

\* character table ( $\omega = e^{2\pi i/3}$ )

| $C_{3i}(c)$ | 1(1) | $3^+_{001}(1)$ | $3^-_{001}(1)$ | -1(1) | $-3^+_{001}(1)$ | $-3^-_{001}(1)$ |
|-------------|------|----------------|----------------|-------|-----------------|-----------------|
| $A_g$       | 1    | 1              |                | 1     | 1               | 1               |
| $E_g^{(a)}$ | 1    | $\omega^*$     | $\omega$       | 1     | $\omega^*$      | $\omega$        |
| $E_g^{(b)}$ | 1    | $\omega$       | $\omega^*$     | 1     | $\omega$        | $\omega^*$      |
| $A_u$       | 1    | 1              |                | -1    | -1              | -1              |
| $E_u^{(a)}$ | 1    | $\omega^*$     | $\omega$       | -1    | $-\omega^*$     | $-\omega$       |
| $E_u^{(b)}$ | 1    | $\omega$       | $\omega^*$     | -1    | $-\omega$       | $-\omega^*$     |

\* polar  $\leftrightarrow$  axial conversion $A_g$  ( $A_u$ )    $E_g^{(a)}$  ( $E_u^{(a)}$ )    $E_g^{(b)}$  ( $E_u^{(b)}$ )    $A_u$  ( $A_g$ )    $E_u^{(a)}$  ( $E_g^{(a)}$ )    $E_u^{(b)}$  ( $E_g^{(b)}$ )

\* symmetric product

|             | $A_g$ | $E_g^{(a)}$ | $E_g^{(b)}$ | $A_u$       | $E_u^{(a)}$ | $E_u^{(b)}$ |
|-------------|-------|-------------|-------------|-------------|-------------|-------------|
| $A_g$       | $A_g$ | $E_g^{(a)}$ | $E_g^{(b)}$ | $A_u$       | $E_u^{(a)}$ | $E_u^{(b)}$ |
| $E_g^{(a)}$ |       | $E_g^{(b)}$ | $A_g$       | $E_u^{(a)}$ | $E_u^{(b)}$ | $A_u$       |
| $E_g^{(b)}$ |       |             | $E_g^{(a)}$ | $E_u^{(b)}$ | $A_u$       | $E_u^{(a)}$ |
| $A_u$       |       |             |             | $A_g$       | $E_g^{(a)}$ | $E_g^{(b)}$ |
| $E_u^{(a)}$ |       |             |             |             | $E_g^{(b)}$ | $A_g$       |
| $E_u^{(b)}$ |       |             |             |             |             | $E_g^{(a)}$ |

\* anti-symmetric product

|  | $A_g$ | $E_g^{(a)}$ | $E_g^{(b)}$ | $A_u$ | $E_u^{(a)}$ | $E_u^{(b)}$ |
|--|-------|-------------|-------------|-------|-------------|-------------|
|  | -     | -           | -           | -     | -           | -           |