

MSG No. 211.57 $I4321'$ [Type II, cubic]

Table 1: Wyckoff site: 2a, site symmetry: $4321'$

No.	position	mapping
1	$[0, 0, 0]$	$[1, 2, 3, 4, 5, 6, 7, 8, 9, 10, 11, 12, 13, 14, 15, 16, 17, 18, 19, 20, 21, 22, 23, 24,$ $49, 50, 51, 52, 53, 54, 55, 56, 57, 58, 59, 60, 61, 62, 63, 64, 65, 66, 67, 68, 69, 70, 71, 72]$
2	$[\frac{1}{2}, \frac{1}{2}, \frac{1}{2}]$	$[25, 26, 27, 28, 29, 30, 31, 32, 33, 34, 35, 36, 37, 38, 39, 40, 41, 42, 43, 44, 45, 46, 47, 48,$ $73, 74, 75, 76, 77, 78, 79, 80, 81, 82, 83, 84, 85, 86, 87, 88, 89, 90, 91, 92, 93, 94, 95, 96]$

Table 2: Wyckoff site: 6b, site symmetry: $42.21'$

No.	position	mapping
1	$[0, \frac{1}{2}, \frac{1}{2}]$	$[1, 2, 3, 8, 9, 10, 13, 14, 49, 50, 51, 56, 57, 58, 61, 62]$
2	$[\frac{1}{2}, \frac{1}{2}, 0]$	$[4, 5, 15, 16, 18, 19, 21, 23, 52, 53, 63, 64, 66, 67, 69, 71]$
3	$[\frac{1}{2}, 0, \frac{1}{2}]$	$[6, 7, 11, 12, 17, 20, 22, 24, 54, 55, 59, 60, 65, 68, 70, 72]$
4	$[\frac{1}{2}, 0, 0]$	$[25, 26, 27, 32, 33, 34, 37, 38, 73, 74, 75, 80, 81, 82, 85, 86]$
5	$[0, 0, \frac{1}{2}]$	$[28, 29, 39, 40, 42, 43, 45, 47, 76, 77, 87, 88, 90, 91, 93, 95]$
6	$[0, \frac{1}{2}, 0]$	$[30, 31, 35, 36, 41, 44, 46, 48, 78, 79, 83, 84, 89, 92, 94, 96]$

Table 3: Wyckoff site: 8c, site symmetry: $.321'$

No.	position	mapping
1	$[\frac{1}{4}, \frac{1}{4}, \frac{1}{4}]$	$[1, 17, 18, 36, 38, 40, 49, 65, 66, 84, 86, 88]$
2	$[\frac{1}{4}, \frac{3}{4}, \frac{1}{4}]$	$[2, 7, 15, 33, 43, 48, 50, 55, 63, 81, 91, 96]$
3	$[\frac{1}{4}, \frac{1}{4}, \frac{3}{4}]$	$[3, 4, 11, 34, 44, 45, 51, 52, 59, 82, 92, 93]$
4	$[\frac{3}{4}, \frac{1}{4}, \frac{1}{4}]$	$[5, 6, 13, 32, 46, 47, 53, 54, 61, 80, 94, 95]$
5	$[\frac{1}{4}, \frac{3}{4}, \frac{3}{4}]$	$[8, 22, 23, 29, 30, 37, 56, 70, 71, 77, 78, 85]$
6	$[\frac{3}{4}, \frac{1}{4}, \frac{3}{4}]$	$[9, 19, 24, 26, 31, 39, 57, 67, 72, 74, 79, 87]$
7	$[\frac{3}{4}, \frac{3}{4}, \frac{1}{4}]$	$[10, 20, 21, 27, 28, 35, 58, 68, 69, 75, 76, 83]$
8	$[\frac{3}{4}, \frac{3}{4}, \frac{3}{4}]$	$[12, 14, 16, 25, 41, 42, 60, 62, 64, 73, 89, 90]$

Table 4: Wyckoff site: 12d, site symmetry: $2.221'$

No.	position	mapping
1	$[\frac{1}{4}, \frac{1}{2}, 0]$	$[1, 8, 37, 38, 49, 56, 85, 86]$
2	$[\frac{1}{4}, 0, \frac{1}{2}]$	$[2, 3, 33, 34, 50, 51, 81, 82]$
3	$[0, \frac{1}{2}, \frac{3}{4}]$	$[4, 16, 42, 45, 52, 64, 90, 93]$
4	$[0, \frac{1}{2}, \frac{1}{4}]$	$[5, 15, 43, 47, 53, 63, 91, 95]$
5	$[\frac{1}{2}, \frac{1}{4}, 0]$	$[6, 11, 44, 46, 54, 59, 92, 94]$
6	$[\frac{1}{2}, \frac{3}{4}, 0]$	$[7, 12, 41, 48, 55, 60, 89, 96]$
7	$[\frac{3}{4}, \frac{1}{2}, 0]$	$[9, 10, 26, 27, 57, 58, 74, 75]$

continued ...

Table 4

No.	position	mapping
8	$[\frac{3}{4}, 0, \frac{1}{2}]$	[13, 14, 25, 32, 61, 62, 73, 80]
9	$[0, \frac{1}{4}, \frac{1}{2}]$	[17, 24, 31, 36, 65, 72, 79, 84]
10	$[\frac{1}{2}, 0, \frac{1}{4}]$	[18, 21, 28, 40, 66, 69, 76, 88]
11	$[\frac{1}{2}, 0, \frac{3}{4}]$	[19, 23, 29, 39, 67, 71, 77, 87]
12	$[0, \frac{3}{4}, \frac{1}{2}]$	[20, 22, 30, 35, 68, 70, 78, 83]

Table 5: Wyckoff site: 12e, site symmetry: $4..1'$

No.	position	mapping
1	$[x, 0, 0]$	[1, 2, 3, 8, 49, 50, 51, 56]
2	$[0, 0, -x]$	[4, 16, 19, 23, 52, 64, 67, 71]
3	$[0, 0, x]$	[5, 15, 18, 21, 53, 63, 66, 69]
4	$[0, x, 0]$	[6, 11, 17, 24, 54, 59, 65, 72]
5	$[0, -x, 0]$	[7, 12, 20, 22, 55, 60, 68, 70]
6	$[-x, 0, 0]$	[9, 10, 13, 14, 57, 58, 61, 62]
7	$[x + \frac{1}{2}, \frac{1}{2}, \frac{1}{2}]$	[25, 26, 27, 32, 73, 74, 75, 80]
8	$[\frac{1}{2}, \frac{1}{2}, \frac{1}{2} - x]$	[28, 40, 43, 47, 76, 88, 91, 95]
9	$[\frac{1}{2}, \frac{1}{2}, x + \frac{1}{2}]$	[29, 39, 42, 45, 77, 87, 90, 93]
10	$[\frac{1}{2}, x + \frac{1}{2}, \frac{1}{2}]$	[30, 35, 41, 48, 78, 83, 89, 96]
11	$[\frac{1}{2}, \frac{1}{2} - x, \frac{1}{2}]$	[31, 36, 44, 46, 79, 84, 92, 94]
12	$[\frac{1}{2} - x, \frac{1}{2}, \frac{1}{2}]$	[33, 34, 37, 38, 81, 82, 85, 86]

Table 6: Wyckoff site: 16f, site symmetry: $.3.1'$

No.	position	mapping
1	$[x, x, x]$	[1, 17, 18, 49, 65, 66]
2	$[x, -x, x]$	[2, 7, 15, 50, 55, 63]
3	$[x, x, -x]$	[3, 4, 11, 51, 52, 59]
4	$[-x, x, x]$	[5, 6, 13, 53, 54, 61]
5	$[x, -x, -x]$	[8, 22, 23, 56, 70, 71]
6	$[-x, x, -x]$	[9, 19, 24, 57, 67, 72]
7	$[-x, -x, x]$	[10, 20, 21, 58, 68, 69]
8	$[-x, -x, -x]$	[12, 14, 16, 60, 62, 64]
9	$[x + \frac{1}{2}, x + \frac{1}{2}, x + \frac{1}{2}]$	[25, 41, 42, 73, 89, 90]
10	$[x + \frac{1}{2}, \frac{1}{2} - x, x + \frac{1}{2}]$	[26, 31, 39, 74, 79, 87]
11	$[x + \frac{1}{2}, x + \frac{1}{2}, \frac{1}{2} - x]$	[27, 28, 35, 75, 76, 83]
12	$[\frac{1}{2} - x, x + \frac{1}{2}, x + \frac{1}{2}]$	[29, 30, 37, 77, 78, 85]
13	$[x + \frac{1}{2}, \frac{1}{2} - x, \frac{1}{2} - x]$	[32, 46, 47, 80, 94, 95]
14	$[\frac{1}{2} - x, x + \frac{1}{2}, \frac{1}{2} - x]$	[33, 43, 48, 81, 91, 96]
15	$[\frac{1}{2} - x, \frac{1}{2} - x, x + \frac{1}{2}]$	[34, 44, 45, 82, 92, 93]
16	$[\frac{1}{2} - x, \frac{1}{2} - x, \frac{1}{2} - x]$	[36, 38, 40, 84, 86, 88]

Table 7: Wyckoff site: 24g, site symmetry: $2..1'$

No.	position	mapping
1	$[x, \frac{1}{2}, 0]$	[1, 8, 49, 56]
2	$[x, 0, \frac{1}{2}]$	[2, 3, 50, 51]
3	$[0, \frac{1}{2}, -x]$	[4, 16, 52, 64]
4	$[0, \frac{1}{2}, x]$	[5, 15, 53, 63]
5	$[\frac{1}{2}, x, 0]$	[6, 11, 54, 59]
6	$[\frac{1}{2}, -x, 0]$	[7, 12, 55, 60]
7	$[-x, \frac{1}{2}, 0]$	[9, 10, 57, 58]
8	$[-x, 0, \frac{1}{2}]$	[13, 14, 61, 62]
9	$[0, x, \frac{1}{2}]$	[17, 24, 65, 72]
10	$[\frac{1}{2}, 0, x]$	[18, 21, 66, 69]
11	$[\frac{1}{2}, 0, -x]$	[19, 23, 67, 71]
12	$[0, -x, \frac{1}{2}]$	[20, 22, 68, 70]
13	$[x + \frac{1}{2}, 0, \frac{1}{2}]$	[25, 32, 73, 80]
14	$[x + \frac{1}{2}, \frac{1}{2}, 0]$	[26, 27, 74, 75]
15	$[\frac{1}{2}, 0, \frac{1}{2} - x]$	[28, 40, 76, 88]
16	$[\frac{1}{2}, 0, x + \frac{1}{2}]$	[29, 39, 77, 87]
17	$[0, x + \frac{1}{2}, \frac{1}{2}]$	[30, 35, 78, 83]
18	$[0, \frac{1}{2} - x, \frac{1}{2}]$	[31, 36, 79, 84]
19	$[\frac{1}{2} - x, 0, \frac{1}{2}]$	[33, 34, 81, 82]
20	$[\frac{1}{2} - x, \frac{1}{2}, 0]$	[37, 38, 85, 86]
21	$[\frac{1}{2}, x + \frac{1}{2}, 0]$	[41, 48, 89, 96]
22	$[0, \frac{1}{2}, x + \frac{1}{2}]$	[42, 45, 90, 93]
23	$[0, \frac{1}{2}, \frac{1}{2} - x]$	[43, 47, 91, 95]
24	$[\frac{1}{2}, \frac{1}{2} - x, 0]$	[44, 46, 92, 94]

Table 8: Wyckoff site: 24h, site symmetry: $..21'$

No.	position	mapping
1	$[0, y, y]$	[1, 13, 49, 61]
2	$[0, -y, y]$	[2, 10, 50, 58]
3	$[0, y, -y]$	[3, 9, 51, 57]
4	$[y, y, 0]$	[4, 18, 52, 66]
5	$[-y, y, 0]$	[5, 19, 53, 67]
6	$[-y, 0, y]$	[6, 20, 54, 68]
7	$[y, 0, y]$	[7, 17, 55, 65]
8	$[0, -y, -y]$	[8, 14, 56, 62]
9	$[y, 0, -y]$	[11, 22, 59, 70]
10	$[-y, 0, -y]$	[12, 24, 60, 72]
11	$[y, -y, 0]$	[15, 23, 63, 71]
12	$[-y, -y, 0]$	[16, 21, 64, 69]
13	$[\frac{1}{2}, y + \frac{1}{2}, y + \frac{1}{2}]$	[25, 37, 73, 85]
14	$[\frac{1}{2}, \frac{1}{2} - y, y + \frac{1}{2}]$	[26, 34, 74, 82]
15	$[\frac{1}{2}, y + \frac{1}{2}, \frac{1}{2} - y]$	[27, 33, 75, 81]

continued ...

Table 8

No.	position	mapping
16	$[y + \frac{1}{2}, y + \frac{1}{2}, \frac{1}{2}]$	[28, 42, 76, 90]
17	$[\frac{1}{2} - y, y + \frac{1}{2}, \frac{1}{2}]$	[29, 43, 77, 91]
18	$[\frac{1}{2} - y, \frac{1}{2}, y + \frac{1}{2}]$	[30, 44, 78, 92]
19	$[y + \frac{1}{2}, \frac{1}{2}, y + \frac{1}{2}]$	[31, 41, 79, 89]
20	$[\frac{1}{2}, \frac{1}{2} - y, \frac{1}{2} - y]$	[32, 38, 80, 86]
21	$[y + \frac{1}{2}, \frac{1}{2}, \frac{1}{2} - y]$	[35, 46, 83, 94]
22	$[\frac{1}{2} - y, \frac{1}{2}, \frac{1}{2} - y]$	[36, 48, 84, 96]
23	$[y + \frac{1}{2}, \frac{1}{2} - y, \frac{1}{2}]$	[39, 47, 87, 95]
24	$[\frac{1}{2} - y, \frac{1}{2} - y, \frac{1}{2}]$	[40, 45, 88, 93]

Table 9: Wyckoff site: 24i, site symmetry: $\dots 21'$

No.	position	mapping
1	$[\frac{1}{4}, y, \frac{1}{2} - y]$	[1, 38, 49, 86]
2	$[\frac{1}{4}, y + \frac{1}{2}, y]$	[2, 33, 50, 81]
3	$[\frac{1}{4}, \frac{1}{2} - y, -y]$	[3, 34, 51, 82]
4	$[\frac{1}{2} - y, y, \frac{3}{4}]$	[4, 45, 52, 93]
5	$[y + \frac{1}{2}, y, \frac{1}{4}]$	[5, 47, 53, 95]
6	$[-y, \frac{1}{4}, \frac{1}{2} - y]$	[6, 46, 54, 94]
7	$[y, \frac{3}{4}, \frac{1}{2} - y]$	[7, 48, 55, 96]
8	$[\frac{1}{4}, -y, y + \frac{1}{2}]$	[8, 37, 56, 85]
9	$[\frac{3}{4}, y, y + \frac{1}{2}]$	[9, 26, 57, 74]
10	$[\frac{3}{4}, -y, \frac{1}{2} - y]$	[10, 27, 58, 75]
11	$[y, \frac{1}{4}, y + \frac{1}{2}]$	[11, 44, 59, 92]
12	$[-y, \frac{3}{4}, y + \frac{1}{2}]$	[12, 41, 60, 89]
13	$[\frac{3}{4}, \frac{1}{2} - y, y]$	[13, 32, 61, 80]
14	$[\frac{3}{4}, y + \frac{1}{2}, -y]$	[14, 25, 62, 73]
15	$[\frac{1}{2} - y, -y, \frac{1}{4}]$	[15, 43, 63, 91]
16	$[y + \frac{1}{2}, -y, \frac{3}{4}]$	[16, 42, 64, 90]
17	$[\frac{1}{2} - y, \frac{1}{4}, y]$	[17, 36, 65, 84]
18	$[y, \frac{1}{2} - y, \frac{1}{4}]$	[18, 40, 66, 88]
19	$[-y, \frac{1}{2} - y, \frac{3}{4}]$	[19, 39, 67, 87]
20	$[y + \frac{1}{2}, \frac{3}{4}, y]$	[20, 35, 68, 83]
21	$[-y, y + \frac{1}{2}, \frac{1}{4}]$	[21, 28, 69, 76]
22	$[\frac{1}{2} - y, \frac{3}{4}, -y]$	[22, 30, 70, 78]
23	$[y, y + \frac{1}{2}, \frac{3}{4}]$	[23, 29, 71, 77]
24	$[y + \frac{1}{2}, \frac{1}{4}, -y]$	[24, 31, 72, 79]

Table 10: Wyckoff site: 48j, site symmetry: 11'

No.	position	mapping
1	$[x, y, z]$	[1,49]
2	$[x, -z, y]$	[2,50]
3	$[x, z, -y]$	[3,51]
4	$[z, y, -x]$	[4,52]
5	$[-z, y, x]$	[5,53]
6	$[-y, x, z]$	[6,54]
7	$[y, -x, z]$	[7,55]
8	$[x, -y, -z]$	[8,56]
9	$[-x, y, -z]$	[9,57]
10	$[-x, -y, z]$	[10,58]
11	$[y, x, -z]$	[11,59]
12	$[-y, -x, -z]$	[12,60]
13	$[-x, z, y]$	[13,61]
14	$[-x, -z, -y]$	[14,62]
15	$[z, -y, x]$	[15,63]
16	$[-z, -y, -x]$	[16,64]
17	$[z, x, y]$	[17,65]
18	$[y, z, x]$	[18,66]
19	$[-y, z, -x]$	[19,67]
20	$[-z, -x, y]$	[20,68]
21	$[-y, -z, x]$	[21,69]
22	$[z, -x, -y]$	[22,70]
23	$[y, -z, -x]$	[23,71]
24	$[-z, x, -y]$	[24,72]
25	$[x + \frac{1}{2}, y + \frac{1}{2}, z + \frac{1}{2}]$	[25,73]
26	$[x + \frac{1}{2}, \frac{1}{2} - z, y + \frac{1}{2}]$	[26,74]
27	$[x + \frac{1}{2}, z + \frac{1}{2}, \frac{1}{2} - y]$	[27,75]
28	$[z + \frac{1}{2}, y + \frac{1}{2}, \frac{1}{2} - x]$	[28,76]
29	$[\frac{1}{2} - z, y + \frac{1}{2}, x + \frac{1}{2}]$	[29,77]
30	$[\frac{1}{2} - y, x + \frac{1}{2}, z + \frac{1}{2}]$	[30,78]
31	$[y + \frac{1}{2}, \frac{1}{2} - x, z + \frac{1}{2}]$	[31,79]
32	$[x + \frac{1}{2}, \frac{1}{2} - y, \frac{1}{2} - z]$	[32,80]
33	$[\frac{1}{2} - x, y + \frac{1}{2}, \frac{1}{2} - z]$	[33,81]
34	$[\frac{1}{2} - x, \frac{1}{2} - y, z + \frac{1}{2}]$	[34,82]
35	$[y + \frac{1}{2}, x + \frac{1}{2}, \frac{1}{2} - z]$	[35,83]
36	$[\frac{1}{2} - y, \frac{1}{2} - x, \frac{1}{2} - z]$	[36,84]
37	$[\frac{1}{2} - x, z + \frac{1}{2}, y + \frac{1}{2}]$	[37,85]
38	$[\frac{1}{2} - x, \frac{1}{2} - z, \frac{1}{2} - y]$	[38,86]
39	$[z + \frac{1}{2}, \frac{1}{2} - y, x + \frac{1}{2}]$	[39,87]
40	$[\frac{1}{2} - z, \frac{1}{2} - y, \frac{1}{2} - x]$	[40,88]
41	$[z + \frac{1}{2}, x + \frac{1}{2}, y + \frac{1}{2}]$	[41,89]
42	$[y + \frac{1}{2}, z + \frac{1}{2}, x + \frac{1}{2}]$	[42,90]
43	$[\frac{1}{2} - y, z + \frac{1}{2}, \frac{1}{2} - x]$	[43,91]
44	$[\frac{1}{2} - z, \frac{1}{2} - x, y + \frac{1}{2}]$	[44,92]
45	$[\frac{1}{2} - y, \frac{1}{2} - z, x + \frac{1}{2}]$	[45,93]
46	$[z + \frac{1}{2}, \frac{1}{2} - x, \frac{1}{2} - y]$	[46,94]

continued ...

Table 10

No.	position	mapping
47	$[y + \frac{1}{2}, \frac{1}{2} - z, \frac{1}{2} - x]$	[47,95]
48	$[\frac{1}{2} - z, x + \frac{1}{2}, \frac{1}{2} - y]$	[48,96]