

MSG No. 208.45 $P4_2321'$ [Type II, cubic]

Table 1: Wyckoff site: 2a, site symmetry: $23.1'$

| No. | position | mapping |
|-----|---|---|
| 1 | $[0, 0, 0]$ | $[1, 8, 9, 10, 17, 18, 19, 20, 21, 22, 23, 24, 25, 32, 33, 34, 41, 42, 43, 44, 45, 46, 47, 48]$ |
| 2 | $[\frac{1}{2}, \frac{1}{2}, \frac{1}{2}]$ | $[2, 3, 4, 5, 6, 7, 11, 12, 13, 14, 15, 16, 26, 27, 28, 29, 30, 31, 35, 36, 37, 38, 39, 40]$ |

Table 2: Wyckoff site: 4b, site symmetry: $.321'$

| No. | position | mapping |
|-----|---|---|
| 1 | $[\frac{1}{4}, \frac{1}{4}, \frac{1}{4}]$ | $[1, 12, 14, 16, 17, 18, 25, 36, 38, 40, 41, 42]$ |
| 2 | $[\frac{3}{4}, \frac{1}{4}, \frac{3}{4}]$ | $[2, 7, 9, 15, 19, 24, 26, 31, 33, 39, 43, 48]$ |
| 3 | $[\frac{3}{4}, \frac{3}{4}, \frac{1}{4}]$ | $[3, 4, 10, 11, 20, 21, 27, 28, 34, 35, 44, 45]$ |
| 4 | $[\frac{1}{4}, \frac{3}{4}, \frac{3}{4}]$ | $[5, 6, 8, 13, 22, 23, 29, 30, 32, 37, 46, 47]$ |

Table 3: Wyckoff site: 4c, site symmetry: $.321'$

| No. | position | mapping |
|-----|---|---|
| 1 | $[\frac{3}{4}, \frac{3}{4}, \frac{3}{4}]$ | $[1, 12, 14, 16, 17, 18, 25, 36, 38, 40, 41, 42]$ |
| 2 | $[\frac{1}{4}, \frac{3}{4}, \frac{1}{4}]$ | $[2, 7, 9, 15, 19, 24, 26, 31, 33, 39, 43, 48]$ |
| 3 | $[\frac{1}{4}, \frac{1}{4}, \frac{3}{4}]$ | $[3, 4, 10, 11, 20, 21, 27, 28, 34, 35, 44, 45]$ |
| 4 | $[\frac{3}{4}, \frac{1}{4}, \frac{1}{4}]$ | $[5, 6, 8, 13, 22, 23, 29, 30, 32, 37, 46, 47]$ |

Table 4: Wyckoff site: 6d, site symmetry: $222..1'$

| No. | position | mapping |
|-----|---------------------------------|------------------------------------|
| 1 | $[0, \frac{1}{2}, \frac{1}{2}]$ | $[1, 8, 9, 10, 25, 32, 33, 34]$ |
| 2 | $[\frac{1}{2}, 0, 0]$ | $[2, 3, 13, 14, 26, 27, 37, 38]$ |
| 3 | $[0, 0, \frac{1}{2}]$ | $[4, 5, 15, 16, 28, 29, 39, 40]$ |
| 4 | $[0, \frac{1}{2}, 0]$ | $[6, 7, 11, 12, 30, 31, 35, 36]$ |
| 5 | $[\frac{1}{2}, 0, \frac{1}{2}]$ | $[17, 20, 22, 24, 41, 44, 46, 48]$ |
| 6 | $[\frac{1}{2}, \frac{1}{2}, 0]$ | $[18, 19, 21, 23, 42, 43, 45, 47]$ |

Table 5: Wyckoff site: 6e, site symmetry: $2.221'$

| No. | position | mapping |
|-----|---------------------------------|----------------------------------|
| 1 | $[\frac{1}{4}, 0, \frac{1}{2}]$ | $[1, 8, 13, 14, 25, 32, 37, 38]$ |
| 2 | $[\frac{3}{4}, 0, \frac{1}{2}]$ | $[2, 3, 9, 10, 26, 27, 33, 34]$ |

continued ...

Table 5

| No. | position | mapping |
|-----|---------------------------------|---------------------------------|
| 3 | $[0, \frac{1}{2}, \frac{1}{4}]$ | [4, 16, 18, 21, 28, 40, 42, 45] |
| 4 | $[0, \frac{1}{2}, \frac{3}{4}]$ | [5, 15, 19, 23, 29, 39, 43, 47] |
| 5 | $[\frac{1}{2}, \frac{3}{4}, 0]$ | [6, 11, 20, 22, 30, 35, 44, 46] |
| 6 | $[\frac{1}{2}, \frac{1}{4}, 0]$ | [7, 12, 17, 24, 31, 36, 41, 48] |

Table 6: Wyckoff site: 6f, site symmetry: $2.221'$

| No. | position | mapping |
|-----|---------------------------------|---------------------------------|
| 1 | $[\frac{1}{4}, \frac{1}{2}, 0]$ | [1, 8, 13, 14, 25, 32, 37, 38] |
| 2 | $[\frac{3}{4}, \frac{1}{2}, 0]$ | [2, 3, 9, 10, 26, 27, 33, 34] |
| 3 | $[\frac{1}{2}, 0, \frac{1}{4}]$ | [4, 16, 18, 21, 28, 40, 42, 45] |
| 4 | $[\frac{1}{2}, 0, \frac{3}{4}]$ | [5, 15, 19, 23, 29, 39, 43, 47] |
| 5 | $[0, \frac{3}{4}, \frac{1}{2}]$ | [6, 11, 20, 22, 30, 35, 44, 46] |
| 6 | $[0, \frac{1}{4}, \frac{1}{2}]$ | [7, 12, 17, 24, 31, 36, 41, 48] |

Table 7: Wyckoff site: 8g, site symmetry: $.3.1'$

| No. | position | mapping |
|-----|---|--------------------------|
| 1 | $[x, x, x]$ | [1, 17, 18, 25, 41, 42] |
| 2 | $[x + \frac{1}{2}, \frac{1}{2} - x, x + \frac{1}{2}]$ | [2, 7, 15, 26, 31, 39] |
| 3 | $[x + \frac{1}{2}, x + \frac{1}{2}, \frac{1}{2} - x]$ | [3, 4, 11, 27, 28, 35] |
| 4 | $[\frac{1}{2} - x, x + \frac{1}{2}, x + \frac{1}{2}]$ | [5, 6, 13, 29, 30, 37] |
| 5 | $[x, -x, -x]$ | [8, 22, 23, 32, 46, 47] |
| 6 | $[-x, x, -x]$ | [9, 19, 24, 33, 43, 48] |
| 7 | $[-x, -x, x]$ | [10, 20, 21, 34, 44, 45] |
| 8 | $[\frac{1}{2} - x, \frac{1}{2} - x, \frac{1}{2} - x]$ | [12, 14, 16, 36, 38, 40] |

Table 8: Wyckoff site: 12h, site symmetry: $2..1'$

| No. | position | mapping |
|-----|---|------------------|
| 1 | $[x, 0, 0]$ | [1, 8, 25, 32] |
| 2 | $[x + \frac{1}{2}, \frac{1}{2}, \frac{1}{2}]$ | [2, 3, 26, 27] |
| 3 | $[\frac{1}{2}, \frac{1}{2}, \frac{1}{2} - x]$ | [4, 16, 28, 40] |
| 4 | $[\frac{1}{2}, \frac{1}{2}, x + \frac{1}{2}]$ | [5, 15, 29, 39] |
| 5 | $[\frac{1}{2}, x + \frac{1}{2}, \frac{1}{2}]$ | [6, 11, 30, 35] |
| 6 | $[\frac{1}{2}, \frac{1}{2} - x, \frac{1}{2}]$ | [7, 12, 31, 36] |
| 7 | $[-x, 0, 0]$ | [9, 10, 33, 34] |
| 8 | $[\frac{1}{2} - x, \frac{1}{2}, \frac{1}{2}]$ | [13, 14, 37, 38] |
| 9 | $[0, x, 0]$ | [17, 24, 41, 48] |

continued ...

Table 8

| No. | position | mapping |
|-----|--------------|--------------------|
| 10 | $[0, 0, x]$ | $[18, 21, 42, 45]$ |
| 11 | $[0, 0, -x]$ | $[19, 23, 43, 47]$ |
| 12 | $[0, -x, 0]$ | $[20, 22, 44, 46]$ |

Table 9: Wyckoff site: 12i, site symmetry: $2..1'$

| No. | position | mapping |
|-----|-------------------------------------|--------------------|
| 1 | $[x, 0, \frac{1}{2}]$ | $[1, 8, 25, 32]$ |
| 2 | $[x + \frac{1}{2}, 0, \frac{1}{2}]$ | $[2, 3, 26, 27]$ |
| 3 | $[0, \frac{1}{2}, \frac{1}{2} - x]$ | $[4, 16, 28, 40]$ |
| 4 | $[0, \frac{1}{2}, x + \frac{1}{2}]$ | $[5, 15, 29, 39]$ |
| 5 | $[\frac{1}{2}, x + \frac{1}{2}, 0]$ | $[6, 11, 30, 35]$ |
| 6 | $[\frac{1}{2}, \frac{1}{2} - x, 0]$ | $[7, 12, 31, 36]$ |
| 7 | $[-x, 0, \frac{1}{2}]$ | $[9, 10, 33, 34]$ |
| 8 | $[\frac{1}{2} - x, 0, \frac{1}{2}]$ | $[13, 14, 37, 38]$ |
| 9 | $[\frac{1}{2}, x, 0]$ | $[17, 24, 41, 48]$ |
| 10 | $[0, \frac{1}{2}, x]$ | $[18, 21, 42, 45]$ |
| 11 | $[0, \frac{1}{2}, -x]$ | $[19, 23, 43, 47]$ |
| 12 | $[\frac{1}{2}, -x, 0]$ | $[20, 22, 44, 46]$ |

Table 10: Wyckoff site: 12j, site symmetry: $2..1'$

| No. | position | mapping |
|-----|-------------------------------------|--------------------|
| 1 | $[x, \frac{1}{2}, 0]$ | $[1, 8, 25, 32]$ |
| 2 | $[x + \frac{1}{2}, \frac{1}{2}, 0]$ | $[2, 3, 26, 27]$ |
| 3 | $[\frac{1}{2}, 0, \frac{1}{2} - x]$ | $[4, 16, 28, 40]$ |
| 4 | $[\frac{1}{2}, 0, x + \frac{1}{2}]$ | $[5, 15, 29, 39]$ |
| 5 | $[0, x + \frac{1}{2}, \frac{1}{2}]$ | $[6, 11, 30, 35]$ |
| 6 | $[0, \frac{1}{2} - x, \frac{1}{2}]$ | $[7, 12, 31, 36]$ |
| 7 | $[-x, \frac{1}{2}, 0]$ | $[9, 10, 33, 34]$ |
| 8 | $[\frac{1}{2} - x, \frac{1}{2}, 0]$ | $[13, 14, 37, 38]$ |
| 9 | $[0, x, \frac{1}{2}]$ | $[17, 24, 41, 48]$ |
| 10 | $[\frac{1}{2}, 0, x]$ | $[18, 21, 42, 45]$ |
| 11 | $[\frac{1}{2}, 0, -x]$ | $[19, 23, 43, 47]$ |
| 12 | $[0, -x, \frac{1}{2}]$ | $[20, 22, 44, 46]$ |

Table 11: Wyckoff site: $12k$, site symmetry: $\dots 21'$

| No. | position | mapping |
|-----|--------------------------------------|--------------------|
| 1 | $[\frac{1}{4}, y, \frac{1}{2} - y]$ | $[1, 14, 25, 38]$ |
| 2 | $[\frac{3}{4}, y, y + \frac{1}{2}]$ | $[2, 9, 26, 33]$ |
| 3 | $[\frac{3}{4}, -y, \frac{1}{2} - y]$ | $[3, 10, 27, 34]$ |
| 4 | $[-y, y + \frac{1}{2}, \frac{1}{4}]$ | $[4, 21, 28, 45]$ |
| 5 | $[y, y + \frac{1}{2}, \frac{3}{4}]$ | $[5, 23, 29, 47]$ |
| 6 | $[\frac{1}{2} - y, \frac{3}{4}, -y]$ | $[6, 22, 30, 46]$ |
| 7 | $[y + \frac{1}{2}, \frac{1}{4}, -y]$ | $[7, 24, 31, 48]$ |
| 8 | $[\frac{1}{4}, -y, y + \frac{1}{2}]$ | $[8, 13, 32, 37]$ |
| 9 | $[y + \frac{1}{2}, \frac{3}{4}, y]$ | $[11, 20, 35, 44]$ |
| 10 | $[\frac{1}{2} - y, \frac{1}{4}, y]$ | $[12, 17, 36, 41]$ |
| 11 | $[-y, \frac{1}{2} - y, \frac{3}{4}]$ | $[15, 19, 39, 43]$ |
| 12 | $[y, \frac{1}{2} - y, \frac{1}{4}]$ | $[16, 18, 40, 42]$ |

Table 12: Wyckoff site: $12l$, site symmetry: $\dots 21'$

| No. | position | mapping |
|-----|--------------------------------------|--------------------|
| 1 | $[\frac{1}{4}, y, y + \frac{1}{2}]$ | $[1, 13, 25, 37]$ |
| 2 | $[\frac{3}{4}, -y, y + \frac{1}{2}]$ | $[2, 10, 26, 34]$ |
| 3 | $[\frac{3}{4}, y, \frac{1}{2} - y]$ | $[3, 9, 27, 33]$ |
| 4 | $[y, y + \frac{1}{2}, \frac{1}{4}]$ | $[4, 18, 28, 42]$ |
| 5 | $[-y, y + \frac{1}{2}, \frac{3}{4}]$ | $[5, 19, 29, 43]$ |
| 6 | $[\frac{1}{2} - y, \frac{3}{4}, y]$ | $[6, 20, 30, 44]$ |
| 7 | $[y + \frac{1}{2}, \frac{1}{4}, y]$ | $[7, 17, 31, 41]$ |
| 8 | $[\frac{1}{4}, -y, \frac{1}{2} - y]$ | $[8, 14, 32, 38]$ |
| 9 | $[y + \frac{1}{2}, \frac{3}{4}, -y]$ | $[11, 22, 35, 46]$ |
| 10 | $[\frac{1}{2} - y, \frac{1}{4}, -y]$ | $[12, 24, 36, 48]$ |
| 11 | $[y, \frac{1}{2} - y, \frac{3}{4}]$ | $[15, 23, 39, 47]$ |
| 12 | $[-y, \frac{1}{2} - y, \frac{1}{4}]$ | $[16, 21, 40, 45]$ |

Table 13: Wyckoff site: $24m$, site symmetry: $11'$

| No. | position | mapping |
|-----|---|-----------|
| 1 | $[x, y, z]$ | $[1, 25]$ |
| 2 | $[x + \frac{1}{2}, \frac{1}{2} - z, y + \frac{1}{2}]$ | $[2, 26]$ |
| 3 | $[x + \frac{1}{2}, z + \frac{1}{2}, \frac{1}{2} - y]$ | $[3, 27]$ |
| 4 | $[z + \frac{1}{2}, y + \frac{1}{2}, \frac{1}{2} - x]$ | $[4, 28]$ |
| 5 | $[\frac{1}{2} - z, y + \frac{1}{2}, x + \frac{1}{2}]$ | $[5, 29]$ |
| 6 | $[\frac{1}{2} - y, x + \frac{1}{2}, z + \frac{1}{2}]$ | $[6, 30]$ |
| 7 | $[y + \frac{1}{2}, \frac{1}{2} - x, z + \frac{1}{2}]$ | $[7, 31]$ |
| 8 | $[x, -y, -z]$ | $[8, 32]$ |
| 9 | $[-x, y, -z]$ | $[9, 33]$ |

continued ...

Table 13

| No. | position | mapping |
|-----|---|---------|
| 10 | $[-x, -y, z]$ | [10,34] |
| 11 | $[y + \frac{1}{2}, x + \frac{1}{2}, \frac{1}{2} - z]$ | [11,35] |
| 12 | $[\frac{1}{2} - y, \frac{1}{2} - x, \frac{1}{2} - z]$ | [12,36] |
| 13 | $[\frac{1}{2} - x, z + \frac{1}{2}, y + \frac{1}{2}]$ | [13,37] |
| 14 | $[\frac{1}{2} - x, \frac{1}{2} - z, \frac{1}{2} - y]$ | [14,38] |
| 15 | $[z + \frac{1}{2}, \frac{1}{2} - y, x + \frac{1}{2}]$ | [15,39] |
| 16 | $[\frac{1}{2} - z, \frac{1}{2} - y, \frac{1}{2} - x]$ | [16,40] |
| 17 | $[z, x, y]$ | [17,41] |
| 18 | $[y, z, x]$ | [18,42] |
| 19 | $[-y, z, -x]$ | [19,43] |
| 20 | $[-z, -x, y]$ | [20,44] |
| 21 | $[-y, -z, x]$ | [21,45] |
| 22 | $[z, -x, -y]$ | [22,46] |
| 23 | $[y, -z, -x]$ | [23,47] |
| 24 | $[-z, x, -y]$ | [24,48] |