

Table 1 Harmonics for rank 0.

No.	multipole	expression
1	$\mathbb{G}_0(A_u)$	1

Table 2 Harmonics for rank 1.

No.	multipole	expression
2	$\mathbb{G}_1(A_g)$	z
3	$\mathbb{G}_{1,1}(E_{1g}^{(a)})$	$\frac{\sqrt{2}(x+iy)}{2}$
4	$\mathbb{G}_{1,1}(E_{1g}^{(b)})$	$\frac{\sqrt{2}(x-iy)}{2}$

Table 3 Harmonics for rank 2.

No.	multipole	expression
5	$\mathbb{G}_2(A_u)$	$-\frac{x^2}{2} - \frac{y^2}{2} + z^2$
6	$\mathbb{G}_{2,1}(E_{1u}^{(a)})$	$\frac{\sqrt{2}(\sqrt{3}xz + \sqrt{3}iyz)}{2}$
7	$\mathbb{G}_{2,1}(E_{1u}^{(b)})$	$\frac{\sqrt{2}(\sqrt{3}xz - \sqrt{3}iyz)}{2}$
8	$\mathbb{G}_{2,1}(E_{2u}^{(a)})$	$\frac{\sqrt{2}\left(-\sqrt{3}ixy + \frac{\sqrt{3}(x-y)(x+y)}{2}\right)}{2}$
9	$\mathbb{G}_{2,1}(E_{2u}^{(b)})$	$\frac{\sqrt{2}\left(\sqrt{3}ixy + \frac{\sqrt{3}(x-y)(x+y)}{2}\right)}{2}$

Table 4 Harmonics for rank 3.

No.	multipole	expression
10	$\mathbb{G}_3(A_g)$	$-\frac{z(3x^2+3y^2-2z^2)}{2}$
11	$\mathbb{G}_3(B_g, 1)$	$\frac{\sqrt{10}y(3x^2-y^2)}{4}$
12	$\mathbb{G}_3(B_g, 2)$	$\frac{\sqrt{10}x(x^2-3y^2)}{4}$
13	$\mathbb{G}_{3,1}(E_{1g}^{(a)})$	$\frac{\sqrt{2}\left(-\frac{\sqrt{6}x(x^2+y^2-4z^2)}{4} - \frac{\sqrt{6}iy(x^2+y^2-4z^2)}{4}\right)}{2}$
14	$\mathbb{G}_{3,1}(E_{1g}^{(b)})$	$\frac{\sqrt{2}\left(-\frac{\sqrt{6}x(x^2+y^2-4z^2)}{4} + \frac{\sqrt{6}iy(x^2+y^2-4z^2)}{4}\right)}{2}$
15	$\mathbb{G}_{3,1}(E_{2g}^{(a)})$	$\frac{\sqrt{2}\left(-\sqrt{15}ixyz + \frac{\sqrt{15}z(x-y)(x+y)}{2}\right)}{2}$
16	$\mathbb{G}_{3,1}(E_{2g}^{(b)})$	$\frac{\sqrt{2}\left(\sqrt{15}ixyz + \frac{\sqrt{15}z(x-y)(x+y)}{2}\right)}{2}$

Table 5 Harmonics for rank 4.

No.	multipole	expression
17	$\mathbb{G}_4(A_u)$	$\frac{3x^4}{8} + \frac{3x^2y^2}{4} - 3x^2z^2 + \frac{3y^4}{8} - 3y^2z^2 + z^4$
18	$\mathbb{G}_4(B_u, 1)$	$\frac{\sqrt{70}xz(x^2-3y^2)}{4}$
19	$\mathbb{G}_4(B_u, 2)$	$\frac{\sqrt{70}yz(3x^2-y^2)}{4}$
20	$\mathbb{G}_{4,1}(E_{1u}^{(a)})$	$\frac{\sqrt{2}\left(-\frac{\sqrt{10}xz(3x^2+3y^2-4z^2)}{4} - \frac{\sqrt{10}yz(3x^2+3y^2-4z^2)}{4}\right)}{2}$
21	$\mathbb{G}_{4,1}(E_{1u}^{(b)})$	$\frac{\sqrt{2}\left(-\frac{\sqrt{10}xz(3x^2+3y^2-4z^2)}{4} + \frac{\sqrt{10}yz(3x^2+3y^2-4z^2)}{4}\right)}{2}$
22	$\mathbb{G}_{4,1}(E_{2u}^{(a)}, 1)$	$\frac{\sqrt{2}\left(\frac{\sqrt{35}xyz(x-y)(x+y)}{2} + \frac{\sqrt{35}(x^2-2xy-y^2)(x^2+2xy-y^2)}{8}\right)}{2}$
23	$\mathbb{G}_{4,1}(E_{2u}^{(a)}, 2)$	$\frac{\sqrt{2}\left(\frac{\sqrt{5}xy(x^2+y^2-6z^2)}{2} - \frac{\sqrt{5}(x-y)(x+y)(x^2+y^2-6z^2)}{4}\right)}{2}$
24	$\mathbb{G}_{4,1}(E_{2u}^{(b)}, 1)$	$\frac{\sqrt{2}\left(-\frac{\sqrt{35}xyz(x-y)(x+y)}{2} + \frac{\sqrt{35}(x^2-2xy-y^2)(x^2+2xy-y^2)}{8}\right)}{2}$
25	$\mathbb{G}_{4,1}(E_{2u}^{(b)}, 2)$	$\frac{\sqrt{2}\left(-\frac{\sqrt{5}xy(x^2+y^2-6z^2)}{2} - \frac{\sqrt{5}(x-y)(x+y)(x^2+y^2-6z^2)}{4}\right)}{2}$

Table 6 Harmonics for rank 5.

No.	multipole	expression
26	$\mathbb{G}_5(A_g)$	$\frac{z(15x^4+30x^2y^2-40x^2z^2+15y^4-40y^2z^2+8z^4)}{8}$
27	$\mathbb{G}_5(B_g, 1)$	$-\frac{\sqrt{70}y(3x^2-y^2)(x^2+y^2-8z^2)}{16}$
28	$\mathbb{G}_5(B_g, 2)$	$-\frac{\sqrt{70}x(x^2-3y^2)(x^2+y^2-8z^2)}{16}$
29	$\mathbb{G}_{5,1}(E_{1g}^{(a)}, 1)$	$\frac{\sqrt{2}\left(\frac{3\sqrt{14}x(x^4-10x^2y^2+5y^4)}{16} - \frac{3\sqrt{14}y(5x^4-10x^2y^2+y^4)}{16}\right)}{2}$
30	$\mathbb{G}_{5,1}(E_{1g}^{(a)}, 2)$	$\frac{\sqrt{2}\left(\frac{\sqrt{15}x(x^4+2x^2y^2-12x^2z^2+y^4-12y^2z^2+8z^4)}{8} + \frac{\sqrt{15}y(x^4+2x^2y^2-12x^2z^2+y^4-12y^2z^2+8z^4)}{8}\right)}{2}$
31	$\mathbb{G}_{5,1}(E_{1g}^{(b)}, 1)$	$\frac{\sqrt{2}\left(\frac{3\sqrt{14}x(x^4-10x^2y^2+5y^4)}{16} + \frac{3\sqrt{14}y(5x^4-10x^2y^2+y^4)}{16}\right)}{2}$
32	$\mathbb{G}_{5,1}(E_{1g}^{(b)}, 2)$	$\frac{\sqrt{2}\left(\frac{\sqrt{15}x(x^4+2x^2y^2-12x^2z^2+y^4-12y^2z^2+8z^4)}{8} - \frac{\sqrt{15}y(x^4+2x^2y^2-12x^2z^2+y^4-12y^2z^2+8z^4)}{8}\right)}{2}$
33	$\mathbb{G}_{5,1}(E_{2g}^{(a)}, 1)$	$\frac{\sqrt{2}\left(\frac{3\sqrt{35}xyz(x-y)(x+y)}{2} + \frac{3\sqrt{35}z(x^2-2xy-y^2)(x^2+2xy-y^2)}{8}\right)}{2}$
34	$\mathbb{G}_{5,1}(E_{2g}^{(a)}, 2)$	$\frac{\sqrt{2}\left(\frac{\sqrt{105}xyz(x^2+y^2-2z^2)}{2} - \frac{\sqrt{105}z(x-y)(x+y)(x^2+y^2-2z^2)}{4}\right)}{2}$
35	$\mathbb{G}_{5,1}(E_{2g}^{(b)}, 1)$	$\frac{\sqrt{2}\left(-\frac{3\sqrt{35}xyz(x-y)(x+y)}{2} + \frac{3\sqrt{35}z(x^2-2xy-y^2)(x^2+2xy-y^2)}{8}\right)}{2}$
36	$\mathbb{G}_{5,1}(E_{2g}^{(b)}, 2)$	$\frac{\sqrt{2}\left(-\frac{\sqrt{105}xyz(x^2+y^2-2z^2)}{2} - \frac{\sqrt{105}z(x-y)(x+y)(x^2+y^2-2z^2)}{4}\right)}{2}$

Table 7 Harmonics for rank 6.

No.	multipole	expression
37	$\mathbb{G}_6(A_u, 1)$	$-\frac{5x^6}{16} - \frac{15x^4y^2}{16} + \frac{45x^4z^2}{8} - \frac{15x^2y^4}{16} + \frac{45x^2y^2z^2}{4} - \frac{15x^2z^4}{2} - \frac{5y^6}{16} + \frac{45y^4z^2}{8} - \frac{15y^2z^4}{2} + z^6$
38	$\mathbb{G}_6(A_u, 2)$	$\frac{\sqrt{462}(x-y)(x+y)(x^2-4xy+y^2)(x^2+4xy+y^2)}{32}$
39	$\mathbb{G}_6(A_u, 3)$	$\frac{\sqrt{462}xy(x^2-3y^2)(3x^2-y^2)}{16}$
40	$\mathbb{G}_6(B_u, 1)$	$-\frac{\sqrt{210}xz(x^2-3y^2)(3x^2+3y^2-8z^2)}{16}$
41	$\mathbb{G}_6(B_u, 2)$	$-\frac{\sqrt{210}yz(3x^2-y^2)(3x^2+3y^2-8z^2)}{16}$
42	$\mathbb{G}_{6,1}(E_{1u}^{(a)}, 1)$	$\frac{\sqrt{2}\left(\frac{3\sqrt{154}xz(x^4-10x^2y^2+5y^4)}{16} - \frac{3\sqrt{154}yz(5x^4-10x^2y^2+y^4)}{16}\right)}{2}$
43	$\mathbb{G}_{6,1}(E_{1u}^{(a)}, 2)$	$\frac{\sqrt{2}\left(\frac{\sqrt{21}xz(5x^4+10x^2y^2-20x^2z^2+5y^4-20y^2z^2+8z^4)}{8} + \frac{\sqrt{21}yz(5x^4+10x^2y^2-20x^2z^2+5y^4-20y^2z^2+8z^4)}{8}\right)}{2}$
44	$\mathbb{G}_{6,1}(E_{1u}^{(b)}, 1)$	$\frac{\sqrt{2}\left(\frac{3\sqrt{154}xz(x^4-10x^2y^2+5y^4)}{16} + \frac{3\sqrt{154}yz(5x^4-10x^2y^2+y^4)}{16}\right)}{2}$
45	$\mathbb{G}_{6,1}(E_{1u}^{(b)}, 2)$	$\frac{\sqrt{2}\left(\frac{\sqrt{21}xz(5x^4+10x^2y^2-20x^2z^2+5y^4-20y^2z^2+8z^4)}{8} - \frac{\sqrt{21}yz(5x^4+10x^2y^2-20x^2z^2+5y^4-20y^2z^2+8z^4)}{8}\right)}{2}$
46	$\mathbb{G}_{6,1}(E_{2u}^{(a)}, 1)$	$\frac{\sqrt{2}\left(-\frac{3\sqrt{7}ixy(x-y)(x+y)(x^2+y^2-10z^2)}{4} - \frac{3\sqrt{7}(x^2+y^2-10z^2)(x^2-2xy-y^2)(x^2+2xy-y^2)}{16}\right)}{2}$
47	$\mathbb{G}_{6,1}(E_{2u}^{(a)}, 2)$	$\frac{\sqrt{2}\left(-\frac{\sqrt{210}ixy(x^4+2x^2y^2-16x^2z^2+y^4-16y^2z^2+16z^4)}{16} + \frac{\sqrt{210}(x-y)(x+y)(x^4+2x^2y^2-16x^2z^2+y^4-16y^2z^2+16z^4)}{32}\right)}{2}$
48	$\mathbb{G}_{6,1}(E_{2u}^{(b)}, 1)$	$\frac{\sqrt{2}\left(\frac{3\sqrt{7}ixy(x-y)(x+y)(x^2+y^2-10z^2)}{4} - \frac{3\sqrt{7}(x^2+y^2-10z^2)(x^2-2xy-y^2)(x^2+2xy-y^2)}{16}\right)}{2}$
49	$\mathbb{G}_{6,1}(E_{2u}^{(b)}, 2)$	$\frac{\sqrt{2}\left(\frac{\sqrt{210}ixy(x^4+2x^2y^2-16x^2z^2+y^4-16y^2z^2+16z^4)}{16} + \frac{\sqrt{210}(x-y)(x+y)(x^4+2x^2y^2-16x^2z^2+y^4-16y^2z^2+16z^4)}{32}\right)}{2}$

Table 8 Harmonics for rank 7.

No.	multipole	expression
50	$\mathbb{G}_7(A_g, 1)$	$\frac{\sqrt{6006}xyz(x^2-3y^2)(3x^2-y^2)}{16}$
51	$\mathbb{G}_7(A_g, 2)$	$-\frac{z(35x^6+105x^4y^2-210x^4z^2+105x^2y^4-420x^2y^2z^2+168x^2z^4+35y^6-210y^4z^2+168y^2z^4-16z^6)}{16}$
52	$\mathbb{G}_7(A_g, 3)$	$\frac{\sqrt{6006}z(x-y)(x+y)(x^2-4xy+y^2)(x^2+4xy+y^2)}{32}$
53	$\mathbb{G}_7(B_g, 1)$	$\frac{\sqrt{21}y(3x^2-y^2)(3x^4+6x^2y^2-60x^2z^2+3y^4-60y^2z^2+80z^4)}{32}$
54	$\mathbb{G}_7(B_g, 2)$	$\frac{\sqrt{21}x(x^2-3y^2)(3x^4+6x^2y^2-60x^2z^2+3y^4-60y^2z^2+80z^4)}{32}$
55	$\mathbb{G}_{7,1}(E_{1g}^{(a)}, 1)$	$\frac{\sqrt{2}\left(\frac{\sqrt{429}x(x^6-21x^4y^2+35x^2y^4-7y^6)}{32} + \frac{\sqrt{429}iy(7x^6-35x^4y^2+21x^2y^4-y^6)}{32}\right)}{2}$
56	$\mathbb{G}_{7,1}(E_{1g}^{(a)}, 2)$	$\frac{\sqrt{2}\left(-\frac{\sqrt{231}x(x^2+y^2-12z^2)(x^4-10x^2y^2+5y^4)}{32} + \frac{\sqrt{231}iy(x^2+y^2-12z^2)(5x^4-10x^2y^2+y^4)}{32}\right)}{2}$
57	$\mathbb{G}_{7,1}(E_{1g}^{(a)}, 3)$	$\frac{\sqrt{2}\left(-\frac{\sqrt{7}x(5x^6+15x^4y^2-120x^4z^2+15x^2y^4-240x^2y^2z^2+240x^2z^4+5y^6-120y^4z^2+240y^2z^4-64z^6)}{32} - \frac{\sqrt{7}iy(5x^6+15x^4y^2-120x^4z^2+15x^2y^4-240x^2y^2z^2+240x^2z^4+5y^6-120y^4z^2+240y^2z^4-64z^6)}{32}\right)}{2}$
58	$\mathbb{G}_{7,1}(E_{1g}^{(b)}, 1)$	$\frac{\sqrt{2}\left(\frac{\sqrt{429}x(x^6-21x^4y^2+35x^2y^4-7y^6)}{32} - \frac{\sqrt{429}iy(7x^6-35x^4y^2+21x^2y^4-y^6)}{32}\right)}{2}$
59	$\mathbb{G}_{7,1}(E_{1g}^{(b)}, 2)$	$\frac{\sqrt{2}\left(-\frac{\sqrt{231}x(x^2+y^2-12z^2)(x^4-10x^2y^2+5y^4)}{32} - \frac{\sqrt{231}iy(x^2+y^2-12z^2)(5x^4-10x^2y^2+y^4)}{32}\right)}{2}$
60	$\mathbb{G}_{7,1}(E_{1g}^{(b)}, 3)$	$\frac{\sqrt{2}\left(-\frac{\sqrt{7}x(5x^6+15x^4y^2-120x^4z^2+15x^2y^4-240x^2y^2z^2+240x^2z^4+5y^6-120y^4z^2+240y^2z^4-64z^6)}{32} + \frac{\sqrt{7}iy(5x^6+15x^4y^2-120x^4z^2+15x^2y^4-240x^2y^2z^2+240x^2z^4+5y^6-120y^4z^2+240y^2z^4-64z^6)}{32}\right)}{2}$
61	$\mathbb{G}_{7,1}(E_{2g}^{(a)}, 1)$	$\frac{\sqrt{2}\left(-\frac{\sqrt{231}ixyz(x-y)(x+y)(3x^2+3y^2-10z^2)}{4} - \frac{\sqrt{231}z(x^2-2xy-y^2)(x^2+2xy-y^2)(3x^2+3y^2-10z^2)}{16}\right)}{2}$
62	$\mathbb{G}_{7,1}(E_{2g}^{(a)}, 2)$	$\frac{\sqrt{2}\left(-\frac{\sqrt{42}ixyz(15x^4+30x^2y^2-80x^2z^2+15y^4-80y^2z^2+48z^4)}{16} + \frac{\sqrt{42}z(x-y)(x+y)(15x^4+30x^2y^2-80x^2z^2+15y^4-80y^2z^2+48z^4)}{32}\right)}{2}$
63	$\mathbb{G}_{7,1}(E_{2g}^{(b)}, 1)$	$\frac{\sqrt{2}\left(\frac{\sqrt{231}ixyz(x-y)(x+y)(3x^2+3y^2-10z^2)}{4} - \frac{\sqrt{231}z(x^2-2xy-y^2)(x^2+2xy-y^2)(3x^2+3y^2-10z^2)}{16}\right)}{2}$
64	$\mathbb{G}_{7,1}(E_{2g}^{(b)}, 2)$	$\frac{\sqrt{2}\left(\frac{\sqrt{42}ixyz(15x^4+30x^2y^2-80x^2z^2+15y^4-80y^2z^2+48z^4)}{16} + \frac{\sqrt{42}z(x-y)(x+y)(15x^4+30x^2y^2-80x^2z^2+15y^4-80y^2z^2+48z^4)}{32}\right)}{2}$

Table 9 Harmonics for rank 8.

No.	multipole	expression
65	$\mathbb{G}_8(A_u, 1)$	$\frac{35x^8}{128} + \frac{35x^6y^2}{32} - \frac{35x^6z^2}{4} + \frac{105x^4y^4}{64} - \frac{105x^4y^2z^2}{4} + \frac{105x^4z^4}{4} + \frac{35x^2y^6}{32} - \frac{105x^2y^4z^2}{4} + \frac{105x^2y^2z^4}{2} - 14x^2z^6 + \frac{35y^8}{128} - \frac{35y^6z^2}{4} + \frac{105y^4z^4}{4} - 14y^2z^6 + z^8$
66	$\mathbb{G}_8(A_u, 2)$	$-\frac{\sqrt{858}(x-y)(x+y)(x^2+y^2-14z^2)(x^2-4xy+y^2)(x^2+4xy+y^2)}{64}$
67	$\mathbb{G}_8(A_u, 3)$	$-\frac{\sqrt{858}xy(x^2-3y^2)(3x^2-y^2)(x^2+y^2-14z^2)}{32}$
68	$\mathbb{G}_8(B_u, 1)$	$\frac{\sqrt{1155}xz(x^2-3y^2)(3x^4+6x^2y^2-20x^2z^2+3y^4-20y^2z^2+16z^4)}{32}$
69	$\mathbb{G}_8(B_u, 2)$	$\frac{\sqrt{1155}yz(3x^2-y^2)(3x^4+6x^2y^2-20x^2z^2+3y^4-20y^2z^2+16z^4)}{32}$
70	$\mathbb{G}_{8,1}(E_{1u}^{(a)}, 1)$	$\sqrt{2} \left(\frac{3\sqrt{715}xz(x^6-21x^4y^2+35x^2y^4-7y^6)}{32} + \frac{3\sqrt{715}yz(7x^6-35x^4y^2+21x^2y^4-y^6)}{32} \right)$
71	$\mathbb{G}_{8,1}(E_{1u}^{(a)}, 2)$	$\sqrt{2} \left(-\frac{3\sqrt{1001}xz(x^2+y^2-4z^2)(x^4-10x^2y^2+5y^4)}{32} + \frac{3\sqrt{1001}yz(x^2+y^2-4z^2)(5x^4-10x^2y^2+y^4)}{32} \right)$
72	$\mathbb{G}_{8,1}(E_{1u}^{(a)}, 3)$	$\sqrt{2} \left(-\frac{3xz(35x^6+105x^4y^2-280x^4z^2+105x^2y^4-560x^2y^2z^2+336x^2z^4+35y^6-280y^4z^2+336y^2z^4-64z^6)}{32} - \frac{3yz(35x^6+105x^4y^2-280x^4z^2+105x^2y^4-560x^2y^2z^2+336x^2z^4+35y^6-280y^4z^2+336y^2z^4-64z^6)}{32} \right)$
73	$\mathbb{G}_{8,1}(E_{1u}^{(b)}, 1)$	$\sqrt{2} \left(\frac{3\sqrt{715}xz(x^6-21x^4y^2+35x^2y^4-7y^6)}{32} - \frac{3\sqrt{715}yz(7x^6-35x^4y^2+21x^2y^4-y^6)}{32} \right)$
74	$\mathbb{G}_{8,1}(E_{1u}^{(b)}, 2)$	$\sqrt{2} \left(-\frac{3\sqrt{1001}xz(x^2+y^2-4z^2)(x^4-10x^2y^2+5y^4)}{32} - \frac{3\sqrt{1001}yz(x^2+y^2-4z^2)(5x^4-10x^2y^2+y^4)}{32} \right)$
75	$\mathbb{G}_{8,1}(E_{1u}^{(b)}, 3)$	$\sqrt{2} \left(-\frac{3xz(35x^6+105x^4y^2-280x^4z^2+105x^2y^4-560x^2y^2z^2+336x^2z^4+35y^6-280y^4z^2+336y^2z^4-64z^6)}{32} + \frac{3yz(35x^6+105x^4y^2-280x^4z^2+105x^2y^4-560x^2y^2z^2+336x^2z^4+35y^6-280y^4z^2+336y^2z^4-64z^6)}{32} \right)$
76	$\mathbb{G}_{8,1}(E_{2u}^{(a)}, 1)$	$\sqrt{2} \left(-\frac{3\sqrt{715}xyz(x-y)(x+y)(x^2-2xy-y^2)(x^2+2xy-y^2)}{16} + \frac{3\sqrt{715}(x^4-4x^3y-6x^2y^2+4xy^3+y^4)(x^4+4x^3y-6x^2y^2-4xy^3+y^4)}{128} \right)$
77	$\mathbb{G}_{8,1}(E_{2u}^{(a)}, 2)$	$\sqrt{2} \left(\frac{3\sqrt{77}xyz(x-y)(x+y)(x^4+2x^2y^2-24x^2z^2+y^4-24y^2z^2+40z^4)}{16} + \frac{3\sqrt{77}(x^2-2xy-y^2)(x^2+2xy-y^2)(x^4+2x^2y^2-24x^2z^2+y^4-24y^2z^2+40z^4)}{64} \right)$
78	$\mathbb{G}_{8,1}(E_{2u}^{(a)}, 3)$	$\sqrt{2} \left(\frac{3\sqrt{70}xyz(x^6+3x^4y^2-30x^4z^2+3x^2y^4-60x^2y^2z^2+80x^2z^4+y^6-30y^4z^2+80y^2z^4-32z^6)}{32} - \frac{3\sqrt{70}(x-y)(x+y)(x^6+3x^4y^2-30x^4z^2+3x^2y^4-60x^2y^2z^2+80x^2z^4+y^6-30y^4z^2+80y^2z^4-32z^6)}{64} \right)$
79	$\mathbb{G}_{8,1}(E_{2u}^{(b)}, 1)$	$\sqrt{2} \left(\frac{3\sqrt{715}xyz(x-y)(x+y)(x^2-2xy-y^2)(x^2+2xy-y^2)}{16} + \frac{3\sqrt{715}(x^4-4x^3y-6x^2y^2+4xy^3+y^4)(x^4+4x^3y-6x^2y^2-4xy^3+y^4)}{128} \right)$
80	$\mathbb{G}_{8,1}(E_{2u}^{(b)}, 2)$	$\sqrt{2} \left(-\frac{3\sqrt{77}xyz(x-y)(x+y)(x^4+2x^2y^2-24x^2z^2+y^4-24y^2z^2+40z^4)}{16} + \frac{3\sqrt{77}(x^2-2xy-y^2)(x^2+2xy-y^2)(x^4+2x^2y^2-24x^2z^2+y^4-24y^2z^2+40z^4)}{64} \right)$
81	$\mathbb{G}_{8,1}(E_{2u}^{(b)}, 3)$	$\sqrt{2} \left(-\frac{3\sqrt{70}xyz(x^6+3x^4y^2-30x^4z^2+3x^2y^4-60x^2y^2z^2+80x^2z^4+y^6-30y^4z^2+80y^2z^4-32z^6)}{32} - \frac{3\sqrt{70}(x-y)(x+y)(x^6+3x^4y^2-30x^4z^2+3x^2y^4-60x^2y^2z^2+80x^2z^4+y^6-30y^4z^2+80y^2z^4-32z^6)}{64} \right)$

Table 10 Harmonics for rank 9.

No.	multipole	expression
82	$\mathbb{G}_9(A_g, 1)$	$-\frac{\sqrt{4290}xyz(x^2-3y^2)(3x^2-y^2)(3x^2+3y^2-14z^2)}{32}$
83	$\mathbb{G}_9(A_g, 2)$	$\frac{z(315x^8+1260x^6y^2-3360x^6z^2+1890x^4y^4-10080x^4y^2z^2+6048x^4z^4+1260x^2y^6-10080x^2y^4z^2+12096x^2y^2z^4-2304x^2z^6+315y^8-3360y^6z^2+6048y^4z^4-2304y^2z^6+128z^8)}{128}$
84	$\mathbb{G}_9(A_g, 3)$	$-\frac{\sqrt{4290}z(x-y)(x+y)(x^2-4xy+y^2)(x^2+4xy+y^2)(3x^2+3y^2-14z^2)}{64}$
85	$\mathbb{G}_9(B_g, 1)$	$\frac{\sqrt{24310}y(3x^2-y^2)(3x^6-27x^4y^2+33x^2y^4-y^6)}{256}$
86	$\mathbb{G}_9(B_g, 2)$	$-\frac{\sqrt{2310}y(3x^2-y^2)(x^6+3x^4y^2-36x^4z^2+3x^2y^4-72x^2y^2z^2+120x^2z^4+y^6-36y^4z^2+120y^2z^4-64z^6)}{128}$
87	$\mathbb{G}_9(B_g, 3)$	$\frac{\sqrt{24310}x(x^2-3y^2)(x^6-33x^4y^2+27x^2y^4-3y^6)}{256}$
88	$\mathbb{G}_9(B_g, 4)$	$-\frac{\sqrt{2310}x(x^2-3y^2)(x^6+3x^4y^2-36x^4z^2+3x^2y^4-72x^2y^2z^2+120x^2z^4+y^6-36y^4z^2+120y^2z^4-64z^6)}{128}$
89	$\mathbb{G}_{9,1}(E_{1g}^{(a)}, 1)$	$\sqrt{2}\left(-\frac{3\sqrt{1430}x(x^2+y^2-16z^2)(x^6-21x^4y^2+35x^2y^4-7y^6)}{256}-\frac{3\sqrt{1430}iy(x^2+y^2-16z^2)(7x^6-35x^4y^2+21x^2y^4-y^6)}{256}\right)$
90	$\mathbb{G}_{9,1}(E_{1g}^{(a)}, 2)$	$\sqrt{2}\left(\frac{3\sqrt{286}x(x^4-10x^2y^2+5y^4)(x^4+2x^2y^2-28x^2z^2+y^4-28y^2z^2+56z^4)}{128}-\frac{3\sqrt{286}iy(5x^4-10x^2y^2+y^4)(x^4+2x^2y^2-28x^2z^2+y^4-28y^2z^2+56z^4)}{128}\right)$
91	$\mathbb{G}_{9,1}(E_{1g}^{(a)}, 3)$	$\sqrt{2}\left(\frac{3\sqrt{5}x(7x^8+28x^6y^2-280x^6z^2+42x^4y^4-840x^4y^2z^2+1120x^4z^4+28x^2y^6-840x^2y^4z^2+2240x^2y^2z^4-896x^2z^6+7y^8-280y^6z^2+1120y^4z^4-896y^2z^6+128z^8)}{128}+\frac{3\sqrt{5}iy(7x^8+28x^6y^2-280x^6z^2+42x^4y^4-840x^4y^2z^2+1120x^4z^4+28x^2y^6-840x^2y^4z^2+2240x^2y^2z^4-896x^2z^6+7y^8-280y^6z^2+1120y^4z^4-896y^2z^6+128z^8)}{128}\right)$
92	$\mathbb{G}_{9,1}(E_{1g}^{(b)}, 1)$	$\sqrt{2}\left(-\frac{3\sqrt{1430}x(x^2+y^2-16z^2)(x^6-21x^4y^2+35x^2y^4-7y^6)}{256}+\frac{3\sqrt{1430}iy(x^2+y^2-16z^2)(7x^6-35x^4y^2+21x^2y^4-y^6)}{256}\right)$
93	$\mathbb{G}_{9,1}(E_{1g}^{(b)}, 2)$	$\sqrt{2}\left(\frac{3\sqrt{286}x(x^4-10x^2y^2+5y^4)(x^4+2x^2y^2-28x^2z^2+y^4-28y^2z^2+56z^4)}{128}+\frac{3\sqrt{286}iy(5x^4-10x^2y^2+y^4)(x^4+2x^2y^2-28x^2z^2+y^4-28y^2z^2+56z^4)}{128}\right)$
94	$\mathbb{G}_{9,1}(E_{1g}^{(b)}, 3)$	$\sqrt{2}\left(\frac{3\sqrt{5}x(7x^8+28x^6y^2-280x^6z^2+42x^4y^4-840x^4y^2z^2+1120x^4z^4+28x^2y^6-840x^2y^4z^2+2240x^2y^2z^4-896x^2z^6+7y^8-280y^6z^2+1120y^4z^4-896y^2z^6+128z^8)}{128}-\frac{3\sqrt{5}iy(7x^8+28x^6y^2-280x^6z^2+42x^4y^4-840x^4y^2z^2+1120x^4z^4+28x^2y^6-840x^2y^4z^2+2240x^2y^2z^4-896x^2z^6+7y^8-280y^6z^2+1120y^4z^4-896y^2z^6+128z^8)}{128}\right)$
95	$\mathbb{G}_{9,1}(E_{2g}^{(a)}, 1)$	$\sqrt{2}\left(-\frac{3\sqrt{12155}ixyz(x-y)(x+y)(x^2-2xy-y^2)(x^2+2xy-y^2)}{16}+\frac{3\sqrt{12155}z(x^4-4x^3y-6x^2y^2+4xy^3+y^4)(x^4+4x^3y-6x^2y^2-4xy^3+y^4)}{128}\right)$
96	$\mathbb{G}_{9,1}(E_{2g}^{(a)}, 2)$	$\sqrt{2}\left(\frac{3\sqrt{5005}ixyz(x-y)(x+y)(x^4+2x^2y^2-8x^2z^2+y^4-8y^2z^2+8z^4)}{16}+\frac{3\sqrt{5005}z(x^2-2xy-y^2)(x^2+2xy-y^2)(x^4+2x^2y^2-8x^2z^2+y^4-8y^2z^2+8z^4)}{64}\right)$
97	$\mathbb{G}_{9,1}(E_{2g}^{(a)}, 3)$	$\sqrt{2}\left(\frac{3\sqrt{110}ixyz(7x^6+21x^4y^2-70x^4z^2+21x^2y^4-140x^2y^2z^2+112x^2z^4+7y^6-70y^4z^2+112y^2z^4-32z^6)}{32}-\frac{3\sqrt{110}z(x-y)(x+y)(7x^6+21x^4y^2-70x^4z^2+21x^2y^4-140x^2y^2z^2+112x^2z^4+7y^6-70y^4z^2+112y^2z^4-32z^6)}{64}\right)$
98	$\mathbb{G}_{9,1}(E_{2g}^{(b)}, 1)$	$\sqrt{2}\left(\frac{3\sqrt{12155}ixyz(x-y)(x+y)(x^2-2xy-y^2)(x^2+2xy-y^2)}{16}+\frac{3\sqrt{12155}z(x^4-4x^3y-6x^2y^2+4xy^3+y^4)(x^4+4x^3y-6x^2y^2-4xy^3+y^4)}{128}\right)$
99	$\mathbb{G}_{9,1}(E_{2g}^{(b)}, 2)$	$\sqrt{2}\left(-\frac{3\sqrt{5005}ixyz(x-y)(x+y)(x^4+2x^2y^2-8x^2z^2+y^4-8y^2z^2+8z^4)}{16}+\frac{3\sqrt{5005}z(x^2-2xy-y^2)(x^2+2xy-y^2)(x^4+2x^2y^2-8x^2z^2+y^4-8y^2z^2+8z^4)}{64}\right)$
100	$\mathbb{G}_{9,1}(E_{2g}^{(b)}, 3)$	$\sqrt{2}\left(-\frac{3\sqrt{110}ixyz(7x^6+21x^4y^2-70x^4z^2+21x^2y^4-140x^2y^2z^2+112x^2z^4+7y^6-70y^4z^2+112y^2z^4-32z^6)}{32}-\frac{3\sqrt{110}z(x-y)(x+y)(7x^6+21x^4y^2-70x^4z^2+21x^2y^4-140x^2y^2z^2+112x^2z^4+7y^6-70y^4z^2+112y^2z^4-32z^6)}{64}\right)$

Table 11 Harmonics for rank 10.

No.	multipole	expression
101	$\mathbb{G}_{10}(A_u, 1)$	$-\frac{63x^{10}}{256} - \frac{315x^8y^2}{256} + \frac{1575x^8z^2}{128} - \frac{315x^6y^4}{128} + \frac{1575x^6y^2z^2}{32} - \frac{525x^6z^4}{8} - \frac{315x^4y^6}{128} + \frac{4725x^4y^4z^2}{64} - \frac{1575x^4y^2z^4}{8} + \frac{315x^4z^6}{4} - \frac{315x^2y^8}{256} + \frac{1575x^2y^6z^2}{32} - \frac{1575x^2y^4z^4}{8} + \frac{315x^2y^2z^6}{2} - \frac{45x^2z^8}{2} - \frac{63y^{10}}{256} + \frac{1575y^8z^2}{128} - \frac{525y^6z^4}{8} + \frac{315y^4z^6}{4} - \frac{45y^2z^8}{2} + z^{10}$
102	$\mathbb{G}_{10}(A_u, 2)$	$\frac{\sqrt{4290}(x-y)(x+y)(x^2-4xy+y^2)(x^2+4xy+y^2)(3x^4+6x^2y^2-96x^2z^2+3y^4-96y^2z^2+224z^4)}{512}$
103	$\mathbb{G}_{10}(A_u, 3)$	$\frac{\sqrt{4290}xy(x^2-3y^2)(3x^2-y^2)(3x^4+6x^2y^2-96x^2z^2+3y^4-96y^2z^2+224z^4)}{256}$
104	$\mathbb{G}_{10}(B_u, 1)$	$\frac{\sqrt{461890}xz(x^2-3y^2)(x^6-33x^4y^2+27x^2y^4-3y^6)}{256}$
105	$\mathbb{G}_{10}(B_u, 2)$	$-\frac{\sqrt{4290}xz(x^2-3y^2)(7x^6+21x^4y^2-84x^4z^2+21x^2y^4-168x^2y^2z^2+168x^2z^4+7y^6-84y^4z^2+168y^2z^4-64z^6)}{128}$
106	$\mathbb{G}_{10}(B_u, 3)$	$\frac{\sqrt{461890}yz(3x^2-y^2)(3x^6-27x^4y^2+33x^2y^4-y^6)}{256}$
107	$\mathbb{G}_{10}(B_u, 4)$	$-\frac{\sqrt{4290}yz(3x^2-y^2)(7x^6+21x^4y^2-84x^4z^2+21x^2y^4-168x^2y^2z^2+168x^2z^4+7y^6-84y^4z^2+168y^2z^4-64z^6)}{256}$
108	$\mathbb{G}_{10,1}(E_{1u}^{(a)}, 1)$	$\sqrt{2}\left(-\frac{\sqrt{72930}xz(3x^2+3y^2-16z^2)(x^6-21x^4y^2+35x^2y^4-7y^6)}{256} - \frac{\sqrt{72930}iyz(3x^2+3y^2-16z^2)(7x^6-35x^4y^2+21x^2y^4-y^6)}{256}\right)$
109	$\mathbb{G}_{10,1}(E_{1u}^{(a)}, 2)$	$\sqrt{2}\left(\frac{2}{128}\left(\frac{\sqrt{858}xz(x^4-10x^2y^2+5y^4)(15x^4+30x^2y^2-140x^2z^2+15y^4-140y^2z^2+168z^4)}{128} - \frac{\sqrt{858}iyz(5x^4-10x^2y^2+y^4)(15x^4+30x^2y^2-140x^2z^2+15y^4-140y^2z^2+168z^4)}{128}\right)\right)$
110	$\mathbb{G}_{10,1}(E_{1u}^{(a)}, 3)$	$\sqrt{2}\left(\frac{2}{128}\left(\frac{\sqrt{55}xz(63x^8+252x^6y^2-840x^6z^2+378x^4y^4-2520x^4y^2z^2+2016x^4z^4+252x^2y^6-2520x^2y^4z^2+4032x^2y^2z^4-1152x^2z^6+63y^8-840y^6z^2+2016y^4z^4-1152y^2z^6+128z^8)}{128} + \frac{\sqrt{55}iyz(63x^8+252x^6y^2-840x^6z^2+378x^4y^4-2520x^4y^2z^2+2016x^4z^4+252x^2y^6-2520x^2y^4z^2+4032x^2y^2z^4-1152x^2z^6+63y^8-840y^6z^2+2016y^4z^4-1152y^2z^6+128z^8)}{128}\right)\right)$
111	$\mathbb{G}_{10,1}(E_{1u}^{(b)}, 1)$	$\sqrt{2}\left(-\frac{\sqrt{72930}xz(3x^2+3y^2-16z^2)(x^6-21x^4y^2+35x^2y^4-7y^6)}{256} + \frac{\sqrt{72930}iyz(3x^2+3y^2-16z^2)(7x^6-35x^4y^2+21x^2y^4-y^6)}{256}\right)$
112	$\mathbb{G}_{10,1}(E_{1u}^{(b)}, 2)$	$\sqrt{2}\left(\frac{2}{128}\left(\frac{\sqrt{858}xz(x^4-10x^2y^2+5y^4)(15x^4+30x^2y^2-140x^2z^2+15y^4-140y^2z^2+168z^4)}{128} + \frac{\sqrt{858}iyz(5x^4-10x^2y^2+y^4)(15x^4+30x^2y^2-140x^2z^2+15y^4-140y^2z^2+168z^4)}{128}\right)\right)$
113	$\mathbb{G}_{10,1}(E_{1u}^{(b)}, 3)$	$\sqrt{2}\left(\frac{2}{128}\left(\frac{\sqrt{55}xz(63x^8+252x^6y^2-840x^6z^2+378x^4y^4-2520x^4y^2z^2+2016x^4z^4+252x^2y^6-2520x^2y^4z^2+4032x^2y^2z^4-1152x^2z^6+63y^8-840y^6z^2+2016y^4z^4-1152y^2z^6+128z^8)}{128} - \frac{\sqrt{55}iyz(63x^8+252x^6y^2-840x^6z^2+378x^4y^4-2520x^4y^2z^2+2016x^4z^4+252x^2y^6-2520x^2y^4z^2+4032x^2y^2z^4-1152x^2z^6+63y^8-840y^6z^2+2016y^4z^4-1152y^2z^6+128z^8)}{128}\right)\right)$
114	$\mathbb{G}_{10,1}(E_{2u}^{(a)}, 1)$	$\sqrt{2}\left(\frac{2}{256}\left(\frac{\sqrt{92378}ixy(x^4-10x^2y^2+5y^4)(5x^4-10x^2y^2+y^4)}{256} + \frac{\sqrt{92378}(x-y)(x+y)(x^4-4x^3y-14x^2y^2-4xy^3+y^4)(x^4+4x^3y-14x^2y^2+4xy^3+y^4)}{512}\right)\right)$
115	$\mathbb{G}_{10,1}(E_{2u}^{(a)}, 2)$	$\sqrt{2}\left(\frac{2}{32}\left(\frac{\sqrt{12155}ixy(x-y)(x+y)(x^2+y^2-18z^2)(x^2-2xy-y^2)(x^2+2xy-y^2)}{32} - \frac{\sqrt{12155}(x^2+y^2-18z^2)(x^4-4x^3y-6x^2y^2+4xy^3+y^4)(x^4+4x^3y-6x^2y^2-4xy^3+y^4)}{256}\right)\right)$
116	$\mathbb{G}_{10,1}(E_{2u}^{(a)}, 3)$	$\sqrt{2}\left(-\frac{2}{32}\left(\frac{\sqrt{2145}ixy(x-y)(x+y)(x^6+3x^4y^2-42x^4z^2+3x^2y^4-84x^2y^2z^2+168x^2z^4+y^6-42y^4z^2+168y^2z^4-112z^6)}{32} - \frac{\sqrt{2145}(x^2-2xy-y^2)(x^2+2xy-y^2)(x^6+3x^4y^2-42x^4z^2+3x^2y^4-84x^2y^2z^2+168x^2z^4+y^6-42y^4z^2+168y^2z^4-112z^6)}{128}\right)\right)$
117	$\mathbb{G}_{10,1}(E_{2u}^{(a)}, 4)$	$\sqrt{2}\left(-\frac{2}{128}\left(\frac{\sqrt{165}ixy(7x^8+28x^6y^2-336x^6z^2+42x^4y^4-1008x^4y^2z^2+1680x^4z^4+28x^2y^6-1008x^2y^4z^2+3360x^2y^2z^4-1792x^2z^6+7y^8-336y^6z^2+1680y^4z^4-1792y^2z^6+384z^8)}{128} + \frac{\sqrt{165}(x-y)(x+y)(7x^8+28x^6y^2-336x^6z^2+42x^4y^4-1008x^4y^2z^2+1680x^4z^4+28x^2y^6-1008x^2y^4z^2+3360x^2y^2z^4-1792x^2z^6+7y^8-336y^6z^2+1680y^4z^4-1792y^2z^6+384z^8)}{256}\right)\right)$
118	$\mathbb{G}_{10,1}(E_{2u}^{(b)}, 1)$	$\sqrt{2}\left(-\frac{2}{256}\left(\frac{\sqrt{92378}ixy(x^4-10x^2y^2+5y^4)(5x^4-10x^2y^2+y^4)}{256} + \frac{\sqrt{92378}(x-y)(x+y)(x^4-4x^3y-14x^2y^2-4xy^3+y^4)(x^4+4x^3y-14x^2y^2+4xy^3+y^4)}{512}\right)\right)$
119	$\mathbb{G}_{10,1}(E_{2u}^{(b)}, 2)$	$\sqrt{2}\left(-\frac{2}{32}\left(\frac{\sqrt{12155}ixy(x-y)(x+y)(x^2+y^2-18z^2)(x^2-2xy-y^2)(x^2+2xy-y^2)}{32} - \frac{\sqrt{12155}(x^2+y^2-18z^2)(x^4-4x^3y-6x^2y^2+4xy^3+y^4)(x^4+4x^3y-6x^2y^2-4xy^3+y^4)}{256}\right)\right)$
120	$\mathbb{G}_{10,1}(E_{2u}^{(b)}, 3)$	$\sqrt{2}\left(\frac{2}{32}\left(\frac{\sqrt{2145}ixy(x-y)(x+y)(x^6+3x^4y^2-42x^4z^2+3x^2y^4-84x^2y^2z^2+168x^2z^4+y^6-42y^4z^2+168y^2z^4-112z^6)}{32} - \frac{\sqrt{2145}(x^2-2xy-y^2)(x^2+2xy-y^2)(x^6+3x^4y^2-42x^4z^2+3x^2y^4-84x^2y^2z^2+168x^2z^4+y^6-42y^4z^2+168y^2z^4-112z^6)}{128}\right)\right)$
121	$\mathbb{G}_{10,1}(E_{2u}^{(b)}, 4)$	$\sqrt{2}\left(\frac{2}{128}\left(\frac{\sqrt{165}ixy(7x^8+28x^6y^2-336x^6z^2+42x^4y^4-1008x^4y^2z^2+1680x^4z^4+28x^2y^6-1008x^2y^4z^2+3360x^2y^2z^4-1792x^2z^6+7y^8-336y^6z^2+1680y^4z^4-1792y^2z^6+384z^8)}{128} + \frac{\sqrt{165}(x-y)(x+y)(7x^8+28x^6y^2-336x^6z^2+42x^4y^4-1008x^4y^2z^2+1680x^4z^4+28x^2y^6-1008x^2y^4z^2+3360x^2y^2z^4-1792x^2z^6+7y^8-336y^6z^2+1680y^4z^4-1792y^2z^6+384z^8)}{256}\right)\right)$

Table 12 Harmonics for rank 11.

No.	multipole	expression
122	$\mathbb{G}_{11}(A_g, 1)$	$\frac{\sqrt{14586}xy z(x^2-3y^2)(3x^2-y^2)(15x^4+30x^2y^2-160x^2z^2+15y^4-160y^2z^2+224z^4)}{256}$
123	$\mathbb{G}_{11}(A_g, 2)$	$-\frac{z(693x^{10}+3465x^8y^2-11550x^8z^2+6930x^6y^4-46200x^6y^2z^2+36960x^6z^4+6930x^4y^6-69300x^4y^4z^2+110880x^4y^2z^4-31680x^4z^6+3465x^2y^8-46200x^2y^6z^2+110880x^2y^4z^4-63360x^2y^2z^6+7040x^2z^8+693y^{10}-11550y^8z^2+36960y^6z^4-31680y^4z^6+7040y^2z^8-256z^{10})}{256}$
124	$\mathbb{G}_{11}(A_g, 3)$	$\frac{\sqrt{14586}z(x-y)(x+y)(x^2-4xy+y^2)(x^2+4xy+y^2)(15x^4+30x^2y^2-160x^2z^2+15y^4-160y^2z^2+224z^4)}{512}$
125	$\mathbb{G}_{11}(B_g, 1)$	$-\frac{\sqrt{46189y}(3x^2-y^2)(x^2+y^2-20z^2)(3x^6-27x^4y^2+33x^2y^4-y^6)}{512}$
126	$\mathbb{G}_{11}(B_g, 2)$	$\frac{\sqrt{30030y}(3x^2-y^2)(x^8+4x^6y^2-56x^6z^2+6x^4y^4-168x^4y^2z^2+336x^4z^4+4x^2y^6-168x^2y^4z^2+672x^2y^2z^4-448x^2z^6+y^8-56y^6z^2+336y^4z^4-448y^2z^6+128z^8)}{512}$
127	$\mathbb{G}_{11}(B_g, 3)$	$-\frac{\sqrt{46189x}(x^2-3y^2)(x^2+y^2-20z^2)(x^6-33x^4y^2+27x^2y^4-3y^6)}{512}$
128	$\mathbb{G}_{11}(B_g, 4)$	$\frac{\sqrt{30030x}(x^2-3y^2)(x^8+4x^6y^2-56x^6z^2+6x^4y^4-168x^4y^2z^2+336x^4z^4+4x^2y^6-168x^2y^4z^2+672x^2y^2z^4-448x^2z^6+y^8-56y^6z^2+336y^4z^4-448y^2z^6+128z^8)}{512}$
129	$\mathbb{G}_{11,1}(E_{1g}^{(a)}, 1)$	$\sqrt{2}\left(\frac{\sqrt{88179}x(x^{10}-55x^8y^2+330x^6y^4-462x^4y^6+165x^2y^8-11y^{10})}{512}-\frac{\sqrt{88179}iy(11x^{10}-165x^8y^2+462x^6y^4-330x^4y^6+55x^2y^8-y^{10})}{512}\right)$
130	$\mathbb{G}_{11,1}(E_{1g}^{(a)}, 2)$	$\sqrt{2}\left(\frac{\sqrt{36465}x(x^6-21x^4y^2+35x^2y^4-7y^6)}{512}+\frac{\sqrt{36465}iy(7x^6-35x^4y^2+21x^2y^4-y^6)}{512}\right)$
131	$\mathbb{G}_{11,1}(E_{1g}^{(a)}, 3)$	$\sqrt{2}\left(-\frac{3\sqrt{143}x(x^4-10x^2y^2+5y^4)(5x^6+15x^4y^2-240x^4z^2+15x^2y^4-480x^2y^2z^2+1120x^2z^4+5y^6-240y^4z^2+1120y^2z^4-896z^6)}{512}+\frac{3\sqrt{143}iy(5x^4-10x^2y^2+y^4)(5x^6+15x^4y^2-240x^4z^2+15x^2y^4-480x^2y^2z^2+1120x^2z^4+5y^6-240y^4z^2+1120y^2z^4-896z^6)}{512}\right)$
132	$\mathbb{G}_{11,1}(E_{1g}^{(a)}, 4)$	$\sqrt{2}\left(-\frac{\sqrt{66}x(21x^{10}+105x^8y^2-1260x^8z^2+210x^6y^4-5040x^6y^2z^2+8400x^6z^4+210x^4y^6-7560x^4y^4z^2+25200x^4y^2z^4-13440x^4z^6+105x^2y^8-5040x^2y^6z^2+25200x^2y^4z^4-26880x^2y^2z^6+5760x^2z^8+21y^{10}-1260y^8z^2+8400y^6z^4-13440y^4z^6+5760y^2z^8-512z^{10})}{512}-\frac{\sqrt{66}iy(21x^{10}+105x^8y^2-1260x^8z^2+210x^6y^4-5040x^6y^2z^2+8400x^6z^4+210x^4y^6-7560x^4y^4z^2+25200x^4y^2z^4-13440x^4z^6+105x^2y^8-5040x^2y^6z^2+25200x^2y^4z^4-26880x^2y^2z^6+5760x^2z^8+21y^{10}-1260y^8z^2+8400y^6z^4-13440y^4z^6+5760y^2z^8-512z^{10})}{512}\right)$
133	$\mathbb{G}_{11,1}(E_{1g}^{(b)}, 1)$	$\sqrt{2}\left(\frac{\sqrt{88179}x(x^{10}-55x^8y^2+330x^6y^4-462x^4y^6+165x^2y^8-11y^{10})}{512}+\frac{\sqrt{88179}iy(11x^{10}-165x^8y^2+462x^6y^4-330x^4y^6+55x^2y^8-y^{10})}{512}\right)$
134	$\mathbb{G}_{11,1}(E_{1g}^{(b)}, 2)$	$\sqrt{2}\left(\frac{\sqrt{36465}x(x^6-21x^4y^2+35x^2y^4-7y^6)}{512}-\frac{\sqrt{36465}iy(7x^6-35x^4y^2+21x^2y^4-y^6)}{512}\right)$
135	$\mathbb{G}_{11,1}(E_{1g}^{(b)}, 3)$	$\sqrt{2}\left(-\frac{3\sqrt{143}x(x^4-10x^2y^2+5y^4)(5x^6+15x^4y^2-240x^4z^2+15x^2y^4-480x^2y^2z^2+1120x^2z^4+5y^6-240y^4z^2+1120y^2z^4-896z^6)}{512}-\frac{3\sqrt{143}iy(5x^4-10x^2y^2+y^4)(5x^6+15x^4y^2-240x^4z^2+15x^2y^4-480x^2y^2z^2+1120x^2z^4+5y^6-240y^4z^2+1120y^2z^4-896z^6)}{512}\right)$
136	$\mathbb{G}_{11,1}(E_{1g}^{(b)}, 4)$	$\sqrt{2}\left(-\frac{\sqrt{66}x(21x^{10}+105x^8y^2-1260x^8z^2+210x^6y^4-5040x^6y^2z^2+8400x^6z^4+210x^4y^6-7560x^4y^4z^2+25200x^4y^2z^4-13440x^4z^6+105x^2y^8-5040x^2y^6z^2+25200x^2y^4z^4-26880x^2y^2z^6+5760x^2z^8+21y^{10}-1260y^8z^2+8400y^6z^4-13440y^4z^6+5760y^2z^8-512z^{10})}{512}+\frac{\sqrt{66}iy(21x^{10}+105x^8y^2-1260x^8z^2+210x^6y^4-5040x^6y^2z^2+8400x^6z^4+210x^4y^6-7560x^4y^4z^2+25200x^4y^2z^4-13440x^4z^6+105x^2y^8-5040x^2y^6z^2+25200x^2y^4z^4-26880x^2y^2z^6+5760x^2z^8+21y^{10}-1260y^8z^2+8400y^6z^4-13440y^4z^6+5760y^2z^8-512z^{10})}{512}\right)$
137	$\mathbb{G}_{11,1}(E_{2g}^{(a)}, 1)$	$\sqrt{2}\left(\frac{\sqrt{1939938}ixyz(x^4-10x^2y^2+5y^4)(5x^4-10x^2y^2+y^4)}{256}+\frac{\sqrt{1939938}z(x-y)(x+y)(x^4-4x^3y-14x^2y^2-4xy^3+y^4)(x^4+4x^3y-14x^2y^2+4xy^3+y^4)}{512}\right)$
138	$\mathbb{G}_{11,1}(E_{2g}^{(a)}, 2)$	$\sqrt{2}\left(\frac{\sqrt{692835}ixyz(x-y)(x+y)(x^2+y^2-6z^2)(x^2-2xy-y^2)(x^2+2xy-y^2)}{32}-\frac{\sqrt{692835}z(x^2+y^2-6z^2)(x^4-4x^3y-6x^2y^2+4xy^3+y^4)(x^4+4x^3y-6x^2y^2-4xy^3+y^4)}{256}\right)$
139	$\mathbb{G}_{11,1}(E_{2g}^{(a)}, 3)$	$\sqrt{2}\left(-\frac{3\sqrt{1001}ixyz(x-y)(x+y)(5x^6+15x^4y^2-70x^4z^2+15x^2y^4-140x^2y^2z^2+168x^2z^4+5y^6-70y^4z^2+168y^2z^4-80z^6)}{32}-\frac{3\sqrt{1001}z(x^2-2xy-y^2)(x^2+2xy-y^2)(5x^6+15x^4y^2-70x^4z^2+15x^2y^4-140x^2y^2z^2+168x^2z^4+5y^6-70y^4z^2+168y^2z^4-80z^6)}{128}\right)$
140	$\mathbb{G}_{11,1}(E_{2g}^{(a)}, 4)$	$\sqrt{2}\left(-\frac{\sqrt{2145}ixyz(21x^8+84x^6y^2-336x^6z^2+126x^4y^4-1008x^4y^2z^2+1008x^4z^4+84x^2y^6-1008x^2y^4z^2+2016x^2y^2z^4-768x^2z^6+21y^8-336y^6z^2+1008y^4z^4-768y^2z^6+128z^8)}{128}+\frac{\sqrt{2145}z(x-y)(x+y)(21x^8+84x^6y^2-336x^6z^2+126x^4y^4-1008x^4y^2z^2+1008x^4z^4+84x^2y^6-1008x^2y^4z^2+2016x^2y^2z^4-768x^2z^6+21y^8-336y^6z^2+1008y^4z^4-768y^2z^6+128z^8)}{256}\right)$
141	$\mathbb{G}_{11,1}(E_{2g}^{(b)}, 1)$	$\sqrt{2}\left(-\frac{\sqrt{1939938}ixyz(x^4-10x^2y^2+5y^4)(5x^4-10x^2y^2+y^4)}{256}+\frac{\sqrt{1939938}z(x-y)(x+y)(x^4-4x^3y-14x^2y^2-4xy^3+y^4)(x^4+4x^3y-14x^2y^2+4xy^3+y^4)}{512}\right)$
142	$\mathbb{G}_{11,1}(E_{2g}^{(b)}, 2)$	$\sqrt{2}\left(-\frac{\sqrt{692835}ixyz(x-y)(x+y)(x^2+y^2-6z^2)(x^2-2xy-y^2)(x^2+2xy-y^2)}{32}-\frac{\sqrt{692835}z(x^2+y^2-6z^2)(x^4-4x^3y-6x^2y^2+4xy^3+y^4)(x^4+4x^3y-6x^2y^2-4xy^3+y^4)}{256}\right)$
143	$\mathbb{G}_{11,1}(E_{2g}^{(b)}, 3)$	$\sqrt{2}\left(\frac{3\sqrt{1001}ixyz(x-y)(x+y)(5x^6+15x^4y^2-70x^4z^2+15x^2y^4-140x^2y^2z^2+168x^2z^4+5y^6-70y^4z^2+168y^2z^4-80z^6)}{32}-\frac{3\sqrt{1001}z(x^2-2xy-y^2)(x^2+2xy-y^2)(5x^6+15x^4y^2-70x^4z^2+15x^2y^4-140x^2y^2z^2+168x^2z^4+5y^6-70y^4z^2+168y^2z^4-80z^6)}{128}\right)$
144	$\mathbb{G}_{11,1}(E_{2g}^{(b)}, 4)$	$\sqrt{2}\left(\frac{\sqrt{2145}ixyz(21x^8+84x^6y^2-336x^6z^2+126x^4y^4-1008x^4y^2z^2+1008x^4z^4+84x^2y^6-1008x^2y^4z^2+2016x^2y^2z^4-768x^2z^6+21y^8-336y^6z^2+1008y^4z^4-768y^2z^6+128z^8)}{128}+\frac{\sqrt{2145}z(x-y)(x+y)(21x^8+84x^6y^2-336x^6z^2+126x^4y^4-1008x^4y^2z^2+1008x^4z^4+84x^2y^6-1008x^2y^4z^2+2016x^2y^2z^4-768x^2z^6+21y^8-336y^6z^2+1008y^4z^4-768y^2z^6+128z^8)}{256}\right)$