

PG No. 13  $C_{4v}$   $4mm$  [ tetragonal ] (polar, internal axial quadrupole)

\* Harmonics for rank 0

\* Harmonics for rank 1

$$\vec{Q}_1^{(2,1)}[g](A_1)$$

\*\* symmetry

$$z$$

\*\* expression

$$\frac{\sqrt{30}G_vxy}{5} - \frac{\sqrt{30}G_{xy}(x-y)(x+y)}{10} + \frac{\sqrt{30}G_{xz}yz}{10} - \frac{\sqrt{30}G_{yz}xz}{10}$$

$$\vec{Q}_{1,1}^{(2,1)}[g](E), \vec{Q}_{1,2}^{(2,1)}[g](E)$$

\*\* symmetry

$$x$$

$$y$$

\*\* expression

$$-\frac{3\sqrt{10}G_uyz}{10} - \frac{\sqrt{30}G_vyz}{10} + \frac{\sqrt{30}G_{xy}xz}{10} - \frac{\sqrt{30}G_{xz}xy}{10} - \frac{\sqrt{30}G_{yz}(y-z)(y+z)}{10}$$

$$\frac{3\sqrt{10}G_{uxz}}{10} - \frac{\sqrt{30}G_vxz}{10} - \frac{\sqrt{30}G_{xy}yz}{10} + \frac{\sqrt{30}G_{xz}(x-z)(x+z)}{10} + \frac{\sqrt{30}G_{yz}xy}{10}$$

\* Harmonics for rank 2

$$\vec{Q}_2^{(2,-1)}[g](A_1)$$

\*\* symmetry

$$-\frac{x^2}{2} - \frac{y^2}{2} + z^2$$

\*\* expression

$$\frac{\sqrt{2}G_{xz}y}{2} - \frac{\sqrt{2}G_{yz}x}{2}$$

$$\vec{Q}_2^{(2,1)}[g](A_1)$$

\*\* symmetry

$$-\frac{x^2}{2} - \frac{y^2}{2} + z^2$$

\*\* expression

$$\frac{5\sqrt{42}G_vxyz}{14} - \frac{5\sqrt{42}G_{xyz}(x-y)(x+y)}{28} - \frac{\sqrt{42}G_{xz}y(x^2+y^2-4z^2)}{28} + \frac{\sqrt{42}G_{yz}x(x^2+y^2-4z^2)}{28}$$

$$\vec{Q}_2^{(2,-1)}[g](B_1)$$

\*\* symmetry

$$\frac{\sqrt{3}(x-y)(x+y)}{2}$$

\*\* expression

$$\frac{\sqrt{6}G_{xyz}}{3} - \frac{\sqrt{6}G_{xz}y}{6} - \frac{\sqrt{6}G_{yz}x}{6}$$

$$\vec{Q}_2^{(2,1)}[g](B_1)$$

\*\* symmetry

$$\frac{\sqrt{3}(x-y)(x+y)}{2}$$

\*\* expression

$$-\frac{5\sqrt{42}G_uxyz}{14} + \frac{\sqrt{14}G_{xyz}(3x^2+3y^2-2z^2)}{28} - \frac{\sqrt{14}G_{xz}y(9x^2-y^2-6z^2)}{28} + \frac{\sqrt{14}G_{yz}x(x^2-9y^2+6z^2)}{28}$$

$$\vec{Q}_2^{(2,-1)}[g](B_2)$$

\*\* symmetry

$$\sqrt{3}xy$$

\*\* expression

$$-\frac{\sqrt{6}G_v z}{3} + \frac{\sqrt{6}G_{xz}x}{6} - \frac{\sqrt{6}G_{yz}y}{6}$$

$$\bar{\mathbb{Q}}_2^{(2,1)}[g](B_2)$$

\*\* symmetry

$$\sqrt{3}xy$$

\*\* expression

$$\frac{5\sqrt{42}G_u z (x-y)(x+y)}{28} - \frac{\sqrt{14}G_v z (3x^2 + 3y^2 - 2z^2)}{28} + \frac{\sqrt{14}G_{xz}x (2x^2 - 3y^2 - 3z^2)}{14} + \frac{\sqrt{14}G_{yz}y (3x^2 - 2y^2 + 3z^2)}{14}$$

$$\bar{\mathbb{Q}}_{2,1}^{(2,-1)}[g](E), \bar{\mathbb{Q}}_{2,2}^{(2,-1)}[g](E)$$

\*\* symmetry

$$\sqrt{3}xz$$

$$\sqrt{3}yz$$

\*\* expression

$$-\frac{\sqrt{2}G_u y}{2} + \frac{\sqrt{6}G_v y}{6} - \frac{\sqrt{6}G_{xy}x}{6} + \frac{\sqrt{6}G_{yz}z}{6}$$

$$\frac{\sqrt{2}G_u x}{2} + \frac{\sqrt{6}G_v x}{6} + \frac{\sqrt{6}G_{xy}y}{6} - \frac{\sqrt{6}G_{xz}z}{6}$$

$$\bar{\mathbb{Q}}_{2,1}^{(2,1)}[g](E), \bar{\mathbb{Q}}_{2,2}^{(2,1)}[g](E)$$

\*\* symmetry

$$\sqrt{3}xz$$

$$\sqrt{3}yz$$

\*\* expression

$$\begin{aligned} & \frac{\sqrt{42}G_u y (x^2 + y^2 - 4z^2)}{28} + \frac{\sqrt{14}G_v y (9x^2 - y^2 - 6z^2)}{28} - \frac{\sqrt{14}G_{xy}x (2x^2 - 3y^2 - 3z^2)}{14} - \frac{\sqrt{14}G_{yz}z (3x^2 + 3y^2 - 2z^2)}{14} \\ & - \frac{\sqrt{42}G_u x (x^2 + y^2 - 4z^2)}{28} - \frac{\sqrt{14}G_v x (x^2 - 9y^2 + 6z^2)}{28} - \frac{\sqrt{14}G_{xy}y (3x^2 - 2y^2 + 3z^2)}{14} + \frac{\sqrt{14}G_{xz}z (3x^2 + 3y^2 - 2z^2)}{14} \end{aligned}$$

\* Harmonics for rank 3

$$\bar{\mathbb{Q}}_3^{(2,-1)}[g](A_1)$$

\*\* symmetry

$$-\frac{z (3x^2 + 3y^2 - 2z^2)}{2}$$

\*\* expression

$$-\frac{\sqrt{30}G_v xy}{10} + \frac{\sqrt{30}G_{xy} (x-y)(x+y)}{20} + \frac{\sqrt{30}G_{xz}yz}{5} - \frac{\sqrt{30}G_{yz}xz}{5}$$

$$\bar{\mathbb{Q}}_3^{(2,1)}[g](A_1)$$

\*\* symmetry

$$-\frac{z (3x^2 + 3y^2 - 2z^2)}{2}$$

\*\* expression

$$-\frac{\sqrt{15}G_v xy (x^2 + y^2 - 6z^2)}{6} + \frac{\sqrt{15}G_{xy} (x-y)(x+y)(x^2 + y^2 - 6z^2)}{12} - \frac{\sqrt{15}G_{xz}yz (3x^2 + 3y^2 - 4z^2)}{12} + \frac{\sqrt{15}G_{yz}xz (3x^2 + 3y^2 - 4z^2)}{12}$$

$$\bar{\mathbb{Q}}_3^{(2,-1)}[g](B_1)$$

\*\* symmetry

$$\frac{\sqrt{15}z (x-y)(x+y)}{2}$$

\*\* expression

$$-\frac{\sqrt{6}G_u xy}{2} - \frac{\sqrt{2}G_{xy} (x^2 + y^2 - 2z^2)}{4}$$

$$\tilde{\mathbb{Q}}_3^{(2,1)}[g](B_1)$$

\*\* symmetry

$$\frac{\sqrt{15}z(x-y)(x+y)}{2}$$

\*\* expression

$$\frac{\sqrt{3}G_u xy(x^2+y^2-6z^2)}{3} + \frac{7G_v xy(x-y)(x+y)}{6} - \frac{G_{xy}(5x^4-18x^2y^2-12x^2z^2+5y^4-12y^2z^2+4z^4)}{12} \\ - \frac{7G_{xz}yz(3x^2+y^2-2z^2)}{12} - \frac{7G_{yz}xz(x^2+3y^2-2z^2)}{12}$$

$$\tilde{\mathbb{Q}}_3^{(2,-1)}[g](B_2)$$

\*\* symmetry

$$\sqrt{15}xyz$$

\*\* expression

$$\frac{\sqrt{6}G_u(x-y)(x+y)}{4} + \frac{\sqrt{2}G_v(x^2+y^2-2z^2)}{4}$$

$$\tilde{\mathbb{Q}}_3^{(2,1)}[g](B_2)$$

\*\* symmetry

$$\sqrt{15}xyz$$

\*\* expression

$$-\frac{\sqrt{3}G_u(x-y)(x+y)(x^2+y^2-6z^2)}{6} - \frac{G_v(x^4-12x^2y^2+6x^2z^2+y^4+6y^2z^2-2z^4)}{6} \\ - \frac{7G_{xy}xy(x-y)(x+y)}{6} + \frac{7G_{xz}xz(x-z)(x+z)}{6} - \frac{7G_{yz}yz(y-z)(y+z)}{6}$$

$$\tilde{\mathbb{Q}}_{3,1}^{(2,-1)}[g](E,1), \tilde{\mathbb{Q}}_{3,2}^{(2,-1)}[g](E,1)$$

\*\* symmetry

$$\frac{x(2x^2-3y^2-3z^2)}{2}$$

$$-\frac{y(3x^2-2y^2+3z^2)}{2}$$

\*\* expression

$$\frac{3\sqrt{10}G_u yz}{20} + \frac{\sqrt{30}G_v yz}{20} + \frac{\sqrt{30}G_{xy}xz}{5} - \frac{\sqrt{30}G_{xz}xy}{5} + \frac{\sqrt{30}G_{yz}(y-z)(y+z)}{20} \\ - \frac{3\sqrt{10}G_u xz}{20} + \frac{\sqrt{30}G_v xz}{20} - \frac{\sqrt{30}G_{xy}yz}{5} - \frac{\sqrt{30}G_{xz}(x-z)(x+z)}{20} + \frac{\sqrt{30}G_{yz}xy}{5}$$

$$\tilde{\mathbb{Q}}_{3,1}^{(2,-1)}[g](E,2), \tilde{\mathbb{Q}}_{3,2}^{(2,-1)}[g](E,2)$$

\*\* symmetry

$$\frac{\sqrt{15}x(y-z)(y+z)}{2}$$

$$\frac{\sqrt{15}y(x-z)(x+z)}{2}$$

\*\* expression

$$\frac{\sqrt{6}G_u yz}{4} - \frac{3\sqrt{2}G_v yz}{4} + \frac{\sqrt{2}G_{yz}(2x^2-y^2-z^2)}{4} \\ - \frac{\sqrt{6}G_u xz}{4} - \frac{3\sqrt{2}G_v xz}{4} + \frac{\sqrt{2}G_{xz}(x^2-2y^2+z^2)}{4}$$

$$\tilde{\mathbb{Q}}_{3,1}^{(2,1)}[g](E,1), \tilde{\mathbb{Q}}_{3,2}^{(2,1)}[g](E,1)$$

\*\* symmetry

$$\frac{x(2x^2-3y^2-3z^2)}{2}$$

$$-\frac{y(3x^2-2y^2+3z^2)}{2}$$

\*\* expression

$$\begin{aligned} & -\frac{\sqrt{5}G_u y z (6x^2 - y^2 - z^2)}{4} - \frac{\sqrt{15}G_v y z (6x^2 - y^2 - z^2)}{12} + \frac{\sqrt{15}G_{xy} x z (4x^2 - 3y^2 - 3z^2)}{12} \\ & - \frac{\sqrt{15}G_{xz} x y (4x^2 - 3y^2 - 3z^2)}{12} - \frac{\sqrt{15}G_{yz} (y - z) (y + z) (6x^2 - y^2 - z^2)}{12} \\ & - \frac{\sqrt{5}G_u x z (x^2 - 6y^2 + z^2)}{4} + \frac{\sqrt{15}G_v x z (x^2 - 6y^2 + z^2)}{12} + \frac{\sqrt{15}G_{xy} y z (3x^2 - 4y^2 + 3z^2)}{12} \\ & - \frac{\sqrt{15}G_{xz} (x - z) (x + z) (x^2 - 6y^2 + z^2)}{12} - \frac{\sqrt{15}G_{yz} x y (3x^2 - 4y^2 + 3z^2)}{12} \end{aligned}$$

$$\tilde{\mathbb{Q}}_{3,1}^{(2,1)}[g](E, 2), \tilde{\mathbb{Q}}_{3,2}^{(2,1)}[g](E, 2)$$

\*\* symmetry

$$\frac{\sqrt{15}x(y-z)(y+z)}{2}$$

$$\frac{\sqrt{15}y(x-z)(x+z)}{2}$$

\*\* expression

$$\begin{aligned} & \frac{\sqrt{3}G_u y z (12x^2 - 9y^2 + 5z^2)}{12} - \frac{G_v y z (36x^2 + y^2 - 13z^2)}{12} + \frac{7G_{xy} x z (2x^2 - 3y^2 - z^2)}{12} \\ & + \frac{7G_{xz} x y (2x^2 - y^2 - 3z^2)}{12} - \frac{G_{yz} (4x^4 - 12x^2 y^2 - 12x^2 z^2 + 5y^4 - 18y^2 z^2 + 5z^4)}{12} \\ & \frac{\sqrt{3}G_u x z (9x^2 - 12y^2 - 5z^2)}{12} - \frac{G_v x z (x^2 + 36y^2 - 13z^2)}{12} + \frac{7G_{xy} y z (3x^2 - 2y^2 + z^2)}{12} \\ & + \frac{G_{xz} (5x^4 - 12x^2 y^2 - 18x^2 z^2 + 4y^4 - 12y^2 z^2 + 5z^4)}{12} + \frac{7G_{yz} x y (x^2 - 2y^2 + 3z^2)}{12} \end{aligned}$$

\* Harmonics for rank 4

$$\tilde{\mathbb{Q}}_4^{(2,-1)}[g](A_1, 1)$$

\*\* symmetry

$$\frac{\sqrt{21}(x^4 - 3x^2 y^2 - 3x^2 z^2 + y^4 - 3y^2 z^2 + z^4)}{6}$$

\*\* expression

$$\frac{\sqrt{5}G_{xy} z (x - y) (x + y)}{2} - \frac{\sqrt{5}G_{xz} y (x - z) (x + z)}{2} + \frac{\sqrt{5}G_{yz} x (y - z) (y + z)}{2}$$

$$\tilde{\mathbb{Q}}_4^{(2,-1)}[g](A_1, 2)$$

\*\* symmetry

$$-\frac{\sqrt{15}(x^4 - 12x^2 y^2 + 6x^2 z^2 + y^4 + 6y^2 z^2 - 2z^4)}{12}$$

\*\* expression

$$-\frac{6\sqrt{7}G_v x y z}{7} - \frac{\sqrt{7}G_{xy} z (x - y) (x + y)}{14} + \frac{\sqrt{7}G_{xz} y (4x^2 - 3y^2 + 5z^2)}{14} + \frac{\sqrt{7}G_{yz} x (3x^2 - 4y^2 - 5z^2)}{14}$$

$$\tilde{\mathbb{Q}}_4^{(2,1)}[g](A_1, 1)$$

\*\* symmetry

$$\frac{\sqrt{21}(x^4 - 3x^2 y^2 - 3x^2 z^2 + y^4 - 3y^2 z^2 + z^4)}{6}$$

\*\* expression

$$\begin{aligned} & -\frac{3\sqrt{2310}G_u x y z (x - y) (x + y)}{44} - \frac{3\sqrt{770}G_v x y z (x^2 + y^2 - 2z^2)}{44} + \frac{\sqrt{770}G_{xy} z (x - y) (x + y) (x^2 + y^2 - 2z^2)}{22} \\ & - \frac{\sqrt{770}G_{xz} y (x - z) (x + z) (x^2 - 2y^2 + z^2)}{22} - \frac{\sqrt{770}G_{yz} x (y - z) (y + z) (2x^2 - y^2 - z^2)}{22} \end{aligned}$$

$$\tilde{\mathbb{Q}}_4^{(2,1)}[g](A_1, 2)$$

\*\* symmetry

$$-\frac{\sqrt{15}(x^4 - 12x^2 y^2 + 6x^2 z^2 + y^4 + 6y^2 z^2 - 2z^4)}{12}$$

\*\* expression

$$\frac{21\sqrt{66}G_uxyz(x-y)(x+y)}{44} - \frac{21\sqrt{22}G_vxyz(x^2+y^2-2z^2)}{44} + \frac{7\sqrt{22}G_{xy}z(x-y)(x+y)(x^2+y^2-2z^2)}{44} + \frac{\sqrt{22}G_{xz}y(17x^4-22x^2y^2-36x^2z^2+3y^4-8y^2z^2+10z^4)}{44} - \frac{\sqrt{22}G_{yz}x(3x^4-22x^2y^2-8x^2z^2+17y^4-36y^2z^2+10z^4)}{44}$$

$$\tilde{\mathbb{Q}}_4^{(2,-1)}[g](A_2)$$

\*\* symmetry

$$\frac{\sqrt{35}xy(x-y)(x+y)}{2}$$

\*\* expression

$$-\frac{\sqrt{3}G_vz(x-y)(x+y)}{2} + \sqrt{3}G_{xy}xyz + \frac{\sqrt{3}G_{xz}x(x^2-3y^2)}{4} - \frac{\sqrt{3}G_{yz}y(3x^2-y^2)}{4}$$

$$\tilde{\mathbb{Q}}_4^{(2,1)}[g](A_2)$$

\*\* symmetry

$$\frac{\sqrt{35}xy(x-y)(x+y)}{2}$$

\*\* expression

$$\frac{9\sqrt{154}G_uz(x^2-2xy-y^2)(x^2+2xy-y^2)}{88} - \frac{\sqrt{462}G_vz(x-y)(x+y)(x^2+y^2-2z^2)}{88} + \frac{\sqrt{462}G_{xy}xyz(x^2+y^2-2z^2)}{44} + \frac{\sqrt{462}G_{xz}x(x^4-8x^2y^2-2x^2z^2+3y^4+6y^2z^2)}{44} + \frac{\sqrt{462}G_{yz}y(3x^4-8x^2y^2+6x^2z^2+y^4-2y^2z^2)}{44}$$

$$\tilde{\mathbb{Q}}_4^{(2,-1)}[g](B_1)$$

\*\* symmetry

$$\frac{\sqrt{5}(x-y)(x+y)(x^2+y^2-6z^2)}{4}$$

\*\* expression

$$\frac{6\sqrt{7}G_uxyz}{7} + \frac{\sqrt{21}G_{xy}z(3x^2+3y^2-2z^2)}{14} - \frac{\sqrt{21}G_{xz}y(2x^2-y^2+z^2)}{14} + \frac{\sqrt{21}G_{yz}x(x^2-2y^2-z^2)}{14}$$

$$\tilde{\mathbb{Q}}_4^{(2,1)}[g](B_1)$$

\*\* symmetry

$$\frac{\sqrt{5}(x-y)(x+y)(x^2+y^2-6z^2)}{4}$$

\*\* expression

$$-\frac{21\sqrt{22}G_uxyz(x^2+y^2-2z^2)}{44} - \frac{21\sqrt{66}G_vxyz(x-y)(x+y)}{44} + \frac{\sqrt{66}G_{xy}z(9x^4-24x^2y^2-10x^2z^2+9y^4-10y^2z^2+2z^4)}{44} - \frac{\sqrt{66}G_{xz}y(x^4+2x^2y^2-12x^2z^2+y^4-12y^2z^2+8z^4)}{44} - \frac{\sqrt{66}G_{yz}x(x^4+2x^2y^2-12x^2z^2+y^4-12y^2z^2+8z^4)}{44}$$

$$\tilde{\mathbb{Q}}_4^{(2,-1)}[g](B_2)$$

\*\* symmetry

$$-\frac{\sqrt{5}xy(x^2+y^2-6z^2)}{2}$$

\*\* expression

$$\frac{3\sqrt{7}G_uz(x-y)(x+y)}{7} + \frac{\sqrt{21}G_vz(3x^2+3y^2-2z^2)}{14} - \frac{\sqrt{21}G_{xz}x(x^2-5y^2+2z^2)}{28} - \frac{\sqrt{21}G_{yz}y(5x^2-y^2-2z^2)}{28}$$

$$\tilde{\mathbb{Q}}_4^{(2,1)}[g](B_2)$$

\*\* symmetry

$$-\frac{\sqrt{5}xy(x^2+y^2-6z^2)}{2}$$

\*\* expression

$$-\frac{21\sqrt{22}G_uz(x-y)(x+y)(x^2+y^2-2z^2)}{88} - \frac{\sqrt{66}G_vz(3x^4-78x^2y^2+20x^2z^2+3y^4+20y^2z^2-4z^4)}{88} - \frac{21\sqrt{66}G_{xy}xyz(x-y)(x+y)}{44} - \frac{\sqrt{66}G_{xz}x(x^4+2x^2y^2-12x^2z^2+y^4-12y^2z^2+8z^4)}{44} + \frac{\sqrt{66}G_{yz}y(x^4+2x^2y^2-12x^2z^2+y^4-12y^2z^2+8z^4)}{44}$$

$$\tilde{\mathbb{Q}}_{4,1}^{(2,-1)}[g](E,1), \tilde{\mathbb{Q}}_{4,2}^{(2,-1)}[g](E,1)$$

\*\* symmetry

$$\frac{\sqrt{35}xz(x-z)(x+z)}{2}$$

$$\frac{\sqrt{35}yz(y-z)(y+z)}{2}$$

\*\* expression

$$-\frac{3G_u y(x-z)(x+z)}{4} + \frac{\sqrt{3}G_v y(x-z)(x+z)}{4} - \frac{\sqrt{3}G_{xy} x(x^2-3z^2)}{4} - \sqrt{3}G_{xz}xyz + \frac{\sqrt{3}G_{yz} z(3x^2-z^2)}{4}$$

$$\frac{3G_u x(y-z)(y+z)}{4} + \frac{\sqrt{3}G_v x(y-z)(y+z)}{4} + \frac{\sqrt{3}G_{xy} y(y^2-3z^2)}{4} - \frac{\sqrt{3}G_{xz} z(3y^2-z^2)}{4} + \sqrt{3}G_{yz}xyz$$

$$\tilde{\mathbb{Q}}_{4,1}^{(2,-1)}[g](E,2), \tilde{\mathbb{Q}}_{4,2}^{(2,-1)}[g](E,2)$$

\*\* symmetry

$$-\frac{\sqrt{5}xz(x^2-6y^2+z^2)}{2}$$

$$\frac{\sqrt{5}yz(6x^2-y^2-z^2)}{2}$$

\*\* expression

$$\frac{3\sqrt{7}G_u y(5x^2-2y^2+z^2)}{28} + \frac{\sqrt{21}G_v y(3x^2+2y^2-9z^2)}{28} + \frac{\sqrt{21}G_{xy} x(x^2+2y^2-5z^2)}{28} + \frac{\sqrt{21}G_{yz} z(5x^2-2y^2-z^2)}{28}$$

$$\frac{3\sqrt{7}G_u x(2x^2-5y^2-z^2)}{28} + \frac{\sqrt{21}G_v x(2x^2+3y^2-9z^2)}{28} - \frac{\sqrt{21}G_{xy} y(2x^2+y^2-5z^2)}{28} + \frac{\sqrt{21}G_{xz} z(2x^2-5y^2+z^2)}{28}$$

$$\tilde{\mathbb{Q}}_{4,1}^{(2,1)}[g](E,1), \tilde{\mathbb{Q}}_{4,2}^{(2,1)}[g](E,1)$$

\*\* symmetry

$$\frac{\sqrt{35}xz(x-z)(x+z)}{2}$$

$$\frac{\sqrt{35}yz(y-z)(y+z)}{2}$$

\*\* expression

$$\frac{3\sqrt{154}G_u y(x^4+x^2y^2-9x^2z^2-y^2z^2+2z^4)}{88} + \frac{\sqrt{462}G_v y(5x^4-x^2y^2-27x^2z^2+y^2z^2+4z^4)}{88} - \frac{\sqrt{462}G_{xy} x(x^4-2x^2y^2-8x^2z^2+6y^2z^2+3z^4)}{44} - \frac{\sqrt{462}G_{xz}xyz(x^2-2y^2+z^2)}{44} - \frac{\sqrt{462}G_{yz} z(3x^4+6x^2y^2-8x^2z^2-2y^2z^2+z^4)}{44}$$

$$-\frac{3\sqrt{154}G_u x(x^2y^2-x^2z^2+y^4-9y^2z^2+2z^4)}{88} - \frac{\sqrt{462}G_v x(x^2y^2-x^2z^2-5y^4+27y^2z^2-4z^4)}{88} - \frac{\sqrt{462}G_{xy} y(2x^2y^2-6x^2z^2-y^4+8y^2z^2-3z^4)}{44} + \frac{\sqrt{462}G_{xz} z(6x^2y^2-2x^2z^2+3y^4-8y^2z^2+z^4)}{44} - \frac{\sqrt{462}G_{yz}xyz(2x^2-y^2-z^2)}{44}$$

$$\tilde{\mathbb{Q}}_{4,1}^{(2,1)}[g](E,2), \tilde{\mathbb{Q}}_{4,2}^{(2,1)}[g](E,2)$$

\*\* symmetry

$$-\frac{\sqrt{5}xz(x^2-6y^2+z^2)}{2}$$

$$\frac{\sqrt{5}yz(6x^2-y^2-z^2)}{2}$$

\*\* expression

$$\begin{aligned} & -\frac{3\sqrt{22}G_u y(5x^4+3x^2y^2-39x^2z^2-2y^4+17y^2z^2-2z^4)}{88} - \frac{\sqrt{66}G_v y(9x^4-31x^2y^2+39x^2z^2+2y^4+11y^2z^2-12z^4)}{88} \\ & + \frac{\sqrt{66}G_{xy} x(x^4-12x^2y^2+2x^2z^2+8y^4-12y^2z^2+z^4)}{44} + \frac{21\sqrt{66}G_{xz}xyz(x-z)(x+z)}{44} - \frac{\sqrt{66}G_{yz} z(x^4-12x^2y^2+2x^2z^2+8y^4-12y^2z^2+z^4)}{44} \\ & -\frac{3\sqrt{22}G_u x(2x^4-3x^2y^2-17x^2z^2-5y^4+39y^2z^2+2z^4)}{88} - \frac{\sqrt{66}G_v x(2x^4-31x^2y^2+11x^2z^2+9y^4+39y^2z^2-12z^4)}{88} \\ & - \frac{\sqrt{66}G_{xy} y(8x^4-12x^2y^2-12x^2z^2+y^4+2y^2z^2+z^4)}{44} + \frac{\sqrt{66}G_{xz} z(8x^4-12x^2y^2-12x^2z^2+y^4+2y^2z^2+z^4)}{44} - \frac{21\sqrt{66}G_{yz}xyz(y-z)(y+z)}{44} \end{aligned}$$