

\* symmetry operation

Table 1: Symmetry operations for 3d polar vector.

| No. | tag  | matrix (polar)   | det | TR |
|-----|--|--|-----|----|
| 1   | {1 0}  | $\begin{bmatrix} 1 & 0 & 0 & 0 \\ 0 & 1 & 0 & 0 \\ 0 & 0 & 1 & 0 \end{bmatrix}$                                | 1   | 1  |
| 2   | {4 <sup>+</sup> <sub>001</sub>   <sub>2</sub> <sup>1</sup> <sub>2</sub> <sup>1</sup> <sub>2</sub> }  | $\begin{bmatrix} 0 & -1 & 0 & \frac{1}{2} \\ 1 & 0 & 0 & 0 \\ 0 & 0 & 1 & \frac{1}{2} \end{bmatrix}$           | 1   | 1  |
| 3   | {4 <sup>-</sup> <sub>001</sub>   <sub>0</sub> <sup>1</sup> <sub>2</sub> <sup>1</sup> <sub>2</sub> }  | $\begin{bmatrix} 0 & 1 & 0 & 0 \\ -1 & 0 & 0 & \frac{1}{2} \\ 0 & 0 & 1 & \frac{1}{2} \end{bmatrix}$           | 1   | 1  |
| 4   | {2 <sub>100</sub>   <sub>2</sub> <sup>1</sup> 00}  | $\begin{bmatrix} 1 & 0 & 0 & \frac{1}{2} \\ 0 & -1 & 0 & 0 \\ 0 & 0 & -1 & 0 \end{bmatrix}$                    | 1   | 1  |
| 5   | {2 <sub>010</sub>  0 <sub>2</sub> <sup>1</sup> 0}  | $\begin{bmatrix} -1 & 0 & 0 & 0 \\ 0 & 1 & 0 & \frac{1}{2} \\ 0 & 0 & -1 & 0 \end{bmatrix}$                    | 1   | 1  |
| 6   | {2 <sub>001</sub>   <sub>2</sub> <sup>1</sup> <sub>2</sub> <sup>0</sup> }                            | $\begin{bmatrix} -1 & 0 & 0 & \frac{1}{2} \\ 0 & -1 & 0 & \frac{1}{2} \\ 0 & 0 & 1 & 0 \end{bmatrix}$          | 1   | 1  |
| 7   | {2 <sub>110</sub>   <sub>2</sub> <sup>1</sup> <sub>2</sub> <sup>1</sup> <sub>2</sub> }               | $\begin{bmatrix} 0 & 1 & 0 & \frac{1}{2} \\ 1 & 0 & 0 & \frac{1}{2} \\ 0 & 0 & -1 & \frac{1}{2} \end{bmatrix}$ | 1   | 1  |
| 8   | {2 <sub>1-10</sub>  00 <sub>2</sub> <sup>1</sup> }   | $\begin{bmatrix} 0 & -1 & 0 & 0 \\ -1 & 0 & 0 & 0 \\ 0 & 0 & -1 & \frac{1}{2} \end{bmatrix}$                   | 1   | 1  |
| 9   | {-1 0}   | $\begin{bmatrix} -1 & 0 & 0 & 0 \\ 0 & -1 & 0 & 0 \\ 0 & 0 & -1 & 0 \end{bmatrix}$                             | -1  | 1  |
| 10  | {-4 <sup>+</sup> <sub>001</sub>   <sub>2</sub> <sup>1</sup> <sub>2</sub> <sup>1</sup> <sub>2</sub> } | $\begin{bmatrix} 0 & 1 & 0 & \frac{1}{2} \\ -1 & 0 & 0 & 0 \\ 0 & 0 & -1 & \frac{1}{2} \end{bmatrix}$          | -1  | 1  |
| 11  | {-4 <sup>-</sup> <sub>001</sub>  0 <sub>2</sub> <sup>1</sup> <sub>2</sub> }                          | $\begin{bmatrix} 0 & -1 & 0 & 0 \\ 1 & 0 & 0 & \frac{1}{2} \\ 0 & 0 & -1 & \frac{1}{2} \end{bmatrix}$          | -1  | 1  |
| 12  | {m <sub>100</sub>   <sub>2</sub> <sup>1</sup> 00}  | $\begin{bmatrix} -1 & 0 & 0 & \frac{1}{2} \\ 0 & 1 & 0 & 0 \\ 0 & 0 & 1 & 0 \end{bmatrix}$                     | -1  | 1  |
| 13  | {m <sub>010</sub>  0 <sub>2</sub> <sup>1</sup> 0}  | $\begin{bmatrix} 1 & 0 & 0 & 0 \\ 0 & -1 & 0 & \frac{1}{2} \\ 0 & 0 & 1 & 0 \end{bmatrix}$                     | -1  | 1  |

continued ...

Table 1

| No. | tag   | matrix (polar)  | det | TR |
|-----|---|---|-----|----|
| 14  | $\{m_{001} \frac{1}{2}\frac{1}{2}0\}$           | $\begin{bmatrix} 1 & 0 & 0 & \frac{1}{2} \\ 0 & 1 & 0 & \frac{1}{2} \\ 0 & 0 & -1 & 0 \end{bmatrix}$            | -1  | 1  |
| 15  | $\{m_{110} \frac{1}{2}\frac{1}{2}\frac{1}{2}\}$ | $\begin{bmatrix} 0 & -1 & 0 & \frac{1}{2} \\ -1 & 0 & 0 & \frac{1}{2} \\ 0 & 0 & 1 & \frac{1}{2} \end{bmatrix}$ | -1  | 1  |
| 16  | $\{m_{1-10} 00\frac{1}{2}\}$                    | $\begin{bmatrix} 0 & 1 & 0 & 0 \\ 1 & 0 & 0 & 0 \\ 0 & 0 & 1 & \frac{1}{2} \end{bmatrix}$                       | -1  | 1  |