

SG No. 176 C_{6h}^2 $P6_3/m$ [hexagonal]

* plus set: $+ [0, 0, 0]$

* Wyckoff site: **2a**, site symmetry: $-6..$

Table 1: Wyckoff bond: **2a@2a**

| No. | vector | center | mapping |
|-----|-------------|-----------------------|----------------------------|
| 1 | $[0, 0, Z]$ | $[0, 0, \frac{1}{4}]$ | $[1, 2, 3, -10, -11, -12]$ |
| 2 | $[0, 0, Z]$ | $[0, 0, \frac{3}{4}]$ | $[4, 5, 6, -7, -8, -9]$ |

Table 2: Wyckoff bond: **6b@2a**

| No. | vector | center | mapping |
|-----|-------------------|-----------------------|-----------|
| 1 | $[X, Y, 0]$ | $[0, 0, \frac{1}{4}]$ | $[1, 10]$ |
| 2 | $[-Y, X - Y, 0]$ | $[0, 0, \frac{1}{4}]$ | $[2, 11]$ |
| 3 | $[-X + Y, -X, 0]$ | $[0, 0, \frac{1}{4}]$ | $[3, 12]$ |
| 4 | $[-X, -Y, 0]$ | $[0, 0, \frac{3}{4}]$ | $[4, 7]$ |
| 5 | $[Y, -X + Y, 0]$ | $[0, 0, \frac{3}{4}]$ | $[5, 8]$ |
| 6 | $[X - Y, X, 0]$ | $[0, 0, \frac{3}{4}]$ | $[6, 9]$ |

Table 3: Wyckoff bond: **12c@2a**

| No. | vector | center | mapping |
|-----|--------------------|-----------------------|---------|
| 1 | $[X, Y, Z]$ | $[0, 0, \frac{1}{4}]$ | $[1]$ |
| 2 | $[-Y, X - Y, Z]$ | $[0, 0, \frac{1}{4}]$ | $[2]$ |
| 3 | $[-X + Y, -X, Z]$ | $[0, 0, \frac{1}{4}]$ | $[3]$ |
| 4 | $[-X, -Y, Z]$ | $[0, 0, \frac{3}{4}]$ | $[4]$ |
| 5 | $[Y, -X + Y, Z]$ | $[0, 0, \frac{3}{4}]$ | $[5]$ |
| 6 | $[X - Y, X, Z]$ | $[0, 0, \frac{3}{4}]$ | $[6]$ |
| 7 | $[-X, -Y, -Z]$ | $[0, 0, \frac{3}{4}]$ | $[7]$ |
| 8 | $[Y, -X + Y, -Z]$ | $[0, 0, \frac{3}{4}]$ | $[8]$ |
| 9 | $[X - Y, X, -Z]$ | $[0, 0, \frac{3}{4}]$ | $[9]$ |
| 10 | $[X, Y, -Z]$ | $[0, 0, \frac{1}{4}]$ | $[10]$ |
| 11 | $[-Y, X - Y, -Z]$ | $[0, 0, \frac{1}{4}]$ | $[11]$ |
| 12 | $[-X + Y, -X, -Z]$ | $[0, 0, \frac{1}{4}]$ | $[12]$ |

* Wyckoff site: **2b**, site symmetry: $-3..$

Table 4: Wyckoff bond: **2a@2b**

| No. | vector | center | mapping |
|-----|-------------|-------------|-------------------------|
| 1 | $[0, 0, Z]$ | $[0, 0, 0]$ | $[1, 2, 3, -7, -8, -9]$ |

continued ...

Table 4

| No. | vector | center | mapping |
|-----|-------------|-----------------------|----------------------------|
| 2 | $[0, 0, Z]$ | $[0, 0, \frac{1}{2}]$ | $[4, 5, 6, -10, -11, -12]$ |

Table 5: Wyckoff bond: **6b@2b**

| No. | vector | center | mapping |
|-----|-------------------|-----------------------|------------|
| 1 | $[X, Y, Z]$ | $[0, 0, 0]$ | $[1, -7]$ |
| 2 | $[-Y, X - Y, Z]$ | $[0, 0, 0]$ | $[2, -8]$ |
| 3 | $[-X + Y, -X, Z]$ | $[0, 0, 0]$ | $[3, -9]$ |
| 4 | $[-X, -Y, Z]$ | $[0, 0, \frac{1}{2}]$ | $[4, -10]$ |
| 5 | $[Y, -X + Y, Z]$ | $[0, 0, \frac{1}{2}]$ | $[5, -11]$ |
| 6 | $[X - Y, X, Z]$ | $[0, 0, \frac{1}{2}]$ | $[6, -12]$ |

* Wyckoff site: **2c**, site symmetry: **-6..**

Table 6: Wyckoff bond: **2a@2c**

| No. | vector | center | mapping |
|-----|-------------|---|----------------------------|
| 1 | $[0, 0, Z]$ | $[\frac{1}{3}, \frac{2}{3}, \frac{1}{4}]$ | $[1, 2, 3, -10, -11, -12]$ |
| 2 | $[0, 0, Z]$ | $[\frac{2}{3}, \frac{1}{3}, \frac{3}{4}]$ | $[4, 5, 6, -7, -8, -9]$ |

Table 7: Wyckoff bond: **6b@2c**

| No. | vector | center | mapping |
|-----|-------------------|---|-----------|
| 1 | $[X, Y, 0]$ | $[\frac{1}{3}, \frac{2}{3}, \frac{1}{4}]$ | $[1, 10]$ |
| 2 | $[-Y, X - Y, 0]$ | $[\frac{1}{3}, \frac{2}{3}, \frac{1}{4}]$ | $[2, 11]$ |
| 3 | $[-X + Y, -X, 0]$ | $[\frac{1}{3}, \frac{2}{3}, \frac{1}{4}]$ | $[3, 12]$ |
| 4 | $[-X, -Y, 0]$ | $[\frac{2}{3}, \frac{1}{3}, \frac{3}{4}]$ | $[4, 7]$ |
| 5 | $[Y, -X + Y, 0]$ | $[\frac{2}{3}, \frac{1}{3}, \frac{3}{4}]$ | $[5, 8]$ |
| 6 | $[X - Y, X, 0]$ | $[\frac{2}{3}, \frac{1}{3}, \frac{3}{4}]$ | $[6, 9]$ |

Table 8: Wyckoff bond: **12c@2c**

| No. | vector | center | mapping |
|-----|-------------------|---|---------|
| 1 | $[X, Y, Z]$ | $[\frac{1}{3}, \frac{2}{3}, \frac{1}{4}]$ | $[1]$ |
| 2 | $[-Y, X - Y, Z]$ | $[\frac{1}{3}, \frac{2}{3}, \frac{1}{4}]$ | $[2]$ |
| 3 | $[-X + Y, -X, Z]$ | $[\frac{1}{3}, \frac{2}{3}, \frac{1}{4}]$ | $[3]$ |
| 4 | $[-X, -Y, Z]$ | $[\frac{2}{3}, \frac{1}{3}, \frac{3}{4}]$ | $[4]$ |
| 5 | $[Y, -X + Y, Z]$ | $[\frac{2}{3}, \frac{1}{3}, \frac{3}{4}]$ | $[5]$ |

continued ...

Table 8

| No. | vector | center | mapping |
|-----|--------------------|---|---------|
| 6 | $[X - Y, X, Z]$ | $[\frac{2}{3}, \frac{1}{3}, \frac{3}{4}]$ | [6] |
| 7 | $[-X, -Y, -Z]$ | $[\frac{2}{3}, \frac{1}{3}, \frac{3}{4}]$ | [7] |
| 8 | $[Y, -X + Y, -Z]$ | $[\frac{2}{3}, \frac{1}{3}, \frac{3}{4}]$ | [8] |
| 9 | $[X - Y, X, -Z]$ | $[\frac{2}{3}, \frac{1}{3}, \frac{3}{4}]$ | [9] |
| 10 | $[X, Y, -Z]$ | $[\frac{1}{3}, \frac{2}{3}, \frac{1}{4}]$ | [10] |
| 11 | $[-Y, X - Y, -Z]$ | $[\frac{1}{3}, \frac{2}{3}, \frac{1}{4}]$ | [11] |
| 12 | $[-X + Y, -X, -Z]$ | $[\frac{1}{3}, \frac{2}{3}, \frac{1}{4}]$ | [12] |

* Wyckoff site: 2d, site symmetry: $-6..$

Table 9: Wyckoff bond: 2a@2d

| No. | vector | center | mapping |
|-----|-------------|---|--------------------------|
| 1 | $[0, 0, Z]$ | $[\frac{2}{3}, \frac{1}{3}, \frac{1}{4}]$ | [1, 2, 3, -10, -11, -12] |
| 2 | $[0, 0, Z]$ | $[\frac{1}{3}, \frac{2}{3}, \frac{3}{4}]$ | [4, 5, 6, -7, -8, -9] |

Table 10: Wyckoff bond: 6b@2d

| No. | vector | center | mapping |
|-----|-------------------|---|---------|
| 1 | $[X, Y, 0]$ | $[\frac{2}{3}, \frac{1}{3}, \frac{1}{4}]$ | [1, 10] |
| 2 | $[-Y, X - Y, 0]$ | $[\frac{2}{3}, \frac{1}{3}, \frac{1}{4}]$ | [2, 11] |
| 3 | $[-X + Y, -X, 0]$ | $[\frac{2}{3}, \frac{1}{3}, \frac{1}{4}]$ | [3, 12] |
| 4 | $[-X, -Y, 0]$ | $[\frac{1}{3}, \frac{2}{3}, \frac{3}{4}]$ | [4, 7] |
| 5 | $[Y, -X + Y, 0]$ | $[\frac{1}{3}, \frac{2}{3}, \frac{3}{4}]$ | [5, 8] |
| 6 | $[X - Y, X, 0]$ | $[\frac{1}{3}, \frac{2}{3}, \frac{3}{4}]$ | [6, 9] |

Table 11: Wyckoff bond: 12c@2d

| No. | vector | center | mapping |
|-----|-------------------|---|---------|
| 1 | $[X, Y, Z]$ | $[\frac{2}{3}, \frac{1}{3}, \frac{1}{4}]$ | [1] |
| 2 | $[-Y, X - Y, Z]$ | $[\frac{2}{3}, \frac{1}{3}, \frac{1}{4}]$ | [2] |
| 3 | $[-X + Y, -X, Z]$ | $[\frac{2}{3}, \frac{1}{3}, \frac{1}{4}]$ | [3] |
| 4 | $[-X, -Y, Z]$ | $[\frac{1}{3}, \frac{2}{3}, \frac{3}{4}]$ | [4] |
| 5 | $[Y, -X + Y, Z]$ | $[\frac{1}{3}, \frac{2}{3}, \frac{3}{4}]$ | [5] |
| 6 | $[X - Y, X, Z]$ | $[\frac{1}{3}, \frac{2}{3}, \frac{3}{4}]$ | [6] |
| 7 | $[-X, -Y, -Z]$ | $[\frac{1}{3}, \frac{2}{3}, \frac{3}{4}]$ | [7] |
| 8 | $[Y, -X + Y, -Z]$ | $[\frac{1}{3}, \frac{2}{3}, \frac{3}{4}]$ | [8] |
| 9 | $[X - Y, X, -Z]$ | $[\frac{1}{3}, \frac{2}{3}, \frac{3}{4}]$ | [9] |
| 10 | $[X, Y, -Z]$ | $[\frac{2}{3}, \frac{1}{3}, \frac{1}{4}]$ | [10] |
| 11 | $[-Y, X - Y, -Z]$ | $[\frac{2}{3}, \frac{1}{3}, \frac{1}{4}]$ | [11] |

continued ...

Table 11

| No. | vector | center | mapping |
|-----|--------------------|---|---------|
| 12 | $[-X + Y, -X, -Z]$ | $[\frac{2}{3}, \frac{1}{3}, \frac{1}{4}]$ | [12] |

* Wyckoff site: **4e**, site symmetry: **3**.

Table 12: Wyckoff bond: **4a@4e**

| No. | vector | center | mapping |
|-----|--------------|---------------------------|--------------|
| 1 | $[0, 0, Z]$ | $[0, 0, z]$ | [1, 2, 3] |
| 2 | $[0, 0, Z]$ | $[0, 0, z + \frac{1}{2}]$ | [4, 5, 6] |
| 3 | $[0, 0, -Z]$ | $[0, 0, -z]$ | [7, 8, 9] |
| 4 | $[0, 0, -Z]$ | $[0, 0, \frac{1}{2} - z]$ | [10, 11, 12] |

Table 13: Wyckoff bond: **12b@4e**

| No. | vector | center | mapping |
|-----|--------------------|---------------------------|---------|
| 1 | $[X, Y, Z]$ | $[0, 0, z]$ | [1] |
| 2 | $[-Y, X - Y, Z]$ | $[0, 0, z]$ | [2] |
| 3 | $[-X + Y, -X, Z]$ | $[0, 0, z]$ | [3] |
| 4 | $[-X, -Y, Z]$ | $[0, 0, z + \frac{1}{2}]$ | [4] |
| 5 | $[Y, -X + Y, Z]$ | $[0, 0, z + \frac{1}{2}]$ | [5] |
| 6 | $[X - Y, X, Z]$ | $[0, 0, z + \frac{1}{2}]$ | [6] |
| 7 | $[-X, -Y, -Z]$ | $[0, 0, -z]$ | [7] |
| 8 | $[Y, -X + Y, -Z]$ | $[0, 0, -z]$ | [8] |
| 9 | $[X - Y, X, -Z]$ | $[0, 0, -z]$ | [9] |
| 10 | $[X, Y, -Z]$ | $[0, 0, \frac{1}{2} - z]$ | [10] |
| 11 | $[-Y, X - Y, -Z]$ | $[0, 0, \frac{1}{2} - z]$ | [11] |
| 12 | $[-X + Y, -X, -Z]$ | $[0, 0, \frac{1}{2} - z]$ | [12] |

* Wyckoff site: **4f**, site symmetry: **3**.

Table 14: Wyckoff bond: **4a@4f**

| No. | vector | center | mapping |
|-----|--------------|---|--------------|
| 1 | $[0, 0, Z]$ | $[\frac{1}{3}, \frac{2}{3}, z]$ | [1, 2, 3] |
| 2 | $[0, 0, Z]$ | $[\frac{2}{3}, \frac{1}{3}, z + \frac{1}{2}]$ | [4, 5, 6] |
| 3 | $[0, 0, -Z]$ | $[\frac{2}{3}, \frac{1}{3}, -z]$ | [7, 8, 9] |
| 4 | $[0, 0, -Z]$ | $[\frac{1}{3}, \frac{2}{3}, \frac{1}{2} - z]$ | [10, 11, 12] |

Table 15: Wyckoff bond: **12b@4f**

| No. | vector | center | mapping |
|-----|--------------------|---|---------|
| 1 | $[X, Y, Z]$ | $[\frac{1}{3}, \frac{2}{3}, z]$ | [1] |
| 2 | $[-Y, X - Y, Z]$ | $[\frac{1}{3}, \frac{2}{3}, z]$ | [2] |
| 3 | $[-X + Y, -X, Z]$ | $[\frac{1}{3}, \frac{2}{3}, z]$ | [3] |
| 4 | $[-X, -Y, Z]$ | $[\frac{2}{3}, \frac{1}{3}, z + \frac{1}{2}]$ | [4] |
| 5 | $[Y, -X + Y, Z]$ | $[\frac{2}{3}, \frac{1}{3}, z + \frac{1}{2}]$ | [5] |
| 6 | $[X - Y, X, Z]$ | $[\frac{2}{3}, \frac{1}{3}, z + \frac{1}{2}]$ | [6] |
| 7 | $[-X, -Y, -Z]$ | $[\frac{2}{3}, \frac{1}{3}, -z]$ | [7] |
| 8 | $[Y, -X + Y, -Z]$ | $[\frac{2}{3}, \frac{1}{3}, -z]$ | [8] |
| 9 | $[X - Y, X, -Z]$ | $[\frac{2}{3}, \frac{1}{3}, -z]$ | [9] |
| 10 | $[X, Y, -Z]$ | $[\frac{1}{3}, \frac{2}{3}, \frac{1}{2} - z]$ | [10] |
| 11 | $[-Y, X - Y, -Z]$ | $[\frac{1}{3}, \frac{2}{3}, \frac{1}{2} - z]$ | [11] |
| 12 | $[-X + Y, -X, -Z]$ | $[\frac{1}{3}, \frac{2}{3}, \frac{1}{2} - z]$ | [12] |

* Wyckoff site: **6g**, site symmetry: -1

Table 16: Wyckoff bond: **6a@6g**

| No. | vector | center | mapping |
|-----|-------------------|---|---------|
| 1 | $[X, Y, Z]$ | $[\frac{1}{2}, 0, 0]$ | [1,-7] |
| 2 | $[-Y, X - Y, Z]$ | $[0, \frac{1}{2}, 0]$ | [2,-8] |
| 3 | $[-X + Y, -X, Z]$ | $[\frac{1}{2}, \frac{1}{2}, 0]$ | [3,-9] |
| 4 | $[-X, -Y, Z]$ | $[\frac{1}{2}, 0, \frac{1}{2}]$ | [4,-10] |
| 5 | $[Y, -X + Y, Z]$ | $[0, \frac{1}{2}, \frac{1}{2}]$ | [5,-11] |
| 6 | $[X - Y, X, Z]$ | $[\frac{1}{2}, \frac{1}{2}, \frac{1}{2}]$ | [6,-12] |

* Wyckoff site: **6h**, site symmetry: $m..$

Table 17: Wyckoff bond: **6a@6h**

| No. | vector | center | mapping |
|-----|-------------------|-----------------------------|---------|
| 1 | $[X, Y, 0]$ | $[x, y, \frac{1}{4}]$ | [1,10] |
| 2 | $[-Y, X - Y, 0]$ | $[-y, x - y, \frac{1}{4}]$ | [2,11] |
| 3 | $[-X + Y, -X, 0]$ | $[-x + y, -x, \frac{1}{4}]$ | [3,12] |
| 4 | $[-X, -Y, 0]$ | $[-x, -y, \frac{3}{4}]$ | [4,7] |
| 5 | $[Y, -X + Y, 0]$ | $[y, -x + y, \frac{3}{4}]$ | [5,8] |
| 6 | $[X - Y, X, 0]$ | $[x - y, x, \frac{3}{4}]$ | [6,9] |

Table 18: Wyckoff bond: **6b@6h**

| No. | vector | center | mapping |
|-----|-------------|-----------------------------|------------|
| 1 | $[0, 0, Z]$ | $[x, y, \frac{1}{4}]$ | $[1, -10]$ |
| 2 | $[0, 0, Z]$ | $[-y, x - y, \frac{1}{4}]$ | $[2, -11]$ |
| 3 | $[0, 0, Z]$ | $[-x + y, -x, \frac{1}{4}]$ | $[3, -12]$ |
| 4 | $[0, 0, Z]$ | $[-x, -y, \frac{3}{4}]$ | $[4, -7]$ |
| 5 | $[0, 0, Z]$ | $[y, -x + y, \frac{3}{4}]$ | $[5, -8]$ |
| 6 | $[0, 0, Z]$ | $[x - y, x, \frac{3}{4}]$ | $[6, -9]$ |

Table 19: Wyckoff bond: **12c@6h**

| No. | vector | center | mapping |
|-----|--------------------|-----------------------------|---------|
| 1 | $[X, Y, Z]$ | $[x, y, \frac{1}{4}]$ | $[1]$ |
| 2 | $[-Y, X - Y, Z]$ | $[-y, x - y, \frac{1}{4}]$ | $[2]$ |
| 3 | $[-X + Y, -X, Z]$ | $[-x + y, -x, \frac{1}{4}]$ | $[3]$ |
| 4 | $[-X, -Y, Z]$ | $[-x, -y, \frac{3}{4}]$ | $[4]$ |
| 5 | $[Y, -X + Y, Z]$ | $[y, -x + y, \frac{3}{4}]$ | $[5]$ |
| 6 | $[X - Y, X, Z]$ | $[x - y, x, \frac{3}{4}]$ | $[6]$ |
| 7 | $[-X, -Y, -Z]$ | $[-x, -y, \frac{3}{4}]$ | $[7]$ |
| 8 | $[Y, -X + Y, -Z]$ | $[y, -x + y, \frac{3}{4}]$ | $[8]$ |
| 9 | $[X - Y, X, -Z]$ | $[x - y, x, \frac{3}{4}]$ | $[9]$ |
| 10 | $[X, Y, -Z]$ | $[x, y, \frac{1}{4}]$ | $[10]$ |
| 11 | $[-Y, X - Y, -Z]$ | $[-y, x - y, \frac{1}{4}]$ | $[11]$ |
| 12 | $[-X + Y, -X, -Z]$ | $[-x + y, -x, \frac{1}{4}]$ | $[12]$ |

* Wyckoff site: **12i**, site symmetry: **1**

Table 20: Wyckoff bond: **12a@12i**

| No. | vector | center | mapping |
|-----|--------------------|---------------------------------|---------|
| 1 | $[X, Y, Z]$ | $[x, y, z]$ | $[1]$ |
| 2 | $[-Y, X - Y, Z]$ | $[-y, x - y, z]$ | $[2]$ |
| 3 | $[-X + Y, -X, Z]$ | $[-x + y, -x, z]$ | $[3]$ |
| 4 | $[-X, -Y, Z]$ | $[-x, -y, z + \frac{1}{2}]$ | $[4]$ |
| 5 | $[Y, -X + Y, Z]$ | $[y, -x + y, z + \frac{1}{2}]$ | $[5]$ |
| 6 | $[X - Y, X, Z]$ | $[x - y, x, z + \frac{1}{2}]$ | $[6]$ |
| 7 | $[-X, -Y, -Z]$ | $[-x, -y, -z]$ | $[7]$ |
| 8 | $[Y, -X + Y, -Z]$ | $[y, -x + y, -z]$ | $[8]$ |
| 9 | $[X - Y, X, -Z]$ | $[x - y, x, -z]$ | $[9]$ |
| 10 | $[X, Y, -Z]$ | $[x, y, \frac{1}{2} - z]$ | $[10]$ |
| 11 | $[-Y, X - Y, -Z]$ | $[-y, x - y, \frac{1}{2} - z]$ | $[11]$ |
| 12 | $[-X + Y, -X, -Z]$ | $[-x + y, -x, \frac{1}{2} - z]$ | $[12]$ |