

SAMB for “kappaET”

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- Group: No. 32 C_{2v}^8 $Pba2$ [orthorhombic]
 - Associated point group: No. 7 C_{2v} $mm2$ [orthorhombic]
 - Generation condition
 - model type: **tight_binding**
 - time-reversal type: **electric**
 - irrep: [A1]
 - **spinful**
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- Unit cell:
 $a = 1.0$, $b = 1.2$, $c = 1.0$, $\alpha = 90.0$, $\beta = 90.0$, $\gamma = 90.0$
- Lattice vectors:
 $\mathbf{a}_1 = (1.0 \ 0 \ 0)$
 $\mathbf{a}_2 = (0 \ 1.2 \ 0)$
 $\mathbf{a}_3 = (0 \ 0 \ 1.0)$

Table 1: High-symmetry line: Γ -X.

symbol	position	symbol	position
Γ	$\begin{pmatrix} 0 & 0 & 0 \end{pmatrix}$	X	$\begin{pmatrix} \frac{1}{2} & 0 & 0 \end{pmatrix}$

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- Kets: dimension = 8

Table 2: Hilbert space for full matrix.

No.	ket	No.	ket	No.	ket	No.	ket	No.	ket
1	$(s, \uparrow)@A_1$	2	$(s, \downarrow)@A_1$	3	$(s, \uparrow)@A_2$	4	$(s, \downarrow)@A_2$	5	$(s, \uparrow)@A_3$
6	$(s, \downarrow)@A_3$	7	$(s, \uparrow)@A_4$	8	$(s, \downarrow)@A_4$				

- Sites in (primitive) unit cell:

Table 3: Site-clusters.

	site	position	mapping
S ₁ [4c: 1]	A ₁	$\begin{pmatrix} \frac{9}{10} & \frac{1}{20} & 0 \end{pmatrix}$	[1]
	A ₂	$\begin{pmatrix} \frac{1}{10} & \frac{19}{20} & 0 \end{pmatrix}$	[2]
	A ₃	$\begin{pmatrix} \frac{2}{5} & \frac{9}{20} & 0 \end{pmatrix}$	[3]
	A ₄	$\begin{pmatrix} \frac{3}{5} & \frac{11}{20} & 0 \end{pmatrix}$	[4]

- Bonds in (primitive) unit cell:

Table 4: Bond-clusters.

	bond	tail	head	n	#	$\mathbf{b@c}$	mapping
B ₁ [2a: ..2]	b ₁	A ₂	A ₁	1	1	$\begin{pmatrix} \frac{1}{5} & -\frac{1}{10} & 0 \end{pmatrix} @ \begin{pmatrix} 0 & 0 & 0 \end{pmatrix}$	[1,-2]
	b ₂	A ₄	A ₃	1	1	$\begin{pmatrix} \frac{1}{5} & \frac{1}{10} & 0 \end{pmatrix} @ \begin{pmatrix} \frac{1}{2} & \frac{1}{2} & 0 \end{pmatrix}$	[3,-4]
B ₂ [4c: 1]	b ₃	A ₄	A ₁	2	1	$\begin{pmatrix} -\frac{3}{10} & \frac{1}{2} & 0 \end{pmatrix} @ \begin{pmatrix} \frac{3}{4} & \frac{3}{10} & 0 \end{pmatrix}$	[1]
	b ₄	A ₃	A ₂	2	1	$\begin{pmatrix} \frac{3}{10} & -\frac{1}{2} & 0 \end{pmatrix} @ \begin{pmatrix} \frac{1}{4} & \frac{7}{10} & 0 \end{pmatrix}$	[2]
	b ₅	A ₃	A ₂	2	1	$\begin{pmatrix} \frac{3}{10} & \frac{1}{2} & 0 \end{pmatrix} @ \begin{pmatrix} \frac{1}{4} & \frac{1}{5} & 0 \end{pmatrix}$	[-3]
	b ₆	A ₄	A ₁	2	1	$\begin{pmatrix} -\frac{3}{10} & -\frac{1}{2} & 0 \end{pmatrix} @ \begin{pmatrix} \frac{3}{4} & \frac{4}{5} & 0 \end{pmatrix}$	[-4]
B ₃ [4c: 1]	b ₇	A ₃	A ₁	3	1	$\begin{pmatrix} \frac{1}{2} & \frac{2}{5} & 0 \end{pmatrix} @ \begin{pmatrix} \frac{3}{20} & \frac{1}{4} & 0 \end{pmatrix}$	[1]

continued ...

Table 4

	bond	tail	head	n	#	$\mathbf{b@c}$	mapping
	$\mathbf{b_8}$	$\mathbf{A_4}$	$\mathbf{A_2}$	$\mathbf{3}$	$\mathbf{1}$	$\begin{pmatrix} -\frac{1}{2} & -\frac{2}{5} & 0 \end{pmatrix} @ \begin{pmatrix} \frac{17}{20} & \frac{3}{4} & 0 \end{pmatrix}$	[2]
	$\mathbf{b_9}$	$\mathbf{A_3}$	$\mathbf{A_1}$	$\mathbf{3}$	$\mathbf{1}$	$\begin{pmatrix} -\frac{1}{2} & \frac{2}{5} & 0 \end{pmatrix} @ \begin{pmatrix} \frac{13}{20} & \frac{1}{4} & 0 \end{pmatrix}$	[-3]
	$\mathbf{b_{10}}$	$\mathbf{A_4}$	$\mathbf{A_2}$	$\mathbf{3}$	$\mathbf{1}$	$\begin{pmatrix} \frac{1}{2} & -\frac{2}{5} & 0 \end{pmatrix} @ \begin{pmatrix} \frac{7}{20} & \frac{3}{4} & 0 \end{pmatrix}$	[-4]

- SAMB:

$$\boxed{\text{No. 1}} \quad \hat{\mathbb{Q}}_0^{(A_1)} [\mathbf{M}_1, \mathbf{S}_1]$$

$$\hat{\mathbb{Z}}_1 = \mathbb{X}_1[\mathbb{Q}_0^{(a, A_1)}] \otimes \mathbb{Y}_1[\mathbb{Q}_0^{(s, A_1)}]$$

$$\boxed{\text{No. 2}} \quad \hat{\mathbb{Q}}_0^{(A_1)} [\mathbf{M}_1, \mathbf{B}_1]$$

$$\hat{\mathbb{Z}}_2 = \mathbb{X}_1[\mathbb{Q}_0^{(a, A_1)}] \otimes \mathbb{Y}_2[\mathbb{Q}_0^{(b, A_1)}]$$

$$\boxed{\text{No. 3}} \quad \hat{\mathbb{Q}}_1^{(A_1)}(1, -1) [\mathbf{M}_1, \mathbf{B}_1]$$

$$\hat{\mathbb{Z}}_3 = -\frac{\sqrt{2}\mathbb{X}_3[\mathbb{M}_1^{(a, B_1)}(1, -1)] \otimes \mathbb{Y}_3[\mathbb{T}_1^{(b, B_1)}]}{2} + \frac{\sqrt{2}\mathbb{X}_4[\mathbb{M}_1^{(a, B_2)}(1, -1)] \otimes \mathbb{Y}_4[\mathbb{T}_1^{(b, B_2)}]}{2}$$

$$\boxed{\text{No. 4}} \quad \hat{\mathbb{G}}_2^{(A_1)}(1, -1) [\mathbf{M}_1, \mathbf{B}_1]$$

$$\hat{\mathbb{Z}}_4 = \frac{\sqrt{2}\mathbb{X}_3[\mathbb{M}_1^{(a, B_1)}(1, -1)] \otimes \mathbb{Y}_3[\mathbb{T}_1^{(b, B_1)}]}{2} + \frac{\sqrt{2}\mathbb{X}_4[\mathbb{M}_1^{(a, B_2)}(1, -1)] \otimes \mathbb{Y}_4[\mathbb{T}_1^{(b, B_2)}]}{2}$$

$$\boxed{\text{No. 5}} \quad \hat{\mathbb{Q}}_0^{(A_1)} [\mathbf{M}_1, \mathbf{B}_2]$$

$$\hat{\mathbb{Z}}_5 = \mathbb{X}_1[\mathbb{Q}_0^{(a, A_1)}] \otimes \mathbb{Y}_5[\mathbb{Q}_0^{(b, A_1)}]$$

$$\boxed{\text{No. 6}} \quad \hat{\mathbb{Q}}_1^{(A_1)}(1, -1) [\mathbf{M}_1, \mathbf{B}_2]$$

$$\hat{\mathbb{Z}}_6 = -\frac{\sqrt{2}\mathbb{X}_3[\mathbb{M}_1^{(a, B_1)}(1, -1)] \otimes \mathbb{Y}_6[\mathbb{T}_1^{(b, B_1)}]}{2} + \frac{\sqrt{2}\mathbb{X}_4[\mathbb{M}_1^{(a, B_2)}(1, -1)] \otimes \mathbb{Y}_7[\mathbb{T}_1^{(b, B_2)}]}{2}$$

$$\boxed{\text{No. 7}} \quad \hat{\mathbb{G}}_2^{(A_1)}(1, -1) [\text{M}_1, \text{B}_2]$$

$$\hat{\mathbb{Z}}_7 = \frac{\sqrt{2}\mathbb{X}_3[\mathbb{M}_1^{(a, B_1)}(1, -1)] \otimes \mathbb{Y}_6[\mathbb{T}_1^{(b, B_1)}]}{2} + \frac{\sqrt{2}\mathbb{X}_4[\mathbb{M}_1^{(a, B_2)}(1, -1)] \otimes \mathbb{Y}_7[\mathbb{T}_1^{(b, B_2)}]}{2}$$

$$\boxed{\text{No. 8}} \quad \hat{\mathbb{Q}}_2^{(A_1, 2)}(1, -1) [\text{M}_1, \text{B}_2]$$

$$\hat{\mathbb{Z}}_8 = -\mathbb{X}_2[\mathbb{M}_1^{(a, A_2)}(1, -1)] \otimes \mathbb{Y}_8[\mathbb{T}_2^{(b, A_2)}]$$

$$\boxed{\text{No. 9}} \quad \hat{\mathbb{Q}}_0^{(A_1)} [\text{M}_1, \text{B}_3]$$

$$\hat{\mathbb{Z}}_9 = \mathbb{X}_1[\mathbb{Q}_0^{(a, A_1)}] \otimes \mathbb{Y}_9[\mathbb{Q}_0^{(b, A_1)}]$$

$$\boxed{\text{No. 10}} \quad \hat{\mathbb{Q}}_1^{(A_1)}(1, -1) [\text{M}_1, \text{B}_3]$$

$$\hat{\mathbb{Z}}_{10} = -\frac{\sqrt{2}\mathbb{X}_3[\mathbb{M}_1^{(a, B_1)}(1, -1)] \otimes \mathbb{Y}_{10}[\mathbb{T}_1^{(b, B_1)}]}{2} + \frac{\sqrt{2}\mathbb{X}_4[\mathbb{M}_1^{(a, B_2)}(1, -1)] \otimes \mathbb{Y}_{11}[\mathbb{T}_1^{(b, B_2)}]}{2}$$

$$\boxed{\text{No. 11}} \quad \hat{\mathbb{G}}_2^{(A_1)}(1, -1) [\text{M}_1, \text{B}_3]$$

$$\hat{\mathbb{Z}}_{11} = \frac{\sqrt{2}\mathbb{X}_3[\mathbb{M}_1^{(a, B_1)}(1, -1)] \otimes \mathbb{Y}_{10}[\mathbb{T}_1^{(b, B_1)}]}{2} + \frac{\sqrt{2}\mathbb{X}_4[\mathbb{M}_1^{(a, B_2)}(1, -1)] \otimes \mathbb{Y}_{11}[\mathbb{T}_1^{(b, B_2)}]}{2}$$

$$\boxed{\text{No. 12}} \quad \hat{\mathbb{Q}}_2^{(A_1, 2)}(1, -1) [\text{M}_1, \text{B}_3]$$

$$\hat{\mathbb{Z}}_{12} = -\mathbb{X}_2[\mathbb{M}_1^{(a, A_2)}(1, -1)] \otimes \mathbb{Y}_{12}[\mathbb{T}_2^{(b, A_2)}]$$

Table 5: Atomic SAMB group.

group	bra	ket
M_1	$(s, \uparrow), (s, \downarrow)$	$(s, \uparrow), (s, \downarrow)$

Table 6: Atomic SAMB.

symbol	type	group	form
\mathbb{X}_1	$\mathbb{Q}_0^{(a, A_1)}$	M_1	$\begin{pmatrix} \frac{\sqrt{2}}{2} & 0 \\ 0 & \frac{\sqrt{2}}{2} \end{pmatrix}$
\mathbb{X}_2	$\mathbb{M}_1^{(a, A_2)}(1, -1)$	M_1	$\begin{pmatrix} \frac{\sqrt{2}}{2} & 0 \\ 0 & -\frac{\sqrt{2}}{2} \end{pmatrix}$
\mathbb{X}_3	$\mathbb{M}_1^{(a, B_1)}(1, -1)$	M_1	$\begin{pmatrix} 0 & -\frac{\sqrt{2}i}{2} \\ \frac{\sqrt{2}i}{2} & 0 \end{pmatrix}$
\mathbb{X}_4	$\mathbb{M}_1^{(a, B_2)}(1, -1)$	M_1	$\begin{pmatrix} 0 & \frac{\sqrt{2}}{2} \\ \frac{\sqrt{2}}{2} & 0 \end{pmatrix}$

Table 7: Cluster SAMB.

symbol	type	cluster	form
\mathbb{Y}_1	$\mathbb{Q}_0^{(s, A_1)}$	S_1	$\begin{pmatrix} \frac{1}{2} & \frac{1}{2} & \frac{1}{2} & \frac{1}{2} \end{pmatrix}$
\mathbb{Y}_2	$\mathbb{Q}_0^{(b, A_1)}$	B_1	$\begin{pmatrix} \frac{\sqrt{2}}{2} & \frac{\sqrt{2}}{2} \end{pmatrix}$
\mathbb{Y}_3	$\mathbb{T}_1^{(b, B_1)}$	B_1	$\begin{pmatrix} \frac{\sqrt{2}i}{2} & \frac{\sqrt{2}i}{2} \end{pmatrix}$
\mathbb{Y}_4	$\mathbb{T}_1^{(b, B_2)}$	B_1	$\begin{pmatrix} \frac{\sqrt{2}i}{2} & -\frac{\sqrt{2}i}{2} \end{pmatrix}$
\mathbb{Y}_5	$\mathbb{Q}_0^{(b, A_1)}$	B_2	$\begin{pmatrix} \frac{1}{2} & \frac{1}{2} & \frac{1}{2} & \frac{1}{2} \end{pmatrix}$
\mathbb{Y}_6	$\mathbb{T}_1^{(b, B_1)}$	B_2	$\begin{pmatrix} \frac{i}{2} & -\frac{i}{2} & -\frac{i}{2} & \frac{i}{2} \end{pmatrix}$
\mathbb{Y}_7	$\mathbb{T}_1^{(b, B_2)}$	B_2	$\begin{pmatrix} \frac{i}{2} & -\frac{i}{2} & \frac{i}{2} & -\frac{i}{2} \end{pmatrix}$
\mathbb{Y}_8	$\mathbb{T}_2^{(b, A_2)}$	B_2	$\begin{pmatrix} \frac{i}{2} & \frac{i}{2} & \frac{i}{2} & \frac{i}{2} \end{pmatrix}$
\mathbb{Y}_9	$\mathbb{Q}_0^{(b, A_1)}$	B_3	$\begin{pmatrix} \frac{1}{2} & \frac{1}{2} & \frac{1}{2} & \frac{1}{2} \end{pmatrix}$
\mathbb{Y}_{10}	$\mathbb{T}_1^{(b, B_1)}$	B_3	$\begin{pmatrix} \frac{i}{2} & -\frac{i}{2} & -\frac{i}{2} & \frac{i}{2} \end{pmatrix}$
\mathbb{Y}_{11}	$\mathbb{T}_1^{(b, B_2)}$	B_3	$\begin{pmatrix} \frac{i}{2} & -\frac{i}{2} & \frac{i}{2} & -\frac{i}{2} \end{pmatrix}$
\mathbb{Y}_{12}	$\mathbb{T}_2^{(b, A_2)}$	B_3	$\begin{pmatrix} \frac{i}{2} & \frac{i}{2} & \frac{i}{2} & \frac{i}{2} \end{pmatrix}$

Table 8: Polar harmonics.

No.	symbol	rank	irrep.	mul.	comp.	form
1	$\mathbb{Q}_0^{(A_1)}$	0	A_1	—	—	1
2	$\mathbb{Q}_1^{(B_1)}$	1	B_1	—	—	x
3	$\mathbb{Q}_1^{(B_2)}$	1	B_2	—	—	y
4	$\mathbb{Q}_2^{(A_2)}$	2	A_2	—	—	$\sqrt{3}xy$

Table 9: Axial harmonics.

No.	symbol	rank	irrep.	mul.	comp.	form
1	$\mathbb{G}_1^{(A_2)}$	1	A_2	—	—	Z
2	$\mathbb{G}_1^{(B_1)}$	1	B_1	—	—	Y
3	$\mathbb{G}_1^{(B_2)}$	1	B_2	—	—	X

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- Group info.: Generator = $\{2_{001}|0\}$, $\{m_{010}|\frac{1}{2}\frac{1}{2}0\}$

Table 10: Conjugacy class (point-group part).

rep. SO	symmetry operations
$\{1 0\}$	$\{1 0\}$
$\{2_{001} 0\}$	$\{2_{001} 0\}$
$\{m_{010} \frac{1}{2}\frac{1}{2}0\}$	$\{m_{010} \frac{1}{2}\frac{1}{2}0\}$
$\{m_{100} \frac{1}{2}\frac{1}{2}0\}$	$\{m_{100} \frac{1}{2}\frac{1}{2}0\}$

Table 11: Symmetry operations.

	No.	SO	No.	SO	No.	SO	No.	SO	No.	SO
	1	$\{1 0\}$	2	$\{2_{001} 0\}$	3	$\{m_{010} \frac{1}{2}\frac{1}{2}0\}$	4	$\{m_{100} \frac{1}{2}\frac{1}{2}0\}$		

Table 12: Character table (point-group part).

	1	2_{001}	m_{010}	m_{100}
A_1	1	1	1	1
A_2	1	1	-1	-1
B_1	1	-1	1	-1
B_2	1	-1	-1	1

Table 13: Parity conversion.

\leftrightarrow	\leftrightarrow	\leftrightarrow	\leftrightarrow
$A_1 (A_2)$	$B_2 (B_1)$	$B_1 (B_2)$	$A_2 (A_1)$

Table 14: Symmetric product, $[\Gamma \otimes \Gamma']_+$.

	A_1	A_2	B_1	B_2
A_1	A_1	A_2	B_1	B_2
A_2		A_1	B_2	B_1
B_1			A_1	A_2
B_2				A_1

Table 15: Anti-symmetric product, $[\Gamma \otimes \Gamma]_-$.

A_1	A_2	B_1	B_2
—	—	—	—

Table 16: Virtual-cluster sites.

No.	position	No.	position	No.	position	No.	position
1	$\begin{pmatrix} 1 & 1 & 0 \end{pmatrix}$	2	$\begin{pmatrix} -1 & -1 & 0 \end{pmatrix}$	3	$\begin{pmatrix} 1 & -1 & 0 \end{pmatrix}$	4	$\begin{pmatrix} -1 & 1 & 0 \end{pmatrix}$

Table 17: Virtual-cluster basis.

symbol	1	2	3	4
$Q_0^{(A1)}$	$\frac{1}{2}$	$\frac{1}{2}$	$\frac{1}{2}$	$\frac{1}{2}$
$Q_1^{(B1)}$	$\frac{1}{2}$	$-\frac{1}{2}$	$\frac{1}{2}$	$-\frac{1}{2}$
$Q_1^{(B2)}$	$\frac{1}{2}$	$-\frac{1}{2}$	$-\frac{1}{2}$	$\frac{1}{2}$
$Q_2^{(A2)}$	$\frac{1}{2}$	$\frac{1}{2}$	$-\frac{1}{2}$	$-\frac{1}{2}$