

PG No. 8  $D_{2h}$   $mmm$  [ orthorhombic ] (axial, internal polar octupole)

\* Harmonics for rank 0

\* Harmonics for rank 1

$\vec{G}_1^{(3,2)}[q](B_{1g})$

\*\* symmetry

$z$

\*\* expression

$$-\frac{3\sqrt{70}Q_{1x}(x^2-3y^2)}{56} + \frac{3\sqrt{70}Q_{2y}(3x^2-y^2)}{56} - \frac{\sqrt{105}Q_{3z}(x-y)(x+y)}{14} - \frac{\sqrt{42}Q_{3xy}(x^2+y^2-4z^2)}{56} + \frac{\sqrt{42}Q_{3yx}(x^2+y^2-4z^2)}{56} + \frac{\sqrt{105}Q_{bzy}xz}{7}$$

$\vec{G}_1^{(3,2)}[q](B_{2g})$

\*\* symmetry

$y$

\*\* expression

$$-\frac{3\sqrt{70}Q_{1xyz}}{28} - \frac{3\sqrt{70}Q_{2z}(x-y)(x+y)}{56} + \frac{\sqrt{105}Q_{3y}(x-z)(x+z)}{14} + \frac{\sqrt{42}Q_{3xz}(11x^2+y^2-4z^2)}{56} + \frac{5\sqrt{42}Q_{3yxyz}}{28} - \frac{3\sqrt{7}Q_{azx}(x^2+y^2-4z^2)}{28} + \frac{\sqrt{105}Q_{bzx}(x^2-y^2-2z^2)}{28}$$

$\vec{G}_1^{(3,2)}[q](B_{3g})$

\*\* symmetry

$x$

\*\* expression

$$\frac{3\sqrt{70}Q_{1z}(x-y)(x+y)}{56} - \frac{3\sqrt{70}Q_{2xyz}}{28} - \frac{\sqrt{105}Q_{3x}(y-z)(y+z)}{14} - \frac{5\sqrt{42}Q_{3xyz}}{28} - \frac{\sqrt{42}Q_{3yz}(x^2+11y^2-4z^2)}{56} + \frac{3\sqrt{7}Q_{azy}(x^2+y^2-4z^2)}{28} - \frac{\sqrt{105}Q_{bzy}(x^2-y^2+2z^2)}{28}$$

\* Harmonics for rank 2

$\vec{G}_2^{(3,0)}[q](A_u, 1)$

\*\* symmetry

$$-\frac{x^2}{2} - \frac{y^2}{2} + z^2$$

\*\* expression

$$-\frac{\sqrt{210}Q_3(x-y)(x+y)}{28} + \frac{\sqrt{21}Q_{3xyz}}{7} - \frac{\sqrt{21}Q_{3yxx}}{7} + \frac{\sqrt{210}Q_{bzy}}{14}$$

$\vec{G}_2^{(3,0)}[q](A_u, 2)$

\*\* symmetry

$$\frac{\sqrt{3}(x-y)(x+y)}{2}$$

\*\* expression

$$\frac{\sqrt{105}Q_{1xz}}{14} - \frac{\sqrt{105}Q_{2yz}}{14} - \frac{\sqrt{70}Q_3(x^2+y^2-2z^2)}{28} - \frac{3\sqrt{7}Q_{3yz}}{14} - \frac{3\sqrt{7}Q_{3yxx}}{14} + \frac{\sqrt{42}Q_{azxy}}{14}$$

$\vec{G}_2^{(3,2)}[q](A_u, 1)$

\*\* symmetry

$$-\frac{x^2}{2} - \frac{y^2}{2} + z^2$$

\*\* expression

$$-\frac{\sqrt{70}Q_{1xz}(x^2-3y^2)}{8} + \frac{\sqrt{70}Q_{2yz}(3x^2-y^2)}{8} + \frac{\sqrt{105}Q_3(x-y)(x+y)(x^2+y^2-6z^2)}{42} - \frac{5\sqrt{42}Q_{3xyz}(3x^2+3y^2-4z^2)}{168} + \frac{5\sqrt{42}Q_{3yxx}(3x^2+3y^2-4z^2)}{168} - \frac{\sqrt{105}Q_{bzy}(x^2+y^2-6z^2)}{21}$$

$\vec{G}_2^{(3,2)}[q](A_u, 2)$

\*\* symmetry

$$\frac{\sqrt{3}(x-y)(x+y)}{2}$$

\*\* expression

$$\frac{\sqrt{210}Q_1xz(3x^2+3y^2-4z^2)}{168} - \frac{\sqrt{210}Q_2yz(3x^2+3y^2-4z^2)}{168} + \frac{\sqrt{35}Q_3(x^4-12x^2y^2+6x^2z^2+y^4+6y^2z^2-2z^4)}{42} \\ - \frac{5\sqrt{14}Q_{3x}yz(27x^2-y^2-8z^2)}{168} + \frac{5\sqrt{14}Q_{3y}xz(x^2-27y^2+8z^2)}{168} + \frac{5\sqrt{21}Q_{az}xy(x^2+y^2-6z^2)}{42} - \frac{\sqrt{35}Q_{bz}xy(x-y)(x+y)}{6}$$

$\vec{\mathbb{G}}_2^{(3,0)}[q](B_{1u})$

\*\* symmetry

$$\sqrt{3}xy$$

\*\* expression

$$-\frac{\sqrt{105}Q_1yz}{14} - \frac{\sqrt{105}Q_2xz}{14} + \frac{3\sqrt{7}Q_{3x}xz}{14} - \frac{3\sqrt{7}Q_{3y}yz}{14} - \frac{\sqrt{42}Q_{az}(x-y)(x+y)}{28} + \frac{\sqrt{70}Q_{bz}(x^2+y^2-2z^2)}{28}$$

$\vec{\mathbb{G}}_2^{(3,2)}[q](B_{1u})$

\*\* symmetry

$$\sqrt{3}xy$$

\*\* expression

$$-\frac{\sqrt{210}Q_1yz(3x^2+3y^2-4z^2)}{168} - \frac{\sqrt{210}Q_2xz(3x^2+3y^2-4z^2)}{168} + \frac{\sqrt{35}Q_3xy(x-y)(x+y)}{6} + \frac{5\sqrt{14}Q_{3x}xz(13x^2-15y^2-8z^2)}{168} \\ + \frac{5\sqrt{14}Q_{3y}yz(15x^2-13y^2+8z^2)}{168} - \frac{5\sqrt{21}Q_{az}(x-y)(x+y)(x^2+y^2-6z^2)}{84} + \frac{\sqrt{35}Q_{bz}(5x^4-18x^2y^2-12x^2z^2+5y^4-12y^2z^2+4z^4)}{84}$$

$\vec{\mathbb{G}}_2^{(3,0)}[q](B_{2u})$

\*\* symmetry

$$\sqrt{3}xz$$

\*\* expression

$$-\frac{\sqrt{105}Q_1(x-y)(x+y)}{28} + \frac{\sqrt{105}Q_2xy}{14} - \frac{3\sqrt{7}Q_{3x}xy}{14} + \frac{\sqrt{7}Q_{3y}(x^2-5y^2+4z^2)}{28} - \frac{\sqrt{42}Q_{az}yz}{7}$$

$\vec{\mathbb{G}}_2^{(3,2)}[q](B_{2u})$

\*\* symmetry

$$\sqrt{3}xz$$

\*\* expression

$$-\frac{\sqrt{210}Q_1(5x^4-21x^2y^2-9x^2z^2+2y^4+9y^2z^2)}{168} + \frac{\sqrt{210}Q_2xy(17x^2-11y^2-18z^2)}{168} - \frac{\sqrt{35}Q_3xz(x-z)(x+z)}{6} + \frac{5\sqrt{14}Q_{3x}xy(x^2+y^2-6z^2)}{168} \\ + \frac{5\sqrt{14}Q_{3y}(x^4+3x^2y^2-9x^2z^2+2y^4-15y^2z^2+4z^4)}{168} + \frac{5\sqrt{21}Q_{az}yz(3x^2+3y^2-4z^2)}{84} + \frac{\sqrt{35}Q_{bz}yz(3x^2+y^2-2z^2)}{12}$$

$\vec{\mathbb{G}}_2^{(3,0)}[q](B_{3u})$

\*\* symmetry

$$\sqrt{3}yz$$

\*\* expression

$$\frac{\sqrt{105}Q_1xy}{14} + \frac{\sqrt{105}Q_2(x-y)(x+y)}{28} + \frac{\sqrt{7}Q_{3x}(5x^2-y^2-4z^2)}{28} + \frac{3\sqrt{7}Q_{3y}xy}{14} + \frac{\sqrt{42}Q_{az}xz}{7}$$

$\vec{\mathbb{G}}_2^{(3,2)}[q](B_{3u})$

\*\* symmetry

$$\sqrt{3}yz$$

\*\* expression

$$-\frac{\sqrt{210}Q_1xy(11x^2-17y^2+18z^2)}{168} - \frac{\sqrt{210}Q_2(2x^4-21x^2y^2+9x^2z^2+5y^4-9y^2z^2)}{168} \\ + \frac{\sqrt{35}Q_3yz(y-z)(y+z)}{6} - \frac{5\sqrt{14}Q_{3x}(2x^4+3x^2y^2-15x^2z^2+y^4-9y^2z^2+4z^4)}{168} \\ - \frac{5\sqrt{14}Q_{3y}xy(x^2+y^2-6z^2)}{168} - \frac{5\sqrt{21}Q_{az}xz(3x^2+3y^2-4z^2)}{84} + \frac{\sqrt{35}Q_{bz}xz(x^2+3y^2-2z^2)}{12}$$

\* Harmonics for rank 3

$\vec{\mathbb{G}}_3^{(3,-2)}[q](A_g)$

\*\* symmetry

$$\sqrt{15}xyz$$

\*\* expression

$$\frac{\sqrt{2}Q_1y}{4} + \frac{\sqrt{2}Q_2x}{4} + \frac{\sqrt{30}Q_{3x}x}{12} - \frac{\sqrt{30}Q_{3y}y}{12} - \frac{\sqrt{3}Q_{bz}z}{3}$$

$$\vec{\mathbb{G}}_3^{(3,0)}[q](A_g)$$

\*\* symmetry

$$\sqrt{15}xyz$$

\*\* expression

$$\frac{Q_1y(x^2+y^2-4z^2)}{4} + \frac{Q_2x(x^2+y^2-4z^2)}{4} + \frac{\sqrt{15}Q_{3x}x(x^2-3y^2)}{12} + \frac{\sqrt{15}Q_{3y}y(3x^2-y^2)}{12} + \frac{\sqrt{10}Q_{az}z(x-y)(x+y)}{4} + \frac{\sqrt{6}Q_{bz}z(3x^2+3y^2-2z^2)}{12}$$

$$\vec{\mathbb{G}}_3^{(3,2)}[q](A_g)$$

\*\* symmetry

$$\sqrt{15}xyz$$

\*\* expression

$$\begin{aligned} & - \frac{\sqrt{22}Q_1y(25x^4-55x^2y^2+15x^2z^2+4y^4+15y^2z^2-10z^4)}{88} - \frac{\sqrt{22}Q_2x(4x^4-55x^2y^2+15x^2z^2+25y^4+15y^2z^2-10z^4)}{88} \\ & - \frac{\sqrt{330}Q_{3x}x(4x^4+x^2y^2-41x^2z^2-3y^4+15y^2z^2+18z^4)}{264} - \frac{\sqrt{330}Q_{3y}y(3x^4-x^2y^2-15x^2z^2-4y^4+41y^2z^2-18z^4)}{264} \\ & - \frac{7\sqrt{55}Q_{az}z(x-y)(x+y)(x^2+y^2-2z^2)}{44} + \frac{\sqrt{33}Q_{bz}z(15x^4+30x^2y^2-40x^2z^2+15y^4-40y^2z^2+8z^4)}{132} \end{aligned}$$

$$\vec{\mathbb{G}}_3^{(3,-2)}[q](B_{1g}, 1)$$

\*\* symmetry

$$- \frac{z(3x^2+3y^2-2z^2)}{2}$$

\*\* expression

$$\frac{\sqrt{2}Q_{3xy}}{2} - \frac{\sqrt{2}Q_{3yx}}{2}$$

$$\vec{\mathbb{G}}_3^{(3,-2)}[q](B_{1g}, 2)$$

\*\* symmetry

$$\frac{\sqrt{15}z(x-y)(x+y)}{2}$$

\*\* expression

$$- \frac{\sqrt{2}Q_1x}{4} + \frac{\sqrt{2}Q_2y}{4} + \frac{\sqrt{3}Q_3z}{3} - \frac{\sqrt{30}Q_{3x}y}{12} - \frac{\sqrt{30}Q_{3y}x}{12}$$

$$\vec{\mathbb{G}}_3^{(3,0)}[q](B_{1g}, 1)$$

\*\* symmetry

$$- \frac{z(3x^2+3y^2-2z^2)}{2}$$

\*\* expression

$$\frac{\sqrt{15}Q_1x(x^2-3y^2)}{12} - \frac{\sqrt{15}Q_2y(3x^2-y^2)}{12} - \frac{\sqrt{10}Q_3z(x-y)(x+y)}{4} - \frac{Q_{3xy}(x^2+y^2-4z^2)}{4} + \frac{Q_{3yx}(x^2+y^2-4z^2)}{4} + \frac{\sqrt{10}Q_{bzx}yz}{2}$$

$$\vec{\mathbb{G}}_3^{(3,0)}[q](B_{1g}, 2)$$

\*\* symmetry

$$\frac{\sqrt{15}z(x-y)(x+y)}{2}$$

\*\* expression

$$- \frac{Q_1x(x^2+y^2-4z^2)}{4} + \frac{Q_2y(x^2+y^2-4z^2)}{4} - \frac{\sqrt{6}Q_3z(3x^2+3y^2-2z^2)}{12} - \frac{\sqrt{15}Q_{3xy}(3x^2-y^2)}{12} + \frac{\sqrt{15}Q_{3yx}(x^2-3y^2)}{12} - \frac{\sqrt{10}Q_{az}xyz}{2}$$

$$\vec{\mathbb{G}}_3^{(3,2)}[q](B_{1g}, 1)$$

\*\* symmetry

$$- \frac{z(3x^2+3y^2-2z^2)}{2}$$

\*\* expression

$$\frac{7\sqrt{330}Q_1x(x^2-3y^2)(x^2+y^2-8z^2)}{528} - \frac{7\sqrt{330}Q_2y(3x^2-y^2)(x^2+y^2-8z^2)}{528} + \frac{7\sqrt{55}Q_3z(x-y)(x+y)(x^2+y^2-2z^2)}{44} \\ + \frac{5\sqrt{22}Q_{3xy}(x^4+2x^2y^2-12x^2z^2+y^4-12y^2z^2+8z^4)}{176} - \frac{5\sqrt{22}Q_{3yx}(x^4+2x^2y^2-12x^2z^2+y^4-12y^2z^2+8z^4)}{176} - \frac{7\sqrt{55}Q_{bzy}yz(x^2+y^2-2z^2)}{22}$$

$$\vec{\mathbb{G}}_3^{(3,2)}[q](B_{1g}, 2)$$

\*\* symmetry

$$\frac{\sqrt{15}z(x-y)(x+y)}{2}$$

\*\* expression

$$- \frac{\sqrt{22}Q_1x(13x^4-100x^2y^2-30x^2z^2+55y^4-30y^2z^2+20z^4)}{176} + \frac{\sqrt{22}Q_2y(55x^4-100x^2y^2-30x^2z^2+13y^4-30y^2z^2+20z^4)}{176} \\ - \frac{\sqrt{33}Q_3z(15x^4+30x^2y^2-40x^2z^2+15y^4-40y^2z^2+8z^4)}{132} + \frac{\sqrt{330}Q_{3xy}(15x^4+16x^2y^2-138x^2z^2+y^4-26y^2z^2+36z^4)}{528} \\ + \frac{\sqrt{330}Q_{3yx}(x^4+16x^2y^2-26x^2z^2+15y^4-138y^2z^2+36z^4)}{528} + \frac{7\sqrt{55}Q_{az}xyz(x^2+y^2-2z^2)}{22}$$

$$\vec{\mathbb{G}}_3^{(3,-2)}[q](B_{2g}, 1)$$

\*\* symmetry

$$- \frac{y(3x^2-2y^2+3z^2)}{2}$$

\*\* expression

$$\frac{\sqrt{30}Q_{2z}}{8} + \frac{\sqrt{2}Q_{3xz}}{8} - \frac{\sqrt{3}Q_{azx}}{4} - \frac{\sqrt{5}Q_{bzx}}{4}$$

$$\vec{\mathbb{G}}_3^{(3,-2)}[q](B_{2g}, 2)$$

\*\* symmetry

$$- \frac{\sqrt{15}y(x-z)(x+z)}{2}$$

\*\* expression

$$\frac{3\sqrt{2}Q_{2z}}{8} + \frac{\sqrt{3}Q_{3y}}{3} - \frac{\sqrt{30}Q_{3xz}}{24} + \frac{\sqrt{5}Q_{azx}}{4} + \frac{\sqrt{3}Q_{bzx}}{12}$$

$$\vec{\mathbb{G}}_3^{(3,0)}[q](B_{2g}, 1)$$

\*\* symmetry

$$- \frac{y(3x^2-2y^2+3z^2)}{2}$$

\*\* expression

$$- \frac{\sqrt{15}Q_1xyz}{4} + \frac{\sqrt{15}Q_2z(3y^2-z^2)}{12} + \frac{\sqrt{10}Q_3y(x-z)(x+z)}{4} - \frac{Q_{3xz}(4x^2-y^2-z^2)}{4} \\ + \frac{5Q_{3y}xyz}{4} + \frac{\sqrt{6}Q_{azx}(2x^2-3y^2-3z^2)}{12} - \frac{\sqrt{10}Q_{bzx}(y-z)(y+z)}{4}$$

$$\vec{\mathbb{G}}_3^{(3,0)}[q](B_{2g}, 2)$$

\*\* symmetry

$$- \frac{\sqrt{15}y(x-z)(x+z)}{2}$$

\*\* expression

$$\frac{5Q_1xyz}{4} + \frac{Q_2z(4x^2-y^2-z^2)}{4} - \frac{\sqrt{6}Q_3y(3x^2-2y^2+3z^2)}{12} + \frac{\sqrt{15}Q_{3xz}(3y^2-z^2)}{12} \\ + \frac{\sqrt{15}Q_{3y}xyz}{4} - \frac{\sqrt{10}Q_{azx}(y-z)(y+z)}{4} - \frac{\sqrt{6}Q_{bzx}(2x^2-3y^2-3z^2)}{12}$$

$$\vec{\mathbb{G}}_3^{(3,2)}[q](B_{2g}, 1)$$

\*\* symmetry

$$- \frac{y(3x^2-2y^2+3z^2)}{2}$$

\*\* expression

$$\frac{7\sqrt{330}Q_1xyz(x^2-2y^2+z^2)}{88} + \frac{\sqrt{330}Q_2z(9x^4-87x^2y^2+11x^2z^2+30y^4-31y^2z^2+2z^4)}{528} - \frac{7\sqrt{55}Q_3y(x-z)(x+z)(x^2-2y^2+z^2)}{44} \\ - \frac{5\sqrt{22}Q_{3xz}(5x^4-39x^2y^2+3x^2z^2-2y^4+17y^2z^2-2z^4)}{176} - \frac{35\sqrt{22}Q_{3y}xyz(x^2-2y^2+z^2)}{88} \\ + \frac{5\sqrt{33}Q_{azx}(x^4-5x^2y^2-5x^2z^2-6y^4+51y^2z^2-6z^4)}{264} - \frac{\sqrt{55}Q_{bzx}(3x^4-29x^2y^2-x^2z^2+10y^4+27y^2z^2-4z^4)}{88}$$

$$\vec{\mathbb{G}}_3^{(3,2)}[q](B_{2g}, 2)$$

\*\* symmetry

$$-\frac{\sqrt{15}y(x-z)(x+z)}{2}$$

\*\* expression

$$\begin{aligned} & -\frac{35\sqrt{22}Q_1xyz(x^2-2y^2+z^2)}{88} - \frac{\sqrt{22}Q_2z(5x^4-165x^2y^2+45x^2z^2+40y^4-25y^2z^2-2z^4)}{176} \\ & - \frac{\sqrt{33}Q_3y(15x^4-40x^2y^2+30x^2z^2+8y^4-40y^2z^2+15z^4)}{132} - \frac{\sqrt{330}Q_{3x}z(45x^4-57x^2y^2-71x^2z^2+24y^4-29y^2z^2+10z^4)}{528} \\ & - \frac{7\sqrt{330}Q_{3y}xyz(x^2-2y^2+z^2)}{88} + \frac{\sqrt{55}Q_{az}x(3x^4-x^2y^2-29x^2z^2-4y^4+27y^2z^2+10z^4)}{88} \\ & - \frac{\sqrt{33}Q_{bz}x(11x^4-55x^2y^2-55x^2z^2+60y^4-195y^2z^2+60z^4)}{264} \end{aligned}$$

$$\vec{\mathbb{G}}_3^{(3,-2)}[q](B_{3g}, 1)$$

\*\* symmetry

$$\frac{x(2x^2-3y^2-3z^2)}{2}$$

\*\* expression

$$\frac{\sqrt{30}Q_1z}{8} - \frac{\sqrt{2}Q_{3y}z}{8} + \frac{\sqrt{3}Q_{az}y}{4} - \frac{\sqrt{5}Q_{bz}y}{4}$$

$$\vec{\mathbb{G}}_3^{(3,-2)}[q](B_{3g}, 2)$$

\*\* symmetry

$$\frac{\sqrt{15}x(y-z)(y+z)}{2}$$

\*\* expression

$$-\frac{3\sqrt{2}Q_1z}{8} + \frac{\sqrt{3}Q_{3x}}{3} - \frac{\sqrt{30}Q_{3y}z}{24} + \frac{\sqrt{5}Q_{az}y}{4} - \frac{\sqrt{3}Q_{bz}y}{12}$$

$$\vec{\mathbb{G}}_3^{(3,0)}[q](B_{3g}, 1)$$

\*\* symmetry

$$\frac{x(2x^2-3y^2-3z^2)}{2}$$

\*\* expression

$$\begin{aligned} & \frac{\sqrt{15}Q_1z(3x^2-z^2)}{12} - \frac{\sqrt{15}Q_2xyz}{4} - \frac{\sqrt{10}Q_3x(y-z)(y+z)}{4} - \frac{5Q_{3x}xyz}{4} \\ & - \frac{Q_{3y}z(x^2-4y^2+z^2)}{4} + \frac{\sqrt{6}Q_{az}y(3x^2-2y^2+3z^2)}{12} - \frac{\sqrt{10}Q_{bz}y(x-z)(x+z)}{4} \end{aligned}$$

$$\vec{\mathbb{G}}_3^{(3,0)}[q](B_{3g}, 2)$$

\*\* symmetry

$$\frac{\sqrt{15}x(y-z)(y+z)}{2}$$

\*\* expression

$$\begin{aligned} & \frac{Q_1z(x^2-4y^2+z^2)}{4} - \frac{5Q_2xyz}{4} + \frac{\sqrt{6}Q_3x(2x^2-3y^2-3z^2)}{12} + \frac{\sqrt{15}Q_{3x}xyz}{4} \\ & + \frac{\sqrt{15}Q_{3y}z(3x^2-z^2)}{12} - \frac{\sqrt{10}Q_{az}y(x-z)(x+z)}{4} - \frac{\sqrt{6}Q_{bz}y(3x^2-2y^2+3z^2)}{12} \end{aligned}$$

$$\vec{\mathbb{G}}_3^{(3,2)}[q](B_{3g}, 1)$$

\*\* symmetry

$$\frac{x(2x^2-3y^2-3z^2)}{2}$$

\*\* expression

$$\begin{aligned} & \frac{\sqrt{330}Q_1z(30x^4-87x^2y^2-31x^2z^2+9y^4+11y^2z^2+2z^4)}{528} - \frac{7\sqrt{330}Q_2xyz(2x^2-y^2-z^2)}{88} - \frac{7\sqrt{55}Q_3x(y-z)(y+z)(2x^2-y^2-z^2)}{44} \\ & - \frac{35\sqrt{22}Q_{3x}xyz(2x^2-y^2-z^2)}{88} - \frac{5\sqrt{22}Q_{3y}z(2x^4+39x^2y^2-17x^2z^2-5y^4-3y^2z^2+2z^4)}{176} \\ & + \frac{5\sqrt{33}Q_{az}y(6x^4+5x^2y^2-51x^2z^2-y^4+5y^2z^2+6z^4)}{264} - \frac{\sqrt{55}Q_{bz}y(10x^4-29x^2y^2+27x^2z^2+3y^4-y^2z^2-4z^4)}{88} \end{aligned}$$

$$\vec{\mathbb{G}}_3^{(3,2)}[q](B_{3g}, 2)$$

\*\* symmetry

$$\frac{\sqrt{15}x(y-z)(y+z)}{2}$$

\*\* expression

$$\begin{aligned} & \frac{\sqrt{22}Q_1z(40x^4 - 165x^2y^2 - 25x^2z^2 + 5y^4 + 45y^2z^2 - 2z^4)}{176} - \frac{35\sqrt{22}Q_2xyz(2x^2 - y^2 - z^2)}{88} \\ & - \frac{\sqrt{33}Q_3x(8x^4 - 40x^2y^2 - 40x^2z^2 + 15y^4 + 30y^2z^2 + 15z^4)}{132} + \frac{7\sqrt{330}Q_{3x}xyz(2x^2 - y^2 - z^2)}{88} \\ & - \frac{\sqrt{330}Q_{3y}z(24x^4 - 57x^2y^2 - 29x^2z^2 + 45y^4 - 71y^2z^2 + 10z^4)}{528} \\ & - \frac{\sqrt{55}Q_{az}y(4x^4 + x^2y^2 - 27x^2z^2 - 3y^4 + 29y^2z^2 - 10z^4)}{88} + \frac{\sqrt{33}Q_{bz}y(60x^4 - 55x^2y^2 - 195x^2z^2 + 11y^4 - 55y^2z^2 + 60z^4)}{264} \end{aligned}$$

\* Harmonics for rank 4

$$\vec{\mathbb{G}}_4^{(3,-2)}[q](A_u, 1)$$

\*\* symmetry

$$\frac{\sqrt{21}(x^4 - 3x^2y^2 - 3x^2z^2 + y^4 - 3y^2z^2 + z^4)}{6}$$

\*\* expression

$$\frac{\sqrt{6}Q_1xz}{4} + \frac{\sqrt{6}Q_2yz}{4} + \frac{\sqrt{10}Q_{3x}yz}{4} - \frac{\sqrt{10}Q_{3y}xz}{4} - Q_{bz}xy$$

$$\vec{\mathbb{G}}_4^{(3,-2)}[q](A_u, 2)$$

\*\* symmetry

$$-\frac{\sqrt{15}(x^4 - 12x^2y^2 + 6x^2z^2 + y^4 + 6y^2z^2 - 2z^4)}{12}$$

\*\* expression

$$-\frac{\sqrt{210}Q_1xz}{20} - \frac{\sqrt{210}Q_2yz}{20} + \frac{3\sqrt{35}Q_3(x-y)(x+y)}{35} + \frac{5\sqrt{14}Q_{3x}yz}{28} - \frac{5\sqrt{14}Q_{3y}xz}{28} + \frac{\sqrt{35}Q_{bz}xy}{35}$$

$$\vec{\mathbb{G}}_4^{(3,-2)}[q](A_u, 3)$$

\*\* symmetry

$$\frac{\sqrt{5}(x-y)(x+y)(x^2 + y^2 - 6z^2)}{4}$$

\*\* expression

$$\frac{9\sqrt{70}Q_1xz}{140} - \frac{9\sqrt{70}Q_2yz}{140} + \frac{\sqrt{105}Q_3(x^2 + y^2 - 2z^2)}{35} + \frac{\sqrt{42}Q_{3x}yz}{28} + \frac{\sqrt{42}Q_{3y}xz}{28} + \frac{3\sqrt{7}Q_{az}xy}{7}$$

$$\vec{\mathbb{G}}_4^{(3,0)}[q](A_u, 1)$$

\*\* symmetry

$$\frac{\sqrt{21}(x^4 - 3x^2y^2 - 3x^2z^2 + y^4 - 3y^2z^2 + z^4)}{6}$$

\*\* expression

$$\begin{aligned} & \frac{5\sqrt{33}Q_1xz(5x^2 - 9y^2 - 2z^2)}{132} - \frac{5\sqrt{33}Q_2yz(9x^2 - 5y^2 + 2z^2)}{132} - \frac{\sqrt{55}Q_{3x}yz(15x^2 + y^2 - 6z^2)}{44} \\ & + \frac{\sqrt{55}Q_{3y}xz(x^2 + 15y^2 - 6z^2)}{44} + \frac{7\sqrt{330}Q_{az}xy(x-y)(x+y)}{132} - \frac{5\sqrt{22}Q_{bz}xy(x^2 + y^2 - 6z^2)}{44} \end{aligned}$$

$$\vec{\mathbb{G}}_4^{(3,0)}[q](A_u, 2)$$

\*\* symmetry

$$-\frac{\sqrt{15}(x^4 - 12x^2y^2 + 6x^2z^2 + y^4 + 6y^2z^2 - 2z^4)}{12}$$

\*\* expression

$$\begin{aligned} & \frac{\sqrt{1155}Q_1xz(x^2 - 9y^2 + 2z^2)}{132} - \frac{\sqrt{1155}Q_2yz(9x^2 - y^2 - 2z^2)}{132} + \frac{3\sqrt{770}Q_3(x-y)(x+y)(x^2 + y^2 - 6z^2)}{308} \\ & + \frac{\sqrt{77}Q_{3x}yz(51x^2 - 47y^2 + 30z^2)}{308} + \frac{\sqrt{77}Q_{3y}xz(47x^2 - 51y^2 - 30z^2)}{308} - \frac{7\sqrt{462}Q_{az}xy(x-y)(x+y)}{132} + \frac{\sqrt{770}Q_{bz}xy(x^2 + y^2 - 6z^2)}{308} \end{aligned}$$

$$\vec{\mathbb{G}}_4^{(3,0)}[q](A_u, 3)$$

\*\* symmetry

$$\frac{\sqrt{5}(x-y)(x+y)(x^2+y^2-6z^2)}{4}$$

\*\* expression

$$\begin{aligned} & \frac{5\sqrt{385}Q_{1xz}(3x^2+3y^2-4z^2)}{308} - \frac{5\sqrt{385}Q_{2yz}(3x^2+3y^2-4z^2)}{308} + \frac{\sqrt{2310}Q_3(x^4-12x^2y^2+6x^2z^2+y^4+6y^2z^2-2z^4)}{308} \\ & + \frac{\sqrt{231}Q_{3xyz}(27x^2-y^2-8z^2)}{308} - \frac{\sqrt{231}Q_{3yxz}(x^2-27y^2+8z^2)}{308} - \frac{13\sqrt{154}Q_{azxy}(x^2+y^2-6z^2)}{308} - \frac{\sqrt{2310}Q_{bzyx}(x-y)(x+y)}{44} \end{aligned}$$

$$\tilde{\mathbb{G}}_4^{(3,2)}[q](A_u, 1)$$

\*\* symmetry

$$\frac{\sqrt{21}(x^4-3x^2y^2-3x^2z^2+y^4-3y^2z^2+z^4)}{6}$$

\*\* expression

$$\begin{aligned} & \frac{\sqrt{4290}Q_{1xz}(17x^4-29x^2y^2-47x^2z^2-46y^4+121y^2z^2+2z^4)}{1144} - \frac{\sqrt{4290}Q_{2yz}(46x^4+29x^2y^2-121x^2z^2-17y^4+47y^2z^2-2z^4)}{1144} \\ & - \frac{3\sqrt{715}Q_3(x-y)(x+y)(x-z)(x+z)(y-z)(y+z)}{26} - \frac{5\sqrt{286}Q_{3xyz}(46x^4-91x^2y^2-x^2z^2-5y^4+47y^2z^2-14z^4)}{1144} \\ & - \frac{5\sqrt{286}Q_{3yxz}(5x^4+91x^2y^2-47x^2z^2-46y^4+y^2z^2+14z^4)}{1144} + \frac{15\sqrt{429}Q_{azxy}(x-y)(x+y)(x^2+y^2-10z^2)}{572} \\ & - \frac{\sqrt{715}Q_{bzyx}(19x^4-94x^2y^2+92x^2z^2+19y^4+92y^2z^2-92z^4)}{572} \end{aligned}$$

$$\tilde{\mathbb{G}}_4^{(3,2)}[q](A_u, 2)$$

\*\* symmetry

$$-\frac{\sqrt{15}(x^4-12x^2y^2+6x^2z^2+y^4+6y^2z^2-2z^4)}{12}$$

\*\* expression

$$\begin{aligned} & \frac{\sqrt{6006}Q_{1xz}(10x^4-25x^2y^2-25x^2z^2-35y^4+95y^2z^2-2z^4)}{1144} - \frac{\sqrt{6006}Q_{2yz}(35x^4+25x^2y^2-95x^2z^2-10y^4+25y^2z^2+2z^4)}{1144} \\ & - \frac{3\sqrt{1001}Q_3(x-y)(x+y)(x^4-9x^2y^2-5x^2z^2+y^4-5y^2z^2+5z^4)}{286} \\ & + \frac{\sqrt{10010}Q_{3xyz}(61x^4-61x^2y^2-61x^2z^2+10y^4-13y^2z^2+10z^4)}{1144} - \frac{\sqrt{10010}Q_{3yxz}(10x^4-61x^2y^2-13x^2z^2+61y^4-61y^2z^2+10z^4)}{1144} \\ & - \frac{3\sqrt{15015}Q_{azxy}(x-y)(x+y)(x^2+y^2-10z^2)}{572} + \frac{\sqrt{1001}Q_{bzyx}(31x^4-70x^2y^2-100x^2z^2+31y^4-100y^2z^2+100z^4)}{572} \end{aligned}$$

$$\tilde{\mathbb{G}}_4^{(3,2)}[q](A_u, 3)$$

\*\* symmetry

$$\frac{\sqrt{5}(x-y)(x+y)(x^2+y^2-6z^2)}{4}$$

\*\* expression

$$\begin{aligned} & \frac{9\sqrt{2002}Q_{1xz}(4x^4-25x^2y^2-5x^2z^2+15y^4-5y^2z^2+2z^4)}{1144} - \frac{9\sqrt{2002}Q_{2yz}(15x^4-25x^2y^2-5x^2z^2+4y^4-5y^2z^2+2z^4)}{1144} \\ & - \frac{\sqrt{3003}Q_3(x^6-15x^4z^2+15x^2z^4+y^6-15y^4z^2+15y^2z^4-2z^6)}{286} \\ & - \frac{\sqrt{30030}Q_{3xyz}(13x^4+17x^2y^2-43x^2z^2+4y^4-19y^2z^2+10z^4)}{1144} - \frac{\sqrt{30030}Q_{3yxz}(4x^4+17x^2y^2-19x^2z^2+13y^4-43y^2z^2+10z^4)}{1144} \\ & + \frac{3\sqrt{5005}Q_{azxy}(x^4+2x^2y^2-16x^2z^2+y^4-16y^2z^2+16z^4)}{572} + \frac{3\sqrt{3003}Q_{bzyx}(x-y)(x+y)(x^2+y^2-10z^2)}{572} \end{aligned}$$

$$\tilde{\mathbb{G}}_4^{(3,-2)}[q](B_{1u}, 1)$$

\*\* symmetry

$$\frac{\sqrt{35}xy(x-y)(x+y)}{2}$$

\*\* expression

$$\frac{3\sqrt{10}Q_{1yz}}{10} - \frac{3\sqrt{10}Q_{2xz}}{10} - \frac{\sqrt{15}Q_{3xy}}{5} + \frac{\sqrt{15}Q_{bz}(x-y)(x+y)}{10}$$

$$\tilde{\mathbb{G}}_4^{(3,-2)}[q](B_{1u}, 2)$$

\*\* symmetry

$$-\frac{\sqrt{5}xy(x^2+y^2-6z^2)}{2}$$

\*\* expression

$$\frac{9\sqrt{70}Q_1yz}{140} + \frac{9\sqrt{70}Q_2xz}{140} + \frac{\sqrt{42}Q_3xz}{28} - \frac{\sqrt{42}Q_3yz}{28} + \frac{3\sqrt{7}Q_{az}(x-y)(x+y)}{14} + \frac{\sqrt{105}Q_{bz}(x^2+y^2-2z^2)}{35}$$

$$\vec{G}_4^{(3,0)}[q](B_{1u}, 1)$$

\*\* symmetry

$$\frac{\sqrt{35}xy(x-y)(x+y)}{2}$$

\*\* expression

$$\frac{\sqrt{55}Q_1yz(3x^2+3y^2-4z^2)}{44} - \frac{\sqrt{55}Q_2xz(3x^2+3y^2-4z^2)}{44} - \frac{\sqrt{330}Q_3xy(x^2+y^2-6z^2)}{44} + \frac{7\sqrt{33}Q_3xz(x^2-3y^2)}{44} - \frac{7\sqrt{33}Q_3yz(3x^2-y^2)}{44} - \frac{7\sqrt{22}Q_{az}(x^2-2xy-y^2)(x^2+2xy-y^2)}{88} + \frac{\sqrt{330}Q_{bz}(x-y)(x+y)(x^2+y^2-6z^2)}{88}$$

$$\vec{G}_4^{(3,0)}[q](B_{1u}, 2)$$

\*\* symmetry

$$-\frac{\sqrt{5}xy(x^2+y^2-6z^2)}{2}$$

\*\* expression

$$\frac{5\sqrt{385}Q_1yz(3x^2+3y^2-4z^2)}{308} + \frac{5\sqrt{385}Q_2xz(3x^2+3y^2-4z^2)}{308} - \frac{\sqrt{2310}Q_3xy(x-y)(x+y)}{44} + \frac{\sqrt{231}Q_3xz(13x^2-15y^2-8z^2)}{308} + \frac{\sqrt{231}Q_3yz(15x^2-13y^2+8z^2)}{308} - \frac{13\sqrt{154}Q_{az}(x-y)(x+y)(x^2+y^2-6z^2)}{616} - \frac{\sqrt{2310}Q_{bz}(5x^4-18x^2y^2-12x^2z^2+5y^4-12y^2z^2+4z^4)}{616}$$

$$\vec{G}_4^{(3,2)}[q](B_{1u}, 1)$$

\*\* symmetry

$$\frac{\sqrt{35}xy(x-y)(x+y)}{2}$$

\*\* expression

$$\frac{3\sqrt{286}Q_1yz(5x^4+10x^2y^2-20x^2z^2+5y^4-20y^2z^2+8z^4)}{2288} - \frac{3\sqrt{286}Q_2xz(5x^4+10x^2y^2-20x^2z^2+5y^4-20y^2z^2+8z^4)}{2288} + \frac{\sqrt{429}Q_3xy(47x^4-170x^2y^2+40x^2z^2+47y^4+40y^2z^2-40z^4)}{572} + \frac{3\sqrt{4290}Q_3xz(17x^4-122x^2y^2-16x^2z^2+37y^4+48y^2z^2)}{2288} + \frac{3\sqrt{4290}Q_3yz(37x^4-122x^2y^2+48x^2z^2+17y^4-16y^2z^2)}{2288} - \frac{9\sqrt{715}Q_{az}(x^2+y^2-10z^2)(x^2-2xy-y^2)(x^2+2xy-y^2)}{1144} + \frac{\sqrt{429}Q_{bz}(x-y)(x+y)(19x^4-226x^2y^2-40x^2z^2+19y^4-40y^2z^2+40z^4)}{1144}$$

$$\vec{G}_4^{(3,2)}[q](B_{1u}, 2)$$

\*\* symmetry

$$-\frac{\sqrt{5}xy(x^2+y^2-6z^2)}{2}$$

\*\* expression

$$-\frac{9\sqrt{2002}Q_1yz(25x^4-60x^2y^2+10x^2z^2+3y^4+10y^2z^2-4z^4)}{2288} - \frac{9\sqrt{2002}Q_2xz(3x^4-60x^2y^2+10x^2z^2+25y^4+10y^2z^2-4z^4)}{2288} + \frac{3\sqrt{3003}Q_3xy(x-y)(x+y)(x^2+y^2-10z^2)}{572} - \frac{\sqrt{30030}Q_3xz(17x^4+16x^2y^2-62x^2z^2-y^4-14y^2z^2+20z^4)}{2288} - \frac{\sqrt{30030}Q_3yz(x^4-16x^2y^2+14x^2z^2-17y^4+62y^2z^2-20z^4)}{2288} + \frac{3\sqrt{5005}Q_{az}(x-y)(x+y)(x^4+2x^2y^2-16x^2z^2+y^4-16y^2z^2+16z^4)}{1144} - \frac{\sqrt{3003}Q_{bz}(x^6+15x^4y^2-30x^4z^2+15x^2y^4-180x^2y^2z^2+60x^2z^4+y^6-30y^4z^2+60y^2z^4-8z^6)}{1144}$$

$$\vec{G}_4^{(3,-2)}[q](B_{2u}, 1)$$

\*\* symmetry

$$-\frac{\sqrt{35}xz(x-z)(x+z)}{2}$$

\*\* expression

$$\frac{3\sqrt{10}Q_1(x-z)(x+z)}{40} - \frac{3\sqrt{10}Q_2xy}{40} - \frac{\sqrt{15}Q_3xz}{5} + \frac{3\sqrt{6}Q_3xy}{8} - \frac{\sqrt{6}Q_3y(x-z)(x+z)}{8} - \frac{3Q_{az}yz}{4} + \frac{3\sqrt{15}Q_{bz}yz}{20}$$

$$\vec{G}_4^{(3,-2)}[q](B_{2u}, 2)$$



\*\* symmetry

$$-\frac{\sqrt{5}xz(x^2-6y^2+z^2)}{2}$$

\*\* expression

$$\frac{3\sqrt{70}Q_1(3x^2+4y^2-7z^2)}{280} + \frac{3\sqrt{70}Q_2xy}{280} + \frac{5\sqrt{42}Q_{3x}xy}{56} + \frac{\sqrt{42}Q_{3y}(5x^2-4y^2-z^2)}{56} + \frac{3\sqrt{7}Q_{az}yz}{28} - \frac{\sqrt{105}Q_{bz}yz}{20}$$

$$\vec{\mathbb{G}}_4^{(3,0)}[q](B_{2u}, 1)$$

\*\* symmetry

$$-\frac{\sqrt{35}xz(x-z)(x+z)}{2}$$

\*\* expression

$$\frac{\sqrt{55}Q_1(5x^4-9x^2y^2-21x^2z^2+9y^2z^2+2z^4)}{88} - \frac{\sqrt{55}Q_2xy(6x^2-y^2-15z^2)}{44} - \frac{\sqrt{330}Q_{3xz}(x^2-6y^2+z^2)}{44} + \frac{\sqrt{33}Q_{3xy}(2x^2-5y^2+9z^2)}{44} \\ + \frac{\sqrt{33}Q_{3y}(x^4+15x^2y^2-21x^2z^2-15y^2z^2+6z^4)}{88} + \frac{\sqrt{22}Q_{az}yz(12x^2+5y^2-9z^2)}{44} + \frac{\sqrt{330}Q_{bz}yz(6x^2-y^2-z^2)}{44}$$

$$\vec{\mathbb{G}}_4^{(3,0)}[q](B_{2u}, 2)$$

\*\* symmetry

$$-\frac{\sqrt{5}xz(x^2-6y^2+z^2)}{2}$$

\*\* expression

$$\frac{\sqrt{385}Q_1(x^4+21x^2y^2-27x^2z^2+6y^4-57y^2z^2+14z^4)}{616} + \frac{\sqrt{385}Q_2xy(6x^2-y^2-15z^2)}{308} + \frac{\sqrt{2310}Q_{3xz}(x-z)(x+z)}{44} \\ + \frac{\sqrt{231}Q_{3xy}(22x^2-27y^2+15z^2)}{308} - \frac{\sqrt{231}Q_{3y}(19x^4-69x^2y^2-45x^2z^2+10y^4+9y^2z^2+6z^4)}{616} \\ + \frac{\sqrt{154}Q_{az}yz(30x^2-19y^2+9z^2)}{308} + \frac{\sqrt{2310}Q_{bz}yz(y-z)(y+z)}{44}$$

$$\vec{\mathbb{G}}_4^{(3,2)}[q](B_{2u}, 1)$$

\*\* symmetry

$$-\frac{\sqrt{35}xz(x-z)(x+z)}{2}$$

\*\* expression

$$\frac{3\sqrt{286}Q_1(17x^6-95x^4y^2-160x^4z^2+20x^2y^4+450x^2y^2z^2+85x^2z^4-20y^4z^2-55y^2z^4-2z^6)}{2288} \\ - \frac{3\sqrt{286}Q_2xy(65x^4-65x^2y^2-455x^2z^2+2y^4+175y^2z^2+140z^4)}{2288} \\ + \frac{\sqrt{429}Q_{3xz}(47x^4+40x^2y^2-170x^2z^2-40y^4+40y^2z^2+47z^4)}{572} - \frac{3\sqrt{4290}Q_{3xy}(3x^4+x^2y^2-33x^2z^2-2y^4+17y^2z^2+8z^4)}{2288} \\ - \frac{\sqrt{4290}Q_{3y}(5x^6+25x^4y^2-100x^4z^2+20x^2y^4-270x^2y^2z^2+145x^2z^4-20y^4z^2+65y^2z^4-14z^6)}{2288} \\ - \frac{3\sqrt{715}Q_{az}yz(29x^4+31x^2y^2-89x^2z^2+2y^4-17y^2z^2+14z^4)}{1144} - \frac{3\sqrt{429}Q_{bz}yz(45x^4+65x^2y^2-155x^2z^2-2y^4-15y^2z^2+20z^4)}{1144}$$

$$\vec{\mathbb{G}}_4^{(3,2)}[q](B_{2u}, 2)$$

\*\* symmetry

$$-\frac{\sqrt{5}xz(x^2-6y^2+z^2)}{2}$$

\*\* expression

$$\frac{3\sqrt{2002}Q_1(3x^6-55x^4y^2+10x^4z^2+70x^2y^4-90x^2y^2z^2+5x^2z^4-4y^6-10y^4z^2+25y^2z^4-2z^6)}{2288} \\ - \frac{3\sqrt{2002}Q_2xy(19x^4-85x^2y^2+65x^2z^2+28y^4-25y^2z^2-20z^4)}{2288} \\ - \frac{3\sqrt{3003}Q_{3xz}(x-z)(x+z)(x^2-10y^2+z^2)}{572} - \frac{\sqrt{30030}Q_{3xy}(11x^4+7x^2y^2-131x^2z^2-4y^4+19y^2z^2+56z^4)}{2288} \\ + \frac{\sqrt{30030}Q_{3y}(x^6-9x^4y^2-6x^4z^2-6x^2y^4+90x^2y^2z^2-9x^2z^4+4y^6-54y^4z^2+39y^2z^4-2z^6)}{2288} \\ - \frac{3\sqrt{5005}Q_{az}yz(19x^4+11x^2y^2-49x^2z^2-8y^4+23y^2z^2-2z^4)}{1144} + \frac{\sqrt{3003}Q_{bz}yz(55x^4+5x^2y^2-115x^2z^2+16y^4-55y^2z^2+28z^4)}{1144}$$

$$\vec{\mathbb{G}}_4^{(3,-2)}[q](B_{3u}, 1)$$

\*\* symmetry

$$\frac{\sqrt{35}yz(y-z)(y+z)}{2}$$

\*\* expression

$$\frac{3\sqrt{10}Q_1xy}{40} - \frac{3\sqrt{10}Q_2(y-z)(y+z)}{40} - \frac{\sqrt{15}Q_3yz}{5} - \frac{\sqrt{6}Q_{3x}(y-z)(y+z)}{8} + \frac{3\sqrt{6}Q_{3y}xy}{8} - \frac{3Q_{az}xz}{4} - \frac{3\sqrt{15}Q_{bz}xz}{20}$$

$$\vec{\mathbb{G}}_4^{(3,-2)}[q](B_{3u}, 2)$$

\*\* symmetry

$$\frac{\sqrt{5}yz(6x^2 - y^2 - z^2)}{2}$$

\*\* expression

$$\frac{3\sqrt{70}Q_1xy}{280} + \frac{3\sqrt{70}Q_2(4x^2 + 3y^2 - 7z^2)}{280} + \frac{\sqrt{42}Q_{3x}(4x^2 - 5y^2 + z^2)}{56} - \frac{5\sqrt{42}Q_{3y}xy}{56} - \frac{3\sqrt{7}Q_{az}xz}{28} - \frac{\sqrt{105}Q_{bz}xz}{20}$$

$$\vec{\mathbb{G}}_4^{(3,0)}[q](B_{3u}, 1)$$

\*\* symmetry

$$\frac{\sqrt{35}yz(y-z)(y+z)}{2}$$

\*\* expression

$$\begin{aligned} & -\frac{\sqrt{55}Q_1xy(x^2 - 6y^2 + 15z^2)}{44} + \frac{\sqrt{55}Q_2(9x^2y^2 - 9x^2z^2 - 5y^4 + 21y^2z^2 - 2z^4)}{88} + \frac{\sqrt{330}Q_{3yz}(6x^2 - y^2 - z^2)}{44} \\ & + \frac{\sqrt{33}Q_{3x}(15x^2y^2 - 15x^2z^2 + y^4 - 21y^2z^2 + 6z^4)}{88} - \frac{\sqrt{33}Q_{3y}xy(5x^2 - 2y^2 - 9z^2)}{44} + \frac{\sqrt{22}Q_{az}xz(5x^2 + 12y^2 - 9z^2)}{44} + \frac{\sqrt{330}Q_{bz}xz(x^2 - 6y^2 + z^2)}{44} \end{aligned}$$

$$\vec{\mathbb{G}}_4^{(3,0)}[q](B_{3u}, 2)$$

\*\* symmetry

$$\frac{\sqrt{5}yz(6x^2 - y^2 - z^2)}{2}$$

\*\* expression

$$\begin{aligned} & -\frac{\sqrt{385}Q_1xy(x^2 - 6y^2 + 15z^2)}{308} + \frac{\sqrt{385}Q_2(6x^4 + 21x^2y^2 - 57x^2z^2 + y^4 - 27y^2z^2 + 14z^4)}{616} \\ & -\frac{\sqrt{2310}Q_{3yz}(y-z)(y+z)}{44} + \frac{\sqrt{231}Q_{3x}(10x^4 - 69x^2y^2 + 9x^2z^2 + 19y^4 - 45y^2z^2 + 6z^4)}{616} \\ & + \frac{\sqrt{231}Q_{3y}xy(27x^2 - 22y^2 - 15z^2)}{308} + \frac{\sqrt{154}Q_{az}xz(19x^2 - 30y^2 - 9z^2)}{308} + \frac{\sqrt{2310}Q_{bz}xz(x-z)(x+z)}{44} \end{aligned}$$

$$\vec{\mathbb{G}}_4^{(3,2)}[q](B_{3u}, 1)$$

\*\* symmetry

$$\frac{\sqrt{35}yz(y-z)(y+z)}{2}$$

\*\* expression

$$\begin{aligned} & \frac{3\sqrt{286}Q_1xy(2x^4 - 65x^2y^2 + 175x^2z^2 + 65y^4 - 455y^2z^2 + 140z^4)}{2288} \\ & -\frac{3\sqrt{286}Q_2(20x^4y^2 - 20x^4z^2 - 95x^2y^4 + 450x^2y^2z^2 - 55x^2z^4 + 17y^6 - 160y^4z^2 + 85y^2z^4 - 2z^6)}{2288} \\ & -\frac{\sqrt{429}Q_{3yz}(40x^4 - 40x^2y^2 - 40x^2z^2 - 47y^4 + 170y^2z^2 - 47z^4)}{572} \\ & -\frac{\sqrt{4290}Q_{3x}(20x^4y^2 - 20x^4z^2 + 25x^2y^4 - 270x^2y^2z^2 + 65x^2z^4 + 5y^6 - 100y^4z^2 + 145y^2z^4 - 14z^6)}{2288} \\ & + \frac{3\sqrt{4290}Q_{3y}xy(2x^4 - x^2y^2 - 17x^2z^2 - 3y^4 + 33y^2z^2 - 8z^4)}{2288} - \frac{3\sqrt{715}Q_{az}xz(2x^4 + 31x^2y^2 - 17x^2z^2 + 29y^4 - 89y^2z^2 + 14z^4)}{1144} \\ & -\frac{3\sqrt{429}Q_{bz}xz(2x^4 - 65x^2y^2 + 15x^2z^2 - 45y^4 + 155y^2z^2 - 20z^4)}{1144} \end{aligned}$$

$$\vec{\mathbb{G}}_4^{(3,2)}[q](B_{3u}, 2)$$

\*\* symmetry

$$\frac{\sqrt{5}yz(6x^2 - y^2 - z^2)}{2}$$

\*\* expression

$$\begin{aligned}
& - \frac{3\sqrt{2002}Q_1xy(28x^4 - 85x^2y^2 - 25x^2z^2 + 19y^4 + 65y^2z^2 - 20z^4)}{2288} \\
& - \frac{3\sqrt{2002}Q_2(4x^6 - 70x^4y^2 + 10x^4z^2 + 55x^2y^4 + 90x^2y^2z^2 - 25x^2z^4 - 3y^6 - 10y^4z^2 - 5y^2z^4 + 2z^6)}{2288} \\
& - \frac{3\sqrt{3003}Q_3yz(y-z)(y+z)(10x^2 - y^2 - z^2)}{572} - \frac{\sqrt{30030}Q_{3x}(4x^6 - 6x^4y^2 - 54x^4z^2 - 9x^2y^4 + 90x^2y^2z^2 + 39x^2z^4 + y^6 - 6y^4z^2 - 9y^2z^4 - 2z^6)}{2288} \\
& - \frac{\sqrt{30030}Q_{3y}xy(4x^4 - 7x^2y^2 - 19x^2z^2 - 11y^4 + 131y^2z^2 - 56z^4)}{2288} - \frac{3\sqrt{5005}Q_{az}xz(8x^4 - 11x^2y^2 - 23x^2z^2 - 19y^4 + 49y^2z^2 + 2z^4)}{1144} \\
& + \frac{\sqrt{3003}Q_{bz}xz(16x^4 + 5x^2y^2 - 55x^2z^2 + 55y^4 - 115y^2z^2 + 28z^4)}{1144}
\end{aligned}$$