1)$ $[\mathrm{M}_1, \mathrm{B}_4]$

$\hat{\mathbb{Z}}_{134} = -\dfrac{\sqrt{3}\mathbb{X}_{26}[\mathbb{M}_3^{(a,B_1,1)}(1,-1)] \otimes \mathbb{Y}_{30}[\mathbb{T}_1^{(b,B_1)}]}{4} - \dfrac{\sqrt{5}\mathbb{X}_{27}[\mathbb{M}_3^{(a,B_1,2)}(1,-1)] \otimes \mathbb{Y}_{30}[\mathbb{T}_1^{(b,B_1)}]}{4}$

$\qquad - \dfrac{\sqrt{3}\mathbb{X}_{31}[\mathbb{M}_3^{(a,B_2,1)}(1,-1)] \otimes \mathbb{Y}_{31}[\mathbb{T}_1^{(b,B_2)}]}{4} + \dfrac{\sqrt{5}\mathbb{X}_{32}[\mathbb{M}_3^{(a,B_2,2)}(1,-1)] \otimes \mathbb{Y}_{31}[\mathbb{T}_1^{(b,B_2)}]}{4}$

No. 135 | $\hat{\mathbb{Q}}_3^{(A_1,1)}(1,-1)$ $[\mathrm{M}_1, \mathrm{B}_4]$

$\hat{\mathbb{Z}}_{135} = \dfrac{\sqrt{3}\mathbb{X}_{26}[\mathbb{M}_3^{(a,B_1,1)}(1,-1)] \otimes \mathbb{Y}_{30}[\mathbb{T}_1^{(b,B_1)}]}{4} - \dfrac{\sqrt{5}\mathbb{X}_{27}[\mathbb{M}_3^{(a,B_1,2)}(1,-1)] \otimes \mathbb{Y}_{30}[\mathbb{T}_1^{(b,B_1)}]}{4}$

$\qquad - \dfrac{\sqrt{3}\mathbb{X}_{31}[\mathbb{M}_3^{(a,B_2,1)}(1,-1)] \otimes \mathbb{Y}_{31}[\mathbb{T}_1^{(b,B_2)}]}{4} - \dfrac{\sqrt{5}\mathbb{X}_{32}[\mathbb{M}_3^{(a,B_2,2)}(1,-1)] \otimes \mathbb{Y}_{31}[\mathbb{T}_1^{(b,B_2)}]}{4}$

No. 136 | $\hat{\mathbb{Q}}_3^{(A_1,2)}(1,-1)$ $[\mathrm{M}_1, \mathrm{B}_4]$

$\hat{\mathbb{Z}}_{136} = \dfrac{\sqrt{5}\mathbb{X}_{26}[\mathbb{M}_3^{(a,B_1,1)}(1,-1)] \otimes \mathbb{Y}_{30}[\mathbb{T}_1^{(b,B_1)}]}{4} - \dfrac{\sqrt{3}\mathbb{X}_{27}[\mathbb{M}_3^{(a,B_1,2)}(1,-1)] \otimes \mathbb{Y}_{30}[\mathbb{T}_1^{(b,B_1)}]}{4}$

$\qquad + \dfrac{\sqrt{5}\mathbb{X}_{31}[\mathbb{M}_3^{(a,B_2,1)}(1,-1)] \otimes \mathbb{Y}_{31}[\mathbb{T}_1^{(b,B_2)}]}{4} + \dfrac{\sqrt{3}\mathbb{X}_{32}[\mathbb{M}_3^{(a,B_2,2)}(1,-1)] \otimes \mathbb{Y}_{31}[\mathbb{T}_1^{(b,B_2)}]}{4}$

No. 137 | $\hat{\mathbb{G}}_4^{(A_1,1)}(1,-1)$ $[\mathrm{M}_1, \mathrm{B}_4]$

$\hat{\mathbb{Z}}_{137} = -\dfrac{\sqrt{5}\mathbb{X}_{26}[\mathbb{M}_3^{(a,B_1,1)}(1,-1)] \otimes \mathbb{Y}_{30}[\mathbb{T}_1^{(b,B_1)}]}{4} - \dfrac{\sqrt{3}\mathbb{X}_{27}[\mathbb{M}_3^{(a,B_1,2)}(1,-1)] \otimes \mathbb{Y}_{30}[\mathbb{T}_1^{(b,B_1)}]}{4}$

$\qquad + \dfrac{\sqrt{5}\mathbb{X}_{31}[\mathbb{M}_3^{(a,B_2,1)}(1,-1)] \otimes \mathbb{Y}_{31}[\mathbb{T}_1^{(b,B_2)}]}{4} - \dfrac{\sqrt{3}\mathbb{X}_{32}[\mathbb{M}_3^{(a,B_2,2)}(1,-1)] \otimes \mathbb{Y}_{31}[\mathbb{T}_1^{(b,B_2)}]}{4}$

No. 138 | $\hat{\mathbb{Q}}_2^{(A_1,1)}(1,-1)$ $[\mathrm{M}_1, \mathrm{B}_4]$

$\hat{\mathbb{Z}}_{138} = \mathbb{X}_{22}[\mathbb{M}_3^{(a,A_2,2)}(1,-1)] \otimes \mathbb{Y}_{32}[\mathbb{T}_2^{(b,A_2)}]$

No. 139 | $\hat{\mathbb{Q}}_2^{(A_1,2)}(1,-1)$ $[\mathrm{M}_1, \mathrm{B}_4]$

$\hat{\mathbb{Z}}_{139} = \mathbb{X}_{21}[\mathbb{M}_3^{(a,A_2,1)}(1,-1)] \otimes \mathbb{Y}_{32}[\mathbb{T}_2^{(b,A_2)}]$

No. 140 $\hat{\mathbb{Q}}_2^{(A_1,1)}(1,0)$ $[\mathrm{M}_1,\mathrm{B}_4]$

$\hat{\mathbb{Z}}_{140} = \mathbb{X}_{35}[\mathbb{T}_2^{(a,A_1,1)}(1,0)] \otimes \mathbb{Y}_{29}[\mathbb{T}_0^{(b,A_1)}]$

No. 141 $\hat{\mathbb{Q}}_2^{(A_1,2)}(1,0)$ $[\mathrm{M}_1,\mathrm{B}_4]$

$\hat{\mathbb{Z}}_{141} = \mathbb{X}_{36}[\mathbb{T}_2^{(a,A_1,2)}(1,0)] \otimes \mathbb{Y}_{29}[\mathbb{T}_0^{(b,A_1)}]$

No. 142 $\hat{\mathbb{Q}}_1^{(A_1)}(1,0)$ $[\mathrm{M}_1,\mathrm{B}_4]$

$\hat{\mathbb{Z}}_{142} = \dfrac{\sqrt{2}\mathbb{X}_{28}[\mathbb{T}_2^{(a,B_1)}(1,0)] \otimes \mathbb{Y}_{30}[\mathbb{T}_1^{(b,B_1)}]}{2} + \dfrac{\sqrt{2}\mathbb{X}_{33}[\mathbb{T}_2^{(a,B_2)}(1,0)] \otimes \mathbb{Y}_{31}[\mathbb{T}_1^{(b,B_2)}]}{2}$

No. 143 $\hat{\mathbb{G}}_2^{(A_1)}(1,0)$ $[\mathrm{M}_1,\mathrm{B}_4]$

$\hat{\mathbb{Z}}_{143} = \dfrac{\sqrt{2}\mathbb{X}_{28}[\mathbb{T}_2^{(a,B_1)}(1,0)] \otimes \mathbb{Y}_{30}[\mathbb{T}_1^{(b,B_1)}]}{2} - \dfrac{\sqrt{2}\mathbb{X}_{33}[\mathbb{T}_2^{(a,B_2)}(1,0)] \otimes \mathbb{Y}_{31}[\mathbb{T}_1^{(b,B_2)}]}{2}$

No. 144 $\hat{\mathbb{Q}}_0^{(A_1)}(1,0)$ $[\mathrm{M}_1,\mathrm{B}_4]$

$\hat{\mathbb{Z}}_{144} = \mathbb{X}_{23}[\mathbb{T}_2^{(a,A_2)}(1,0)] \otimes \mathbb{Y}_{32}[\mathbb{T}_2^{(b,A_2)}]$

Table 5: Atomic SAMB group.

group	bra	ket
M_1	$(p_x,\uparrow),(p_x,\downarrow),(p_y,\uparrow),(p_y,\downarrow),(p_z,\uparrow),(p_z,\downarrow)$	$(p_x,\uparrow),(p_x,\downarrow),(p_y,\uparrow),(p_y,\downarrow),(p_z,\uparrow),(p_z,\downarrow)$

Table 6: Atomic SAMB.

symbol	type	group	form
$\mathbb{X}_1$	$\mathbb{Q}_0^{(a,A_1)}$	M_1	$\begin{pmatrix} \frac{\sqrt{6}}{6} & 0 & 0 & 0 & 0 & 0 \\ 0 & \frac{\sqrt{6}}{6} & 0 & 0 & 0 & 0 \\ 0 & 0 & \frac{\sqrt{6}}{6} & 0 & 0 & 0 \\ 0 & 0 & 0 & \frac{\sqrt{6}}{6} & 0 & 0 \\ 0 & 0 & 0 & 0 & \frac{\sqrt{6}}{6} & 0 \\ 0 & 0 & 0 & 0 & 0 & \frac{\sqrt{6}}{6} \end{pmatrix}$
$\mathbb{X}_2$	$\mathbb{Q}_2^{(a,A_1,1)}$	M_1	$\begin{pmatrix} -\frac{\sqrt{3}}{6} & 0 & 0 & 0 & 0 & 0 \\ 0 & -\frac{\sqrt{3}}{6} & 0 & 0 & 0 & 0 \\ 0 & 0 & -\frac{\sqrt{3}}{6} & 0 & 0 & 0 \\ 0 & 0 & 0 & -\frac{\sqrt{3}}{6} & 0 & 0 \\ 0 & 0 & 0 & 0 & \frac{\sqrt{3}}{3} & 0 \\ 0 & 0 & 0 & 0 & 0 & \frac{\sqrt{3}}{3} \end{pmatrix}$
$\mathbb{X}_3$	$\mathbb{Q}_2^{(a,A_1,2)}$	M_1	$\begin{pmatrix} \frac{1}{2} & 0 & 0 & 0 & 0 & 0 \\ 0 & \frac{1}{2} & 0 & 0 & 0 & 0 \\ 0 & 0 & -\frac{1}{2} & 0 & 0 & 0 \\ 0 & 0 & 0 & -\frac{1}{2} & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 \end{pmatrix}$
$\mathbb{X}_4$	$\mathbb{Q}_0^{(a,A_1)}(1,1)$	M_1	$\begin{pmatrix} 0 & 0 & -\frac{\sqrt{3}i}{6} & 0 & 0 & \frac{\sqrt{3}}{6} \\ 0 & 0 & 0 & \frac{\sqrt{3}i}{6} & -\frac{\sqrt{3}}{6} & 0 \\ \frac{\sqrt{3}i}{6} & 0 & 0 & 0 & 0 & -\frac{\sqrt{3}i}{6} \\ 0 & -\frac{\sqrt{3}i}{6} & 0 & 0 & -\frac{\sqrt{3}i}{6} & 0 \\ 0 & -\frac{\sqrt{3}}{6} & 0 & \frac{\sqrt{3}i}{6} & 0 & 0 \\ \frac{\sqrt{3}}{6} & 0 & \frac{\sqrt{3}i}{6} & 0 & 0 & 0 \end{pmatrix}$
$\mathbb{X}_5$	$\mathbb{Q}_2^{(a,A_1,1)}(1,-1)$	M_1	$\begin{pmatrix} 0 & 0 & -\frac{\sqrt{6}i}{6} & 0 & 0 & -\frac{\sqrt{6}}{12} \\ 0 & 0 & 0 & \frac{\sqrt{6}i}{6} & \frac{\sqrt{6}}{12} & 0 \\ \frac{\sqrt{6}i}{6} & 0 & 0 & 0 & 0 & \frac{\sqrt{6}i}{12} \\ 0 & -\frac{\sqrt{6}i}{6} & 0 & 0 & \frac{\sqrt{6}i}{12} & 0 \\ 0 & \frac{\sqrt{6}}{12} & 0 & -\frac{\sqrt{6}i}{12} & 0 & 0 \\ -\frac{\sqrt{6}}{12} & 0 & -\frac{\sqrt{6}i}{12} & 0 & 0 & 0 \end{pmatrix}$

Table 6

symbol	type	group	form
$\mathbb{X}_6$	$\mathbb{Q}_2^{(a,A_1,2)}(1,-1)$	M_1	$\begin{pmatrix} 0 & 0 & 0 & 0 & 0 & -\frac{\sqrt{2}}{4} \\ 0 & 0 & 0 & 0 & \frac{\sqrt{2}}{4} & 0 \\ 0 & 0 & 0 & 0 & 0 & -\frac{\sqrt{2}i}{4} \\ 0 & 0 & 0 & 0 & -\frac{\sqrt{2}i}{4} & 0 \\ 0 & \frac{\sqrt{2}}{4} & 0 & \frac{\sqrt{2}i}{4} & 0 & 0 \\ -\frac{\sqrt{2}}{4} & 0 & \frac{\sqrt{2}i}{4} & 0 & 0 & 0 \end{pmatrix}$
$\mathbb{X}_7$	$\mathbb{Q}_2^{(a,A_2)}$	M_1	$\begin{pmatrix} 0 & 0 & \frac{1}{2} & 0 & 0 & 0 \\ 0 & 0 & 0 & \frac{1}{2} & 0 & 0 \\ \frac{1}{2} & 0 & 0 & 0 & 0 & 0 \\ 0 & \frac{1}{2} & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 \end{pmatrix}$
$\mathbb{X}_8$	$\mathbb{Q}_2^{(a,B_1)}$	M_1	$\begin{pmatrix} 0 & 0 & 0 & 0 & \frac{1}{2} & 0 \\ 0 & 0 & 0 & 0 & 0 & \frac{1}{2} \\ 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 \\ \frac{1}{2} & 0 & 0 & 0 & 0 & 0 \\ 0 & \frac{1}{2} & 0 & 0 & 0 & 0 \end{pmatrix}$
$\mathbb{X}_9$	$\mathbb{Q}_2^{(a,B_2)}$	M_1	$\begin{pmatrix} 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & \frac{1}{2} & 0 \\ 0 & 0 & 0 & 0 & 0 & \frac{1}{2} \\ 0 & 0 & \frac{1}{2} & 0 & 0 & 0 \\ 0 & 0 & 0 & \frac{1}{2} & 0 & 0 \end{pmatrix}$
$\mathbb{X}_{10}$	$\mathbb{Q}_2^{(a,A_2)}(1,-1)$	M_1	$\begin{pmatrix} 0 & 0 & 0 & 0 & 0 & \frac{\sqrt{2}i}{4} \\ 0 & 0 & 0 & 0 & \frac{\sqrt{2}i}{4} & 0 \\ 0 & 0 & 0 & 0 & 0 & -\frac{\sqrt{2}}{4} \\ 0 & 0 & 0 & 0 & \frac{\sqrt{2}}{4} & 0 \\ 0 & -\frac{\sqrt{2}i}{4} & 0 & \frac{\sqrt{2}}{4} & 0 & 0 \\ -\frac{\sqrt{2}i}{4} & 0 & -\frac{\sqrt{2}}{4} & 0 & 0 & 0 \end{pmatrix}$

Table 6

symbol	type	group	form
$\mathbb{X}_{11}$	$\mathbb{G}_1^{(a,A_2)}(1,0)$	M_1	$\begin{pmatrix} 0 & 0 & 0 & 0 & 0 & \frac{\sqrt{2}i}{4} \\ 0 & 0 & 0 & 0 & \frac{\sqrt{2}i}{4} & 0 \\ 0 & 0 & 0 & 0 & 0 & \frac{\sqrt{2}}{4} \\ 0 & 0 & 0 & 0 & -\frac{\sqrt{2}}{4} & 0 \\ 0 & -\frac{\sqrt{2}i}{4} & 0 & -\frac{\sqrt{2}}{4} & 0 & 0 \\ -\frac{\sqrt{2}i}{4} & 0 & \frac{\sqrt{2}}{4} & 0 & 0 & 0 \end{pmatrix}$
$\mathbb{X}_{12}$	$\mathbb{Q}_2^{(a,B_1)}(1,-1)$	M_1	$\begin{pmatrix} 0 & 0 & 0 & -\frac{\sqrt{2}i}{4} & 0 & 0 \\ 0 & 0 & -\frac{\sqrt{2}i}{4} & 0 & 0 & 0 \\ 0 & \frac{\sqrt{2}i}{4} & 0 & 0 & -\frac{\sqrt{2}i}{4} & 0 \\ \frac{\sqrt{2}i}{4} & 0 & 0 & 0 & 0 & \frac{\sqrt{2}i}{4} \\ 0 & 0 & \frac{\sqrt{2}i}{4} & 0 & 0 & 0 \\ 0 & 0 & 0 & -\frac{\sqrt{2}i}{4} & 0 & 0 \end{pmatrix}$
$\mathbb{X}_{13}$	$\mathbb{G}_1^{(a,B_1)}(1,0)$	M_1	$\begin{pmatrix} 0 & 0 & 0 & \frac{\sqrt{2}i}{4} & 0 & 0 \\ 0 & 0 & \frac{\sqrt{2}i}{4} & 0 & 0 & 0 \\ 0 & -\frac{\sqrt{2}i}{4} & 0 & 0 & -\frac{\sqrt{2}i}{4} & 0 \\ -\frac{\sqrt{2}i}{4} & 0 & 0 & 0 & 0 & \frac{\sqrt{2}i}{4} \\ 0 & 0 & \frac{\sqrt{2}i}{4} & 0 & 0 & 0 \\ 0 & 0 & 0 & -\frac{\sqrt{2}i}{4} & 0 & 0 \end{pmatrix}$
$\mathbb{X}_{14}$	$\mathbb{Q}_2^{(a,B_2)}(1,-1)$	M_1	$\begin{pmatrix} 0 & 0 & 0 & -\frac{\sqrt{2}}{4} & \frac{\sqrt{2}i}{4} & 0 \\ 0 & 0 & \frac{\sqrt{2}}{4} & 0 & 0 & -\frac{\sqrt{2}i}{4} \\ 0 & \frac{\sqrt{2}}{4} & 0 & 0 & 0 & 0 \\ -\frac{\sqrt{2}}{4} & 0 & 0 & 0 & 0 & 0 \\ -\frac{\sqrt{2}i}{4} & 0 & 0 & 0 & 0 & 0 \\ 0 & \frac{\sqrt{2}i}{4} & 0 & 0 & 0 & 0 \end{pmatrix}$
$\mathbb{X}_{15}$	$\mathbb{G}_1^{(a,B_2)}(1,0)$	M_1	$\begin{pmatrix} 0 & 0 & 0 & -\frac{\sqrt{2}}{4} & -\frac{\sqrt{2}i}{4} & 0 \\ 0 & 0 & \frac{\sqrt{2}}{4} & 0 & 0 & \frac{\sqrt{2}i}{4} \\ 0 & \frac{\sqrt{2}}{4} & 0 & 0 & 0 & 0 \\ -\frac{\sqrt{2}}{4} & 0 & 0 & 0 & 0 & 0 \\ \frac{\sqrt{2}i}{4} & 0 & 0 & 0 & 0 & 0 \\ 0 & -\frac{\sqrt{2}i}{4} & 0 & 0 & 0 & 0 \end{pmatrix}$

continued …

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Table 6

symbol	type	group	form
$\mathbb{X}_{16}$	$\mathbb{M}_1^{(a,A_2)}$	M_1	$\begin{pmatrix} 0 & 0 & -\frac{i}{2} & 0 & 0 & 0 \\ 0 & 0 & 0 & -\frac{i}{2} & 0 & 0 \\ \frac{i}{2} & 0 & 0 & 0 & 0 & 0 \\ 0 & \frac{i}{2} & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 \end{pmatrix}$
$\mathbb{X}_{17}$	$\mathbb{M}_1^{(a,B_1)}$	M_1	$\begin{pmatrix} 0 & 0 & 0 & 0 & \frac{i}{2} & 0 \\ 0 & 0 & 0 & 0 & 0 & \frac{i}{2} \\ 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 \\ -\frac{i}{2} & 0 & 0 & 0 & 0 & 0 \\ 0 & -\frac{i}{2} & 0 & 0 & 0 & 0 \end{pmatrix}$
$\mathbb{X}_{18}$	$\mathbb{M}_1^{(a,B_2)}$	M_1	$\begin{pmatrix} 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & -\frac{i}{2} & 0 \\ 0 & 0 & 0 & 0 & 0 & -\frac{i}{2} \\ 0 & 0 & \frac{i}{2} & 0 & 0 & 0 \\ 0 & 0 & 0 & \frac{i}{2} & 0 & 0 \end{pmatrix}$
$\mathbb{X}_{19}$	$\mathbb{M}_1^{(a,A_2)}(1,1)$	M_1	$\begin{pmatrix} -\frac{\sqrt{30}}{30} & 0 & 0 & 0 & 0 & \frac{\sqrt{30}}{20} \\ 0 & \frac{\sqrt{30}}{30} & 0 & 0 & \frac{\sqrt{30}}{20} & 0 \\ 0 & 0 & -\frac{\sqrt{30}}{30} & 0 & 0 & -\frac{\sqrt{30}i}{20} \\ 0 & 0 & 0 & \frac{\sqrt{30}}{30} & \frac{\sqrt{30}i}{20} & 0 \\ 0 & \frac{\sqrt{30}}{20} & 0 & -\frac{\sqrt{30}i}{20} & \frac{\sqrt{30}}{15} & 0 \\ \frac{\sqrt{30}}{20} & 0 & \frac{\sqrt{30}i}{20} & 0 & 0 & -\frac{\sqrt{30}}{15} \end{pmatrix}$
$\mathbb{X}_{20}$	$\mathbb{M}_1^{(a,A_2)}(1,-1)$	M_1	$\begin{pmatrix} \frac{\sqrt{6}}{6} & 0 & 0 & 0 & 0 & 0 \\ 0 & -\frac{\sqrt{6}}{6} & 0 & 0 & 0 & 0 \\ 0 & 0 & \frac{\sqrt{6}}{6} & 0 & 0 & 0 \\ 0 & 0 & 0 & -\frac{\sqrt{6}}{6} & 0 & 0 \\ 0 & 0 & 0 & 0 & \frac{\sqrt{6}}{6} & 0 \\ 0 & 0 & 0 & 0 & 0 & -\frac{\sqrt{6}}{6} \end{pmatrix}$

Table 6

symbol	type	group	form
$\mathbb{X}_{21}$	$\mathbb{M}_3^{(a,A_2,1)}(1,-1)$	M_1	$\begin{pmatrix} -\frac{\sqrt{5}}{10} & 0 & 0 & 0 & 0 & -\frac{\sqrt{5}}{10} \\ 0 & \frac{\sqrt{5}}{10} & 0 & 0 & -\frac{\sqrt{5}}{10} & 0 \\ 0 & 0 & -\frac{\sqrt{5}}{10} & 0 & 0 & \frac{\sqrt{5}i}{10} \\ 0 & 0 & 0 & \frac{\sqrt{5}}{10} & -\frac{\sqrt{5}i}{10} & 0 \\ 0 & -\frac{\sqrt{5}}{10} & 0 & \frac{\sqrt{5}i}{10} & \frac{\sqrt{5}}{5} & 0 \\ -\frac{\sqrt{5}}{10} & 0 & -\frac{\sqrt{5}i}{10} & 0 & 0 & -\frac{\sqrt{5}}{5} \end{pmatrix}$
$\mathbb{X}_{22}$	$\mathbb{M}_3^{(a,A_2,2)}(1,-1)$	M_1	$\begin{pmatrix} \frac{\sqrt{3}}{6} & 0 & 0 & 0 & 0 & \frac{\sqrt{3}}{6} \\ 0 & -\frac{\sqrt{3}}{6} & 0 & 0 & \frac{\sqrt{3}}{6} & 0 \\ 0 & 0 & -\frac{\sqrt{3}}{6} & 0 & 0 & \frac{\sqrt{3}i}{6} \\ 0 & 0 & 0 & \frac{\sqrt{3}}{6} & -\frac{\sqrt{3}i}{6} & 0 \\ 0 & \frac{\sqrt{3}}{6} & 0 & \frac{\sqrt{3}i}{6} & 0 & 0 \\ \frac{\sqrt{3}}{6} & 0 & -\frac{\sqrt{3}i}{6} & 0 & 0 & 0 \end{pmatrix}$
$\mathbb{X}_{23}$	$\mathbb{T}_2^{(a,A_2)}(1,0)$	M_1	$\begin{pmatrix} \frac{\sqrt{6}}{6} & 0 & 0 & 0 & 0 & -\frac{\sqrt{6}}{12} \\ 0 & -\frac{\sqrt{6}}{6} & 0 & 0 & -\frac{\sqrt{6}}{12} & 0 \\ 0 & 0 & -\frac{\sqrt{6}}{6} & 0 & 0 & -\frac{\sqrt{6}i}{12} \\ 0 & 0 & 0 & \frac{\sqrt{6}}{6} & \frac{\sqrt{6}i}{12} & 0 \\ 0 & -\frac{\sqrt{6}}{12} & 0 & -\frac{\sqrt{6}i}{12} & 0 & 0 \\ -\frac{\sqrt{6}}{12} & 0 & \frac{\sqrt{6}i}{12} & 0 & 0 & 0 \end{pmatrix}$
$\mathbb{X}_{24}$	$\mathbb{M}_1^{(a,B_1)}(1,1)$	M_1	$\begin{pmatrix} 0 & \frac{\sqrt{30}i}{30} & 0 & \frac{\sqrt{30}}{20} & 0 & 0 \\ -\frac{\sqrt{30}i}{30} & 0 & \frac{\sqrt{30}}{20} & 0 & 0 & 0 \\ 0 & \frac{\sqrt{30}}{20} & 0 & -\frac{\sqrt{30}i}{15} & \frac{\sqrt{30}}{20} & 0 \\ \frac{\sqrt{30}}{20} & 0 & \frac{\sqrt{30}i}{15} & 0 & 0 & -\frac{\sqrt{30}}{20} \\ 0 & 0 & \frac{\sqrt{30}}{20} & 0 & 0 & \frac{\sqrt{30}i}{30} \\ 0 & 0 & 0 & -\frac{\sqrt{30}}{20} & -\frac{\sqrt{30}i}{30} & 0 \end{pmatrix}$
$\mathbb{X}_{25}$	$\mathbb{M}_1^{(a,B_1)}(1,-1)$	M_1	$\begin{pmatrix} 0 & -\frac{\sqrt{6}i}{6} & 0 & 0 & 0 & 0 \\ \frac{\sqrt{6}i}{6} & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & -\frac{\sqrt{6}i}{6} & 0 & 0 \\ 0 & 0 & \frac{\sqrt{6}i}{6} & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & -\frac{\sqrt{6}i}{6} \\ 0 & 0 & 0 & 0 & \frac{\sqrt{6}i}{6} & 0 \end{pmatrix}$

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Table 6

symbol	type	group	form
$\mathbb{X}_{26}$	$\mathbb{M}_3^{(a,B_1,1)}(1,-1)$	M_1	$\begin{pmatrix} 0 & \frac{\sqrt{5}i}{10} & 0 & -\frac{\sqrt{5}}{10} & 0 & 0 \\ -\frac{\sqrt{5}i}{10} & 0 & -\frac{\sqrt{5}}{10} & 0 & 0 & 0 \\ 0 & -\frac{\sqrt{5}}{10} & 0 & -\frac{\sqrt{5}}{5} & -\frac{\sqrt{5}}{10} & 0 \\ -\frac{\sqrt{5}}{10} & 0 & \frac{\sqrt{5}i}{5} & 0 & 0 & \frac{\sqrt{5}}{10} \\ 0 & 0 & -\frac{\sqrt{5}}{10} & 0 & 0 & \frac{\sqrt{5}i}{10} \\ 0 & 0 & 0 & \frac{\sqrt{5}}{10} & -\frac{\sqrt{5}i}{10} & 0 \end{pmatrix}$
$\mathbb{X}_{27}$	$\mathbb{M}_3^{(a,B_1,2)}(1,-1)$	M_1	$\begin{pmatrix} 0 & \frac{\sqrt{3}i}{6} & 0 & -\frac{\sqrt{3}}{6} & 0 & 0 \\ -\frac{\sqrt{3}i}{6} & 0 & -\frac{\sqrt{3}}{6} & 0 & 0 & 0 \\ 0 & -\frac{\sqrt{3}}{6} & 0 & 0 & \frac{\sqrt{3}}{6} & 0 \\ -\frac{\sqrt{3}}{6} & 0 & 0 & 0 & 0 & -\frac{\sqrt{3}}{6} \\ 0 & 0 & \frac{\sqrt{3}}{6} & 0 & 0 & -\frac{\sqrt{3}i}{6} \\ 0 & 0 & 0 & -\frac{\sqrt{3}}{6} & \frac{\sqrt{3}i}{6} & 0 \end{pmatrix}$
$\mathbb{X}_{28}$	$\mathbb{T}_2^{(a,B_1)}(1,0)$	M_1	$\begin{pmatrix} 0 & \frac{\sqrt{6}i}{6} & 0 & \frac{\sqrt{6}}{12} & 0 & 0 \\ -\frac{\sqrt{6}i}{6} & 0 & \frac{\sqrt{6}}{12} & 0 & 0 & 0 \\ 0 & \frac{\sqrt{6}}{12} & 0 & 0 & -\frac{\sqrt{6}}{12} & 0 \\ \frac{\sqrt{6}}{12} & 0 & 0 & 0 & 0 & \frac{\sqrt{6}}{12} \\ 0 & 0 & -\frac{\sqrt{6}}{12} & 0 & 0 & -\frac{\sqrt{6}i}{6} \\ 0 & 0 & 0 & \frac{\sqrt{6}}{12} & \frac{\sqrt{6}i}{6} & 0 \end{pmatrix}$
$\mathbb{X}_{29}$	$\mathbb{M}_1^{(a,B_2)}(1,1)$	M_1	$\begin{pmatrix} 0 & \frac{\sqrt{30}}{15} & 0 & -\frac{\sqrt{30}i}{20} & \frac{\sqrt{30}}{20} & 0 \\ \frac{\sqrt{30}}{15} & 0 & \frac{\sqrt{30}i}{20} & 0 & 0 & -\frac{\sqrt{30}}{20} \\ 0 & -\frac{\sqrt{30}i}{20} & 0 & -\frac{\sqrt{30}}{30} & 0 & 0 \\ \frac{\sqrt{30}i}{20} & 0 & -\frac{\sqrt{30}}{30} & 0 & 0 & 0 \\ -\frac{\sqrt{30}}{20} & 0 & 0 & 0 & 0 & -\frac{\sqrt{30}}{30} \\ 0 & -\frac{\sqrt{30}}{20} & 0 & 0 & -\frac{\sqrt{30}}{30} & 0 \end{pmatrix}$
$\mathbb{X}_{30}$	$\mathbb{M}_1^{(a,B_2)}(1,-1)$	M_1	$\begin{pmatrix} 0 & \frac{\sqrt{6}}{6} & 0 & 0 & 0 & 0 \\ \frac{\sqrt{6}}{6} & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & \frac{\sqrt{6}}{6} & 0 & 0 \\ 0 & 0 & \frac{\sqrt{6}}{6} & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & \frac{\sqrt{6}}{6} \\ 0 & 0 & 0 & 0 & \frac{\sqrt{6}}{6} & 0 \end{pmatrix}$

continued ...

Table 6

symbol	type	group	form
$\mathbb{X}_{31}$	$\mathbb{M}_3^{(a,B_2,1)}(1,-1)$	M_1	$\begin{pmatrix} 0 & \frac{\sqrt{5}}{5} & 0 & \frac{\sqrt{5}i}{10} & -\frac{\sqrt{5}}{10} & 0 \\ \frac{\sqrt{5}}{5} & 0 & -\frac{\sqrt{5}i}{10} & 0 & 0 & \frac{\sqrt{5}}{10} \\ 0 & \frac{\sqrt{5}i}{10} & 0 & -\frac{\sqrt{5}}{10} & 0 & 0 \\ -\frac{\sqrt{5}i}{10} & 0 & -\frac{\sqrt{5}}{10} & 0 & 0 & 0 \\ -\frac{\sqrt{5}}{10} & 0 & 0 & 0 & 0 & -\frac{\sqrt{5}}{10} \\ 0 & \frac{\sqrt{5}}{10} & 0 & 0 & -\frac{\sqrt{5}}{10} & 0 \end{pmatrix}$
$\mathbb{X}_{32}$	$\mathbb{M}_3^{(a,B_2,2)}(1,-1)$	M_1	$\begin{pmatrix} 0 & 0 & 0 & -\frac{\sqrt{3}i}{6} & -\frac{\sqrt{3}}{6} & 0 \\ 0 & 0 & \frac{\sqrt{3}i}{6} & 0 & 0 & \frac{\sqrt{3}}{6} \\ 0 & -\frac{\sqrt{3}i}{6} & 0 & \frac{\sqrt{3}}{6} & 0 & 0 \\ \frac{\sqrt{3}i}{6} & 0 & \frac{\sqrt{3}}{6} & 0 & 0 & 0 \\ -\frac{\sqrt{3}}{6} & 0 & 0 & 0 & 0 & -\frac{\sqrt{3}}{6} \\ 0 & \frac{\sqrt{3}}{6} & 0 & 0 & -\frac{\sqrt{3}}{6} & 0 \end{pmatrix}$
$\mathbb{X}_{33}$	$\mathbb{T}_2^{(a,B_2)}(1,0)$	M_1	$\begin{pmatrix} 0 & 0 & 0 & \frac{\sqrt{6}i}{12} & \frac{\sqrt{6}}{12} & 0 \\ 0 & 0 & -\frac{\sqrt{6}i}{12} & 0 & 0 & -\frac{\sqrt{6}}{12} \\ 0 & \frac{\sqrt{6}i}{12} & 0 & \frac{\sqrt{6}}{6} & 0 & 0 \\ -\frac{\sqrt{6}i}{12} & 0 & \frac{\sqrt{6}}{6} & 0 & 0 & 0 \\ \frac{\sqrt{6}}{12} & 0 & 0 & 0 & 0 & -\frac{\sqrt{6}}{6} \\ 0 & -\frac{\sqrt{6}}{12} & 0 & 0 & -\frac{\sqrt{6}}{6} & 0 \end{pmatrix}$
$\mathbb{X}_{34}$	$\mathbb{M}_3^{(a,A_1)}(1,-1)$	M_1	$\begin{pmatrix} 0 & 0 & \frac{\sqrt{3}}{6} & 0 & 0 & -\frac{\sqrt{3}i}{6} \\ 0 & 0 & 0 & -\frac{\sqrt{3}}{6} & \frac{\sqrt{3}i}{6} & 0 \\ \frac{\sqrt{3}}{6} & 0 & 0 & 0 & 0 & \frac{\sqrt{3}}{6} \\ 0 & -\frac{\sqrt{3}}{6} & 0 & 0 & \frac{\sqrt{3}}{6} & 0 \\ 0 & -\frac{\sqrt{3}i}{6} & 0 & \frac{\sqrt{3}}{6} & 0 & 0 \\ \frac{\sqrt{3}i}{6} & 0 & \frac{\sqrt{3}}{6} & 0 & 0 & 0 \end{pmatrix}$
$\mathbb{X}_{35}$	$\mathbb{T}_2^{(a,A_1,1)}(1,0)$	M_1	$\begin{pmatrix} 0 & 0 & 0 & 0 & 0 & \frac{\sqrt{2}i}{4} \\ 0 & 0 & 0 & 0 & -\frac{\sqrt{2}i}{4} & 0 \\ 0 & 0 & 0 & 0 & 0 & \frac{\sqrt{2}}{4} \\ 0 & 0 & 0 & 0 & \frac{\sqrt{2}}{4} & 0 \\ 0 & \frac{\sqrt{2}i}{4} & 0 & \frac{\sqrt{2}}{4} & 0 & 0 \\ -\frac{\sqrt{2}i}{4} & 0 & \frac{\sqrt{2}}{4} & 0 & 0 & 0 \end{pmatrix}$

continued ...

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Table 6

symbol	type	group	form
$\mathbb{X}_{36}$	$\mathbb{T}_2^{(a,A_1,2)}(1,0)$	M_1	$\begin{pmatrix} 0 & 0 & -\frac{\sqrt{6}}{6} & 0 & 0 & -\frac{\sqrt{6}i}{12} \\ 0 & 0 & 0 & \frac{\sqrt{6}}{6} & \frac{\sqrt{6}i}{12} & 0 \\ -\frac{\sqrt{6}}{6} & 0 & 0 & 0 & 0 & \frac{\sqrt{6}}{12} \\ 0 & \frac{\sqrt{6}}{6} & 0 & 0 & \frac{\sqrt{6}}{12} & 0 \\ 0 & -\frac{\sqrt{6}i}{12} & 0 & \frac{\sqrt{6}}{12} & 0 & 0 \\ \frac{\sqrt{6}i}{12} & 0 & \frac{\sqrt{6}}{12} & 0 & 0 & 0 \end{pmatrix}$

Table 7: Cluster SAMB.

symbol	type	cluster	form
$\mathbb{Y}_1$	$\mathbb{Q}_0^{(s,A_1)}$	S_1	$\begin{pmatrix} \frac{\sqrt{2}}{2} & \frac{\sqrt{2}}{2} \end{pmatrix}$
$\mathbb{Y}_2$	$\mathbb{Q}_1^{(s,B_2)}$	S_1	$\begin{pmatrix} \frac{\sqrt{2}}{2} & -\frac{\sqrt{2}}{2} \end{pmatrix}$
$\mathbb{Y}_3$	$\mathbb{Q}_0^{(s,A_1)}$	S_2	$\begin{pmatrix} \frac{\sqrt{2}}{2} & \frac{\sqrt{2}}{2} \end{pmatrix}$
$\mathbb{Y}_4$	$\mathbb{Q}_1^{(s,B_2)}$	S_2	$\begin{pmatrix} \frac{\sqrt{2}}{2} & -\frac{\sqrt{2}}{2} \end{pmatrix}$
$\mathbb{Y}_5$	$\mathbb{Q}_0^{(b,A_1)}$	B_1	$\begin{pmatrix} \frac{\sqrt{2}}{2} & \frac{\sqrt{2}}{2} \end{pmatrix}$
$\mathbb{Y}_6$	$\mathbb{Q}_1^{(b,B_2)}$	B_1	$\begin{pmatrix} \frac{\sqrt{2}}{2} & -\frac{\sqrt{2}}{2} \end{pmatrix}$
$\mathbb{Y}_7$	$\mathbb{T}_0^{(b,A_1)}$	B_1	$\begin{pmatrix} \frac{\sqrt{2}i}{2} & \frac{\sqrt{2}i}{2} \end{pmatrix}$
$\mathbb{Y}_8$	$\mathbb{T}_1^{(b,B_2)}$	B_1	$\begin{pmatrix} \frac{\sqrt{2}i}{2} & -\frac{\sqrt{2}i}{2} \end{pmatrix}$
$\mathbb{Y}_9$	$\mathbb{Q}_0^{(b,A_1)}$	B_2	$\begin{pmatrix} \frac{1}{2} & \frac{1}{2} & \frac{1}{2} & \frac{1}{2} \end{pmatrix}$
$\mathbb{Y}_{10}$	$\mathbb{Q}_1^{(b,B_1)}$	B_2	$\begin{pmatrix} \frac{1}{2} & -\frac{1}{2} & \frac{1}{2} & -\frac{1}{2} \end{pmatrix}$
$\mathbb{Y}_{11}$	$\mathbb{Q}_1^{(b,B_2)}$	B_2	$\begin{pmatrix} \frac{1}{2} & -\frac{1}{2} & -\frac{1}{2} & \frac{1}{2} \end{pmatrix}$
$\mathbb{Y}_{12}$	$\mathbb{Q}_2^{(b,A_2)}$	B_2	$\begin{pmatrix} \frac{1}{2} & \frac{1}{2} & -\frac{1}{2} & -\frac{1}{2} \end{pmatrix}$
$\mathbb{Y}_{13}$	$\mathbb{T}_0^{(b,A_1)}$	B_2	$\begin{pmatrix} \frac{i}{2} & \frac{i}{2} & \frac{i}{2} & \frac{i}{2} \end{pmatrix}$
$\mathbb{Y}_{14}$	$\mathbb{T}_1^{(b,B_1)}$	B_2	$\begin{pmatrix} \frac{i}{2} & -\frac{i}{2} & \frac{i}{2} & -\frac{i}{2} \end{pmatrix}$
$\mathbb{Y}_{15}$	$\mathbb{T}_1^{(b,B_2)}$	B_2	$\begin{pmatrix} \frac{i}{2} & -\frac{i}{2} & -\frac{i}{2} & \frac{i}{2} \end{pmatrix}$
$\mathbb{Y}_{16}$	$\mathbb{T}_2^{(b,A_2)}$	B_2	$\begin{pmatrix} \frac{i}{2} & \frac{i}{2} & -\frac{i}{2} & -\frac{i}{2} \end{pmatrix}$
$\mathbb{Y}_{17}$	$\mathbb{Q}_0^{(b,A_1)}$	B_3	$\begin{pmatrix} \frac{1}{2} & \frac{1}{2} & \frac{1}{2} & \frac{1}{2} \end{pmatrix}$

continued ...

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Table 7

symbol	type	cluster	form			
$\mathbb{Y}_{18}$	$\mathbb{Q}_1^{(b,B_1)}$	B_3	$\frac{1}{2}$	$-\frac{1}{2}$	$\frac{1}{2}$	$-\frac{1}{2}$
$\mathbb{Y}_{19}$	$\mathbb{Q}_1^{(b,B_2)}$	B_3	$\frac{1}{2}$	$-\frac{1}{2}$	$-\frac{1}{2}$	$\frac{1}{2}$
$\mathbb{Y}_{20}$	$\mathbb{Q}_2^{(b,A_2)}$	B_3	$\frac{1}{2}$	$\frac{1}{2}$	$-\frac{1}{2}$	$-\frac{1}{2}$
$\mathbb{Y}_{21}$	$\mathbb{T}_0^{(b,A_1)}$	B_3	$\frac{i}{2}$	$-\frac{i}{2}$	$-\frac{i}{2}$	$\frac{i}{2}$
$\mathbb{Y}_{22}$	$\mathbb{T}_1^{(b,B_1)}$	B_3	$\frac{i}{2}$	$\frac{i}{2}$	$-\frac{i}{2}$	$-\frac{i}{2}$
$\mathbb{Y}_{23}$	$\mathbb{T}_1^{(b,B_2)}$	B_3	$\frac{i}{2}$	$\frac{i}{2}$	$\frac{i}{2}$	$\frac{i}{2}$
$\mathbb{Y}_{24}$	$\mathbb{T}_2^{(b,A_2)}$	B_3	$\frac{i}{2}$	$-\frac{i}{2}$	$\frac{i}{2}$	$-\frac{i}{2}$
$\mathbb{Y}_{25}$	$\mathbb{Q}_0^{(b,A_1)}$	B_4	$\frac{1}{2}$	$\frac{1}{2}$	$\frac{1}{2}$	$\frac{1}{2}$
$\mathbb{Y}_{26}$	$\mathbb{Q}_1^{(b,B_1)}$	B_4	$\frac{1}{2}$	$-\frac{1}{2}$	$\frac{1}{2}$	$-\frac{1}{2}$
$\mathbb{Y}_{27}$	$\mathbb{Q}_1^{(b,B_2)}$	B_4	$\frac{1}{2}$	$-\frac{1}{2}$	$-\frac{1}{2}$	$\frac{1}{2}$
$\mathbb{Y}_{28}$	$\mathbb{Q}_2^{(b,A_2)}$	B_4	$\frac{1}{2}$	$\frac{1}{2}$	$-\frac{1}{2}$	$-\frac{1}{2}$
$\mathbb{Y}_{29}$	$\mathbb{T}_0^{(b,A_1)}$	B_4	$\frac{i}{2}$	$-\frac{i}{2}$	$-\frac{i}{2}$	$\frac{i}{2}$
$\mathbb{Y}_{30}$	$\mathbb{T}_1^{(b,B_1)}$	B_4	$\frac{i}{2}$	$\frac{i}{2}$	$-\frac{i}{2}$	$-\frac{i}{2}$
$\mathbb{Y}_{31}$	$\mathbb{T}_1^{(b,B_2)}$	B_4	$\frac{i}{2}$	$\frac{i}{2}$	$\frac{i}{2}$	$\frac{i}{2}$
$\mathbb{Y}_{32}$	$\mathbb{T}_2^{(b,A_2)}$	B_4	$\frac{i}{2}$	$-\frac{i}{2}$	$\frac{i}{2}$	$-\frac{i}{2}$

Table 8: Polar harmonics.

No.	symbol	rank	irrep.	mul.	comp.	form
1	$\mathbb{Q}_0^{(A_1)}$	0	A_1	–	–	1
2	$\mathbb{Q}_1^{(B_1)}$	1	B_1	–	–	x
3	$\mathbb{Q}_1^{(B_2)}$	1	B_2	–	–	y
4	$\mathbb{Q}_2^{(A_1,1)}$	2	A_1	1	–	$-\frac{x^2}{2}-\frac{y^2}{2}+z^2$
5	$\mathbb{Q}_2^{(A_1,2)}$	2	A_1	2	–	$\frac{\sqrt{3}(x-y)(x+y)}{2}$
6	$\mathbb{Q}_2^{(A_2)}$	2	A_2	–	–	$\sqrt{3}xy$

continued ...

Table 8

No.	symbol	rank	irrep.	mul.	comp.	form
7	$\mathbb{Q}_2^{(B_1)}$	2	B_1	–	–	$\sqrt{3}xz$
8	$\mathbb{Q}_2^{(B_2)}$	2	B_2	–	–	$\sqrt{3}yz$

Table 9: Axial harmonics.

No.	symbol	rank	irrep.	mul.	comp.	form
1	$\mathbb{G}_1^{(A_2)}$	1	A_2	–	–	Z
2	$\mathbb{G}_1^{(B_1)}$	1	B_1	–	–	Y
3	$\mathbb{G}_1^{(B_2)}$	1	B_2	–	–	X
4	$\mathbb{G}_3^{(A_1)}$	3	A_1	–	–	$\sqrt{15}XYZ$
5	$\mathbb{G}_3^{(A_2,1)}$	3	A_2	1	–	$-\frac{Z(3X^2+3Y^2-2Z^2)}{2}$
6	$\mathbb{G}_3^{(A_2,2)}$	3	A_2	2	–	$\frac{\sqrt{15}Z(X-Y)(X+Y)}{2}$
7	$\mathbb{G}_3^{(B_1,1)}$	3	B_1	1	–	$-\frac{Y(3X^2-2Y^2+3Z^2)}{2}$
8	$\mathbb{G}_3^{(B_1,2)}$	3	B_1	2	–	$-\frac{\sqrt{15}Y(X-Z)(X+Z)}{2}$
9	$\mathbb{G}_3^{(B_2,1)}$	3	B_2	1	–	$\frac{X(2X^2-3Y^2-3Z^2)}{2}$
10	$\mathbb{G}_3^{(B_2,2)}$	3	B_2	2	–	$\frac{\sqrt{15}X(Y-Z)(Y+Z)}{2}$

- Group info.: Generator = $\{2_{001}|\frac{1}{2}0\frac{1}{2}\}$, $\{m_{010}|\frac{1}{2}0\frac{1}{2}\}$

Table 10: Conjugacy class (point-group part).

rep. SO	symmetry operations
$\{1\|0\}$	$\{1\|0\}$
$\{2_{001}\|\frac{1}{2}0\frac{1}{2}\}$	$\{2_{001}\|\frac{1}{2}0\frac{1}{2}\}$

continued ...

Table 10

rep. SO	symmetry operations
$\{m_{010}|\frac{1}{2}0\frac{1}{2}\}$	$\{m_{010}|\frac{1}{2}0\frac{1}{2}\}$
$\{m_{100}|0\}$	$\{m_{100}|0\}$

Table 11: Symmetry operations.

No.	SO	No.	SO	No.	SO	No.	SO	No.	SO
1	$\{1|0\}$	2	$\{2_{001}|\frac{1}{2}0\frac{1}{2}\}$	3	$\{m_{010}|\frac{1}{2}0\frac{1}{2}\}$	4	$\{m_{100}|0\}$		

Table 12: Character table (point-group part).

	1	2_{001}	m_{010}	m_{100}
A_1	1	1	1	1
A_2	1	1	-1	-1
B_1	1	-1	1	-1
B_2	1	-1	-1	1

Table 13: Parity conversion.

$\leftrightarrow$	$\leftrightarrow$	$\leftrightarrow$	$\leftrightarrow$
A_1 (A_2)	B_2 (B_1)	B_1 (B_2)	A_2 (A_1)

Table 14: Symmetric product, $[\Gamma \otimes \Gamma']_+$.

	A_1	A_2	B_1	B_2
A_1	A_1	A_2	B_1	B_2
A_2		A_1	B_2	B_1
B_1			A_1	A_2
B_2				A_1

Table 15: Anti-symmetric product, $[\Gamma \otimes \Gamma]_-$.

A_1	A_2	B_1	B_2
$-$	$-$	$-$	$-$

Table 16: Virtual-cluster sites.

No.	position	No.	position	No.	position	No.	position
1	$\begin{pmatrix} 1 & 1 & 0 \end{pmatrix}$	2	$\begin{pmatrix} -1 & -1 & 0 \end{pmatrix}$	3	$\begin{pmatrix} 1 & -1 & 0 \end{pmatrix}$	4	$\begin{pmatrix} -1 & 1 & 0 \end{pmatrix}$

Table 17: Virtual-cluster basis.

symbol	1	2	3	4
$\mathbb{Q}_0^{(A_1)}$	$\frac{1}{2}$	$\frac{1}{2}$	$\frac{1}{2}$	$\frac{1}{2}$
$\mathbb{Q}_1^{(B_1)}$	$\frac{1}{2}$	$-\frac{1}{2}$	$\frac{1}{2}$	$-\frac{1}{2}$
$\mathbb{Q}_1^{(B_2)}$	$\frac{1}{2}$	$-\frac{1}{2}$	$-\frac{1}{2}$	$\frac{1}{2}$
$\mathbb{Q}_2^{(A_2)}$	$\frac{1}{2}$	$\frac{1}{2}$	$-\frac{1}{2}$	$-\frac{1}{2}$