No. 29 T_h m-3 [cubic] (axial)

表 1 rank 0

No.	irrep.	(tag)	mul.	comp.	harmonics	(tag)	definition
1	A_u	Au	_	-	$\mathbb{G}_0^{(h,A_u)}$	${\tt Gh}({\tt O},{\tt Au},,)$	C_0

表 2 rank 1

No	o. irrej	o. (tag)	mul.	comp.	harmonics	(tag)	definition
2	T_g	Tg	-	0	$\mathbb{G}_{1,0}^{(h,T_g)}$	${\tt Gh}(1,{\tt Tg},,0)$	C_1
3	T_g	Tg	_	1	-,-	(, 0, , ,	S_1
4	T_g	Tg		2	$\mathbb{G}_{1,2}^{(h,T_g)}$	${\tt Gh(1,Tg,,2)}$	C_0

表 3 rank 2

No.	irrep.	(tag)	mul.	comp.	harmonics	(tag)	definition
5	E_u	Eu	_	0	$\mathbb{G}_{2,0}^{(h,E_u)}$	${\tt Gh(2,Eu,,0)}$	C_0
6	E_u	Eu	_	1	$\mathbb{G}_{2,1}^{(h,E_u)}$	${\tt Gh(2,Eu,,1)}$	C_2
7	T_u	Tu	_	0	$\mathbb{G}_{2,0}^{(h,T_u)}$	${\tt Gh(2,Tu,,0)}$	S_1
8	T_u	Tu	_	1	$\mathbb{G}_{2,1}^{(h,T_u)}$	${\tt Gh(2,Tu,,1)}$	C_1
9	T_u	Tu	-	2	$\mathbb{G}_{2,2}^{(h,T_u)}$	${\tt Gh(2,Tu,,2)}$	S_2

表 4 rank 3

No.	irrep.	(tag)	mul.	comp.	harmonics	(tag)	definition
10	A_g	Ag	_	_	$\mathbb{G}_3^{(h,A_g)}$	${\tt Gh(3,Ag,,)}$	S_2
11	T_g	Tg	1	0	$\mathbb{G}_{3,0}^{(h,T_g,1)}$	${\tt Gh(3,Tg,1,0)}$	$-\frac{\sqrt{6}C_1}{4} + \frac{\sqrt{10}C_3}{4}$
12	T_g	Tg	1	1	$\mathbb{G}_{3,1}^{(h,T_g,1)}$	${\tt Gh(3,Tg,1,1)}$	$-\frac{\sqrt{6}S_1}{4} - \frac{\sqrt{10}S_3}{4}$
13	T_g	Tg	1	2	$\mathbb{G}_{3,2}^{(h,T_g,1)}$	${\tt Gh}(3,{\tt Tg},1,2)$	C_0
14	T_g	Tg	2	0	$\mathbb{G}_{3,0}^{(h,T_g,2)}$	${\tt Gh(3,Tg,2,0)}$	$-\frac{\sqrt{10}C_1}{4} - \frac{\sqrt{6}C_3}{4}$
15	T_g	Tg	2	1	$\mathbb{G}_{3,1}^{(h,T_g,2)}$	${\tt Gh}({\tt 3},{\tt Tg},2,1)$	$\frac{\sqrt{10}S_1}{4} - \frac{\sqrt{6}S_3}{4}$
16	T_g	Tg	2	2	$\mathbb{G}_{3,2}^{(h,T_g,2)}$	${\tt Gh(3,Tg,2,2)}$	C_2

表 5 rank 4

No.	irrep.	(tag)	mul.	comp.	harmonics	(tag)	definition
17	A_u	Au	_	_	$\mathbb{G}_4^{(h,A_u)}$	${\tt Gh(4,Au,,)}$	$\frac{\sqrt{21}C_0}{6} + \frac{\sqrt{15}C_4}{6}$
18	E_u	Eu	_	0	$\mathbb{G}_{4,0}^{(h,E_u)}$	${\tt Gh(4,Eu,,0)}$	$\frac{\sqrt{15}C_0}{6} - \frac{\sqrt{21}C_4}{6}$
19	E_u	Eu	_	1	$\mathbb{G}_{4,1}^{(h,E_u)}$	${\tt Gh(4,Eu,,1)}$	$-C_2$
20	T_u	Tu	1	0	$\mathbb{G}_{4,0}^{(h,T_u,1)}$	${\tt Gh(4,Tu,1,0)}$	$-\frac{\sqrt{14}S_1}{4} - \frac{\sqrt{2}S_3}{4}$
21	T_u	Tu	1	1	$\mathbb{G}_{4,1}^{(h,T_u,1)}$	${\tt Gh}(4,{\tt Tu},1,1)$	$\frac{\sqrt{14}C_1}{4} - \frac{\sqrt{2}C_3}{4}$
22	T_u	Tu	1	2	$\mathbb{G}_{4,2}^{(h,T_u,1)}$	${\tt Gh}(4,{\tt Tu},1,2)$	S_4
23	T_u	Tu	2	0	$\mathbb{G}_{4,0}^{(h,T_u,2)}$	${\tt Gh(4,Tu,2,0)}$	$-\frac{\sqrt{2}S_1}{4} + \frac{\sqrt{14}S_3}{4}$
24	T_u	Tu	2	1	$\mathbb{G}_{4,1}^{(h,T_u,2)}$	${\tt Gh}(4,{\tt Tu},2,1)$	$-\frac{\sqrt{2}C_1}{4} - \frac{\sqrt{14}C_3}{4}$
25	T_u	Tu	2	2	$\mathbb{G}_{4,2}^{(h,T_u,2)}$	${\tt Gh}(4,{\tt Tu},2,2)$	S_2

表 6 rank 5

No.	irrep.	(tag)	mul.	comp.	harmonics	(tag)	definition
26	E_g	Eg	-	0	$\mathbb{G}_{5,0}^{(h,E_g)}$	${\tt Gh}({\tt 5},{\tt Eg},,{\tt 0})$	S_4
27	E_g	Eg	_	1	$\mathbb{G}_{5,1}^{(h,E_g)}$	${\tt Gh(5,Eg,,1)}$	$-S_2$
28	T_g	Tg	1	0	$\mathbb{G}_{5,0}^{(h,T_g,1)}$	${\tt Gh(5,Tg,1,0)}$	$\frac{\sqrt{15}C_1}{8} - \frac{\sqrt{70}C_3}{16} + \frac{3\sqrt{14}C_5}{16}$
29	T_g	Tg	1	1	$\mathbb{G}_{5,1}^{(h,T_g,1)}$	${\tt Gh}({\tt 5},{\tt Tg},{\tt 1},{\tt 1})$	$\frac{\sqrt{15}S_1}{8} + \frac{\sqrt{70}S_3}{16} + \frac{3\sqrt{14}S_5}{16}$
30	T_g	Tg	1	2	$\mathbb{G}_{5,2}^{(h,T_g,1)}$	${\tt Gh}({\tt 5},{\tt Tg},{\tt 1},{\tt 2})$	C_0
31	T_g	Tg	2	0	$\mathbb{G}_{5,0}^{(h,T_g,2)}$	${\tt Gh}({\tt 5},{\tt Tg},{\tt 2},{\tt 0})$	$\frac{\sqrt{21}C_1}{8} + \frac{9\sqrt{2}C_3}{16} + \frac{\sqrt{10}C_5}{16}$
32	T_g	Tg	2	1	$\mathbb{G}_{5,1}^{(h,T_g,2)}$	${\tt Gh(5,Tg,2,1)}$	$\frac{\sqrt{21}S_1}{8} - \frac{9\sqrt{2}S_3}{16} + \frac{\sqrt{10}S_5}{16}$
33	T_g	Tg	2	2	$\mathbb{G}_{5,2}^{(h,T_g,2)}$	${\tt Gh(5,Tg,2,2)}$	C_4
34	T_g	Tg	3	0	$\mathbb{G}_{5,0}^{(h,T_g,3)}$	${\tt Gh(5,Tg,3,0)}$	$\frac{\sqrt{7}C_1}{4} - \frac{\sqrt{6}C_3}{8} - \frac{\sqrt{30}C_5}{8}$
35	T_g	Tg	3	1	$\mathbb{G}_{5,1}^{(h,T_g,3)}$	${\tt Gh(5,Tg,3,1)}$	$-\frac{\sqrt{7}S_1}{4} - \frac{\sqrt{6}S_3}{8} + \frac{\sqrt{30}S_5}{8}$
36	T_g	Tg	3	2	$\mathbb{G}_{5,2}^{(h,T_g,3)}$	${\tt Gh(5,Tg,3,2)}$	C_2

表 7 rank 6

No.	irrep.	(tag)	mul.	comp.	harmonics	(tag)	definition
37	A_u	Au	1	-	$\mathbb{G}_6^{(h,A_u,1)}$	${\tt Gh(6,Au,1,)}$	$\frac{\sqrt{2}C_0}{4} = \frac{\sqrt{14}C_4}{4}$
38	A_u	Au	2	_	$\mathbb{G}_6^{(h,A_u,2)}$	${\tt Gh(6,Au,2,)}$	$\frac{\sqrt{11}C_2}{4} - \frac{\sqrt{5}C_6}{4}$
39	E_u	Eu	_	0	$\mathbb{G}_{6,0}^{(h,E_u)}$	${\tt Gh}(6, {\tt Eu},, 0)$	$\frac{\sqrt{2}\left(\sqrt{7}C_0 + C_4\right)}{4}$
40	E_u	Eu	_	1	$\mathbb{G}_{6,1}^{(h,E_u)}$	${\tt Gh}(6, {\tt Eu},, 1)$	$\frac{\sqrt{5}C_2}{4} + \frac{\sqrt{11}C_6}{4}$
41	T_u	Tu	1	0	$\mathbb{G}_{6,0}^{(h,T_u,1)}$	${\tt Gh}(6,{\tt Tu},1,0)$	$\frac{\sqrt{3}S_1}{4} - \frac{\sqrt{30}S_3}{8} - \frac{\sqrt{22}S_5}{8}$
42	T_u	Tu	1	1	$\mathbb{G}_{6,1}^{(h,T_u,1)}$	${\tt Gh}(6,{\tt Tu},1,1)$	$-\frac{\sqrt{3}C_1}{4} - \frac{\sqrt{30}C_3}{8} + \frac{\sqrt{22}C_5}{8}$
43	T_u	Tu	1	2	$\mathbb{G}_{6,2}^{(h,T_u,1)}$	${\tt Gh}(6,{\tt Tu},1,2)$	S_4
44	T_u	Tu	2	0	$\mathbb{G}_{6,0}^{(h,T_u,2)}$	${\tt Gh}(6,{\tt Tu},2,0)$	$\frac{3\sqrt{22}S_1}{16} + \frac{\sqrt{55}S_3}{16} + \frac{\sqrt{3}S_5}{16}$
45	T_u	Tu	2	1	$\mathbb{G}_{6,1}^{(h,T_u,2)}$	${\tt Gh}(6,{\tt Tu},2,1)$	$\frac{3\sqrt{22}C_1}{16} - \frac{\sqrt{55}C_3}{16} + \frac{\sqrt{3}C_5}{16}$
46	T_u	Tu	2	2	$\mathbb{G}_{6,2}^{(h,T_u,2)}$	${\tt Gh}(6,{\tt Tu},2,2)$	S_6
47	T_u	Tu	3	0	$\mathbb{G}_{6,0}^{(h,T_u,3)}$	${\tt Gh}(6,{\tt Tu},3,0)$	$\frac{\sqrt{10}S_1}{16} - \frac{9S_3}{16} + \frac{\sqrt{165}S_5}{16}$
48	T_u	Tu	3	1	$\mathbb{G}_{6,1}^{(h,T_u,3)}$	${\tt Gh}(6,{\tt Tu},3,1)$	$\frac{\sqrt{10}C_1}{16} + \frac{9C_3}{16} + \frac{\sqrt{165}C_5}{16}$
49	T_u	Tu	3	2	$\mathbb{G}_{6,2}^{(h,T_u,3)}$	${\tt Gh}(6,{\tt Tu},3,2)$	S_2

表 8 rank 7

No.	irrep.	(tag)	mul.	comp.	harmonics	(tag)	definition
50	A_g	Ag	_	_	$\mathbb{G}_7^{(h,A_g)}$	${\tt Gh(7,Ag,,)}$	$\frac{\sqrt{78}S_2}{12} + \frac{\sqrt{66}S_6}{12}$
51	E_g	Eg	_	0	$\mathbb{G}_{7,0}^{(h,E_g)}$	${\tt Gh(7,Eg,,0)}$	S_4
52	E_g	Eg	_	1	$\mathbb{G}_{7,1}^{(h,E_g)}$	${\tt Gh(7,Eg,,1)}$	$\frac{\sqrt{66}S_2}{12} - \frac{\sqrt{78}S_6}{12}$
53	T_g	Tg	1	0	$\mathbb{G}_{7,0}^{(h,T_g,1)}$	${\tt Gh(7,Tg,1,0)}$	$-\frac{5\sqrt{7}C_1}{32} + \frac{3\sqrt{21}C_3}{32} - \frac{\sqrt{231}C_5}{32} + \frac{\sqrt{429}C_7}{32}$
54	T_g	Tg	1	1	$\mathbb{G}_{7,1}^{(h,T_g,1)}$	${\tt Gh(7,Tg,1,1)}$	$-\frac{5\sqrt{7}S_1}{32} - \frac{3\sqrt{21}S_3}{32} - \frac{\sqrt{231}S_5}{32} - \frac{\sqrt{429}S_7}{32}$
55	T_g	Tg	1	2	$\mathbb{G}_{7,2}^{(h,T_g,1)}$	${\tt Gh}(7,{\tt Tg},1,2)$	C_0
56	T_g	Tg	2	0	$\mathbb{G}_{7,0}^{(h,T_g,2)}$	${\tt Gh}(7,{\tt Tg},2,0)$	$-\frac{3\sqrt{33}C_1}{32} - \frac{\sqrt{11}C_3}{32} + \frac{25C_5}{32} + \frac{\sqrt{91}C_7}{32}$
57	T_g	Tg	2	1	$\mathbb{G}_{7,1}^{(h,T_g,2)}$	${\tt Gh(7,Tg,2,1)}$	$-\frac{3\sqrt{33}S_1}{32} + \frac{\sqrt{11}S_3}{32} + \frac{25S_5}{32} - \frac{\sqrt{91}S_7}{32}$
58	T_g	Tg	2	2	$\mathbb{G}_{7,2}^{(h,T_g,2)}$	${\tt Gh(7,Tg,2,2)}$	C_4
59	T_g	Tg	3	0	$\mathbb{G}_{7,0}^{(h,T_g,3)}$	${\tt Gh(7,Tg,3,0)}$	$-\frac{\sqrt{858}C_1}{64} - \frac{3\sqrt{286}C_3}{64} - \frac{5\sqrt{26}C_5}{64} - \frac{\sqrt{14}C_7}{64}$
60	T_g	Tg	3	1	$\mathbb{G}_{7,1}^{(h,T_g,3)}$	${\tt Gh(7,Tg,3,1)}$	$\frac{\sqrt{858}S_1}{64} - \frac{3\sqrt{286}S_3}{64} + \frac{5\sqrt{26}S_5}{64} - \frac{\sqrt{14}S_7}{64}$
61	T_g	Tg	3	2	$\mathbb{G}_{7,2}^{(h,T_g,3)}$	${\tt Gh}(7,{\tt Tg},3,2)$	C_6
62	T_g	Tg	4	0	$\mathbb{G}_{7,0}^{(h,T_g,4)}$	${\tt Gh(7,Tg,4,0)}$	$-\frac{15\sqrt{6}C_1}{64} + \frac{19\sqrt{2}C_3}{64} - \frac{\sqrt{22}C_5}{64} - \frac{\sqrt{2002}C_7}{64}$
63	T_g	Tg	4	1	$\mathbb{G}_{7,1}^{(h,T_g,4)}$	${\tt Gh}(7,{\tt Tg},4,1)$	$\frac{15\sqrt{6}S_1}{64} + \frac{19\sqrt{2}S_3}{64} + \frac{\sqrt{22}S_5}{64} - \frac{\sqrt{2002}S_7}{64}$
64	T_g	Tg	4	2	$\mathbb{G}_{7,2}^{(h,T_g,4)}$	${\tt Gh}(7,{\tt Tg},4,2)$	C_2

表 9 rank 8

No.	irrep.	(tag)	mul.	comp.	harmonics	(tag)	definition
65	A_u	Au	_	_	$\mathbb{G}_8^{(h,A_u)}$	Gh(8, Au,,)	$\frac{\sqrt{33}C_0}{8} + \frac{\sqrt{21}C_4}{12} + \frac{\sqrt{195}C_8}{24}$
66	E_u	Eu	1	0	$\mathbb{G}_{8,0}^{(h,E_u,1)}$	${\tt Gh(8,Eu,1,0)}$	$-\frac{\sqrt{286}C_0}{32} + \frac{\sqrt{182}C_4}{16} + \frac{\sqrt{10}C_8}{32}$
67	E_u	Eu	1	1	$\mathbb{G}_{8,1}^{(h,E_u,1)}$	${\tt Gh(8,Eu,1,1)}$	C_6
68	E_u	Eu	2	0	$\mathbb{G}_{8,0}^{(h,E_u,2)}$	${\tt Gh(8,Eu,2,0)}$	$-\frac{\sqrt{210}C_0}{32} - \frac{\sqrt{330}C_4}{48} + \frac{\sqrt{6006}C_8}{96}$
69	E_u	Eu	2	1	$\mathbb{G}_{8,1}^{(h,E_u,2)}$	${\tt Gh(8,Eu,2,1)}$	C_2
70	T_u	Tu	1	0	$\mathbb{G}_{8,0}^{(h,T_u,1)}$	${\tt Gh(8,Tu,1,0)}$	$-\frac{\sqrt{715}S_1}{32} - \frac{\sqrt{273}S_3}{32} - \frac{\sqrt{35}S_5}{32} - \frac{S_7}{32}$
71	T_u	Tu	1	1	$\mathbb{G}_{8,1}^{(h,T_u,1)}$	${\tt Gh(8,Tu,1,1)}$	$\frac{\sqrt{715}C_1}{32} - \frac{\sqrt{273}C_3}{32} + \frac{\sqrt{35}C_5}{32} - \frac{C_7}{32}$
72	T_u	Tu	1	2	$\mathbb{G}_{8,2}^{(h,T_u,1)}$	${\tt Gh(8,Tu,1,2)}$	S_8
73	T_u	Tu	2	0	$\mathbb{G}_{8,0}^{(h,T_u,2)}$	${\tt Gh(8,Tu,2,0)}$	$-\frac{\sqrt{77}S_1}{32} + \frac{5\sqrt{15}S_3}{32} - \frac{3\sqrt{13}S_5}{32} - \frac{\sqrt{455}S_7}{32}$
74	T_u	Tu	2	1	$\mathbb{G}_{8,1}^{(h,T_u,2)}$	${\tt Gh(8,Tu,2,1)}$	$\frac{\sqrt{77}C_1}{32} + \frac{5\sqrt{15}C_3}{32} + \frac{3\sqrt{13}C_5}{32} - \frac{\sqrt{455}C_7}{32}$
75	T_u	Tu	2	2	$\mathbb{G}_{8,2}^{(h,T_u,2)}$	${\tt Gh(8,Tu,2,2)}$	S_4
76	T_u	Tu	3	0	$\mathbb{G}_{8,0}^{(h,T_u,3)}$	${\tt Gh(8,Tu,3,0)}$	$-\frac{\sqrt{858}S_1}{64} + \frac{\sqrt{910}S_3}{64} + \frac{7\sqrt{42}S_5}{64} + \frac{3\sqrt{30}S_7}{64}$
77	T_u	Tu	3	1	$\mathbb{G}_{8,1}^{(h,T_u,3)}$	${\tt Gh(8,Tu,3,1)}$	$-\frac{\sqrt{858}C_1}{64} - \frac{\sqrt{910}C_3}{64} + \frac{7\sqrt{42}C_5}{64} - \frac{3\sqrt{30}C_7}{64}$
78	T_u	Tu	3	2	$\mathbb{G}_{8,2}^{(h,T_u,3)}$	${\tt Gh(8,Tu,3,2)}$	S_6
79	T_u	Tu	4	0	$\mathbb{G}_{8,0}^{(h,T_u,4)}$	${\tt Gh(8,Tu,4,0)}$	$-\frac{\sqrt{70}S_1}{64} + \frac{3\sqrt{66}S_3}{64} - \frac{\sqrt{1430}S_5}{64} + \frac{\sqrt{2002}S_7}{64}$
80	T_u	Tu	4	1	$\mathbb{G}_{8,1}^{(h,T_u,4)}$	${\tt Gh(8,Tu,4,1)}$	$-\frac{\sqrt{70}C_1}{64} - \frac{3\sqrt{66}C_3}{64} - \frac{\sqrt{1430}C_5}{64} - \frac{\sqrt{2002}C_7}{64}$
81	T_u	Tu	4	2	$\mathbb{G}_{8,2}^{(h,T_u,4)}$	${\tt Gh(8,Tu,4,2)}$	S_2

No.	irrep.	(tag)	mul.	comp.	harmonics	(tag)	definition
82	A_g	Ag	1	-	$\mathbb{G}_9^{(h,A_g,1)}$	Gh(9, Ag, 1,)	$\frac{\sqrt{102}S_4}{12} - \frac{\sqrt{42}S_8}{12}$
83	A_g	Ag	2	-	$\mathbb{G}_9^{(h,A_g,2)}$	${\tt Gh(9,Ag,2,)}$	$rac{\sqrt{3}S_2}{4} - rac{\sqrt{13}S_6}{4}$
84	E_g	Eg	_	0	$\mathbb{G}_{9,0}^{(h,E_g)}$	${\tt Gh}(9, {\tt Eg},, 0)$	$rac{\sqrt{42}S_4}{12} + rac{\sqrt{102}S_8}{12}$
85	E_g	Eg	_	1	$\mathbb{G}_{9,1}^{(h,E_g)}$	${\tt Gh}(9,{\tt Eg},,1)$	$-rac{\sqrt{13}S_2}{4} - rac{\sqrt{3}S_6}{4}$
86	T_g	Tg	1	0	$\mathbb{G}_{9,0}^{(h,T_g,1)}$	${\tt Gh(9,Tg,1,0)}$	$\frac{21\sqrt{5}C_1}{128} - \frac{\sqrt{2310}C_3}{128} + \frac{3\sqrt{286}C_5}{128} - \frac{3\sqrt{1430}C_7}{256} + \frac{\sqrt{24310}C_9}{256}$
87	T_g	Tg	1	1	$\mathbb{G}_{9,1}^{(h,T_g,1)}$	${\tt Gh(9,Tg,1,1)}$	$\frac{21\sqrt{5}S_1}{128} + \frac{\sqrt{2310}S_3}{128} + \frac{3\sqrt{286}S_5}{128} + \frac{3\sqrt{1430}S_7}{256} + \frac{\sqrt{24310}S_9}{256}$
88	T_g	Tg	1	2	$\mathbb{G}_{9,2}^{(h,T_g,1)}$	${\tt Gh(9,Tg,1,2)}$	C_0
89	T_g	Tg	2	0	$\mathbb{G}_{9,0}^{(h,T_g,2)}$	${\tt Gh(9,Tg,2,0)}$	$\frac{\sqrt{2431}C_1}{128} + \frac{\sqrt{9282}C_3}{128} + \frac{5\sqrt{170}C_5}{128} + \frac{7\sqrt{34}C_7}{256} + \frac{3\sqrt{2}C_9}{256}$
90	T_g	Tg	2	1	$\mathbb{G}_{9,1}^{(h,T_g,2)}$	${\tt Gh(9,Tg,2,1)}$	$\frac{\sqrt{2431}S_1}{128} - \frac{\sqrt{9282}S_3}{128} + \frac{5\sqrt{170}S_5}{128} - \frac{7\sqrt{34}S_7}{256} + \frac{3\sqrt{2}S_9}{256}$
91	T_g	Tg	2	2	$\mathbb{G}_{9,2}^{(h,T_g,2)}$	${\tt Gh(9,Tg,2,2)}$	C_8
92	T_g	Tg	3	0	$\mathbb{G}_{9,0}^{(h,T_g,3)}$	${\tt Gh(9,Tg,3,0)}$	$\frac{\sqrt{1001}C_1}{64} - \frac{\sqrt{78}C_3}{64} - \frac{3\sqrt{70}C_5}{64} + \frac{23\sqrt{14}C_7}{128} + \frac{3\sqrt{238}C_9}{128}$
93	T_g	Tg	3	1	$\mathbb{G}_{9,1}^{(h,T_g,3)}$	${\tt Gh(9,Tg,3,1)}$	$\frac{\sqrt{1001}S_1}{64} + \frac{\sqrt{78}S_3}{64} - \frac{3\sqrt{70}S_5}{64} - \frac{23\sqrt{14}S_7}{128} + \frac{3\sqrt{238}S_9}{128}$
94	T_g	Tg	3	2	$\mathbb{G}_{9,2}^{(h,T_g,3)}$	${\tt Gh(9,Tg,3,2)}$	C_4
95	T_g	Tg	4	0	$\mathbb{G}_{9,0}^{(h,T_g,4)}$	${\tt Gh(9,Tg,4,0)}$	$\frac{\sqrt{858}C_1}{64} + \frac{\sqrt{91}C_3}{32} - \frac{5\sqrt{15}C_5}{32} - \frac{21\sqrt{3}C_7}{64} - \frac{\sqrt{51}C_9}{64}$
96	T_g	Tg	4	1	$\mathbb{G}_{9,1}^{(h,T_g,4)}$	${\tt Gh(9,Tg,4,1)}$	$-\frac{\sqrt{858}S_1}{64} + \frac{\sqrt{91}S_3}{32} + \frac{5\sqrt{15}S_5}{32} - \frac{21\sqrt{3}S_7}{64} + \frac{\sqrt{51}S_9}{64}$
97	T_g	Tg	4	2	$\mathbb{G}_{9,2}^{(h,T_g,4)}$	${\tt Gh(9,Tg,4,2)}$	C_6
98	T_g	Tg	5	0	$\mathbb{G}_{9,0}^{(h,T_g,5)}$	${\tt Gh(9,Tg,5,0)}$	$\frac{7\sqrt{22}C_1}{64} - \frac{3\sqrt{21}C_3}{32} + \frac{\sqrt{65}C_5}{32} + \frac{\sqrt{13}C_7}{64} - \frac{3\sqrt{221}C_9}{64}$
99	T_g	Tg	5	1	$\mathbb{G}_{9,1}^{(h,T_g,5)}$	${\tt Gh(9,Tg,5,1)}$	$-\frac{7\sqrt{22}S_1}{64} - \frac{3\sqrt{21}S_3}{32} - \frac{\sqrt{65}S_5}{32} + \frac{\sqrt{13}S_7}{64} + \frac{3\sqrt{221}S_9}{64}$
100	T_g	Tg	5	2	$\mathbb{G}_{9,2}^{(h,T_g,5)}$	${\tt Gh}(9,{\tt Tg},{\tt 5},{\tt 2})$	C_2

表 11 rank 10

No.	irrep.	(tag)	mul.	comp.	harmonics	(tag)	definition
101	A_u	Au	1	-	$\mathbb{G}_{10}^{(h,A_u,1)}$	${\tt Gh(10,Au,1,)}$	$\frac{\sqrt{390}C_0}{48} - \frac{\sqrt{22}C_4}{8} - \frac{\sqrt{1122}C_8}{48}$
102	A_u	Au	2	-	$\mathbb{G}_{10}^{(h,A_u,2)}$	${\tt Gh(10,Au,2,)}$	$-\frac{\sqrt{85}C_{10}}{16} + \frac{\sqrt{1482}C_2}{48} + \frac{\sqrt{57}C_6}{48}$
103	E_u	Eu	1	0	$\mathbb{G}_{10,0}^{(h,E_u,1)}$	${\tt Gh(10,Eu,1,0)}$	$\frac{11\sqrt{420189}C_0}{8988} + \frac{\sqrt{827645}C_4}{1498} - \frac{\sqrt{146055}C_8}{8988}$
104	E_u	Eu	1	1	$\mathbb{G}_{10,1}^{(h,E_u,1)}$	${\tt Gh(10,Eu,1,1)}$	$\frac{\sqrt{370006}C_{10}}{749} + \frac{\sqrt{190995}C_2}{749}$
105	E_u	Eu	2	0	$\mathbb{G}_{10,0}^{(h,E_u,2)}$	${\tt Gh(10,Eu,2,0)}$	$\frac{3\sqrt{3213210}C_0}{11984} - \frac{83\sqrt{1498}C_4}{5992} + \frac{31\sqrt{76398}C_8}{11984}$
106	E_u	Eu	2	1	$\mathbb{G}_{10,1}^{(h,E_u,2)}$	${\tt Gh(10,Eu,2,1)}$	$\frac{\sqrt{1209635}C_{10}}{11984} - \frac{19\sqrt{58422}C_2}{35952} + \frac{\sqrt{2247}C_6}{48}$
107	T_u	Tu	1	0	$\mathbb{G}_{10,0}^{(h,T_u,1)}$	${\tt Gh(10,Tu,1,0)}$	$\frac{\sqrt{221}S_1}{32} - \frac{\sqrt{102}S_3}{32} - \frac{\sqrt{510}S_5}{32} - \frac{11\sqrt{6}S_7}{64} - \frac{\sqrt{38}S_9}{64}$
108	T_u	Tu	1	1	$\mathbb{G}_{10,1}^{(h,T_u,1)}$	${\tt Gh(10,Tu,1,1)}$	$-\frac{\sqrt{221}C_1}{32} - \frac{\sqrt{102}C_3}{32} + \frac{\sqrt{510}C_5}{32} - \frac{11\sqrt{6}C_7}{64} + \frac{\sqrt{38}C_9}{64}$
109	T_u	Tu	1	2	$\mathbb{G}_{10,2}^{(h,T_u,1)}$	${\tt Gh(10,Tu,1,2)}$	S_8
110	T_u	Tu	2	0	$\mathbb{G}_{10,0}^{(h,T_u,2)}$	${\tt Gh(10,Tu,2,0)}$	$\frac{\sqrt{39}S_1}{32} - \frac{11\sqrt{2}S_3}{32} + \frac{5\sqrt{10}S_5}{32} - \frac{\sqrt{34}S_7}{64} - \frac{\sqrt{1938}S_9}{64}$
111	T_u	Tu	2	1	$\mathbb{G}_{10,1}^{(h,T_u,2)}$	${\tt Gh(10,Tu,2,1)}$	$-\frac{\sqrt{39}C_1}{32} - \frac{11\sqrt{2}C_3}{32} - \frac{5\sqrt{10}C_5}{32} - \frac{\sqrt{34}C_7}{64} + \frac{\sqrt{1938}C_9}{64}$
112	T_u	Tu	2	2	$\mathbb{G}_{10,2}^{(h,T_u,2)}$	${\tt Gh(10,Tu,2,2)}$	S_4
113	T_u	Tu	3	0	$\mathbb{G}_{10,0}^{(h,T_u,3)}$	${\tt Gh(10,Tu,3,0)}$	$\frac{\sqrt{41990}S_1}{256} + \frac{\sqrt{4845}S_3}{128} + \frac{\sqrt{969}S_5}{128} + \frac{\sqrt{285}S_7}{256} + \frac{\sqrt{5}S_9}{256}$
114	T_u	Tu	3	1	$\mathbb{G}_{10,1}^{(h,T_u,3)}$	${\tt Gh(10,Tu,3,1)}$	$\frac{\sqrt{41990}C_1}{256} - \frac{\sqrt{4845}C_3}{128} + \frac{\sqrt{969}C_5}{128} - \frac{\sqrt{285}C_7}{256} + \frac{\sqrt{5}C_9}{256}$
115	T_u	Tu	3	2	$\mathbb{G}_{10,2}^{(h,T_u,3)}$	${\tt Gh(10,Tu,3,2)}$	S_{10}
116	T_u	Tu	4	0	$\mathbb{G}_{10,0}^{(h,T_u,4)}$	${\tt Gh(10,Tu,4,0)}$	$\frac{9\sqrt{78}S_1}{256} - \frac{69S_3}{128} - \frac{\sqrt{5}S_5}{128} + \frac{43\sqrt{17}S_7}{256} + \frac{3\sqrt{969}S_9}{256}$
117	T_u	Tu	4	1	$\mathbb{G}_{10,1}^{(h,T_u,4)}$	${\tt Gh(10,Tu,4,1)}$	$\frac{9\sqrt{78}C_1}{256} + \frac{69C_3}{128} - \frac{\sqrt{5}C_5}{128} - \frac{43\sqrt{17}C_7}{256} + \frac{3\sqrt{969}C_9}{256}$
118	T_u	Tu	4	2	$\mathbb{G}_{10,2}^{(h,T_u,4)}$	${\tt Gh(10,Tu,4,2)}$	S_6
119	T_u	Tu	5	0	$\mathbb{G}_{10,0}^{(h,T_u,5)}$	${\tt Gh(10,Tu,5,0)}$	$\frac{7\sqrt{3}S_1}{128} - \frac{7\sqrt{26}S_3}{128} + \frac{5\sqrt{130}S_5}{128} - \frac{7\sqrt{442}S_7}{256} + \frac{\sqrt{25194}S_9}{256}$
120	T_u	Tu	5	1	$\mathbb{G}_{10,1}^{(h,T_u,5)}$	${\tt Gh(10,Tu,5,1)}$	$\frac{7\sqrt{3}C_1}{128} + \frac{7\sqrt{26}C_3}{128} + \frac{5\sqrt{130}C_5}{128} + \frac{7\sqrt{442}C_7}{256} + \frac{\sqrt{25194}C_9}{256}$
121	T_u	Tu	5	2	$\mathbb{G}_{10,2}^{(h,T_u,5)}$	${\tt Gh(10,Tu,5,2)}$	S_2

表 12 rank 11

						20,12	TAUK II
No.	irrep.	(tag)	mul.	comp.	harmonics	(tag)	definition
122	A_g	Ag	-	-	$\mathbb{G}_{11}^{(h,A_g)}$	${\tt Gh(11,Ag,,)}$	$\frac{\sqrt{798}S_{10}}{48} + \frac{\sqrt{255}S_2}{24} + \frac{3\sqrt{6}S_6}{16}$
123	E_g	Eg	1	0	$\mathbb{G}_{11,0}^{(h,E_g,1)}$	$\mathtt{Gh}(\mathtt{11},\mathtt{Eg},\mathtt{1},\mathtt{0})$	S_8
124	E_g	Eg	1	1	$\mathbb{G}_{11,1}^{(h,E_g,1)}$	$\mathtt{Gh}(\mathtt{11},\mathtt{Eg},\mathtt{1},\mathtt{1})$	$-\frac{\sqrt{210}S_{10}}{96} + \frac{\sqrt{969}S_2}{48} - \frac{\sqrt{570}S_6}{32}$
125	E_g	Eg	2	0	$\mathbb{G}_{11,0}^{(h,E_g,2)}$	${\tt Gh(11,Eg,2,0)}$	S_4
126	E_g	Eg	2	1	$\mathbb{G}_{11,1}^{(h,E_g,2)}$	${\tt Gh(11,Eg,2,1)}$	$-rac{\sqrt{646}S_{10}}{32}+rac{\sqrt{35}S_2}{16}+rac{\sqrt{238}S_6}{32}$
127	T_g	Tg	1	0	$\mathbb{G}_{11,0}^{(h,T_g,1)}$	$\mathtt{Gh}(\mathtt{11},\mathtt{Tg},\mathtt{1},\mathtt{0})$	$-\frac{21\sqrt{66}C_1}{512} + \frac{\sqrt{88179}C_{11}}{512} + \frac{\sqrt{30030}C_3}{512} - \frac{15\sqrt{143}C_5}{512} + \frac{\sqrt{36465}C_7}{512} - \frac{\sqrt{46189}C_9}{512}$
128	T_g	Tg	1	1	$\mathbb{G}_{11,1}^{(h,T_g,1)}$	$\mathtt{Gh}(\mathtt{11},\mathtt{Tg},\mathtt{1},\mathtt{1})$	$-\frac{21\sqrt{66}S_1}{512}-\frac{\sqrt{88179}S_{11}}{512}-\frac{\sqrt{30030}S_3}{512}-\frac{15\sqrt{143}S_5}{512}-\frac{\sqrt{36465}S_7}{512}-\frac{\sqrt{46189}S_9}{512}$
129	T_g	Tg	1	2	$\mathbb{G}_{11,2}^{(h,T_g,1)}$	${\tt Gh(11,Tg,1,2)}$	C_0
130	T_g	Tg	2	0	$\mathbb{G}_{11,0}^{(h,T_g,2)}$	${\tt Gh(11,Tg,2,0)}$	$-\frac{\sqrt{41990}C_1}{512} + \frac{\sqrt{385}C_{11}}{512} - \frac{3\sqrt{4522}C_3}{512} + \frac{3\sqrt{4845}C_5}{512} + \frac{77\sqrt{19}C_7}{512} + \frac{39\sqrt{15}C_9}{512}$
131	T_g	Tg	2	1	$\mathbb{G}_{11,1}^{(h,T_g,2)}$	${\tt Gh}({\tt 11},{\tt Tg},{\tt 2},{\tt 1})$	$-\frac{\sqrt{41990}S_1}{512} - \frac{\sqrt{385}S_{11}}{512} + \frac{3\sqrt{4522}S_3}{512} + \frac{3\sqrt{4845}S_5}{512} - \frac{77\sqrt{19}S_7}{512} + \frac{39\sqrt{15}S_9}{512}$
132	T_g	Tg	2	2	$\mathbb{G}_{11,2}^{(h,T_g,2)}$	${\tt Gh(11,Tg,2,2)}$	C_8
133	T_g	Tg	3	0	$\mathbb{G}_{11,0}^{(h,T_g,3)}$	${\tt Gh(11,Tg,3,0)}$	$-\frac{5\sqrt{546}C_1}{256}+\frac{\sqrt{10659}C_{11}}{256}+\frac{11\sqrt{30}C_3}{256}+\frac{13\sqrt{7}C_5}{256}-\frac{3\sqrt{1785}C_7}{256}+\frac{3\sqrt{2261}C_9}{256}$
134	T_g	Tg	3	1	$\mathbb{G}_{11,1}^{(h,T_g,3)}$	${\tt Gh(11,Tg,3,1)}$	$-\frac{5\sqrt{546}S_1}{256} - \frac{\sqrt{10659}S_{11}}{256} - \frac{11\sqrt{30}S_3}{256} + \frac{13\sqrt{7}S_5}{256} + \frac{3\sqrt{1785}S_7}{256} + \frac{3\sqrt{2261}S_9}{256}$
135	T_g	Tg	3	2	$\mathbb{G}_{11,2}^{(h,T_g,3)}$	${\tt Gh(11,Tg,3,2)}$	C_4
136	T_g	Tg	4	0	$\mathbb{G}_{11,0}^{(h,T_g,4)}$	${\tt Gh(11,Tg,4,0)}$	$-\frac{\sqrt{29393}C_1}{512} - \frac{\sqrt{22}C_{11}}{1024} - \frac{9\sqrt{1615}C_3}{512} - \frac{5\sqrt{13566}C_5}{1024} - \frac{7\sqrt{1330}C_7}{1024} - \frac{9\sqrt{42}C_9}{1024}$
137	T_g	Tg	4	1	$\mathbb{G}_{11,1}^{(h,T_g,4)}$	${\tt Gh}({\tt 11},{\tt Tg},{\tt 4},{\tt 1})$	$\frac{\sqrt{29393}S_1}{512} - \frac{\sqrt{22}S_{11}}{1024} - \frac{9\sqrt{1615}S_3}{512} + \frac{5\sqrt{13566}S_5}{1024} - \frac{7\sqrt{1330}S_7}{1024} + \frac{9\sqrt{42}S_9}{1024}$
138	T_g	Tg	4	2	$\mathbb{G}_{11,2}^{(h,T_g,4)}$	${\tt Gh}({\tt 11},{\tt Tg},{\tt 4},{\tt 2})$	C_{10}
139	T_g	Tg	5	0	$\mathbb{G}_{11,0}^{(h,T_g,5)}$	${\tt Gh(11,Tg,5,0)}$	$-\frac{15\sqrt{221}C_1}{512}-\frac{3\sqrt{2926}C_{11}}{1024}-\frac{\sqrt{595}C_3}{512}+\frac{53\sqrt{102}C_5}{1024}-\frac{105\sqrt{10}C_7}{1024}-\frac{61\sqrt{114}C_9}{1024}$
140	T_g	Tg	5	1	$\mathbb{G}_{11,1}^{(h,T_g,5)}$	${\tt Gh(11,Tg,5,1)}$	$\frac{15\sqrt{221}S_1}{512} - \frac{3\sqrt{2926}S_{11}}{1024} - \frac{\sqrt{595}S_3}{512} - \frac{53\sqrt{102}S_5}{1024} - \frac{105\sqrt{10}S_7}{1024} + \frac{61\sqrt{114}S_9}{1024}$
141	T_g	Tg	5	2	$\mathbb{G}_{11,2}^{(h,T_g,5)}$	${\tt Gh(11,Tg,5,2)}$	C_6
142	T_g	Tg	6	0	$\mathbb{G}_{11,0}^{(h,T_g,6)}$	${\tt Gh(11,Tg,6,0)}$	$-\frac{21\sqrt{130}C_1}{512} - \frac{\sqrt{124355}C_{11}}{512} + \frac{57\sqrt{14}C_3}{512} - \frac{41\sqrt{15}C_5}{512} + \frac{17\sqrt{17}C_7}{512} + \frac{\sqrt{4845}C_9}{512}$
143	T_g	Tg	6	1	$\mathbb{G}_{11,1}^{(h,T_g,6)}$	$\mathtt{Gh}(\mathtt{11},\mathtt{Tg},6,\mathtt{1})$	$\frac{21\sqrt{130}S_1}{512} - \frac{\sqrt{124355}S_{11}}{512} + \frac{57\sqrt{14}S_3}{512} + \frac{41\sqrt{15}S_5}{512} + \frac{17\sqrt{17}S_7}{512} - \frac{\sqrt{4845}S_9}{512}$
144	T_g	Tg	6	2	$\mathbb{G}_{11,2}^{(h,T_g,6)}$	${\tt Gh(11,Tg,6,2)}$	C_2