

SG No. 220  $T_d^6$   $I\bar{4}3d$  [ cubic ]

\* generator :  $\{2_{001}| \frac{1}{2}0\frac{1}{2}\}$ ,  $\{2_{010}| 0\frac{1}{2}\frac{1}{2}\}$ ,  $\{3_{111}^+| 0\}$ ,  $\{\text{m}_{1-10}| \frac{1}{4}\frac{1}{4}\frac{1}{4}\}$

\* symmetry operation + [0, 0, 0], + [ $\frac{1}{2}, \frac{1}{2}, \frac{1}{2}$ ]

Table 1: Symmetry operations for 3d polar vector.

| No. | tag  | matrix (polar)  | det |
|-----|--|---|-----|
| 1   | $\{1 0\}$  | $\begin{bmatrix} 1 & 0 & 0 & 0 \\ 0 & 1 & 0 & 0 \\ 0 & 0 & 1 & 0 \end{bmatrix}$                               | 1   |
| 2   | $\{2_{001}  \frac{1}{2}0\frac{1}{2}\}$                   | $\begin{bmatrix} -1 & 0 & 0 & \frac{1}{2} \\ 0 & -1 & 0 & 0 \\ 0 & 0 & 1 & \frac{1}{2} \end{bmatrix}$         | 1   |
| 3   | $\{2_{010}  0\frac{1}{2}\frac{1}{2}\}$                   | $\begin{bmatrix} -1 & 0 & 0 & 0 \\ 0 & 1 & 0 & \frac{1}{2} \\ 0 & 0 & -1 & \frac{1}{2} \end{bmatrix}$         | 1   |
| 4   | $\{2_{100}  \frac{1}{2}\frac{1}{2}0\}$                   | $\begin{bmatrix} 1 & 0 & 0 & \frac{1}{2} \\ 0 & -1 & 0 & \frac{1}{2} \\ 0 & 0 & -1 & 0 \end{bmatrix}$         | 1   |
| 5   | $\{3_{111}^+  0\}$                                       | $\begin{bmatrix} 0 & 0 & 1 & 0 \\ 1 & 0 & 0 & 0 \\ 0 & 1 & 0 & 0 \end{bmatrix}$                               | 1   |
| 6   | $\{3_{-11-1}^+  \frac{1}{2}\frac{1}{2}0\}$               | $\begin{bmatrix} 0 & 0 & 1 & \frac{1}{2} \\ -1 & 0 & 0 & \frac{1}{2} \\ 0 & -1 & 0 & 0 \end{bmatrix}$         | 1   |
| 7   | $\{3_{1-1-1}^+  \frac{1}{2}0\frac{1}{2}\}$               | $\begin{bmatrix} 0 & 0 & -1 & \frac{1}{2} \\ -1 & 0 & 0 & 0 \\ 0 & 1 & 0 & \frac{1}{2} \end{bmatrix}$         | 1   |
| 8   | $\{3_{-1-11}^+  0\frac{1}{2}\frac{1}{2}\}$               | $\begin{bmatrix} 0 & 0 & -1 & 0 \\ 1 & 0 & 0 & \frac{1}{2} \\ 0 & -1 & 0 & \frac{1}{2} \end{bmatrix}$         | 1   |
| 9   | $\{3_{111}^-  0\}$                                       | $\begin{bmatrix} 0 & 1 & 0 & 0 \\ 0 & 0 & 1 & 0 \\ 1 & 0 & 0 & 0 \end{bmatrix}$                               | 1   |
| 10  | $\{3_{-1-1-1}^-  0\frac{1}{2}\frac{1}{2}\}$              | $\begin{bmatrix} 0 & -1 & 0 & 0 \\ 0 & 0 & 1 & \frac{1}{2} \\ -1 & 0 & 0 & \frac{1}{2} \end{bmatrix}$         | 1   |
| 11  | $\{3_{-1-11}^-  \frac{1}{2}\frac{1}{2}0\}$               | $\begin{bmatrix} 0 & 1 & 0 & \frac{1}{2} \\ 0 & 0 & -1 & \frac{1}{2} \\ -1 & 0 & 0 & 0 \end{bmatrix}$         | 1   |
| 12  | $\{3_{-11-1}^-  \frac{1}{2}0\frac{1}{2}\}$               | $\begin{bmatrix} 0 & -1 & 0 & \frac{1}{2} \\ 0 & 0 & -1 & 0 \\ 1 & 0 & 0 & \frac{1}{2} \end{bmatrix}$         | 1   |
| 13  | $\{\text{m}_{1-10}  \frac{1}{4}\frac{1}{4}\frac{1}{4}\}$ | $\begin{bmatrix} 0 & 1 & 0 & \frac{1}{4} \\ 1 & 0 & 0 & \frac{1}{4} \\ 0 & 0 & 1 & \frac{1}{4} \end{bmatrix}$ | -1  |

continued ...

Table 1

| No. | tag  | matrix (polar)  | det |
|-----|--|---|-----|
| 14  | $\{m_{110}   \frac{1}{4} \frac{3}{4} \frac{3}{4}\}$    | $\begin{bmatrix} 0 & -1 & 0 & \frac{1}{4} \\ -1 & 0 & 0 & \frac{3}{4} \\ 0 & 0 & 1 & \frac{3}{4} \end{bmatrix}$ | -1  |
| 15  | $\{-4^+_{001}   \frac{3}{4} \frac{1}{4} \frac{3}{4}\}$ | $\begin{bmatrix} 0 & 1 & 0 & \frac{3}{4} \\ -1 & 0 & 0 & \frac{1}{4} \\ 0 & 0 & -1 & \frac{3}{4} \end{bmatrix}$ | -1  |
| 16  | $\{-4^-_{001}   \frac{3}{4} \frac{3}{4} \frac{1}{4}\}$ | $\begin{bmatrix} 0 & -1 & 0 & \frac{3}{4} \\ 1 & 0 & 0 & \frac{3}{4} \\ 0 & 0 & -1 & \frac{1}{4} \end{bmatrix}$ | -1  |
| 17  | $\{m_{01-1}   \frac{1}{4} \frac{1}{4} \frac{1}{4}\}$   | $\begin{bmatrix} 1 & 0 & 0 & \frac{1}{4} \\ 0 & 0 & 1 & \frac{1}{4} \\ 0 & 1 & 0 & \frac{1}{4} \end{bmatrix}$   | -1  |
| 18  | $\{-4^+_{100}   \frac{3}{4} \frac{3}{4} \frac{1}{4}\}$ | $\begin{bmatrix} -1 & 0 & 0 & \frac{3}{4} \\ 0 & 0 & 1 & \frac{3}{4} \\ 0 & -1 & 0 & \frac{1}{4} \end{bmatrix}$ | -1  |
| 19  | $\{-4^-_{100}   \frac{1}{4} \frac{3}{4} \frac{3}{4}\}$ | $\begin{bmatrix} -1 & 0 & 0 & \frac{1}{4} \\ 0 & 0 & -1 & \frac{3}{4} \\ 0 & 1 & 0 & \frac{3}{4} \end{bmatrix}$ | -1  |
| 20  | $\{m_{011}   \frac{3}{4} \frac{1}{4} \frac{3}{4}\}$    | $\begin{bmatrix} 1 & 0 & 0 & \frac{3}{4} \\ 0 & 0 & -1 & \frac{1}{4} \\ 0 & -1 & 0 & \frac{3}{4} \end{bmatrix}$ | -1  |
| 21  | $\{m_{-101}   \frac{1}{4} \frac{1}{4} \frac{1}{4}\}$   | $\begin{bmatrix} 0 & 0 & 1 & \frac{1}{4} \\ 0 & 1 & 0 & \frac{1}{4} \\ 1 & 0 & 0 & \frac{1}{4} \end{bmatrix}$   | -1  |
| 22  | $\{-4^-_{010}   \frac{3}{4} \frac{1}{4} \frac{3}{4}\}$ | $\begin{bmatrix} 0 & 0 & 1 & \frac{3}{4} \\ 0 & -1 & 0 & \frac{1}{4} \\ -1 & 0 & 0 & \frac{3}{4} \end{bmatrix}$ | -1  |
| 23  | $\{m_{101}   \frac{3}{4} \frac{3}{4} \frac{1}{4}\}$    | $\begin{bmatrix} 0 & 0 & -1 & \frac{3}{4} \\ 0 & 1 & 0 & \frac{3}{4} \\ -1 & 0 & 0 & \frac{1}{4} \end{bmatrix}$ | -1  |
| 24  | $\{-4^+_{010}   \frac{1}{4} \frac{3}{4} \frac{3}{4}\}$ | $\begin{bmatrix} 0 & 0 & -1 & \frac{1}{4} \\ 0 & -1 & 0 & \frac{3}{4} \\ 1 & 0 & 0 & \frac{3}{4} \end{bmatrix}$ | -1  |