No. 7 C_{2v} mm2 [orthorhombic] (polar)

表 1 rank 0

No.	irrep.	(tag)	mul.	comp.	harmonics	(tag)	definition
1	A_1	A1	_	_	$\mathbb{Q}_0^{(h,A_1)}$	$\mathtt{Qh}(\mathtt{0},\mathtt{A1},,)$	C_0

表 2 rank 1

No.	irrep.	(tag)	mul.	comp.	harmonics	(tag)	definition
2	A_1	A1	-	-	$\mathbb{Q}_1^{(h,A_1)}$	$\mathtt{Qh}(\mathtt{1},\mathtt{A1},,)$	C_0
3	B_1	B1	_	-	$\mathbb{Q}_1^{(h,B_1)}$	$\mathtt{Qh}(\mathtt{1},\mathtt{B1},,)$	C_1
4	B_2	B2			$\mathbb{Q}_1^{(h,B_2)}$	$\mathtt{Qh}(\mathtt{1},\mathtt{B2},,)$	S_1

表 3 rank 2

No.	irrep.	(tag)	mul.	comp.	harmonics	(tag)	definition
5	A_1	A1	1	-	$\mathbb{Q}_2^{(h,A_1,1)}$	$\mathtt{Qh}(\mathtt{2},\mathtt{A1},\mathtt{1},)$	C_0
6	A_1	A1	2	_	$\mathbb{Q}_2^{(h,A_1,2)}$	$\mathtt{Qh}(\mathtt{2},\mathtt{A1},\mathtt{2},)$	C_2
7	A_2	A2	_	_	$\mathbb{Q}_2^{(h,A_2)}$	$\mathtt{Qh}(\mathtt{2},\mathtt{A2},,)$	S_2
8	B_1	B1	_	_	$\mathbb{Q}_2^{(h,B_1)}$	$\mathtt{Qh}(\mathtt{2},\mathtt{B1},,)$	C_1
9	B_2	B2	-	-	$\mathbb{Q}_2^{(h,B_2)}$	$\mathtt{Qh}(\mathtt{2},\mathtt{B2},,)$	S_1

表 4 rank 3

No.	irrep.	(tag)	mul.	comp.	harmonics	(tag)	definition
10	A_1	A1	1	_	$\mathbb{Q}_3^{(h,A_1,1)}$	$\mathtt{Qh}(\mathtt{3},\mathtt{A1},\mathtt{1},)$	C_0
11	A_1	A1	2	-	$\mathbb{Q}_3^{(h,A_1,2)}$	$\mathtt{Qh}(\mathtt{3},\mathtt{A1},\mathtt{2},)$	C_2
12	A_2	A2	_	_	$\mathbb{Q}_3^{(h,A_2)}$	$\mathtt{Qh}(\mathtt{3},\mathtt{A2},,)$	S_2
13	B_1	B1	1	_	$\mathbb{Q}_3^{(h,B_1,1)}$	$\mathtt{Qh}(\mathtt{3},\mathtt{B1},\mathtt{1},)$	$-\frac{\sqrt{6}C_1}{4} + \frac{\sqrt{10}C_3}{4}$
14	B_1	B1	2	_	$\mathbb{Q}_3^{(h,B_1,2)}$	$\mathtt{Qh}(\mathtt{3},\mathtt{B1},\mathtt{2},)$	$-\frac{\sqrt{10}C_1}{4} - \frac{\sqrt{6}C_3}{4}$
15	B_2	B2	1	_	$\mathbb{Q}_3^{(h,B_2,1)}$	$\mathtt{Qh}(3,\mathtt{B2},1,)$	$-\frac{\sqrt{6}S_1}{4} - \frac{\sqrt{10}S_3}{4}$
16	B_2	B2	2	_	$\mathbb{Q}_3^{(h,B_2,2)}$	$\mathtt{Qh}(\mathtt{3},\mathtt{B2},\mathtt{2},)$	$\frac{\sqrt{10}S_1}{4} - \frac{\sqrt{6}S_3}{4}$

表 5 rank 4

No.	irrep.	(tag)	mul.	comp.	harmonics	(tag)	definition
17	A_1	A1	1	_	$\mathbb{Q}_4^{(h,A_1,1)}$	$\mathtt{Qh}(\mathtt{4},\mathtt{A1},\mathtt{1},)$	$\frac{\sqrt{21}C_0}{6} + \frac{\sqrt{15}C_4}{6}$
18	A_1	A1	2	-	$\mathbb{Q}_4^{(h,A_1,2)}$	$\mathtt{Qh}(\mathtt{4},\mathtt{A1},\mathtt{2},)$	$\frac{\sqrt{15}C_0}{6} - \frac{\sqrt{21}C_4}{6}$
19	A_1	A1	3	_	$\mathbb{Q}_4^{(h,A_1,3)}$	$\mathtt{Qh}(\mathtt{4},\mathtt{A1},\mathtt{3},)$	$-C_2$
20	A_2	A2	1	_	$\mathbb{Q}_4^{(h,A_2,1)}$	$\mathtt{Qh}(\mathtt{4},\mathtt{A2},\mathtt{1},)$	S_4
21	A_2	A2	2	_	$\mathbb{Q}_4^{(h,A_2,2)}$	$\mathtt{Qh}(\mathtt{4},\mathtt{A2},\mathtt{2},)$	S_2
22	B_1	B1	1	_	$\mathbb{Q}_4^{(h,B_1,1)}$	$\mathtt{Qh}(\mathtt{4},\mathtt{B1},\mathtt{1},)$	$\frac{\sqrt{14}C_1}{4} - \frac{\sqrt{2}C_3}{4}$
23	B_1	B1	2	_	$\mathbb{Q}_4^{(h,B_1,2)}$	$\mathtt{Qh}(\mathtt{4},\mathtt{B1},\mathtt{2},)$	$-\frac{\sqrt{2}C_1}{4} - \frac{\sqrt{14}C_3}{4}$
24	B_2	B2	1	-	$\mathbb{Q}_4^{(h,B_2,1)}$	$\mathtt{Qh}(\mathtt{4},\mathtt{B2},\mathtt{1},)$	$-\frac{\sqrt{14}S_1}{4} - \frac{\sqrt{2}S_3}{4}$
25	B_2	B2	2	_	$\mathbb{Q}_4^{(h,B_2,2)}$	$\mathtt{Qh}(\mathtt{4},\mathtt{B2},\mathtt{2},)$	$-\frac{\sqrt{2}S_1}{4} + \frac{\sqrt{14}S_3}{4}$

表 6 rank 5

No.	irrep.	(tag)	mul.	comp.	harmonics	(tag)	definition
26	A_1	A1	1	-	$\mathbb{Q}_{5}^{(h,A_{1},1)}$	$\mathtt{Qh}(\mathtt{5},\mathtt{A1},\mathtt{1},)$	C_0
27	A_1	A1	2	_	$\mathbb{Q}_{5}^{(h,A_{1},2)}$	$\mathtt{Qh}(\mathtt{5},\mathtt{A1},\mathtt{2},)$	C_4
28	A_1	A1	3	_	$\mathbb{Q}_5^{(h,A_1,3)}$	$\mathtt{Qh}(\mathtt{5},\mathtt{A1},\mathtt{3},)$	C_2
29	A_2	A2	1	_	$\mathbb{Q}_5^{(h,A_2,1)}$	$\mathtt{Qh}(\mathtt{5},\mathtt{A2},\mathtt{1},)$	S_4
30	A_2	A2	2	_	$\mathbb{Q}_{5}^{(h,A_{2},2)}$	$\mathtt{Qh}(\mathtt{5},\mathtt{A2},\mathtt{2},)$	$-S_2$
31	B_1	B1	1	_	$\mathbb{Q}_5^{(h,B_1,1)}$	$\mathtt{Qh}(\mathtt{5},\mathtt{B1},\mathtt{1},)$	$\frac{\sqrt{15}C_1}{8} - \frac{\sqrt{70}C_3}{16} + \frac{3\sqrt{14}C_5}{16}$
32	B_1	B1	2	_	$\mathbb{Q}_5^{(h,B_1,2)}$	$\mathtt{Qh}(\mathtt{5},\mathtt{B1},\mathtt{2},)$	$\frac{\sqrt{21}C_1}{8} + \frac{9\sqrt{2}C_3}{16} + \frac{\sqrt{10}C_5}{16}$
33	B_1	B1	3	_	$\mathbb{Q}_5^{(h,B_1,3)}$	$\mathtt{Qh}(\mathtt{5},\mathtt{B1},\mathtt{3},)$	$\frac{\sqrt{7}C_1}{4} - \frac{\sqrt{6}C_3}{8} - \frac{\sqrt{30}C_5}{8}$
34	B_2	B2	1	_	$\mathbb{Q}_5^{(h,B_2,1)}$	$\mathtt{Qh}(\mathtt{5},\mathtt{B2},\mathtt{1},)$	$\frac{\sqrt{15}S_1}{8} + \frac{\sqrt{70}S_3}{16} + \frac{3\sqrt{14}S_5}{16}$
35	B_2	B2	2	_	$\mathbb{Q}_5^{(h,B_2,2)}$	$\mathtt{Qh}(\mathtt{5},\mathtt{B2},\mathtt{2},)$	$\frac{\sqrt{21}S_1}{8} - \frac{9\sqrt{2}S_3}{16} + \frac{\sqrt{10}S_5}{16}$
36	B_2	B2	3	_	$\mathbb{Q}_5^{(h,B_2,3)}$	Qh(5, B2, 3,)	$-\frac{\sqrt{7}S_1}{4} - \frac{\sqrt{6}S_3}{8} + \frac{\sqrt{30}S_5}{8}$

表 7 rank 6

No.	irrep.	(tag)	mul.	comp.	harmonics	(tag)	definition
37	A_1	A1	1	_	$\mathbb{Q}_6^{(h,A_1,1)}$	$\mathtt{Qh}(6,\mathtt{A1},\mathtt{1},)$	$\frac{\sqrt{2}C_0}{4} - \frac{\sqrt{14}C_4}{4}$
38	A_1	A1	2	_	$\mathbb{Q}_6^{(h,A_1,2)}$	$\mathtt{Qh}(6,\mathtt{A1},\mathtt{2},)$	$\frac{\sqrt{11}C_2}{4} - \frac{\sqrt{5}C_6}{4}$
39	A_1	A1	3	_	$\mathbb{Q}_6^{(h,A_1,3)}$	$\mathtt{Qh}(6,\mathtt{A1},\mathtt{3},)$	$\frac{\sqrt{14}C_0}{4} + \frac{\sqrt{2}C_4}{4}$
40	A_1	A1	4	_	$\mathbb{Q}_6^{(h,A_1,4)}$	$\mathtt{Qh}(6,\mathtt{A1},4,)$	$\frac{\sqrt{5}C_2}{4} + \frac{\sqrt{11}C_6}{4}$
41	A_2	A2	1	_	$\mathbb{Q}_6^{(h,A_2,1)}$	$\mathtt{Qh}(6,\mathtt{A2},\mathtt{1},)$	S_4
42	A_2	A2	2	_	$\mathbb{Q}_6^{(h,A_2,2)}$	$\mathtt{Qh}(6,\mathtt{A2},\mathtt{2},)$	S_6
43	A_2	A2	3	_	$\mathbb{Q}_6^{(h,A_2,3)}$	$\mathtt{Qh}(6,\mathtt{A2},\mathtt{3},)$	S_2
44	B_1	B1	1	_	$\mathbb{Q}_6^{(h,B_1,1)}$	$\mathtt{Qh}(6,\mathtt{B1},\mathtt{1},)$	$-\frac{\sqrt{3}C_1}{4} - \frac{\sqrt{30}C_3}{8} + \frac{\sqrt{22}C_5}{8}$
45	B_1	B1	2	_	$\mathbb{Q}_6^{(h,B_1,2)}$	$\mathtt{Qh}(6,\mathtt{B1},2,)$	$\frac{3\sqrt{22}C_1}{16} - \frac{\sqrt{55}C_3}{16} + \frac{\sqrt{3}C_5}{16}$
46	B_1	B1	3	_	$\mathbb{Q}_6^{(h,B_1,3)}$	$\mathtt{Qh}(6,\mathtt{B1},\mathtt{3},)$	$\frac{\sqrt{10}C_1}{16} + \frac{9C_3}{16} + \frac{\sqrt{165}C_5}{16}$
47	B_2	B2	1	_	$\mathbb{Q}_6^{(h,B_2,1)}$	$\mathtt{Qh}(6,\mathtt{B2},\mathtt{1},)$	$\frac{\sqrt{3}S_1}{4} - \frac{\sqrt{30}S_3}{8} - \frac{\sqrt{22}S_5}{8}$
48	B_2	B2	2	_	$\mathbb{Q}_6^{(h,B_2,2)}$	$\mathtt{Qh}(6,\mathtt{B2},2,)$	$\frac{3\sqrt{22}S_1}{16} + \frac{\sqrt{55}S_3}{16} + \frac{\sqrt{3}S_5}{16}$
49	B_2	B2	3	_	$\mathbb{Q}_6^{(h,B_2,3)}$	$\mathtt{Qh}(6,\mathtt{B2},\mathtt{3},)$	$\frac{\sqrt{10}S_1}{16} - \frac{9S_3}{16} + \frac{\sqrt{165}S_5}{16}$

表 8 rank 7

No.	irrep.	(tag)	mul.	comp.	harmonics	(tag)	definition
50	A_1	A1	1	_	$\mathbb{Q}_7^{(h,A_1,1)}$	$\mathtt{Qh}(7,\mathtt{A1},\mathtt{1},)$	C_0
51	A_1	A1	2	_	$\mathbb{Q}_7^{(h,A_1,2)}$	$\mathtt{Qh}(7,\mathtt{A1},\mathtt{2},)$	C_4
52	A_1	A1	3	_	$\mathbb{Q}_7^{(h,A_1,3)}$	$\mathtt{Qh}(7,\mathtt{A1},\mathtt{3},)$	C_6
53	A_1	A1	4	-	$\mathbb{Q}_7^{(h,A_1,4)}$	$\mathtt{Qh}(7,\mathtt{A1},\mathtt{4},)$	C_2
54	A_2	A2	1	-	$\mathbb{Q}_7^{(h,A_2,1)}$	$\mathtt{Qh}(7,\mathtt{A2},1,)$	$\frac{\sqrt{78}S_2}{12} + \frac{\sqrt{66}S_6}{12}$
55	A_2	A2	2	_	$\mathbb{Q}_7^{(h,A_2,2)}$	$\mathtt{Qh}(7,\mathtt{A2},\mathtt{2},)$	S_4
56	A_2	A2	3	_	$\mathbb{Q}_7^{(h,A_2,3)}$	$\mathtt{Qh}(7,\mathtt{A2},\mathtt{3},)$	$rac{\sqrt{66}S_2}{12} - rac{\sqrt{78}S_6}{12}$
57	B_1	B1	1	-	$\mathbb{Q}_7^{(h,B_1,1)}$	$\mathtt{Qh}(7,\mathtt{B1},1,)$	$-\frac{5\sqrt{7}C_1}{32} + \frac{3\sqrt{21}C_3}{32} - \frac{\sqrt{231}C_5}{32} + \frac{\sqrt{429}C_7}{32}$
58	B_1	B1	2	_	$\mathbb{Q}_7^{(h,B_1,2)}$	$\mathtt{Qh}(7,\mathtt{B1},\mathtt{2},)$	$-\frac{3\sqrt{33}C_1}{32} - \frac{\sqrt{11}C_3}{32} + \frac{25C_5}{32} + \frac{\sqrt{91}C_7}{32}$
59	B_1	B1	3	_	$\mathbb{Q}_7^{(h,B_1,3)}$	$\mathtt{Qh}(7,\mathtt{B1},\mathtt{3},)$	$-\frac{\sqrt{858}C_1}{64} - \frac{3\sqrt{286}C_3}{64} - \frac{5\sqrt{26}C_5}{64} - \frac{\sqrt{14}C_7}{64}$
60	B_1	B1	4	_	$\mathbb{Q}_7^{(h,B_1,4)}$	$\mathtt{Qh}(7,\mathtt{B1},4,)$	$-\frac{15\sqrt{6}C_1}{64} + \frac{19\sqrt{2}C_3}{64} - \frac{\sqrt{22}C_5}{64} - \frac{\sqrt{2002}C_7}{64}$
61	B_2	B2	1	_	$\mathbb{Q}_7^{(h,B_2,1)}$	$\mathtt{Qh}(7,\mathtt{B2},1,)$	$-\frac{5\sqrt{7}S_1}{32} - \frac{3\sqrt{21}S_3}{32} - \frac{\sqrt{231}S_5}{32} - \frac{\sqrt{429}S_7}{32}$
62	B_2	B2	2	_	$\mathbb{Q}_7^{(h,B_2,2)}$	$\mathtt{Qh}(7,\mathtt{B2},2,)$	$-\frac{3\sqrt{33}S_1}{32} + \frac{\sqrt{11}S_3}{32} + \frac{25S_5}{32} - \frac{\sqrt{91}S_7}{32}$
63	B_2	B2	3	_	$\mathbb{Q}_7^{(h,B_2,3)}$	$\mathtt{Qh}(7,\mathtt{B2},3,)$	$\frac{\sqrt{858}S_1}{64} - \frac{3\sqrt{286}S_3}{64} + \frac{5\sqrt{26}S_5}{64} - \frac{\sqrt{14}S_7}{64}$
64	B_2	B2	4	_	$\mathbb{Q}_7^{(h,B_2,4)}$	$\mathtt{Qh}(7,\mathtt{B2},4,)$	$\frac{15\sqrt{6}S_1}{64} + \frac{19\sqrt{2}S_3}{64} + \frac{\sqrt{22}S_5}{64} - \frac{\sqrt{2002}S_7}{64}$

表 9 rank 8

No.	irrep.	(tag)	mul.	comp.	harmonics	(tag)	definition
65	A_1	A1	1	_	$\mathbb{Q}_8^{(h,A_1,1)}$	Qh(8, A1, 1,)	$\frac{\sqrt{33}C_0}{8} + \frac{\sqrt{21}C_4}{12} + \frac{\sqrt{195}C_8}{24}$
66	A_1	A1	2	_	$\mathbb{Q}_8^{(h,A_1,2)}$	$\mathtt{Qh}(\mathtt{8},\mathtt{A1},\mathtt{2},)$	$-\frac{\sqrt{286}C_0}{32} + \frac{\sqrt{182}C_4}{16} + \frac{\sqrt{10}C_8}{32}$
67	A_1	A1	3	_	$\mathbb{Q}_8^{(h,A_1,3)}$	$\mathtt{Qh}(8,\mathtt{A1},\mathtt{3},)$	C_6
68	A_1	A1	4	_	$\mathbb{Q}_8^{(h,A_1,4)}$	$\mathtt{Qh}(\mathtt{8},\mathtt{A1},\mathtt{4},)$	$-\frac{\sqrt{210}C_0}{32} - \frac{\sqrt{330}C_4}{48} + \frac{\sqrt{6006}C_8}{96}$
69	A_1	A1	5	-	$\mathbb{Q}_8^{(h,A_1,5)}$	$\mathtt{Qh}(8,\mathtt{A1},5,)$	C_2
70	A_2	A2	1	-	$\mathbb{Q}_8^{(h,A_2,1)}$	$\mathtt{Qh}(8,\mathtt{A2},\mathtt{1},)$	S_8
71	A_2	A2	2	-	$\mathbb{Q}_8^{(h,A_2,2)}$	$\mathtt{Qh}(8,\mathtt{A2},\mathtt{2},)$	S_4
72	A_2	A2	3	-	$\mathbb{Q}_8^{(h,A_2,3)}$	$\mathtt{Qh}(8,\mathtt{A2},\mathtt{3},)$	S_6
73	A_2	A2	4	_	$\mathbb{Q}_8^{(h,A_2,4)}$	$\mathtt{Qh}(8,\mathtt{A2},4,)$	S_2
74	B_1	B1	1	_	$\mathbb{Q}_8^{(h,B_1,1)}$	$\mathtt{Qh}(8,\mathtt{B1},\mathtt{1},)$	$\frac{\sqrt{715}C_1}{32} - \frac{\sqrt{273}C_3}{32} + \frac{\sqrt{35}C_5}{32} - \frac{C_7}{32}$
75	B_1	B1	2	_	$\mathbb{Q}_8^{(h,B_1,2)}$	$\mathtt{Qh}(8,\mathtt{B1},2,)$	$\frac{\sqrt{77}C_1}{32} + \frac{5\sqrt{15}C_3}{32} + \frac{3\sqrt{13}C_5}{32} - \frac{\sqrt{455}C_7}{32}$
76	B_1	B1	3	_	$\mathbb{Q}_8^{(h,B_1,3)}$	$\mathtt{Qh}(8,\mathtt{B1},3,)$	$-\frac{\sqrt{858}C_1}{64} - \frac{\sqrt{910}C_3}{64} + \frac{7\sqrt{42}C_5}{64} - \frac{3\sqrt{30}C_7}{64}$
77	B_1	B1	4	-	$\mathbb{Q}_8^{(h,B_1,4)}$	$\mathtt{Qh}(8,\mathtt{B1},4,)$	$-\frac{\sqrt{70}C_1}{64} - \frac{3\sqrt{66}C_3}{64} - \frac{\sqrt{1430}C_5}{64} - \frac{\sqrt{2002}C_7}{64}$
78	B_2	B2	1	-	$\mathbb{Q}_8^{(h,B_2,1)}$	$\mathtt{Qh}(8,\mathtt{B2},\mathtt{1},)$	$-\frac{\sqrt{715}S_1}{32} - \frac{\sqrt{273}S_3}{32} - \frac{\sqrt{35}S_5}{32} - \frac{S_7}{32}$
79	B_2	B2	2	-	$\mathbb{Q}_8^{(h,B_2,2)}$	$\mathtt{Qh}(8,\mathtt{B2},\mathtt{2},)$	$-\frac{\sqrt{77}S_1}{32} + \frac{5\sqrt{15}S_3}{32} - \frac{3\sqrt{13}S_5}{32} - \frac{\sqrt{455}S_7}{32}$
80	B_2	B2	3	_	$\mathbb{Q}_8^{(h,B_2,3)}$	$\mathtt{Qh}(8,\mathtt{B2},\mathtt{3},)$	$-\frac{\sqrt{858}S_1}{64} + \frac{\sqrt{910}S_3}{64} + \frac{7\sqrt{42}S_5}{64} + \frac{3\sqrt{30}S_7}{64}$
81	B_2	B2	4	_	$\mathbb{Q}_8^{(h,B_2,4)}$	$\mathtt{Qh}(8,\mathtt{B2},4,)$	$-\frac{\sqrt{70}S_1}{64} + \frac{3\sqrt{66}S_3}{64} - \frac{\sqrt{1430}S_5}{64} + \frac{\sqrt{2002}S_7}{64}$

表 10 rank 9

No.	irrep.	(tag)	mul.	comp.	harmonics	(tag)	definition
82	A_1	A1	1	-	$\mathbb{Q}_9^{(h,A_1,1)}$	$\mathtt{Qh}(9,\mathtt{A1},\mathtt{1},)$	C_0
83	A_1	A1	2	-	$\mathbb{Q}_9^{(h,A_1,2)}$	$\mathtt{Qh}(9,\mathtt{A1},2,)$	C_8
84	A_1	A1	3	_	$\mathbb{Q}_9^{(h,A_1,3)}$	$\mathtt{Qh}(9,\mathtt{A1},\mathtt{3},)$	C_4
85	A_1	A1	4	_	$\mathbb{Q}_9^{(h,A_1,4)}$	$\mathtt{Qh}(9,\mathtt{A1},4,)$	C_6
86	A_1	A1	5	=	$\mathbb{Q}_9^{(h,A_1,5)}$	$\mathtt{Qh}(9,\mathtt{A1},5,)$	C_2
87	A_2	A2	1	_	$\mathbb{Q}_9^{(h,A_2,1)}$	$\mathtt{Qh}(9,\mathtt{A2},\mathtt{1},)$	$\frac{\sqrt{102}S_4}{12} - \frac{\sqrt{42}S_8}{12}$
88	A_2	A2	2	_	$\mathbb{Q}_9^{(h,A_2,2)}$	$\mathtt{Qh}(9,\mathtt{A2},2,)$	$rac{\sqrt{3}S_2}{4} - rac{\sqrt{13}S_6}{4}$
89	A_2	A2	3	-	$\mathbb{Q}_9^{(h,A_2,3)}$	$\mathtt{Qh}(9,\mathtt{A2},\mathtt{3},)$	$\frac{\sqrt{42}S_4}{12} + \frac{\sqrt{102}S_8}{12}$
90	A_2	A2	4	-	$\mathbb{Q}_9^{(h,A_2,4)}$	$\mathtt{Qh}(9,\mathtt{A2},4,)$	$-rac{\sqrt{13}S_2}{4} - rac{\sqrt{3}S_6}{4}$
91	B_1	B1	1	-	$\mathbb{Q}_9^{(h,B_1,1)}$	$\mathtt{Qh}(9,\mathtt{B1},1,)$	$\frac{21\sqrt{5}C_1}{128} - \frac{\sqrt{2310}C_3}{128} + \frac{3\sqrt{286}C_5}{128} - \frac{3\sqrt{1430}C_7}{256} + \frac{\sqrt{24310}C_9}{256}$
92	B_1	B1	2	_	$\mathbb{Q}_9^{(h,B_1,2)}$	$\mathtt{Qh}(9,\mathtt{B1},2,)$	$\frac{\sqrt{2431}C_1}{128} + \frac{\sqrt{9282}C_3}{128} + \frac{5\sqrt{170}C_5}{128} + \frac{7\sqrt{34}C_7}{256} + \frac{3\sqrt{2}C_9}{256}$
93	B_1	B1	3	_	$\mathbb{Q}_9^{(h,B_1,3)}$	$\mathtt{Qh}(9,\mathtt{B1},\mathtt{3},)$	$\frac{\sqrt{1001}C_1}{64} - \frac{\sqrt{78}C_3}{64} - \frac{3\sqrt{70}C_5}{64} + \frac{23\sqrt{14}C_7}{128} + \frac{3\sqrt{238}C_9}{128}$
94	B_1	B1	4	_	$\mathbb{Q}_9^{(h,B_1,4)}$	$\mathtt{Qh}(9,\mathtt{B1},4,)$	$\frac{\sqrt{858}C_1}{64} + \frac{\sqrt{91}C_3}{32} - \frac{5\sqrt{15}C_5}{32} - \frac{21\sqrt{3}C_7}{64} - \frac{\sqrt{51}C_9}{64}$
95	B_1	B1	5	-	$\mathbb{Q}_9^{(h,B_1,5)}$	$\mathtt{Qh}(9,\mathtt{B1},5,)$	$\frac{7\sqrt{22}C_1}{64} - \frac{3\sqrt{21}C_3}{32} + \frac{\sqrt{65}C_5}{32} + \frac{\sqrt{13}C_7}{64} - \frac{3\sqrt{221}C_9}{64}$
96	B_2	B2	1	_	$\mathbb{Q}_9^{(h,B_2,1)}$	$\mathtt{Qh}(9,\mathtt{B2},1,)$	$\frac{21\sqrt{5}S_1}{128} + \frac{\sqrt{2310}S_3}{128} + \frac{3\sqrt{286}S_5}{128} + \frac{3\sqrt{1430}S_7}{256} + \frac{\sqrt{24310}S_9}{256}$
97	B_2	B2	2	_	$\mathbb{Q}_9^{(h,B_2,2)}$	$\mathtt{Qh}(9,\mathtt{B2},\mathtt{2},)$	$\frac{\sqrt{2431}S_1}{128} - \frac{\sqrt{9282}S_3}{128} + \frac{5\sqrt{170}S_5}{128} - \frac{7\sqrt{34}S_7}{256} + \frac{3\sqrt{2}S_9}{256}$
98	B_2	B2	3	_	$\mathbb{Q}_9^{(h,B_2,3)}$	$\mathtt{Qh}(9,\mathtt{B2},3,)$	$\frac{\sqrt{1001}S_1}{64} + \frac{\sqrt{78}S_3}{64} - \frac{3\sqrt{70}S_5}{64} - \frac{23\sqrt{14}S_7}{128} + \frac{3\sqrt{238}S_9}{128}$
99	B_2	B2	4	_	$\mathbb{Q}_9^{(h,B_2,4)}$	$\mathtt{Qh}(9,\mathtt{B2},4,)$	$-\frac{\sqrt{858}S_1}{64} + \frac{\sqrt{91}S_3}{32} + \frac{5\sqrt{15}S_5}{32} - \frac{21\sqrt{3}S_7}{64} + \frac{\sqrt{51}S_9}{64}$
100	B_2	B2	5	_	$\mathbb{Q}_9^{(h,B_2,5)}$	Qh(9,B2,5,)	$-\frac{7\sqrt{22}S_1}{64} - \frac{3\sqrt{21}S_3}{32} - \frac{\sqrt{65}S_5}{32} + \frac{\sqrt{13}S_7}{64} + \frac{3\sqrt{221}S_9}{64}$

表 11 rank 10

NI -	•	(+)	1		1	(+)	definition
No.	irrep.	(tag)	mul.	comp.	harmonics	(tag)	
101	A_1	A1	1	_	$\mathbb{Q}_{10}^{(h,A_1,1)}$	$\mathtt{Qh}(\mathtt{10},\mathtt{A1},\mathtt{1},)$	$\frac{\sqrt{390}C_0}{48} - \frac{\sqrt{22}C_4}{8} - \frac{\sqrt{1122}C_8}{48}$
102	A_1	A1	2	-	$\mathbb{Q}_{10}^{(h,A_1,2)}$	$\mathtt{Qh}(\mathtt{10},\mathtt{A1},\mathtt{2},)$	$-\frac{\sqrt{85}C_{10}}{16} + \frac{\sqrt{1482}C_2}{48} + \frac{\sqrt{57}C_6}{48}$
103	A_1	A1	3	_	$\mathbb{Q}_{10}^{(h,A_1,3)}$	$\mathtt{Qh}(\mathtt{10},\mathtt{A1},\mathtt{3},)$	$\frac{11\sqrt{420189}C_0}{8988} + \frac{\sqrt{827645}C_4}{1498} - \frac{\sqrt{146055}C_8}{8988}$
104	A_1	A1	4	-	$\mathbb{Q}_{10}^{(h,A_1,4)}$	$\mathtt{Qh}(\mathtt{10},\mathtt{A1},\mathtt{4},)$	$\frac{\sqrt{370006}C_{10}}{749} + \frac{\sqrt{190995}C_2}{749}$
105	A_1	A1	5	_	$\mathbb{Q}_{10}^{(h,A_1,5)}$	$\mathtt{Qh}(\mathtt{10},\mathtt{A1},\mathtt{5},)$	$\frac{3\sqrt{3213210}C_0}{11984} - \frac{83\sqrt{1498}C_4}{5992} + \frac{31\sqrt{76398}C_8}{11984}$
106	A_1	A1	6	_	$\mathbb{Q}_{10}^{(h,A_1,6)}$	$\mathtt{Qh}(\mathtt{10},\mathtt{A1},6,)$	$\frac{\sqrt{1209635}C_{10}}{11984} - \frac{19\sqrt{58422}C_2}{35952} + \frac{\sqrt{2247}C_6}{48}$
107	A_2	A2	1	_	$\mathbb{Q}_{10}^{(h,A_2,1)}$	$\mathtt{Qh}(\mathtt{10},\mathtt{A2},\mathtt{1},)$	S_8
108	A_2	A2	2	_	$\mathbb{Q}_{10}^{(h,A_2,2)}$	$\mathtt{Qh}(\mathtt{10},\mathtt{A2},\mathtt{2},)$	S_4
109	A_2	A2	3	_	$\mathbb{Q}_{10}^{(h,A_2,3)}$	$\mathtt{Qh}(\mathtt{10},\mathtt{A2},\mathtt{3},)$	S_{10}
110	A_2	A2	4	_	$\mathbb{Q}_{10}^{(h,A_2,4)}$	$\mathtt{Qh}(\mathtt{10},\mathtt{A2},\mathtt{4},)$	S_6
111	A_2	A2	5	-	$\mathbb{Q}_{10}^{(h,A_2,5)}$	$\mathtt{Qh}(\mathtt{10},\mathtt{A2},\mathtt{5},)$	S_2
112	B_1	B1	1	-	$\mathbb{Q}_{10}^{(h,B_1,1)}$	$\mathtt{Qh}(\mathtt{10},\mathtt{B1},\mathtt{1},)$	$-\frac{\sqrt{221}C_1}{32} - \frac{\sqrt{102}C_3}{32} + \frac{\sqrt{510}C_5}{32} - \frac{11\sqrt{6}C_7}{64} + \frac{\sqrt{38}C_9}{64}$
113	B_1	B1	2	_	$\mathbb{Q}_{10}^{(h,B_1,2)}$	$\mathtt{Qh}(\mathtt{10},\mathtt{B1},\mathtt{2},)$	$-\frac{\sqrt{39}C_1}{32} - \frac{11\sqrt{2}C_3}{32} - \frac{5\sqrt{10}C_5}{32} - \frac{\sqrt{34}C_7}{64} + \frac{\sqrt{1938}C_9}{64}$
114	B_1	B1	3	_	$\mathbb{Q}_{10}^{(h,B_1,3)}$	$\mathtt{Qh}(\mathtt{10},\mathtt{B1},\mathtt{3},)$	$\frac{\sqrt{41990}C_1}{256} - \frac{\sqrt{4845}C_3}{128} + \frac{\sqrt{969}C_5}{128} - \frac{\sqrt{285}C_7}{256} + \frac{\sqrt{5}C_9}{256}$
115	B_1	B1	4	_	$\mathbb{Q}_{10}^{(h,B_1,4)}$	$\mathtt{Qh}(\mathtt{10},\mathtt{B1},\mathtt{4},)$	$\frac{9\sqrt{78}C_1}{256} + \frac{69C_3}{128} - \frac{\sqrt{5}C_5}{128} - \frac{43\sqrt{17}C_7}{256} + \frac{3\sqrt{969}C_9}{256}$
116	B_1	B1	5	_	$\mathbb{Q}_{10}^{(h,B_1,5)}$	$\mathtt{Qh}(\mathtt{10},\mathtt{B1},\mathtt{5},)$	$\frac{7\sqrt{3}C_1}{128} + \frac{7\sqrt{26}C_3}{128} + \frac{5\sqrt{130}C_5}{128} + \frac{7\sqrt{442}C_7}{256} + \frac{\sqrt{25194}C_9}{256}$
117	B_2	B2	1	_	$\mathbb{Q}_{10}^{(h,B_2,1)}$	$\mathtt{Qh}(\mathtt{10},\mathtt{B2},\mathtt{1},)$	$\frac{\sqrt{221}S_1}{32} - \frac{\sqrt{102}S_3}{32} - \frac{\sqrt{510}S_5}{32} - \frac{11\sqrt{6}S_7}{64} - \frac{\sqrt{38}S_9}{64}$
118	B_2	B2	2	_	$\mathbb{Q}_{10}^{(h,B_2,2)}$	$\mathtt{Qh}(\mathtt{10},\mathtt{B2},\mathtt{2},)$	$\frac{\sqrt{39}S_1}{32} - \frac{11\sqrt{2}S_3}{32} + \frac{5\sqrt{10}S_5}{32} - \frac{\sqrt{34}S_7}{64} - \frac{\sqrt{1938}S_9}{64}$
119	B_2	B2	3	_	$\mathbb{Q}_{10}^{(h,B_2,3)}$	$\mathtt{Qh}(\mathtt{10},\mathtt{B2},\mathtt{3},)$	$\frac{\sqrt{41990}S_1}{256} + \frac{\sqrt{4845}S_3}{128} + \frac{\sqrt{969}S_5}{128} + \frac{\sqrt{285}S_7}{256} + \frac{\sqrt{5}S_9}{256}$
120	B_2	B2	4	_	$\mathbb{Q}_{10}^{(h,B_2,4)}$	$\mathtt{Qh}(\mathtt{10},\mathtt{B2},\mathtt{4},)$	$\frac{9\sqrt{78}S_1}{256} - \frac{69S_3}{128} - \frac{\sqrt{5}S_5}{128} + \frac{43\sqrt{17}S_7}{256} + \frac{3\sqrt{969}S_9}{256}$
121	B_2	B2	5	_	$\mathbb{Q}_{10}^{(h,B_2,5)}$	$\mathtt{Qh}(\mathtt{10},\mathtt{B2},\mathtt{5},)$	$\frac{7\sqrt{3}S_1}{128} - \frac{7\sqrt{26}S_3}{128} + \frac{5\sqrt{130}S_5}{128} - \frac{7\sqrt{442}S_7}{256} + \frac{\sqrt{25194}S_9}{256}$

表 12 rank 11

						1 12	rank 11
No.	irrep.	(tag)	mul.	comp.	harmonics	(tag)	definition
122	A_1	A1	1	-	$\mathbb{Q}_{11}^{(h,A_1,1)}$	$\mathtt{Qh}(\mathtt{11},\mathtt{A1},\mathtt{1},)$	C_0
123	A_1	A1	2	-	$\mathbb{Q}_{11}^{(h,A_1,2)}$	$\mathtt{Qh}(\mathtt{11},\mathtt{A1},\mathtt{2},)$	C_8
124	A_1	A1	3	-	$\mathbb{Q}_{11}^{(h,A_1,3)}$	$\mathtt{Qh}(\mathtt{11},\mathtt{A1},\mathtt{3},)$	C_4
125	A_1	A1	4	-	$\mathbb{Q}_{11}^{(h,A_1,4)}$	$\mathtt{Qh}(\mathtt{11},\mathtt{A1},\mathtt{4},)$	C_{10}
126	A_1	A1	5	-	$\mathbb{Q}_{11}^{(h,A_1,5)}$	$\mathtt{Qh}(\mathtt{11},\mathtt{A1},\mathtt{5},)$	C_6
127	A_1	A1	6	-	$\mathbb{Q}_{11}^{(h,A_1,6)}$	$\mathtt{Qh}(\mathtt{11},\mathtt{A1},6,)$	C_2
128	A_2	A2	1	-	$\mathbb{Q}_{11}^{(h,A_2,1)}$	$\mathtt{Qh}(\mathtt{11},\mathtt{A2},\mathtt{1},)$	$\frac{\sqrt{798}S_{10}}{48} + \frac{\sqrt{255}S_2}{24} + \frac{3\sqrt{6}S_6}{16}$
129	A_2	A2	2	_	$\mathbb{Q}_{11}^{(h,A_2,2)}$	$\mathtt{Qh}(\mathtt{11},\mathtt{A2},\mathtt{2},)$	S_8
130	A_2	A2	3	_	$\mathbb{Q}_{11}^{(h,A_2,3)}$	$\mathtt{Qh}(\mathtt{11},\mathtt{A2},\mathtt{3},)$	$-\frac{\sqrt{210}S_{10}}{96} + \frac{\sqrt{969}S_2}{48} - \frac{\sqrt{570}S_6}{32}$
131	A_2	A2	4	_	$\mathbb{Q}_{11}^{(h,A_2,4)}$	$\mathtt{Qh}(\mathtt{11},\mathtt{A2},\mathtt{4},)$	S_4
132	A_2	A2	5	=	$\mathbb{Q}_{11}^{(h,A_2,5)}$	$\mathtt{Qh}(\mathtt{11},\mathtt{A2},\mathtt{5},)$	$-rac{\sqrt{646}S_{10}}{32}+rac{\sqrt{35}S_2}{16}+rac{\sqrt{238}S_6}{32}$
133	B_1	B1	1	_	$\mathbb{Q}_{11}^{(h,B_1,1)}$	$\mathtt{Qh}(\mathtt{11},\mathtt{B1},\mathtt{1},)$	$-\frac{21\sqrt{66}C_1}{512} + \frac{\sqrt{88179}C_{11}}{512} + \frac{\sqrt{30030}C_3}{512} - \frac{15\sqrt{143}C_5}{512} + \frac{\sqrt{36465}C_7}{512} - \frac{\sqrt{46189}C_9}{512}$
134	B_1	B1	2	_	$\mathbb{Q}_{11}^{(h,B_1,2)}$	$\mathtt{Qh}(\mathtt{11},\mathtt{B1},\mathtt{2},)$	$-\frac{\sqrt{41990}C_1}{512} + \frac{\sqrt{385}C_{11}}{512} - \frac{3\sqrt{4522}C_3}{512} + \frac{3\sqrt{4845}C_5}{512} + \frac{77\sqrt{19}C_7}{512} + \frac{39\sqrt{15}C_9}{512}$
135	B_1	B1	3	_	$\mathbb{Q}_{11}^{(h,B_1,3)}$	$\mathtt{Qh}(\mathtt{11},\mathtt{B1},\mathtt{3},)$	$-\frac{5\sqrt{546}C_1}{256} + \frac{\sqrt{10659}C_{11}}{256} + \frac{11\sqrt{30}C_3}{256} + \frac{13\sqrt{7}C_5}{256} - \frac{3\sqrt{1785}C_7}{256} + \frac{3\sqrt{2261}C_9}{256}$
136	B_1	B1	4	_	$\mathbb{Q}_{11}^{(h,B_1,4)}$	$\mathtt{Qh}(\mathtt{11},\mathtt{B1},\mathtt{4},)$	$-\frac{\sqrt{29393}C_1}{512}-\frac{\sqrt{22}C_{11}}{1024}-\frac{9\sqrt{1615}C_3}{512}-\frac{5\sqrt{13566}C_5}{1024}-\frac{7\sqrt{1330}C_7}{1024}-\frac{9\sqrt{42}C_9}{1024}$
137	B_1	B1	5	_	$\mathbb{Q}_{11}^{(h,B_1,5)}$	$\mathtt{Qh}(\mathtt{11},\mathtt{B1},\mathtt{5},)$	$-\frac{15\sqrt{221}C_1}{512}-\frac{3\sqrt{2926}C_{11}}{1024}-\frac{\sqrt{595}C_3}{512}+\frac{53\sqrt{102}C_5}{1024}-\frac{105\sqrt{10}C_7}{1024}-\frac{61\sqrt{114}C_9}{1024}$
138	B_1	B1	6	_	$\mathbb{Q}_{11}^{(h,B_1,6)}$	$\mathtt{Qh}(\mathtt{11},\mathtt{B1},6,)$	$-\frac{21\sqrt{130}C_1}{512} - \frac{\sqrt{124355}C_{11}}{512} + \frac{57\sqrt{14}C_3}{512} - \frac{41\sqrt{15}C_5}{512} + \frac{17\sqrt{17}C_7}{512} + \frac{\sqrt{4845}C_9}{512}$
139	B_2	B2	1	_	$\mathbb{Q}_{11}^{(h,B_2,1)}$	$\mathtt{Qh}(\mathtt{11},\mathtt{B2},\mathtt{1},)$	$-\frac{21\sqrt{66}S_1}{512}-\frac{\sqrt{88179}S_{11}}{512}-\frac{\sqrt{30030}S_3}{512}-\frac{15\sqrt{143}S_5}{512}-\frac{\sqrt{36465}S_7}{512}-\frac{\sqrt{46189}S_9}{512}$
140	B_2	B2	2	_	$\mathbb{Q}_{11}^{(h,B_2,2)}$	$\mathtt{Qh}(\mathtt{11},\mathtt{B2},\mathtt{2},)$	$-\frac{\sqrt{41990}S_1}{512} - \frac{\sqrt{385}S_{11}}{512} + \frac{3\sqrt{4522}S_3}{512} + \frac{3\sqrt{4845}S_5}{512} - \frac{77\sqrt{19}S_7}{512} + \frac{39\sqrt{15}S_9}{512}$
141	B_2	B2	3	_	$\mathbb{Q}_{11}^{(h,B_2,3)}$	$\mathtt{Qh}(\mathtt{11},\mathtt{B2},\mathtt{3},)$	$-\frac{5\sqrt{546}S_1}{256} - \frac{\sqrt{10659}S_{11}}{256} - \frac{11\sqrt{30}S_3}{256} + \frac{13\sqrt{7}S_5}{256} + \frac{3\sqrt{1785}S_7}{256} + \frac{3\sqrt{2261}S_9}{256}$
142	B_2	B2	4	_	$\mathbb{Q}_{11}^{(h,B_2,4)}$	$\mathtt{Qh}(\mathtt{11},\mathtt{B2},\mathtt{4},)$	$\frac{\sqrt{29393}S_1}{512} - \frac{\sqrt{22}S_{11}}{1024} - \frac{9\sqrt{1615}S_3}{512} + \frac{5\sqrt{13566}S_5}{1024} - \frac{7\sqrt{1330}S_7}{1024} + \frac{9\sqrt{42}S_9}{1024}$
143	B_2	B2	5	_	$\mathbb{Q}_{11}^{(h,B_2,5)}$	$\mathtt{Qh}(\mathtt{11},\mathtt{B2},\mathtt{5},)$	$\frac{15\sqrt{221}S_1}{512} - \frac{3\sqrt{2926}S_{11}}{1024} - \frac{\sqrt{595}S_3}{512} - \frac{53\sqrt{102}S_5}{1024} - \frac{105\sqrt{10}S_7}{1024} + \frac{61\sqrt{114}S_9}{1024}$
144	B_2	B2	6	_	$\mathbb{Q}_{11}^{(h,B_2,6)}$	Qh(11, B2, 6,)	$\frac{21\sqrt{130}S_1}{512} - \frac{\sqrt{124355}S_{11}}{512} + \frac{57\sqrt{14}S_3}{512} + \frac{41\sqrt{15}S_5}{512} + \frac{17\sqrt{17}S_7}{512} - \frac{\sqrt{4845}S_9}{512}$