

SG No. 113 D_{2d}^3 $P\bar{4}2_1m$ [tetragonal]

* plus set: +[0, 0, 0]

* Wyckoff site: 2a, site symmetry: -4..

Table 1: Wyckoff bond: 2a@2a

| No. | vector | center | mapping |
|-----|------------|-------------------------------|----------------|
| 1 | [0, 0, Z] | [0, 0, 0] | [1, 2, -3, -4] |
| 2 | [0, 0, -Z] | [\frac{1}{2}, \frac{1}{2}, 0] | [5, 6, -7, -8] |

Table 2: Wyckoff bond: 4b@2a

| No. | vector | center | mapping |
|-----|-------------|-------------------------------|---------|
| 1 | [X, Y, 0] | [0, 0, 0] | [1, -2] |
| 2 | [Y, -X, 0] | [0, 0, 0] | [3, -4] |
| 3 | [-X, Y, 0] | [\frac{1}{2}, \frac{1}{2}, 0] | [5, -6] |
| 4 | [-Y, -X, 0] | [\frac{1}{2}, \frac{1}{2}, 0] | [7, -8] |

Table 3: Wyckoff bond: 8c@2a

| No. | vector | center | mapping |
|-----|-------------|-------------------------------|---------|
| 1 | [X, Y, Z] | [0, 0, 0] | [1] |
| 2 | [-X, -Y, Z] | [0, 0, 0] | [2] |
| 3 | [Y, -X, -Z] | [0, 0, 0] | [3] |
| 4 | [-Y, X, -Z] | [0, 0, 0] | [4] |
| 5 | [-X, Y, -Z] | [\frac{1}{2}, \frac{1}{2}, 0] | [5] |
| 6 | [X, -Y, -Z] | [\frac{1}{2}, \frac{1}{2}, 0] | [6] |
| 7 | [-Y, -X, Z] | [\frac{1}{2}, \frac{1}{2}, 0] | [7] |
| 8 | [Y, X, Z] | [\frac{1}{2}, \frac{1}{2}, 0] | [8] |

* Wyckoff site: 2b, site symmetry: -4..

Table 4: Wyckoff bond: 2a@2b

| No. | vector | center | mapping |
|-----|------------|---|----------------|
| 1 | [0, 0, Z] | [0, 0, \frac{1}{2}] | [1, 2, -3, -4] |
| 2 | [0, 0, -Z] | [\frac{1}{2}, \frac{1}{2}, \frac{1}{2}] | [5, 6, -7, -8] |

Table 5: Wyckoff bond: 4b@2b

| No. | vector | center | mapping |
|-----|---------------|---|---------|
| 1 | $[X, Y, 0]$ | $[0, 0, \frac{1}{2}]$ | [1,-2] |
| 2 | $[Y, -X, 0]$ | $[0, 0, \frac{1}{2}]$ | [3,-4] |
| 3 | $[-X, Y, 0]$ | $[\frac{1}{2}, \frac{1}{2}, \frac{1}{2}]$ | [5,-6] |
| 4 | $[-Y, -X, 0]$ | $[\frac{1}{2}, \frac{1}{2}, \frac{1}{2}]$ | [7,-8] |

Table 6: Wyckoff bond: 8c@2b

| No. | vector | center | mapping |
|-----|---------------|---|---------|
| 1 | $[X, Y, Z]$ | $[0, 0, \frac{1}{2}]$ | [1] |
| 2 | $[-X, -Y, Z]$ | $[0, 0, \frac{1}{2}]$ | [2] |
| 3 | $[Y, -X, -Z]$ | $[0, 0, \frac{1}{2}]$ | [3] |
| 4 | $[-Y, X, -Z]$ | $[0, 0, \frac{1}{2}]$ | [4] |
| 5 | $[-X, Y, -Z]$ | $[\frac{1}{2}, \frac{1}{2}, \frac{1}{2}]$ | [5] |
| 6 | $[X, -Y, -Z]$ | $[\frac{1}{2}, \frac{1}{2}, \frac{1}{2}]$ | [6] |
| 7 | $[-Y, -X, Z]$ | $[\frac{1}{2}, \frac{1}{2}, \frac{1}{2}]$ | [7] |
| 8 | $[Y, X, Z]$ | $[\frac{1}{2}, \frac{1}{2}, \frac{1}{2}]$ | [8] |

* Wyckoff site: 2c, site symmetry: 2.m̄m

Table 7: Wyckoff bond: 2a@2c

| No. | vector | center | mapping |
|-----|--------------|------------------------|-------------|
| 1 | $[X, X, 0]$ | $[0, \frac{1}{2}, z]$ | [1,-2,-7,8] |
| 2 | $[X, -X, 0]$ | $[\frac{1}{2}, 0, -z]$ | [3,-4,-5,6] |

Table 8: Wyckoff bond: 2b@2c

| No. | vector | center | mapping |
|-----|---------------|------------------------|-------------|
| 1 | $[X, -X, 0]$ | $[0, \frac{1}{2}, z]$ | [1,-2,7,-8] |
| 2 | $[-X, -X, 0]$ | $[\frac{1}{2}, 0, -z]$ | [3,-4,5,-6] |

Table 9: Wyckoff bond: 2c@2c

| No. | vector | center | mapping |
|-----|--------------|------------------------|-----------|
| 1 | $[0, 0, Z]$ | $[0, \frac{1}{2}, z]$ | [1,2,7,8] |
| 2 | $[0, 0, -Z]$ | $[\frac{1}{2}, 0, -z]$ | [3,4,5,6] |

Table 10: Wyckoff bond: 4d@2c

| No. | vector | center | mapping |
|-----|-------------|--------------------------|---------|
| 1 | [X, X, Z] | [0, $\frac{1}{2}$, z] | [1,8] |
| 2 | [-X, -X, Z] | [0, $\frac{1}{2}$, z] | [2,7] |
| 3 | [X, -X, -Z] | [$\frac{1}{2}$, 0, -z] | [3,6] |
| 4 | [-X, X, -Z] | [$\frac{1}{2}$, 0, -z] | [4,5] |

Table 11: Wyckoff bond: 4e@2c

| No. | vector | center | mapping |
|-----|--------------|--------------------------|---------|
| 1 | [X, -X, Z] | [0, $\frac{1}{2}$, z] | [1,7] |
| 2 | [-X, X, Z] | [0, $\frac{1}{2}$, z] | [2,8] |
| 3 | [-X, -X, -Z] | [$\frac{1}{2}$, 0, -z] | [3,5] |
| 4 | [X, X, -Z] | [$\frac{1}{2}$, 0, -z] | [4,6] |

Table 12: Wyckoff bond: 4f@2c

| No. | vector | center | mapping |
|-----|-------------|--------------------------|---------|
| 1 | [X, Y, 0] | [0, $\frac{1}{2}$, z] | [1,-2] |
| 2 | [Y, -X, 0] | [$\frac{1}{2}$, 0, -z] | [3,-4] |
| 3 | [-X, Y, 0] | [$\frac{1}{2}$, 0, -z] | [5,-6] |
| 4 | [-Y, -X, 0] | [0, $\frac{1}{2}$, z] | [7,-8] |

Table 13: Wyckoff bond: 8g@2c

| No. | vector | center | mapping |
|-----|-------------|--------------------------|---------|
| 1 | [X, Y, Z] | [0, $\frac{1}{2}$, z] | [1] |
| 2 | [-X, -Y, Z] | [0, $\frac{1}{2}$, z] | [2] |
| 3 | [Y, -X, -Z] | [$\frac{1}{2}$, 0, -z] | [3] |
| 4 | [-Y, X, -Z] | [$\frac{1}{2}$, 0, -z] | [4] |
| 5 | [-X, Y, -Z] | [$\frac{1}{2}$, 0, -z] | [5] |
| 6 | [X, -Y, -Z] | [$\frac{1}{2}$, 0, -z] | [6] |
| 7 | [-Y, -X, Z] | [0, $\frac{1}{2}$, z] | [7] |
| 8 | [Y, X, Z] | [0, $\frac{1}{2}$, z] | [8] |

* Wyckoff site: 4d, site symmetry: 2..

Table 14: Wyckoff bond: 4a@4d

| No. | vector | center | mapping |
|-----|-------------|--------------------------------|---------|
| 1 | [X, Y, 0] | [0, 0, z] | [1, -2] |
| 2 | [Y, -X, 0] | [0, 0, -z] | [3, -4] |
| 3 | [-X, Y, 0] | [\frac{1}{2}, \frac{1}{2}, -z] | [5, -6] |
| 4 | [-Y, -X, 0] | [\frac{1}{2}, \frac{1}{2}, z] | [7, -8] |

Table 15: Wyckoff bond: 4b@4d

| No. | vector | center | mapping |
|-----|------------|--------------------------------|---------|
| 1 | [0, 0, Z] | [0, 0, z] | [1, 2] |
| 2 | [0, 0, -Z] | [0, 0, -z] | [3, 4] |
| 3 | [0, 0, -Z] | [\frac{1}{2}, \frac{1}{2}, -z] | [5, 6] |
| 4 | [0, 0, Z] | [\frac{1}{2}, \frac{1}{2}, z] | [7, 8] |

Table 16: Wyckoff bond: 8c@4d

| No. | vector | center | mapping |
|-----|-------------|--------------------------------|---------|
| 1 | [X, Y, Z] | [0, 0, z] | [1] |
| 2 | [-X, -Y, Z] | [0, 0, z] | [2] |
| 3 | [Y, -X, -Z] | [0, 0, -z] | [3] |
| 4 | [-Y, X, -Z] | [0, 0, -z] | [4] |
| 5 | [-X, Y, -Z] | [\frac{1}{2}, \frac{1}{2}, -z] | [5] |
| 6 | [X, -Y, -Z] | [\frac{1}{2}, \frac{1}{2}, -z] | [6] |
| 7 | [-Y, -X, Z] | [\frac{1}{2}, \frac{1}{2}, z] | [7] |
| 8 | [Y, X, Z] | [\frac{1}{2}, \frac{1}{2}, z] | [8] |

* Wyckoff site: 4e, site symmetry: . . m

Table 17: Wyckoff bond: 4a@4e

| No. | vector | center | mapping |
|-----|-------------|---------------------------|---------|
| 1 | [X, X, Z] | [x, x + \frac{1}{2}, z] | [1, 8] |
| 2 | [-X, -X, Z] | [-x, \frac{1}{2} - x, z] | [2, 7] |
| 3 | [X, -X, -Z] | [x + \frac{1}{2}, -x, -z] | [3, 6] |
| 4 | [-X, X, -Z] | [\frac{1}{2} - x, x, -z] | [4, 5] |

Table 18: Wyckoff bond: 4b@4e

| No. | vector | center | mapping |
|-----|---------------|-----------------------------|---------|
| 1 | $[X, -X, 0]$ | $[x, x + \frac{1}{2}, z]$ | [1, -8] |
| 2 | $[-X, X, 0]$ | $[-x, \frac{1}{2} - x, z]$ | [2, -7] |
| 3 | $[-X, -X, 0]$ | $[x + \frac{1}{2}, -x, -z]$ | [3, -6] |
| 4 | $[X, X, 0]$ | $[\frac{1}{2} - x, x, -z]$ | [4, -5] |

Table 19: Wyckoff bond: 8c@4e

| No. | vector | center | mapping |
|-----|---------------|-----------------------------|---------|
| 1 | $[X, Y, Z]$ | $[x, x + \frac{1}{2}, z]$ | [1] |
| 2 | $[-X, -Y, Z]$ | $[-x, \frac{1}{2} - x, z]$ | [2] |
| 3 | $[Y, -X, -Z]$ | $[x + \frac{1}{2}, -x, -z]$ | [3] |
| 4 | $[-Y, X, -Z]$ | $[\frac{1}{2} - x, x, -z]$ | [4] |
| 5 | $[-X, Y, -Z]$ | $[\frac{1}{2} - x, x, -z]$ | [5] |
| 6 | $[X, -Y, -Z]$ | $[x + \frac{1}{2}, -x, -z]$ | [6] |
| 7 | $[-Y, -X, Z]$ | $[-x, \frac{1}{2} - x, z]$ | [7] |
| 8 | $[Y, X, Z]$ | $[x, x + \frac{1}{2}, z]$ | [8] |

* Wyckoff site: 8f, site symmetry: 1

Table 20: Wyckoff bond: 8a@8f

| No. | vector | center | mapping |
|-----|---------------|--|---------|
| 1 | $[X, Y, Z]$ | $[x, y, z]$ | [1] |
| 2 | $[-X, -Y, Z]$ | $[-x, -y, z]$ | [2] |
| 3 | $[Y, -X, -Z]$ | $[y, -x, -z]$ | [3] |
| 4 | $[-Y, X, -Z]$ | $[-y, x, -z]$ | [4] |
| 5 | $[-X, Y, -Z]$ | $[\frac{1}{2} - x, y + \frac{1}{2}, -z]$ | [5] |
| 6 | $[X, -Y, -Z]$ | $[x + \frac{1}{2}, \frac{1}{2} - y, -z]$ | [6] |
| 7 | $[-Y, -X, Z]$ | $[\frac{1}{2} - y, \frac{1}{2} - x, z]$ | [7] |
| 8 | $[Y, X, Z]$ | $[y + \frac{1}{2}, x + \frac{1}{2}, z]$ | [8] |