SAMB for "01"

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- Group: No. 207 O^1 P432 [cubic]
- Associated point group: No. 30 O 432 [cubic]
- Generation condition

 - time-reversal type: electric
 - irrep: [A1]
 - spinful
- Unit cell:

$$a=1.0,\ b=1.0,\ c=1.0,\ \alpha=90.0,\ \beta=90.0,\ \gamma=90.0$$

• Lattice vectors:

$$\boldsymbol{a}_1 = \begin{pmatrix} 1.0 & 0 & 0 \end{pmatrix}$$

$$\boldsymbol{a}_2 = \begin{pmatrix} 0 & 1.0 & 0 \end{pmatrix}$$

$$\mathbf{a}_3 = \begin{pmatrix} 0 & 0 & 1.0 \end{pmatrix}$$

Table 1: High-symmetry line: Γ -X.

symbol	position	n	symbol	pc	sitio	on
Γ	$\begin{pmatrix} 0 & 0 \end{pmatrix}$	0)	X	$\left(\frac{1}{2}\right)$	0	0)

• Kets: dimension = 8

Table 2: Hilbert space for full matrix.

No.	ket	No.	ket	No.	ket	No.	ket	No.	ket
 1	(s,\uparrow) @A ₁	2	(s,\downarrow) @A ₁	3	(p_x,\uparrow) @A ₁	4	(p_x,\downarrow) @A ₁	5	(p_y,\uparrow) @A ₁
6	(p_y,\downarrow) @A ₁	7	(p_z,\uparrow) @A ₁	8	(p_z,\downarrow) @A ₁				

• Sites in (primitive) unit cell:

Table 3: Site-clusters.

	site	position	mapping
S_1	A_1	$\begin{pmatrix} 0 & 0 & 0 \end{pmatrix}$	[1,2,3,4,5,6,7,8,9,10,11,12,13,14,15,16,17,18,19,20,21,22,23,24]

• Bonds in (primitive) unit cell:

Table 4: Bond-clusters.

				_	_	
	bond	tail	head	n	#	$oldsymbol{b@c}$ mapping
B_1	b_1	A_1	A_1	1	1	
	b_2	A_1	A_1	1	1	$ \left \begin{array}{ccc} \left(1 & 0 & 0\right) @ \left(\frac{1}{2} & 0 & 0\right) & \left \begin{array}{ccc} [6, -9, 11, -12, 13, -14, 21, -24] \end{array} \right $
	b_3	A_1	A_1	1	1	$ \left \begin{array}{ccc} \left(0 & 1 & 0\right) @ \left(0 & \frac{1}{2} & 0\right) & \left \begin{array}{ccc} [7,-10,15,16,-17,-18,-20,23] \end{array} \right. $
B_2	b_4	A_1	A_1	2	1	$(0 1 1) @ (0 \frac{1}{2} \frac{1}{2}) $ [1,-3,7,-10]
	b_5	A_1	A_1	2	1	$\begin{pmatrix} 0 & 1 & -1 \end{pmatrix} @ \begin{pmatrix} 0 & \frac{1}{2} & \frac{1}{2} \end{pmatrix} [-2,4,-20,23]$
	b_6	A_1	A_1	2	1	$\left(\begin{array}{ccc} 1 & 0 & -1 \end{array} \right) @ \left(\begin{array}{ccc} \frac{1}{2} & 0 & \frac{1}{2} \end{array} \right) \ \left[\begin{array}{ccc} [5,-12,13,-19] \end{array} \right]$
	b_7	A_1	A_1	2	1	$\left(\begin{array}{cccccccccccccccccccccccccccccccccccc$
	b_8	A_1	A_1	2	1	$(1 0 1) @ (\frac{1}{2} 0 \frac{1}{2})$ [-8,11,-14,22]
	b_9	A_1	A_1	2	1	$\left[\begin{array}{cccc} \left(1 & 1 & 0 \right) @ \left(\frac{1}{2} & \frac{1}{2} & 0 \right) & \left[-9,15,-17,21 \right] \end{array} \right]$

• SAMB:

No. 1
$$\hat{\mathbb{Q}}_0^{(A_1)}$$
 [M₁, S₁]

$$\hat{\mathbb{Z}}_1 = \mathbb{X}_1[\mathbb{Q}_0^{(a,A_1)}] \otimes \mathbb{Y}_1[\mathbb{Q}_0^{(s,A_1)}]$$

$$\hat{\mathbb{Z}}_1(\boldsymbol{k}) = \mathbb{X}_1[\mathbb{Q}_0^{(a,A_1)}] \otimes \mathbb{U}_1[\mathbb{Q}_0^{(s,A_1)}]$$

No. 2
$$\hat{\mathbb{G}}_0^{(A_1)}(1,1)$$
 [M₂,S₁]

$$\hat{\mathbb{Z}}_2 = \mathbb{X}_5[\mathbb{G}_0^{(a,A_1)}(1,1)] \otimes \mathbb{Y}_1[\mathbb{Q}_0^{(s,A_1)}]$$

$$\hat{\mathbb{Z}}_2(\boldsymbol{k}) = \mathbb{X}_5[\mathbb{G}_0^{(a,A_1)}(1,1)] \otimes \mathbb{U}_1[\mathbb{Q}_0^{(s,A_1)}]$$

No. 3
$$\hat{\mathbb{Q}}_0^{(A_1)}$$
 [M₃, S₁]

$$\hat{\mathbb{Z}}_3 = \mathbb{X}_{11}[\mathbb{Q}_0^{(a,A_1)}] \otimes \mathbb{Y}_1[\mathbb{Q}_0^{(s,A_1)}]$$

$$\hat{\mathbb{Z}}_3(\boldsymbol{k}) = \mathbb{X}_{11}[\mathbb{Q}_0^{(a,A_1)}] \otimes \mathbb{U}_1[\mathbb{Q}_0^{(s,A_1)}]$$

No. 4
$$\hat{\mathbb{Q}}_0^{(A_1)}(1,1)$$
 [M₃, S₁]

$$\hat{\mathbb{Z}}_4 = \mathbb{X}_{12}[\mathbb{Q}_0^{(a,A_1)}(1,1)] \otimes \mathbb{Y}_1[\mathbb{Q}_0^{(s,A_1)}]$$

$$\hat{\mathbb{Z}}_4(\mathbf{k}) = \mathbb{X}_{12}[\mathbb{Q}_0^{(a,A_1)}(1,1)] \otimes \mathbb{U}_1[\mathbb{Q}_0^{(s,A_1)}]$$

No. 5
$$\hat{\mathbb{Q}}_0^{(A_1)}$$
 [M₁, B₁]

$$\hat{\mathbb{Z}}_5 = \mathbb{X}_1[\mathbb{Q}_0^{(a,A_1)}] \otimes \mathbb{Y}_2[\mathbb{Q}_0^{(b,A_1)}]$$

$$\hat{\mathbb{Z}}_5(\boldsymbol{k}) = \mathbb{X}_1[\mathbb{Q}_0^{(a,A_1)}] \otimes \mathbb{U}_1[\mathbb{Q}_0^{(s,A_1)}] \otimes \mathbb{F}_1[\mathbb{Q}_0^{(k,A_1)}]$$

No. 6
$$\hat{\mathbb{Q}}_4^{(A_1)}(1,-1)$$
 [M₁, B₁]

$$\hat{\mathbb{Z}}_6 = -\frac{\sqrt{3}\mathbb{X}_2[\mathbb{M}_{1,0}^{(a,T_1)}(1,-1)]\otimes\mathbb{Y}_5[\mathbb{T}_{4,0}^{(b,T_1)}]}{3} - \frac{\sqrt{3}\mathbb{X}_3[\mathbb{M}_{1,1}^{(a,T_1)}(1,-1)]\otimes\mathbb{Y}_6[\mathbb{T}_{4,1}^{(b,T_1)}]}{3} - \frac{\sqrt{3}\mathbb{X}_4[\mathbb{M}_{1,2}^{(a,T_1)}(1,-1)]\otimes\mathbb{Y}_7[\mathbb{T}_{4,2}^{(b,T_1)}]}{3} - \frac{\mathbb{X}_7[\mathbb{M}_{1,2}^{(b,T_1)}(1,-1)]\otimes\mathbb{Y}_7[\mathbb{T}_{4,2}^{(b,T_1)}]}{3} - \frac{\mathbb{X}_7[\mathbb{M}_{1,2}^{(b,T_1)}(1,-1)]\otimes\mathbb{Y}_7[\mathbb{T}_{4,2}^{(b,T_1)}]}{3} - \frac{\mathbb{X}_7[\mathbb{M}_{1,2}^{(b,T_1)}(1,-1)]\otimes\mathbb{Y}_7[\mathbb{M}_{1,2}^{(b,T_1)}(1,-1)]}{3} - \frac{\mathbb{X}_7[\mathbb{M}_{1,2}^{(b,T_1)}(1,-1)]\otimes\mathbb{X}_7[\mathbb{M}_{1,2}^{(b,T_1)}(1,-1)]}{3} - \frac{\mathbb{X}_7[\mathbb{M}_{1,2}^{(b,T_1)}(1,-1)]\otimes\mathbb{X}_7[\mathbb{M}_{1,2}^{(b,T_1)}(1,-1)]}{3} - \frac{\mathbb{X}_7[\mathbb{M}_{1,2}^{(b,T_1)}(1,-1)]\otimes\mathbb{X}_7$$

$$\hat{\mathbb{Z}}_{6}(\boldsymbol{k}) = -\frac{\sqrt{3}\mathbb{X}_{2}[\mathbb{M}_{1,0}^{(a,T_{1})}(1,-1)] \otimes \mathbb{U}_{1}[\mathbb{Q}_{0}^{(s,A_{1})}] \otimes \mathbb{F}_{4}[\mathbb{T}_{4,0}^{(k,T_{1})}]}{3} - \frac{\sqrt{3}\mathbb{X}_{3}[\mathbb{M}_{1,1}^{(a,T_{1})}(1,-1)] \otimes \mathbb{U}_{1}[\mathbb{Q}_{0}^{(s,A_{1})}] \otimes \mathbb{F}_{5}[\mathbb{T}_{4,1}^{(k,T_{1})}]}{3} - \frac{\sqrt{3}\mathbb{X}_{4}[\mathbb{M}_{1,2}^{(a,T_{1})}(1,-1)] \otimes \mathbb{U}_{1}[\mathbb{Q}_{0}^{(s,A_{1})}] \otimes \mathbb{F}_{6}[\mathbb{T}_{4,2}^{(k,T_{1})}]}{3} - \frac{\sqrt{3}\mathbb{X}_{4}[\mathbb{M}_{1,2}^{(a,T_{1})}(1,-1)] \otimes \mathbb{U}_{1}[\mathbb{Q}_{0}^{(s,A_{1})}]}{3} - \frac{\sqrt{3}\mathbb{X}_{4}[\mathbb{M}_{1,2}^{(a,T_{1})}(1,-1)] \otimes \mathbb{U}_{1}[\mathbb{Q}_{0}^{(s,A_{1})}]}{3} - \frac{\sqrt{3}\mathbb{X}_{4}[\mathbb{M}_{1,2}^{(a,T_{1})}(1,-1)] \otimes \mathbb{U}_{1}[\mathbb{Q}_{0}^{(s,A_{1})}]}{3} - \frac{\mathbb{W}_{1,2}[\mathbb{Q}_{0}^{(s,A_{1})}]}{3} - \frac{\mathbb{W}_{1,2}[\mathbb{Q}_{0}^{(s,A_{1})}]}{$$

No. 7
$$\hat{\mathbb{G}}_0^{(A_1)}(1,1)$$
 [M₂, B₁]

$$\hat{\mathbb{Z}}_7 = \mathbb{X}_5[\mathbb{G}_0^{(a,A_1)}(1,1)] \otimes \mathbb{Y}_2[\mathbb{Q}_0^{(b,A_1)}]$$

$$\hat{\mathbb{Z}}_{7}(\mathbf{k}) = \mathbb{X}_{5}[\mathbb{Q}_{0}^{(a,A_{1})}(1,1)] \otimes \mathbb{U}_{1}[\mathbb{Q}_{0}^{(s,A_{1})}] \otimes \mathbb{F}_{1}[\mathbb{Q}_{0}^{(k,A_{1})}]$$

No. 8
$$\hat{\mathbb{G}}_0^{(A_1)}(1,-1)$$
 [M₂, B₁]

$$\hat{\mathbb{Z}}_8 = \frac{\sqrt{2}\mathbb{X}_6[\mathbb{G}_{2,0}^{(a,E)}(1,-1)] \otimes \mathbb{Y}_3[\mathbb{Q}_{2,0}^{(b,E)}]}{2} + \frac{\sqrt{2}\mathbb{X}_7[\mathbb{G}_{2,1}^{(a,E)}(1,-1)] \otimes \mathbb{Y}_4[\mathbb{Q}_{2,1}^{(b,E)}]}{2}$$

$$\hat{\mathbb{Z}}_8(\textbf{\textit{k}}) = \frac{\sqrt{2}\mathbb{X}_6[\mathbb{G}_{2,0}^{(a,E)}(1,-1)] \otimes \mathbb{U}_1[\mathbb{Q}_0^{(s,A_1)}] \otimes \mathbb{F}_2[\mathbb{Q}_{2,0}^{(k,E)}]}{2} + \frac{\sqrt{2}\mathbb{X}_7[\mathbb{G}_{2,1}^{(a,E)}(1,-1)] \otimes \mathbb{U}_1[\mathbb{Q}_0^{(s,A_1)}] \otimes \mathbb{F}_3[\mathbb{Q}_{2,1}^{(k,E)}]}{2}$$

No. 9
$$\hat{\mathbb{Q}}_0^{(A_1)}$$
 [M₃, B₁]

$$\hat{\mathbb{Z}}_9 = \mathbb{X}_{11}[\mathbb{Q}_0^{(a,A_1)}] \otimes \mathbb{Y}_2[\mathbb{Q}_0^{(b,A_1)}]$$

$$\hat{\mathbb{Z}}_9(\mathbf{k}) = \mathbb{X}_{11}[\mathbb{Q}_0^{(a,A_1)}] \otimes \mathbb{U}_1[\mathbb{Q}_0^{(s,A_1)}] \otimes \mathbb{F}_1[\mathbb{Q}_0^{(k,A_1)}]$$

No. 10
$$\hat{\mathbb{Q}}_0^{(A_1)}(1,1)$$
 [M₃, B₁]

$$\hat{\mathbb{Z}}_{10} = \mathbb{X}_{12}[\mathbb{Q}_0^{(a,A_1)}(1,1)] \otimes \mathbb{Y}_2[\mathbb{Q}_0^{(b,A_1)}]$$

$$\hat{\mathbb{Z}}_{10}(\pmb{k}) = \mathbb{X}_{12}[\mathbb{Q}_0^{(a,A_1)}(1,1)] \otimes \mathbb{U}_1[\mathbb{Q}_0^{(s,A_1)}] \otimes \mathbb{F}_1[\mathbb{Q}_0^{(k,A_1)}]$$

No. 11
$$\hat{\mathbb{Q}}_0^{(A_1)}$$
 [M₃, B₁]

$$\hat{\mathbb{Z}}_{11} = \frac{\sqrt{2}\mathbb{X}_{13}[\mathbb{Q}_{2,0}^{(a,E)}] \otimes \mathbb{Y}_{3}[\mathbb{Q}_{2,0}^{(b,E)}]}{2} + \frac{\sqrt{2}\mathbb{X}_{14}[\mathbb{Q}_{2,1}^{(a,E)}] \otimes \mathbb{Y}_{4}[\mathbb{Q}_{2,1}^{(b,E)}]}{2}$$

$$\hat{\mathbb{Z}}_{11}(\textbf{\textit{k}}) = \frac{\sqrt{2}\mathbb{X}_{13}[\mathbb{Q}_{2,0}^{(a,E)}] \otimes \mathbb{U}_{1}[\mathbb{Q}_{0}^{(s,A_{1})}] \otimes \mathbb{F}_{2}[\mathbb{Q}_{2,0}^{(k,E)}]}{2} + \frac{\sqrt{2}\mathbb{X}_{14}[\mathbb{Q}_{2,1}^{(a,E)}] \otimes \mathbb{U}_{1}[\mathbb{Q}_{0}^{(s,A_{1})}] \otimes \mathbb{F}_{3}[\mathbb{Q}_{2,1}^{(k,E)}]}{2}$$

No. 12
$$\hat{\mathbb{Q}}_0^{(A_1)}(1,-1)$$
 [M₃, B₁]

$$\hat{\mathbb{Z}}_{12} = \frac{\sqrt{2}\mathbb{X}_{18}[\mathbb{Q}_{2,0}^{(a,E)}(1,-1)] \otimes \mathbb{Y}_{3}[\mathbb{Q}_{2,0}^{(b,E)}]}{2} + \frac{\sqrt{2}\mathbb{X}_{19}[\mathbb{Q}_{2,1}^{(a,E)}(1,-1)] \otimes \mathbb{Y}_{4}[\mathbb{Q}_{2,1}^{(b,E)}]}{2}$$

$$\hat{\mathbb{Z}}_{12}(\textbf{\textit{k}}) = \frac{\sqrt{2}\mathbb{X}_{18}[\mathbb{Q}_{2,0}^{(a,E)}(1,-1)] \otimes \mathbb{U}_{1}[\mathbb{Q}_{0}^{(s,A_{1})}] \otimes \mathbb{F}_{2}[\mathbb{Q}_{2,0}^{(k,E)}]}{2} + \frac{\sqrt{2}\mathbb{X}_{19}[\mathbb{Q}_{2,1}^{(a,E)}(1,-1)] \otimes \mathbb{U}_{1}[\mathbb{Q}_{0}^{(s,A_{1})}] \otimes \mathbb{F}_{3}[\mathbb{Q}_{2,1}^{(k,E)}]}{2} + \frac{\sqrt{2}\mathbb{X}_{19}[\mathbb{Q}_{2,1}^{(a,E)}(1,-1)] \otimes \mathbb{U}_{1}[\mathbb{Q}_{0}^{(s,A_{1})}]}{2} \otimes \mathbb{F}_{3}[\mathbb{Q}_{2,1}^{(k,E)}]}$$

No. 13 $\hat{\mathbb{Q}}_4^{(A_1)}$ [M₃, B₁]

$$\hat{\mathbb{Z}}_{13} = -\frac{\sqrt{3}\mathbb{X}_{23}[\mathbb{M}_{1,0}^{(a,T_1)}] \otimes \mathbb{Y}_{5}[\mathbb{T}_{4,0}^{(b,T_1)}]}{3} - \frac{\sqrt{3}\mathbb{X}_{24}[\mathbb{M}_{1,1}^{(a,T_1)}] \otimes \mathbb{Y}_{6}[\mathbb{T}_{4,1}^{(b,T_1)}]}{3} - \frac{\sqrt{3}\mathbb{X}_{25}[\mathbb{M}_{1,2}^{(a,T_1)}] \otimes \mathbb{Y}_{7}[\mathbb{T}_{4,2}^{(b,T_1)}]}{3}$$

$$\hat{\mathbb{Z}}_{13}(\boldsymbol{k}) = -\frac{\sqrt{3}\mathbb{X}_{23}[\mathbb{M}_{1,0}^{(a,T_1)}] \otimes \mathbb{U}_1[\mathbb{Q}_0^{(s,A_1)}] \otimes \mathbb{F}_4[\mathbb{T}_{4,0}^{(k,T_1)}]}{3} - \frac{\sqrt{3}\mathbb{X}_{24}[\mathbb{M}_{1,1}^{(a,T_1)}] \otimes \mathbb{U}_1[\mathbb{Q}_0^{(s,A_1)}] \otimes \mathbb{F}_5[\mathbb{T}_{4,1}^{(k,T_1)}]}{3} - \frac{\sqrt{3}\mathbb{X}_{25}[\mathbb{M}_{1,2}^{(a,T_1)}] \otimes \mathbb{U}_1[\mathbb{Q}_0^{(s,A_1)}] \otimes \mathbb{F}_6[\mathbb{T}_{4,2}^{(k,T_1)}]}{3} - \frac{\sqrt{3}\mathbb{X}_{25}[\mathbb{M}_{1,2}^{(a,T_1)}] \otimes \mathbb{U}_1[\mathbb{Q}_0^{(s,A_1)}]}{3} - \frac{\sqrt{3}\mathbb{X}_{25}[\mathbb{M}_{1,2}^{(a,T_1)}]}{3} - \frac{\mathbb{X}_{25}[\mathbb{M}_{1,2}^{(a,T_1)}] \otimes \mathbb{U}_1[\mathbb{Q}_0^{(s,A_1)}]}{3} - \frac{\mathbb{X}_{25}[\mathbb{M}_{1,2}^{(a,T_1)}] \otimes \mathbb{U}_1[\mathbb{Q}_0^{(s,A_1)}]}{3} - \frac{\mathbb{X}_{25}[\mathbb{M}_{1,2}^{(a,T_1)}] \otimes \mathbb{X}_{25}[\mathbb{M}_{1,2}^{(a,T_1)}]}{3} - \frac{\mathbb{X}_{25}[\mathbb{M}_{1,2}^{(a,T_1)}]}{3} -$$

No. 14 $\hat{\mathbb{Q}}_{4}^{(A_1)}(1,1)$ [M₃, B₁]

$$\hat{\mathbb{Z}}_{14} = -\frac{\sqrt{3}\mathbb{X}_{26}[\mathbb{M}_{1,0}^{(a,T_1)}(1,1)]\otimes\mathbb{Y}_{5}[\mathbb{T}_{4,0}^{(b,T_1)}]}{3} - \frac{\sqrt{3}\mathbb{X}_{27}[\mathbb{M}_{1,1}^{(a,T_1)}(1,1)]\otimes\mathbb{Y}_{6}[\mathbb{T}_{4,1}^{(b,T_1)}]}{3} - \frac{\sqrt{3}\mathbb{X}_{28}[\mathbb{M}_{1,2}^{(a,T_1)}(1,1)]\otimes\mathbb{Y}_{7}[\mathbb{T}_{4,2}^{(b,T_1)}]}{3} - \frac{\mathbb{X}_{1,2}[\mathbb{M}_{1,2}^{(a,T_1)}(1,1)]\otimes\mathbb{Y}_{1,2}[\mathbb{M}_{1,2}^{(b,T_1)}]}{3} - \frac{\mathbb{X}_{1,2}[\mathbb{M}_{1,2}^{(b,T_1)}(1,1)]\otimes\mathbb{Y}_{1,2}[\mathbb{M}_{1,2}^{(b,T_1)}(1,1)]}{3} - \frac{\mathbb{X}_{1,2}[\mathbb{M}_{1,2}^{(b,T_1)}(1,1)]\otimes\mathbb{Y}_{1,2}[\mathbb{M}_{1,2}^{(b,T_1)}(1,1)]$$

$$\hat{\mathbb{Z}}_{14}(\boldsymbol{k}) = -\frac{\sqrt{3}\mathbb{X}_{26}[\mathbb{M}_{1,0}^{(a,T_1)}(1,1)] \otimes \mathbb{U}_1[\mathbb{Q}_0^{(s,A_1)}] \otimes \mathbb{F}_4[\mathbb{T}_{4,0}^{(k,T_1)}]}{3} - \frac{\sqrt{3}\mathbb{X}_{27}[\mathbb{M}_{1,1}^{(a,T_1)}(1,1)] \otimes \mathbb{U}_1[\mathbb{Q}_0^{(s,A_1)}] \otimes \mathbb{F}_5[\mathbb{T}_{4,1}^{(k,T_1)}]}{3} - \frac{\sqrt{3}\mathbb{X}_{28}[\mathbb{M}_{1,2}^{(a,T_1)}(1,1)] \otimes \mathbb{U}_1[\mathbb{Q}_0^{(s,A_1)}] \otimes \mathbb{F}_6[\mathbb{T}_{4,2}^{(k,T_1)}]}{3} - \frac{\sqrt{3}\mathbb{X}_{28}[\mathbb{M}_{1,2}^{(a,T_1)}(1,1)] \otimes \mathbb{U}_1[\mathbb{Q}_0^{(s,A_1)}]}{3} - \frac{\sqrt{3}\mathbb{X}_{28}[\mathbb{M}_1^{(a,T_1)}(1,1)] \otimes \mathbb{U}_1[\mathbb{Q}_0^{(s,A_1)}]}{3} - \frac{\sqrt{3}\mathbb{X}_{28}[\mathbb{Q}_0^{(s,A_1)}(1,1)] \otimes \mathbb{U}_1[\mathbb{Q}_0^{(s,A_1)}]}{3} - \frac{\sqrt{3}\mathbb{X}_{28}[\mathbb{Q}_0^{(s,A_1)}(1,1$$

No. 15 $\hat{\mathbb{Q}}_4^{(A_1)}(1,-1)$ [M₃, B₁]

$$\hat{\mathbb{Z}}_{15} = -\frac{\sqrt{3}\mathbb{X}_{29}[\mathbb{M}_{1,0}^{(a,T_1)}(1,-1)]\otimes\mathbb{Y}_{5}[\mathbb{T}_{4,0}^{(b,T_1)}]}{3} - \frac{\sqrt{3}\mathbb{X}_{30}[\mathbb{M}_{1,1}^{(a,T_1)}(1,-1)]\otimes\mathbb{Y}_{6}[\mathbb{T}_{4,1}^{(b,T_1)}]}{3} - \frac{\sqrt{3}\mathbb{X}_{31}[\mathbb{M}_{1,2}^{(a,T_1)}(1,-1)]\otimes\mathbb{Y}_{7}[\mathbb{T}_{4,2}^{(b,T_1)}]}{3} - \frac{\sqrt{3}\mathbb{X}_{40}[\mathbb{T}_{4,2}^{(a,T_1)}(1,-1)]\otimes\mathbb{Y}_{10}[\mathbb{T}_{4,2}^{(b,T_1)}]}{3} - \frac{\sqrt{3}\mathbb{X}_{40}[\mathbb{T}_{4,2}^{(a,T_1)}(1,-1)]\otimes\mathbb{Y}_{10}[\mathbb{T}_{4,2}^{(b,T_1)}]}{3} - \frac{\sqrt{3}\mathbb{X}_{40}[\mathbb{T}_{4,2}^{(a,T_1)}(1,-1)]\otimes\mathbb{Y}_{10}[\mathbb{T}_{4,2}^{(b,T_1)}]}{3} - \frac{\sqrt{3}\mathbb{X}_{40}[\mathbb{T}_{4,2}^{(a,T_1)}(1,-1)]\otimes\mathbb{Y}_{10}[\mathbb{T}_{4,2}^{(b,T_1)}]}{3} - \frac{\sqrt{3}\mathbb{X}_{40}[\mathbb{T}_{4,2}^{(a,T_1)}(1,-1)]\otimes\mathbb{Y}_{10}[\mathbb{T}_{4,2}^{(b,T_1)}]}{3} - \frac{\mathbb{T}_{40}[\mathbb{T}_{4,2}^{(b,T_1)}]}{3} - \frac{\mathbb{T}_{40}[\mathbb{T}_{40,2}^{(b,T_1)}]}{3} - \frac{\mathbb{T}_{40}[\mathbb{T}_{40,2}^{(b,T_1)}]}{3}$$

$$\hat{\mathbb{Z}}_{15}(\textbf{\textit{k}}) = -\frac{\sqrt{3}\mathbb{X}_{29}[\mathbb{M}_{1,0}^{(a,T_1)}(1,-1)] \otimes \mathbb{U}_{1}[\mathbb{Q}_{0}^{(s,A_1)}] \otimes \mathbb{F}_{4}[\mathbb{T}_{4,0}^{(k,T_1)}]}{3} - \frac{\sqrt{3}\mathbb{X}_{30}[\mathbb{M}_{1,1}^{(a,T_1)}(1,-1)] \otimes \mathbb{U}_{1}[\mathbb{Q}_{0}^{(s,A_1)}] \otimes \mathbb{F}_{5}[\mathbb{T}_{4,1}^{(k,T_1)}]}{3} - \frac{\sqrt{3}\mathbb{X}_{31}[\mathbb{M}_{1,2}^{(a,T_1)}(1,-1)] \otimes \mathbb{U}_{1}[\mathbb{Q}_{0}^{(s,A_1)}] \otimes \mathbb{F}_{6}[\mathbb{T}_{4,2}^{(k,T_1)}]}{3} - \frac{\sqrt{3}\mathbb{X}_{10}[\mathbb{M}_{1,2}^{(a,T_1)}(1,-1)] \otimes \mathbb{U}_{1}[\mathbb{Q}_{0}^{(s,A_1)}] \otimes \mathbb{F}_{6}[\mathbb{T}_{4,2}^{(k,T_1)}]}{3} - \frac{\sqrt{3}\mathbb{X}_{10}[\mathbb{M}_{1,2}^{(k,T_1)}(1,-1)] \otimes \mathbb{U}_{1}[\mathbb{Q}_{0}^{(s,A_1)}]}{3} - \frac{\sqrt{3}\mathbb{X}_{10}[\mathbb{M}_{1,2}^{(k,T_1)}]}{3} - \frac{\sqrt{3}\mathbb{X}_{10}[\mathbb{M}_{1,2}^{(k,T_1)}(1,-1)] \otimes \mathbb{U}_{1}[\mathbb{Q}_{0}^{(s,A_1)}]}{3} - \frac{\sqrt{3}\mathbb{X}_{10}[\mathbb{M}_{1,2}^{(k,T_1)}]}{3} - \frac{\sqrt{3$$

No. 16 $\hat{\mathbb{Q}}_{4}^{(A_1)}(1,-1)$ [M₃, B₁]

$$\hat{\mathbb{Z}}_{16} = \frac{\sqrt{3}\mathbb{X}_{32}[\mathbb{M}_{3,0}^{(a,T_1)}(1,-1)]\otimes\mathbb{Y}_{5}[\mathbb{T}_{4,0}^{(b,T_1)}]}{3} + \frac{\sqrt{3}\mathbb{X}_{33}[\mathbb{M}_{3,1}^{(a,T_1)}(1,-1)]\otimes\mathbb{Y}_{6}[\mathbb{T}_{4,1}^{(b,T_1)}]}{3} + \frac{\sqrt{3}\mathbb{X}_{34}[\mathbb{M}_{3,2}^{(a,T_1)}(1,-1)]\otimes\mathbb{Y}_{7}[\mathbb{T}_{4,2}^{(b,T_1)}]}{3} + \frac{\sqrt{3}\mathbb{X}_{44}[\mathbb{M}_{3,2}^{(a,T_1)}(1,-1)]\otimes\mathbb{Y}_{7}[\mathbb{T}_{4,2}^{(b,T_1)}]}{3} + \frac{\sqrt{3}\mathbb{X}_{44}[\mathbb{M}_{3,2}^{(a,T_1)}(1,-1)]\otimes\mathbb{Y}_{7}[\mathbb{M}_{4,2}^{(b,T_1)}]}{3} + \frac{\sqrt{3}\mathbb{X}_{44}[\mathbb{M}_{3,2}^{(a,T_1)}(1,-1)]\otimes\mathbb{Y}_{7}[\mathbb{M}_{4,2}^{(b,T_1)}]}{3} + \frac{\sqrt{3}\mathbb{X}_{44}[\mathbb{M}_{3,2}^{(a,T_1)}(1,-1)]\otimes\mathbb{Y}_{7}[\mathbb{M}_{4,2}^{(b,T_1)}]}{3} + \frac{\sqrt{3}\mathbb{X}_{44}[\mathbb{M}_{4,2}^{(a,T_1)}(1,-1)]\otimes\mathbb{Y}_{7}[\mathbb{M}_{4,2}^{(b,T_1)}]}{3} + \frac{\sqrt{3}\mathbb{X}_{44}[\mathbb{M}_{4,2}^{(b,T_1)}(1,-1)]\otimes\mathbb{Y}_{7}[\mathbb{M}_{4,2}^{(b,T_1)}]}{3} + \frac{\sqrt{3}\mathbb{X}_{44}[\mathbb{M}_{4,2}^{(b,T_1)}(1,-1)]\otimes\mathbb{Y}_{7}[\mathbb{M}_{4,2}^{(b,T_1)}(1,-1)]}{3} + \frac{\sqrt{3}\mathbb{X}_{44}[\mathbb{M}_{44,2}^{(b,T_1)}(1,-1)]\otimes\mathbb{Y}_{7}[\mathbb{M}_{44,2}^{(b,T_1)}(1,-1)]}{3} + \frac{\sqrt{3}\mathbb{X}_{44}[\mathbb{M}_{44,2}^{(b,T_1)}(1,-1)]\otimes\mathbb{Y}_{7}[\mathbb{M}_{44,2}^{(b,T_1)}(1,-1)]}{3} + \frac{\sqrt{3}\mathbb{X}_{44}[\mathbb{M}_{44,2}^{(b,T_1)}(1,-1)]\otimes\mathbb{Y}_{7}[\mathbb{M}_{44,2}^{(b,T_1)}(1,-1)]}{3} + \frac{\sqrt{3}\mathbb{X}_{44}[\mathbb{M}_{44,2}^{(b,T_1)}(1,-1)]\otimes\mathbb{Y}_{7}[\mathbb{M}_{44,2}^{(b,T_1)}(1,-1)]}{3} + \frac{\sqrt{3}\mathbb{X}_{44}[\mathbb{M}_{44,2}^{(b,T_1)}(1,-1)]\otimes\mathbb{Y}_{7}[\mathbb{M}_{44,2}^{(b,T_1)}(1,-1)]}{3} + \frac{\sqrt{3}\mathbb{X}_{44}[\mathbb{M}_{44,2}^{(b,T_1)}(1$$

$$\hat{\mathbb{Z}}_{16}(\textbf{\textit{k}}) = \frac{\sqrt{3}\mathbb{X}_{32}[\mathbb{M}_{3,0}^{(a,T_1)}(1,-1)] \otimes \mathbb{U}_1[\mathbb{Q}_0^{(s,A_1)}] \otimes \mathbb{F}_4[\mathbb{T}_{4,0}^{(k,T_1)}]}{3} + \frac{\sqrt{3}\mathbb{X}_{33}[\mathbb{M}_{3,1}^{(a,T_1)}(1,-1)] \otimes \mathbb{U}_1[\mathbb{Q}_0^{(s,A_1)}] \otimes \mathbb{F}_5[\mathbb{T}_{4,1}^{(k,T_1)}]}{3} + \frac{\sqrt{3}\mathbb{X}_{34}[\mathbb{M}_{3,2}^{(a,T_1)}(1,-1)] \otimes \mathbb{U}_1[\mathbb{Q}_0^{(s,A_1)}] \otimes \mathbb{F}_6[\mathbb{T}_{4,2}^{(k,T_1)}]}{3} + \frac{\sqrt{3}\mathbb{X}_{34}[\mathbb{M}_{3,2}^{(a,T_1)}(1,-1)] \otimes \mathbb{U}_1[\mathbb{Q}_0^{(s,A_1)}] \otimes \mathbb{F}_6[\mathbb{T}_{4,2}^{(k,T_1)}]}{3} + \frac{\sqrt{3}\mathbb{X}_{34}[\mathbb{M}_{3,2}^{(a,T_1)}(1,-1)] \otimes \mathbb{U}_1[\mathbb{Q}_0^{(s,A_1)}] \otimes \mathbb{F}_6[\mathbb{T}_{4,2}^{(k,T_1)}]}{3} + \frac{\sqrt{3}\mathbb{X}_{34}[\mathbb{M}_{3,2}^{(a,T_1)}(1,-1)] \otimes \mathbb{U}_1[\mathbb{Q}_0^{(s,A_1)}] \otimes \mathbb{F}_6[\mathbb{Q}_0^{(s,A_1)}]}{3} + \frac{\sqrt{3}\mathbb{X}_{34}[\mathbb{M}_{3,2}^{(a,T_1)}(1,-1)] \otimes \mathbb{U}_1[\mathbb{Q}_0^{(s,A_1)}]}{3} + \frac{\sqrt{3}\mathbb{X}_{34}[\mathbb{M}_{3,2}^{(a,T_1)}(1,-1)] \otimes \mathbb{U}_1[\mathbb{Q}_0^{(s,A_1)}]}{3} + \frac{\sqrt{3}\mathbb{X}_{34}[\mathbb{M}_{3,2}^{(a,T_1)}(1,-1)] \otimes \mathbb{U}_1[\mathbb{Q}_0^{(s,A_1)}]}{3} + \frac{\sqrt{3}\mathbb{X}_{34}[\mathbb{M}_{3,2}^{(a,T_1)}(1,-1)] \otimes \mathbb{U}_1[\mathbb{Q}_0^{(s,A_1)}]}{3} + \frac{\sqrt{3}\mathbb{X}_{34}[\mathbb{M}_{3,2}^{(a,T_1)}(1,-1)]}{3} + \frac{\sqrt{3}\mathbb{X}_{34}[\mathbb{M}_{34}[\mathbb{M}_{34}(1,-1)]}{3} + \frac{\sqrt{3}\mathbb{X}_{34}[\mathbb{M$$

No. 17
$$\hat{\mathbb{Q}}_0^{(A_1)}$$
 [M₁, B₂]

$$\hat{\mathbb{Z}}_{17} = \mathbb{X}_1[\mathbb{Q}_0^{(a,A_1)}] \otimes \mathbb{Y}_8[\mathbb{Q}_0^{(b,A_1)}]$$

$$\hat{\mathbb{Z}}_{17}(\boldsymbol{k}) = \mathbb{X}_1[\mathbb{Q}_0^{(a,A_1)}] \otimes \mathbb{U}_1[\mathbb{Q}_0^{(s,A_1)}] \otimes \mathbb{F}_7[\mathbb{Q}_0^{(k,A_1)}]$$

No. 18
$$\hat{\mathbb{G}}_0^{(A_1)}(1,-1)$$
 [M₁, B₂]

$$\hat{\mathbb{Z}}_{18} = \frac{\sqrt{3}\mathbb{X}_2[\mathbb{M}_{1,0}^{(a,T_1)}(1,-1)] \otimes \mathbb{Y}_{14}[\mathbb{T}_{1,0}^{(b,T_1)}]}{3} + \frac{\sqrt{3}\mathbb{X}_3[\mathbb{M}_{1,1}^{(a,T_1)}(1,-1)] \otimes \mathbb{Y}_{15}[\mathbb{T}_{1,1}^{(b,T_1)}]}{3} + \frac{\sqrt{3}\mathbb{X}_4[\mathbb{M}_{1,2}^{(a,T_1)}(1,-1)] \otimes \mathbb{Y}_{16}[\mathbb{T}_{1,2}^{(b,T_1)}]}{3} + \frac{\sqrt{3}\mathbb{X}_4[\mathbb{M}_{1,2}^{(a,T_1)}(1,-1)] \otimes \mathbb{Y}_{18}[\mathbb{T}_{1,2}^{(b,T_1)}]}{3} + \frac{\sqrt{3}\mathbb{X}_4[\mathbb{M}_{1,2}^{(a,T_1)}(1,-1)] \otimes \mathbb{Y}_{18}[\mathbb{T}_{1,2}^{(b,T_1)}]}}{3} + \frac{\sqrt{3}\mathbb{X}_4[\mathbb{M}_{1,2}^{(a,T_1)}(1,-1)] \otimes \mathbb{Y}_{18}[\mathbb{T}_{1,2}^{(b,T_1)}]}{3} + \frac{\sqrt{3}\mathbb{X}_4[\mathbb{M}_{1,2}^{(a,T_1)}(1,-1)] \otimes \mathbb{Y}_{18}[\mathbb{T}_{1,2}^{(b,T_1)}]}{3} + \frac{\sqrt{3}\mathbb{X}_4[\mathbb{M}_{1,2}^{(b,T_1)}(1,-1)] \otimes \mathbb{Y}_{18}[\mathbb{M}_{1,2}^{(b,T_1)}]}}{3} + \frac{\sqrt{3}\mathbb{X}_4[\mathbb{M}_{1,2}^{(b,T_1)}(1,-1)] \otimes \mathbb{Y}_{18}[\mathbb{M}_{1,2}^{(b,T_1)}(1,-1)]}{3} + \frac{\sqrt{3}\mathbb{X}_4[\mathbb{M}_{1,2}^{(b,T_1)}(1,-1)] \otimes \mathbb{Y}_{18}[\mathbb{M}_{1,2}^{(b,T_1)}(1,-1)]}{3} + \frac{\sqrt{3}\mathbb{X}_4[\mathbb{M}_{1,2}^{(b,T_1)}(1,-1)] \otimes \mathbb{Y}_{18}[\mathbb{M}_{1,2}^{(b,T_1)}(1,-1)]}{3} + \frac{\sqrt{3}\mathbb{X}_4[\mathbb{M}_{1,2}^{(b,T_1)}(1,-1)] \otimes \mathbb{Y}_{18}[\mathbb{M}_{1,2}^{$$

$$\hat{\mathbb{Z}}_{18}(\textbf{\textit{k}}) = \frac{\sqrt{3}\mathbb{X}_{2}[\mathbb{M}_{1,0}^{(a,T_{1})}(1,-1)] \otimes \mathbb{U}_{1}[\mathbb{Q}_{0}^{(s,A_{1})}] \otimes \mathbb{F}_{13}[\mathbb{T}_{1,0}^{(k,T_{1})}]}{3} + \frac{\sqrt{3}\mathbb{X}_{3}[\mathbb{M}_{1,1}^{(a,T_{1})}(1,-1)] \otimes \mathbb{U}_{1}[\mathbb{Q}_{0}^{(s,A_{1})}] \otimes \mathbb{F}_{14}[\mathbb{T}_{1,1}^{(k,T_{1})}]}{3} + \frac{\sqrt{3}\mathbb{X}_{4}[\mathbb{M}_{1,2}^{(a,T_{1})}(1,-1)] \otimes \mathbb{U}_{1}[\mathbb{Q}_{0}^{(s,A_{1})}] \otimes \mathbb{F}_{15}[\mathbb{T}_{1,2}^{(k,T_{1})}]}{3} + \frac{\sqrt{3}\mathbb{X}_{10}[\mathbb{M}_{1,2}^{(a,T_{1})}(1,-1)] \otimes \mathbb{U}_{10}[\mathbb{Q}_{0}^{(s,A_{1})}] \otimes \mathbb{F}_{15}[\mathbb{T}_{1,2}^{(k,T_{1})}]}{3} + \frac{\sqrt{3}\mathbb{X}_{10}[\mathbb{M}_{1,2}^{(a,T_{1})}(1,-1)] \otimes \mathbb{U}_{10}[\mathbb{Q}_{0}^{(s,A_{1})}] \otimes \mathbb{F}_{15}[\mathbb{T}_{1,2}^{(k,T_{1})}]}{3} + \frac{\sqrt{3}\mathbb{X}_{10}[\mathbb{Q}_{10}^{(s,A_{1})}] \otimes \mathbb{F}_{10}[\mathbb{Q}_{10}^{(s,A_{1})}] \otimes \mathbb{F}_{10}[\mathbb{Q}_{10}^{(s,A_{1})}]}{3} + \frac{\sqrt{3}\mathbb{X}_{10}[\mathbb{Q}_{10}^{(s,A_{1})}] \otimes \mathbb{F}_{10}[\mathbb{Q}_{10}^{(s,A_{1})}]}{3} + \frac{\sqrt{3}\mathbb{X}_{10}[\mathbb{Q}_{10}^{(s,A_{1})}]}{3} + \frac{\sqrt{3}\mathbb{Z}_{10}[\mathbb{Q}_{10}^{(s,A_{1})}]}{3} + \frac{\sqrt{3}\mathbb{Z}_{10}[$$

No. 19
$$\hat{\mathbb{G}}_0^{(A_1)}(1,1)$$
 [M₂, B₂]

$$\hat{\mathbb{Z}}_{19} = \mathbb{X}_5[\mathbb{Q}_0^{(a,A_1)}(1,1)] \otimes \mathbb{Y}_8[\mathbb{Q}_0^{(b,A_1)}]$$

$$\hat{\mathbb{Z}}_{19}(\mathbf{k}) = \mathbb{X}_{5}[\mathbb{Q}_{0}^{(a,A_{1})}(1,1)] \otimes \mathbb{U}_{1}[\mathbb{Q}_{0}^{(s,A_{1})}] \otimes \mathbb{F}_{7}[\mathbb{Q}_{0}^{(k,A_{1})}]$$

No. 20
$$\hat{\mathbb{G}}_0^{(A_1)}(1,-1)$$
 [M₂, B₂]

$$\hat{\mathbb{Z}}_{20} = \frac{\sqrt{2}\mathbb{X}_{6}[\mathbb{G}_{2,0}^{(a,E)}(1,-1)] \otimes \mathbb{Y}_{9}[\mathbb{Q}_{2,0}^{(b,E)}]}{2} + \frac{\sqrt{2}\mathbb{X}_{7}[\mathbb{G}_{2,1}^{(a,E)}(1,-1)] \otimes \mathbb{Y}_{10}[\mathbb{Q}_{2,1}^{(b,E)}]}{2}$$

$$\hat{\mathbb{Z}}_{20}(\textbf{\textit{k}}) = \frac{\sqrt{2}\mathbb{X}_{6}[\mathbb{G}_{2,0}^{(a,E)}(1,-1)] \otimes \mathbb{U}_{1}[\mathbb{Q}_{0}^{(s,A_{1})}] \otimes \mathbb{F}_{8}[\mathbb{Q}_{2,0}^{(k,E)}]}{2} + \frac{\sqrt{2}\mathbb{X}_{7}[\mathbb{G}_{2,1}^{(a,E)}(1,-1)] \otimes \mathbb{U}_{1}[\mathbb{Q}_{0}^{(s,A_{1})}] \otimes \mathbb{F}_{9}[\mathbb{Q}_{2,1}^{(k,E)}]}{2}$$

No. 21
$$\hat{\mathbb{Q}}_{4}^{(A_1)}(1,-1)$$
 [M₂, B₂]

$$\hat{\mathbb{Z}}_{21} = \frac{\sqrt{3}\mathbb{X}_{10}[\mathbb{G}_{2,2}^{(a,T_2)}(1,-1)] \otimes \mathbb{Y}_{13}[\mathbb{Q}_{3,2}^{(b,T_2)}]}{3} + \frac{\sqrt{3}\mathbb{X}_{8}[\mathbb{G}_{2,0}^{(a,T_2)}(1,-1)] \otimes \mathbb{Y}_{11}[\mathbb{Q}_{3,0}^{(b,T_2)}]}{3} + \frac{\sqrt{3}\mathbb{X}_{9}[\mathbb{G}_{2,1}^{(a,T_2)}(1,-1)] \otimes \mathbb{Y}_{12}[\mathbb{Q}_{3,1}^{(b,T_2)}]}{3} + \frac{\sqrt{3}\mathbb{X}_{9}[\mathbb{G}_{2,1}^{(a,T_2)}(1,-1)] \otimes \mathbb{Y}_{13}[\mathbb{Q}_{3,1}^{(b,T_2)}]}{3} + \frac{\sqrt{3}\mathbb{X}_{9}[\mathbb{Q}_{3,1}^{(a,T_2)}(1,-1)] \otimes \mathbb{Y}_{13}[\mathbb{Q}_{3,1}^{(b,T_2)}]}{3} + \frac{\sqrt{3}\mathbb{X}_{9}[\mathbb{Q}_{3,1}^{(b,T_2)}(1,-1)] \otimes \mathbb{Y}_{13}[\mathbb{Q}_{3,1}^{(b,T_2)}]}{3} + \frac{\sqrt{3}\mathbb{X}_{9}[\mathbb{Q}_{3,1}^{(b,T_2)}(1,-1)] \otimes \mathbb{Y}_{13}[\mathbb{Q}_{3,1}^{(b,T_2)}(1,-1)]}{3} + \frac{\sqrt{3}\mathbb{X}_{9}[\mathbb{Q}_{3,1}^{(b,T_2)}(1,-1)] \otimes \mathbb{Y}_{13}[\mathbb{Q}_{3,1}^{(b,T_2)}(1,-1)]}{3} + \frac{\sqrt{3}\mathbb{X}_{9}[\mathbb{Q}_{3,1}^{(b,T_2)}(1,-1)] \otimes \mathbb{Y}_{13}[\mathbb{Q}_{3,1}^{(b,T_2)}(1,-1)]}{3} + \frac{\sqrt{3}\mathbb{X}_{9}[\mathbb{Q}_{3,1}^{(b,T_2)}(1,-1)]}{3} + \frac{\sqrt{3}\mathbb{X}_{9}[\mathbb{Q}_{3,1}^{(b,T_2)}(1,-1)]}{3$$

$$\hat{\mathbb{Z}}_{21}(\textbf{\textit{k}}) = \frac{\sqrt{3}\mathbb{X}_{10}[\mathbb{G}_{2,2}^{(a,T_2)}(1,-1)] \otimes \mathbb{U}_1[\mathbb{Q}_0^{(s,A_1)}] \otimes \mathbb{F}_{12}[\mathbb{Q}_{3,2}^{(k,T_2)}]}{3} + \frac{\sqrt{3}\mathbb{X}_8[\mathbb{G}_{2,0}^{(a,T_2)}(1,-1)] \otimes \mathbb{U}_1[\mathbb{Q}_0^{(s,A_1)}] \otimes \mathbb{F}_{10}[\mathbb{Q}_{3,0}^{(k,T_2)}]}{3} + \frac{\sqrt{3}\mathbb{X}_9[\mathbb{G}_{2,1}^{(a,T_2)}(1,-1)] \otimes \mathbb{U}_1[\mathbb{Q}_0^{(s,A_1)}] \otimes \mathbb{F}_{11}[\mathbb{Q}_{3,1}^{(k,T_2)}]}{3} + \frac{\sqrt{3}\mathbb{X}_9[\mathbb{G}_{2,1}^{(a,T_2)}(1,-1)] \otimes \mathbb{U}_1[\mathbb{Q}_0^{(s,A_1)}] \otimes \mathbb{F}_{11}[\mathbb{Q}_{3,1}^{(k,T_2)}]}{3} + \frac{\sqrt{3}\mathbb{X}_9[\mathbb{Q}_{3,0}^{(a,T_2)}(1,-1)] \otimes \mathbb{U}_1[\mathbb{Q}_0^{(s,A_1)}] \otimes \mathbb{F}_{11}[\mathbb{Q}_3^{(k,T_2)}]}{3} + \frac{\sqrt{3}\mathbb{X}_9[\mathbb{Q}_3^{(a,T_2)}(1,-1)] \otimes \mathbb{U}_1[\mathbb{Q}_3^{(a,T_2)}]}{3} + \frac{\sqrt{3}\mathbb{X}_9[\mathbb{Q}_3^{(a,T_2)}(1,-1)] \otimes \mathbb{U}_1[\mathbb{Q}_3^{(a,T_2)}(1,-1)]}{3} + \frac{\sqrt{3}\mathbb{X}_9[\mathbb{Q}_3^{(a,T_2)}(1,-1)] \otimes \mathbb{U}_1[\mathbb{Q}_3^{(a,T_2)}(1,-1)]}{3} + \frac{\sqrt{3}\mathbb{X}_9[\mathbb{Q}_3^{(a,T_2)}(1,-1)]}{3} + \frac{\sqrt{3}\mathbb{X}_9[\mathbb{Q}_3^{(a,T_2)}(1,-1)]}{3} + \frac{\sqrt{3}\mathbb{X}_9[\mathbb{Q}_3^{(a,T_2)}(1,-1)]}{3}$$

No. 22
$$\hat{\mathbb{Q}}_0^{(A_1)}$$
 [M₃, B₂]

$$\hat{\mathbb{Z}}_{22} = \mathbb{X}_{11}[\mathbb{Q}_0^{(a,A_1)}] \otimes \mathbb{Y}_8[\mathbb{Q}_0^{(b,A_1)}]$$

$$\hat{\mathbb{Z}}_{22}(\mathbf{k}) = \mathbb{X}_{11}[\mathbb{Q}_0^{(a,A_1)}] \otimes \mathbb{U}_1[\mathbb{Q}_0^{(s,A_1)}] \otimes \mathbb{F}_7[\mathbb{Q}_0^{(k,A_1)}]$$

No. 23
$$\hat{\mathbb{Q}}_0^{(A_1)}(1,1)$$
 [M₃, B₂]

$$\hat{\mathbb{Z}}_{23} = \mathbb{X}_{12}[\mathbb{Q}_0^{(a,A_1)}(1,1)] \otimes \mathbb{Y}_8[\mathbb{Q}_0^{(b,A_1)}]$$

$$\hat{\mathbb{Z}}_{23}(\mathbf{k}) = \mathbb{X}_{12}[\mathbb{Q}_0^{(a,A_1)}(1,1)] \otimes \mathbb{U}_1[\mathbb{Q}_0^{(s,A_1)}] \otimes \mathbb{F}_7[\mathbb{Q}_0^{(k,A_1)}]$$

No. 24
$$\hat{\mathbb{Q}}_0^{(A_1)}$$
 [M₃, B₂]

$$\hat{\mathbb{Z}}_{24} = \frac{\sqrt{2}\mathbb{X}_{13}[\mathbb{Q}_{2,0}^{(a,E)}] \otimes \mathbb{Y}_{9}[\mathbb{Q}_{2,0}^{(b,E)}]}{2} + \frac{\sqrt{2}\mathbb{X}_{14}[\mathbb{Q}_{2,1}^{(a,E)}] \otimes \mathbb{Y}_{10}[\mathbb{Q}_{2,1}^{(b,E)}]}{2}$$

$$\hat{\mathbb{Z}}_{24}(\textbf{\textit{k}}) = \frac{\sqrt{2}\mathbb{X}_{13}[\mathbb{Q}_{2,0}^{(a,E)}] \otimes \mathbb{U}_{1}[\mathbb{Q}_{0}^{(s,A_{1})}] \otimes \mathbb{F}_{8}[\mathbb{Q}_{2,0}^{(k,E)}]}{2} + \frac{\sqrt{2}\mathbb{X}_{14}[\mathbb{Q}_{2,1}^{(a,E)}] \otimes \mathbb{U}_{1}[\mathbb{Q}_{0}^{(s,A_{1})}] \otimes \mathbb{F}_{9}[\mathbb{Q}_{2,1}^{(k,E)}]}{2}$$

No. 25
$$\hat{\mathbb{G}}_{4}^{(A_1)}$$
 [M₃, B₂]

$$\hat{\mathbb{Z}}_{25} = \frac{\sqrt{3}\mathbb{X}_{15}[\mathbb{Q}_{2,0}^{(a,T_2)}] \otimes \mathbb{Y}_{11}[\mathbb{Q}_{3,0}^{(b,T_2)}]}{3} + \frac{\sqrt{3}\mathbb{X}_{16}[\mathbb{Q}_{2,1}^{(a,T_2)}] \otimes \mathbb{Y}_{12}[\mathbb{Q}_{3,1}^{(b,T_2)}]}{3} + \frac{\sqrt{3}\mathbb{X}_{17}[\mathbb{Q}_{2,2}^{(a,T_2)}] \otimes \mathbb{Y}_{13}[\mathbb{Q}_{3,2}^{(b,T_2)}]}{3}$$

$$\hat{\mathbb{Z}}_{25}(\boldsymbol{k}) = \frac{\sqrt{3}\mathbb{X}_{15}[\mathbb{Q}_{2,0}^{(a,T_2)}] \otimes \mathbb{U}_1[\mathbb{Q}_0^{(s,A_1)}] \otimes \mathbb{F}_{10}[\mathbb{Q}_{3,0}^{(k,T_2)}]}{3} + \frac{\sqrt{3}\mathbb{X}_{16}[\mathbb{Q}_{2,1}^{(a,T_2)}] \otimes \mathbb{U}_1[\mathbb{Q}_0^{(s,A_1)}] \otimes \mathbb{F}_{11}[\mathbb{Q}_{3,1}^{(k,T_2)}]}{3} + \frac{\sqrt{3}\mathbb{X}_{17}[\mathbb{Q}_{2,2}^{(a,T_2)}] \otimes \mathbb{U}_1[\mathbb{Q}_0^{(s,A_1)}] \otimes \mathbb{F}_{12}[\mathbb{Q}_{3,2}^{(k,T_2)}]}{3} + \frac{\sqrt{3}\mathbb{X}_{17}[\mathbb{Q}_{2,2}^{(a,T_2)}] \otimes \mathbb{U}_1[\mathbb{Q}_0^{(s,A_1)}] \otimes \mathbb{F}_{12}[\mathbb{Q}_3^{(k,T_2)}]}{3} + \frac{\sqrt{3}\mathbb{X}_{17}[\mathbb{Q}_{2,2}^{(a,T_2)}] \otimes \mathbb{U}_1[\mathbb{Q}_0^{(s,A_1)}] \otimes \mathbb{F}_{12}[\mathbb{Q}_3^{(k,T_2)}]}{3} + \frac{\sqrt{3}\mathbb{X}_{17}[\mathbb{Q}_3^{(a,T_2)}] \otimes \mathbb{U}_1[\mathbb{Q}_3^{(s,A_1)}] \otimes \mathbb{F}_{12}[\mathbb{Q}_3^{(k,T_2)}]}{3} + \frac{\sqrt{3}\mathbb{X}_{17}[\mathbb{Q}_3^{(k,T_2)}] \otimes \mathbb{U}_1[\mathbb{Q}_3^{(k,T_2)}]}{3} + \frac{\sqrt{3}\mathbb{X}_{17}[\mathbb{Q}_3^{(k,T_2)}] \otimes \mathbb{U}_1[\mathbb{Q}_3^{(k,T_2)}]}{3} + \frac{\sqrt{3}\mathbb{X}_{17}[\mathbb{Q}_3^{(k,T_2)}] \otimes \mathbb{U}_1[\mathbb{Q}_3^{(k,T_2)}]}{3} + \frac{\sqrt{3}\mathbb{X}_{17}[\mathbb{Q}_3^{(k,T_2)}]}{3} + \frac{\sqrt{3}\mathbb{X}_{17}[\mathbb{Q}_3^{(k,T_2)}] \otimes \mathbb{U}_1[\mathbb{Q}_3^{(k,T_2)}]}{3} + \frac{\sqrt{3}\mathbb{X}_{17}[\mathbb{Q}_3^{(k,T_2)}] \otimes \mathbb{U}_1[\mathbb{Q}_3^{(k,T_2)}]}{3} + \frac{\sqrt{3}\mathbb{X}_{17}[\mathbb{Q}_3^{(k,T_2)}]}{3} +$$

No. 26
$$\hat{\mathbb{Q}}_0^{(A_1)}(1,-1)$$
 [M₃, B₂]

$$\hat{\mathbb{Z}}_{26} = \frac{\sqrt{2}\mathbb{X}_{18}[\mathbb{Q}_{2,0}^{(a,E)}(1,-1)] \otimes \mathbb{Y}_{9}[\mathbb{Q}_{2,0}^{(b,E)}]}{2} + \frac{\sqrt{2}\mathbb{X}_{19}[\mathbb{Q}_{2,1}^{(a,E)}(1,-1)] \otimes \mathbb{Y}_{10}[\mathbb{Q}_{2,1}^{(b,E)}]}{2}$$

$$\hat{\mathbb{Z}}_{26}(\textbf{\textit{k}}) = \frac{\sqrt{2}\mathbb{X}_{18}[\mathbb{Q}_{2,0}^{(a,E)}(1,-1)] \otimes \mathbb{U}_{1}[\mathbb{Q}_{0}^{(s,A_{1})}] \otimes \mathbb{F}_{8}[\mathbb{Q}_{2,0}^{(k,E)}]}{2} + \frac{\sqrt{2}\mathbb{X}_{19}[\mathbb{Q}_{2,1}^{(a,E)}(1,-1)] \otimes \mathbb{U}_{1}[\mathbb{Q}_{0}^{(s,A_{1})}] \otimes \mathbb{F}_{9}[\mathbb{Q}_{2,1}^{(k,E)}]}{2} + \frac{\sqrt{2}\mathbb{X}_{19}[\mathbb{Q}_{2,1}^{(a,E)}(1,-1)] \otimes \mathbb{U}_{1}[\mathbb{Q}_{0}^{(s,A_{1})}]}{2} \otimes \mathbb{F}_{9}[\mathbb{Q}_{2,1}^{(k,E)}]}$$

No. 27 $\hat{\mathbb{G}}_4^{(A_1)}(1,-1)$ [M₃, B₂]

$$\hat{\mathbb{Z}}_{27} = \frac{\sqrt{3}\mathbb{X}_{20}[\mathbb{Q}_{2,0}^{(a,T_2)}(1,-1)] \otimes \mathbb{Y}_{11}[\mathbb{Q}_{3,0}^{(b,T_2)}]}{3} + \frac{\sqrt{3}\mathbb{X}_{21}[\mathbb{Q}_{2,1}^{(a,T_2)}(1,-1)] \otimes \mathbb{Y}_{12}[\mathbb{Q}_{3,1}^{(b,T_2)}]}{3} + \frac{\sqrt{3}\mathbb{X}_{22}[\mathbb{Q}_{2,2}^{(a,T_2)}(1,-1)] \otimes \mathbb{Y}_{13}[\mathbb{Q}_{3,2}^{(b,T_2)}]}{3} + \frac{\sqrt{3}\mathbb{X}_{22}[\mathbb{Q}_{3,2}^{(a,T_2)}(1,-1)] \otimes \mathbb{Y}_{13}[\mathbb{Q}_{3,2}^{(a,T_2)}]}{3} + \frac{\sqrt{3}\mathbb{X}_{22}[\mathbb{Q}_{3,2}^{(a,T_2)}(1,-1)] \otimes \mathbb{Y}_{13}[\mathbb{Q}_{3,2}^{(a,T_2)}]}{3} + \frac{\sqrt{3}\mathbb{X}_{22}[\mathbb{Q}_{3,2}^{(a,T_2)}(1,-1)] \otimes \mathbb{Y}_{13}[\mathbb{Q}_{3,2}^{(a,T_2)}]}{3} + \frac{\sqrt{3}\mathbb{X}_{22}[\mathbb{Q}_{3,2}^{(a,T_2)}(1,-1)] \otimes \mathbb{Y}_{13}[\mathbb{Q}_{3,2}^{(a,T_2)}]}{3} + \frac{\sqrt{3}\mathbb{X}_{22}[\mathbb{Q}_{3,2}^{(a,T_2)}(1,-1)] \otimes \mathbb{Y}_{23}[\mathbb{Q}_{3,2}^{(a,T_2)}]}{3} + \frac{\sqrt{3}\mathbb{X}_{22}[\mathbb{Q}_{3,2}^{(a,T_2)}(1,-1)] \otimes \mathbb{Y}_{23}[\mathbb{Q}_{3,2}^{(a,T_2)}]}{3} + \frac{\sqrt{3}\mathbb{Z}_{2$$

 $\hat{\mathbb{Z}}_{27}(k)$

$$=\frac{\sqrt{3}\mathbb{X}_{20}[\mathbb{Q}_{2,0}^{(a,T_2)}(1,-1)]\otimes\mathbb{U}_1[\mathbb{Q}_0^{(s,A_1)}]\otimes\mathbb{F}_{10}[\mathbb{Q}_{3,0}^{(s,A_1)}]}{3}+\frac{\sqrt{3}\mathbb{X}_{21}[\mathbb{Q}_{2,1}^{(a,T_2)}(1,-1)]\otimes\mathbb{U}_1[\mathbb{Q}_0^{(s,A_1)}]\otimes\mathbb{F}_{11}[\mathbb{Q}_{3,1}^{(k,T_2)}]}{3}+\frac{\sqrt{3}\mathbb{X}_{22}[\mathbb{Q}_{2,2}^{(a,T_2)}(1,-1)]\otimes\mathbb{U}_1[\mathbb{Q}_0^{(s,A_1)}]\otimes\mathbb{F}_{12}[\mathbb{Q}_{3,2}^{(k,T_2)}]}{3}+\frac{\sqrt{3}\mathbb{X}_{22}[\mathbb{Q}_{2,2}^{(a,T_2)}(1,-1)]\otimes\mathbb{U}_1[\mathbb{Q}_0^{(s,A_1)}]\otimes\mathbb{F}_{12}[\mathbb{Q}_{3,2}^{(k,T_2)}]}{3}+\frac{\sqrt{3}\mathbb{X}_{22}[\mathbb{Q}_{2,2}^{(a,T_2)}(1,-1)]\otimes\mathbb{U}_1[\mathbb{Q}_0^{(s,A_1)}]\otimes\mathbb{F}_{12}[\mathbb{Q}_{3,2}^{(k,T_2)}]\otimes\mathbb{P}_{12}[\mathbb{Q}_{3,2}^{(k,T_2)}]\otimes\mathbb{P}_{12}[\mathbb{Q}_{3,2}^{(k,T_2)}]\otimes\mathbb{P}_{12}[\mathbb{Q}_{3,$$

No. 28 $\hat{\mathbb{G}}_0^{(A_1)}$ [M₃, B₂]

$$\hat{\mathbb{Z}}_{28} = \frac{\sqrt{3}\mathbb{X}_{23}[\mathbb{M}_{1,0}^{(a,T_1)}] \otimes \mathbb{Y}_{14}[\mathbb{T}_{1,0}^{(b,T_1)}]}{3} + \frac{\sqrt{3}\mathbb{X}_{24}[\mathbb{M}_{1,1}^{(a,T_1)}] \otimes \mathbb{Y}_{15}[\mathbb{T}_{1,1}^{(b,T_1)}]}{3} + \frac{\sqrt{3}\mathbb{X}_{25}[\mathbb{M}_{1,2}^{(a,T_1)}] \otimes \mathbb{Y}_{16}[\mathbb{T}_{1,2}^{(b,T_1)}]}{3}$$

$$\hat{\mathbb{Z}}_{28}(\boldsymbol{k}) = \frac{\sqrt{3}\mathbb{X}_{23}[\mathbb{M}_{1,0}^{(a,T_1)}] \otimes \mathbb{U}_1[\mathbb{Q}_0^{(s,A_1)}] \otimes \mathbb{F}_{13}[\mathbb{T}_{1,0}^{(k,T_1)}]}{3} + \frac{\sqrt{3}\mathbb{X}_{24}[\mathbb{M}_{1,1}^{(a,T_1)}] \otimes \mathbb{U}_1[\mathbb{Q}_0^{(s,A_1)}] \otimes \mathbb{F}_{14}[\mathbb{T}_{1,1}^{(k,T_1)}]}{3} + \frac{\sqrt{3}\mathbb{X}_{25}[\mathbb{M}_{1,2}^{(a,T_1)}] \otimes \mathbb{U}_1[\mathbb{Q}_0^{(s,A_1)}] \otimes \mathbb{F}_{15}[\mathbb{T}_{1,2}^{(k,T_1)}]}{3} + \frac{\sqrt{3}\mathbb{X}_{25}[\mathbb{M}_{1,2}^{(a,T_1)}] \otimes \mathbb{U}_1[\mathbb{Q}_0^{(s,A_1)}] \otimes \mathbb{F}_{15}[\mathbb{Q}_0^{(s,A_1)}]}{3} \otimes \mathbb{F}_{15}[\mathbb{Q}_0^{(s,A_1)}] \otimes \mathbb{$$

No. 29 $\hat{\mathbb{G}}_0^{(A_1)}(1,1)$ [M₃, B₂]

$$\hat{\mathbb{Z}}_{29} = \frac{\sqrt{3}\mathbb{X}_{26}[\mathbb{M}_{1,0}^{(a,T_1)}(1,1)] \otimes \mathbb{Y}_{14}[\mathbb{T}_{1,0}^{(b,T_1)}]}{3} + \frac{\sqrt{3}\mathbb{X}_{27}[\mathbb{M}_{1,1}^{(a,T_1)}(1,1)] \otimes \mathbb{Y}_{15}[\mathbb{T}_{1,1}^{(b,T_1)}]}{3} + \frac{\sqrt{3}\mathbb{X}_{28}[\mathbb{M}_{1,2}^{(a,T_1)}(1,1)] \otimes \mathbb{Y}_{16}[\mathbb{T}_{1,2}^{(b,T_1)}]}{3} + \frac{\sqrt{3}\mathbb{X}_{28}[\mathbb{M}_{1,2}^{(a,T_1)}(1,1)] \otimes \mathbb{Y}_{16}[\mathbb{T}_{1,2}^{(a,T_1)}(1,1)]}{3} + \frac{\sqrt{3}\mathbb{X}_{28}[\mathbb{M}_{1,2}^{(a,T_1)}(1,1)] \otimes \mathbb{Y}_{16}[\mathbb{M}_{1,2}^{(a,T_1)}(1,1)]}{3} + \frac{\sqrt{3}\mathbb$$

$$\hat{\mathbb{Z}}_{29}(\boldsymbol{k}) = \frac{\sqrt{3}\mathbb{X}_{26}[\mathbb{M}_{1,0}^{(a,T_1)}(1,1)] \otimes \mathbb{U}_1[\mathbb{Q}_0^{(s,A_1)}] \otimes \mathbb{F}_{13}[\mathbb{T}_{1,0}^{(k,T_1)}]}{3} + \frac{\sqrt{3}\mathbb{X}_{27}[\mathbb{M}_{1,1}^{(a,T_1)}(1,1)] \otimes \mathbb{U}_1[\mathbb{Q}_0^{(s,A_1)}] \otimes \mathbb{F}_{14}[\mathbb{T}_{1,1}^{(k,T_1)}]}{3} + \frac{\sqrt{3}\mathbb{X}_{28}[\mathbb{M}_{1,2}^{(a,T_1)}(1,1)] \otimes \mathbb{U}_1[\mathbb{Q}_0^{(s,A_1)}] \otimes \mathbb{F}_{15}[\mathbb{T}_{1,2}^{(k,T_1)}]}{3} + \frac{\sqrt{3}\mathbb{X}_{28}[\mathbb{M}_{1,2}^{(a,T_1)}(1,1)] \otimes \mathbb{U}_1[\mathbb{Q}_0^{(s,A_1)}] \otimes \mathbb{F}_{15}[\mathbb{Q}_0^{(s,A_1)}]}{3} + \frac{\sqrt{3}\mathbb{X}_{28}[\mathbb{Q}_0^{(s,A_1)}] \otimes \mathbb{F}_{15}[\mathbb{Q}_0^{(s,A_1)}]}{3} + \frac{\sqrt{3}\mathbb{X}_{28}[\mathbb{Q}_0^{(s,A_1)}] \otimes \mathbb{Q}_1[\mathbb{Q}_0^{(s,A_1)}]}{3} + \frac{\sqrt{3}\mathbb{X}_{28}[\mathbb{Q}_0^{(s,A_1)}] \otimes \mathbb{Q}_1[\mathbb{Q}_0^{(s,A_1)}]}{3} + \frac{\sqrt{3}\mathbb{Z}_{28}[\mathbb{Q}_0^{(s,A_1)}] \otimes \mathbb{Q}_1[\mathbb{Q}_0^{(s,A_1)}]}{3} + \frac{\sqrt{3}\mathbb{Z}_{28}[\mathbb{Q}_0^{(s,A_1)}]}{3} + \frac{\sqrt{3}\mathbb{Z}_{28}[\mathbb{Q}_0^{(s,A_1)}] \otimes \mathbb{Q}_1[\mathbb{Q}_0^{(s,A_1)}]}{3} + \frac{\sqrt{3}\mathbb{Z}_{28}[\mathbb{Q}_0^{(s,A_1)}] \otimes \mathbb{Q}_1[\mathbb{Q}_0^{(s,A_1)}]}{3} + \frac{\sqrt{3}\mathbb{Z}_{28}[\mathbb{Q}_0^{(s,A_1)}]}{3} + \frac{\sqrt{3}\mathbb{Z}_{$$

No. 30 $\hat{\mathbb{G}}_0^{(A_1)}(1,-1)$ [M₃, B₂]

$$\hat{\mathbb{Z}}_{30} = \frac{\sqrt{3}\mathbb{X}_{29}[\mathbb{M}_{1,0}^{(a,T_1)}(1,-1)] \otimes \mathbb{Y}_{14}[\mathbb{T}_{1,0}^{(b,T_1)}]}{3} + \frac{\sqrt{3}\mathbb{X}_{30}[\mathbb{M}_{1,1}^{(a,T_1)}(1,-1)] \otimes \mathbb{Y}_{15}[\mathbb{T}_{1,1}^{(b,T_1)}]}{3} + \frac{\sqrt{3}\mathbb{X}_{31}[\mathbb{M}_{1,2}^{(a,T_1)}(1,-1)] \otimes \mathbb{Y}_{16}[\mathbb{T}_{1,2}^{(b,T_1)}]}{3} + \frac{\sqrt{3}\mathbb{X}_{31}[\mathbb{M}_{1,2}^{(a,T_1)}(1,-1)] \otimes \mathbb{Y}_{16}[\mathbb{T}_{1,2}^{(a,T_1)}]}{3} + \frac{\sqrt{3}\mathbb{X}_{31}[\mathbb{M}_{1,2}^{(a,T_1)}(1,-1)] \otimes \mathbb{Y}_{16}[\mathbb{T}_{1,2}^{(a,T_1)}]}{3} + \frac{\sqrt{3}\mathbb{X}_{31}[\mathbb{M}_{1,2}^{(a,T_1)}(1,-1)] \otimes \mathbb{Y}_{16}[\mathbb{T}_{1,2}^{(a,T_1)}]}{3} + \frac{\sqrt{3}\mathbb{X}_{31}[\mathbb{M}_{1,2}^{(a,T_1)}(1,-1)] \otimes \mathbb{Y}_{16}[\mathbb{T}_{1,2}^{(a,T_1)}]}{3} + \frac{\sqrt{3}\mathbb{X}_{31}[\mathbb{M}_{1,2}^{(a,T_1)}(1,-1)] \otimes \mathbb{Y}_{16}[\mathbb{M}_{1,2}^{(a,T_1)}(1,-1)]}{3} + \frac{\sqrt{3}\mathbb{X}_{16}[\mathbb{M}_{1,2}^{(a,T_1)}(1,-1)] \otimes \mathbb{Y}_{16}[\mathbb{M}_{1,2}^{(a,T_1)}(1,-1)]}{3} + \frac$$

 $\hat{\mathbb{Z}}_{20}(\mathbf{k})$

$$=\frac{\sqrt{3}\mathbb{X}_{29}[\mathbb{M}_{1,0}^{(a,T_1)}(1,-1)]\otimes\mathbb{U}_{1}[\mathbb{Q}_{0}^{(s,A_1)}]\otimes\mathbb{F}_{13}[\mathbb{T}_{1,0}^{(k,T_1)}]}{3}+\frac{\sqrt{3}\mathbb{X}_{30}[\mathbb{M}_{1,1}^{(a,T_1)}(1,-1)]\otimes\mathbb{U}_{1}[\mathbb{Q}_{0}^{(s,A_1)}]\otimes\mathbb{F}_{14}[\mathbb{T}_{1,1}^{(k,T_1)}]}{3}+\frac{\sqrt{3}\mathbb{X}_{31}[\mathbb{M}_{1,2}^{(a,T_1)}(1,-1)]\otimes\mathbb{U}_{1}[\mathbb{Q}_{0}^{(s,A_1)}]\otimes\mathbb{F}_{15}[\mathbb{T}_{1,2}^{(k,T_1)}]}{3}+\frac{\sqrt{3}\mathbb{X}_{31}[\mathbb{M}_{1,2}^{(a,T_1)}(1,-1)]\otimes\mathbb{U}_{1}[\mathbb{Q}_{0}^{(s,A_1)}]\otimes\mathbb{F}_{15}[\mathbb{T}_{1,2}^{(k,T_1)}]}{3}+\frac{\sqrt{3}\mathbb{X}_{31}[\mathbb{M}_{1,2}^{(a,T_1)}(1,-1)]\otimes\mathbb{U}_{1}[\mathbb{Q}_{0}^{(s,A_1)}]\otimes\mathbb{F}_{15}[\mathbb{T}_{1,2}^{(k,T_1)}]}{3}+\frac{\sqrt{3}\mathbb{X}_{31}[\mathbb{M}_{1,2}^{(a,T_1)}(1,-1)]\otimes\mathbb{U}_{1}[\mathbb{Q}_{0}^{(s,A_1)}]\otimes\mathbb{F}_{15}[\mathbb{T}_{1,2}^{(k,T_1)}]}{3}+\frac{\sqrt{3}\mathbb{X}_{31}[\mathbb{M}_{1,2}^{(a,T_1)}(1,-1)]\otimes\mathbb{U}_{1}[\mathbb{Q}_{0}^{(s,A_1)}]\otimes\mathbb{F}_{15}[\mathbb{Q}_{0}^{(s,A_1$$

$$\hat{\mathbb{Z}}_{31} = \frac{\sqrt{3}\mathbb{X}_{32}[\mathbb{M}_{3,0}^{(a,T_1)}(1,-1)] \otimes \mathbb{Y}_{14}[\mathbb{T}_{1,0}^{(b,T_1)}]}{3} + \frac{\sqrt{3}\mathbb{X}_{33}[\mathbb{M}_{3,1}^{(a,T_1)}(1,-1)] \otimes \mathbb{Y}_{15}[\mathbb{T}_{1,1}^{(b,T_1)}]}{3} + \frac{\sqrt{3}\mathbb{X}_{34}[\mathbb{M}_{3,2}^{(a,T_1)}(1,-1)] \otimes \mathbb{Y}_{16}[\mathbb{T}_{1,2}^{(b,T_1)}]}{3} + \frac{\sqrt{3}\mathbb{X}_{34}[\mathbb{M}_{3,2}^{(a,T_1)}(1,-1)]}{3} + \frac{\sqrt{3}\mathbb{X}_{34}[\mathbb{M}_{3,2}^{(a,T_1)}(1,-1)] \otimes \mathbb{Y}_{16}[\mathbb{T}_{1,2}^{(b,T_1)}]}{3} + \frac{\sqrt{3}\mathbb{X}_{34}[\mathbb{M}_{3,2}^{(a,T_1)}(1,-1)]}{3} +$$

$$= \frac{\sqrt{3}\mathbb{X}_{32}[\mathbb{M}_{3,0}^{(a,T_1)}(1,-1)] \otimes \mathbb{U}_1[\mathbb{Q}_0^{(s,A_1)}] \otimes \mathbb{F}_{13}[\mathbb{T}_{1,0}^{(k,T_1)}]}{3} + \frac{\sqrt{3}\mathbb{X}_{33}[\mathbb{M}_{3,1}^{(a,T_1)}(1,-1)] \otimes \mathbb{U}_1[\mathbb{Q}_0^{(s,A_1)}] \otimes \mathbb{F}_{14}[\mathbb{T}_{1,1}^{(k,T_1)}]}{3} + \frac{\sqrt{3}\mathbb{X}_{34}[\mathbb{M}_{3,2}^{(a,T_1)}(1,-1)] \otimes \mathbb{U}_1[\mathbb{Q}_0^{(s,A_1)}] \otimes \mathbb{F}_{15}[\mathbb{T}_{1,2}^{(k,T_1)}]}{3} + \frac{\sqrt{3}\mathbb{X}_{34}[\mathbb{M}_{3,2}^{(a,T_1)}(1,-1)] \otimes \mathbb{U}_1[\mathbb{Q}_0^{(s,A_1)}] \otimes \mathbb{F}_{15}[\mathbb{Q}_0^{(s,A_1)}]}{3} + \frac{\sqrt{3}\mathbb{X}_{34}[\mathbb{M}_{3,2}^{(a,T_1)}(1,-1)] \otimes \mathbb{U}_1[\mathbb{Q}_0^{(s,A_1)}]}{3} + \frac{\sqrt{3}\mathbb{X}_{34}[\mathbb{M}_{3,2}^{(a,T_1)}(1,-1)]}{3} + \frac{$$

No. 32
$$\hat{\mathbb{Q}}_4^{(A_1)}(1,-1)$$
 [M₃, B₂]

$$\hat{\mathbb{Z}}_{32} = -\frac{\sqrt{3}\mathbb{X}_{35}[\mathbb{M}_{3,0}^{(a,T_2)}(1,-1)]\otimes\mathbb{Y}_{17}[\mathbb{T}_{2,0}^{(b,T_2)}]}{3} - \frac{\sqrt{3}\mathbb{X}_{36}[\mathbb{M}_{3,1}^{(a,T_2)}(1,-1)]\otimes\mathbb{Y}_{18}[\mathbb{T}_{2,1}^{(b,T_2)}]}{3} - \frac{\sqrt{3}\mathbb{X}_{37}[\mathbb{M}_{3,2}^{(a,T_2)}(1,-1)]\otimes\mathbb{Y}_{19}[\mathbb{T}_{2,2}^{(b,T_2)}]}{3} - \frac{\mathbb{X}_{37}[\mathbb{M}_{3,2}^{(a,T_2)}(1,-1)]\otimes\mathbb{Y}_{19}[\mathbb{T}_{2,2}^{(b,T_2)}]}{3} - \frac{\mathbb{X}_{37}[\mathbb{M}_{3,2}^{(a,T_2)}(1,-1)]\otimes\mathbb{Y}_{19}[\mathbb{T}_{2,2}^{(b,T_2)}]}{3} - \frac{\mathbb{X}_{37}[\mathbb{M}_{3,2}^{(a,T_2)}(1,-1)]\otimes\mathbb{Y}_{19}[\mathbb{T}_{2,2}^{(b,T_2)}]}{3} - \frac{\mathbb{X}_{37}[\mathbb{M}_{3,2}^{(a,T_2)}(1,-1)]\otimes\mathbb{Y}_{19}[\mathbb{T}_{2,2}^{(b,T_2)}]}{3} - \frac{\mathbb{X}_{37}[\mathbb{M}_{3,2}^{(a,T_2)}(1,-1)]\otimes\mathbb{Y}_{19}[\mathbb{T}_{2,2}^{(b,T_2)}]}{3} - \frac{\mathbb{X}_{37}[\mathbb{M}_{3,2}^{(a,T_2)}(1,-1)]\otimes\mathbb{Y}_{19}[\mathbb{T}_{2,2}^{(b,T_2)}]}{3} - \frac{\mathbb{X}_{37}[\mathbb{M}_{3,2}^{(b,T_2)}(1,-1)]\otimes\mathbb{Y}_{19}[\mathbb{T}_{2,2}^{(b,T_2)}]}{3} - \frac{\mathbb{X}_{37}[\mathbb{M}_{3,2}^{(b,T_2)}(1,-1)]\otimes\mathbb{Y}_{19}[\mathbb{M}_{3,2}^{(b,T_2)}(1,-1)]}{3} - \frac{\mathbb{X}_{37}[\mathbb{M}_{3,2}^{(b,T_2)}(1,-1)]\otimes\mathbb{Y}_{19}[\mathbb{M}_{3,2}^{(b,T_2)}(1,-$$

$$\begin{split} \hat{\mathbb{Z}}_{32}(\pmb{k}) &= -\frac{\sqrt{3}\mathbb{X}_{35}[\mathbb{M}_{3,0}^{(a,T_2)}(1,-1)] \otimes \mathbb{U}_1[\mathbb{Q}_0^{(s,A_1)}] \otimes \mathbb{F}_{16}[\mathbb{T}_{2,0}^{(k,T_2)}]}{3} - \frac{\sqrt{3}\mathbb{X}_{36}[\mathbb{M}_{3,1}^{(a,T_2)}(1,-1)] \otimes \mathbb{U}_1[\mathbb{Q}_0^{(s,A_1)}] \otimes \mathbb{F}_{17}[\mathbb{T}_{2,1}^{(k,T_2)}]}{3} \\ &- \frac{\sqrt{3}\mathbb{X}_{37}[\mathbb{M}_{3,2}^{(a,T_2)}(1,-1)] \otimes \mathbb{U}_1[\mathbb{Q}_0^{(s,A_1)}] \otimes \mathbb{F}_{18}[\mathbb{T}_{2,2}^{(k,T_2)}]}{3} \end{split}$$

No. 33
$$\hat{\mathbb{Q}}_0^{(A_1)}(1,0) [M_3, B_2]$$

$$\hat{\mathbb{Z}}_{33} = \frac{\sqrt{3}\mathbb{X}_{38}[\mathbb{T}_{2,0}^{(a,T_2)}(1,0)] \otimes \mathbb{Y}_{17}[\mathbb{T}_{2,0}^{(b,T_2)}]}{3} + \frac{\sqrt{3}\mathbb{X}_{39}[\mathbb{T}_{2,1}^{(a,T_2)}(1,0)] \otimes \mathbb{Y}_{18}[\mathbb{T}_{2,1}^{(b,T_2)}]}{3} + \frac{\sqrt{3}\mathbb{X}_{40}[\mathbb{T}_{2,2}^{(a,T_2)}(1,0)] \otimes \mathbb{Y}_{19}[\mathbb{T}_{2,2}^{(b,T_2)}]}{3} + \frac{\sqrt{3}\mathbb{X}_{40}[\mathbb{T}_{2,2}^{(a,T_2)}(1,0)] \otimes \mathbb{Y}_{19}[\mathbb{T}_{2,2}^{(b,T_2)}(1,0)]}{3} + \frac{\sqrt{3}\mathbb{X}_{40}[\mathbb{T}_{2,2}^{(a,T_2)}(1,0)] \otimes \mathbb{Y}_{19}[\mathbb{T}_{2,2}^{(b,T_2)}(1,0)]}{3} + \frac{\sqrt{3}\mathbb{X}_{40}[\mathbb{T}_{2,2}^{(a,T_2)}(1,0)] \otimes \mathbb{Y}_{19}[\mathbb{T}_{2,2}^{(a,T_2)}(1,0)]}{3} + \frac{\sqrt{3}\mathbb{X}_{40}[\mathbb{T}_{2,2}^{(a,T_2)}(1,0)] \otimes \mathbb{Y}_{19}[\mathbb{T}_{2,2}^{(a,T_2)}(1,0)]}{3} + \frac{\sqrt{3}\mathbb{X}_{40}[\mathbb{T}_{2,2}^{(a,T_2)}(1,0)] \otimes \mathbb{Y}_{19}[\mathbb{T}_{2,2}^{(a,T_2)}(1,0)]}{3} + \frac{\sqrt{3}\mathbb{X}_{40}[\mathbb{T}_{2,2}^{(a,T_2)}(1,0)] \otimes \mathbb{Y}_{19}[\mathbb{T}_{2,2}^{(a,T_2)}(1,0)]}{3} + \frac{\sqrt{3}\mathbb{X}_{40}[\mathbb{T}_{2,2}^{(a,T_2)}(1,0)]}{3} + \frac{\sqrt{3}\mathbb{X}_{40}[\mathbb{T}_{2,2}^{(a,T_2)}(1,0)$$

$$\hat{\mathbb{Z}}_{33}(\textbf{\textit{k}}) = \frac{\sqrt{3}\mathbb{X}_{38}[\mathbb{T}_{2,0}^{(a,T_2)}(1,0)] \otimes \mathbb{U}_1[\mathbb{Q}_0^{(s,A_1)}] \otimes \mathbb{F}_{16}[\mathbb{T}_{2,0}^{(k,T_2)}]}{3} + \frac{\sqrt{3}\mathbb{X}_{39}[\mathbb{T}_{2,1}^{(a,T_2)}(1,0)] \otimes \mathbb{U}_1[\mathbb{Q}_0^{(s,A_1)}] \otimes \mathbb{F}_{17}[\mathbb{T}_{2,1}^{(k,T_2)}]}{3} + \frac{\sqrt{3}\mathbb{X}_{40}[\mathbb{T}_{2,2}^{(a,T_2)}(1,0)] \otimes \mathbb{U}_1[\mathbb{Q}_0^{(s,A_1)}] \otimes \mathbb{F}_{18}[\mathbb{T}_{2,2}^{(k,T_2)}]}{3} + \frac{\sqrt{3}\mathbb{X}_{40}[\mathbb{T}_{2,2}^{(k,T_2)}]}{3} + \frac{\sqrt{3}\mathbb{X}_{40}[\mathbb{T}_{2,2}^{(k,T_2)}]}{3$$

Table 5: Atomic SAMB group.

group	bra	ket
M_1	$(s,\uparrow),(s,\downarrow)$	$(s,\uparrow),(s,\downarrow)$
M_2	$(s,\uparrow),(s,\downarrow)$	$(p_x,\uparrow),(p_x,\downarrow),(p_y,\uparrow),(p_y,\downarrow),(p_z,\uparrow),(p_z,\downarrow)$
M_3	$(p_x,\uparrow),(p_x,\downarrow),(p_y,\uparrow),(p_y,\downarrow),(p_z,\uparrow),(p_z,\downarrow)$	$(p_x,\uparrow),(p_x,\downarrow),(p_y,\uparrow),(p_y,\downarrow),(p_z,\uparrow),(p_z,\downarrow)$

Table 6: Atomic SAMB.

symbol	type	group	form
\mathbb{X}_1	$\mathbb{Q}_0^{(a,A_1)}$	M_1	$\begin{pmatrix} \frac{\sqrt{2}}{2} & 0\\ 0 & \frac{\sqrt{2}}{2} \end{pmatrix}$
\mathbb{X}_2	$\mathbb{M}_{1,0}^{(a,T_1)}(1,-1)$	M_1	$\begin{pmatrix} 0 & \frac{\sqrt{2}}{2} \\ 0 & \frac{\sqrt{2}}{2} \\ \frac{\sqrt{2}}{2} & 0 \end{pmatrix}$
\mathbb{X}_3	$\mathbb{M}_{1,1}^{(a,T_1)}(1,-1)$	M_1	$\begin{pmatrix} 0 & -\frac{\sqrt{2}i}{2} \\ \frac{\sqrt{2}i}{2} & 0 \\ \frac{\sqrt{2}}{2} & 0 \\ 0 & -\frac{\sqrt{2}}{2} \end{pmatrix}$
\mathbb{X}_4	$\mathbb{M}_{1,2}^{(a,T_1)}(1,-1)$	M_1	$\begin{pmatrix} \frac{\sqrt{2}}{2} & 0 \\ 0 & -\frac{\sqrt{2}}{2} \end{pmatrix}$
\mathbb{X}_5	$\mathbb{G}_0^{(a,A_1)}(1,1)$	M_2	$ \begin{pmatrix} \frac{\sqrt{2}i}{2} & 0 \\ \left(\frac{\sqrt{2}}{2} & 0 \\ 0 & -\frac{\sqrt{2}}{2} \end{pmatrix} $ $ \begin{pmatrix} 0 & \frac{\sqrt{6}i}{6} & 0 & \frac{\sqrt{6}}{6} & \frac{\sqrt{6}i}{6} & 0 \\ \frac{\sqrt{6}i}{6} & 0 & -\frac{\sqrt{6}}{6} & 0 & 0 & -\frac{\sqrt{6}i}{6} \end{pmatrix} $ $ \begin{pmatrix} 0 & -\frac{\sqrt{3}i}{6} & 0 & -\frac{\sqrt{3}}{6} & \frac{\sqrt{3}i}{3} & 0 \\ -\frac{\sqrt{3}i}{6} & 0 & \frac{\sqrt{3}}{6} & 0 & 0 & -\frac{\sqrt{3}i}{3} \end{pmatrix} $ $ \begin{pmatrix} 0 & \frac{i}{2} & 0 & -\frac{1}{2} & 0 & 0 \\ \frac{i}{2} & 0 & \frac{1}{2} & 0 & 0 & 0 \end{pmatrix} $ $ \begin{pmatrix} 0 & 0 & \frac{i}{2} & 0 & 0 & \frac{1}{2} \\ 0 & 0 & 0 & -\frac{i}{2} & -\frac{1}{2} & 0 \end{pmatrix} $ $ \begin{pmatrix} \frac{i}{2} & 0 & 0 & 0 & 0 & 0 & \frac{i}{2} \end{pmatrix} $
\mathbb{X}_6	$\mathbb{G}_{2,0}^{(a,E)}(1,-1)$	M_2	$\begin{pmatrix} 0 & -\frac{\sqrt{3}i}{6} & 0 & -\frac{\sqrt{3}}{6} & \frac{\sqrt{3}i}{3} & 0 \\ -\frac{\sqrt{3}i}{6} & 0 & \frac{\sqrt{3}}{6} & 0 & 0 & -\frac{\sqrt{3}i}{3} \end{pmatrix}$
\mathbb{X}_7	$\mathbb{G}_{2,1}^{(a,E)}(1,-1)$	M_2	$\begin{pmatrix} 0 & \frac{i}{2} & 0 & -\frac{1}{2} & 0 & 0 \\ \frac{i}{2} & 0 & \frac{1}{2} & 0 & 0 & 0 \end{pmatrix}$
\mathbb{X}_8	$\mathbb{G}_{2,0}^{(a,T_2)}(1,-1)$	M_2	$\begin{pmatrix} \frac{1}{2} & 0 & \frac{1}{2} & 0 & 0 & 0 \\ 0 & 0 & \frac{i}{2} & 0 & 0 & \frac{1}{2} \\ 0 & 0 & 0 & -\frac{i}{2} & -\frac{1}{2} & 0 \end{pmatrix}$
\mathbb{X}_9	$\mathbb{G}_{2,1}^{(a,T_2)}(1,-1)$	M_2	$ \begin{pmatrix} \frac{1}{2} & 0 & 0 & 0 & \frac{1}{2} \\ 0 & -\frac{i}{2} & 0 & 0 & \frac{i}{2} & 0 \end{pmatrix} $
\mathbb{X}_{10}	$\mathbb{G}_{2,2}^{(a,T_2)}(1,-1)$	M_2	$\left(-\frac{1}{2} 0 \frac{t}{2} 0 0 0\right)$
\mathbb{X}_{11}	$\mathbb{Q}_0^{(a,A_1)}$	$ m M_3$	$\begin{pmatrix} \frac{\sqrt{6}}{6} & 0 & 0 & 0 & 0 & 0 \\ 0 & \frac{\sqrt{6}}{6} & 0 & 0 & 0 & 0 \\ 0 & 0 & \frac{\sqrt{6}}{6} & 0 & 0 & 0 \\ 0 & 0 & 0 & \frac{\sqrt{6}}{6} & 0 & 0 \\ 0 & 0 & 0 & 0 & \frac{\sqrt{6}}{6} & 0 \\ 0 & 0 & 0 & 0 & 0 & \frac{\sqrt{6}}{6} \end{pmatrix}$
\mathbb{X}_{12}	$\mathbb{Q}_0^{(a,A_1)}(1,1)$	$ m M_3$	$\begin{pmatrix} 0 & 0 & -\frac{\sqrt{3}i}{6} & 0 & 0 & \frac{\sqrt{3}}{6} \\ 0 & 0 & 0 & \frac{\sqrt{3}i}{6} & -\frac{\sqrt{3}}{6} & 0 \\ \frac{\sqrt{3}i}{6} & 0 & 0 & 0 & -\frac{\sqrt{3}i}{6} \\ 0 & -\frac{\sqrt{3}i}{6} & 0 & 0 & -\frac{\sqrt{3}i}{6} & 0 \\ 0 & -\frac{\sqrt{3}}{6} & 0 & \frac{\sqrt{3}i}{6} & 0 & 0 \\ \frac{\sqrt{3}}{6} & 0 & \frac{\sqrt{3}i}{6} & 0 & 0 \end{pmatrix}$

continued ...

Table 6

symbol	type	group	form
X ₁₃	$\mathbb{Q}_{2,0}^{(a,E)}$	M ₃	$\begin{pmatrix} -\frac{\sqrt{3}}{6} & 0 & 0 & 0 & 0 & 0 \\ 0 & -\frac{\sqrt{3}}{6} & 0 & 0 & 0 & 0 \\ 0 & 0 & -\frac{\sqrt{3}}{6} & 0 & 0 & 0 \\ 0 & 0 & 0 & -\frac{\sqrt{3}}{6} & 0 & 0 \\ 0 & 0 & 0 & 0 & \frac{\sqrt{3}}{3} & 0 \\ 0 & 0 & 0 & 0 & 0 & \frac{\sqrt{3}}{3} \end{pmatrix}$
\mathbb{X}_{14}	$\mathbb{Q}_{2,1}^{(a,E)}$	$ m M_3$	$\begin{pmatrix} \frac{1}{2} & 0 & 0 & 0 & 0 & 0 \\ 0 & \frac{1}{2} & 0 & 0 & 0 & 0 \\ 0 & 0 & -\frac{1}{2} & 0 & 0 & 0 \\ 0 & 0 & 0 & -\frac{1}{2} & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 &$
\mathbb{X}_{15}	$\mathbb{Q}_{2,0}^{(a,T_2)}$	$ m M_3$	$\begin{pmatrix} 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 &$
\mathbb{X}_{16}	$\mathbb{Q}_{2,1}^{(a,T_2)}$	M_3	$\begin{pmatrix} 0 & 0 & 0 & 0 & \frac{1}{2} & 0 \\ 0 & 0 & 0 & 0 & 0 & \frac{1}{2} \\ 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0$
\mathbb{X}_{17}	$\mathbb{Q}_{2,2}^{(a,T_2)}$	$ m M_3$	$\begin{pmatrix} 0 & 0 & \frac{1}{2} & 0 & 0 & 0 \\ 0 & 0 & 0 & \frac{1}{2} & 0 & 0 \\ \frac{1}{2} & 0 & 0 & 0 & 0 & 0 \\ 0 & \frac{1}{2} & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0$

Table 6

symbol	type	group	form
\mathbb{X}_{18}	$\mathbb{Q}_{2,0}^{(a,E)}(1,-1)$	$ m M_3$	$\begin{pmatrix} 0 & 0 & -\frac{\sqrt{6}i}{6} & 0 & 0 & -\frac{\sqrt{6}}{12} \\ 0 & 0 & 0 & \frac{\sqrt{6}i}{6} & \frac{\sqrt{6}}{12} & 0 \\ \frac{\sqrt{6}i}{6} & 0 & 0 & 0 & 0 & \frac{\sqrt{6}i}{12} \\ 0 & -\frac{\sqrt{6}i}{6} & 0 & 0 & \frac{\sqrt{6}i}{12} & 0 \\ 0 & \frac{\sqrt{6}}{12} & 0 & -\frac{\sqrt{6}i}{12} & 0 & 0 \\ -\frac{\sqrt{6}}{12} & 0 & -\frac{\sqrt{6}i}{12} & 0 & 0 & 0 \end{pmatrix}$
\mathbb{X}_{19}	$\mathbb{Q}_{2,1}^{(a,E)}(1,-1)$	$ m M_3$	$\begin{pmatrix} 0 & 0 & 0 & 0 & 0 & -\frac{\sqrt{2}}{4} \\ 0 & 0 & 0 & 0 & \frac{\sqrt{2}}{4} & 0 \\ 0 & 0 & 0 & 0 & 0 & -\frac{\sqrt{2}i}{4} \\ 0 & 0 & 0 & 0 & -\frac{\sqrt{2}i}{4} & 0 \\ 0 & \frac{\sqrt{2}}{4} & 0 & \frac{\sqrt{2}i}{4} & 0 & 0 \\ -\frac{\sqrt{2}}{4} & 0 & \frac{\sqrt{2}i}{4} & 0 & 0 & 0 \end{pmatrix}$
\mathbb{X}_{20}	$\mathbb{Q}_{2,0}^{(a,T_2)}(1,-1)$	$ m M_3$	$\begin{pmatrix} 0 & 0 & 0 & -\frac{1}{4} & \frac{1}{4} & 0 \\ 0 & 0 & \frac{\sqrt{2}}{4} & 0 & 0 & -\frac{\sqrt{2}i}{4} \\ 0 & \frac{\sqrt{2}}{4} & 0 & 0 & 0 & 0 \\ -\frac{\sqrt{2}}{4} & 0 & 0 & 0 & 0 & 0 \\ -\frac{\sqrt{2}i}{4} & 0 & 0 & 0 & 0 & 0 \\ 0 & \frac{\sqrt{2}i}{4} & 0 & 0 & 0 & 0 \end{pmatrix}$
\mathbb{X}_{21}	$\mathbb{Q}_{2,1}^{(a,T_2)}(1,-1)$	$ m M_3$	$\begin{pmatrix} 0 & 0 & 0 & -\frac{\sqrt{2}i}{4} & 0 & 0\\ 0 & 0 & -\frac{\sqrt{2}i}{4} & 0 & 0 & 0\\ 0 & \frac{\sqrt{2}i}{4} & 0 & 0 & -\frac{\sqrt{2}i}{4} & 0\\ \frac{\sqrt{2}i}{4} & 0 & 0 & 0 & 0 & \frac{\sqrt{2}i}{4}\\ 0 & 0 & \frac{\sqrt{2}i}{4} & 0 & 0 & 0\\ 0 & 0 & 0 & -\frac{\sqrt{2}i}{4} & 0 & 0 \end{pmatrix}$
\mathbb{X}_{22}	$\mathbb{Q}_{2,2}^{(a,T_2)}(1,-1)$	$ m M_3$	$\begin{pmatrix} 0 & 0 & 0 & 0 & \frac{\sqrt{2}i}{4} \\ 0 & 0 & 0 & 0 & \frac{\sqrt{2}i}{4} & 0 \\ 0 & 0 & 0 & 0 & 0 & -\frac{\sqrt{2}}{4} \\ 0 & 0 & 0 & 0 & \frac{\sqrt{2}}{4} & 0 \\ 0 & -\frac{\sqrt{2}i}{4} & 0 & \frac{\sqrt{2}}{4} & 0 & 0 \\ -\frac{\sqrt{2}i}{4} & 0 & -\frac{\sqrt{2}}{4} & 0 & 0 & 0 \end{pmatrix}$

symbol	type	group	form
\mathbb{X}_{23}	$\mathbb{M}_{1,0}^{(a,T_1)}$	$ m M_3$	$\begin{pmatrix} 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 &$
\mathbb{X}_{24}	$\mathbb{M}_{1,1}^{(a,T_1)}$	$ m M_3$	$\begin{pmatrix} 0 & 0 & 0 & 0 & \frac{i}{2} & 0 \\ 0 & 0 & 0 & 0 & 0 & \frac{i}{2} \\ 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0$
\mathbb{X}_{25}	$\mathbb{M}_{1,2}^{(a,T_1)}$	$ m M_3$	$\begin{pmatrix} 0 & 0 & -\frac{i}{2} & 0 & 0 & 0 \\ 0 & 0 & 0 & -\frac{i}{2} & 0 & 0 \\ \frac{i}{2} & 0 & 0 & 0 & 0 & 0 \\ 0 & \frac{i}{2} & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0$
\mathbb{X}_{26}	$\mathbb{M}_{1,0}^{(a,T_1)}(1,1)$	M ₃	$ \begin{bmatrix} 0 & \frac{\sqrt{30}}{15} & 0 & -\frac{\sqrt{30}i}{20} & \frac{\sqrt{30}}{20} & 0 \\ \frac{\sqrt{30}}{15} & 0 & \frac{\sqrt{30}i}{20} & 0 & 0 & -\frac{\sqrt{30}}{20} \\ 0 & -\frac{\sqrt{30}i}{20} & 0 & -\frac{\sqrt{30}}{30} & 0 & 0 \\ \frac{\sqrt{30}i}{20} & 0 & -\frac{\sqrt{30}}{30} & 0 & 0 & 0 \\ \frac{\sqrt{30}}{20} & 0 & 0 & 0 & 0 & -\frac{\sqrt{30}}{30} \\ 0 & -\frac{\sqrt{30}}{20} & 0 & 0 & 0 & -\frac{\sqrt{30}}{30} & 0 \end{bmatrix} $
\mathbb{X}_{27}	$\mathbb{M}_{1,1}^{(a,T_1)}(1,1)$	$ m M_3$	$ \begin{pmatrix} 20 & -\frac{\sqrt{30}}{20} & 0 & 0 & -\frac{\sqrt{30}}{30} & 0 \\ 0 & \frac{\sqrt{30}i}{30} & 0 & \frac{\sqrt{30}}{20} & 0 & 0 \\ -\frac{\sqrt{30}i}{30} & 0 & \frac{\sqrt{30}}{20} & 0 & 0 & 0 \\ 0 & \frac{\sqrt{30}}{20} & 0 & -\frac{\sqrt{30}i}{15} & \frac{\sqrt{30}}{20} & 0 \\ \frac{\sqrt{30}}{20} & 0 & \frac{\sqrt{30}i}{15} & 0 & 0 & -\frac{\sqrt{30}}{20} \\ 0 & 0 & \frac{\sqrt{30}}{20} & 0 & 0 & 0 & \frac{\sqrt{30}i}{30} \\ \end{pmatrix} $

symbol	type	group	form
X ₂₈	$\mathbb{M}_{1,2}^{(a,T_1)}(1,1)$	M_3	$\begin{pmatrix} -\frac{\sqrt{30}}{30} & 0 & 0 & 0 & 0 & \frac{\sqrt{30}}{20} \\ 0 & \frac{\sqrt{30}}{30} & 0 & 0 & \frac{\sqrt{30}}{20} & 0 \\ 0 & 0 & -\frac{\sqrt{30}}{30} & 0 & 0 & -\frac{\sqrt{30}i}{20} \\ 0 & 0 & 0 & \frac{\sqrt{30}}{30} & \frac{\sqrt{30}i}{20} & 0 \\ 0 & \frac{\sqrt{30}}{20} & 0 & -\frac{\sqrt{30}i}{20} & \frac{\sqrt{30}}{15} & 0 \\ \frac{\sqrt{30}}{20} & 0 & \frac{\sqrt{30}i}{20} & 0 & 0 & -\frac{\sqrt{30}}{15} \end{pmatrix}$
\mathbb{X}_{29}	$\mathbb{M}_{1,0}^{(a,T_1)}(1,-1)$	$ m M_3$	$\begin{pmatrix} 0 & \frac{\sqrt{6}}{6} & 0 & 0 & 0 & 0 \\ \frac{\sqrt{6}}{6} & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & \frac{\sqrt{6}}{6} & 0 & 0 \\ 0 & 0 & \frac{\sqrt{6}}{6} & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & \frac{\sqrt{6}}{6} \\ 0 & 0 & 0 & 0 & 0 & \frac{\sqrt{6}}{6} & 0 \end{pmatrix}$
\mathbb{X}_{30}	$\mathbb{M}_{1,1}^{(a,T_1)}(1,-1)$	$ m M_3$	$\begin{pmatrix} 0 & -\frac{\sqrt{6}i}{6} & 0 & 0 & 0 & 0\\ \frac{\sqrt{6}i}{6} & 0 & 0 & 0 & 0 & 0\\ 0 & 0 & 0 & -\frac{\sqrt{6}i}{6} & 0 & 0\\ 0 & 0 & \frac{\sqrt{6}i}{6} & 0 & 0 & 0\\ 0 & 0 & 0 & 0 & 0 & -\frac{\sqrt{6}i}{6}\\ 0 & 0 & 0 & 0 & 0 & \frac{\sqrt{6}i}{6} & 0 \end{pmatrix}$
\mathbb{X}_{31}	$\mathbb{M}_{1,2}^{(a,T_1)}(1,-1)$	$ m M_3$	$\begin{pmatrix} \frac{\sqrt{6}}{6} & 0 & 0 & 0 & 0 & 0 \\ 0 & -\frac{\sqrt{6}}{6} & 0 & 0 & 0 & 0 \\ 0 & 0 & \frac{\sqrt{6}}{6} & 0 & 0 & 0 \\ 0 & 0 & 0 & -\frac{\sqrt{6}}{6} & 0 & 0 \\ 0 & 0 & 0 & 0 & \frac{\sqrt{6}}{6} & 0 \\ 0 & 0 & 0 & 0 & 0 & -\frac{\sqrt{6}}{6} \end{pmatrix}$
\mathbb{X}_{32}	$\mathbb{M}_{3,0}^{(a,T_1)}(1,-1)$	$ m M_3$	$\begin{pmatrix} 0 & \frac{\sqrt{5}}{5} & 0 & \frac{\sqrt{5}i}{10} & -\frac{\sqrt{5}}{10} & 0\\ \frac{\sqrt{5}}{5} & 0 & -\frac{\sqrt{5}i}{10} & 0 & 0 & \frac{\sqrt{5}}{10}\\ 0 & \frac{\sqrt{5}i}{10} & 0 & -\frac{\sqrt{5}}{10} & 0 & 0\\ -\frac{\sqrt{5}i}{10} & 0 & -\frac{\sqrt{5}}{10} & 0 & 0 & 0\\ -\frac{\sqrt{5}}{10} & 0 & 0 & 0 & 0 & -\frac{\sqrt{5}}{10}\\ 0 & \frac{\sqrt{5}}{10} & 0 & 0 & -\frac{\sqrt{5}}{10} & 0 \end{pmatrix}$

Table 6

symbol	type	group	form
X33	$\mathbb{M}_{3,1}^{(a,T_1)}(1,-1)$	М3	$\begin{pmatrix} 0 & \frac{\sqrt{5}i}{10} & 0 & -\frac{\sqrt{5}}{10} & 0 & 0\\ -\frac{\sqrt{5}i}{10} & 0 & -\frac{\sqrt{5}}{10} & 0 & 0 & 0\\ 0 & -\frac{\sqrt{5}}{10} & 0 & -\frac{\sqrt{5}i}{5} & -\frac{\sqrt{5}}{10} & 0\\ -\frac{\sqrt{5}}{10} & 0 & \frac{\sqrt{5}i}{5} & 0 & 0 & \frac{\sqrt{5}}{10}\\ 0 & 0 & -\frac{\sqrt{5}}{10} & 0 & 0 & \frac{\sqrt{5}i}{10}\\ 0 & 0 & 0 & \frac{\sqrt{5}}{10} & -\frac{\sqrt{5}i}{10} & 0 \end{pmatrix}$
\mathbb{X}_{34}	$\mathbb{M}_{3,2}^{(a,T_1)}(1,-1)$	$ m M_3$	$\begin{pmatrix} 0 & 0 & 0 & \frac{1}{10} & -\frac{1}{10} & 0 \\ -\frac{\sqrt{5}}{10} & 0 & 0 & 0 & -\frac{\sqrt{5}}{10} & 0 \\ 0 & \frac{\sqrt{5}}{10} & 0 & 0 & -\frac{\sqrt{5}}{10} & 0 \\ 0 & 0 & -\frac{\sqrt{5}}{10} & 0 & 0 & \frac{\sqrt{5}i}{10} \\ 0 & 0 & 0 & \frac{\sqrt{5}}{10} & -\frac{\sqrt{5}i}{10} & 0 \\ 0 & -\frac{\sqrt{5}}{10} & 0 & \frac{\sqrt{5}i}{10} & \frac{\sqrt{5}}{5} & 0 \\ -\frac{\sqrt{5}}{10} & 0 & -\frac{\sqrt{5}i}{10} & 0 & 0 & -\frac{\sqrt{5}}{5} \end{pmatrix} \begin{pmatrix} 0 & 0 & 0 & -\frac{\sqrt{5}}{5} \\ -\frac{\sqrt{5}}{10} & 0 & -\frac{\sqrt{3}i}{10} & 0 & 0 & -\frac{\sqrt{5}}{5} \end{pmatrix} \begin{pmatrix} 0 & 0 & 0 & -\frac{\sqrt{3}i}{6} & 0 \\ 0 & 0 & -\frac{\sqrt{3}i}{6} & 0 & 0 & 0 \\ 0 & 0 & \frac{\sqrt{3}i}{6} & 0 & 0 & 0 \\ -\frac{\sqrt{3}i}{6} & 0 & \frac{\sqrt{3}}{6} & 0 & 0 & 0 \\ 0 & \frac{\sqrt{3}i}{6} & 0 & 0 & -\frac{\sqrt{3}}{6} & 0 \end{pmatrix} \begin{pmatrix} 0 & \frac{\sqrt{3}i}{6} & 0 & 0 & 0 \\ -\frac{\sqrt{3}i}{6} & 0 & -\frac{\sqrt{3}}{6} & 0 & 0 & 0 \\ 0 & -\frac{\sqrt{3}i}{6} & 0 & -\frac{\sqrt{3}}{6} & 0 & 0 \\ 0 & -\frac{\sqrt{3}}{6} & 0 & 0 & 0 & -\frac{\sqrt{3}}{6} \\ 0 & 0 & 0 & \frac{\sqrt{3}}{6} & 0 & 0 & -\frac{\sqrt{3}}{6} \\ 0 & 0 & 0 & -\frac{\sqrt{3}}{6} & \frac{\sqrt{3}i}{6} & 0 \end{pmatrix} \begin{pmatrix} \frac{\sqrt{3}}{6} & 0 & 0 & 0 & -\frac{\sqrt{3}}{6} \\ 0 & 0 & 0 & -\frac{\sqrt{3}}{6} & \frac{\sqrt{3}i}{6} & 0 \end{pmatrix} \begin{pmatrix} \frac{\sqrt{3}}{6} & 0 & 0 & 0 & -\frac{\sqrt{3}}{6} \\ 0 & 0 & 0 & -\frac{\sqrt{3}}{6} & \frac{\sqrt{3}i}{6} & 0 \end{pmatrix} \begin{pmatrix} \frac{\sqrt{3}}{6} & 0 & 0 & 0 & 0 & \frac{\sqrt{3}}{6} \\ 0 & 0 & 0 & -\frac{\sqrt{3}}{6} & \frac{\sqrt{3}i}{6} & 0 \end{pmatrix} \begin{pmatrix} \frac{\sqrt{3}}{6} & 0 & 0 & 0 & 0 & \frac{\sqrt{3}}{6} \\ 0 & 0 & 0 & -\frac{\sqrt{3}}{6} & \frac{\sqrt{3}i}{6} & 0 \end{pmatrix} \begin{pmatrix} \frac{\sqrt{3}}{6} & 0 & 0 & 0 & 0 & \frac{\sqrt{3}}{6} \\ 0 & 0 & 0 & -\frac{\sqrt{3}}{6} & \frac{\sqrt{3}i}{6} & 0 \end{pmatrix} \begin{pmatrix} \frac{\sqrt{3}}{6} & 0 & 0 & 0 & 0 & \frac{\sqrt{3}}{6} \\ 0 & 0 & 0 & -\frac{\sqrt{3}}{6} & \frac{\sqrt{3}i}{6} & 0 & 0 \end{pmatrix} \begin{pmatrix} \frac{\sqrt{3}}{6} & 0 & 0 & 0 & 0 & \frac{\sqrt{3}}{6} \\ 0 & 0 & 0 & -\frac{\sqrt{3}}{6} & \frac{\sqrt{3}i}{6} & 0 & 0 & 0 \end{pmatrix} \begin{pmatrix} \frac{\sqrt{3}}{6} & 0 & 0 & 0 & 0 & \frac{\sqrt{3}}{6} \\ 0 & 0 & 0 & 0 & -\frac{\sqrt{3}}{6} & 0 & 0 & 0 & 0 \end{pmatrix} \begin{pmatrix} \frac{\sqrt{3}}{6} & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & -\frac{\sqrt{3}}{6} & 0 & 0 & 0 & 0 & 0 \end{pmatrix} \begin{pmatrix} \frac{\sqrt{3}}{6} & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0$
\mathbb{X}_{35}	$\mathbb{M}_{3,0}^{(a,T_2)}(1,-1)$	$ m M_3$	$ \begin{pmatrix} 0 & 0 & 0 & -\frac{\sqrt{3}i}{6} & -\frac{\sqrt{3}}{6} & 0\\ 0 & 0 & \frac{\sqrt{3}i}{6} & 0 & 0 & \frac{\sqrt{3}}{6}\\ 0 & -\frac{\sqrt{3}i}{6} & 0 & \frac{\sqrt{3}}{6} & 0 & 0\\ \frac{\sqrt{3}i}{6} & 0 & \frac{\sqrt{3}}{6} & 0 & 0 & 0\\ -\frac{\sqrt{3}}{6} & 0 & 0 & 0 & 0 & -\frac{\sqrt{3}}{6}\\ 0 & \frac{\sqrt{3}}{6} & 0 & 0 & -\frac{\sqrt{3}}{6} & 0 \end{pmatrix} $
\mathbb{X}_{36}	$\mathbb{M}_{3,1}^{(a,T_2)}(1,-1)$	$ m M_3$	$\begin{pmatrix} 0 & \frac{\sqrt{3}i}{6} & 0 & -\frac{\sqrt{3}}{6} & 0 & 0\\ -\frac{\sqrt{3}i}{6} & 0 & -\frac{\sqrt{3}}{6} & 0 & 0 & 0\\ 0 & -\frac{\sqrt{3}}{6} & 0 & 0 & \frac{\sqrt{3}}{6} & 0\\ -\frac{\sqrt{3}}{6} & 0 & 0 & 0 & -\frac{\sqrt{3}}{6}\\ 0 & 0 & \frac{\sqrt{3}}{6} & 0 & 0 & -\frac{\sqrt{3}i}{6}\\ 0 & 0 & 0 & -\frac{\sqrt{3}}{6} & \frac{\sqrt{3}i}{6} & 0 \end{pmatrix}$
\mathbb{X}_{37}	$\mathbb{M}_{3,2}^{(a,T_2)}(1,-1)$	$ m M_3$	$\begin{pmatrix} \frac{\sqrt{3}}{6} & 0 & 0 & 0 & \frac{\sqrt{3}}{6} \\ 0 & -\frac{\sqrt{3}}{6} & 0 & 0 & \frac{\sqrt{3}}{6} & 0 \\ 0 & 0 & -\frac{\sqrt{3}}{6} & 0 & 0 & \frac{\sqrt{3}i}{6} \\ 0 & 0 & 0 & \frac{\sqrt{3}}{6} & -\frac{\sqrt{3}i}{6} & 0 \\ 0 & \frac{\sqrt{3}}{6} & 0 & \frac{\sqrt{3}i}{6} & 0 & 0 \\ \frac{\sqrt{3}}{6} & 0 & -\frac{\sqrt{3}i}{6} & 0 & 0 & 0 \end{pmatrix}$

symbol	type	group	form
X38	$\mathbb{T}_{2,0}^{(a,T_2)}(1,0)$	M ₃	$\begin{pmatrix} 0 & 0 & 0 & \frac{\sqrt{6}i}{12} & \frac{\sqrt{6}}{12} & 0\\ 0 & 0 & -\frac{\sqrt{6}i}{12} & 0 & 0 & -\frac{\sqrt{6}}{12}\\ 0 & \frac{\sqrt{6}i}{12} & 0 & \frac{\sqrt{6}}{6} & 0 & 0\\ -\frac{\sqrt{6}i}{12} & 0 & \frac{\sqrt{6}}{6} & 0 & 0 & 0\\ \frac{\sqrt{6}}{12} & 0 & 0 & 0 & 0 & -\frac{\sqrt{6}}{6}\\ 0 & -\frac{\sqrt{6}}{12} & 0 & 0 & -\frac{\sqrt{6}}{6} & 0 \end{pmatrix}$
\mathbb{X}_{39}	$\mathbb{T}_{2,1}^{(a,T_2)}(1,0)$	$ m M_3$	$\begin{pmatrix} \frac{\sqrt{6}}{12} & 0 & 0 & 0 & 0 & -\frac{\sqrt{6}}{6} \\ 0 & -\frac{\sqrt{6}}{12} & 0 & 0 & -\frac{\sqrt{6}}{6} & 0 \end{pmatrix}$ $\begin{pmatrix} 0 & \frac{\sqrt{6}i}{6} & 0 & \frac{\sqrt{6}}{12} & 0 & 0 \\ -\frac{\sqrt{6}i}{6} & 0 & \frac{\sqrt{6}}{12} & 0 & 0 & 0 \\ 0 & \frac{\sqrt{6}}{12} & 0 & 0 & -\frac{\sqrt{6}}{12} & 0 \\ \frac{\sqrt{6}}{12} & 0 & 0 & 0 & \frac{\sqrt{6}}{12} & 0 \\ 0 & 0 & -\frac{\sqrt{6}}{12} & 0 & 0 & -\frac{\sqrt{6}i}{6} \\ 0 & 0 & 0 & \frac{\sqrt{6}}{12} & \frac{\sqrt{6}i}{6} & 0 \end{pmatrix}$
\mathbb{X}_{40}	$\mathbb{T}_{2,2}^{(a,T_2)}(1,0)$	$ m M_3$	$\begin{pmatrix} \frac{\sqrt{6}}{6} & 0 & 0 & 0 & 0 & -\frac{\sqrt{6}}{12} \\ 0 & -\frac{\sqrt{6}}{6} & 0 & 0 & -\frac{\sqrt{6}}{12} & 0 \\ 0 & 0 & -\frac{\sqrt{6}}{6} & 0 & 0 & -\frac{\sqrt{6}i}{12} \\ 0 & 0 & 0 & \frac{\sqrt{6}}{6} & \frac{\sqrt{6}i}{12} & 0 \\ 0 & -\frac{\sqrt{6}}{12} & 0 & -\frac{\sqrt{6}i}{12} & 0 & 0 \\ -\frac{\sqrt{6}}{12} & 0 & \frac{\sqrt{6}i}{12} & 0 & 0 & 0 \end{pmatrix}$

Table 7: Cluster SAMB.

symbol	type	cluster	form
\mathbb{Y}_1	$\mathbb{Q}_0^{(s,A_1)}$	S_1	(1)
\mathbb{Y}_2	$\mathbb{Q}_0^{(b,A_1)}$	B_1	$\begin{pmatrix} \frac{\sqrt{3}}{3} & \frac{\sqrt{3}}{3} & \frac{\sqrt{3}}{3} \end{pmatrix}$
\mathbb{Y}_3	$\mathbb{Q}_{2,0}^{(b,E)}$	B_1	$\begin{pmatrix} -\frac{\sqrt{6}}{3} & \frac{\sqrt{6}}{6} & \frac{\sqrt{6}}{6} \\ 0 & -\frac{\sqrt{2}}{2} & \frac{\sqrt{2}}{2} \end{pmatrix}$
\mathbb{Y}_4	$\mathbb{Q}_{2,1}^{(b,E)}$	B_1	$\left(0 - \frac{\sqrt{2}}{2} - \frac{\sqrt{2}}{2}\right)$
\mathbb{Y}_5	$\mathbb{T}_{4,0}^{(b,T_1)}$	B_1	$\begin{pmatrix} 0 & i & 0 \end{pmatrix}$
\mathbb{Y}_6	$\mathbb{T}_{4,1}^{(b,T_1)}$	B_1	$\begin{pmatrix} 0 & 0 & i \end{pmatrix}$

Table 7

symbol	type	cluster	form
\mathbb{Y}_7	$\mathbb{T}_{4,2}^{(b,T_1)}$	B_1	$\begin{pmatrix} i & 0 & 0 \end{pmatrix}$
\mathbb{Y}_8	$\mathbb{Q}_0^{(b,A_1)}$	B_2	
\mathbb{Y}_9	$\mathbb{Q}_{2,0}^{(b,E)}$	B_2	$\left(-\frac{\sqrt{3}}{6} - \frac{\sqrt{3}}{6} - \frac{\sqrt{3}}{6} - \frac{\sqrt{3}}{6} - \frac{\sqrt{3}}{3} - \frac{\sqrt{3}}{6} - \frac{\sqrt{3}}{3} \right)$
\mathbb{Y}_{10}	$\mathbb{Q}_{2,0}^{(b,E)}$ $\mathbb{Q}_{2,1}^{(b,T)}$	B_2	$\begin{pmatrix} \frac{1}{2} & \frac{1}{2} & -\frac{1}{2} & 0 & -\frac{1}{2} & 0 \end{pmatrix}$
\mathbb{Y}_{11}	$\mathbb{Q}_{3,0}^{(b,T_2)}$	B_2	$\begin{pmatrix} \frac{\sqrt{2}}{2} & -\frac{\sqrt{2}}{2} & 0 & 0 & 0 & 0 \end{pmatrix}$
\mathbb{Y}_{12}	$\mathbb{Q}_{3,1}^{(b,1_2)}$	$_{ m B_2}$	$\begin{pmatrix} 0 & 0 & -\frac{\sqrt{2}}{2} & 0 & \frac{\sqrt{2}}{2} & 0 \end{pmatrix}$
\mathbb{Y}_{13}	$\mathbb{Q}_{3,2}^{(b,T_2)}$	$_{ m B_2}$	$\begin{pmatrix} 0 & 0 & 0 & -\frac{\sqrt{2}}{2} & 0 & \frac{\sqrt{2}}{2} \end{pmatrix}$
\mathbb{Y}_{14}	$\mathbb{T}_{1,0}^{(b,T_1)}$	$_{\mathrm{B}_{2}}$	$\left(0 0 \frac{i}{2} \frac{i}{2} \frac{i}{2} \frac{i}{2} \right)$
\mathbb{Y}_{15}	$\mathbb{T}_{1,1}^{(b,T_1)}$	$_{ m B_2}$	$\left(\begin{array}{ccccc} \frac{i}{2} & \frac{i}{2} & 0 & -\frac{i}{2} & 0 & \frac{i}{2} \end{array}\right)$
\mathbb{Y}_{16}	$\mathbb{T}_{1,2}^{(b,T_1)}$	$_{ m B_2}$	$\left(\begin{array}{ccccc} \frac{i}{2} & -\frac{i}{2} & -\frac{i}{2} & 0 & \frac{i}{2} & 0 \end{array}\right)$
\mathbb{Y}_{17}	$\mathbb{T}_{2,0}^{(b,T_2)}$	$_{ m B_2}$	$\left(egin{matrix} 0 & 0 & rac{i}{2} & -rac{i}{2} & rac{i}{2} & -rac{i}{2} \end{matrix} ight)$
\mathbb{Y}_{18}	$\mathbb{T}_{2,1}^{(b,T_2)}$	$_{\mathrm{B}_{2}}$	$\left(egin{array}{ccccc} -rac{i}{2} & -rac{i}{2} & 0 & -rac{i}{2} & 0 & rac{i}{2} \end{array} ight)$
\mathbb{Y}_{19}	$\mathbb{T}_{2,2}^{(b,T_2)}$	B_2	

Table 8: Uniform SAMB.

symbol	type	cluster	form	
\mathbb{U}_1	$\mathbb{Q}_0^{(s,A_1)}$	S_1	(1)	

Table 9: Structure SAMB.

symbol	type	cluster	form
\mathbb{F}_1	$\mathbb{Q}_0^{(k,A_1)}$	B_1	$\frac{\sqrt{6}c_{001}}{3} + \frac{\sqrt{6}c_{002}}{3} + \frac{\sqrt{6}c_{003}}{3}$
\mathbb{F}_2	$\mathbb{Q}_{2,0}^{(k,E)}$	B_1	$-\frac{2\sqrt{3}c_{001}}{3} + \frac{\sqrt{3}c_{002}}{3} + \frac{\sqrt{3}c_{003}}{3}$

Table 9

11	4	-1	C
symbol	type	cluster	form
\mathbb{F}_3	$\mathbb{Q}_{2,1}^{(k,E)}$	B_1	$-c_{002} + c_{003}$
\mathbb{F}_4	$\mathbb{T}_{4,0}^{(k,T_1)}$	B_1	$\sqrt{2}s_{002}$
\mathbb{F}_5	$\mathbb{T}_{4,1}^{(k,T_1)}$	B_1	$\sqrt{2}s_{003}$
\mathbb{F}_6	$\mathbb{T}_{4,2}^{(k,T_1)}$	B_1	$\sqrt{2}s_{001}$
\mathbb{F}_7	$\mathbb{Q}_0^{(k,A_1)}$	B_2	$\frac{\sqrt{3}c_{004}}{3} + \frac{\sqrt{3}c_{005}}{3} + \frac{\sqrt{3}c_{006}}{3} + \frac{\sqrt{3}c_{007}}{3} + \frac{\sqrt{3}c_{008}}{3} + \frac{\sqrt{3}c_{009}}{3}$
\mathbb{F}_8	$\mathbb{Q}_{2,0}^{(k,E)}$	B_2	$-\frac{\sqrt{6}c_{004}}{6} - \frac{\sqrt{6}c_{005}}{6} - \frac{\sqrt{6}c_{006}}{6} + \frac{\sqrt{6}c_{007}}{3} - \frac{\sqrt{6}c_{008}}{6} + \frac{\sqrt{6}c_{009}}{3}$
\mathbb{F}_9	$\bigcap(k,E)$	B_2	$rac{\sqrt{2}c_{004}}{2} + rac{\sqrt{2}c_{005}}{2} - rac{\sqrt{2}c_{006}}{2} - rac{\sqrt{2}c_{008}}{2}$
\mathbb{F}_{10}	$\mathbb{Q}_{3,0}^{(k,T_2)}$	B_2	$c_{004}-c_{005}$
\mathbb{F}_{11}	$\mathbb{Q}_{3,1}^{(\kappa, r_2)}$	B_2	$-c_{006} + c_{008}$
\mathbb{F}_{12}	$\mathbb{Q}_{3,2}^{(\kappa,r_2)}$	B_2	$-c_{007} + c_{009}$
\mathbb{F}_{13}	$\mathbb{T}_{1,0}^{(k,T_1)}$	B_2	$\frac{\sqrt{2}s_{006}}{2} + \frac{\sqrt{2}s_{007}}{2} + \frac{\sqrt{2}s_{008}}{2} + \frac{\sqrt{2}s_{009}}{2}$
\mathbb{F}_{14}	$\mathbb{T}_{1,1}^{(k,T_1)}$	B_2	$rac{\sqrt{2s_{004}}}{2} + rac{\sqrt{2s_{005}}}{2} - rac{\sqrt{2s_{007}}}{2} + rac{\sqrt{2s_{009}}}{2}$
\mathbb{F}_{15}	$\mathbb{T}_{1,2}^{(k,T_1)}$	B_2	$rac{\sqrt{2} s_{004}}{2} - rac{\sqrt{2} s_{005}}{2} - rac{\sqrt{2} s_{006}}{2} + rac{\sqrt{2} s_{008}}{2}$
\mathbb{F}_{16}	$\mathbb{T}_{2,0}^{(k,T_2)}$	B_2	$rac{\sqrt{2} s_{006}}{2} - rac{\sqrt{2} s_{007}}{2} + rac{\sqrt{2} s_{008}}{2} - rac{\sqrt{2} s_{009}}{2}$
\mathbb{F}_{17}	$\mathbb{T}_{2,1}^{(k,T_2)}$	B_2	$-rac{\sqrt{2}s_{004}}{2}-rac{\sqrt{2}s_{005}}{2}-rac{\sqrt{2}s_{007}}{2}+rac{\sqrt{2}s_{009}}{2}$
\mathbb{F}_{18}	$\mathbb{T}_{2,2}^{(k,T_2)}$	B_2	$\frac{\sqrt{2}s_{004}}{2} - \frac{\sqrt{2}s_{005}}{2} + \frac{\sqrt{2}s_{006}}{2} - \frac{\sqrt{2}s_{008}}{2}$

Table 10: Polar harmonics.

No.	symbol	rank	irrep.	mul.	comp.	form
1	$\mathbb{Q}_0^{(A_1)}$	0	A_1	_	_	1
2	$\mathbb{Q}_{1,0}^{(T_1)}$	1	T_1	_	0	x
3	$\mathbb{Q}_{1,1}^{(T_1)}$	1	T_1	_	1	y
4	$\mathbb{Q}_{1,2}^{(T_1)}$	1	T_1	_	2	z
5	$\mathbb{Q}_{2,0}^{(E)}$	2	E	_	0	$-\frac{x^2}{2} - \frac{y^2}{2} + z^2$
6	$\mathbb{Q}_{2,1}^{(E)}$	2	E	_	1	$\frac{\sqrt{3}(x-y)(x+y)}{2}$
7	$\mathbb{Q}_{2,0}^{(\hat{T}_2)}$	2	T_2	_	0	$\sqrt{3}yz$

Table 10

No.	symbol	rank	irrep.	mul.	comp.	form
8	$\mathbb{Q}_{2,1}^{(T_2)}$	2	T_2	_	1	$\sqrt{3}xz$
9	$\mathbb{Q}_{2,2}^{(T_2)}$	2	T_2	_	2	$\sqrt{3}xy$
10	$\mathbb{Q}_{3,0}^{(T_2)}$	3	T_2	_	0	$\frac{\sqrt{15}x(y-z)(y+z)}{2}$
11	$\mathbb{Q}_{3,1}^{(T_2)}$	3	T_2	_	1	$-\frac{\sqrt{15}y(x-z)(x+z)}{2}$
12	$\mathbb{Q}_{3,2}^{(T_2)}$	3	T_2	_	2	$\frac{\sqrt{15}z(x-y)(x+y)}{2}$
13	$\mathbb{Q}_{4,0}^{(T_1)}$	4	T_1	_	0	$\frac{\sqrt{35}yz(y-z)(y+z)}{2}$
14	$\mathbb{Q}_{4,1}^{(T_1)}$	4	T_1	_	1	$-\frac{\sqrt{35}xz(x-z)(x+z)}{2}$
15	$\mathbb{Q}_{4,2}^{(T_1)}$	4	T_1	_	2	$\frac{\sqrt{35}xy(x-y)(x+y)}{2}$

Table 11: Axial harmonics.

No.	symbol	rank	irrep.	mul.	comp.	form
1	$\mathbb{G}_0^{(A_1)}$	0	A_1	-	_	1
2	$\mathbb{G}_{1,0}^{(T_1)}$	1	T_1	_	0	X
3	$\mathbb{G}_{1,1}^{(I_1)}$	1	T_1	_	1	Y
4	$\mathbb{G}_{1,2}^{(T_1)}$	1	T_1	_	2	Z
5	$\mathbb{G}_{2,0}^{(E)}$	2	E	-	0	$-\frac{X^2}{2} - \frac{Y^2}{2} + Z^2$
6	$\mathbb{G}_{2,1}^{(E)}$	2	E	_	1	$\frac{\sqrt{3}(X-Y)(X+Y)}{2}$
7	$\mathbb{G}_{2,0}^{(T_2)}$	2	T_2	_	0	$\sqrt{3}YZ$
8	$\mathbb{G}_{2,1}^{(T_2)}$	2	T_2	_	1	$\sqrt{3}XZ$
9	$\mathbb{G}_{2,2}^{(T_2)}$	2	T_2	_	2	$\sqrt{3}XY$
10	$\mathbb{G}_{3,0}^{(T_1)}$	3	T_1	_	0	$\frac{X(2X^2-3Y^2-3Z^2)}{2}$
11	$\mathbb{G}_{3,1}^{(T_1)}$	3	T_1	_	1	$-\frac{Y(3X^2-2Y^2+3Z^2)}{2}$
12	$\mathbb{G}_{3,2}^{(T_1)}$	3	T_1	_	2	$-\frac{Z(3X^2+3Y^2-2Z^2)}{2}$
13	$\mathbb{G}_{3,0}^{(T_2)}$	3	T_2	_	0	$-\frac{Y(3X^2 - 2Y^2 + 3Z^2)}{2} - \frac{Z(3X^2 + 3Y^2 - 2Z^2)}{\sqrt{15}X(Y - Z)(Y + Z)}$
14	$\mathbb{G}_{3,1}^{(T_2)}$	3	T_2	_	1	$-\frac{\sqrt{15}Y(X-Z)(X+Z)}{2}$
15	$\mathbb{G}_{3,2}^{(T_2)}$	3	T_2	_	2	$\frac{\sqrt{15}Z(X-\tilde{Y})(X+Y)}{2}$

 \bullet Group info.: Generator = $\{2_{001}|0\},~\{2_{010}|0\},~\{3_{~111}^{+}|0\},~\{2_{110}|0\}$

Table 12: Conjugacy class (point-group part).

rep. SO	symmetry operations
{1 0}	{1 0}
$\{2_{001} 0\}$	$\{2_{001} 0\}, \{2_{100} 0\}, \{2_{010} 0\}$
$\{2_{110} 0\}$	$\{2_{110} 0\}, \{2_{101} 0\}, \{2_{011} 0\}, \{2_{1-10} 0\}, \{2_{-101} 0\}, \{2_{01-1} 0\}$
${3^{+}_{111} 0}$	$\left \ \{3^{+}_{111} 0\}, \ \{3^{+}_{1-1-1} 0\}, \ \{3^{+}_{-11-1} 0\}, \ \{3^{+}_{-1-11} 0\}, \ \{3^{-}_{111} 0\}, \ \{3^{-}_{1-1-1} 0\}, \ \{3^{-}_{-11-1} 0\}, \ \{3^{}_{-11-1} 0\}, \ \{3^{-}_{-11-1} 0\}, \ \{3^{-}_{-11-1} 0\}, \ \{3^{-}_$
$\{4^{+}_{001} 0\}$	$\left \begin{array}{cccccccccccccccccccccccccccccccccccc$

Table 13: Symmetry operations.

No.	SO	No.	SO	No.	SO	No.	SO	No.	SO
 1	$\{1 0\}$	2	$\{2_{001} 0\}$	3	$\{2_{100} 0\}$	4	$\{2_{010} 0\}$	5	$\{2_{110} 0\}$
6	$\{2_{101} 0\}$	7	$\{2_{011} 0\}$	8	$\{2_{1-10} 0\}$	9	$\{2_{-101} 0\}$	10	$\{2_{01-1} 0\}$
11	$\{3^{+}_{111} 0\}$	12	$\{3^+_{1-1-1} 0\}$	13	$\{3^{+}_{-11-1} 0\}$	14	$\{3^{+}_{-1-11} 0\}$	15	$\{3^{-}_{111} 0\}$
16	$\{3^{1-1-1} 0\}$	17	$\{3^{-}_{-11-1} 0\}$	18	$\{3^{-}_{-1-11} 0\}$	19	$\{4^{+}_{001} 0\}$	20	$\{4^{+}_{100} 0\}$
21	$\{4^{+}_{010} 0\}$	22	$\{4^{-}_{001} 0\}$	23	$\{4^{-}_{100} 0\}$	24	$\{4^{-}_{010} 0\}$		

Table 14: Character table (point-group part).

	1	2_{001}	2_{110}	3^{+}_{111}	4^{+}_{001}
A_1	1	1	1	1	1
A_2	1	1	-1	1	-1
E	2	2	0	-1	0
T_1	3	-1	-1	0	1
T_2	3	-1	1	0	-1

Table 15: Parity conversion.

\longrightarrow	\leftrightarrow	\leftrightarrow	\leftrightarrow	\leftrightarrow
$A_1 (A_1)$	$A_2 (A_2)$	E(E)	T_1 (T_1)	T_2 (T_2)

Table 16: Symmetric product, $[\Gamma \otimes \Gamma']_+$.

	A_1	A_2	E	T_1	T_2
$\overline{A_1}$	A_1	A_2	E	T_1	T_2
A_2		A_1	E	T_2	T_1
E			$A_1 + E$	$T_1 + T_2$	$T_1 + T_2$
T_1				$A_1 + E + T_2$	$A_2 + E + T_1 + T_2$
T_2					$A_1 + E + T_2$

Table 17: Anti-symmetric product, $[\Gamma \otimes \Gamma]_{-}$.

A 1	<i>A</i> o	E	<i>T</i> ₁	T_0
	- 112	40	T_1	T.
_	_	A_2	<i>1</i> 1	11

Table 18: Virtual-cluster sites.

No.	position	No.	position	No.	position	No.	position
1	$\begin{pmatrix} 2 & 1 & 0 \end{pmatrix}$	2	$\begin{pmatrix} -2 & -1 & 0 \end{pmatrix}$	3	$\begin{pmatrix} 2 & -1 & 0 \end{pmatrix}$	4	$\begin{pmatrix} -2 & 1 & 0 \end{pmatrix}$
5	$\begin{pmatrix} 1 & 2 & 0 \end{pmatrix}$	6	$\begin{pmatrix} 0 & -1 & 2 \end{pmatrix}$	7	$\begin{pmatrix} -2 & 0 & 1 \end{pmatrix}$	8	$\begin{pmatrix} -1 & -2 & 0 \end{pmatrix}$
9	$\begin{pmatrix} 0 & -1 & -2 \end{pmatrix}$	10	$\begin{pmatrix} -2 & 0 & -1 \end{pmatrix}$	11	$\begin{pmatrix} 0 & 2 & 1 \end{pmatrix}$	12	$\begin{pmatrix} 0 & -2 & 1 \end{pmatrix}$
13	$\begin{pmatrix} 0 & -2 & -1 \end{pmatrix}$	14	$\begin{pmatrix} 0 & 2 & -1 \end{pmatrix}$	15	$\begin{pmatrix} 1 & 0 & 2 \end{pmatrix}$	16	$\begin{pmatrix} -1 & 0 & -2 \end{pmatrix}$

Table 18

No.	position	No.	position	No.	position	No.	position
17	$\begin{pmatrix} -1 & 0 & 2 \end{pmatrix}$	18	$\begin{pmatrix} 1 & 0 & -2 \end{pmatrix}$	19	$\begin{pmatrix} -1 & 2 & 0 \end{pmatrix}$	20	$\begin{pmatrix} 2 & 0 & 1 \end{pmatrix}$
21	$\begin{pmatrix} 0 & 1 & -2 \end{pmatrix}$	22	$\begin{pmatrix} 1 & -2 & 0 \end{pmatrix}$	23	$\begin{pmatrix} 2 & 0 & -1 \end{pmatrix}$	24	$\begin{pmatrix} 0 & 1 & 2 \end{pmatrix}$

Table 19: Virtual-cluster basis.

symbol	1	2	3	4	5	6	7	8	9	10
$\mathbb{Q}_0^{(A_1)}$	$\frac{\sqrt{6}}{12}$	$\frac{\sqrt{6}}{12}$	$\frac{\sqrt{6}}{12}$	$\frac{\sqrt{6}}{12}$	$\frac{\sqrt{6}}{12}$	$\frac{\sqrt{6}}{12}$	$\frac{\sqrt{6}}{12}$	$\frac{\sqrt{6}}{12}$	$\frac{\sqrt{6}}{12}$	$\frac{\sqrt{6}}{12}$
€0	$\frac{12}{\frac{\sqrt{6}}{12}}$	$\frac{12}{\frac{\sqrt{6}}{12}}$	$\frac{12}{\frac{\sqrt{6}}{12}}$	$\frac{\sqrt{6}}{12}$	$\frac{\sqrt{6}}{12}$	$\frac{\sqrt{6}}{12}$	$\frac{\sqrt{6}}{12}$	$\frac{\sqrt{6}}{12}$	$\frac{\sqrt{6}}{12}$	$\frac{\sqrt{6}}{12}$
					12	12	12	12	12	12
(T.)	$\frac{\sqrt{6}}{12}$	$\frac{\sqrt{6}}{12}$	$\frac{\sqrt{6}}{12}$	$\frac{\sqrt{6}}{12}$						
$\mathbb{Q}_{1,0}^{(T_1)}$	$\frac{\sqrt{10}}{10}$	$-\frac{\sqrt{10}}{10}$	$\frac{\sqrt{10}}{10}$	$-\frac{\sqrt{10}}{10}$	$\frac{\sqrt{10}}{20}$	0	$-\frac{\sqrt{10}}{10}$	$-\frac{\sqrt{10}}{20}$	0	$-\frac{\sqrt{10}}{10}$
	0	0	0	0	$\frac{\sqrt{10}}{20}$	$-\frac{\sqrt{10}}{20}$	$-\frac{\sqrt{10}}{20}$	$\frac{\sqrt{10}}{20}$	$-\frac{\sqrt{10}}{20}$	$\frac{\sqrt{10}}{10}$
	0	$\frac{\sqrt{10}}{20}$	$\frac{\sqrt{10}}{10}$	0						
$\mathbb{Q}_{1,1}^{(T_1)}$	$\frac{\sqrt{10}}{20}$	$-\frac{\sqrt{10}}{20}$	$-\frac{\sqrt{10}}{20}$	$\frac{\sqrt{10}}{20}$	$\frac{\sqrt{10}}{10}$	$-\frac{\sqrt{10}}{20}$	0	$-\frac{\sqrt{10}}{10}$	$-\frac{\sqrt{10}}{20}$	0
	$\frac{\sqrt{10}}{10}$	$-\frac{\sqrt{10}}{10}$	$-\frac{\sqrt{10}}{10}$	$\frac{\sqrt{10}}{10}$	0	0	0	0	$\frac{\sqrt{10}}{10}$	0
	$\frac{\sqrt{10}}{20}$	$-\frac{\sqrt{10}}{10}$	0	$\frac{\sqrt{10}}{20}$						
$\mathbb{Q}_{1,2}^{(T_1)}$	0	0	0	0	0	$\frac{\sqrt{10}}{10}$	$\frac{\sqrt{10}}{20}$	0	$-\frac{\sqrt{10}}{10}$	$-\frac{\sqrt{10}}{20}$
	$\frac{\sqrt{10}}{20}$	$\frac{\sqrt{10}}{20}$	$-\frac{\sqrt{10}}{20}$	$-\frac{\sqrt{10}}{20}$	$\frac{\sqrt{10}}{10}$	$-\frac{\sqrt{10}}{10}$	$\frac{\sqrt{10}}{10}$	$-\frac{\sqrt{10}}{10}$	0	$\frac{\sqrt{10}}{20}$
	$-\frac{\sqrt{10}}{10}$	0	$-\frac{\sqrt{10}}{20}$	$\frac{\sqrt{10}}{10}$						
$\mathbb{Q}_{2,0}^{(E)}$	$-\frac{5\sqrt{39}}{156}$	$-\frac{5\sqrt{39}}{156}$	$-\frac{5\sqrt{39}}{156}$	$-\frac{5\sqrt{39}}{156}$	$-\frac{5\sqrt{39}}{156}$	$\frac{7\sqrt{39}}{156}$	$-\frac{\sqrt{39}}{78}$	$-\frac{5\sqrt{39}}{156}$	$\frac{7\sqrt{39}}{156}$	$-\frac{\sqrt{39}}{78}$
	$-\frac{\sqrt{39}}{78}$	$-\frac{\sqrt{39}}{78}$	$-\frac{\sqrt{39}}{78}$	$-\frac{\sqrt{39}}{78}$	$\frac{7\sqrt{39}}{156}$	$\frac{7\sqrt{39}}{156}$	$\frac{7\sqrt{39}}{156}$	$\frac{7\sqrt{39}}{156}$	$-\frac{5\sqrt{39}}{156}$	$-\frac{\sqrt{39}}{78}$
	$\frac{7\sqrt{39}}{156}$	$-\frac{5\sqrt{39}}{156}$	$-\frac{\sqrt{39}}{78}$	$\frac{7\sqrt{39}}{156}$						
$\mathbb{Q}_{2,1}^{(E)}$	$\frac{3\sqrt{13}}{52}$	$\frac{3\sqrt{13}}{52}$	$\frac{3\sqrt{13}}{52}$	$\frac{3\sqrt{13}}{52}$	$-\frac{3\sqrt{13}}{52}$	$-\frac{\sqrt{13}}{52}$	$\frac{\sqrt{13}}{13}$	$-\frac{3\sqrt{13}}{52}$	$-\frac{\sqrt{13}}{52}$	$\frac{\sqrt{13}}{13}$
	$-\frac{\sqrt{13}}{13}$	$-\frac{\sqrt{13}}{13}$	$-\frac{\sqrt{13}}{13}$	$-\frac{\sqrt{13}}{13}$	$\frac{\sqrt{13}}{52}$	$\frac{\sqrt{13}}{52}$	$\frac{\sqrt{13}}{52}$	$\frac{\sqrt{13}}{52}$	$-\frac{3\sqrt{13}}{52}$	$\frac{\sqrt{13}}{13}$
	$-\frac{\sqrt{13}}{52}$	$-\frac{3\sqrt{13}}{52}$	$\frac{\sqrt{13}}{13}$	$-\frac{\sqrt{13}}{52}$						
$\mathbb{Q}_{2,0}^{(T_2)}$	0	0	0	0	0	$-\frac{\sqrt{2}}{4}$	0	0	$\frac{\sqrt{2}}{4}$	0
	$\frac{\sqrt{2}}{4}$	$-\frac{\sqrt{2}}{4}$	$\frac{\sqrt{2}}{4}$	$-\frac{\sqrt{2}}{4}$	0	0	0	0	0	0

Table 19

Table 19										
symbol	1	2	3	4	5	6	7	8	9	10
	$-\frac{\sqrt{2}}{4}$	0	0	$\frac{\sqrt{2}}{4}$						
$\mathbb{Q}_{2,1}^{(T_2)}$	0	0	0	0	0	0	$-\frac{\sqrt{2}}{4}$	0	0	$\frac{\sqrt{2}}{4}$
	0	0	0	0	$\frac{\sqrt{2}}{4}$	$\frac{\sqrt{2}}{4}$	$-\frac{\sqrt{2}}{4}$	$-\frac{\sqrt{2}}{4}$	0	$\frac{\sqrt{2}}{4}$
	0	0	$-\frac{\sqrt{2}}{4}$	0						
$\mathbb{Q}_{2,2}^{(T_2)}$	$\frac{\sqrt{2}}{4}$	$\frac{\sqrt{2}}{4}$	$-\frac{\sqrt{2}}{4}$	$-\frac{\sqrt{2}}{4}$	$\frac{\sqrt{2}}{4}$	0	0	$\frac{\sqrt{2}}{4}$	0	0
	0	0	0	0	0	0	0	0	$-\frac{\sqrt{2}}{4}$	0
	0	$-\frac{\sqrt{2}}{4}$	0	0						
$\mathbb{Q}_{3,0}^{(T_1)}$	$\frac{\sqrt{10}}{20}$	$-\frac{\sqrt{10}}{20}$	$\frac{\sqrt{10}}{20}$	$-\frac{\sqrt{10}}{20}$	$-\frac{\sqrt{10}}{10}$	0	$-\frac{\sqrt{10}}{20}$	$\frac{\sqrt{10}}{10}$	0	$-\frac{\sqrt{10}}{20}$
	0	0	0	0	$-\frac{\sqrt{10}}{10}$	$\frac{\sqrt{10}}{10}$	$\frac{\sqrt{10}}{10}$	$-\frac{\sqrt{10}}{10}$	$\frac{\sqrt{10}}{10}$	$\frac{\sqrt{10}}{20}$
	0	$-\frac{\sqrt{10}}{10}$	$\frac{\sqrt{10}}{20}$	0						
$\mathbb{Q}_{3,1}^{(T_1)}$	$-\frac{\sqrt{10}}{10}$	$\frac{\sqrt{10}}{10}$	$\frac{\sqrt{10}}{10}$	$-\frac{\sqrt{10}}{10}$	$\frac{\sqrt{10}}{20}$	$\frac{\sqrt{10}}{10}$	0	$-\frac{\sqrt{10}}{20}$	$\frac{\sqrt{10}}{10}$	0
	$\frac{\sqrt{10}}{20}$	$-\frac{\sqrt{10}}{20}$	$-\frac{\sqrt{10}}{20}$	$\frac{\sqrt{10}}{20}$	0	0	0	0	$\frac{\sqrt{10}}{20}$	0
	$-\frac{\sqrt{10}}{10}$	$-\frac{\sqrt{10}}{20}$	0	$-\frac{\sqrt{10}}{10}$						
$\mathbb{Q}_{3,2}^{(T_1)}$	0	0	0	0	0	$\frac{\sqrt{10}}{20}$	$-\frac{\sqrt{10}}{10}$	0	$-\frac{\sqrt{10}}{20}$	$\frac{\sqrt{10}}{10}$
	$-\frac{\sqrt{10}}{10}$	$-\frac{\sqrt{10}}{10}$	$\frac{\sqrt{10}}{10}$	$\frac{\sqrt{10}}{10}$	$\frac{\sqrt{10}}{20}$	$-\frac{\sqrt{10}}{20}$	$\frac{\sqrt{10}}{20}$	$-\frac{\sqrt{10}}{20}$	0	$-\frac{\sqrt{10}}{10}$
	$-\frac{\sqrt{10}}{20}$	0	$\frac{\sqrt{10}}{10}$	$\frac{\sqrt{10}}{20}$						
$\mathbb{Q}_{3,0}^{(T_2)}$	$\frac{\sqrt{10}}{20}$	$-\frac{\sqrt{10}}{20}$	$\frac{\sqrt{10}}{20}$	$-\frac{\sqrt{10}}{20}$	$\frac{\sqrt{10}}{10}$	0	$\frac{\sqrt{10}}{20}$	$-\frac{\sqrt{10}}{10}$	0	$\frac{\sqrt{10}}{20}$
	0	0	0	0	$-\frac{\sqrt{10}}{10}$	$\frac{\sqrt{10}}{10}$	$\frac{\sqrt{10}}{10}$	$-\frac{\sqrt{10}}{10}$	$-\frac{\sqrt{10}}{10}$	$-\frac{\sqrt{10}}{20}$
	0	$\frac{\sqrt{10}}{10}$	$-\frac{\sqrt{10}}{20}$	0						
$\mathbb{Q}_{3,1}^{(T_2)}$	$-\frac{\sqrt{10}}{10}$	$\frac{\sqrt{10}}{10}$	$\frac{\sqrt{10}}{10}$	$-\frac{\sqrt{10}}{10}$	$-\frac{\sqrt{10}}{20}$	$-\frac{\sqrt{10}}{10}$	0	$\frac{\sqrt{10}}{20}$	$-\frac{\sqrt{10}}{10}$	0
	$\frac{\sqrt{10}}{20}$	$-\frac{\sqrt{10}}{20}$	$-\frac{\sqrt{10}}{20}$	$\frac{\sqrt{10}}{20}$	0	0	0	0	$-\frac{\sqrt{10}}{20}$	0
	$\frac{\sqrt{10}}{10}$	$\frac{\sqrt{10}}{20}$	0	$\frac{\sqrt{10}}{10}$						
$\mathbb{Q}_{3,2}^{(T_2)}$	0	0	0	0	0	$-\frac{\sqrt{10}}{20}$	$\frac{\sqrt{10}}{10}$	0	$\frac{\sqrt{10}}{20}$	$-\frac{\sqrt{10}}{10}$
	$-\frac{\sqrt{10}}{10}$	$-\frac{\sqrt{10}}{10}$	$\frac{\sqrt{10}}{10}$	$\frac{\sqrt{10}}{10}$	$\frac{\sqrt{10}}{20}$	$-\frac{\sqrt{10}}{20}$	$\frac{\sqrt{10}}{20}$	$-\frac{\sqrt{10}}{20}$	0	$\frac{\sqrt{10}}{10}$
	$\frac{\sqrt{10}}{20}$	0	$-\frac{\sqrt{10}}{10}$	$-\frac{\sqrt{10}}{20}$						
$\mathbb{Q}_{4,0}^{(E)}$	$\frac{3\sqrt{13}}{52}$	$\frac{3\sqrt{13}}{52}$	$\frac{3\sqrt{13}}{52}$	$\frac{3\sqrt{13}}{52}$	$\frac{3\sqrt{13}}{52}$	$\frac{\sqrt{13}}{52}$	$-\frac{\sqrt{13}}{13}$	$\frac{3\sqrt{13}}{52}$	$\frac{\sqrt{13}}{52}$	$-\frac{\sqrt{13}}{13}$
	$-\frac{\sqrt{13}}{13}$	$-\frac{\sqrt{13}}{13}$	$-\frac{\sqrt{13}}{13}$	$-\frac{\sqrt{13}}{13}$	$\frac{\sqrt{13}}{52}$	$\frac{\sqrt{13}}{52}$	$\frac{\sqrt{13}}{52}$	$\frac{\sqrt{13}}{52}$	$\frac{3\sqrt{13}}{52}$	$-\frac{\sqrt{13}}{13}$
	$\frac{\sqrt{13}}{52}$	$\frac{3\sqrt{13}}{52}$	$-\frac{\sqrt{13}}{13}$	$\frac{\sqrt{13}}{52}$						
$\mathbb{Q}_{4,1}^{(E)}$	$\frac{5\sqrt{39}}{156}$	$\frac{5\sqrt{39}}{156}$	$\frac{5\sqrt{39}}{156}$	$\frac{5\sqrt{39}}{156}$	$-\frac{5\sqrt{39}}{156}$	$\frac{7\sqrt{39}}{156}$	$-\frac{\sqrt{39}}{78}$	$-\frac{5\sqrt{39}}{156}$	$\frac{7\sqrt{39}}{156}$	$-\frac{\sqrt{39}}{78}$

Table 19

Table 19										
symbol	1	2	3	4	5	6	7	8	9	10
	$\frac{\sqrt{39}}{78}$	$\frac{\sqrt{39}}{78}$	$\frac{\sqrt{39}}{78}$	$\frac{\sqrt{39}}{78}$	$-\frac{7\sqrt{39}}{156}$	$-\frac{7\sqrt{39}}{156}$	$-\frac{7\sqrt{39}}{156}$	$-\frac{7\sqrt{39}}{156}$	$-\frac{5\sqrt{39}}{156}$	$-\frac{\sqrt{39}}{78}$
	$\frac{7\sqrt{39}}{156}$	$-\frac{5\sqrt{39}}{156}$	$-\frac{\sqrt{39}}{78}$	$\frac{7\sqrt{39}}{156}$						
$\mathbb{Q}_{4,0}^{(T_1)}$	0	0	0	0	0	$\frac{\sqrt{2}}{4}$	0	0	$-\frac{\sqrt{2}}{4}$	0
	$\frac{\sqrt{2}}{4}$	$-\frac{\sqrt{2}}{4}$	$\frac{\sqrt{2}}{4}$	$-\frac{\sqrt{2}}{4}$	0	0	0	0	0	0
	$\frac{\sqrt{2}}{4}$	0	0	$-\frac{\sqrt{2}}{4}$						
$\mathbb{Q}_{4,1}^{(T_1)}$	0	0	0	0	0	0	$\frac{\sqrt{2}}{4}$	0	0	$-\frac{\sqrt{2}}{4}$
	0	0	0	0	$\frac{\sqrt{2}}{4}$	$\frac{\sqrt{2}}{4}$	$-\frac{\sqrt{2}}{4}$	$-\frac{\sqrt{2}}{4}$	0	$-\frac{\sqrt{2}}{4}$
	0	0	$\frac{\sqrt{2}}{4}$	0						
$\mathbb{Q}_{4,2}^{(T_1)}$	$\frac{\sqrt{2}}{4}$	$\frac{\sqrt{2}}{4}$	$-\frac{\sqrt{2}}{4}$	$-\frac{\sqrt{2}}{4}$	$-\frac{\sqrt{2}}{4}$	0	0	$-\frac{\sqrt{2}}{4}$	0	0
	0	0	0	0	0	0	0	0	$\frac{\sqrt{2}}{4}$	0
	0	$\frac{\sqrt{2}}{4}$	0	0						
$\mathbb{Q}_{5,0}^{(T_2)}$	$\frac{\sqrt{10}}{10}$	$-\frac{\sqrt{10}}{10}$	$\frac{\sqrt{10}}{10}$	$-\frac{\sqrt{10}}{10}$	$-\frac{\sqrt{10}}{20}$	0	$\frac{\sqrt{10}}{10}$	$\frac{\sqrt{10}}{20}$	0	$\frac{\sqrt{10}}{10}$
	0	0	0	0	$\frac{\sqrt{10}}{20}$	$-\frac{\sqrt{10}}{20}$	$-\frac{\sqrt{10}}{20}$	$\frac{\sqrt{10}}{20}$	$\frac{\sqrt{10}}{20}$	$-\frac{\sqrt{10}}{10}$
	0	$-\frac{\sqrt{10}}{20}$	$-\frac{\sqrt{10}}{10}$	0						
$\mathbb{Q}_{5,1}^{(T_2)}$	$\frac{\sqrt{10}}{20}$	$-\frac{\sqrt{10}}{20}$	$-\frac{\sqrt{10}}{20}$	$\frac{\sqrt{10}}{20}$	$-\frac{\sqrt{10}}{10}$	$\frac{\sqrt{10}}{20}$	0	$\frac{\sqrt{10}}{10}$	$\frac{\sqrt{10}}{20}$	0
	$\frac{\sqrt{10}}{10}$	$-\frac{\sqrt{10}}{10}$	$-\frac{\sqrt{10}}{10}$	$\frac{\sqrt{10}}{10}$	0	0	0	0	$-\frac{\sqrt{10}}{10}$	0
	$-\frac{\sqrt{10}}{20}$	$\frac{\sqrt{10}}{10}$	0	$-\frac{\sqrt{10}}{20}$						
$\mathbb{Q}_{5,2}^{(T_2)}$	0	0	0	0	0	$-\frac{\sqrt{10}}{10}$	$-\frac{\sqrt{10}}{20}$	0	$\frac{\sqrt{10}}{10}$	$\frac{\sqrt{10}}{20}$
	$\frac{\sqrt{10}}{20}$	$\frac{\sqrt{10}}{20}$	$-\frac{\sqrt{10}}{20}$	$-\frac{\sqrt{10}}{20}$	$\frac{\sqrt{10}}{10}$	$-\frac{\sqrt{10}}{10}$	$\frac{\sqrt{10}}{10}$	$-\frac{\sqrt{10}}{10}$	0	$-\frac{\sqrt{10}}{20}$
	$\frac{\sqrt{10}}{10}$	0	$\frac{\sqrt{10}}{20}$	$-\frac{\sqrt{10}}{10}$						
$\mathbb{Q}_6^{(A_2)}$	$\frac{\sqrt{6}}{12}$	$\frac{\sqrt{6}}{12}$	$\frac{\sqrt{6}}{12}$	$\frac{\sqrt{6}}{12}$	$-\frac{\sqrt{6}}{12}$	$-\frac{\sqrt{6}}{12}$	$-\frac{\sqrt{6}}{12}$	$-\frac{\sqrt{6}}{12}$	$-\frac{\sqrt{6}}{12}$	$-\frac{\sqrt{6}}{12}$
	$\frac{\sqrt{6}}{12}$	$\frac{\sqrt{6}}{12}$	$\frac{\sqrt{6}}{12}$	$\frac{\sqrt{6}}{12}$	$\frac{\sqrt{6}}{12}$	$\frac{\sqrt{6}}{12}$	$\frac{\sqrt{6}}{12}$	$\frac{\sqrt{6}}{12}$	$-\frac{\sqrt{6}}{12}$	$-\frac{\sqrt{6}}{12}$
	$-\frac{\sqrt{6}}{12}$	$-\frac{\sqrt{6}}{12}$	$-\frac{\sqrt{6}}{12}$	$-\frac{\sqrt{6}}{12}$						