

SG No. 99 C_{4v}^1 $P4mm$ [tetragonal]

* plus set: $+ [0, 0, 0]$

* Wyckoff site: **1a**, site symmetry: $4mm$

Table 1: Wyckoff bond: **1a@1a**

| No. | vector | center | mapping |
|-----|-------------|-------------|----------------------------|
| 1 | $[0, 0, Z]$ | $[0, 0, z]$ | $[1, 2, 3, 4, 5, 6, 7, 8]$ |

Table 2: Wyckoff bond: **2b@1a**

| No. | vector | center | mapping |
|-----|-------------|-------------|------------------|
| 1 | $[X, 0, 0]$ | $[0, 0, z]$ | $[1, -2, 5, -6]$ |
| 2 | $[0, X, 0]$ | $[0, 0, z]$ | $[3, -4, -7, 8]$ |

Table 3: Wyckoff bond: **2c@1a**

| No. | vector | center | mapping |
|-----|--------------|-------------|------------------|
| 1 | $[X, X, 0]$ | $[0, 0, z]$ | $[1, -2, -7, 8]$ |
| 2 | $[-X, X, 0]$ | $[0, 0, z]$ | $[3, -4, -5, 6]$ |

Table 4: Wyckoff bond: **4d@1a**

| No. | vector | center | mapping |
|-----|--------------|-------------|----------|
| 1 | $[X, 0, Z]$ | $[0, 0, z]$ | $[1, 5]$ |
| 2 | $[-X, 0, Z]$ | $[0, 0, z]$ | $[2, 6]$ |
| 3 | $[0, X, Z]$ | $[0, 0, z]$ | $[3, 8]$ |
| 4 | $[0, -X, Z]$ | $[0, 0, z]$ | $[4, 7]$ |

Table 5: Wyckoff bond: **4e@1a**

| No. | vector | center | mapping |
|-----|---------------|-------------|----------|
| 1 | $[X, X, Z]$ | $[0, 0, z]$ | $[1, 8]$ |
| 2 | $[-X, -X, Z]$ | $[0, 0, z]$ | $[2, 7]$ |
| 3 | $[-X, X, Z]$ | $[0, 0, z]$ | $[3, 6]$ |
| 4 | $[X, -X, Z]$ | $[0, 0, z]$ | $[4, 5]$ |

Table 6: Wyckoff bond: **4f@1a**

| No. | vector | center | mapping |
|-----|---------------|-------------|-----------|
| 1 | $[X, Y, 0]$ | $[0, 0, z]$ | $[1, -2]$ |
| 2 | $[-Y, X, 0]$ | $[0, 0, z]$ | $[3, -4]$ |
| 3 | $[X, -Y, 0]$ | $[0, 0, z]$ | $[5, -6]$ |
| 4 | $[-Y, -X, 0]$ | $[0, 0, z]$ | $[7, -8]$ |

Table 7: Wyckoff bond: **8g@1a**

| No. | vector | center | mapping |
|-----|---------------|-------------|---------|
| 1 | $[X, Y, Z]$ | $[0, 0, z]$ | $[1]$ |
| 2 | $[-X, -Y, Z]$ | $[0, 0, z]$ | $[2]$ |
| 3 | $[-Y, X, Z]$ | $[0, 0, z]$ | $[3]$ |
| 4 | $[Y, -X, Z]$ | $[0, 0, z]$ | $[4]$ |
| 5 | $[X, -Y, Z]$ | $[0, 0, z]$ | $[5]$ |
| 6 | $[-X, Y, Z]$ | $[0, 0, z]$ | $[6]$ |
| 7 | $[-Y, -X, Z]$ | $[0, 0, z]$ | $[7]$ |
| 8 | $[Y, X, Z]$ | $[0, 0, z]$ | $[8]$ |

* Wyckoff site: **1b**, site symmetry: **4mm**

Table 8: Wyckoff bond: **1a@1b**

| No. | vector | center | mapping |
|-----|-------------|---------------------------------|----------------------------|
| 1 | $[0, 0, Z]$ | $[\frac{1}{2}, \frac{1}{2}, z]$ | $[1, 2, 3, 4, 5, 6, 7, 8]$ |

Table 9: Wyckoff bond: **2b@1b**

| No. | vector | center | mapping |
|-----|-------------|---------------------------------|------------------|
| 1 | $[X, 0, 0]$ | $[\frac{1}{2}, \frac{1}{2}, z]$ | $[1, -2, 5, -6]$ |
| 2 | $[0, X, 0]$ | $[\frac{1}{2}, \frac{1}{2}, z]$ | $[3, -4, -7, 8]$ |

Table 10: Wyckoff bond: **2c@1b**

| No. | vector | center | mapping |
|-----|--------------|---------------------------------|------------------|
| 1 | $[X, X, 0]$ | $[\frac{1}{2}, \frac{1}{2}, z]$ | $[1, -2, -7, 8]$ |
| 2 | $[-X, X, 0]$ | $[\frac{1}{2}, \frac{1}{2}, z]$ | $[3, -4, -5, 6]$ |

Table 11: Wyckoff bond: **4d@1b**

| No. | vector | center | mapping |
|-----|--------------|---------------------------------|----------|
| 1 | $[X, 0, Z]$ | $[\frac{1}{2}, \frac{1}{2}, z]$ | $[1, 5]$ |
| 2 | $[-X, 0, Z]$ | $[\frac{1}{2}, \frac{1}{2}, z]$ | $[2, 6]$ |
| 3 | $[0, X, Z]$ | $[\frac{1}{2}, \frac{1}{2}, z]$ | $[3, 8]$ |
| 4 | $[0, -X, Z]$ | $[\frac{1}{2}, \frac{1}{2}, z]$ | $[4, 7]$ |

Table 12: Wyckoff bond: **4e@1b**

| No. | vector | center | mapping |
|-----|---------------|---------------------------------|----------|
| 1 | $[X, X, Z]$ | $[\frac{1}{2}, \frac{1}{2}, z]$ | $[1, 8]$ |
| 2 | $[-X, -X, Z]$ | $[\frac{1}{2}, \frac{1}{2}, z]$ | $[2, 7]$ |
| 3 | $[-X, X, Z]$ | $[\frac{1}{2}, \frac{1}{2}, z]$ | $[3, 6]$ |
| 4 | $[X, -X, Z]$ | $[\frac{1}{2}, \frac{1}{2}, z]$ | $[4, 5]$ |

Table 13: Wyckoff bond: **4f@1b**

| No. | vector | center | mapping |
|-----|---------------|---------------------------------|-----------|
| 1 | $[X, Y, 0]$ | $[\frac{1}{2}, \frac{1}{2}, z]$ | $[1, -2]$ |
| 2 | $[-Y, X, 0]$ | $[\frac{1}{2}, \frac{1}{2}, z]$ | $[3, -4]$ |
| 3 | $[X, -Y, 0]$ | $[\frac{1}{2}, \frac{1}{2}, z]$ | $[5, -6]$ |
| 4 | $[-Y, -X, 0]$ | $[\frac{1}{2}, \frac{1}{2}, z]$ | $[7, -8]$ |

Table 14: Wyckoff bond: **8g@1b**

| No. | vector | center | mapping |
|-----|---------------|---------------------------------|---------|
| 1 | $[X, Y, Z]$ | $[\frac{1}{2}, \frac{1}{2}, z]$ | $[1]$ |
| 2 | $[-X, -Y, Z]$ | $[\frac{1}{2}, \frac{1}{2}, z]$ | $[2]$ |
| 3 | $[-Y, X, Z]$ | $[\frac{1}{2}, \frac{1}{2}, z]$ | $[3]$ |
| 4 | $[Y, -X, Z]$ | $[\frac{1}{2}, \frac{1}{2}, z]$ | $[4]$ |
| 5 | $[X, -Y, Z]$ | $[\frac{1}{2}, \frac{1}{2}, z]$ | $[5]$ |
| 6 | $[-X, Y, Z]$ | $[\frac{1}{2}, \frac{1}{2}, z]$ | $[6]$ |
| 7 | $[-Y, -X, Z]$ | $[\frac{1}{2}, \frac{1}{2}, z]$ | $[7]$ |
| 8 | $[Y, X, Z]$ | $[\frac{1}{2}, \frac{1}{2}, z]$ | $[8]$ |

* Wyckoff site: **2c**, site symmetry: **2mm**.

Table 15: Wyckoff bond: 2a@2c

| No. | vector | center | mapping |
|-----|-------------|-----------------------|------------------|
| 1 | $[X, 0, 0]$ | $[\frac{1}{2}, 0, z]$ | $[1, -2, 5, -6]$ |
| 2 | $[0, X, 0]$ | $[0, \frac{1}{2}, z]$ | $[3, -4, -7, 8]$ |

Table 16: Wyckoff bond: 2b@2c

| No. | vector | center | mapping |
|-----|--------------|-----------------------|------------------|
| 1 | $[0, X, 0]$ | $[\frac{1}{2}, 0, z]$ | $[1, -2, -5, 6]$ |
| 2 | $[-X, 0, 0]$ | $[0, \frac{1}{2}, z]$ | $[3, -4, 7, -8]$ |

Table 17: Wyckoff bond: 2c@2c

| No. | vector | center | mapping |
|-----|-------------|-----------------------|----------------|
| 1 | $[0, 0, Z]$ | $[\frac{1}{2}, 0, z]$ | $[1, 2, 5, 6]$ |
| 2 | $[0, 0, Z]$ | $[0, \frac{1}{2}, z]$ | $[3, 4, 7, 8]$ |

Table 18: Wyckoff bond: 4d@2c

| No. | vector | center | mapping |
|-----|--------------|-----------------------|----------|
| 1 | $[X, 0, Z]$ | $[\frac{1}{2}, 0, z]$ | $[1, 5]$ |
| 2 | $[-X, 0, Z]$ | $[\frac{1}{2}, 0, z]$ | $[2, 6]$ |
| 3 | $[0, X, Z]$ | $[0, \frac{1}{2}, z]$ | $[3, 8]$ |
| 4 | $[0, -X, Z]$ | $[0, \frac{1}{2}, z]$ | $[4, 7]$ |

Table 19: Wyckoff bond: 4e@2c

| No. | vector | center | mapping |
|-----|--------------|-----------------------|----------|
| 1 | $[0, X, Z]$ | $[\frac{1}{2}, 0, z]$ | $[1, 6]$ |
| 2 | $[0, -X, Z]$ | $[\frac{1}{2}, 0, z]$ | $[2, 5]$ |
| 3 | $[-X, 0, Z]$ | $[0, \frac{1}{2}, z]$ | $[3, 7]$ |
| 4 | $[X, 0, Z]$ | $[0, \frac{1}{2}, z]$ | $[4, 8]$ |

Table 20: Wyckoff bond: **4f@2c**

| No. | vector | center | mapping |
|-----|---------------|-----------------------|-----------|
| 1 | $[X, Y, 0]$ | $[\frac{1}{2}, 0, z]$ | $[1, -2]$ |
| 2 | $[-Y, X, 0]$ | $[0, \frac{1}{2}, z]$ | $[3, -4]$ |
| 3 | $[X, -Y, 0]$ | $[\frac{1}{2}, 0, z]$ | $[5, -6]$ |
| 4 | $[-Y, -X, 0]$ | $[0, \frac{1}{2}, z]$ | $[7, -8]$ |

Table 21: Wyckoff bond: **8g@2c**

| No. | vector | center | mapping |
|-----|---------------|-----------------------|---------|
| 1 | $[X, Y, Z]$ | $[\frac{1}{2}, 0, z]$ | $[1]$ |
| 2 | $[-X, -Y, Z]$ | $[\frac{1}{2}, 0, z]$ | $[2]$ |
| 3 | $[-Y, X, Z]$ | $[0, \frac{1}{2}, z]$ | $[3]$ |
| 4 | $[Y, -X, Z]$ | $[0, \frac{1}{2}, z]$ | $[4]$ |
| 5 | $[X, -Y, Z]$ | $[\frac{1}{2}, 0, z]$ | $[5]$ |
| 6 | $[-X, Y, Z]$ | $[\frac{1}{2}, 0, z]$ | $[6]$ |
| 7 | $[-Y, -X, Z]$ | $[0, \frac{1}{2}, z]$ | $[7]$ |
| 8 | $[Y, X, Z]$ | $[0, \frac{1}{2}, z]$ | $[8]$ |

* Wyckoff site: **4d**, site symmetry: $\bar{3}m$

Table 22: Wyckoff bond: **4a@4d**

| No. | vector | center | mapping |
|-----|---------------|---------------|----------|
| 1 | $[X, X, Z]$ | $[x, x, z]$ | $[1, 8]$ |
| 2 | $[-X, -X, Z]$ | $[-x, -x, z]$ | $[2, 7]$ |
| 3 | $[-X, X, Z]$ | $[-x, x, z]$ | $[3, 6]$ |
| 4 | $[X, -X, Z]$ | $[x, -x, z]$ | $[4, 5]$ |

Table 23: Wyckoff bond: **4b@4d**

| No. | vector | center | mapping |
|-----|---------------|---------------|-----------|
| 1 | $[X, -X, 0]$ | $[x, x, z]$ | $[1, -8]$ |
| 2 | $[-X, X, 0]$ | $[-x, -x, z]$ | $[2, -7]$ |
| 3 | $[X, X, 0]$ | $[-x, x, z]$ | $[3, -6]$ |
| 4 | $[-X, -X, 0]$ | $[x, -x, z]$ | $[4, -5]$ |

Table 24: Wyckoff bond: **8c@4d**

| No. | vector | center | mapping |
|-----|---------------|---------------|---------|
| 1 | $[X, Y, Z]$ | $[x, x, z]$ | [1] |
| 2 | $[-X, -Y, Z]$ | $[-x, -x, z]$ | [2] |
| 3 | $[-Y, X, Z]$ | $[-x, x, z]$ | [3] |
| 4 | $[Y, -X, Z]$ | $[x, -x, z]$ | [4] |
| 5 | $[X, -Y, Z]$ | $[x, -x, z]$ | [5] |
| 6 | $[-X, Y, Z]$ | $[-x, x, z]$ | [6] |
| 7 | $[-Y, -X, Z]$ | $[-x, -x, z]$ | [7] |
| 8 | $[Y, X, Z]$ | $[x, x, z]$ | [8] |

* Wyckoff site: **4e**, site symmetry: **.m**.

Table 25: Wyckoff bond: **4a@4e**

| No. | vector | center | mapping |
|-----|--------------|--------------|---------|
| 1 | $[X, 0, Z]$ | $[x, 0, z]$ | [1,5] |
| 2 | $[-X, 0, Z]$ | $[-x, 0, z]$ | [2,6] |
| 3 | $[0, X, Z]$ | $[0, x, z]$ | [3,8] |
| 4 | $[0, -X, Z]$ | $[0, -x, z]$ | [4,7] |

Table 26: Wyckoff bond: **4b@4e**

| No. | vector | center | mapping |
|-----|--------------|--------------|---------|
| 1 | $[0, X, 0]$ | $[x, 0, z]$ | [1,-5] |
| 2 | $[0, -X, 0]$ | $[-x, 0, z]$ | [2,-6] |
| 3 | $[-X, 0, 0]$ | $[0, x, z]$ | [3,-8] |
| 4 | $[X, 0, 0]$ | $[0, -x, z]$ | [4,-7] |

Table 27: Wyckoff bond: **8c@4e**

| No. | vector | center | mapping |
|-----|---------------|--------------|---------|
| 1 | $[X, Y, Z]$ | $[x, 0, z]$ | [1] |
| 2 | $[-X, -Y, Z]$ | $[-x, 0, z]$ | [2] |
| 3 | $[-Y, X, Z]$ | $[0, x, z]$ | [3] |
| 4 | $[Y, -X, Z]$ | $[0, -x, z]$ | [4] |
| 5 | $[X, -Y, Z]$ | $[x, 0, z]$ | [5] |
| 6 | $[-X, Y, Z]$ | $[-x, 0, z]$ | [6] |
| 7 | $[-Y, -X, Z]$ | $[0, -x, z]$ | [7] |
| 8 | $[Y, X, Z]$ | $[0, x, z]$ | [8] |

* Wyckoff site: **4f**, site symmetry: **.m**.

Table 28: Wyckoff bond: **4a@4f**

| No. | vector | center | mapping |
|-----|--------------|------------------------|----------|
| 1 | $[X, 0, Z]$ | $[x, \frac{1}{2}, z]$ | $[1, 5]$ |
| 2 | $[-X, 0, Z]$ | $[-x, \frac{1}{2}, z]$ | $[2, 6]$ |
| 3 | $[0, X, Z]$ | $[\frac{1}{2}, x, z]$ | $[3, 8]$ |
| 4 | $[0, -X, Z]$ | $[\frac{1}{2}, -x, z]$ | $[4, 7]$ |

Table 29: Wyckoff bond: **4b@4f**

| No. | vector | center | mapping |
|-----|--------------|------------------------|-----------|
| 1 | $[0, X, 0]$ | $[x, \frac{1}{2}, z]$ | $[1, -5]$ |
| 2 | $[0, -X, 0]$ | $[-x, \frac{1}{2}, z]$ | $[2, -6]$ |
| 3 | $[-X, 0, 0]$ | $[\frac{1}{2}, x, z]$ | $[3, -8]$ |
| 4 | $[X, 0, 0]$ | $[\frac{1}{2}, -x, z]$ | $[4, -7]$ |

Table 30: Wyckoff bond: **8c@4f**

| No. | vector | center | mapping |
|-----|---------------|------------------------|---------|
| 1 | $[X, Y, Z]$ | $[x, \frac{1}{2}, z]$ | $[1]$ |
| 2 | $[-X, -Y, Z]$ | $[-x, \frac{1}{2}, z]$ | $[2]$ |
| 3 | $[-Y, X, Z]$ | $[\frac{1}{2}, x, z]$ | $[3]$ |
| 4 | $[Y, -X, Z]$ | $[\frac{1}{2}, -x, z]$ | $[4]$ |
| 5 | $[X, -Y, Z]$ | $[x, \frac{1}{2}, z]$ | $[5]$ |
| 6 | $[-X, Y, Z]$ | $[-x, \frac{1}{2}, z]$ | $[6]$ |
| 7 | $[-Y, -X, Z]$ | $[\frac{1}{2}, -x, z]$ | $[7]$ |
| 8 | $[Y, X, Z]$ | $[\frac{1}{2}, x, z]$ | $[8]$ |

* Wyckoff site: **8g**, site symmetry: **1**

Table 31: Wyckoff bond: **8a@8g**

| No. | vector | center | mapping |
|-----|---------------|---------------|---------|
| 1 | $[X, Y, Z]$ | $[x, y, z]$ | $[1]$ |
| 2 | $[-X, -Y, Z]$ | $[-x, -y, z]$ | $[2]$ |
| 3 | $[-Y, X, Z]$ | $[-y, x, z]$ | $[3]$ |
| 4 | $[Y, -X, Z]$ | $[y, -x, z]$ | $[4]$ |
| 5 | $[X, -Y, Z]$ | $[x, -y, z]$ | $[5]$ |
| 6 | $[-X, Y, Z]$ | $[-x, y, z]$ | $[6]$ |
| 7 | $[-Y, -X, Z]$ | $[-y, -x, z]$ | $[7]$ |

| | | | |
|---|-------------|-------------|-----|
| 8 | $[Y, X, Z]$ | $[y, x, z]$ | [8] |
|---|-------------|-------------|-----|