

SG No. 167  $D_{3d}^6$   $R\bar{3}c$  [ trigonal ]

\* plus set:  $+ [0, 0, 0]$ ,  $+ [\frac{2}{3}, \frac{1}{3}, \frac{1}{3}]$ ,  $+ [\frac{1}{3}, \frac{2}{3}, \frac{2}{3}]$

\* Wyckoff site: **6a**, site symmetry: **32**

Table 1: Wyckoff bond: **6a@6a**

| No. | vector       | center                | mapping                    |
|-----|--------------|-----------------------|----------------------------|
| 1   | $[0, 0, Z]$  | $[0, 0, \frac{1}{4}]$ | $[1, 2, 3, -4, -5, -6]$    |
| 2   | $[0, 0, -Z]$ | $[0, 0, \frac{3}{4}]$ | $[7, 8, 9, -10, -11, -12]$ |

Table 2: Wyckoff bond: **18b@6a**

| No. | vector          | center                | mapping    |
|-----|-----------------|-----------------------|------------|
| 1   | $[X, -X, Z]$    | $[0, 0, \frac{1}{4}]$ | $[1, -4]$  |
| 2   | $[X, 2X, Z]$    | $[0, 0, \frac{1}{4}]$ | $[2, -6]$  |
| 3   | $[-2X, -X, Z]$  | $[0, 0, \frac{1}{4}]$ | $[3, -5]$  |
| 4   | $[-X, X, -Z]$   | $[0, 0, \frac{3}{4}]$ | $[7, -10]$ |
| 5   | $[-X, -2X, -Z]$ | $[0, 0, \frac{3}{4}]$ | $[8, -12]$ |
| 6   | $[2X, X, -Z]$   | $[0, 0, \frac{3}{4}]$ | $[9, -11]$ |

Table 3: Wyckoff bond: **18c@6a**

| No. | vector        | center                | mapping   |
|-----|---------------|-----------------------|-----------|
| 1   | $[X, 0, 0]$   | $[0, 0, \frac{1}{4}]$ | $[1, 5]$  |
| 2   | $[0, X, 0]$   | $[0, 0, \frac{1}{4}]$ | $[2, 4]$  |
| 3   | $[-X, -X, 0]$ | $[0, 0, \frac{1}{4}]$ | $[3, 6]$  |
| 4   | $[-X, 0, 0]$  | $[0, 0, \frac{3}{4}]$ | $[7, 11]$ |
| 5   | $[0, -X, 0]$  | $[0, 0, \frac{3}{4}]$ | $[8, 10]$ |
| 6   | $[X, X, 0]$   | $[0, 0, \frac{3}{4}]$ | $[9, 12]$ |

Table 4: Wyckoff bond: **36d@6a**

| No. | vector             | center                | mapping |
|-----|--------------------|-----------------------|---------|
| 1   | $[X, Y, Z]$        | $[0, 0, \frac{1}{4}]$ | $[1]$   |
| 2   | $[-Y, X - Y, Z]$   | $[0, 0, \frac{1}{4}]$ | $[2]$   |
| 3   | $[-X + Y, -X, Z]$  | $[0, 0, \frac{1}{4}]$ | $[3]$   |
| 4   | $[Y, X, -Z]$       | $[0, 0, \frac{1}{4}]$ | $[4]$   |
| 5   | $[X - Y, -Y, -Z]$  | $[0, 0, \frac{1}{4}]$ | $[5]$   |
| 6   | $[-X, -X + Y, -Z]$ | $[0, 0, \frac{1}{4}]$ | $[6]$   |
| 7   | $[-X, -Y, -Z]$     | $[0, 0, \frac{3}{4}]$ | $[7]$   |
| 8   | $[Y, -X + Y, -Z]$  | $[0, 0, \frac{3}{4}]$ | $[8]$   |
| 9   | $[X - Y, X, -Z]$   | $[0, 0, \frac{3}{4}]$ | $[9]$   |

*continued ...*

Table 4

| No. | vector           | center                | mapping |
|-----|------------------|-----------------------|---------|
| 10  | $[-Y, -X, Z]$    | $[0, 0, \frac{3}{4}]$ | [10]    |
| 11  | $[-X + Y, Y, Z]$ | $[0, 0, \frac{3}{4}]$ | [11]    |
| 12  | $[X, X - Y, Z]$  | $[0, 0, \frac{3}{4}]$ | [12]    |

\* Wyckoff site: 6b, site symmetry:  $-3$ .

Table 5: Wyckoff bond: 6a@6b

| No. | vector       | center                | mapping                    |
|-----|--------------|-----------------------|----------------------------|
| 1   | $[0, 0, Z]$  | $[0, 0, 0]$           | $[1, 2, 3, -7, -8, -9]$    |
| 2   | $[0, 0, -Z]$ | $[0, 0, \frac{1}{2}]$ | $[4, 5, 6, -10, -11, -12]$ |

Table 6: Wyckoff bond: 18b@6b

| No. | vector             | center                | mapping  |
|-----|--------------------|-----------------------|----------|
| 1   | $[X, Y, Z]$        | $[0, 0, 0]$           | [1, -7]  |
| 2   | $[-Y, X - Y, Z]$   | $[0, 0, 0]$           | [2, -8]  |
| 3   | $[-X + Y, -X, Z]$  | $[0, 0, 0]$           | [3, -9]  |
| 4   | $[Y, X, -Z]$       | $[0, 0, \frac{1}{2}]$ | [4, -10] |
| 5   | $[X - Y, -Y, -Z]$  | $[0, 0, \frac{1}{2}]$ | [5, -11] |
| 6   | $[-X, -X + Y, -Z]$ | $[0, 0, \frac{1}{2}]$ | [6, -12] |

\* Wyckoff site: 12c, site symmetry:  $3$ .

Table 7: Wyckoff bond: 12a@12c

| No. | vector       | center                    | mapping      |
|-----|--------------|---------------------------|--------------|
| 1   | $[0, 0, Z]$  | $[0, 0, z]$               | [1, 2, 3]    |
| 2   | $[0, 0, -Z]$ | $[0, 0, \frac{1}{2} - z]$ | [4, 5, 6]    |
| 3   | $[0, 0, -Z]$ | $[0, 0, -z]$              | [7, 8, 9]    |
| 4   | $[0, 0, Z]$  | $[0, 0, z + \frac{1}{2}]$ | [10, 11, 12] |

Table 8: Wyckoff bond: 36b@12c

| No. | vector            | center      | mapping |
|-----|-------------------|-------------|---------|
| 1   | $[X, Y, Z]$       | $[0, 0, z]$ | [1]     |
| 2   | $[-Y, X - Y, Z]$  | $[0, 0, z]$ | [2]     |
| 3   | $[-X + Y, -X, Z]$ | $[0, 0, z]$ | [3]     |

*continued ...*

Table 8

| No. | vector             | center                    | mapping |
|-----|--------------------|---------------------------|---------|
| 4   | $[Y, X, -Z]$       | $[0, 0, \frac{1}{2} - z]$ | [4]     |
| 5   | $[X - Y, -Y, -Z]$  | $[0, 0, \frac{1}{2} - z]$ | [5]     |
| 6   | $[-X, -X + Y, -Z]$ | $[0, 0, \frac{1}{2} - z]$ | [6]     |
| 7   | $[-X, -Y, -Z]$     | $[0, 0, -z]$              | [7]     |
| 8   | $[Y, -X + Y, -Z]$  | $[0, 0, -z]$              | [8]     |
| 9   | $[X - Y, X, -Z]$   | $[0, 0, -z]$              | [9]     |
| 10  | $[-Y, -X, Z]$      | $[0, 0, z + \frac{1}{2}]$ | [10]    |
| 11  | $[-X + Y, Y, Z]$   | $[0, 0, z + \frac{1}{2}]$ | [11]    |
| 12  | $[X, X - Y, Z]$    | $[0, 0, z + \frac{1}{2}]$ | [12]    |

\* Wyckoff site: 18d, site symmetry:  $-1$

Table 9: Wyckoff bond: 18a@18d

| No. | vector             | center                                    | mapping |
|-----|--------------------|---|---------|
| 1   | $[X, Y, Z]$        | $[\frac{1}{2}, 0, 0]$                     | [1,-7]  |
| 2   | $[-Y, X - Y, Z]$   | $[0, \frac{1}{2}, 0]$                     | [2,-8]  |
| 3   | $[-X + Y, -X, Z]$  | $[\frac{1}{2}, \frac{1}{2}, 0]$           | [3,-9]  |
| 4   | $[Y, X, -Z]$       | $[0, \frac{1}{2}, \frac{1}{2}]$           | [4,-10] |
| 5   | $[X - Y, -Y, -Z]$  | $[\frac{1}{2}, 0, \frac{1}{2}]$           | [5,-11] |
| 6   | $[-X, -X + Y, -Z]$ | $[\frac{1}{2}, \frac{1}{2}, \frac{1}{2}]$ | [6,-12] |

\* Wyckoff site: 18e, site symmetry:  $.2$

Table 10: Wyckoff bond: 18a@18e

| No. | vector          | center                  | mapping |
|-----|-----------------|-------------------------|---------|
| 1   | $[X, 2X, Z]$    | $[x, 0, \frac{1}{4}]$   | [1,-5]  |
| 2   | $[-2X, -X, Z]$  | $[0, x, \frac{1}{4}]$   | [2,-4]  |
| 3   | $[X, -X, Z]$    | $[-x, -x, \frac{1}{4}]$ | [3,-6]  |
| 4   | $[-X, -2X, -Z]$ | $[-x, 0, \frac{3}{4}]$  | [7,-11] |
| 5   | $[2X, X, -Z]$   | $[0, -x, \frac{3}{4}]$  | [8,-10] |
| 6   | $[-X, X, -Z]$   | $[x, x, \frac{3}{4}]$   | [9,-12] |

Table 11: Wyckoff bond: 18b@18e

| No. | vector        | center                  | mapping |
|-----|---------------|-------------------------|---------|
| 1   | $[X, 0, 0]$   | $[x, 0, \frac{1}{4}]$   | [1,5]   |
| 2   | $[0, X, 0]$   | $[0, x, \frac{1}{4}]$   | [2,4]   |
| 3   | $[-X, -X, 0]$ | $[-x, -x, \frac{1}{4}]$ | [3,6]   |
| 4   | $[-X, 0, 0]$  | $[-x, 0, \frac{3}{4}]$  | [7,11]  |

*continued ...*

Table 11

| No. | vector       | center                 | mapping   |
|-----|--------------|------------------------|-----------|
| 5   | $[0, -X, 0]$ | $[0, -x, \frac{3}{4}]$ | $[8, 10]$ |
| 6   | $[X, X, 0]$  | $[x, x, \frac{3}{4}]$  | $[9, 12]$ |

Table 12: Wyckoff bond: **36c@18e**

| No. | vector             | center                  | mapping |
|-----|--------------------|-------------------------|---------|
| 1   | $[X, Y, Z]$        | $[x, 0, \frac{1}{4}]$   | $[1]$   |
| 2   | $[-Y, X - Y, Z]$   | $[0, x, \frac{1}{4}]$   | $[2]$   |
| 3   | $[-X + Y, -X, Z]$  | $[-x, -x, \frac{1}{4}]$ | $[3]$   |
| 4   | $[Y, X, -Z]$       | $[0, x, \frac{1}{4}]$   | $[4]$   |
| 5   | $[X - Y, -Y, -Z]$  | $[x, 0, \frac{1}{4}]$   | $[5]$   |
| 6   | $[-X, -X + Y, -Z]$ | $[-x, -x, \frac{1}{4}]$ | $[6]$   |
| 7   | $[-X, -Y, -Z]$     | $[-x, 0, \frac{3}{4}]$  | $[7]$   |
| 8   | $[Y, -X + Y, -Z]$  | $[0, -x, \frac{3}{4}]$  | $[8]$   |
| 9   | $[X - Y, X, -Z]$   | $[x, x, \frac{3}{4}]$   | $[9]$   |
| 10  | $[-Y, -X, Z]$      | $[0, -x, \frac{3}{4}]$  | $[10]$  |
| 11  | $[-X + Y, Y, Z]$   | $[-x, 0, \frac{3}{4}]$  | $[11]$  |
| 12  | $[X, X - Y, Z]$    | $[x, x, \frac{3}{4}]$   | $[12]$  |

\* Wyckoff site: **36f**, site symmetry: **1**

Table 13: Wyckoff bond: **36a@36f**

| No. | vector             | center                          | mapping |
|-----|--------------------|---------------------------------|---------|
| 1   | $[X, Y, Z]$        | $[x, y, z]$                     | $[1]$   |
| 2   | $[-Y, X - Y, Z]$   | $[-y, x - y, z]$                | $[2]$   |
| 3   | $[-X + Y, -X, Z]$  | $[-x + y, -x, z]$               | $[3]$   |
| 4   | $[Y, X, -Z]$       | $[y, x, \frac{1}{2} - z]$       | $[4]$   |
| 5   | $[X - Y, -Y, -Z]$  | $[x - y, -y, \frac{1}{2} - z]$  | $[5]$   |
| 6   | $[-X, -X + Y, -Z]$ | $[-x, -x + y, \frac{1}{2} - z]$ | $[6]$   |
| 7   | $[-X, -Y, -Z]$     | $[-x, -y, -z]$                  | $[7]$   |
| 8   | $[Y, -X + Y, -Z]$  | $[y, -x + y, -z]$               | $[8]$   |
| 9   | $[X - Y, X, -Z]$   | $[x - y, x, -z]$                | $[9]$   |
| 10  | $[-Y, -X, Z]$      | $[-y, -x, z + \frac{1}{2}]$     | $[10]$  |
| 11  | $[-X + Y, Y, Z]$   | $[-x + y, y, z + \frac{1}{2}]$  | $[11]$  |
| 12  | $[X, X - Y, Z]$    | $[x, x - y, z + \frac{1}{2}]$   | $[12]$  |