

SG No. 227 O_h^7 $Fd\bar{3}m$ [cubic]

* generator : $\{2_{001}|\frac{3}{4}\frac{1}{4}\frac{1}{2}\}$, $\{2_{010}|\frac{1}{4}\frac{1}{2}\frac{3}{4}\}$, $\{3_{111}^+|0\}$, $\{2_{110}|\frac{3}{4}\frac{1}{4}\frac{1}{2}\}$, $\{-1|0\}$

* symmetry operation $+ [0, 0, 0]$, $+ [0, \frac{1}{2}, \frac{1}{2}]$, $+ [\frac{1}{2}, 0, \frac{1}{2}]$, $+ [\frac{1}{2}, \frac{1}{2}, 0]$

Table 1: Symmetry operations for 3d polar vector.

| No. | tag | matrix (polar) | det |
|-----|---|---|-----|
| 1 | $\{1 0\}$ | $\begin{bmatrix} 1 & 0 & 0 & 0 \\ 0 & 1 & 0 & 0 \\ 0 & 0 & 1 & 0 \end{bmatrix}$ | 1 |
| 2 | $\{2_{001} \frac{3}{4}\frac{1}{4}\frac{1}{2}\}$ | $\begin{bmatrix} -1 & 0 & 0 & \frac{3}{4} \\ 0 & -1 & 0 & \frac{1}{4} \\ 0 & 0 & 1 & \frac{1}{2} \end{bmatrix}$ | 1 |
| 3 | $\{2_{010} \frac{1}{4}\frac{1}{2}\frac{3}{4}\}$ | $\begin{bmatrix} -1 & 0 & 0 & \frac{1}{4} \\ 0 & 1 & 0 & \frac{1}{2} \\ 0 & 0 & -1 & \frac{3}{4} \end{bmatrix}$ | 1 |
| 4 | $\{2_{100} \frac{1}{2}\frac{3}{4}\frac{1}{4}\}$ | $\begin{bmatrix} 1 & 0 & 0 & \frac{1}{2} \\ 0 & -1 & 0 & \frac{3}{4} \\ 0 & 0 & -1 & \frac{1}{4} \end{bmatrix}$ | 1 |
| 5 | $\{3_{111}^+ 0\}$ | $\begin{bmatrix} 0 & 0 & 1 & 0 \\ 1 & 0 & 0 & 0 \\ 0 & 1 & 0 & 0 \end{bmatrix}$ | 1 |
| 6 | $\{3_{-11-1}^+ \frac{1}{2}\frac{3}{4}\frac{1}{4}\}$ | $\begin{bmatrix} 0 & 0 & 1 & \frac{1}{2} \\ -1 & 0 & 0 & \frac{3}{4} \\ 0 & -1 & 0 & \frac{1}{4} \end{bmatrix}$ | 1 |
| 7 | $\{3_{1-1-1}^+ \frac{3}{4}\frac{1}{4}\frac{1}{2}\}$ | $\begin{bmatrix} 0 & 0 & -1 & \frac{3}{4} \\ -1 & 0 & 0 & \frac{1}{4} \\ 0 & 1 & 0 & \frac{1}{2} \end{bmatrix}$ | 1 |
| 8 | $\{3_{-1-11}^+ \frac{1}{4}\frac{1}{2}\frac{3}{4}\}$ | $\begin{bmatrix} 0 & 0 & -1 & \frac{1}{4} \\ 1 & 0 & 0 & \frac{1}{2} \\ 0 & -1 & 0 & \frac{3}{4} \end{bmatrix}$ | 1 |
| 9 | $\{3_{111}^- 0\}$ | $\begin{bmatrix} 0 & 1 & 0 & 0 \\ 0 & 0 & 1 & 0 \\ 1 & 0 & 0 & 0 \end{bmatrix}$ | 1 |
| 10 | $\{3_{1-1-1}^- \frac{1}{4}\frac{1}{2}\frac{3}{4}\}$ | $\begin{bmatrix} 0 & -1 & 0 & \frac{1}{4} \\ 0 & 0 & 1 & \frac{1}{2} \\ -1 & 0 & 0 & \frac{3}{4} \end{bmatrix}$ | 1 |
| 11 | $\{3_{-1-11}^- \frac{1}{2}\frac{3}{4}\frac{1}{4}\}$ | $\begin{bmatrix} 0 & 1 & 0 & \frac{1}{2} \\ 0 & 0 & -1 & \frac{3}{4} \\ -1 & 0 & 0 & \frac{1}{4} \end{bmatrix}$ | 1 |
| 12 | $\{3_{-11-1}^- \frac{3}{4}\frac{1}{4}\frac{1}{2}\}$ | $\begin{bmatrix} 0 & -1 & 0 & \frac{3}{4} \\ 0 & 0 & -1 & \frac{1}{4} \\ 1 & 0 & 0 & \frac{1}{2} \end{bmatrix}$ | 1 |
| 13 | $\{2_{110} \frac{3}{4}\frac{1}{4}\frac{1}{2}\}$ | $\begin{bmatrix} 0 & 1 & 0 & \frac{3}{4} \\ 1 & 0 & 0 & \frac{1}{4} \\ 0 & 0 & -1 & \frac{1}{2} \end{bmatrix}$ | 1 |

continued ...

Table 1

| No. | tag | matrix (polar) | det |
|-----|--|--|-----|
| 14 | $\{2_{1-10} 0\rangle\}$ | $\begin{bmatrix} 0 & -1 & 0 & 0 \\ -1 & 0 & 0 & 0 \\ 0 & 0 & -1 & 0 \end{bmatrix}$ | 1 |
| 15 | $\{4_{001}^{-} \frac{1}{4}\frac{1}{2}\frac{3}{4}\rangle\}$ | $\begin{bmatrix} 0 & 1 & 0 & \frac{1}{4} \\ -1 & 0 & 0 & \frac{1}{2} \\ 0 & 0 & 1 & \frac{3}{4} \end{bmatrix}$ | 1 |
| 16 | $\{4_{001}^{+} \frac{1}{2}\frac{3}{4}\frac{1}{4}\rangle\}$ | $\begin{bmatrix} 0 & -1 & 0 & \frac{1}{2} \\ 1 & 0 & 0 & \frac{3}{4} \\ 0 & 0 & 1 & \frac{1}{4} \end{bmatrix}$ | 1 |
| 17 | $\{4_{100}^{-} \frac{3}{4}\frac{1}{4}\frac{1}{2}\rangle\}$ | $\begin{bmatrix} 1 & 0 & 0 & \frac{3}{4} \\ 0 & 0 & 1 & \frac{1}{4} \\ 0 & -1 & 0 & \frac{1}{2} \end{bmatrix}$ | 1 |
| 18 | $\{2_{011} \frac{1}{2}\frac{3}{4}\frac{1}{4}\rangle\}$ | $\begin{bmatrix} -1 & 0 & 0 & \frac{1}{2} \\ 0 & 0 & 1 & \frac{3}{4} \\ 0 & 1 & 0 & \frac{1}{4} \end{bmatrix}$ | 1 |
| 19 | $\{2_{01-1} 0\rangle\}$ | $\begin{bmatrix} -1 & 0 & 0 & 0 \\ 0 & 0 & -1 & 0 \\ 0 & -1 & 0 & 0 \end{bmatrix}$ | 1 |
| 20 | $\{4_{100}^{+} \frac{1}{4}\frac{1}{2}\frac{3}{4}\rangle\}$ | $\begin{bmatrix} 1 & 0 & 0 & \frac{1}{4} \\ 0 & 0 & -1 & \frac{1}{2} \\ 0 & 1 & 0 & \frac{3}{4} \end{bmatrix}$ | 1 |
| 21 | $\{4_{010}^{+} \frac{3}{4}\frac{1}{4}\frac{1}{2}\rangle\}$ | $\begin{bmatrix} 0 & 0 & 1 & \frac{3}{4} \\ 0 & 1 & 0 & \frac{1}{4} \\ -1 & 0 & 0 & \frac{1}{2} \end{bmatrix}$ | 1 |
| 22 | $\{2_{101} \frac{1}{4}\frac{1}{2}\frac{3}{4}\rangle\}$ | $\begin{bmatrix} 0 & 0 & 1 & \frac{1}{4} \\ 0 & -1 & 0 & \frac{1}{2} \\ 1 & 0 & 0 & \frac{3}{4} \end{bmatrix}$ | 1 |
| 23 | $\{4_{010}^{-} \frac{1}{2}\frac{3}{4}\frac{1}{4}\rangle\}$ | $\begin{bmatrix} 0 & 0 & -1 & \frac{1}{2} \\ 0 & 1 & 0 & \frac{3}{4} \\ 1 & 0 & 0 & \frac{1}{4} \end{bmatrix}$ | 1 |
| 24 | $\{2_{-101} 0\rangle\}$ | $\begin{bmatrix} 0 & 0 & -1 & 0 \\ 0 & -1 & 0 & 0 \\ -1 & 0 & 0 & 0 \end{bmatrix}$ | 1 |
| 25 | $\{-1 0\rangle\}$ | $\begin{bmatrix} -1 & 0 & 0 & 0 \\ 0 & -1 & 0 & 0 \\ 0 & 0 & -1 & 0 \end{bmatrix}$ | -1 |
| 26 | $\{m_{001} \frac{1}{4}\frac{3}{4}\frac{1}{2}\rangle\}$ | $\begin{bmatrix} 1 & 0 & 0 & \frac{1}{4} \\ 0 & 1 & 0 & \frac{3}{4} \\ 0 & 0 & -1 & \frac{1}{2} \end{bmatrix}$ | -1 |
| 27 | $\{m_{010} \frac{3}{4}\frac{1}{2}\frac{1}{4}\rangle\}$ | $\begin{bmatrix} 1 & 0 & 0 & \frac{3}{4} \\ 0 & -1 & 0 & \frac{1}{2} \\ 0 & 0 & 1 & \frac{1}{4} \end{bmatrix}$ | -1 |

continued ...

Table 1

| No. | tag | matrix (polar) | det |
|-----|--|---|-----|
| 28 | $\{m_{100} \frac{1}{2}\frac{1}{4}\frac{3}{4}\}$ | $\begin{bmatrix} -1 & 0 & 0 & \frac{1}{2} \\ 0 & 1 & 0 & \frac{1}{4} \\ 0 & 0 & 1 & \frac{3}{4} \end{bmatrix}$ | -1 |
| 29 | $\{-3_{111}^+ 0\}$ | $\begin{bmatrix} 0 & 0 & -1 & 0 \\ -1 & 0 & 0 & 0 \\ 0 & -1 & 0 & 0 \end{bmatrix}$ | -1 |
| 30 | $\{-3_{-11-1}^+ \frac{1}{2}\frac{1}{4}\frac{3}{4}\}$ | $\begin{bmatrix} 0 & 0 & -1 & \frac{1}{2} \\ 1 & 0 & 0 & \frac{1}{4} \\ 0 & 1 & 0 & \frac{3}{4} \end{bmatrix}$ | -1 |
| 31 | $\{-3_{1-1-1}^+ \frac{1}{4}\frac{3}{4}\frac{1}{2}\}$ | $\begin{bmatrix} 0 & 0 & 1 & \frac{1}{4} \\ 1 & 0 & 0 & \frac{3}{4} \\ 0 & -1 & 0 & \frac{1}{2} \end{bmatrix}$ | -1 |
| 32 | $\{-3_{-1-11}^+ \frac{3}{4}\frac{1}{2}\frac{1}{4}\}$ | $\begin{bmatrix} 0 & 0 & 1 & \frac{3}{4} \\ -1 & 0 & 0 & \frac{1}{2} \\ 0 & 1 & 0 & \frac{1}{4} \end{bmatrix}$ | -1 |
| 33 | $\{-3_{111}^- 0\}$ | $\begin{bmatrix} 0 & -1 & 0 & 0 \\ 0 & 0 & -1 & 0 \\ -1 & 0 & 0 & 0 \end{bmatrix}$ | -1 |
| 34 | $\{-3_{1-1-1}^- \frac{3}{4}\frac{1}{2}\frac{1}{4}\}$ | $\begin{bmatrix} 0 & 1 & 0 & \frac{3}{4} \\ 0 & 0 & -1 & \frac{1}{2} \\ 1 & 0 & 0 & \frac{1}{4} \end{bmatrix}$ | -1 |
| 35 | $\{-3_{-1-11}^- \frac{1}{2}\frac{1}{4}\frac{3}{4}\}$ | $\begin{bmatrix} 0 & -1 & 0 & \frac{1}{2} \\ 0 & 0 & 1 & \frac{1}{4} \\ 1 & 0 & 0 & \frac{3}{4} \end{bmatrix}$ | -1 |
| 36 | $\{-3_{-11-1}^- \frac{1}{4}\frac{3}{4}\frac{1}{2}\}$ | $\begin{bmatrix} 0 & 1 & 0 & \frac{1}{4} \\ 0 & 0 & 1 & \frac{3}{4} \\ -1 & 0 & 0 & \frac{1}{2} \end{bmatrix}$ | -1 |
| 37 | $\{m_{110} \frac{1}{4}\frac{3}{4}\frac{1}{2}\}$ | $\begin{bmatrix} 0 & -1 & 0 & \frac{1}{4} \\ -1 & 0 & 0 & \frac{3}{4} \\ 0 & 0 & 1 & \frac{1}{2} \end{bmatrix}$ | -1 |
| 38 | $\{m_{1-10} 0\}$ | $\begin{bmatrix} 0 & 1 & 0 & 0 \\ 1 & 0 & 0 & 0 \\ 0 & 0 & 1 & 0 \end{bmatrix}$ | -1 |
| 39 | $\{-4_{001}^- \frac{3}{4}\frac{1}{2}\frac{1}{4}\}$ | $\begin{bmatrix} 0 & -1 & 0 & \frac{3}{4} \\ 1 & 0 & 0 & \frac{1}{2} \\ 0 & 0 & -1 & \frac{1}{4} \end{bmatrix}$ | -1 |
| 40 | $\{-4_{001}^+ \frac{1}{2}\frac{1}{4}\frac{3}{4}\}$ | $\begin{bmatrix} 0 & 1 & 0 & \frac{1}{2} \\ -1 & 0 & 0 & \frac{1}{4} \\ 0 & 0 & -1 & \frac{3}{4} \end{bmatrix}$ | -1 |
| 41 | $\{-4_{100}^- \frac{1}{4}\frac{3}{4}\frac{1}{2}\}$ | $\begin{bmatrix} -1 & 0 & 0 & \frac{1}{4} \\ 0 & 0 & -1 & \frac{3}{4} \\ 0 & 1 & 0 & \frac{1}{2} \end{bmatrix}$ | -1 |

continued ...

Table 1

| No. | tag | matrix (polar) | det |
|-----|--|---|-----|
| 42 | $\{m_{011} \frac{1}{2}\frac{1}{4}\frac{3}{4}\}$ | $\begin{bmatrix} 1 & 0 & 0 & \frac{1}{2} \\ 0 & 0 & -1 & \frac{1}{4} \\ 0 & -1 & 0 & \frac{3}{4} \end{bmatrix}$ | -1 |
| 43 | $\{m_{01-1} 0\}$ | $\begin{bmatrix} 1 & 0 & 0 & 0 \\ 0 & 0 & 1 & 0 \\ 0 & 1 & 0 & 0 \end{bmatrix}$ | -1 |
| 44 | $\{-4_{100}^+ \frac{3}{4}\frac{1}{2}\frac{1}{4}\}$ | $\begin{bmatrix} -1 & 0 & 0 & \frac{3}{4} \\ 0 & 0 & 1 & \frac{1}{2} \\ 0 & -1 & 0 & \frac{1}{4} \end{bmatrix}$ | -1 |
| 45 | $\{-4_{010}^+ \frac{1}{4}\frac{3}{4}\frac{1}{2}\}$ | $\begin{bmatrix} 0 & 0 & -1 & \frac{1}{4} \\ 0 & -1 & 0 & \frac{3}{4} \\ 1 & 0 & 0 & \frac{1}{2} \end{bmatrix}$ | -1 |
| 46 | $\{m_{101} \frac{3}{4}\frac{1}{2}\frac{1}{4}\}$ | $\begin{bmatrix} 0 & 0 & -1 & \frac{3}{4} \\ 0 & 1 & 0 & \frac{1}{2} \\ -1 & 0 & 0 & \frac{1}{4} \end{bmatrix}$ | -1 |
| 47 | $\{-4_{010}^- \frac{1}{2}\frac{1}{4}\frac{3}{4}\}$ | $\begin{bmatrix} 0 & 0 & 1 & \frac{1}{2} \\ 0 & -1 & 0 & \frac{1}{4} \\ -1 & 0 & 0 & \frac{3}{4} \end{bmatrix}$ | -1 |
| 48 | $\{m_{-101} 0\}$ | $\begin{bmatrix} 0 & 0 & 1 & 0 \\ 0 & 1 & 0 & 0 \\ 1 & 0 & 0 & 0 \end{bmatrix}$ | -1 |