

No. 30 O 432 [cubic] (polar)

表 1 rank 0

| No. | irrep. | (tag) | mul. | comp. | harmonics | (tag) | definition |
|-----|--------|-----------|------|-------|--------------------------|----------------------|------------|
| 1 | A_1 | A1 | — | — | $\mathbb{Q}_0^{(h,A_1)}$ | Qh(0, A1, ,) | C_0 |

表 2 rank 1

| No. | irrep. | (tag) | mul. | comp. | harmonics | (tag) | definition |
|-----|--------|-----------|------|-------|------------------------------|-----------------------|------------|
| 2 | T_1 | T1 | — | 0 | $\mathbb{Q}_{1,0}^{(h,T_1)}$ | Qh(1, T1, , 0) | C_1 |
| 3 | T_1 | T1 | — | 1 | $\mathbb{Q}_{1,1}^{(h,T_1)}$ | Qh(1, T1, , 1) | S_1 |
| 4 | T_1 | T1 | — | 2 | $\mathbb{Q}_{1,2}^{(h,T_1)}$ | Qh(1, T1, , 2) | C_0 |

表 3 rank 2

| No. | irrep. | (tag) | mul. | comp. | harmonics | (tag) | definition |
|-----|--------|-----------|------|-------|------------------------------|-----------------------|------------|
| 5 | E | E | — | 0 | $\mathbb{Q}_{2,0}^{(h,E)}$ | Qh(2, E, , 0) | C_0 |
| 6 | E | E | — | 1 | $\mathbb{Q}_{2,1}^{(h,E)}$ | Qh(2, E, , 1) | C_2 |
| 7 | T_2 | T2 | — | 0 | $\mathbb{Q}_{2,0}^{(h,T_2)}$ | Qh(2, T2, , 0) | S_1 |
| 8 | T_2 | T2 | — | 1 | $\mathbb{Q}_{2,1}^{(h,T_2)}$ | Qh(2, T2, , 1) | C_1 |
| 9 | T_2 | T2 | — | 2 | $\mathbb{Q}_{2,2}^{(h,T_2)}$ | Qh(2, T2, , 2) | S_2 |

表 4 rank 3

| No. | irrep. | (tag) | mul. | comp. | harmonics | (tag) | definition |
|-----|--------|-----------|------|-------|------------------------------|-----------------------|---|
| 10 | A_2 | A2 | — | — | $\mathbb{Q}_3^{(h,A_2)}$ | Qh(3, A2, ,) | S_2 |
| 11 | T_1 | T1 | — | 0 | $\mathbb{Q}_{3,0}^{(h,T_1)}$ | Qh(3, T1, , 0) | $-\frac{\sqrt{6}C_1}{4} + \frac{\sqrt{10}C_3}{4}$ |
| 12 | T_1 | T1 | — | 1 | $\mathbb{Q}_{3,1}^{(h,T_1)}$ | Qh(3, T1, , 1) | $-\frac{\sqrt{6}S_1}{4} - \frac{\sqrt{10}S_3}{4}$ |
| 13 | T_1 | T1 | — | 2 | $\mathbb{Q}_{3,2}^{(h,T_1)}$ | Qh(3, T1, , 2) | C_0 |
| 14 | T_2 | T2 | — | 0 | $\mathbb{Q}_{3,0}^{(h,T_2)}$ | Qh(3, T2, , 0) | $-\frac{\sqrt{10}C_1}{4} - \frac{\sqrt{6}C_3}{4}$ |
| 15 | T_2 | T2 | — | 1 | $\mathbb{Q}_{3,1}^{(h,T_2)}$ | Qh(3, T2, , 1) | $\frac{\sqrt{10}S_1}{4} - \frac{\sqrt{6}S_3}{4}$ |
| 16 | T_2 | T2 | — | 2 | $\mathbb{Q}_{3,2}^{(h,T_2)}$ | Qh(3, T2, , 2) | C_2 |

表 5 rank 4

| No. | irrep. | (tag) | mul. | comp. | harmonics | (tag) | definition |
|-----|--------|-----------|------|-------|------------------------------|-----------------------|---|
| 17 | A_1 | A1 | — | — | $\mathbb{Q}_4^{(h,A_1)}$ | Qh(4, A1, ,) | $\frac{\sqrt{21}C_0}{6} + \frac{\sqrt{15}C_4}{6}$ |
| 18 | E | E | — | 0 | $\mathbb{Q}_{4,0}^{(h,E)}$ | Qh(4, E, , 0) | $\frac{\sqrt{15}C_0}{6} - \frac{\sqrt{21}C_4}{6}$ |
| 19 | E | E | — | 1 | $\mathbb{Q}_{4,1}^{(h,E)}$ | Qh(4, E, , 1) | $-C_2$ |
| 20 | T_1 | T1 | — | 0 | $\mathbb{Q}_{4,0}^{(h,T_1)}$ | Qh(4, T1, , 0) | $-\frac{\sqrt{14}S_1}{4} - \frac{\sqrt{2}S_3}{4}$ |
| 21 | T_1 | T1 | — | 1 | $\mathbb{Q}_{4,1}^{(h,T_1)}$ | Qh(4, T1, , 1) | $\frac{\sqrt{14}C_1}{4} - \frac{\sqrt{2}C_3}{4}$ |
| 22 | T_1 | T1 | — | 2 | $\mathbb{Q}_{4,2}^{(h,T_1)}$ | Qh(4, T1, , 2) | S_4 |
| 23 | T_2 | T2 | — | 0 | $\mathbb{Q}_{4,0}^{(h,T_2)}$ | Qh(4, T2, , 0) | $-\frac{\sqrt{2}S_1}{4} + \frac{\sqrt{14}S_3}{4}$ |
| 24 | T_2 | T2 | — | 1 | $\mathbb{Q}_{4,1}^{(h,T_2)}$ | Qh(4, T2, , 1) | $-\frac{\sqrt{2}C_1}{4} - \frac{\sqrt{14}C_3}{4}$ |
| 25 | T_2 | T2 | — | 2 | $\mathbb{Q}_{4,2}^{(h,T_2)}$ | Qh(4, T2, , 2) | S_2 |

表 6 rank 5

| No. | irrep. | (tag) | mul. | comp. | harmonics | (tag) | definition |
|-----|--------|-----------|------|-------|-----------------------|---------------------------------|---|
| 26 | E | E | — | 0 | $Q_{5,0}^{(h,E)}$ | $\text{Qh}(5, \text{E}, , 0)$ | S_4 |
| 27 | E | E | — | 1 | $Q_{5,1}^{(h,E)}$ | $\text{Qh}(5, \text{E}, , 1)$ | $-S_2$ |
| 28 | T_1 | T1 | 1 | 0 | $Q_{5,0}^{(h,T_1,1)}$ | $\text{Qh}(5, \text{T1}, 1, 0)$ | $\frac{\sqrt{15}C_1}{8} - \frac{\sqrt{70}C_3}{16} + \frac{3\sqrt{14}C_5}{16}$ |
| 29 | T_1 | T1 | 1 | 1 | $Q_{5,1}^{(h,T_1,1)}$ | $\text{Qh}(5, \text{T1}, 1, 1)$ | $\frac{\sqrt{15}S_1}{8} + \frac{\sqrt{70}S_3}{16} + \frac{3\sqrt{14}S_5}{16}$ |
| 30 | T_1 | T1 | 1 | 2 | $Q_{5,2}^{(h,T_1,1)}$ | $\text{Qh}(5, \text{T1}, 1, 2)$ | C_0 |
| 31 | T_1 | T1 | 2 | 0 | $Q_{5,0}^{(h,T_1,2)}$ | $\text{Qh}(5, \text{T1}, 2, 0)$ | $\frac{\sqrt{21}C_1}{8} + \frac{9\sqrt{2}C_3}{16} + \frac{\sqrt{10}C_5}{16}$ |
| 32 | T_1 | T1 | 2 | 1 | $Q_{5,1}^{(h,T_1,2)}$ | $\text{Qh}(5, \text{T1}, 2, 1)$ | $\frac{\sqrt{21}S_1}{8} - \frac{9\sqrt{2}S_3}{16} + \frac{\sqrt{10}S_5}{16}$ |
| 33 | T_1 | T1 | 2 | 2 | $Q_{5,2}^{(h,T_1,2)}$ | $\text{Qh}(5, \text{T1}, 2, 2)$ | C_4 |
| 34 | T_2 | T2 | — | 0 | $Q_{5,0}^{(h,T_2)}$ | $\text{Qh}(5, \text{T2}, , 0)$ | $\frac{\sqrt{7}C_1}{4} - \frac{\sqrt{6}C_3}{8} - \frac{\sqrt{30}C_5}{8}$ |
| 35 | T_2 | T2 | — | 1 | $Q_{5,1}^{(h,T_2)}$ | $\text{Qh}(5, \text{T2}, , 1)$ | $-\frac{\sqrt{7}S_1}{4} - \frac{\sqrt{6}S_3}{8} + \frac{\sqrt{30}S_5}{8}$ |
| 36 | T_2 | T2 | — | 2 | $Q_{5,2}^{(h,T_2)}$ | $\text{Qh}(5, \text{T2}, , 2)$ | C_2 |

表 7 rank 6

| No. | irrep. | (tag) | mul. | comp. | harmonics | (tag) | definition |
|-----|--------|-----------|------|-------|-----------------------|---------------------------------|---|
| 37 | A_1 | A1 | — | — | $Q_6^{(h,A_1)}$ | $\text{Qh}(6, \text{A1}, ,)$ | $\frac{\sqrt{2}C_0}{4} - \frac{\sqrt{14}C_4}{4}$ |
| 38 | A_2 | A2 | — | — | $Q_6^{(h,A_2)}$ | $\text{Qh}(6, \text{A2}, ,)$ | $\frac{\sqrt{11}C_2}{4} - \frac{\sqrt{5}C_6}{4}$ |
| 39 | E | E | — | 0 | $Q_{6,0}^{(h,E)}$ | $\text{Qh}(6, \text{E}, , 0)$ | $\frac{\sqrt{14}C_0}{4} + \frac{\sqrt{2}C_4}{4}$ |
| 40 | E | E | — | 1 | $Q_{6,1}^{(h,E)}$ | $\text{Qh}(6, \text{E}, , 1)$ | $\frac{\sqrt{5}C_2}{4} + \frac{\sqrt{11}C_6}{4}$ |
| 41 | T_1 | T1 | — | 0 | $Q_{6,0}^{(h,T_1)}$ | $\text{Qh}(6, \text{T1}, , 0)$ | $\frac{\sqrt{3}S_1}{4} - \frac{\sqrt{30}S_3}{8} - \frac{\sqrt{22}S_5}{8}$ |
| 42 | T_1 | T1 | — | 1 | $Q_{6,1}^{(h,T_1)}$ | $\text{Qh}(6, \text{T1}, , 1)$ | $-\frac{\sqrt{3}C_1}{4} - \frac{\sqrt{30}C_3}{8} + \frac{\sqrt{22}C_5}{8}$ |
| 43 | T_1 | T1 | — | 2 | $Q_{6,2}^{(h,T_1)}$ | $\text{Qh}(6, \text{T1}, , 2)$ | S_4 |
| 44 | T_2 | T2 | 1 | 0 | $Q_{6,0}^{(h,T_2,1)}$ | $\text{Qh}(6, \text{T2}, 1, 0)$ | $\frac{3\sqrt{22}S_1}{16} + \frac{\sqrt{55}S_3}{16} + \frac{\sqrt{3}S_5}{16}$ |
| 45 | T_2 | T2 | 1 | 1 | $Q_{6,1}^{(h,T_2,1)}$ | $\text{Qh}(6, \text{T2}, 1, 1)$ | $\frac{3\sqrt{22}C_1}{16} - \frac{\sqrt{55}C_3}{16} + \frac{\sqrt{3}C_5}{16}$ |
| 46 | T_2 | T2 | 1 | 2 | $Q_{6,2}^{(h,T_2,1)}$ | $\text{Qh}(6, \text{T2}, 1, 2)$ | S_6 |
| 47 | T_2 | T2 | 2 | 0 | $Q_{6,0}^{(h,T_2,2)}$ | $\text{Qh}(6, \text{T2}, 2, 0)$ | $\frac{\sqrt{10}S_1}{16} - \frac{9S_3}{16} + \frac{\sqrt{165}S_5}{16}$ |
| 48 | T_2 | T2 | 2 | 1 | $Q_{6,1}^{(h,T_2,2)}$ | $\text{Qh}(6, \text{T2}, 2, 1)$ | $\frac{\sqrt{10}C_1}{16} + \frac{9C_3}{16} + \frac{\sqrt{165}C_5}{16}$ |
| 49 | T_2 | T2 | 2 | 2 | $Q_{6,2}^{(h,T_2,2)}$ | $\text{Qh}(6, \text{T2}, 2, 2)$ | S_2 |

表 8 rank 7

| No. | irrep. | (tag) | mul. | comp. | harmonics | (tag) | definition |
|-----|--------|-------|------|-------|-----------------------|-----------------|--|
| 50 | A_2 | A2 | — | — | $Q_7^{(h,A_2)}$ | Qh(7, A2, ,) | $\frac{\sqrt{78}S_2}{12} + \frac{\sqrt{66}S_6}{12}$ |
| 51 | E | E | — | 0 | $Q_{7,0}^{(h,E)}$ | Qh(7, E, , 0) | S_4 |
| 52 | E | E | — | 1 | $Q_{7,1}^{(h,E)}$ | Qh(7, E, , 1) | $\frac{\sqrt{66}S_2}{12} - \frac{\sqrt{78}S_6}{12}$ |
| 53 | T_1 | T1 | 1 | 0 | $Q_{7,0}^{(h,T_1,1)}$ | Qh(7, T1, 1, 0) | $-\frac{5\sqrt{7}C_1}{32} + \frac{3\sqrt{21}C_3}{32} - \frac{\sqrt{231}C_5}{32} + \frac{\sqrt{429}C_7}{32}$ |
| 54 | T_1 | T1 | 1 | 1 | $Q_{7,1}^{(h,T_1,1)}$ | Qh(7, T1, 1, 1) | $-\frac{5\sqrt{7}S_1}{32} - \frac{3\sqrt{21}S_3}{32} - \frac{\sqrt{231}S_5}{32} - \frac{\sqrt{429}S_7}{32}$ |
| 55 | T_1 | T1 | 1 | 2 | $Q_{7,2}^{(h,T_1,1)}$ | Qh(7, T1, 1, 2) | C_0 |
| 56 | T_1 | T1 | 2 | 0 | $Q_{7,0}^{(h,T_1,2)}$ | Qh(7, T1, 2, 0) | $-\frac{3\sqrt{33}C_1}{32} - \frac{\sqrt{11}C_3}{32} + \frac{25C_5}{32} + \frac{\sqrt{91}C_7}{32}$ |
| 57 | T_1 | T1 | 2 | 1 | $Q_{7,1}^{(h,T_1,2)}$ | Qh(7, T1, 2, 1) | $-\frac{3\sqrt{33}S_1}{32} + \frac{\sqrt{11}S_3}{32} + \frac{25S_5}{32} - \frac{\sqrt{91}S_7}{32}$ |
| 58 | T_1 | T1 | 2 | 2 | $Q_{7,2}^{(h,T_1,2)}$ | Qh(7, T1, 2, 2) | C_4 |
| 59 | T_2 | T2 | 1 | 0 | $Q_{7,0}^{(h,T_2,1)}$ | Qh(7, T2, 1, 0) | $-\frac{\sqrt{858}C_1}{64} - \frac{3\sqrt{286}C_3}{64} - \frac{5\sqrt{26}C_5}{64} - \frac{\sqrt{14}C_7}{64}$ |
| 60 | T_2 | T2 | 1 | 1 | $Q_{7,1}^{(h,T_2,1)}$ | Qh(7, T2, 1, 1) | $\frac{\sqrt{858}S_1}{64} - \frac{3\sqrt{286}S_3}{64} + \frac{5\sqrt{26}S_5}{64} - \frac{\sqrt{14}S_7}{64}$ |
| 61 | T_2 | T2 | 1 | 2 | $Q_{7,2}^{(h,T_2,1)}$ | Qh(7, T2, 1, 2) | C_6 |
| 62 | T_2 | T2 | 2 | 0 | $Q_{7,0}^{(h,T_2,2)}$ | Qh(7, T2, 2, 0) | $-\frac{15\sqrt{6}C_1}{64} + \frac{19\sqrt{2}C_3}{64} - \frac{\sqrt{22}C_5}{64} - \frac{\sqrt{2002}C_7}{64}$ |
| 63 | T_2 | T2 | 2 | 1 | $Q_{7,1}^{(h,T_2,2)}$ | Qh(7, T2, 2, 1) | $\frac{15\sqrt{6}S_1}{64} + \frac{19\sqrt{2}S_3}{64} + \frac{\sqrt{22}S_5}{64} - \frac{\sqrt{2002}S_7}{64}$ |
| 64 | T_2 | T2 | 2 | 2 | $Q_{7,2}^{(h,T_2,2)}$ | Qh(7, T2, 2, 2) | C_2 |

表 9 rank 8

| No. | irrep. | (tag) | mul. | comp. | harmonics | (tag) | definition |
|-----|--------|-------|------|-------|-----------------------|-----------------|---|
| 65 | A_1 | A1 | — | — | $Q_8^{(h,A_1)}$ | Qh(8, A1, ,) | $\frac{\sqrt{33}C_0}{8} + \frac{\sqrt{21}C_4}{12} + \frac{\sqrt{195}C_8}{24}$ |
| 66 | E | E | 1 | 0 | $Q_{8,0}^{(h,E,1)}$ | Qh(8, E, 1, 0) | $-\frac{\sqrt{286}C_0}{32} + \frac{\sqrt{182}C_4}{16} + \frac{\sqrt{10}C_8}{32}$ |
| 67 | E | E | 1 | 1 | $Q_{8,1}^{(h,E,1)}$ | Qh(8, E, 1, 1) | C_6 |
| 68 | E | E | 2 | 0 | $Q_{8,0}^{(h,E,2)}$ | Qh(8, E, 2, 0) | $-\frac{\sqrt{210}C_0}{32} - \frac{\sqrt{330}C_4}{48} + \frac{\sqrt{6006}C_8}{96}$ |
| 69 | E | E | 2 | 1 | $Q_{8,1}^{(h,E,2)}$ | Qh(8, E, 2, 1) | C_2 |
| 70 | T_1 | T1 | 1 | 0 | $Q_{8,0}^{(h,T_1,1)}$ | Qh(8, T1, 1, 0) | $-\frac{\sqrt{715}S_1}{32} - \frac{\sqrt{273}S_3}{32} - \frac{\sqrt{35}S_5}{32} - \frac{S_7}{32}$ |
| 71 | T_1 | T1 | 1 | 1 | $Q_{8,1}^{(h,T_1,1)}$ | Qh(8, T1, 1, 1) | $\frac{\sqrt{715}C_1}{32} - \frac{\sqrt{273}C_3}{32} + \frac{\sqrt{35}C_5}{32} - \frac{C_7}{32}$ |
| 72 | T_1 | T1 | 1 | 2 | $Q_{8,2}^{(h,T_1,1)}$ | Qh(8, T1, 1, 2) | S_8 |
| 73 | T_1 | T1 | 2 | 0 | $Q_{8,0}^{(h,T_1,2)}$ | Qh(8, T1, 2, 0) | $-\frac{\sqrt{77}S_1}{32} + \frac{5\sqrt{15}S_3}{32} - \frac{3\sqrt{13}S_5}{32} - \frac{\sqrt{455}S_7}{32}$ |
| 74 | T_1 | T1 | 2 | 1 | $Q_{8,1}^{(h,T_1,2)}$ | Qh(8, T1, 2, 1) | $\frac{\sqrt{77}C_1}{32} + \frac{5\sqrt{15}C_3}{32} + \frac{3\sqrt{13}C_5}{32} - \frac{\sqrt{455}C_7}{32}$ |
| 75 | T_1 | T1 | 2 | 2 | $Q_{8,2}^{(h,T_1,2)}$ | Qh(8, T1, 2, 2) | S_4 |
| 76 | T_2 | T2 | 1 | 0 | $Q_{8,0}^{(h,T_2,1)}$ | Qh(8, T2, 1, 0) | $-\frac{\sqrt{858}S_1}{64} + \frac{\sqrt{910}S_3}{64} + \frac{7\sqrt{42}S_5}{64} + \frac{3\sqrt{30}S_7}{64}$ |
| 77 | T_2 | T2 | 1 | 1 | $Q_{8,1}^{(h,T_2,1)}$ | Qh(8, T2, 1, 1) | $-\frac{\sqrt{858}C_1}{64} - \frac{\sqrt{910}C_3}{64} + \frac{7\sqrt{42}C_5}{64} - \frac{3\sqrt{30}C_7}{64}$ |
| 78 | T_2 | T2 | 1 | 2 | $Q_{8,2}^{(h,T_2,1)}$ | Qh(8, T2, 1, 2) | S_6 |
| 79 | T_2 | T2 | 2 | 0 | $Q_{8,0}^{(h,T_2,2)}$ | Qh(8, T2, 2, 0) | $-\frac{\sqrt{70}S_1}{64} + \frac{3\sqrt{66}S_3}{64} - \frac{\sqrt{1430}S_5}{64} + \frac{\sqrt{2002}S_7}{64}$ |
| 80 | T_2 | T2 | 2 | 1 | $Q_{8,1}^{(h,T_2,2)}$ | Qh(8, T2, 2, 1) | $-\frac{\sqrt{70}C_1}{64} - \frac{3\sqrt{66}C_3}{64} - \frac{\sqrt{1430}C_5}{64} - \frac{\sqrt{2002}C_7}{64}$ |
| 81 | T_2 | T2 | 2 | 2 | $Q_{8,2}^{(h,T_2,2)}$ | Qh(8, T2, 2, 2) | S_2 |

表 10 rank 9

| No. | irrep. | (tag) | mul. | comp. | harmonics | (tag) | definition |
|-----|--------|-------|------|-------|--------------------------------|--------------------------|---|
| 82 | A_1 | A1 | — | — | $\mathbb{Q}_9^{(h,A_1)}$ | $\text{Qh}(9, A1, ,)$ | $\frac{\sqrt{102}S_4}{12} - \frac{\sqrt{42}S_8}{12}$ |
| 83 | A_2 | A2 | — | — | $\mathbb{Q}_9^{(h,A_2)}$ | $\text{Qh}(9, A2, ,)$ | $\frac{\sqrt{3}S_2}{4} - \frac{\sqrt{13}S_6}{4}$ |
| 84 | E | E | — | 0 | $\mathbb{Q}_{9,0}^{(h,E)}$ | $\text{Qh}(9, E, , 0)$ | $\frac{\sqrt{42}S_4}{12} + \frac{\sqrt{102}S_8}{12}$ |
| 85 | E | E | — | 1 | $\mathbb{Q}_{9,1}^{(h,E)}$ | $\text{Qh}(9, E, , 1)$ | $-\frac{\sqrt{13}S_2}{4} - \frac{\sqrt{3}S_6}{4}$ |
| 86 | T_1 | T1 | 1 | 0 | $\mathbb{Q}_{9,0}^{(h,T_1,1)}$ | $\text{Qh}(9, T1, 1, 0)$ | $\frac{21\sqrt{5}C_1}{128} - \frac{\sqrt{2310}C_3}{128} + \frac{3\sqrt{286}C_5}{128} - \frac{3\sqrt{1430}C_7}{256} + \frac{\sqrt{24310}C_9}{256}$ |
| 87 | T_1 | T1 | 1 | 1 | $\mathbb{Q}_{9,1}^{(h,T_1,1)}$ | $\text{Qh}(9, T1, 1, 1)$ | $\frac{21\sqrt{5}S_1}{128} + \frac{\sqrt{2310}S_3}{128} + \frac{3\sqrt{286}S_5}{128} + \frac{3\sqrt{1430}S_7}{256} + \frac{\sqrt{24310}S_9}{256}$ |
| 88 | T_1 | T1 | 1 | 2 | $\mathbb{Q}_{9,2}^{(h,T_1,1)}$ | $\text{Qh}(9, T1, 1, 2)$ | C_0 |
| 89 | T_1 | T1 | 2 | 0 | $\mathbb{Q}_{9,0}^{(h,T_1,2)}$ | $\text{Qh}(9, T1, 2, 0)$ | $\frac{\sqrt{2431}C_1}{128} + \frac{\sqrt{9282}C_3}{128} + \frac{5\sqrt{170}C_5}{128} + \frac{7\sqrt{34}C_7}{256} + \frac{3\sqrt{2}C_9}{256}$ |
| 90 | T_1 | T1 | 2 | 1 | $\mathbb{Q}_{9,1}^{(h,T_1,2)}$ | $\text{Qh}(9, T1, 2, 1)$ | $\frac{\sqrt{2431}S_1}{128} - \frac{\sqrt{9282}S_3}{128} + \frac{5\sqrt{170}S_5}{128} - \frac{7\sqrt{34}S_7}{256} + \frac{3\sqrt{2}S_9}{256}$ |
| 91 | T_1 | T1 | 2 | 2 | $\mathbb{Q}_{9,2}^{(h,T_1,2)}$ | $\text{Qh}(9, T1, 2, 2)$ | C_8 |
| 92 | T_1 | T1 | 3 | 0 | $\mathbb{Q}_{9,0}^{(h,T_1,3)}$ | $\text{Qh}(9, T1, 3, 0)$ | $\frac{\sqrt{1001}C_1}{64} - \frac{\sqrt{78}C_3}{64} - \frac{3\sqrt{70}C_5}{64} + \frac{23\sqrt{14}C_7}{128} + \frac{3\sqrt{238}C_9}{128}$ |
| 93 | T_1 | T1 | 3 | 1 | $\mathbb{Q}_{9,1}^{(h,T_1,3)}$ | $\text{Qh}(9, T1, 3, 1)$ | $\frac{\sqrt{1001}S_1}{64} + \frac{\sqrt{78}S_3}{64} - \frac{3\sqrt{70}S_5}{64} - \frac{23\sqrt{14}S_7}{128} + \frac{3\sqrt{238}S_9}{128}$ |
| 94 | T_1 | T1 | 3 | 2 | $\mathbb{Q}_{9,2}^{(h,T_1,3)}$ | $\text{Qh}(9, T1, 3, 2)$ | C_4 |
| 95 | T_2 | T2 | 1 | 0 | $\mathbb{Q}_{9,0}^{(h,T_2,1)}$ | $\text{Qh}(9, T2, 1, 0)$ | $\frac{\sqrt{858}C_1}{64} + \frac{\sqrt{91}C_3}{32} - \frac{5\sqrt{15}C_5}{32} - \frac{21\sqrt{3}C_7}{64} - \frac{\sqrt{51}C_9}{64}$ |
| 96 | T_2 | T2 | 1 | 1 | $\mathbb{Q}_{9,1}^{(h,T_2,1)}$ | $\text{Qh}(9, T2, 1, 1)$ | $-\frac{\sqrt{858}S_1}{64} + \frac{\sqrt{91}S_3}{32} + \frac{5\sqrt{15}S_5}{32} - \frac{21\sqrt{3}S_7}{64} + \frac{\sqrt{51}S_9}{64}$ |
| 97 | T_2 | T2 | 1 | 2 | $\mathbb{Q}_{9,2}^{(h,T_2,1)}$ | $\text{Qh}(9, T2, 1, 2)$ | C_6 |
| 98 | T_2 | T2 | 2 | 0 | $\mathbb{Q}_{9,0}^{(h,T_2,2)}$ | $\text{Qh}(9, T2, 2, 0)$ | $\frac{7\sqrt{22}C_1}{64} - \frac{3\sqrt{21}C_3}{32} + \frac{\sqrt{65}C_5}{32} + \frac{\sqrt{13}C_7}{64} - \frac{3\sqrt{221}C_9}{64}$ |
| 99 | T_2 | T2 | 2 | 1 | $\mathbb{Q}_{9,1}^{(h,T_2,2)}$ | $\text{Qh}(9, T2, 2, 1)$ | $-\frac{7\sqrt{22}S_1}{64} - \frac{3\sqrt{21}S_3}{32} - \frac{\sqrt{65}S_5}{32} + \frac{\sqrt{13}S_7}{64} + \frac{3\sqrt{221}S_9}{64}$ |
| 100 | T_2 | T2 | 2 | 2 | $\mathbb{Q}_{9,2}^{(h,T_2,2)}$ | $\text{Qh}(9, T2, 2, 2)$ | C_2 |

表 11 rank 10

| No. | irrep. | (tag) | mul. | comp. | harmonics | (tag) | definition |
|-----|--------|-------|------|-------|---------------------------------|---------------------------|--|
| 101 | A_1 | A1 | — | — | $\mathbb{Q}_{10}^{(h,A_1)}$ | $\text{Qh}(10, A1, ,)$ | $\frac{\sqrt{390}C_0}{48} - \frac{\sqrt{22}C_4}{8} - \frac{\sqrt{1122}C_8}{48}$ |
| 102 | A_2 | A2 | — | — | $\mathbb{Q}_{10}^{(h,A_2)}$ | $\text{Qh}(10, A2, ,)$ | $-\frac{\sqrt{85}C_{10}}{16} + \frac{\sqrt{1482}C_2}{48} + \frac{\sqrt{57}C_6}{48}$ |
| 103 | E | E | 1 | 0 | $\mathbb{Q}_{10,0}^{(h,E,1)}$ | $\text{Qh}(10, E, 1, 0)$ | $\frac{11\sqrt{420189}C_0}{8988} + \frac{\sqrt{827645}C_4}{1498} - \frac{\sqrt{146055}C_8}{8988}$ |
| 104 | E | E | 1 | 1 | $\mathbb{Q}_{10,1}^{(h,E,1)}$ | $\text{Qh}(10, E, 1, 1)$ | $\frac{\sqrt{370006}C_{10}}{749} + \frac{\sqrt{190995}C_2}{749}$ |
| 105 | E | E | 2 | 0 | $\mathbb{Q}_{10,0}^{(h,E,2)}$ | $\text{Qh}(10, E, 2, 0)$ | $\frac{3\sqrt{3213210}C_0}{11984} - \frac{83\sqrt{1498}C_4}{5992} + \frac{31\sqrt{76398}C_8}{11984}$ |
| 106 | E | E | 2 | 1 | $\mathbb{Q}_{10,1}^{(h,E,2)}$ | $\text{Qh}(10, E, 2, 1)$ | $\frac{\sqrt{1209635}C_{10}}{11984} - \frac{19\sqrt{58422}C_2}{35952} + \frac{\sqrt{2247}C_6}{48}$ |
| 107 | T_1 | T1 | 1 | 0 | $\mathbb{Q}_{10,0}^{(h,T_1,1)}$ | $\text{Qh}(10, T1, 1, 0)$ | $\frac{\sqrt{221}S_1}{32} - \frac{\sqrt{102}S_3}{32} - \frac{\sqrt{510}S_5}{32} - \frac{11\sqrt{6}S_7}{64} - \frac{\sqrt{38}S_9}{64}$ |
| 108 | T_1 | T1 | 1 | 1 | $\mathbb{Q}_{10,1}^{(h,T_1,1)}$ | $\text{Qh}(10, T1, 1, 1)$ | $-\frac{\sqrt{221}C_1}{32} - \frac{\sqrt{102}C_3}{32} + \frac{\sqrt{510}C_5}{32} - \frac{11\sqrt{6}C_7}{64} + \frac{\sqrt{38}C_9}{64}$ |
| 109 | T_1 | T1 | 1 | 2 | $\mathbb{Q}_{10,2}^{(h,T_1,1)}$ | $\text{Qh}(10, T1, 1, 2)$ | S_8 |
| 110 | T_1 | T1 | 2 | 0 | $\mathbb{Q}_{10,0}^{(h,T_1,2)}$ | $\text{Qh}(10, T1, 2, 0)$ | $\frac{\sqrt{39}S_1}{32} - \frac{11\sqrt{2}S_3}{32} + \frac{5\sqrt{10}S_5}{32} - \frac{\sqrt{34}S_7}{64} - \frac{\sqrt{1938}S_9}{64}$ |
| 111 | T_1 | T1 | 2 | 1 | $\mathbb{Q}_{10,1}^{(h,T_1,2)}$ | $\text{Qh}(10, T1, 2, 1)$ | $-\frac{\sqrt{39}C_1}{32} - \frac{11\sqrt{2}C_3}{32} - \frac{5\sqrt{10}C_5}{32} - \frac{\sqrt{34}C_7}{64} + \frac{\sqrt{1938}C_9}{64}$ |
| 112 | T_1 | T1 | 2 | 2 | $\mathbb{Q}_{10,2}^{(h,T_1,2)}$ | $\text{Qh}(10, T1, 2, 2)$ | S_4 |
| 113 | T_2 | T2 | 1 | 0 | $\mathbb{Q}_{10,0}^{(h,T_2,1)}$ | $\text{Qh}(10, T2, 1, 0)$ | $\frac{\sqrt{41990}S_1}{256} + \frac{\sqrt{4845}S_3}{128} + \frac{\sqrt{969}S_5}{128} + \frac{\sqrt{285}S_7}{256} + \frac{\sqrt{5}S_9}{256}$ |
| 114 | T_2 | T2 | 1 | 1 | $\mathbb{Q}_{10,1}^{(h,T_2,1)}$ | $\text{Qh}(10, T2, 1, 1)$ | $\frac{\sqrt{41990}C_1}{256} - \frac{\sqrt{4845}C_3}{128} + \frac{\sqrt{969}C_5}{128} - \frac{\sqrt{285}C_7}{256} + \frac{\sqrt{5}C_9}{256}$ |
| 115 | T_2 | T2 | 1 | 2 | $\mathbb{Q}_{10,2}^{(h,T_2,1)}$ | $\text{Qh}(10, T2, 1, 2)$ | S_{10} |
| 116 | T_2 | T2 | 2 | 0 | $\mathbb{Q}_{10,0}^{(h,T_2,2)}$ | $\text{Qh}(10, T2, 2, 0)$ | $\frac{9\sqrt{78}S_1}{256} - \frac{69S_3}{128} - \frac{\sqrt{5}S_5}{128} + \frac{43\sqrt{17}S_7}{256} + \frac{3\sqrt{969}S_9}{256}$ |
| 117 | T_2 | T2 | 2 | 1 | $\mathbb{Q}_{10,1}^{(h,T_2,2)}$ | $\text{Qh}(10, T2, 2, 1)$ | $\frac{9\sqrt{78}C_1}{256} + \frac{69C_3}{128} - \frac{\sqrt{5}C_5}{128} - \frac{43\sqrt{17}C_7}{256} + \frac{3\sqrt{969}C_9}{256}$ |
| 118 | T_2 | T2 | 2 | 2 | $\mathbb{Q}_{10,2}^{(h,T_2,2)}$ | $\text{Qh}(10, T2, 2, 2)$ | S_6 |
| 119 | T_2 | T2 | 3 | 0 | $\mathbb{Q}_{10,0}^{(h,T_2,3)}$ | $\text{Qh}(10, T2, 3, 0)$ | $\frac{7\sqrt{3}S_1}{128} - \frac{7\sqrt{26}S_3}{128} + \frac{5\sqrt{130}S_5}{128} - \frac{7\sqrt{442}S_7}{256} + \frac{\sqrt{25194}S_9}{256}$ |
| 120 | T_2 | T2 | 3 | 1 | $\mathbb{Q}_{10,1}^{(h,T_2,3)}$ | $\text{Qh}(10, T2, 3, 1)$ | $\frac{7\sqrt{3}C_1}{128} + \frac{7\sqrt{26}C_3}{128} + \frac{5\sqrt{130}C_5}{128} - \frac{7\sqrt{442}C_7}{256} + \frac{\sqrt{25194}C_9}{256}$ |
| 121 | T_2 | T2 | 3 | 2 | $\mathbb{Q}_{10,2}^{(h,T_2,3)}$ | $\text{Qh}(10, T2, 3, 2)$ | S_2 |

表 12 rank 11

| No. | irrep. | (tag) | mul. | comp. | harmonics | (tag) | definition |
|-----|--------|-------|------|-------|------------------------|------------------|---|
| 122 | A_2 | A2 | — | — | $Q_{11}^{(h,A_2)}$ | Qh(11, A2, ,) | $\frac{\sqrt{798}S_{10}}{48} + \frac{\sqrt{255}S_2}{24} + \frac{3\sqrt{6}S_6}{16}$ |
| 123 | E | E | 1 | 0 | $Q_{11,0}^{(h,E,1)}$ | Qh(11, E, 1, 0) | S_8 |
| 124 | E | E | 1 | 1 | $Q_{11,1}^{(h,E,1)}$ | Qh(11, E, 1, 1) | $-\frac{\sqrt{210}S_{10}}{96} + \frac{\sqrt{969}S_2}{48} - \frac{\sqrt{570}S_6}{32}$ |
| 125 | E | E | 2 | 0 | $Q_{11,0}^{(h,E,2)}$ | Qh(11, E, 2, 0) | S_4 |
| 126 | E | E | 2 | 1 | $Q_{11,1}^{(h,E,2)}$ | Qh(11, E, 2, 1) | $-\frac{\sqrt{646}S_{10}}{32} + \frac{\sqrt{35}S_2}{16} + \frac{\sqrt{238}S_6}{32}$ |
| 127 | T_1 | T1 | 1 | 0 | $Q_{11,0}^{(h,T_1,1)}$ | Qh(11, T1, 1, 0) | $-\frac{21\sqrt{66}C_1}{512} + \frac{\sqrt{88179}C_{11}}{512} + \frac{\sqrt{30030}C_3}{512} - \frac{15\sqrt{143}C_5}{512} + \frac{\sqrt{36465}C_7}{512} - \frac{\sqrt{46189}C_9}{512}$ |
| 128 | T_1 | T1 | 1 | 1 | $Q_{11,1}^{(h,T_1,1)}$ | Qh(11, T1, 1, 1) | $-\frac{21\sqrt{66}S_1}{512} - \frac{\sqrt{88179}S_{11}}{512} - \frac{\sqrt{30030}S_3}{512} - \frac{15\sqrt{143}S_5}{512} - \frac{\sqrt{36465}S_7}{512} - \frac{\sqrt{46189}S_9}{512}$ |
| 129 | T_1 | T1 | 1 | 2 | $Q_{11,2}^{(h,T_1,1)}$ | Qh(11, T1, 1, 2) | C_0 |
| 130 | T_1 | T1 | 2 | 0 | $Q_{11,0}^{(h,T_1,2)}$ | Qh(11, T1, 2, 0) | $-\frac{\sqrt{41990}C_1}{512} + \frac{\sqrt{385}C_{11}}{512} - \frac{3\sqrt{4522}C_3}{512} + \frac{3\sqrt{4845}C_5}{512} + \frac{77\sqrt{19}C_7}{512} + \frac{39\sqrt{15}C_9}{512}$ |
| 131 | T_1 | T1 | 2 | 1 | $Q_{11,1}^{(h,T_1,2)}$ | Qh(11, T1, 2, 1) | $-\frac{\sqrt{41990}S_1}{512} - \frac{\sqrt{385}S_{11}}{512} + \frac{3\sqrt{4522}S_3}{512} + \frac{3\sqrt{4845}S_5}{512} - \frac{77\sqrt{19}S_7}{512} + \frac{39\sqrt{15}S_9}{512}$ |
| 132 | T_1 | T1 | 2 | 2 | $Q_{11,2}^{(h,T_1,2)}$ | Qh(11, T1, 2, 2) | C_8 |
| 133 | T_1 | T1 | 3 | 0 | $Q_{11,0}^{(h,T_1,3)}$ | Qh(11, T1, 3, 0) | $-\frac{5\sqrt{546}C_1}{256} + \frac{\sqrt{10659}C_{11}}{256} + \frac{11\sqrt{30}C_3}{256} + \frac{13\sqrt{7}C_5}{256} - \frac{3\sqrt{1785}C_7}{256} + \frac{3\sqrt{2261}C_9}{256}$ |
| 134 | T_1 | T1 | 3 | 1 | $Q_{11,1}^{(h,T_1,3)}$ | Qh(11, T1, 3, 1) | $-\frac{5\sqrt{546}S_1}{256} - \frac{\sqrt{10659}S_{11}}{256} - \frac{11\sqrt{30}S_3}{256} + \frac{13\sqrt{7}S_5}{256} + \frac{3\sqrt{1785}S_7}{256} + \frac{3\sqrt{2261}S_9}{256}$ |
| 135 | T_1 | T1 | 3 | 2 | $Q_{11,2}^{(h,T_1,3)}$ | Qh(11, T1, 3, 2) | C_4 |
| 136 | T_2 | T2 | 1 | 0 | $Q_{11,0}^{(h,T_2,1)}$ | Qh(11, T2, 1, 0) | $-\frac{\sqrt{29393}C_1}{512} - \frac{\sqrt{22}C_{11}}{1024} - \frac{9\sqrt{1615}C_3}{512} - \frac{5\sqrt{13566}C_5}{1024} - \frac{7\sqrt{1330}C_7}{1024} - \frac{9\sqrt{42}C_9}{1024}$ |
| 137 | T_2 | T2 | 1 | 1 | $Q_{11,1}^{(h,T_2,1)}$ | Qh(11, T2, 1, 1) | $\frac{\sqrt{29393}S_1}{512} - \frac{\sqrt{22}S_{11}}{1024} - \frac{9\sqrt{1615}S_3}{512} + \frac{5\sqrt{13566}S_5}{1024} - \frac{7\sqrt{1330}S_7}{1024} + \frac{9\sqrt{42}S_9}{1024}$ |
| 138 | T_2 | T2 | 1 | 2 | $Q_{11,2}^{(h,T_2,1)}$ | Qh(11, T2, 1, 2) | C_{10} |
| 139 | T_2 | T2 | 2 | 0 | $Q_{11,0}^{(h,T_2,2)}$ | Qh(11, T2, 2, 0) | $-\frac{15\sqrt{221}C_1}{512} - \frac{3\sqrt{2926}C_{11}}{1024} - \frac{\sqrt{595}C_3}{512} + \frac{53\sqrt{102}C_5}{1024} - \frac{105\sqrt{10}C_7}{1024} - \frac{61\sqrt{114}C_9}{1024}$ |
| 140 | T_2 | T2 | 2 | 1 | $Q_{11,1}^{(h,T_2,2)}$ | Qh(11, T2, 2, 1) | $\frac{15\sqrt{221}S_1}{512} - \frac{3\sqrt{2926}S_{11}}{1024} - \frac{\sqrt{595}S_3}{512} - \frac{53\sqrt{102}S_5}{1024} - \frac{105\sqrt{10}S_7}{1024} + \frac{61\sqrt{114}S_9}{1024}$ |
| 141 | T_2 | T2 | 2 | 2 | $Q_{11,2}^{(h,T_2,2)}$ | Qh(11, T2, 2, 2) | C_6 |
| 142 | T_2 | T2 | 3 | 0 | $Q_{11,0}^{(h,T_2,3)}$ | Qh(11, T2, 3, 0) | $-\frac{21\sqrt{130}C_1}{512} - \frac{\sqrt{124355}C_{11}}{512} + \frac{57\sqrt{14}C_3}{512} - \frac{41\sqrt{15}C_5}{512} + \frac{17\sqrt{17}C_7}{512} + \frac{\sqrt{4845}C_9}{512}$ |
| 143 | T_2 | T2 | 3 | 1 | $Q_{11,1}^{(h,T_2,3)}$ | Qh(11, T2, 3, 1) | $\frac{21\sqrt{130}S_1}{512} - \frac{\sqrt{124355}S_{11}}{512} + \frac{57\sqrt{14}S_3}{512} + \frac{41\sqrt{15}S_5}{512} + \frac{17\sqrt{17}S_7}{512} - \frac{\sqrt{4845}S_9}{512}$ |
| 144 | T_2 | T2 | 3 | 2 | $Q_{11,2}^{(h,T_2,3)}$ | Qh(11, T2, 3, 2) | C_2 |