

SG No. 98  $D_4^{10}$   $I4_122$  [ tetragonal ]

\* plus set:  $+ [0, 0, 0], + [\frac{1}{2}, \frac{1}{2}, \frac{1}{2}]$

\* Wyckoff site: **4a**, site symmetry: **2.22**

Table 1: Wyckoff bond: **4a@4a**

| No. | vector       | center                          | mapping          |
|-----|--------------|---------------------------------|------------------|
| 1   | $[X, X, 0]$  | $[0, 0, 0]$                     | $[1, -2, 7, -8]$ |
| 2   | $[-X, X, 0]$ | $[0, \frac{1}{2}, \frac{1}{4}]$ | $[3, -4, 5, -6]$ |

Table 2: Wyckoff bond: **4b@4a**

| No. | vector       | center                          | mapping          |
|-----|--------------|---------------------------------|------------------|
| 1   | $[X, -X, 0]$ | $[0, 0, 0]$                     | $[1, -2, -7, 8]$ |
| 2   | $[X, X, 0]$  | $[0, \frac{1}{2}, \frac{1}{4}]$ | $[3, -4, -5, 6]$ |

Table 3: Wyckoff bond: **4c@4a**

| No. | vector      | center                          | mapping          |
|-----|-------------|---------------------------------|------------------|
| 1   | $[0, 0, Z]$ | $[0, 0, 0]$                     | $[1, 2, -7, -8]$ |
| 2   | $[0, 0, Z]$ | $[0, \frac{1}{2}, \frac{1}{4}]$ | $[3, 4, -5, -6]$ |

Table 4: Wyckoff bond: **8d@4a**

| No. | vector        | center                          | mapping   |
|-----|---------------|---------------------------------|-----------|
| 1   | $[X, X, Z]$   | $[0, 0, 0]$                     | $[1, -8]$ |
| 2   | $[-X, -X, Z]$ | $[0, 0, 0]$                     | $[2, -7]$ |
| 3   | $[-X, X, Z]$  | $[0, \frac{1}{2}, \frac{1}{4}]$ | $[3, -6]$ |
| 4   | $[X, -X, Z]$  | $[0, \frac{1}{2}, \frac{1}{4}]$ | $[4, -5]$ |

Table 5: Wyckoff bond: **8e@4a**

| No. | vector        | center                          | mapping   |
|-----|---------------|---------------------------------|-----------|
| 1   | $[X, -X, Z]$  | $[0, 0, 0]$                     | $[1, -7]$ |
| 2   | $[-X, X, Z]$  | $[0, 0, 0]$                     | $[2, -8]$ |
| 3   | $[X, X, Z]$   | $[0, \frac{1}{2}, \frac{1}{4}]$ | $[3, -5]$ |
| 4   | $[-X, -X, Z]$ | $[0, \frac{1}{2}, \frac{1}{4}]$ | $[4, -6]$ |

Table 6: Wyckoff bond: **8f@4a**

| No. | vector       | center                          | mapping   |
|-----|--------------|---------------------------------|-----------|
| 1   | $[X, Y, 0]$  | $[0, 0, 0]$                     | $[1, -2]$ |
| 2   | $[-Y, X, 0]$ | $[0, \frac{1}{2}, \frac{1}{4}]$ | $[3, -4]$ |
| 3   | $[-X, Y, 0]$ | $[0, \frac{1}{2}, \frac{1}{4}]$ | $[5, -6]$ |
| 4   | $[Y, X, 0]$  | $[0, 0, 0]$                     | $[7, -8]$ |

Table 7: Wyckoff bond: **16g@4a**

| No. | vector         | center                          | mapping |
|-----|----------------|---------------------------------|---------|
| 1   | $[X, Y, Z]$    | $[0, 0, 0]$                     | $[1]$   |
| 2   | $[-X, -Y, Z]$  | $[0, 0, 0]$                     | $[2]$   |
| 3   | $[-Y, X, Z]$   | $[0, \frac{1}{2}, \frac{1}{4}]$ | $[3]$   |
| 4   | $[Y, -X, Z]$   | $[0, \frac{1}{2}, \frac{1}{4}]$ | $[4]$   |
| 5   | $[-X, Y, -Z]$  | $[0, \frac{1}{2}, \frac{1}{4}]$ | $[5]$   |
| 6   | $[X, -Y, -Z]$  | $[0, \frac{1}{2}, \frac{1}{4}]$ | $[6]$   |
| 7   | $[Y, X, -Z]$   | $[0, 0, 0]$                     | $[7]$   |
| 8   | $[-Y, -X, -Z]$ | $[0, 0, 0]$                     | $[8]$   |

\* Wyckoff site: **4b**, site symmetry: **2.22**

Table 8: Wyckoff bond: **4a@4b**

| No. | vector       | center                          | mapping          |
|-----|--------------|---------------------------------|------------------|
| 1   | $[X, X, 0]$  | $[0, 0, \frac{1}{2}]$           | $[1, -2, 7, -8]$ |
| 2   | $[-X, X, 0]$ | $[0, \frac{1}{2}, \frac{3}{4}]$ | $[3, -4, 5, -6]$ |

Table 9: Wyckoff bond: **4b@4b**

| No. | vector       | center                          | mapping          |
|-----|--------------|---------------------------------|------------------|
| 1   | $[X, -X, 0]$ | $[0, 0, \frac{1}{2}]$           | $[1, -2, -7, 8]$ |
| 2   | $[X, X, 0]$  | $[0, \frac{1}{2}, \frac{3}{4}]$ | $[3, -4, -5, 6]$ |

Table 10: Wyckoff bond: **4c@4b**

| No. | vector      | center                          | mapping          |
|-----|-------------|---------------------------------|------------------|
| 1   | $[0, 0, Z]$ | $[0, 0, \frac{1}{2}]$           | $[1, 2, -7, -8]$ |
| 2   | $[0, 0, Z]$ | $[0, \frac{1}{2}, \frac{3}{4}]$ | $[3, 4, -5, -6]$ |

Table 11: Wyckoff bond: **8d@4b**

| No. | vector        | center                          | mapping   |
|-----|---------------|---------------------------------|-----------|
| 1   | $[X, X, Z]$   | $[0, 0, \frac{1}{2}]$           | $[1, -8]$ |
| 2   | $[-X, -X, Z]$ | $[0, 0, \frac{1}{2}]$           | $[2, -7]$ |
| 3   | $[-X, X, Z]$  | $[0, \frac{1}{2}, \frac{3}{4}]$ | $[3, -6]$ |
| 4   | $[X, -X, Z]$  | $[0, \frac{1}{2}, \frac{3}{4}]$ | $[4, -5]$ |

Table 12: Wyckoff bond: **8e@4b**

| No. | vector        | center                          | mapping   |
|-----|---------------|---------------------------------|-----------|
| 1   | $[X, -X, Z]$  | $[0, 0, \frac{1}{2}]$           | $[1, -7]$ |
| 2   | $[-X, X, Z]$  | $[0, 0, \frac{1}{2}]$           | $[2, -8]$ |
| 3   | $[X, X, Z]$   | $[0, \frac{1}{2}, \frac{3}{4}]$ | $[3, -5]$ |
| 4   | $[-X, -X, Z]$ | $[0, \frac{1}{2}, \frac{3}{4}]$ | $[4, -6]$ |

Table 13: Wyckoff bond: **8f@4b**

| No. | vector       | center                          | mapping   |
|-----|--------------|---------------------------------|-----------|
| 1   | $[X, Y, 0]$  | $[0, 0, \frac{1}{2}]$           | $[1, -2]$ |
| 2   | $[-Y, X, 0]$ | $[0, \frac{1}{2}, \frac{3}{4}]$ | $[3, -4]$ |
| 3   | $[-X, Y, 0]$ | $[0, \frac{1}{2}, \frac{3}{4}]$ | $[5, -6]$ |
| 4   | $[Y, X, 0]$  | $[0, 0, \frac{1}{2}]$           | $[7, -8]$ |

Table 14: Wyckoff bond: **16g@4b**

| No. | vector         | center                          | mapping |
|-----|----------------|---------------------------------|---------|
| 1   | $[X, Y, Z]$    | $[0, 0, \frac{1}{2}]$           | $[1]$   |
| 2   | $[-X, -Y, Z]$  | $[0, 0, \frac{1}{2}]$           | $[2]$   |
| 3   | $[-Y, X, Z]$   | $[0, \frac{1}{2}, \frac{3}{4}]$ | $[3]$   |
| 4   | $[Y, -X, Z]$   | $[0, \frac{1}{2}, \frac{3}{4}]$ | $[4]$   |
| 5   | $[-X, Y, -Z]$  | $[0, \frac{1}{2}, \frac{3}{4}]$ | $[5]$   |
| 6   | $[X, -Y, -Z]$  | $[0, \frac{1}{2}, \frac{3}{4}]$ | $[6]$   |
| 7   | $[Y, X, -Z]$   | $[0, 0, \frac{1}{2}]$           | $[7]$   |
| 8   | $[-Y, -X, -Z]$ | $[0, 0, \frac{1}{2}]$           | $[8]$   |

\* Wyckoff site: **8c**, site symmetry: **2** . .

Table 15: Wyckoff bond: **8a@8c**

| No. | vector       | center                                        | mapping   |
|-----|--------------|-----------------------------------------------|-----------|
| 1   | $[X, Y, 0]$  | $[0, 0, z]$                                   | $[1, -2]$ |
| 2   | $[-Y, X, 0]$ | $[0, \frac{1}{2}, z + \frac{1}{4}]$           | $[3, -4]$ |
| 3   | $[-X, Y, 0]$ | $[\frac{1}{2}, 0, \frac{3}{4} - z]$           | $[5, -6]$ |
| 4   | $[Y, X, 0]$  | $[\frac{1}{2}, \frac{1}{2}, \frac{1}{2} - z]$ | $[7, -8]$ |

Table 16: Wyckoff bond: **8b@8c**

| No. | vector       | center                                        | mapping  |
|-----|--------------|-----------------------------------------------|----------|
| 1   | $[0, 0, Z]$  | $[0, 0, z]$                                   | $[1, 2]$ |
| 2   | $[0, 0, Z]$  | $[0, \frac{1}{2}, z + \frac{1}{4}]$           | $[3, 4]$ |
| 3   | $[0, 0, -Z]$ | $[\frac{1}{2}, 0, \frac{3}{4} - z]$           | $[5, 6]$ |
| 4   | $[0, 0, -Z]$ | $[\frac{1}{2}, \frac{1}{2}, \frac{1}{2} - z]$ | $[7, 8]$ |

Table 17: Wyckoff bond: **16c@8c**

| No. | vector         | center                                        | mapping |
|-----|----------------|-----------------------------------------------|---------|
| 1   | $[X, Y, Z]$    | $[0, 0, z]$                                   | $[1]$   |
| 2   | $[-X, -Y, Z]$  | $[0, 0, z]$                                   | $[2]$   |
| 3   | $[-Y, X, Z]$   | $[0, \frac{1}{2}, z + \frac{1}{4}]$           | $[3]$   |
| 4   | $[Y, -X, Z]$   | $[0, \frac{1}{2}, z + \frac{1}{4}]$           | $[4]$   |
| 5   | $[-X, Y, -Z]$  | $[\frac{1}{2}, 0, \frac{3}{4} - z]$           | $[5]$   |
| 6   | $[X, -Y, -Z]$  | $[\frac{1}{2}, 0, \frac{3}{4} - z]$           | $[6]$   |
| 7   | $[Y, X, -Z]$   | $[\frac{1}{2}, \frac{1}{2}, \frac{1}{2} - z]$ | $[7]$   |
| 8   | $[-Y, -X, -Z]$ | $[\frac{1}{2}, \frac{1}{2}, \frac{1}{2} - z]$ | $[8]$   |

\* Wyckoff site: **8d**, site symmetry:  $\dots 2$

Table 18: Wyckoff bond: **8a@8d**

| No. | vector        | center                                            | mapping   |
|-----|---------------|---------------------------------------------------|-----------|
| 1   | $[X, -X, Z]$  | $[x, x, 0]$                                       | $[1, -7]$ |
| 2   | $[-X, X, Z]$  | $[\frac{1}{2} - x, \frac{1}{2} - x, \frac{1}{2}]$ | $[2, -8]$ |
| 3   | $[X, X, Z]$   | $[-x, x + \frac{1}{2}, \frac{1}{4}]$              | $[3, -5]$ |
| 4   | $[-X, -X, Z]$ | $[x + \frac{1}{2}, -x, \frac{3}{4}]$              | $[4, -6]$ |

Table 19: Wyckoff bond: **8b@8d**

| No. | vector        | center                                            | mapping  |
|-----|---------------|---------------------------------------------------|----------|
| 1   | $[X, X, 0]$   | $[x, x, 0]$                                       | $[1, 7]$ |
| 2   | $[-X, -X, 0]$ | $[\frac{1}{2} - x, \frac{1}{2} - x, \frac{1}{2}]$ | $[2, 8]$ |
| 3   | $[-X, X, 0]$  | $[-x, x + \frac{1}{2}, \frac{1}{4}]$              | $[3, 5]$ |
| 4   | $[X, -X, 0]$  | $[x + \frac{1}{2}, -x, \frac{3}{4}]$              | $[4, 6]$ |

Table 20: Wyckoff bond: **16c@8d**

| No. | vector         | center                                            | mapping |
|-----|----------------|---------------------------------------------------|---------|
| 1   | $[X, Y, Z]$    | $[x, x, 0]$                                       | $[1]$   |
| 2   | $[-X, -Y, Z]$  | $[\frac{1}{2} - x, \frac{1}{2} - x, \frac{1}{2}]$ | $[2]$   |
| 3   | $[-Y, X, Z]$   | $[-x, x + \frac{1}{2}, \frac{1}{4}]$              | $[3]$   |
| 4   | $[Y, -X, Z]$   | $[x + \frac{1}{2}, -x, \frac{3}{4}]$              | $[4]$   |
| 5   | $[-X, Y, -Z]$  | $[-x, x + \frac{1}{2}, \frac{1}{4}]$              | $[5]$   |
| 6   | $[X, -Y, -Z]$  | $[x + \frac{1}{2}, -x, \frac{3}{4}]$              | $[6]$   |
| 7   | $[Y, X, -Z]$   | $[x, x, 0]$                                       | $[7]$   |
| 8   | $[-Y, -X, -Z]$ | $[\frac{1}{2} - x, \frac{1}{2} - x, \frac{1}{2}]$ | $[8]$   |

\* Wyckoff site: **8e**, site symmetry:  $\dots 2$

Table 21: Wyckoff bond: **8a@8e**

| No. | vector        | center                                            | mapping   |
|-----|---------------|---------------------------------------------------|-----------|
| 1   | $[X, X, Z]$   | $[x, -x, 0]$                                      | $[1, -8]$ |
| 2   | $[-X, -X, Z]$ | $[\frac{1}{2} - x, x + \frac{1}{2}, \frac{1}{2}]$ | $[2, -7]$ |
| 3   | $[-X, X, Z]$  | $[x, x + \frac{1}{2}, \frac{1}{4}]$               | $[3, -6]$ |
| 4   | $[X, -X, Z]$  | $[\frac{1}{2} - x, -x, \frac{3}{4}]$              | $[4, -5]$ |

Table 22: Wyckoff bond: **8b@8e**

| No. | vector        | center                                            | mapping  |
|-----|---------------|---------------------------------------------------|----------|
| 1   | $[X, -X, 0]$  | $[x, -x, 0]$                                      | $[1, 8]$ |
| 2   | $[-X, X, 0]$  | $[\frac{1}{2} - x, x + \frac{1}{2}, \frac{1}{2}]$ | $[2, 7]$ |
| 3   | $[X, X, 0]$   | $[x, x + \frac{1}{2}, \frac{1}{4}]$               | $[3, 6]$ |
| 4   | $[-X, -X, 0]$ | $[\frac{1}{2} - x, -x, \frac{3}{4}]$              | $[4, 5]$ |

Table 23: Wyckoff bond: **16c@8e**

| No. | vector         | center                                            | mapping |
|-----|----------------|---------------------------------------------------|---------|
| 1   | $[X, Y, Z]$    | $[x, -x, 0]$                                      | [1]     |
| 2   | $[-X, -Y, Z]$  | $[\frac{1}{2} - x, x + \frac{1}{2}, \frac{1}{2}]$ | [2]     |
| 3   | $[-Y, X, Z]$   | $[x, x + \frac{1}{2}, \frac{1}{4}]$               | [3]     |
| 4   | $[Y, -X, Z]$   | $[\frac{1}{2} - x, -x, \frac{3}{4}]$              | [4]     |
| 5   | $[-X, Y, -Z]$  | $[\frac{1}{2} - x, -x, \frac{3}{4}]$              | [5]     |
| 6   | $[X, -Y, -Z]$  | $[x, x + \frac{1}{2}, \frac{1}{4}]$               | [6]     |
| 7   | $[Y, X, -Z]$   | $[\frac{1}{2} - x, x + \frac{1}{2}, \frac{1}{2}]$ | [7]     |
| 8   | $[-Y, -X, -Z]$ | $[x, -x, 0]$                                      | [8]     |

\* Wyckoff site: **8f**, site symmetry: **.2**.

Table 24: Wyckoff bond: **8a@8f**

| No. | vector       | center                                        | mapping |
|-----|--------------|-----------------------------------------------|---------|
| 1   | $[0, X, Z]$  | $[x, \frac{1}{4}, \frac{1}{8}]$               | [1,-6]  |
| 2   | $[0, -X, Z]$ | $[\frac{1}{2} - x, \frac{1}{4}, \frac{5}{8}]$ | [2,-5]  |
| 3   | $[-X, 0, Z]$ | $[\frac{3}{4}, x + \frac{1}{2}, \frac{3}{8}]$ | [3,-7]  |
| 4   | $[X, 0, Z]$  | $[\frac{3}{4}, -x, \frac{7}{8}]$              | [4,-8]  |

Table 25: Wyckoff bond: **8b@8f**

| No. | vector       | center                                        | mapping |
|-----|--------------|-----------------------------------------------|---------|
| 1   | $[X, 0, 0]$  | $[x, \frac{1}{4}, \frac{1}{8}]$               | [1,6]   |
| 2   | $[-X, 0, 0]$ | $[\frac{1}{2} - x, \frac{1}{4}, \frac{5}{8}]$ | [2,5]   |
| 3   | $[0, X, 0]$  | $[\frac{3}{4}, x + \frac{1}{2}, \frac{3}{8}]$ | [3,7]   |
| 4   | $[0, -X, 0]$ | $[\frac{3}{4}, -x, \frac{7}{8}]$              | [4,8]   |

Table 26: Wyckoff bond: **16c@8f**

| No. | vector         | center                                        | mapping |
|-----|----------------|-----------------------------------------------|---------|
| 1   | $[X, Y, Z]$    | $[x, \frac{1}{4}, \frac{1}{8}]$               | [1]     |
| 2   | $[-X, -Y, Z]$  | $[\frac{1}{2} - x, \frac{1}{4}, \frac{5}{8}]$ | [2]     |
| 3   | $[-Y, X, Z]$   | $[\frac{3}{4}, x + \frac{1}{2}, \frac{3}{8}]$ | [3]     |
| 4   | $[Y, -X, Z]$   | $[\frac{3}{4}, -x, \frac{7}{8}]$              | [4]     |
| 5   | $[-X, Y, -Z]$  | $[\frac{1}{2} - x, \frac{1}{4}, \frac{5}{8}]$ | [5]     |
| 6   | $[X, -Y, -Z]$  | $[x, \frac{1}{4}, \frac{1}{8}]$               | [6]     |
| 7   | $[Y, X, -Z]$   | $[\frac{3}{4}, x + \frac{1}{2}, \frac{3}{8}]$ | [7]     |
| 8   | $[-Y, -X, -Z]$ | $[\frac{3}{4}, -x, \frac{7}{8}]$              | [8]     |

\* Wyckoff site: 16g, site symmetry: 1

Table 27: Wyckoff bond: 16a@16g

| No. | vector         | center                                                | mapping |
|-----|----------------|-------------------------------------------------------|---------|
| 1   | $[X, Y, Z]$    | $[x, y, z]$                                           | [1]     |
| 2   | $[-X, -Y, Z]$  | $[\frac{1}{2} - x, \frac{1}{2} - y, z + \frac{1}{2}]$ | [2]     |
| 3   | $[-Y, X, Z]$   | $[-y, x + \frac{1}{2}, z + \frac{1}{4}]$              | [3]     |
| 4   | $[Y, -X, Z]$   | $[y + \frac{1}{2}, -x, z + \frac{3}{4}]$              | [4]     |
| 5   | $[-X, Y, -Z]$  | $[\frac{1}{2} - x, y, \frac{3}{4} - z]$               | [5]     |
| 6   | $[X, -Y, -Z]$  | $[x, \frac{1}{2} - y, \frac{1}{4} - z]$               | [6]     |
| 7   | $[Y, X, -Z]$   | $[y + \frac{1}{2}, x + \frac{1}{2}, \frac{1}{2} - z]$ | [7]     |
| 8   | $[-Y, -X, -Z]$ | $[-y, -x, -z]$                                        | [8]     |