

# SG No. 223 $O_h^3$ $Pm\bar{3}n$ [ cubic ]

\* plus set:  $+ [0, 0, 0]$

Table 1: Wyckoff site: 2a, site symmetry:  $m\bar{3}$ .

| No. | position                                  | mapping  |
|-----|---|--|
| 1   | $[0, 0, 0]$                               | $[1, 2, 3, 4, 5, 6, 7, 8, 9, 10, 11, 12, 25, 26, 27, 28, 29, 30, 31, 32, 33, 34, 35, 36]$          |
| 2   | $[\frac{1}{2}, \frac{1}{2}, \frac{1}{2}]$ | $[13, 14, 15, 16, 17, 18, 19, 20, 21, 22, 23, 24, 37, 38, 39, 40, 41, 42, 43, 44, 45, 46, 47, 48]$ |

Table 2: Wyckoff site: 6b, site symmetry:  $mmm..$

| No. | position                        | mapping                            |
|-----|---------------------------------|------------------------------------|
| 1   | $[0, \frac{1}{2}, \frac{1}{2}]$ | $[1, 2, 3, 4, 25, 26, 27, 28]$     |
| 2   | $[\frac{1}{2}, 0, \frac{1}{2}]$ | $[5, 6, 7, 8, 29, 30, 31, 32]$     |
| 3   | $[\frac{1}{2}, \frac{1}{2}, 0]$ | $[9, 10, 11, 12, 33, 34, 35, 36]$  |
| 4   | $[0, \frac{1}{2}, 0]$           | $[13, 14, 15, 16, 37, 38, 39, 40]$ |
| 5   | $[\frac{1}{2}, 0, 0]$           | $[17, 18, 19, 20, 41, 42, 43, 44]$ |
| 6   | $[0, 0, \frac{1}{2}]$           | $[21, 22, 23, 24, 45, 46, 47, 48]$ |

Table 3: Wyckoff site: 6c, site symmetry:  $-4m.2$

| No. | position                        | mapping                            |
|-----|---------------------------------|------------------------------------|
| 1   | $[\frac{1}{4}, 0, \frac{1}{2}]$ | $[1, 4, 18, 19, 26, 27, 41, 44]$   |
| 2   | $[\frac{3}{4}, 0, \frac{1}{2}]$ | $[2, 3, 17, 20, 25, 28, 42, 43]$   |
| 3   | $[\frac{1}{2}, \frac{1}{4}, 0]$ | $[5, 8, 14, 15, 30, 31, 37, 40]$   |
| 4   | $[\frac{1}{2}, \frac{3}{4}, 0]$ | $[6, 7, 13, 16, 29, 32, 38, 39]$   |
| 5   | $[0, \frac{1}{2}, \frac{1}{4}]$ | $[9, 12, 21, 24, 34, 35, 46, 47]$  |
| 6   | $[0, \frac{1}{2}, \frac{3}{4}]$ | $[10, 11, 22, 23, 33, 36, 45, 48]$ |

Table 4: Wyckoff site: 6d, site symmetry:  $-4m.2$

| No. | position                        | mapping                            |
|-----|---------------------------------|------------------------------------|
| 1   | $[\frac{1}{4}, \frac{1}{2}, 0]$ | $[1, 4, 18, 19, 26, 27, 41, 44]$   |
| 2   | $[\frac{3}{4}, \frac{1}{2}, 0]$ | $[2, 3, 17, 20, 25, 28, 42, 43]$   |
| 3   | $[0, \frac{1}{4}, \frac{1}{2}]$ | $[5, 8, 14, 15, 30, 31, 37, 40]$   |
| 4   | $[0, \frac{3}{4}, \frac{1}{2}]$ | $[6, 7, 13, 16, 29, 32, 38, 39]$   |
| 5   | $[\frac{1}{2}, 0, \frac{1}{4}]$ | $[9, 12, 21, 24, 34, 35, 46, 47]$  |
| 6   | $[\frac{1}{2}, 0, \frac{3}{4}]$ | $[10, 11, 22, 23, 33, 36, 45, 48]$ |

Table 5: Wyckoff site: **8e**, site symmetry:  $\bar{4}2$ 

| No. | position                                  | mapping                    |
|-----|---|----------------------------|
| 1   | $[\frac{1}{4}, \frac{1}{4}, \frac{1}{4}]$ | $[1, 5, 9, 14, 19, 24]$    |
| 2   | $[\frac{3}{4}, \frac{3}{4}, \frac{1}{4}]$ | $[2, 7, 12, 13, 17, 21]$   |
| 3   | $[\frac{3}{4}, \frac{1}{4}, \frac{3}{4}]$ | $[3, 8, 10, 15, 20, 22]$   |
| 4   | $[\frac{1}{4}, \frac{3}{4}, \frac{3}{4}]$ | $[4, 6, 11, 16, 18, 23]$   |
| 5   | $[\frac{3}{4}, \frac{3}{4}, \frac{3}{4}]$ | $[25, 29, 33, 38, 43, 48]$ |
| 6   | $[\frac{1}{4}, \frac{1}{4}, \frac{3}{4}]$ | $[26, 31, 36, 37, 41, 45]$ |
| 7   | $[\frac{1}{4}, \frac{3}{4}, \frac{1}{4}]$ | $[27, 32, 34, 39, 44, 46]$ |
| 8   | $[\frac{3}{4}, \frac{1}{4}, \frac{1}{4}]$ | $[28, 30, 35, 40, 42, 47]$ |

Table 6: Wyckoff site: **12f**, site symmetry:  $mm2$ 

| No. | position                                      | mapping            |
|-----|---|--------------------|
| 1   | $[x, 0, 0]$                                   | $[1, 4, 26, 27]$   |
| 2   | $[-x, 0, 0]$                                  | $[2, 3, 25, 28]$   |
| 3   | $[0, x, 0]$                                   | $[5, 8, 30, 31]$   |
| 4   | $[0, -x, 0]$                                  | $[6, 7, 29, 32]$   |
| 5   | $[0, 0, x]$                                   | $[9, 12, 34, 35]$  |
| 6   | $[0, 0, -x]$                                  | $[10, 11, 33, 36]$ |
| 7   | $[\frac{1}{2}, x + \frac{1}{2}, \frac{1}{2}]$ | $[13, 16, 38, 39]$ |
| 8   | $[\frac{1}{2}, \frac{1}{2} - x, \frac{1}{2}]$ | $[14, 15, 37, 40]$ |
| 9   | $[x + \frac{1}{2}, \frac{1}{2}, \frac{1}{2}]$ | $[17, 20, 42, 43]$ |
| 10  | $[\frac{1}{2} - x, \frac{1}{2}, \frac{1}{2}]$ | $[18, 19, 41, 44]$ |
| 11  | $[\frac{1}{2}, \frac{1}{2}, \frac{1}{2} - x]$ | $[21, 24, 46, 47]$ |
| 12  | $[\frac{1}{2}, \frac{1}{2}, x + \frac{1}{2}]$ | $[22, 23, 45, 48]$ |

Table 7: Wyckoff site: **12g**, site symmetry:  $mm2$ 

| No. | position                            | mapping            |
|-----|-------------------------------------|--------------------|
| 1   | $[x, 0, \frac{1}{2}]$               | $[1, 4, 26, 27]$   |
| 2   | $[-x, 0, \frac{1}{2}]$              | $[2, 3, 25, 28]$   |
| 3   | $[\frac{1}{2}, x, 0]$               | $[5, 8, 30, 31]$   |
| 4   | $[\frac{1}{2}, -x, 0]$              | $[6, 7, 29, 32]$   |
| 5   | $[0, \frac{1}{2}, x]$               | $[9, 12, 34, 35]$  |
| 6   | $[0, \frac{1}{2}, -x]$              | $[10, 11, 33, 36]$ |
| 7   | $[\frac{1}{2}, x + \frac{1}{2}, 0]$ | $[13, 16, 38, 39]$ |
| 8   | $[\frac{1}{2}, \frac{1}{2} - x, 0]$ | $[14, 15, 37, 40]$ |
| 9   | $[x + \frac{1}{2}, 0, \frac{1}{2}]$ | $[17, 20, 42, 43]$ |
| 10  | $[\frac{1}{2} - x, 0, \frac{1}{2}]$ | $[18, 19, 41, 44]$ |
| 11  | $[0, \frac{1}{2}, \frac{1}{2} - x]$ | $[21, 24, 46, 47]$ |
| 12  | $[0, \frac{1}{2}, x + \frac{1}{2}]$ | $[22, 23, 45, 48]$ |

Table 8: Wyckoff site: 12h, site symmetry:  $mm2$ .

| No. | position                            | mapping          |
|-----|-------------------------------------|------------------|
| 1   | $[x, \frac{1}{2}, 0]$               | [1, 4, 26, 27]   |
| 2   | $[-x, \frac{1}{2}, 0]$              | [2, 3, 25, 28]   |
| 3   | $[0, x, \frac{1}{2}]$               | [5, 8, 30, 31]   |
| 4   | $[0, -x, \frac{1}{2}]$              | [6, 7, 29, 32]   |
| 5   | $[\frac{1}{2}, 0, x]$               | [9, 12, 34, 35]  |
| 6   | $[\frac{1}{2}, 0, -x]$              | [10, 11, 33, 36] |
| 7   | $[0, x + \frac{1}{2}, \frac{1}{2}]$ | [13, 16, 38, 39] |
| 8   | $[0, \frac{1}{2} - x, \frac{1}{2}]$ | [14, 15, 37, 40] |
| 9   | $[x + \frac{1}{2}, \frac{1}{2}, 0]$ | [17, 20, 42, 43] |
| 10  | $[\frac{1}{2} - x, \frac{1}{2}, 0]$ | [18, 19, 41, 44] |
| 11  | $[\frac{1}{2}, 0, \frac{1}{2} - x]$ | [21, 24, 46, 47] |
| 12  | $[\frac{1}{2}, 0, x + \frac{1}{2}]$ | [22, 23, 45, 48] |

Table 9: Wyckoff site: 16i, site symmetry:  $\bar{3}$ .

| No. | position  | mapping      |
|-----|---|--------------|
| 1   | $[x, x, x]$   | [1, 5, 9]    |
| 2   | $[-x, -x, x]$   | [2, 7, 12]   |
| 3   | $[-x, x, -x]$   | [3, 8, 10]   |
| 4   | $[x, -x, -x]$   | [4, 6, 11]   |
| 5   | $[x + \frac{1}{2}, x + \frac{1}{2}, \frac{1}{2} - x]$ | [13, 17, 21] |
| 6   | $[\frac{1}{2} - x, \frac{1}{2} - x, \frac{1}{2} - x]$ | [14, 19, 24] |
| 7   | $[x + \frac{1}{2}, \frac{1}{2} - x, x + \frac{1}{2}]$ | [15, 20, 22] |
| 8   | $[\frac{1}{2} - x, x + \frac{1}{2}, x + \frac{1}{2}]$ | [16, 18, 23] |
| 9   | $[-x, -x, -x]$  | [25, 29, 33] |
| 10  | $[x, x, -x]$  | [26, 31, 36] |
| 11  | $[x, -x, x]$  | [27, 32, 34] |
| 12  | $[-x, x, x]$  | [28, 30, 35] |
| 13  | $[\frac{1}{2} - x, \frac{1}{2} - x, x + \frac{1}{2}]$ | [37, 41, 45] |
| 14  | $[x + \frac{1}{2}, x + \frac{1}{2}, x + \frac{1}{2}]$ | [38, 43, 48] |
| 15  | $[\frac{1}{2} - x, x + \frac{1}{2}, \frac{1}{2} - x]$ | [39, 44, 46] |
| 16  | $[x + \frac{1}{2}, \frac{1}{2} - x, \frac{1}{2} - x]$ | [40, 42, 47] |

Table 10: Wyckoff site: 24j, site symmetry:  $\bar{3}2$ 

| No. | position                             | mapping |
|-----|--------------------------------------|---------|
| 1   | $[\frac{1}{4}, y, y + \frac{1}{2}]$  | [1, 18] |
| 2   | $[\frac{3}{4}, -y, y + \frac{1}{2}]$ | [2, 20] |
| 3   | $[\frac{3}{4}, y, \frac{1}{2} - y]$  | [3, 17] |
| 4   | $[\frac{1}{4}, -y, \frac{1}{2} - y]$ | [4, 19] |
| 5   | $[y + \frac{1}{2}, \frac{1}{4}, y]$  | [5, 15] |

*continued ...*

Table 10

| No. | position                             | mapping |
|-----|--------------------------------------|---------|
| 6   | $[y + \frac{1}{2}, \frac{3}{4}, -y]$ | [6,13]  |
| 7   | $[\frac{1}{2} - y, \frac{3}{4}, y]$  | [7,16]  |
| 8   | $[\frac{1}{2} - y, \frac{1}{4}, -y]$ | [8,14]  |
| 9   | $[y, y + \frac{1}{2}, \frac{1}{4}]$  | [9,21]  |
| 10  | $[-y, y + \frac{1}{2}, \frac{3}{4}]$ | [10,23] |
| 11  | $[y, \frac{1}{2} - y, \frac{3}{4}]$  | [11,22] |
| 12  | $[-y, \frac{1}{2} - y, \frac{1}{4}]$ | [12,24] |
| 13  | $[\frac{3}{4}, -y, \frac{1}{2} - y]$ | [25,42] |
| 14  | $[\frac{1}{4}, y, \frac{1}{2} - y]$  | [26,44] |
| 15  | $[\frac{1}{4}, -y, y + \frac{1}{2}]$ | [27,41] |
| 16  | $[\frac{3}{4}, y, y + \frac{1}{2}]$  | [28,43] |
| 17  | $[\frac{1}{2} - y, \frac{3}{4}, -y]$ | [29,39] |
| 18  | $[\frac{1}{2} - y, \frac{1}{4}, y]$  | [30,37] |
| 19  | $[y + \frac{1}{2}, \frac{1}{4}, -y]$ | [31,40] |
| 20  | $[y + \frac{1}{2}, \frac{3}{4}, y]$  | [32,38] |
| 21  | $[-y, \frac{1}{2} - y, \frac{3}{4}]$ | [33,45] |
| 22  | $[y, \frac{1}{2} - y, \frac{1}{4}]$  | [34,47] |
| 23  | $[-y, y + \frac{1}{2}, \frac{1}{4}]$ | [35,46] |
| 24  | $[y, y + \frac{1}{2}, \frac{3}{4}]$  | [36,48] |

Table 11: Wyckoff site: 24k, site symmetry:  $m\bar{3}m$ .

| No. | position  | mapping |
|-----|---|---------|
| 1   | $[0, y, z]$                                       | [1,28]  |
| 2   | $[0, -y, z]$                                      | [2,27]  |
| 3   | $[0, y, -z]$                                      | [3,26]  |
| 4   | $[0, -y, -z]$                                     | [4,25]  |
| 5   | $[z, 0, y]$                                       | [5,32]  |
| 6   | $[z, 0, -y]$                                      | [6,31]  |
| 7   | $[-z, 0, y]$                                      | [7,30]  |
| 8   | $[-z, 0, -y]$                                     | [8,29]  |
| 9   | $[y, z, 0]$                                       | [9,36]  |
| 10  | $[-y, z, 0]$                                      | [10,35] |
| 11  | $[y, -z, 0]$                                      | [11,34] |
| 12  | $[-y, -z, 0]$                                     | [12,33] |
| 13  | $[y + \frac{1}{2}, \frac{1}{2}, \frac{1}{2} - z]$ | [13,40] |
| 14  | $[\frac{1}{2} - y, \frac{1}{2}, \frac{1}{2} - z]$ | [14,39] |
| 15  | $[y + \frac{1}{2}, \frac{1}{2}, z + \frac{1}{2}]$ | [15,38] |
| 16  | $[\frac{1}{2} - y, \frac{1}{2}, z + \frac{1}{2}]$ | [16,37] |
| 17  | $[\frac{1}{2}, z + \frac{1}{2}, \frac{1}{2} - y]$ | [17,44] |
| 18  | $[\frac{1}{2}, z + \frac{1}{2}, y + \frac{1}{2}]$ | [18,43] |
| 19  | $[\frac{1}{2}, \frac{1}{2} - z, \frac{1}{2} - y]$ | [19,42] |
| 20  | $[\frac{1}{2}, \frac{1}{2} - z, y + \frac{1}{2}]$ | [20,41] |
| 21  | $[z + \frac{1}{2}, y + \frac{1}{2}, \frac{1}{2}]$ | [21,48] |

continued ...

Table 11

| No. | position  | mapping  |
|-----|---|----------|
| 22  | $[z + \frac{1}{2}, \frac{1}{2} - y, \frac{1}{2}]$ | [22, 47] |
| 23  | $[\frac{1}{2} - z, y + \frac{1}{2}, \frac{1}{2}]$ | [23, 46] |
| 24  | $[\frac{1}{2} - z, \frac{1}{2} - y, \frac{1}{2}]$ | [24, 45] |

Table 12: Wyckoff site: 481, site symmetry: 1

| No. | position  | mapping |
|-----|---|---------|
| 1   | $[x, y, z]$   | [1]     |
| 2   | $[-x, -y, z]$   | [2]     |
| 3   | $[-x, y, -z]$   | [3]     |
| 4   | $[x, -y, -z]$   | [4]     |
| 5   | $[z, x, y]$   | [5]     |
| 6   | $[z, -x, -y]$   | [6]     |
| 7   | $[-z, -x, y]$   | [7]     |
| 8   | $[-z, x, -y]$   | [8]     |
| 9   | $[y, z, x]$   | [9]     |
| 10  | $[-y, z, -x]$   | [10]    |
| 11  | $[y, -z, -x]$   | [11]    |
| 12  | $[-y, -z, x]$   | [12]    |
| 13  | $[y + \frac{1}{2}, x + \frac{1}{2}, \frac{1}{2} - z]$ | [13]    |
| 14  | $[\frac{1}{2} - y, \frac{1}{2} - x, \frac{1}{2} - z]$ | [14]    |
| 15  | $[y + \frac{1}{2}, \frac{1}{2} - x, z + \frac{1}{2}]$ | [15]    |
| 16  | $[\frac{1}{2} - y, x + \frac{1}{2}, z + \frac{1}{2}]$ | [16]    |
| 17  | $[x + \frac{1}{2}, z + \frac{1}{2}, \frac{1}{2} - y]$ | [17]    |
| 18  | $[\frac{1}{2} - x, z + \frac{1}{2}, y + \frac{1}{2}]$ | [18]    |
| 19  | $[\frac{1}{2} - x, \frac{1}{2} - z, \frac{1}{2} - y]$ | [19]    |
| 20  | $[x + \frac{1}{2}, \frac{1}{2} - z, y + \frac{1}{2}]$ | [20]    |
| 21  | $[z + \frac{1}{2}, y + \frac{1}{2}, \frac{1}{2} - x]$ | [21]    |
| 22  | $[z + \frac{1}{2}, \frac{1}{2} - y, x + \frac{1}{2}]$ | [22]    |
| 23  | $[\frac{1}{2} - z, y + \frac{1}{2}, x + \frac{1}{2}]$ | [23]    |
| 24  | $[\frac{1}{2} - z, \frac{1}{2} - y, \frac{1}{2} - x]$ | [24]    |
| 25  | $[-x, -y, -z]$  | [25]    |
| 26  | $[x, y, -z]$  | [26]    |
| 27  | $[x, -y, z]$  | [27]    |
| 28  | $[-x, y, z]$  | [28]    |
| 29  | $[-z, -x, -y]$  | [29]    |
| 30  | $[-z, x, y]$  | [30]    |
| 31  | $[z, x, -y]$  | [31]    |
| 32  | $[z, -x, y]$  | [32]    |
| 33  | $[-y, -z, -x]$  | [33]    |
| 34  | $[y, -z, x]$  | [34]    |
| 35  | $[-y, z, x]$  | [35]    |
| 36  | $[y, z, -x]$  | [36]    |
| 37  | $[\frac{1}{2} - y, \frac{1}{2} - x, z + \frac{1}{2}]$ | [37]    |

continued ...

Table 12

| No. | position  | mapping |
|-----|---|---------|
| 38  | $[y + \frac{1}{2}, x + \frac{1}{2}, z + \frac{1}{2}]$ | [38]    |
| 39  | $[\frac{1}{2} - y, x + \frac{1}{2}, \frac{1}{2} - z]$ | [39]    |
| 40  | $[y + \frac{1}{2}, \frac{1}{2} - x, \frac{1}{2} - z]$ | [40]    |
| 41  | $[\frac{1}{2} - x, \frac{1}{2} - z, y + \frac{1}{2}]$ | [41]    |
| 42  | $[x + \frac{1}{2}, \frac{1}{2} - z, \frac{1}{2} - y]$ | [42]    |
| 43  | $[x + \frac{1}{2}, z + \frac{1}{2}, y + \frac{1}{2}]$ | [43]    |
| 44  | $[\frac{1}{2} - x, z + \frac{1}{2}, \frac{1}{2} - y]$ | [44]    |
| 45  | $[\frac{1}{2} - z, \frac{1}{2} - y, x + \frac{1}{2}]$ | [45]    |
| 46  | $[\frac{1}{2} - z, y + \frac{1}{2}, \frac{1}{2} - x]$ | [46]    |
| 47  | $[z + \frac{1}{2}, \frac{1}{2} - y, \frac{1}{2} - x]$ | [47]    |
| 48  | $[z + \frac{1}{2}, y + \frac{1}{2}, x + \frac{1}{2}]$ | [48]    |