

MPG No. 22.3.81 $\bar{6}'$ [Type III, hexagonal] [Q tensor]

* Rank 0 tensor.

$$[Q]$$

$$Q = Q_s^{(1)}$$

* Rank 1 tensor. * Rank 2 tensor (s).

$$\begin{bmatrix} Q_{xx} & 0 & 0 \\ 0 & Q_{xx} & 0 \\ 0 & 0 & Q_{zz} \end{bmatrix}$$

$$Q_{xx} = -Q_{du}^{(1)} + Q_s^{(1)}$$

$$Q_{zz} = 2Q_{du}^{(1)} + Q_s^{(1)}$$

* Rank 2 tensor (a).

$$\begin{bmatrix} 0 & Q_{xy} & 0 \\ -Q_{xy} & 0 & 0 \\ 0 & 0 & 0 \end{bmatrix}$$

$$Q_{xy} = G_{pz}^{(1)}$$

* Rank 3 tensor (s).

$$\begin{bmatrix} Q_{xxx} & Q_{xxy} & 0 \\ -Q_{xxx} & -Q_{xxy} & 0 \\ 0 & 0 & 0 \\ 0 & 0 & 0 \\ Q_{xxy} & -Q_{xxx} & 0 \end{bmatrix}$$

$$Q_{xxx} = Q_{f2}^{(1)}$$

$$Q_{xxy} = Q_{f1}^{(1)}$$

* Rank 3 tensor (a). * Rank 4 tensor (sss).

$$\begin{bmatrix} Q_{xxxx} & Q_{xxyy} & Q_{xxzz} & 0 & 0 & 0 \\ Q_{xxyy} & Q_{xxxx} & Q_{xxzz} & 0 & 0 & 0 \\ Q_{xxzz} & Q_{xxzz} & Q_{zzzz} & 0 & 0 & 0 \\ 0 & 0 & 0 & Q_{yzyz} & 0 & 0 \\ 0 & 0 & 0 & 0 & Q_{yzyz} & 0 \\ 0 & 0 & 0 & 0 & 0 & \frac{Q_{xxxx}}{2} - \frac{Q_{xxyy}}{2} \end{bmatrix}$$

$$Q_{xxxx} = -2Q_{du}^{(1)} - 4Q_{du}^{(2)} + 3Q_{g0}^{(1)} + Q_s^{(1)} + 2Q_s^{(2)}$$

$$Q_{xxyy} = -2Q_{du}^{(1)} + Q_{g0}^{(1)} + Q_s^{(1)}$$

$$Q_{xxzz} = Q_{du}^{(1)} - 4Q_{g0}^{(1)} + Q_s^{(1)}$$

$$Q_{zzzz} = 4Q_{du}^{(1)} + 8Q_{du}^{(2)} + 8Q_{g0}^{(1)} + Q_s^{(1)} + 2Q_s^{(2)}$$

$$Q_{yzyz} = Q_{du}^{(2)} - 4Q_{g0}^{(1)} + Q_s^{(2)}$$

* Rank 4 tensor (ssa).

$$\begin{bmatrix} 0 & 0 & Q_{xxzz} & 0 & 0 & Q_{xxyy} \\ 0 & 0 & Q_{xxzz} & 0 & 0 & -Q_{xxyy} \\ -Q_{xxzz} & -Q_{xxzz} & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & Q_{yzzx} & 0 \\ 0 & 0 & 0 & -Q_{yzzx} & 0 & 0 \\ -Q_{xxyy} & Q_{xxyy} & 0 & 0 & 0 & 0 \end{bmatrix}$$

$$\begin{aligned} Q_{xxzz} &= 3Q_{du}^{(3)} \\ Q_{xxyy} &= -2G_{faz}^{(1)} + 2G_{pz}^{(1)} \\ Q_{yzzx} &= -4G_{faz}^{(1)} - G_{pz}^{(1)} \end{aligned}$$

* Rank 4 tensor (aas).

$$\begin{bmatrix} Q_{yzyz} & 0 & 0 \\ 0 & Q_{yzyz} & 0 \\ 0 & 0 & Q_{xyxy} \end{bmatrix}$$

$$\begin{aligned} Q_{yzyz} &= -2Q_{du}^{(4)} + Q_s^{(3)} \\ Q_{xyxy} &= 4Q_{du}^{(4)} + Q_s^{(3)} \end{aligned}$$

* Rank 4 tensor (aaa).

$$\begin{bmatrix} 0 & Q_{yzzx} & 0 \\ -Q_{yzzx} & 0 & 0 \\ 0 & 0 & 0 \end{bmatrix}$$

$$Q_{yzzx} = -G_{pz}^{(2)}$$

* Rank 4 tensor (sa).

$$\begin{bmatrix} 0 & 0 & Q_{xxxy} \\ 0 & 0 & Q_{xxxy} \\ 0 & 0 & Q_{zzxy} \\ Q_{yzyz} & Q_{yzzx} & 0 \\ Q_{yzzx} & -Q_{yzyz} & 0 \\ 0 & 0 & 0 \end{bmatrix}$$

$$\begin{aligned} Q_{xxxy} &= -G_{faz}^{(2)} + G_{pz}^{(3)} \\ Q_{zzxy} &= 2G_{faz}^{(2)} + G_{pz}^{(3)} + 2G_{pz}^{(4)} \\ Q_{yzyz} &= -3Q_{du}^{(5)} \\ Q_{yzzx} &= -G_{faz}^{(2)} + G_{pz}^{(4)} \end{aligned}$$

* Rank 4 tensor (as).

$$\begin{bmatrix} 0 & 0 & 0 & Q_{yzyz} & Q_{yzzx} & 0 \\ 0 & 0 & 0 & Q_{yzzx} & -Q_{yzyz} & 0 \\ Q_{xyxx} & Q_{xyxx} & Q_{xyzz} & 0 & 0 & 0 \end{bmatrix}$$

$$\begin{aligned} Q_{yzyz} &= -3Q_{du}^{(6)} \\ Q_{yzzx} &= -G_{faz}^{(3)} + G_{pz}^{(6)} \\ Q_{xyxx} &= -G_{faz}^{(3)} + G_{pz}^{(5)} \\ Q_{xyzz} &= 2G_{faz}^{(3)} + G_{pz}^{(5)} + 2G_{pz}^{(6)} \end{aligned}$$

* Rank 4 tensor (s).

$$\begin{bmatrix} Q_{xxxx} & Q_{xxyy} & Q_{xxzz} & 0 & 0 & Q_{xxxy} & 0 & 0 & Q_{xxyx} \\ Q_{xxyy} & Q_{xxxx} & Q_{xxzz} & 0 & 0 & -Q_{xxxy} & 0 & 0 & -Q_{xxyx} \\ Q_{zzxx} & Q_{zzxx} & Q_{zzzz} & 0 & 0 & Q_{zzxy} & 0 & 0 & -Q_{zzxy} \\ 0 & 0 & 0 & Q_{yzyz} & Q_{yzzx} & 0 & Q_{yzyy} & Q_{yzzz} & 0 \\ 0 & 0 & 0 & -Q_{yzzx} & Q_{yzzz} & 0 & -Q_{yzzx} & Q_{yzyz} & 0 \\ -\frac{Q_{xxxx}}{2} - \frac{Q_{xxyx}}{2} & \frac{Q_{xxyx}}{2} + \frac{Q_{xxxx}}{2} & 0 & 0 & 0 & \frac{Q_{xxxx}}{2} - \frac{Q_{xxyx}}{2} & 0 & 0 & \frac{Q_{xxxx}}{2} - \frac{Q_{xxyx}}{2} \end{bmatrix}$$

$$\begin{aligned}
Q_{xxxx} &= -2Q_{du}^{(1)} - 4Q_{du}^{(2)} + 3Q_{g0}^{(1)} + Q_s^{(1)} + 2Q_s^{(2)} \\
Q_{xxyy} &= -2Q_{du}^{(1)} + Q_{g0}^{(1)} + Q_s^{(1)} \\
Q_{xxzz} &= Q_{du}^{(1)} + 3Q_{du}^{(3)} - 4Q_{g0}^{(1)} + Q_s^{(1)} \\
Q_{xxxz} &= -2G_{faz}^{(1)} - G_{faz}^{(2)} + 2G_{pz}^{(1)} + G_{pz}^{(3)} \\
Q_{xxyx} &= -2G_{faz}^{(1)} + G_{faz}^{(2)} + 2G_{pz}^{(1)} - G_{pz}^{(3)} \\
Q_{zzxx} &= Q_{du}^{(1)} - 3Q_{du}^{(3)} - 4Q_{g0}^{(1)} + Q_s^{(1)} \\
Q_{zzzz} &= 4Q_{du}^{(1)} + 8Q_{du}^{(2)} + 8Q_{g0}^{(1)} + Q_s^{(1)} + 2Q_s^{(2)} \\
Q_{zzxy} &= 2G_{faz}^{(2)} + G_{pz}^{(3)} + 2G_{pz}^{(4)} \\
Q_{yzyz} &= Q_{du}^{(2)} - 3Q_{du}^{(5)} - 4Q_{g0}^{(1)} + Q_s^{(2)} \\
Q_{yzzx} &= -4G_{faz}^{(1)} - G_{faz}^{(2)} - G_{pz}^{(1)} + G_{pz}^{(4)} \\
Q_{yzzy} &= Q_{du}^{(2)} + 3Q_{du}^{(5)} - 4Q_{g0}^{(1)} + Q_s^{(2)} \\
Q_{yzxz} &= -4G_{faz}^{(1)} + G_{faz}^{(2)} - G_{pz}^{(1)} - G_{pz}^{(4)}
\end{aligned}$$

* Rank 4 tensor (a).

$$\begin{bmatrix} 0 & 0 & 0 & Q_{yzyz} & Q_{yzzx} & 0 & Q_{yzyy} & Q_{yzxz} & 0 \\ 0 & 0 & 0 & Q_{yzzx} & -Q_{yzyy} & 0 & Q_{yzzx} & -Q_{yzyz} & 0 \\ Q_{xyxx} & Q_{xyxx} & Q_{xyzz} & 0 & 0 & Q_{xyxy} & 0 & 0 & -Q_{xyxy} \end{bmatrix}$$

$$\begin{aligned}
Q_{yzyz} &= -2Q_{du}^{(4)} - 3Q_{du}^{(6)} + Q_s^{(3)} \\
Q_{yzzx} &= -G_{faz}^{(3)} - G_{pz}^{(2)} + G_{pz}^{(6)} \\
Q_{yzyy} &= 2Q_{du}^{(4)} - 3Q_{du}^{(6)} - Q_s^{(3)} \\
Q_{yzxz} &= -G_{faz}^{(3)} + G_{pz}^{(2)} + G_{pz}^{(6)} \\
Q_{xyxx} &= -G_{faz}^{(3)} + G_{pz}^{(5)} \\
Q_{xyzz} &= 2G_{faz}^{(3)} + G_{pz}^{(5)} + 2G_{pz}^{(6)} \\
Q_{xyxy} &= 4Q_{du}^{(4)} + Q_s^{(3)}
\end{aligned}$$

* Rank 4 tensor (t).

$$\begin{bmatrix} Q_{xxxx} & 0 & 0 & & & & & & \\ 0 & Q_{xxxx} & 0 & & & & & & \\ 0 & 0 & Q_{zzzz} & & & & & & \\ 0 & 0 & Q_{yyzz} & & & & & & \\ Q_{zzxx} & 0 & 0 & & & & & & \\ 0 & Q_{xyyy} & 0 & & & & & & \\ 0 & Q_{yzyy} & 0 & & & & & & \\ 0 & 0 & -\frac{Q_{xxxx}}{2} + \frac{3Q_{xyyy}}{2} + Q_{yyzz} - Q_{yzyy} + Q_{zzxx} & & & & & & \\ \frac{Q_{xxxx}}{2} - \frac{Q_{xyyy}}{2} & 0 & 0 & & & & & & \\ 0 & 0 & 0 & & & & & & \end{bmatrix}$$

$$\begin{aligned}
Q_{xxxx} &= -2Q_{du}^{(1)} - 4Q_{du}^{(2)} + 3Q_{g0}^{(1)} + 3Q_s^{(1)} \\
Q_{zzzz} &= 4Q_{du}^{(1)} + 8Q_{du}^{(2)} + 8Q_{g0}^{(1)} + 3Q_s^{(1)} \\
Q_{yyzz} &= Q_{du}^{(1)} + 3Q_{du}^{(3)} - 4Q_{g0}^{(1)} + Q_s^{(1)} \\
Q_{zzxx} &= Q_{du}^{(1)} - 3Q_{du}^{(3)} - 4Q_{g0}^{(1)} + Q_s^{(1)} \\
Q_{xyyy} &= -2Q_{du}^{(1)} + Q_{g0}^{(1)} + Q_s^{(1)} \\
Q_{yzyy} &= Q_{du}^{(2)} + 3Q_{du}^{(5)} - 4Q_{g0}^{(1)} + Q_s^{(1)}
\end{aligned}$$