

PG No. 3 C_2 2 (b-axis setting) [monoclinic] (polar, internal axial dipole)

* Harmonics for rank 0

* Harmonics for rank 1

$$\vec{\mathbb{Q}}_1^{(1,0)}[g](A)$$

** symmetry

y

** expression

$$-\frac{\sqrt{2}G_xz}{2} + \frac{\sqrt{2}G_zx}{2}$$

$$\vec{\mathbb{Q}}_1^{(1,0)}[g](B, 1)$$

** symmetry

x

** expression

$$\frac{\sqrt{2}G_yz}{2} - \frac{\sqrt{2}G_zy}{2}$$

$$\vec{\mathbb{Q}}_1^{(1,0)}[g](B, 2)$$

** symmetry

z

** expression

$$\frac{\sqrt{2}G_xy}{2} - \frac{\sqrt{2}G_yx}{2}$$

* Harmonics for rank 2

$$\vec{\mathbb{Q}}_2^{(1,0)}[g](A, 1)$$

** symmetry

$$-\frac{x^2}{2} - \frac{y^2}{2} + z^2$$

** expression

$$\frac{\sqrt{6}G_xyz}{2} - \frac{\sqrt{6}G_yxz}{2}$$

$$\vec{\mathbb{Q}}_2^{(1,0)}[g](A, 2)$$

** symmetry

$$\frac{\sqrt{3}(x-y)(x+y)}{2}$$

** expression

$$\frac{\sqrt{2}G_xyz}{2} + \frac{\sqrt{2}G_yxz}{2} - \sqrt{2}G_zxy$$

$$\vec{\mathbb{Q}}_2^{(1,0)}[g](A, 3)$$

** symmetry

$$\sqrt{3}xz$$

** expression

$$\frac{\sqrt{2}G_xxy}{2} - \frac{\sqrt{2}G_y(x-z)(x+z)}{2} - \frac{\sqrt{2}G_zyz}{2}$$

$$\vec{\mathbb{Q}}_2^{(1,0)}[g](B, 1)$$

** symmetry

$$\sqrt{3}yz$$

** expression

$$\frac{\sqrt{2}G_x(y-z)(y+z)}{2} - \frac{\sqrt{2}G_yxy}{2} + \frac{\sqrt{2}G_zxz}{2}$$

$$\vec{\mathbb{Q}}_2^{(1,0)}[g](B, 2)$$

** symmetry

$$\sqrt{3}xy$$

** expression

$$-\frac{\sqrt{2}G_xxz}{2} + \frac{\sqrt{2}G_yyz}{2} + \frac{\sqrt{2}G_z(x-y)(x+y)}{2}$$

* Harmonics for rank 3

$$\vec{\mathbb{Q}}_3^{(1,0)}[g](A, 1)$$

** symmetry

$$\sqrt{15}xyz$$

** expression

$$\frac{\sqrt{5}G_xx(y-z)(y+z)}{2} - \frac{\sqrt{5}G_yy(x-z)(x+z)}{2} + \frac{\sqrt{5}G_zz(x-y)(x+y)}{2}$$

$$\vec{\mathbb{Q}}_3^{(1,0)}[g](A, 2)$$

** symmetry

$$-\frac{y(3x^2 - 2y^2 + 3z^2)}{2}$$

** expression

$$\frac{\sqrt{3}G_xz(x^2 - 4y^2 + z^2)}{4} - \frac{\sqrt{3}G_zx(x^2 - 4y^2 + z^2)}{4}$$

$$\vec{\mathbb{Q}}_3^{(1,0)}[g](A, 3)$$

** symmetry

$$-\frac{\sqrt{15}y(x-z)(x+z)}{2}$$

** expression

$$\frac{\sqrt{5}G_xz(x^2 + 2y^2 - z^2)}{4} - \sqrt{5}G_yxyz - \frac{\sqrt{5}G_zx(x^2 - 2y^2 - z^2)}{4}$$

$$\vec{\mathbb{Q}}_3^{(1,0)}[g](B, 1)$$

** symmetry

$$\frac{x(2x^2 - 3y^2 - 3z^2)}{2}$$

** expression

$$\frac{\sqrt{3}G_yz(4x^2 - y^2 - z^2)}{4} - \frac{\sqrt{3}G_zy(4x^2 - y^2 - z^2)}{4}$$

$$\vec{\mathbb{Q}}_3^{(1,0)}[g](B, 2)$$

** symmetry

$$-\frac{z(3x^2 + 3y^2 - 2z^2)}{2}$$

** expression

$$-\frac{\sqrt{3}G_xy(x^2 + y^2 - 4z^2)}{4} + \frac{\sqrt{3}G_yx(x^2 + y^2 - 4z^2)}{4}$$

$$\vec{\mathbb{Q}}_3^{(1,0)}[g](B, 3)$$

** symmetry

$$\frac{\sqrt{15}x(y-z)(y+z)}{2}$$

** expression

$$-\sqrt{5}G_xxyz + \frac{\sqrt{5}G_yz(2x^2 + y^2 - z^2)}{4} + \frac{\sqrt{5}G_zy(2x^2 - y^2 + z^2)}{4}$$

$$\vec{\mathbb{Q}}_3^{(1,0)}[g](B, 4)$$

** symmetry

$$\frac{\sqrt{15}z(x-y)(x+y)}{2}$$

** expression

$$\frac{\sqrt{5}G_xy(x^2 - y^2 + 2z^2)}{4} - \frac{\sqrt{5}G_yx(x^2 - y^2 - 2z^2)}{4} - \sqrt{5}G_zxyz$$

* Harmonics for rank 4

$$\vec{\mathbb{Q}}_4^{(1,0)}[g](A, 1)$$

** symmetry

$$\frac{\sqrt{21} (x^4 - 3x^2y^2 - 3x^2z^2 + y^4 - 3y^2z^2 + z^4)}{6}$$

** expression

$$-\frac{\sqrt{105}G_xyz(y-z)(y+z)}{6} + \frac{\sqrt{105}G_yxz(x-z)(x+z)}{6} - \frac{\sqrt{105}G_zxy(x-y)(x+y)}{6}$$

$$\vec{\mathbb{Q}}_4^{(1,0)}[g](A, 2)$$

** symmetry

$$-\frac{\sqrt{15} (x^4 - 12x^2y^2 + 6x^2z^2 + y^4 + 6y^2z^2 - 2z^4)}{12}$$

** expression

$$-\frac{\sqrt{3}G_xyz(9x^2 + 2y^2 - 5z^2)}{6} + \frac{\sqrt{3}G_yxz(2x^2 + 9y^2 - 5z^2)}{6} + \frac{7\sqrt{3}G_zxy(x-y)(x+y)}{6}$$

$$\vec{\mathbb{Q}}_4^{(1,0)}[g](A, 3)$$

** symmetry

$$\frac{\sqrt{5}(x-y)(x+y)(x^2 + y^2 - 6z^2)}{4}$$

** expression

$$-\frac{G_xxyz(3x^2 - 4y^2 + 3z^2)}{2} + \frac{G_yxz(4x^2 - 3y^2 - 3z^2)}{2} - \frac{G_zxy(x^2 + y^2 - 6z^2)}{2}$$

$$\vec{\mathbb{Q}}_4^{(1,0)}[g](A, 4)$$

** symmetry

$$-\frac{\sqrt{35}xz(x-z)(x+z)}{2}$$

** expression

$$-\frac{\sqrt{7}G_xxy(x^2 - 3z^2)}{4} + \frac{\sqrt{7}G_y(x^2 - 2xz - z^2)(x^2 + 2xz - z^2)}{4} + \frac{\sqrt{7}G_zyz(3x^2 - z^2)}{4}$$

$$\vec{\mathbb{Q}}_4^{(1,0)}[g](A, 5)$$

** symmetry

$$-\frac{\sqrt{5}xz(x^2 - 6y^2 + z^2)}{2}$$

** expression

$$-\frac{G_xxy(x^2 - 6y^2 + 15z^2)}{4} + \frac{G_y(x-z)(x+z)(x^2 - 6y^2 + z^2)}{4} + \frac{G_zyz(15x^2 - 6y^2 + z^2)}{4}$$

$$\vec{\mathbb{Q}}_4^{(1,0)}[g](B, 1)$$

** symmetry

$$\frac{\sqrt{35}yz(y-z)(y+z)}{2}$$

** expression

$$\frac{\sqrt{7}G_x(y^2 - 2yz - z^2)(y^2 + 2yz - z^2)}{4} - \frac{\sqrt{7}G_yxy(y^2 - 3z^2)}{4} + \frac{\sqrt{7}G_zxz(3y^2 - z^2)}{4}$$

$$\vec{\mathbb{Q}}_4^{(1,0)}[g](B, 2)$$

** symmetry

$$\frac{\sqrt{35}xy(x-y)(x+y)}{2}$$

** expression

$$-\frac{\sqrt{7}G_xxz(x^2 - 3y^2)}{4} + \frac{\sqrt{7}G_yyz(3x^2 - y^2)}{4} + \frac{\sqrt{7}G_z(x^2 - 2xy - y^2)(x^2 + 2xy - y^2)}{4}$$

$$\vec{\mathbb{Q}}_4^{(1,0)}[g](B, 3)$$

** symmetry

$$\frac{\sqrt{5}yz(6x^2 - y^2 - z^2)}{2}$$

** expression

$$\frac{G_x (y - z) (y + z) (6x^2 - y^2 - z^2)}{4} - \frac{G_y xy (6x^2 - y^2 - 15z^2)}{4} + \frac{G_z xz (6x^2 - 15y^2 - z^2)}{4}$$

$\tilde{\mathbb{Q}}_4^{(1,0)}[g](B, 4)$

** symmetry

$$-\frac{\sqrt{5}xy(x^2 + y^2 - 6z^2)}{2}$$

** expression

$$\frac{G_x xz (x^2 + 15y^2 - 6z^2)}{4} - \frac{G_y yz (15x^2 + y^2 - 6z^2)}{4} - \frac{G_z (x - y)(x + y)(x^2 + y^2 - 6z^2)}{4}$$