

MPG No. 32.1.118  $m\bar{3}m$  [ Type I, cubic ]

\* symmetry operation

Table 1: Symmetry operations for 3d polar vector.

| No. | tag           | matrix (polar)   | det | TR |
|-----|---------------|--|-----|----|
| 1   | 1             | $\begin{bmatrix} 1 & 0 & 0 \\ 0 & 1 & 0 \\ 0 & 0 & 1 \end{bmatrix}$    | 1   | 1  |
| 2   | $2_{100}$     | $\begin{bmatrix} 1 & 0 & 0 \\ 0 & -1 & 0 \\ 0 & 0 & -1 \end{bmatrix}$  | 1   | 1  |
| 3   | $2_{010}$     | $\begin{bmatrix} -1 & 0 & 0 \\ 0 & 1 & 0 \\ 0 & 0 & -1 \end{bmatrix}$  | 1   | 1  |
| 4   | $2_{001}$     | $\begin{bmatrix} -1 & 0 & 0 \\ 0 & -1 & 0 \\ 0 & 0 & 1 \end{bmatrix}$  | 1   | 1  |
| 5   | $3^-_{111}$   | $\begin{bmatrix} 0 & 1 & 0 \\ 0 & 0 & 1 \\ 1 & 0 & 0 \end{bmatrix}$    | 1   | 1  |
| 6   | $3^-_{-1-11}$ | $\begin{bmatrix} 0 & 1 & 0 \\ 0 & 0 & -1 \\ -1 & 0 & 0 \end{bmatrix}$  | 1   | 1  |
| 7   | $3^-_{1-1-1}$ | $\begin{bmatrix} 0 & -1 & 0 \\ 0 & 0 & 1 \\ -1 & 0 & 0 \end{bmatrix}$  | 1   | 1  |
| 8   | $3^-_{-11-1}$ | $\begin{bmatrix} 0 & -1 & 0 \\ 0 & 0 & -1 \\ 1 & 0 & 0 \end{bmatrix}$  | 1   | 1  |
| 9   | $3^+_{111}$   | $\begin{bmatrix} 0 & 0 & 1 \\ 1 & 0 & 0 \\ 0 & 1 & 0 \end{bmatrix}$    | 1   | 1  |
| 10  | $3^+_{-11-1}$ | $\begin{bmatrix} 0 & 0 & 1 \\ -1 & 0 & 0 \\ 0 & -1 & 0 \end{bmatrix}$  | 1   | 1  |
| 11  | $3^+_{-1-11}$ | $\begin{bmatrix} 0 & 0 & -1 \\ 1 & 0 & 0 \\ 0 & -1 & 0 \end{bmatrix}$  | 1   | 1  |
| 12  | $3^+_{1-1-1}$ | $\begin{bmatrix} 0 & 0 & -1 \\ -1 & 0 & 0 \\ 0 & 1 & 0 \end{bmatrix}$  | 1   | 1  |
| 13  | $2_{1-10}$    | $\begin{bmatrix} 0 & -1 & 0 \\ -1 & 0 & 0 \\ 0 & 0 & -1 \end{bmatrix}$ | 1   | 1  |

continued ...

Table 1

| No. | tag         | matrix (polar)   | det | TR |
|-----|-------------|--|-----|----|
| 14  | $4_{001}^+$ | $\begin{bmatrix} 0 & -1 & 0 \\ 1 & 0 & 0 \\ 0 & 0 & 1 \end{bmatrix}$   | 1   | 1  |
| 15  | $4_{001}^-$ | $\begin{bmatrix} 0 & 1 & 0 \\ -1 & 0 & 0 \\ 0 & 0 & 1 \end{bmatrix}$   | 1   | 1  |
| 16  | $2_{110}$   | $\begin{bmatrix} 0 & 1 & 0 \\ 1 & 0 & 0 \\ 0 & 0 & -1 \end{bmatrix}$   | 1   | 1  |
| 17  | $2_{01-1}$  | $\begin{bmatrix} -1 & 0 & 0 \\ 0 & 0 & -1 \\ 0 & -1 & 0 \end{bmatrix}$ | 1   | 1  |
| 18  | $2_{011}$   | $\begin{bmatrix} -1 & 0 & 0 \\ 0 & 0 & 1 \\ 0 & 1 & 0 \end{bmatrix}$   | 1   | 1  |
| 19  | $4_{100}^+$ | $\begin{bmatrix} 1 & 0 & 0 \\ 0 & 0 & -1 \\ 0 & 1 & 0 \end{bmatrix}$   | 1   | 1  |
| 20  | $4_{100}^-$ | $\begin{bmatrix} 1 & 0 & 0 \\ 0 & 0 & 1 \\ 0 & -1 & 0 \end{bmatrix}$   | 1   | 1  |
| 21  | $2_{-101}$  | $\begin{bmatrix} 0 & 0 & -1 \\ 0 & -1 & 0 \\ -1 & 0 & 0 \end{bmatrix}$ | 1   | 1  |
| 22  | $4_{010}^-$ | $\begin{bmatrix} 0 & 0 & -1 \\ 0 & 1 & 0 \\ 1 & 0 & 0 \end{bmatrix}$   | 1   | 1  |
| 23  | $2_{101}$   | $\begin{bmatrix} 0 & 0 & 1 \\ 0 & -1 & 0 \\ 1 & 0 & 0 \end{bmatrix}$   | 1   | 1  |
| 24  | $4_{010}^+$ | $\begin{bmatrix} 0 & 0 & 1 \\ 0 & 1 & 0 \\ -1 & 0 & 0 \end{bmatrix}$   | 1   | 1  |
| 25  | -1          | $\begin{bmatrix} -1 & 0 & 0 \\ 0 & -1 & 0 \\ 0 & 0 & -1 \end{bmatrix}$ | -1  | 1  |
| 26  | $m_{100}$   | $\begin{bmatrix} -1 & 0 & 0 \\ 0 & 1 & 0 \\ 0 & 0 & 1 \end{bmatrix}$   | -1  | 1  |
| 27  | $m_{010}$   | $\begin{bmatrix} 1 & 0 & 0 \\ 0 & -1 & 0 \\ 0 & 0 & 1 \end{bmatrix}$   | -1  | 1  |

continued ...

Table 1

| No. | tag             | matrix (polar)   | det | TR |
|-----|-----------------|--|-----|----|
| 28  | $m_{001}$       | $\begin{bmatrix} 1 & 0 & 0 \\ 0 & 1 & 0 \\ 0 & 0 & -1 \end{bmatrix}$   | -1  | 1  |
| 29  | $-3^-_{111}$    | $\begin{bmatrix} 0 & -1 & 0 \\ 0 & 0 & -1 \\ -1 & 0 & 0 \end{bmatrix}$ | -1  | 1  |
| 30  | $-3^-_{-1-11}$  | $\begin{bmatrix} 0 & -1 & 0 \\ 0 & 0 & 1 \\ 1 & 0 & 0 \end{bmatrix}$   | -1  | 1  |
| 31  | $-3^-_{-1-1-1}$ | $\begin{bmatrix} 0 & 1 & 0 \\ 0 & 0 & -1 \\ 1 & 0 & 0 \end{bmatrix}$   | -1  | 1  |
| 32  | $-3^-_{-11-1}$  | $\begin{bmatrix} 0 & 1 & 0 \\ 0 & 0 & 1 \\ -1 & 0 & 0 \end{bmatrix}$   | -1  | 1  |
| 33  | $-3^+_{111}$    | $\begin{bmatrix} 0 & 0 & -1 \\ -1 & 0 & 0 \\ 0 & -1 & 0 \end{bmatrix}$ | -1  | 1  |
| 34  | $-3^+_{-11-1}$  | $\begin{bmatrix} 0 & 0 & -1 \\ 1 & 0 & 0 \\ 0 & 1 & 0 \end{bmatrix}$   | -1  | 1  |
| 35  | $-3^+_{-1-11}$  | $\begin{bmatrix} 0 & 0 & 1 \\ -1 & 0 & 0 \\ 0 & 1 & 0 \end{bmatrix}$   | -1  | 1  |
| 36  | $-3^+_{1-1-1}$  | $\begin{bmatrix} 0 & 0 & 1 \\ 1 & 0 & 0 \\ 0 & -1 & 0 \end{bmatrix}$   | -1  | 1  |
| 37  | $m_{1-10}$      | $\begin{bmatrix} 0 & 1 & 0 \\ 1 & 0 & 0 \\ 0 & 0 & 1 \end{bmatrix}$    | -1  | 1  |
| 38  | $-4^+_{001}$    | $\begin{bmatrix} 0 & 1 & 0 \\ -1 & 0 & 0 \\ 0 & 0 & -1 \end{bmatrix}$  | -1  | 1  |
| 39  | $-4^-_{001}$    | $\begin{bmatrix} 0 & -1 & 0 \\ 1 & 0 & 0 \\ 0 & 0 & -1 \end{bmatrix}$  | -1  | 1  |
| 40  | $m_{110}$       | $\begin{bmatrix} 0 & -1 & 0 \\ -1 & 0 & 0 \\ 0 & 0 & 1 \end{bmatrix}$  | -1  | 1  |
| 41  | $m_{01-1}$      | $\begin{bmatrix} 1 & 0 & 0 \\ 0 & 0 & 1 \\ 0 & 1 & 0 \end{bmatrix}$    | -1  | 1  |

continued ...

Table 1

| No. | tag          | matrix (polar)  | det | TR |
|-----|--------------|---|-----|----|
| 42  | $m_{011}$    | $\begin{bmatrix} 1 & 0 & 0 \\ 0 & 0 & -1 \\ 0 & -1 & 0 \end{bmatrix}$ | -1  | 1  |
| 43  | $-4^+_{100}$ | $\begin{bmatrix} -1 & 0 & 0 \\ 0 & 0 & 1 \\ 0 & -1 & 0 \end{bmatrix}$ | -1  | 1  |
| 44  | $-4^-_{100}$ | $\begin{bmatrix} -1 & 0 & 0 \\ 0 & 0 & -1 \\ 0 & 1 & 0 \end{bmatrix}$ | -1  | 1  |
| 45  | $m_{-101}$   | $\begin{bmatrix} 0 & 0 & 1 \\ 0 & 1 & 0 \\ 1 & 0 & 0 \end{bmatrix}$   | -1  | 1  |
| 46  | $-4^-_{010}$ | $\begin{bmatrix} 0 & 0 & 1 \\ 0 & -1 & 0 \\ -1 & 0 & 0 \end{bmatrix}$ | -1  | 1  |
| 47  | $m_{101}$    | $\begin{bmatrix} 0 & 0 & -1 \\ 0 & 1 & 0 \\ -1 & 0 & 0 \end{bmatrix}$ | -1  | 1  |
| 48  | $-4^+_{010}$ | $\begin{bmatrix} 0 & 0 & -1 \\ 0 & -1 & 0 \\ 1 & 0 & 0 \end{bmatrix}$ | -1  | 1  |