

\* symmetry operation

Table 1: Symmetry operations for 3d polar vector.

| No. | tag          | matrix (polar)   | det | TR |
|-----|--------------|--|-----|----|
| 1   | 1            | $\begin{bmatrix} 1 & 0 & 0 \\ 0 & 1 & 0 \\ 0 & 0 & 1 \end{bmatrix}$    | 1   | 1  |
| 2   | $m_{100}$    | $\begin{bmatrix} -1 & 0 & 0 \\ 0 & 1 & 0 \\ 0 & 0 & 1 \end{bmatrix}$   | -1  | 1  |
| 3   | $m_{010}$    | $\begin{bmatrix} 1 & 0 & 0 \\ 0 & -1 & 0 \\ 0 & 0 & 1 \end{bmatrix}$   | -1  | 1  |
| 4   | $2_{001}$    | $\begin{bmatrix} -1 & 0 & 0 \\ 0 & -1 & 0 \\ 0 & 0 & 1 \end{bmatrix}$  | 1   | 1  |
| 5   | $2_{1-10}$   | $\begin{bmatrix} 0 & -1 & 0 \\ -1 & 0 & 0 \\ 0 & 0 & -1 \end{bmatrix}$ | 1   | 1  |
| 6   | $-4_{001}^+$ | $\begin{bmatrix} 0 & 1 & 0 \\ -1 & 0 & 0 \\ 0 & 0 & -1 \end{bmatrix}$  | -1  | 1  |
| 7   | $-4_{001}^-$ | $\begin{bmatrix} 0 & -1 & 0 \\ 1 & 0 & 0 \\ 0 & 0 & -1 \end{bmatrix}$  | -1  | 1  |
| 8   | $2_{110}$    | $\begin{bmatrix} 0 & 1 & 0 \\ 1 & 0 & 0 \\ 0 & 0 & -1 \end{bmatrix}$   | 1   | 1  |