## No. 18 $D_3$ 312 (312 setting) [trigonal] (axial)

表 1 rank 0

No.	irrep.	(tag)	mul.	comp.	harmonics	(tag)	definition
1	$A_1$	A1	_	_	$\mathbb{G}_0^{(h,A_1)}$	${\tt Gh}({\tt O},{\tt A1},,)$	$C_0$

表 2 rank 1

No.	irrep.	(tag)	mul.	comp.	harmonics	(tag)	definition
2	$A_2$	A2	-	_	$\mathbb{G}_1^{(h,A_2)}$	${\tt Gh(1,A2,,)}$	$C_0$
3	E	E	_	0	$\mathbb{G}_{1,0}^{(h,E)}$	${\tt Gh(1,E,,0)}$	$-S_1$
4	E	E	_	1	$\mathbb{G}_{1,1}^{(h,E)}$	${\tt Gh(1,E,,1)}$	$C_1$

表 3 rank 2

No.	irrep.	(tag)	mul.	comp.	harmonics	(tag)	definition
5	$A_1$	A1	_	_	$\mathbb{G}_2^{(h,A_1)}$	${\tt Gh(2,A1,,)}$	$C_0$
6	E	E	1	0	$\mathbb{G}_{2,0}^{(h,E,1)}$	${\tt Gh(2,E,1,0)}$	$C_1$
7	E	E	1	1	$\mathbb{G}_{2,1}^{(h,E,1)}$	${\tt Gh(2,E,1,1)}$	$S_1$
8	E	E	2	0	$\mathbb{G}_{2,0}^{(h,E,2)}$	${\tt Gh(2,E,2,0)}$	$C_2$
9	E	E	2	1	$\mathbb{G}_{2,1}^{(h,E,2)}$	${\tt Gh(2,E,2,1)}$	$-S_2$

表 4 rank 3

No.	irrep.	(tag)	mul.	comp.	harmonics	(tag)	definition
10	$A_1$	A1	_	_	$\mathbb{G}_3^{(h,A_1)}$	${\tt Gh(3,A1,,)}$	$S_3$
11	$A_2$	A2	1	_	$\mathbb{G}_3^{(h,A_2,1)}$	${\tt Gh(3,A2,1,)}$	$C_0$
12	$A_2$	A2	2	_	$\mathbb{G}_3^{(h,A_2,2)}$	${\tt Gh(3,A2,2,)}$	$C_3$
13	E	E	1	0	$\mathbb{G}_{3,0}^{(h,E,1)}$	${\tt Gh(3,E,1,0)}$	$-S_1$
14	E	E	1	1	$\mathbb{G}_{3,1}^{(h,E,1)}$	${\tt Gh(3,E,1,1)}$	$C_1$
15	E	E	2	0	$\mathbb{G}_{3,0}^{(h,E,2)}$	${\tt Gh(3,E,2,0)}$	$S_2$
16	E	E	2	1	$\mathbb{G}_{3,1}^{(h,E,2)}$	${\tt Gh(3,E,2,1)}$	$C_2$

表 5 rank 4

No.	irrep.	(tag)	mul.	comp.	harmonics	(tag)	definition
17	$A_1$	A1	1	_	$\mathbb{G}_4^{(h,A_1,1)}$	${\tt Gh(4,A1,1,)}$	$C_0$
18	$A_1$	A1	2	_	$\mathbb{G}_4^{(h,A_1,2)}$	${\tt Gh(4,A1,2,)}$	$C_3$
19	$A_2$	A2	_	-	$\mathbb{G}_4^{(h,A_2)}$	${\tt Gh(4,A2,,)}$	$S_3$
20	E	E	1	0	$\mathbb{G}_{4,0}^{(h,E,1)}$	${\tt Gh(4,E,1,0)}$	$C_1$
21	E	E	1	1	$\mathbb{G}_{4,1}^{(h,E,1)}$	${\tt Gh(4,E,1,1)}$	$S_1$
22	E	E	2	0	$\mathbb{G}_{4,0}^{(h,E,2)}$	${\tt Gh(4,E,2,0)}$	$C_4$
23	E	E	2	1	$\mathbb{G}_{4,1}^{(h,E,2)}$	${\tt Gh(4,E,2,1)}$	$S_4$
24	E	E	3	0	$\mathbb{G}_{4,0}^{(h,E,3)}$	${\tt Gh(4,E,3,0)}$	$C_2$
25	E	E	3	1	$\mathbb{G}_{4,1}^{(h,E,3)}$	${\tt Gh(4,E,3,1)}$	$-S_2$

表 6 rank 5

No.	irrep.	(tag)	mul.	comp.	harmonics	(tag)	definition
26	$A_1$	A1	_	_	$\mathbb{G}_5^{(h,A_1)}$	${\tt Gh(5,A1,,)}$	$S_3$
27	$A_2$	A2	1	_	$\mathbb{G}_{5}^{(h,A_{2},1)}$	${\tt Gh(5,A2,1,)}$	$C_0$
28	$A_2$	A2	2	_	$\mathbb{G}_{5}^{(h,A_{2},2)}$	${\tt Gh(5,A2,2,)}$	$C_3$
29	E	E	1	0	$\mathbb{G}_{5,0}^{(h,E,1)}$	${\tt Gh(5,E,1,0)}$	$S_5$
30	E	E	1	1	$\mathbb{G}_{5,1}^{(h,E,1)}$	${\tt Gh(5,E,1,1)}$	$C_5$
31	E	E	2	0	$\mathbb{G}_{5,0}^{(h,E,2)}$	${\tt Gh(5,E,2,0)}$	$-S_1$
32	E	E	2	1	$\mathbb{G}_{5,1}^{(h,E,2)}$	${\tt Gh(5,E,2,1)}$	$C_1$
33	E	E	3	0	$\mathbb{G}_{5,0}^{(h,E,3)}$	${\tt Gh(5,E,3,0)}$	$-S_4$
34	E	E	3	1	$\mathbb{G}_{5,1}^{(h,E,3)}$	${\tt Gh(5,E,3,1)}$	$C_4$
35	E	E	4	0	$\mathbb{G}_{5,0}^{(h,E,4)}$	${\tt Gh(5,E,4,0)}$	$S_2$
36	E	E	4	1	$\mathbb{G}_{5,1}^{(h,E,4)}$	${\tt Gh(5,E,4,1)}$	$C_2$

表 7 rank 6

No.	irrep.	(tag)	mul.	comp.	harmonics	(tag)	definition
37	$A_1$	A1	1	_	$\mathbb{G}_6^{(h,A_1,1)}$	Gh(6, A1, 1,)	$C_0$
38	$A_1$	A1	2	-	$\mathbb{G}_6^{(h,A_1,2)}$	${\tt Gh(6,A1,2,)}$	$C_6$
39	$A_1$	A1	3	-	$\mathbb{G}_6^{(h,A_1,3)}$	${\tt Gh(6,A1,3,)}$	$C_3$
40	$A_2$	A2	1	_	$\mathbb{G}_6^{(h,A_2,1)}$	${\tt Gh(6,A2,1,)}$	$S_6$
41	$A_2$	A2	2	_	$\mathbb{G}_6^{(h,A_2,2)}$	${\tt Gh(6,A2,2,)}$	$S_3$
42	E	E	1	0	$\mathbb{G}_{6,0}^{(h,E,1)}$	${\tt Gh}({\tt 6},{\tt E},{\tt 1},{\tt 0})$	$C_5$
43	E	E	1	1	$\mathbb{G}_{6,1}^{(h,E,1)}$	${\tt Gh}({\tt 6},{\tt E},{\tt 1},{\tt 1})$	$-S_5$
44	E	E	2	0	$\mathbb{G}_{6,0}^{(h,E,2)}$	${\tt Gh}({\tt 6},{\tt E},{\tt 2},{\tt 0})$	$C_1$
45	E	E	2	1	$\mathbb{G}_{6,1}^{(h,E,2)}$	${\tt Gh}({\tt 6},{\tt E},2,1)$	$S_1$
46	E	E	3	0	$\mathbb{G}_{6,0}^{(h,E,3)}$	${\tt Gh}(6,{\tt E},3,0)$	$C_4$
47	E	E	3	1	$\mathbb{G}_{6,1}^{(h,E,3)}$	${\tt Gh}(6,{\tt E},3,1)$	$S_4$
48	E	E	4	0	$\mathbb{G}_{6,0}^{(h,E,4)}$	${\tt Gh(6,E,4,0)}$	$C_2$
49	E	E	4	1	$\mathbb{G}_{6,1}^{(h,E,4)}$	${\tt Gh(6,E,4,1)}$	$-S_2$

表 8 rank 7

No.	irrep.	(tag)	mul.	comp.	harmonics	(tag)	definition
50	$A_1$	A1	1	_	$\mathbb{G}_7^{(h,A_1,1)}$	Gh(7, A1, 1,)	$S_6$
51	$A_1$	A1	2	-	$\mathbb{G}_7^{(h,A_1,2)}$	${\tt Gh(7,A1,2,)}$	$S_3$
52	$A_2$	A2	1	_	$\mathbb{G}_7^{(h,A_2,1)}$	${\tt Gh(7,A2,1,)}$	$C_0$
53	$A_2$	A2	2	_	$\mathbb{G}_7^{(h,A_2,2)}$	${\tt Gh(7,A2,2,)}$	$C_6$
54	$A_2$	A2	3	_	$\mathbb{G}_7^{(h,A_2,3)}$	${\tt Gh(7,A2,3,)}$	$C_3$
55	E	E	1	0	$\mathbb{G}_{7,0}^{(h,E,1)}$	${\tt Gh(7,E,1,0)}$	$-S_7$
56	E	E	1	1	$\mathbb{G}_{7,1}^{(h,E,1)}$	${\tt Gh(7,E,1,1)}$	$C_7$
57	E	E	2	0	$\mathbb{G}_{7,0}^{(h,E,2)}$	${\tt Gh(7,E,2,0)}$	$S_5$
58	E	E	2	1	$\mathbb{G}_{7,1}^{(h,E,2)}$	${\tt Gh(7,E,2,1)}$	$C_5$
59	E	E	3	0	$\mathbb{G}_{7,0}^{(h,E,3)}$	${\tt Gh(7,E,3,0)}$	$-S_1$
60	E	E	3	1	$\mathbb{G}_{7,1}^{(h,E,3)}$	${\tt Gh(7,E,3,1)}$	$C_1$
61	E	E	4	0	$\mathbb{G}_{7,0}^{(h,E,4)}$	${\tt Gh(7,E,4,0)}$	$-S_4$
62	E	E	4	1	$\mathbb{G}_{7,1}^{(h,E,4)}$	${\tt Gh(7,E,4,1)}$	$C_4$
63	E	E	5	0	$\mathbb{G}_{7,0}^{(h,E,5)}$	${\tt Gh(7,E,5,0)}$	$S_2$
64	E	E	5	1	$\mathbb{G}_{7,1}^{(h,E,5)}$	${\tt Gh(7,E,5,1)}$	$C_2$

表 9 rank 8

No.	irrep.	(tag)	mul.	comp.	harmonics	(tag)	definition
65	$A_1$	A1	1	-	$\mathbb{G}_8^{(h,A_1,1)}$	${\tt Gh(8,A1,1,)}$	$C_0$
66	$A_1$	A1	2	_	$\mathbb{G}_8^{(h,A_1,2)}$	${\tt Gh(8,A1,2,)}$	$C_6$
67	$A_1$	A1	3	_	$\mathbb{G}_8^{(h,A_1,3)}$	${\tt Gh(8,A1,3,)}$	$C_3$
68	$A_2$	A2	1	_	$\mathbb{G}_8^{(h,A_2,1)}$	${\tt Gh(8,A2,1,)}$	$S_6$
69	$A_2$	A2	2	_	$\mathbb{G}_8^{(h,A_2,2)}$	${\tt Gh(8,A2,2,)}$	$S_3$
70	E	E	1	0	$\mathbb{G}_{8,0}^{(h,E,1)}$	${\tt Gh(8,E,1,0)}$	$C_7$
71	E	E	1	1	$\mathbb{G}_{8,1}^{(h,E,1)}$	${\tt Gh(8,E,1,1)}$	$S_7$
72	E	E	2	0	$\mathbb{G}_{8,0}^{(h,E,2)}$	${\tt Gh(8,E,2,0)}$	$C_5$
73	E	E	2	1	$\mathbb{G}_{8,1}^{(h,E,2)}$	${\tt Gh(8,E,2,1)}$	$-S_5$
74	E	E	3	0	$\mathbb{G}_{8,0}^{(h,E,3)}$	${\tt Gh(8,E,3,0)}$	$C_1$
75	E	E	3	1	$\mathbb{G}_{8,1}^{(h,E,3)}$	${\tt Gh(8,E,3,1)}$	$S_1$
76	E	E	4	0	$\mathbb{G}_{8,0}^{(h,E,4)}$	${\tt Gh(8,E,4,0)}$	$C_8$
77	E	E	4	1	$\mathbb{G}_{8,1}^{(h,E,4)}$	${\tt Gh(8,E,4,1)}$	$-S_8$
78	E	E	5	0	$\mathbb{G}_{8,0}^{(h,E,5)}$	${\tt Gh(8,E,5,0)}$	$C_4$
79	E	E	5	1	$\mathbb{G}_{8,1}^{(h,E,5)}$	${\tt Gh(8,E,5,1)}$	$S_4$
80	E	E	6	0	$\mathbb{G}_{8,0}^{(h,E,6)}$	${\tt Gh(8,E,6,0)}$	$C_2$
81	E	E	6	1	$\mathbb{G}_{8,1}^{(h,E,6)}$	${\tt Gh(8,E,6,1)}$	$-S_2$

表 10 rank 9

No.	irrep.	(tag)	mul.	comp.	harmonics	(tag)	definition
82	$A_1$	A1	1	_	$\mathbb{G}_9^{(h,A_1,1)}$	Gh(9, A1, 1,)	$S_6$
83	$A_1$	A1	2	_	$\mathbb{G}_9^{(h,A_1,2)}$	${\tt Gh(9,A1,2,)}$	$S_9$
84	$A_1$	A1	3	_	$\mathbb{G}_9^{(h,A_1,3)}$	${\tt Gh(9,A1,3,)}$	$S_3$
85	$A_2$	A2	1	_	$\mathbb{G}_9^{(h,A_2,1)}$	${\tt Gh(9,A2,1,)}$	$C_0$
86	$A_2$	A2	2	_	$\mathbb{G}_9^{(h,A_2,2)}$	${\tt Gh(9,A2,2,)}$	$C_6$
87	$A_2$	A2	3	_	$\mathbb{G}_9^{(h,A_2,3)}$	${\tt Gh(9,A2,3,)}$	$C_9$
88	$A_2$	A2	4	_	$\mathbb{G}_9^{(h,A_2,4)}$	${\tt Gh(9,A2,4,)}$	$C_3$
89	E	E	1	0	$\mathbb{G}_{9,0}^{(h,E,1)}$	${\tt Gh(9,E,1,0)}$	$-S_7$
90	E	E	1	1	$\mathbb{G}_{9,1}^{(h,E,1)}$	${\tt Gh(9,E,1,1)}$	$C_7$
91	E	E	2	0	$\mathbb{G}_{9,0}^{(h,E,2)}$	${\tt Gh(9,E,2,0)}$	$S_5$
92	E	E	2	1	$\mathbb{G}_{9,1}^{(h,E,2)}$	${\tt Gh(9,E,2,1)}$	$C_5$
93	E	E	3	0	$\mathbb{G}_{9,0}^{(h,E,3)}$	${\tt Gh(9,E,3,0)}$	$-S_1$
94	E	E	3	1	$\mathbb{G}_{9,1}^{(h,E,3)}$	${\tt Gh(9,E,3,1)}$	$C_1$
95	E	E	4	0	$\mathbb{G}_{9,0}^{(h,E,4)}$	${\tt Gh(9,E,4,0)}$	$S_8$
96	E	E	4	1	$\mathbb{G}_{9,1}^{(h,E,4)}$	${\tt Gh(9,E,4,1)}$	$C_8$
97	E	E	5	0	$\mathbb{G}_{9,0}^{(h,E,5)}$	${\tt Gh(9,E,5,0)}$	$-S_4$
98	E	E	5	1	$\mathbb{G}_{9,1}^{(h,E,5)}$	${\tt Gh(9,E,5,1)}$	$C_4$
99	E	E	6	0	$\mathbb{G}_{9,0}^{(h,E,6)}$	${\tt Gh(9,E,6,0)}$	$S_2$
100	E	E	6	1	$\mathbb{G}_{9,1}^{(h,E,6)}$	${\tt Gh(9,E,6,1)}$	$C_2$

表 11 rank 10

No.	irrep.	(tag)	mul.	comp.	harmonics	(tag)	definition
101	$A_1$	A1	1	_	$\mathbb{G}_{10}^{(h,A_1,1)}$	Gh(10, A1, 1,)	$C_0$
102	$A_1$	A1	2	_	$\mathbb{G}_{10}^{(h,A_1,2)}$	${\tt Gh(10,A1,2,)}$	$C_6$
103	$A_1$	A1	3	-	$\mathbb{G}_{10}^{(h,A_1,3)}$	${\tt Gh(10,A1,3,)}$	$C_9$
104	$A_1$	A1	4	_	$\mathbb{G}_{10}^{(h,A_1,4)}$	${\tt Gh(10,A1,4,)}$	$C_3$
105	$A_2$	A2	1	-	$\mathbb{G}_{10}^{(h,A_2,1)}$	${\tt Gh(10,A2,1,)}$	$S_6$
106	$A_2$	A2	2	_	$\mathbb{G}_{10}^{(h,A_2,2)}$	${\tt Gh(10,A2,2,)}$	$S_9$
107	$A_2$	A2	3	_	$\mathbb{G}_{10}^{(h,A_2,3)}$	${\tt Gh(10,A2,3,)}$	$S_3$
108	E	E	1	0	$\mathbb{G}_{10,0}^{(h,E,1)}$	${\tt Gh(10,E,1,0)}$	$C_7$
109	E	E	1	1	$\mathbb{G}_{10,1}^{(h,E,1)}$	${\tt Gh(10,E,1,1)}$	$S_7$
110	E	E	2	0	$\mathbb{G}_{10,0}^{(h,E,2)}$	${\tt Gh(10,E,2,0)}$	$C_5$
111	E	E	2	1	$\mathbb{G}_{10,1}^{(h,E,2)}$	${\tt Gh(10,E,2,1)}$	$-S_5$
112	E	E	3	0	$\mathbb{G}_{10,0}^{(h,E,3)}$	${\tt Gh(10,E,3,0)}$	$C_1$
113	E	E	3	1	$\mathbb{G}_{10,1}^{(h,E,3)}$	${\tt Gh(10,E,3,1)}$	$S_1$
114	E	E	4	0	$\mathbb{G}_{10,0}^{(h,E,4)}$	${\tt Gh(10,E,4,0)}$	$C_{10}$
115	E	E	4	1	$\mathbb{G}_{10,1}^{(h,E,4)}$	${\tt Gh(10,E,4,1)}$	$S_{10}$
116	E	E	5	0	$\mathbb{G}_{10,0}^{(h,E,5)}$	${\tt Gh(10,E,5,0)}$	$C_8$
117	E	E	5	1	$\mathbb{G}_{10,1}^{(h,E,5)}$	${\tt Gh(10,E,5,1)}$	$-S_8$
118	E	E	6	0	$\mathbb{G}_{10,0}^{(h,E,6)}$	${\tt Gh(10,E,6,0)}$	$C_4$
119	E	E	6	1	$\mathbb{G}_{10,1}^{(h,E,6)}$	${\tt Gh(10,E,6,1)}$	$S_4$
120	E	E	7	0	$\mathbb{G}_{10,0}^{(h,E,7)}$	${\tt Gh(10,E,7,0)}$	$C_2$
121	E	E	7	1	$\mathbb{G}_{10,1}^{(h,E,7)}$	Gh(10, E, 7, 1)	$-S_2$

表 12 rank 11

No.	irrep.	(tag)	mul.	comp.	harmonics	(tag)	definition
122	$A_1$	A1	1	_	$\mathbb{G}_{11}^{(h,A_1,1)}$	${\tt Gh(11,A1,1,)}$	$S_6$
123	$A_1$	A1	2	_	$\mathbb{G}_{11}^{(h,A_1,2)}$	${\tt Gh(11,A1,2,)}$	$S_9$
124	$A_1$	A1	3	_	$\mathbb{G}_{11}^{(h,A_1,3)}$	${\tt Gh(11,A1,3,)}$	$S_3$
125	$A_2$	A2	1	_	$\mathbb{G}_{11}^{(h,A_2,1)}$	${\tt Gh(11,A2,1,)}$	$C_0$
126	$A_2$	A2	2	_	$\mathbb{G}_{11}^{(h,A_2,2)}$	${\tt Gh(11,A2,2,)}$	$C_6$
127	$A_2$	A2	3	_	$\mathbb{G}_{11}^{(h,A_2,3)}$	${\tt Gh(11,A2,3,)}$	$C_9$
128	$A_2$	A2	4	_	$\mathbb{G}_{11}^{(h,A_2,4)}$	${\tt Gh(11,A2,4,)}$	$C_3$
129	E	E	1	0	$\mathbb{G}_{11,0}^{(h,E,1)}$	${\tt Gh(11,E,1,0)}$	$S_{11}$
130	E	E	1	1	$\mathbb{G}_{11,1}^{(h,E,1)}$	${\tt Gh(11,E,1,1)}$	$C_{11}$
131	E	E	2	0	$\mathbb{G}_{11,0}^{(h,E,2)}$	${\tt Gh(11,E,2,0)}$	$-S_7$
132	E	E	2	1	$\mathbb{G}_{11,1}^{(h,E,2)}$	${\tt Gh(11,E,2,1)}$	$C_7$
133	E	E	3	0	$\mathbb{G}_{11,0}^{(h,E,3)}$	${\tt Gh(11,E,3,0)}$	$S_5$
134	E	E	3	1	$\mathbb{G}_{11,1}^{(h,E,3)}$	${\tt Gh(11,E,3,1)}$	$C_5$
135	E	E	4	0	$\mathbb{G}_{11,0}^{(h,E,4)}$	${\tt Gh(11,E,4,0)}$	$-S_1$
136	E	E	4	1	$\mathbb{G}_{11,1}^{(h,E,4)}$	${\tt Gh(11,E,4,1)}$	$C_1$
137	E	E	5	0	$\mathbb{G}_{11,0}^{(h,E,5)}$	${\tt Gh(11,E,5,0)}$	$-S_{10}$
138	E	E	5	1	$\mathbb{G}_{11,1}^{(h,E,5)}$	${\tt Gh(11,E,5,1)}$	$C_{10}$
139	E	E	6	0	$\mathbb{G}_{11,0}^{(h,E,6)}$	${\tt Gh(11,E,6,0)}$	$S_8$
140	E	E	6	1	$\mathbb{G}_{11,1}^{(h,E,6)}$	${\tt Gh(11,E,6,1)}$	$C_8$
141	E	E	7	0	$\mathbb{G}_{11,0}^{(h,E,7)}$	${\tt Gh(11,E,7,0)}$	$-S_4$
142	E	E	7	1	$\mathbb{G}_{11,1}^{(h,E,7)}$	${\tt Gh(11,E,7,1)}$	$C_4$
143	E	E	8	0	$\mathbb{G}_{11,0}^{(h,E,8)}$	${\tt Gh(11,E,8,0)}$	$S_2$
144	E	E	8	1	$\mathbb{G}_{11,1}^{(h,E,8)}$	${\tt Gh}({\tt 11},{\tt E},{\tt 8},{\tt 1})$	$C_2$