

\* symmetry operation

Table 1: Symmetry operations for 3d polar vector.

No.	tag	matrix (polar)	det	TR
1	{1 0}	$\begin{bmatrix} 1 & 0 & 0 & 0 \\ 0 & 1 & 0 & 0 \\ 0 & 0 & 1 & 0 \end{bmatrix}$	1	1
2	{3 <sup>+</sup> <sub>001</sub>  00 <sub>3</sub> <sup>2</sup> }	$\begin{bmatrix} 0 & -1 & 0 & 0 \\ 1 & -1 & 0 & 0 \\ 0 & 0 & 1 & \frac{2}{3} \end{bmatrix}$	1	1
3	{3 <sup>-</sup> <sub>001</sub>  00 <sub>3</sub> <sup>1</sup> }	$\begin{bmatrix} -1 & 1 & 0 & 0 \\ -1 & 0 & 0 & 0 \\ 0 & 0 & 1 & \frac{1}{3} \end{bmatrix}$	1	1
4	{2 <sub>100</sub>  0}	$\begin{bmatrix} 1 & -1 & 0 & 0 \\ 0 & -1 & 0 & 0 \\ 0 & 0 & -1 & 0 \end{bmatrix}$	1	1
5	{2 <sub>110</sub>  00 <sub>3</sub> <sup>2</sup> }	$\begin{bmatrix} 0 & 1 & 0 & 0 \\ 1 & 0 & 0 & 0 \\ 0 & 0 & -1 & \frac{2}{3} \end{bmatrix}$	1	1
6	{2 <sub>010</sub>  00 <sub>3</sub> <sup>1</sup> }	$\begin{bmatrix} -1 & 0 & 0 & 0 \\ -1 & 1 & 0 & 0 \\ 0 & 0 & -1 & \frac{1}{3} \end{bmatrix}$	1	1
7	{6 <sup>+</sup> <sub>001</sub> ' 00 <sub>3</sub> <sup>1</sup> }	$\begin{bmatrix} 1 & -1 & 0 & 0 \\ 1 & 0 & 0 & 0 \\ 0 & 0 & 1 & \frac{1}{3} \end{bmatrix}$	1	-1
8	{2 <sub>001</sub> ' 0}	$\begin{bmatrix} -1 & 0 & 0 & 0 \\ 0 & -1 & 0 & 0 \\ 0 & 0 & 1 & 0 \end{bmatrix}$	1	-1
9	{6 <sup>-</sup> <sub>001</sub> ' 00 <sub>3</sub> <sup>2</sup> }	$\begin{bmatrix} 0 & 1 & 0 & 0 \\ -1 & 1 & 0 & 0 \\ 0 & 0 & 1 & \frac{2}{3} \end{bmatrix}$	1	-1
10	{2 <sub>210</sub> ' 00 <sub>3</sub> <sup>1</sup> }	$\begin{bmatrix} 1 & 0 & 0 & 0 \\ 1 & -1 & 0 & 0 \\ 0 & 0 & -1 & \frac{1}{3} \end{bmatrix}$	1	-1
11	{2 <sub>120</sub> ' 0}	$\begin{bmatrix} -1 & 1 & 0 & 0 \\ 0 & 1 & 0 & 0 \\ 0 & 0 & -1 & 0 \end{bmatrix}$	1	-1
12	{2 <sub>1-10</sub> ' 00 <sub>3</sub> <sup>2</sup> }	$\begin{bmatrix} 0 & -1 & 0 & 0 \\ -1 & 0 & 0 & 0 \\ 0 & 0 & -1 & \frac{2}{3} \end{bmatrix}$	1	-1