

MPG No. 11.3.37 $4'/m$ [Type III, tetragonal] [T tensor]

* Rank 0 tensor. * Rank 1 tensor. * Rank 2 tensor (s).

$$\begin{bmatrix} T_{xx} & T_{xy} & 0 \\ T_{xy} & -T_{xx} & 0 \\ 0 & 0 & 0 \end{bmatrix}$$

$$T_{xx} = T_{dv}^{(1)}$$

$$T_{xy} = T_{dx}^{(1)}$$

* Rank 2 tensor (a). * Rank 3 tensor (s). * Rank 3 tensor (a). * Rank 4 tensor (sss).

$$\begin{bmatrix} T_{xxxx} & 0 & T_{xxzz} & 0 & 0 & T_{xxxz} \\ 0 & -T_{xxxx} & -T_{xxzz} & 0 & 0 & T_{xxxy} \\ T_{xxzz} & -T_{xxzz} & 0 & 0 & 0 & T_{zzxy} \\ 0 & 0 & 0 & T_{yzyz} & T_{yzzx} & 0 \\ 0 & 0 & 0 & T_{yzzx} & -T_{yzyz} & 0 \\ T_{xxxz} & T_{xxxy} & T_{zzxy} & 0 & 0 & 0 \end{bmatrix}$$

$$T_{xxxx} = 2T_{dv}^{(1)} + 4T_{dv}^{(2)} + T_{gv}^{(1)}$$

$$T_{xxzz} = T_{dv}^{(1)} - T_{gv}^{(1)}$$

$$T_{xxxy} = T_{dy}^{(1)} + 2T_{dy}^{(2)} - T_{gbz}^{(1)}$$

$$T_{zzxy} = T_{dy}^{(1)} + 2T_{gbz}^{(1)}$$

$$T_{yzyz} = -T_{dv}^{(2)} + T_{gv}^{(1)}$$

$$T_{yzzx} = T_{dy}^{(2)} + 2T_{gbz}^{(1)}$$

* Rank 4 tensor (ssa).

$$\begin{bmatrix} 0 & T_{xxyy} & T_{xxzz} & 0 & 0 & T_{xxxz} \\ -T_{xxyy} & 0 & -T_{xxzz} & 0 & 0 & T_{xxxy} \\ -T_{xxzz} & T_{xxzz} & 0 & 0 & 0 & T_{zzxy} \\ 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 \\ -T_{xxxz} & -T_{xxxy} & -T_{zzxy} & 0 & 0 & 0 \end{bmatrix}$$

$$T_{xxyy} = 4M_{f3}^{(1)} - 2T_{dv}^{(3)}$$

$$T_{xxzz} = -4M_{f3}^{(1)} - T_{dv}^{(3)}$$

$$T_{xxxy} = 2M_{fbz}^{(1)} + T_{dy}^{(3)}$$

$$T_{zzxy} = -4M_{fbz}^{(1)} + T_{dy}^{(3)}$$

* Rank 4 tensor (aas).

$$\begin{bmatrix} T_{yzyz} & T_{yzzx} & 0 \\ T_{yzzx} & -T_{yzyz} & 0 \\ 0 & 0 & 0 \end{bmatrix}$$

$$T_{yzyz} = 2T_{dv}^{(4)}$$

$$T_{yzzx} = 2T_{dy}^{(4)}$$

* Rank 4 tensor (aaa). * Rank 4 tensor (sa).

$$\begin{bmatrix} 0 & 0 & T_{xxyy} \\ 0 & 0 & -T_{xxxy} \\ 0 & 0 & 0 \\ T_{yzyz} & T_{yzzx} & 0 \\ -T_{yzzx} & T_{yzyz} & 0 \\ 0 & 0 & T_{xyxy} \end{bmatrix}$$

$$T_{xxxy} = M_{fbz}^{(2)} - 2T_{dxy}^{(5)}$$

$$T_{yzyz} = M_{f3}^{(2)} - T_{dv}^{(5)}$$

$$T_{yzzx} = -M_{fbz}^{(2)} - T_{dxy}^{(5)}$$

$$T_{xyxy} = M_{f3}^{(2)} + 2T_{dv}^{(5)}$$

* Rank 4 tensor (as).

$$\begin{bmatrix} 0 & 0 & 0 & T_{yzyz} & T_{yzzx} & 0 \\ 0 & 0 & 0 & -T_{yzzx} & T_{yzyz} & 0 \\ T_{xyxx} & -T_{xyxx} & 0 & 0 & 0 & T_{xyxy} \end{bmatrix}$$

$$T_{yzyz} = M_{f3}^{(3)} - T_{dv}^{(6)}$$

$$T_{yzzx} = M_{fbz}^{(3)} + T_{dxy}^{(6)}$$

$$T_{xyxx} = M_{fbz}^{(3)} - 2T_{dxy}^{(6)}$$

$$T_{xyxy} = M_{f3}^{(3)} + 2T_{dv}^{(6)}$$

* Rank 4 tensor (s).

$$\begin{bmatrix} T_{xxxx} & T_{xxyy} & T_{xxzz} & 0 & 0 & T_{xxxy} & 0 & 0 & T_{xxyx} \\ -T_{xxyy} & -T_{xxxx} & -T_{xxzz} & 0 & 0 & T_{xxyx} & 0 & 0 & T_{xxyy} \\ T_{zzxx} & -T_{zzxx} & 0 & 0 & 0 & T_{zzyy} & 0 & 0 & T_{zzxy} \\ 0 & 0 & 0 & T_{yzyz} & T_{yzzx} & 0 & T_{yzyy} & T_{yzxz} & 0 \\ 0 & 0 & 0 & T_{yzxz} & -T_{yzyy} & 0 & T_{yzzx} & -T_{yzyz} & 0 \\ T_{xyxx} & T_{xyxx} & T_{xyzz} & 0 & 0 & T_{xyxy} & 0 & 0 & -T_{xyxy} \end{bmatrix}$$

$$T_{xxxx} = 2T_{dv}^{(1)} + 4T_{dv}^{(2)} + T_{gv}^{(1)}$$

$$T_{xxyy} = 4M_{f3}^{(1)} - 2T_{dv}^{(3)}$$

$$T_{xxzz} = -4M_{f3}^{(1)} + T_{dv}^{(1)} - T_{dv}^{(3)} - T_{gv}^{(1)}$$

$$T_{xxxy} = 2M_{fbz}^{(1)} + M_{fbz}^{(2)} + T_{dxy}^{(1)} + 2T_{dxy}^{(2)} + T_{dxy}^{(3)} - 2T_{dxy}^{(5)} - T_{gbz}^{(1)}$$

$$T_{xyyx} = 2M_{fbz}^{(1)} - M_{fbz}^{(2)} + T_{dxy}^{(1)} + 2T_{dxy}^{(2)} + T_{dxy}^{(3)} + 2T_{dxy}^{(5)} - T_{gbz}^{(1)}$$

$$T_{zzxx} = 4M_{f3}^{(1)} + T_{dv}^{(1)} + T_{dv}^{(3)} - T_{gv}^{(1)}$$

$$T_{zzxy} = -4M_{fbz}^{(1)} + T_{dxy}^{(1)} + T_{dxy}^{(3)} + 2T_{gbz}^{(1)}$$

$$T_{yzyz} = M_{f3}^{(2)} - T_{dv}^{(2)} - T_{dv}^{(5)} + T_{gv}^{(1)}$$

$$T_{yzzx} = -M_{fbz}^{(2)} + T_{dxy}^{(2)} - T_{dxy}^{(5)} + 2T_{gbz}^{(1)}$$

$$T_{yzyy} = -M_{f3}^{(2)} - T_{dv}^{(2)} + T_{dv}^{(5)} + T_{gv}^{(1)}$$

$$T_{yzxz} = M_{fbz}^{(2)} + T_{dxy}^{(2)} + T_{dxy}^{(5)} + 2T_{gbz}^{(1)}$$

$$T_{xyxx} = -2M_{fbz}^{(1)} + T_{dxy}^{(1)} + 2T_{dxy}^{(2)} - T_{dxy}^{(3)} - T_{gbz}^{(1)}$$

$$T_{xyzz} = 4M_{fbz}^{(1)} + T_{dxy}^{(1)} - T_{dxy}^{(3)} + 2T_{gbz}^{(1)}$$

$$T_{xyxy} = M_{f3}^{(2)} + 2T_{dv}^{(5)}$$

* Rank 4 tensor (a).

$$\begin{bmatrix} 0 & 0 & 0 & T_{yzyz} & T_{yzzx} & 0 & T_{yzyy} & T_{yzxz} & 0 \\ 0 & 0 & 0 & -T_{yzzx} & T_{yzyz} & 0 & -T_{yzzx} & T_{yzyz} & 0 \\ T_{xyxx} & -T_{xyxx} & 0 & 0 & 0 & T_{xyxy} & 0 & 0 & T_{xyxy} \end{bmatrix}$$

$$\begin{aligned}
T_{yzyz} &= M_{f3}^{(3)} + 2T_{dv}^{(4)} - T_{dv}^{(6)} \\
T_{yzzx} &= M_{fbz}^{(3)} + 2T_{dxy}^{(4)} + T_{dxy}^{(6)} \\
T_{yzzy} &= M_{f3}^{(3)} - 2T_{dv}^{(4)} - T_{dv}^{(6)} \\
T_{yzxz} &= M_{fbz}^{(3)} - 2T_{dxy}^{(4)} + T_{dxy}^{(6)} \\
T_{xyxx} &= M_{fbz}^{(3)} - 2T_{dxy}^{(6)} \\
T_{xyxy} &= M_{f3}^{(3)} + 2T_{dv}^{(6)}
\end{aligned}$$

* Rank 4 tensor (t).

$$\left[\begin{array}{ccc}
T_{xxxx} & T_{xxxz} & 0 \\
T_{xxxy} & -T_{xxxx} & 0 \\
0 & 0 & 0 \\
0 & 0 & T_{yyzz} \\
T_{zzxx} & T_{zzxy} & 0 \\
T_{xxyx} & -T_{yyzz} - T_{zzxx} & 0 \\
T_{yzzx} & T_{yzyz} & 0 \\
0 & 0 & T_{zxxz} \\
-T_{yzyz} - T_{zzxz} & T_{xyyy} & 0 \\
0 & 0 & -\frac{T_{xxxy}}{2} - \frac{T_{xxyx}}{2} + T_{xyyy} + T_{zzxy}
\end{array} \right]$$

$$\begin{aligned}
T_{xxxx} &= 2T_{dv}^{(1)} + 4T_{dv}^{(2)} + T_{gv}^{(1)} \\
T_{xxxy} &= T_{dxy}^{(1)} + 2T_{dxy}^{(2)} + T_{dxy}^{(3)} - 2T_{dxy}^{(5)} - T_{gbz}^{(1)} \\
T_{yyzz} &= -T_{dv}^{(1)} + T_{dv}^{(3)} + T_{gv}^{(1)} \\
T_{zzxx} &= T_{dv}^{(1)} + T_{dv}^{(3)} - T_{gv}^{(1)} \\
T_{zzxy} &= T_{dxy}^{(1)} + T_{dxy}^{(3)} + 2T_{gbz}^{(1)} \\
T_{xxyx} &= T_{dxy}^{(1)} + 2T_{dxy}^{(2)} + T_{dxy}^{(3)} + 2T_{dxy}^{(5)} - T_{gbz}^{(1)} \\
T_{yzzx} &= T_{dxy}^{(2)} - T_{dxy}^{(5)} + 2T_{gbz}^{(1)} \\
T_{yzyz} &= -T_{dv}^{(2)} + T_{dv}^{(5)} + T_{gv}^{(1)} \\
T_{zxxz} &= T_{dv}^{(2)} + T_{dv}^{(5)} - T_{gv}^{(1)} \\
T_{xyyy} &= T_{dxy}^{(1)} + 2T_{dxy}^{(2)} - T_{dxy}^{(3)} - T_{gbz}^{(1)}
\end{aligned}$$