

PG No. 4  $C_s$   $m$  (b-axis setting) [ monoclinic ] (polar, internal axial dipole)

\* Harmonics for rank 0

\* Harmonics for rank 1

$$\bar{Q}_1^{(1,0)}[g](A', 1)$$

\*\* symmetry

$$x$$

\*\* expression

$$\frac{\sqrt{2}G_y z}{2} - \frac{\sqrt{2}G_z y}{2}$$

$$\bar{Q}_1^{(1,0)}[g](A', 2)$$

\*\* symmetry

$$z$$

\*\* expression

$$\frac{\sqrt{2}G_x y}{2} - \frac{\sqrt{2}G_y x}{2}$$

$$\bar{Q}_1^{(1,0)}[g](A'')$$

\*\* symmetry

$$y$$

\*\* expression

$$-\frac{\sqrt{2}G_x z}{2} + \frac{\sqrt{2}G_z x}{2}$$

\* Harmonics for rank 2

$$\bar{Q}_2^{(1,0)}[g](A', 1)$$

\*\* symmetry

$$-\frac{x^2}{2} - \frac{y^2}{2} + z^2$$

\*\* expression

$$\frac{\sqrt{6}G_x y z}{2} - \frac{\sqrt{6}G_y x z}{2}$$

$$\bar{Q}_2^{(1,0)}[g](A', 2)$$

\*\* symmetry

$$\frac{\sqrt{3}(x-y)(x+y)}{2}$$

\*\* expression

$$\frac{\sqrt{2}G_x y z}{2} + \frac{\sqrt{2}G_y x z}{2} - \sqrt{2}G_z x y$$

$$\bar{Q}_2^{(1,0)}[g](A', 3)$$

\*\* symmetry

$$\sqrt{3}x z$$

\*\* expression

$$\frac{\sqrt{2}G_x x y}{2} - \frac{\sqrt{2}G_y (x-z)(x+z)}{2} - \frac{\sqrt{2}G_z y z}{2}$$

$$\bar{Q}_2^{(1,0)}[g](A'', 1)$$

\*\* symmetry

$$\sqrt{3}y z$$

\*\* expression

$$\frac{\sqrt{2}G_x (y-z)(y+z)}{2} - \frac{\sqrt{2}G_y x y}{2} + \frac{\sqrt{2}G_z x z}{2}$$

$$\bar{Q}_2^{(1,0)}[g](A'', 2)$$

\*\* symmetry

$$\sqrt{3}x y$$

\*\* expression

$$-\frac{\sqrt{2}G_x x z}{2} + \frac{\sqrt{2}G_y y z}{2} + \frac{\sqrt{2}G_z (x-y)(x+y)}{2}$$

\* Harmonics for rank 3

$$\tilde{\mathbb{Q}}_3^{(1,0)}[g](A', 1)$$

\*\* symmetry

$$\frac{x(2x^2 - 3y^2 - 3z^2)}{2}$$

\*\* expression

$$\frac{\sqrt{3}G_y z(4x^2 - y^2 - z^2)}{4} - \frac{\sqrt{3}G_z y(4x^2 - y^2 - z^2)}{4}$$

$$\tilde{\mathbb{Q}}_3^{(1,0)}[g](A', 2)$$

\*\* symmetry

$$-\frac{z(3x^2 + 3y^2 - 2z^2)}{2}$$

\*\* expression

$$-\frac{\sqrt{3}G_x y(x^2 + y^2 - 4z^2)}{4} + \frac{\sqrt{3}G_y x(x^2 + y^2 - 4z^2)}{4}$$

$$\tilde{\mathbb{Q}}_3^{(1,0)}[g](A', 3)$$

\*\* symmetry

$$\frac{\sqrt{15}x(y-z)(y+z)}{2}$$

\*\* expression

$$-\sqrt{5}G_x x y z + \frac{\sqrt{5}G_y z(2x^2 + y^2 - z^2)}{4} + \frac{\sqrt{5}G_z y(2x^2 - y^2 + z^2)}{4}$$

$$\tilde{\mathbb{Q}}_3^{(1,0)}[g](A', 4)$$

\*\* symmetry

$$\frac{\sqrt{15}z(x-y)(x+y)}{2}$$

\*\* expression

$$\frac{\sqrt{5}G_x y(x^2 - y^2 + 2z^2)}{4} - \frac{\sqrt{5}G_y x(x^2 - y^2 - 2z^2)}{4} - \sqrt{5}G_z x y z$$

$$\tilde{\mathbb{Q}}_3^{(1,0)}[g](A'', 1)$$

\*\* symmetry

$$\sqrt{15}x y z$$

\*\* expression

$$\frac{\sqrt{5}G_x x(y-z)(y+z)}{2} - \frac{\sqrt{5}G_y y(x-z)(x+z)}{2} + \frac{\sqrt{5}G_z z(x-y)(x+y)}{2}$$

$$\tilde{\mathbb{Q}}_3^{(1,0)}[g](A'', 2)$$

\*\* symmetry

$$-\frac{y(3x^2 - 2y^2 + 3z^2)}{2}$$

\*\* expression

$$\frac{\sqrt{3}G_x z(x^2 - 4y^2 + z^2)}{4} - \frac{\sqrt{3}G_z x(x^2 - 4y^2 + z^2)}{4}$$

$$\tilde{\mathbb{Q}}_3^{(1,0)}[g](A'', 3)$$

\*\* symmetry

$$-\frac{\sqrt{15}y(x-z)(x+z)}{2}$$

\*\* expression

$$\frac{\sqrt{5}G_x z(x^2 + 2y^2 - z^2)}{4} - \sqrt{5}G_y x y z - \frac{\sqrt{5}G_z x(x^2 - 2y^2 - z^2)}{4}$$

\* Harmonics for rank 4

$$\bar{\mathbb{Q}}_4^{(1,0)}[g](A', 1)$$

\*\* symmetry

$$\frac{\sqrt{21} (x^4 - 3x^2y^2 - 3x^2z^2 + y^4 - 3y^2z^2 + z^4)}{6}$$

\*\* expression

$$-\frac{\sqrt{105}G_x y z (y - z) (y + z)}{6} + \frac{\sqrt{105}G_y x z (x - z) (x + z)}{6} - \frac{\sqrt{105}G_z x y (x - y) (x + y)}{6}$$

$$\bar{\mathbb{Q}}_4^{(1,0)}[g](A', 2)$$

\*\* symmetry

$$-\frac{\sqrt{15} (x^4 - 12x^2y^2 + 6x^2z^2 + y^4 + 6y^2z^2 - 2z^4)}{12}$$

\*\* expression

$$-\frac{\sqrt{3}G_x y z (9x^2 + 2y^2 - 5z^2)}{6} + \frac{\sqrt{3}G_y x z (2x^2 + 9y^2 - 5z^2)}{6} + \frac{7\sqrt{3}G_z x y (x - y) (x + y)}{6}$$

$$\bar{\mathbb{Q}}_4^{(1,0)}[g](A', 3)$$

\*\* symmetry

$$\frac{\sqrt{5} (x - y) (x + y) (x^2 + y^2 - 6z^2)}{4}$$

\*\* expression

$$-\frac{G_x y z (3x^2 - 4y^2 + 3z^2)}{2} + \frac{G_y x z (4x^2 - 3y^2 - 3z^2)}{2} - \frac{G_z x y (x^2 + y^2 - 6z^2)}{2}$$

$$\bar{\mathbb{Q}}_4^{(1,0)}[g](A', 4)$$

\*\* symmetry

$$-\frac{\sqrt{35} x z (x - z) (x + z)}{2}$$

\*\* expression

$$-\frac{\sqrt{7}G_x x y (x^2 - 3z^2)}{4} + \frac{\sqrt{7}G_y (x^2 - 2xz - z^2) (x^2 + 2xz - z^2)}{4} + \frac{\sqrt{7}G_z y z (3x^2 - z^2)}{4}$$

$$\bar{\mathbb{Q}}_4^{(1,0)}[g](A', 5)$$

\*\* symmetry

$$-\frac{\sqrt{5} x z (x^2 - 6y^2 + z^2)}{2}$$

\*\* expression

$$-\frac{G_x x y (x^2 - 6y^2 + 15z^2)}{4} + \frac{G_y (x - z) (x + z) (x^2 - 6y^2 + z^2)}{4} + \frac{G_z y z (15x^2 - 6y^2 + z^2)}{4}$$

$$\bar{\mathbb{Q}}_4^{(1,0)}[g](A'', 1)$$

\*\* symmetry

$$\frac{\sqrt{35} y z (y - z) (y + z)}{2}$$

\*\* expression

$$\frac{\sqrt{7}G_x (y^2 - 2yz - z^2) (y^2 + 2yz - z^2)}{4} - \frac{\sqrt{7}G_y x y (y^2 - 3z^2)}{4} + \frac{\sqrt{7}G_z x z (3y^2 - z^2)}{4}$$

$$\bar{\mathbb{Q}}_4^{(1,0)}[g](A'', 2)$$

\*\* symmetry

$$\frac{\sqrt{35} x y (x - y) (x + y)}{2}$$

\*\* expression

$$-\frac{\sqrt{7}G_x x z (x^2 - 3y^2)}{4} + \frac{\sqrt{7}G_y y z (3x^2 - y^2)}{4} + \frac{\sqrt{7}G_z (x^2 - 2xy - y^2) (x^2 + 2xy - y^2)}{4}$$

$$\bar{\mathbb{Q}}_4^{(1,0)}[g](A'', 3)$$

\*\* symmetry

$$\frac{\sqrt{5} y z (6x^2 - y^2 - z^2)}{2}$$

\*\* expression

$$\frac{G_x (y-z) (y+z) (6x^2 - y^2 - z^2)}{4} - \frac{G_y xy (6x^2 - y^2 - 15z^2)}{4} + \frac{G_z xz (6x^2 - 15y^2 - z^2)}{4}$$

$$\vec{\mathbb{Q}}_4^{(1,0)}[g](A'',4)$$

\*\* symmetry

$$-\frac{\sqrt{5}xy\left(x^2+y^2-6z^2\right)}{2}$$

\*\* expression

$$\frac{G_x xz \left(x^2+15y^2-6z^2\right)}{4}-\frac{G_y yz \left(15x^2+y^2-6z^2\right)}{4}-\frac{G_z \left(x-y\right) \left(x+y\right) \left(x^2+y^2-6z^2\right)}{4}$$