

MSG No. 166.97 $R\bar{3}m$ [Type I, trigonal]

Table 1: Wyckoff site: 3a, site symmetry: -3m.

| No. | position | mapping |
|-----|---|---------------------------------------|
| 1 | [0, 0, 0] | [1,2,3,4,5,6,7,8,9,10,11,12] |
| 2 | $[\frac{2}{3}, \frac{1}{3}, \frac{1}{3}]$ | [13,14,15,16,17,18,19,20,21,22,23,24] |
| 3 | $[\frac{1}{3}, \frac{2}{3}, \frac{2}{3}]$ | [25,26,27,28,29,30,31,32,33,34,35,36] |

Table 2: Wyckoff site: 3b, site symmetry: -3m.

| No. | position | mapping |
|-----|---|---------------------------------------|
| 1 | $[0, 0, \frac{1}{2}]$ | [1,2,3,4,5,6,7,8,9,10,11,12] |
| 2 | $[\frac{2}{3}, \frac{1}{3}, \frac{5}{6}]$ | [13,14,15,16,17,18,19,20,21,22,23,24] |
| 3 | $[\frac{1}{3}, \frac{2}{3}, \frac{1}{6}]$ | [25,26,27,28,29,30,31,32,33,34,35,36] |

Table 3: Wyckoff site: 6c, site symmetry: 3m.

| No. | position | mapping |
|-----|---|---------------------|
| 1 | $[0, 0, z]$ | [1,2,3,10,11,12] |
| 2 | $[0, 0, -z]$ | [4,5,6,7,8,9] |
| 3 | $[\frac{2}{3}, \frac{1}{3}, z + \frac{1}{3}]$ | [13,14,15,22,23,24] |
| 4 | $[\frac{2}{3}, \frac{1}{3}, \frac{1}{3} - z]$ | [16,17,18,19,20,21] |
| 5 | $[\frac{1}{3}, \frac{2}{3}, z + \frac{2}{3}]$ | [25,26,27,34,35,36] |
| 6 | $[\frac{1}{3}, \frac{2}{3}, \frac{2}{3} - z]$ | [28,29,30,31,32,33] |

Table 4: Wyckoff site: 9d, site symmetry: .2/m.

| No. | position | mapping |
|-----|---|---------------|
| 1 | $[\frac{1}{2}, 0, \frac{1}{2}]$ | [1,4,7,10] |
| 2 | $[0, \frac{1}{2}, \frac{1}{2}]$ | [2,5,8,11] |
| 3 | $[\frac{1}{2}, \frac{1}{2}, \frac{1}{2}]$ | [3,6,9,12] |
| 4 | $[\frac{1}{6}, \frac{1}{3}, \frac{5}{6}]$ | [13,16,19,22] |
| 5 | $[\frac{2}{3}, \frac{5}{6}, \frac{5}{6}]$ | [14,17,20,23] |
| 6 | $[\frac{1}{6}, \frac{5}{6}, \frac{5}{6}]$ | [15,18,21,24] |
| 7 | $[\frac{5}{6}, \frac{2}{3}, \frac{1}{6}]$ | [25,28,31,34] |
| 8 | $[\frac{1}{3}, \frac{1}{6}, \frac{1}{6}]$ | [26,29,32,35] |
| 9 | $[\frac{5}{6}, \frac{1}{6}, \frac{1}{6}]$ | [27,30,33,36] |

Table 5: Wyckoff site: 9e, site symmetry: .2/m.

| No. | position | mapping |
|-----|---|---------------|
| 1 | $[\frac{1}{2}, 0, 0]$ | [1,4,7,10] |
| 2 | $[0, \frac{1}{2}, 0]$ | [2,5,8,11] |
| 3 | $[\frac{1}{2}, \frac{1}{2}, 0]$ | [3,6,9,12] |
| 4 | $[\frac{1}{6}, \frac{1}{3}, \frac{1}{3}]$ | [13,16,19,22] |
| 5 | $[\frac{2}{3}, \frac{5}{6}, \frac{1}{3}]$ | [14,17,20,23] |
| 6 | $[\frac{1}{6}, \frac{5}{6}, \frac{1}{3}]$ | [15,18,21,24] |
| 7 | $[\frac{5}{6}, \frac{2}{3}, \frac{2}{3}]$ | [25,28,31,34] |
| 8 | $[\frac{1}{3}, \frac{1}{6}, \frac{2}{3}]$ | [26,29,32,35] |
| 9 | $[\frac{5}{6}, \frac{1}{6}, \frac{2}{3}]$ | [27,30,33,36] |

Table 6: Wyckoff site: 18f, site symmetry: .2.

| No. | position | mapping |
|-----|---|---------|
| 1 | $[x, 0, 0]$ | [1,4] |
| 2 | $[0, x, 0]$ | [2,5] |
| 3 | $[-x, -x, 0]$ | [3,6] |
| 4 | $[-x, 0, 0]$ | [7,10] |
| 5 | $[0, -x, 0]$ | [8,11] |
| 6 | $[x, x, 0]$ | [9,12] |
| 7 | $[x + \frac{2}{3}, \frac{1}{3}, \frac{1}{3}]$ | [13,16] |
| 8 | $[\frac{2}{3}, x + \frac{1}{3}, \frac{1}{3}]$ | [14,17] |
| 9 | $[\frac{2}{3} - x, \frac{1}{3} - x, \frac{1}{3}]$ | [15,18] |
| 10 | $[\frac{2}{3} - x, \frac{1}{3}, \frac{1}{3}]$ | [19,22] |
| 11 | $[\frac{2}{3}, \frac{1}{3} - x, \frac{1}{3}]$ | [20,23] |
| 12 | $[x + \frac{2}{3}, x + \frac{1}{3}, \frac{1}{3}]$ | [21,24] |
| 13 | $[x + \frac{1}{3}, \frac{2}{3}, \frac{2}{3}]$ | [25,28] |
| 14 | $[\frac{1}{3}, x + \frac{2}{3}, \frac{2}{3}]$ | [26,29] |
| 15 | $[\frac{1}{3} - x, \frac{2}{3} - x, \frac{2}{3}]$ | [27,30] |
| 16 | $[\frac{1}{3} - x, \frac{2}{3}, \frac{2}{3}]$ | [31,34] |
| 17 | $[\frac{1}{3}, \frac{2}{3} - x, \frac{2}{3}]$ | [32,35] |
| 18 | $[x + \frac{1}{3}, x + \frac{2}{3}, \frac{2}{3}]$ | [33,36] |

Table 7: Wyckoff site: 18g, site symmetry: .2.

| No. | position | mapping |
|-----|-------------------------|---------|
| 1 | $[x, 0, \frac{1}{2}]$ | [1,4] |
| 2 | $[0, x, \frac{1}{2}]$ | [2,5] |
| 3 | $[-x, -x, \frac{1}{2}]$ | [3,6] |
| 4 | $[-x, 0, \frac{1}{2}]$ | [7,10] |
| 5 | $[0, -x, \frac{1}{2}]$ | [8,11] |
| 6 | $[x, x, \frac{1}{2}]$ | [9,12] |

continued ...

Table 7

| No. | position | mapping |
|-----|---|---------|
| 7 | $[x + \frac{2}{3}, \frac{1}{3}, \frac{5}{6}]$ | [13,16] |
| 8 | $[\frac{2}{3}, x + \frac{1}{3}, \frac{5}{6}]$ | [14,17] |
| 9 | $[\frac{2}{3} - x, \frac{1}{3} - x, \frac{5}{6}]$ | [15,18] |
| 10 | $[\frac{2}{3} - x, \frac{1}{3}, \frac{5}{6}]$ | [19,22] |
| 11 | $[\frac{2}{3}, \frac{1}{3} - x, \frac{5}{6}]$ | [20,23] |
| 12 | $[x + \frac{2}{3}, x + \frac{1}{3}, \frac{5}{6}]$ | [21,24] |
| 13 | $[x + \frac{1}{3}, \frac{2}{3}, \frac{1}{6}]$ | [25,28] |
| 14 | $[\frac{1}{3}, x + \frac{2}{3}, \frac{1}{6}]$ | [26,29] |
| 15 | $[\frac{1}{3} - x, \frac{2}{3} - x, \frac{1}{6}]$ | [27,30] |
| 16 | $[\frac{1}{3} - x, \frac{2}{3}, \frac{1}{6}]$ | [31,34] |
| 17 | $[\frac{1}{3}, \frac{2}{3} - x, \frac{1}{6}]$ | [32,35] |
| 18 | $[x + \frac{1}{3}, x + \frac{2}{3}, \frac{1}{6}]$ | [33,36] |

Table 8: Wyckoff site: 18h, site symmetry: .m.

| No. | position | mapping |
|-----|--|---------|
| 1 | $[x, -x, z]$ | [1,11] |
| 2 | $[x, 2x, z]$ | [2,12] |
| 3 | $[-2x, -x, z]$ | [3,10] |
| 4 | $[2x, x, -z]$ | [4,9] |
| 5 | $[-x, x, -z]$ | [5,7] |
| 6 | $[-x, -2x, -z]$ | [6,8] |
| 7 | $[x + \frac{2}{3}, \frac{1}{3} - x, z + \frac{1}{3}]$ | [13,23] |
| 8 | $[x + \frac{2}{3}, 2x + \frac{1}{3}, z + \frac{1}{3}]$ | [14,24] |
| 9 | $[\frac{2}{3} - 2x, \frac{1}{3} - x, z + \frac{1}{3}]$ | [15,22] |
| 10 | $[2x + \frac{2}{3}, x + \frac{1}{3}, \frac{1}{3} - z]$ | [16,21] |
| 11 | $[\frac{2}{3} - x, x + \frac{1}{3}, \frac{1}{3} - z]$ | [17,19] |
| 12 | $[\frac{2}{3} - x, \frac{1}{3} - 2x, \frac{1}{3} - z]$ | [18,20] |
| 13 | $[x + \frac{1}{3}, \frac{2}{3} - x, z + \frac{2}{3}]$ | [25,35] |
| 14 | $[x + \frac{1}{3}, 2x + \frac{2}{3}, z + \frac{2}{3}]$ | [26,36] |
| 15 | $[\frac{1}{3} - 2x, \frac{2}{3} - x, z + \frac{2}{3}]$ | [27,34] |
| 16 | $[2x + \frac{1}{3}, x + \frac{2}{3}, \frac{2}{3} - z]$ | [28,33] |
| 17 | $[\frac{1}{3} - x, x + \frac{2}{3}, \frac{2}{3} - z]$ | [29,31] |
| 18 | $[\frac{1}{3} - x, \frac{2}{3} - 2x, \frac{2}{3} - z]$ | [30,32] |

Table 9: Wyckoff site: 36i, site symmetry: 1

| No. | position | mapping |
|-----|-------------------|---------|
| 1 | $[x, y, z]$ | [1] |
| 2 | $[-y, x - y, z]$ | [2] |
| 3 | $[-x + y, -x, z]$ | [3] |
| 4 | $[x - y, -y, -z]$ | [4] |

continued ...

Table 9

| No. | position | mapping |
|-----|--|---------|
| 5 | $[y, x, -z]$ | [5] |
| 6 | $[-x, -x + y, -z]$ | [6] |
| 7 | $[-x, -y, -z]$ | [7] |
| 8 | $[y, -x + y, -z]$ | [8] |
| 9 | $[x - y, x, -z]$ | [9] |
| 10 | $[-x + y, y, z]$ | [10] |
| 11 | $[-y, -x, z]$ | [11] |
| 12 | $[x, x - y, z]$ | [12] |
| 13 | $[x + \frac{2}{3}, y + \frac{1}{3}, z + \frac{1}{3}]$ | [13] |
| 14 | $[\frac{2}{3} - y, x - y + \frac{1}{3}, z + \frac{1}{3}]$ | [14] |
| 15 | $[-x + y + \frac{2}{3}, \frac{1}{3} - x, z + \frac{1}{3}]$ | [15] |
| 16 | $[x - y + \frac{2}{3}, \frac{1}{3} - y, \frac{1}{3} - z]$ | [16] |
| 17 | $[y + \frac{2}{3}, x + \frac{1}{3}, \frac{1}{3} - z]$ | [17] |
| 18 | $[\frac{2}{3} - x, -x + y + \frac{1}{3}, \frac{1}{3} - z]$ | [18] |
| 19 | $[\frac{2}{3} - x, \frac{1}{3} - y, \frac{1}{3} - z]$ | [19] |
| 20 | $[y + \frac{2}{3}, -x + y + \frac{1}{3}, \frac{1}{3} - z]$ | [20] |
| 21 | $[x - y + \frac{2}{3}, x + \frac{1}{3}, \frac{1}{3} - z]$ | [21] |
| 22 | $[-x + y + \frac{2}{3}, y + \frac{1}{3}, z + \frac{1}{3}]$ | [22] |
| 23 | $[\frac{2}{3} - y, \frac{1}{3} - x, z + \frac{1}{3}]$ | [23] |
| 24 | $[x + \frac{2}{3}, x - y + \frac{1}{3}, z + \frac{1}{3}]$ | [24] |
| 25 | $[x + \frac{1}{3}, y + \frac{2}{3}, z + \frac{2}{3}]$ | [25] |
| 26 | $[\frac{1}{3} - y, x - y + \frac{2}{3}, z + \frac{2}{3}]$ | [26] |
| 27 | $[-x + y + \frac{1}{3}, \frac{2}{3} - x, z + \frac{2}{3}]$ | [27] |
| 28 | $[x - y + \frac{1}{3}, \frac{2}{3} - y, \frac{2}{3} - z]$ | [28] |
| 29 | $[y + \frac{1}{3}, x + \frac{2}{3}, \frac{2}{3} - z]$ | [29] |
| 30 | $[\frac{1}{3} - x, -x + y + \frac{2}{3}, \frac{2}{3} - z]$ | [30] |
| 31 | $[\frac{1}{3} - x, \frac{2}{3} - y, \frac{2}{3} - z]$ | [31] |
| 32 | $[y + \frac{1}{3}, -x + y + \frac{2}{3}, \frac{2}{3} - z]$ | [32] |
| 33 | $[x - y + \frac{1}{3}, x + \frac{2}{3}, \frac{2}{3} - z]$ | [33] |
| 34 | $[-x + y + \frac{1}{3}, y + \frac{2}{3}, z + \frac{2}{3}]$ | [34] |
| 35 | $[\frac{1}{3} - y, \frac{2}{3} - x, z + \frac{2}{3}]$ | [35] |
| 36 | $[x + \frac{1}{3}, x - y + \frac{2}{3}, z + \frac{2}{3}]$ | [36] |