

\* symmetry operation

Table 1: Symmetry operations for 3d polar vector.

| No. | tag   | matrix (polar)  | det | TR |
|-----|---|---|-----|----|
| 1   | {1 0}   | $\begin{bmatrix} 1 & 0 & 0 & 0 \\ 0 & 1 & 0 & 0 \\ 0 & 0 & 1 & 0 \end{bmatrix}$                                 | 1   | 1  |
| 2   | {2 <sub>100</sub>  0}   | $\begin{bmatrix} 1 & 0 & 0 & 0 \\ 0 & -1 & 0 & 0 \\ 0 & 0 & -1 & 0 \end{bmatrix}$                               | 1   | 1  |
| 3   | {2 <sub>010</sub>  00 <sub>2</sub> <sup>1</sup> }   | $\begin{bmatrix} -1 & 0 & 0 & 0 \\ 0 & 1 & 0 & 0 \\ 0 & 0 & -1 & \frac{1}{2} \end{bmatrix}$                     | 1   | 1  |
| 4   | {2 <sub>001</sub>  00 <sub>2</sub> <sup>1</sup> }   | $\begin{bmatrix} -1 & 0 & 0 & 0 \\ 0 & -1 & 0 & 0 \\ 0 & 0 & 1 & \frac{1}{2} \end{bmatrix}$                     | 1   | 1  |
| 5   | {-1' 0}   | $\begin{bmatrix} -1 & 0 & 0 & 0 \\ 0 & -1 & 0 & 0 \\ 0 & 0 & -1 & 0 \end{bmatrix}$                              | -1  | -1 |
| 6   | {m <sub>100</sub> ' 0}  | $\begin{bmatrix} -1 & 0 & 0 & 0 \\ 0 & 1 & 0 & 0 \\ 0 & 0 & 1 & 0 \end{bmatrix}$                                | -1  | -1 |
| 7   | {m <sub>010</sub> ' 00 <sub>2</sub> <sup>1</sup> }  | $\begin{bmatrix} 1 & 0 & 0 & 0 \\ 0 & -1 & 0 & 0 \\ 0 & 0 & 1 & \frac{1}{2} \end{bmatrix}$                      | -1  | -1 |
| 8   | {m <sub>001</sub> ' 00 <sub>2</sub> <sup>1</sup> }  | $\begin{bmatrix} 1 & 0 & 0 & 0 \\ 0 & 1 & 0 & 0 \\ 0 & 0 & -1 & \frac{1}{2} \end{bmatrix}$                      | -1  | -1 |
| 9   | {1  <sub>2</sub> <sup>1</sup> <sub>2</sub> <sup>1</sup> 0}  | $\begin{bmatrix} 1 & 0 & 0 & \frac{1}{2} \\ 0 & 1 & 0 & \frac{1}{2} \\ 0 & 0 & 1 & 0 \end{bmatrix}$             | 1   | 1  |
| 10  | {2 <sub>100</sub>   <sub>2</sub> <sup>1</sup> <sub>2</sub> <sup>1</sup> 0}                          | $\begin{bmatrix} 1 & 0 & 0 & \frac{1}{2} \\ 0 & -1 & 0 & \frac{1}{2} \\ 0 & 0 & -1 & 0 \end{bmatrix}$           | 1   | 1  |
| 11  | {2 <sub>010</sub>   <sub>2</sub> <sup>1</sup> <sub>2</sub> <sup>1</sup> <sub>2</sub> <sup>1</sup> } | $\begin{bmatrix} -1 & 0 & 0 & \frac{1}{2} \\ 0 & 1 & 0 & \frac{1}{2} \\ 0 & 0 & -1 & \frac{1}{2} \end{bmatrix}$ | 1   | 1  |
| 12  | {2 <sub>001</sub>   <sub>2</sub> <sup>1</sup> <sub>2</sub> <sup>1</sup> <sub>2</sub> <sup>1</sup> } | $\begin{bmatrix} -1 & 0 & 0 & \frac{1}{2} \\ 0 & -1 & 0 & \frac{1}{2} \\ 0 & 0 & 1 & \frac{1}{2} \end{bmatrix}$ | 1   | 1  |
| 13  | {-1'  <sub>2</sub> <sup>1</sup> <sub>2</sub> <sup>1</sup> 0}  | $\begin{bmatrix} -1 & 0 & 0 & \frac{1}{2} \\ 0 & -1 & 0 & \frac{1}{2} \\ 0 & 0 & -1 & 0 \end{bmatrix}$          | -1  | -1 |

continued ...

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| No. | tag  | matrix (polar)   | det | TR |
|-----|--|--|-----|----|
| 14  | $\{m_{100}'   \frac{1}{2} \frac{1}{2} 0\}$           | $\begin{bmatrix} -1 & 0 & 0 & \frac{1}{2} \\ 0 & 1 & 0 & \frac{1}{2} \\ 0 & 0 & 1 & 0 \end{bmatrix}$           | -1  | -1 |
| 15  | $\{m_{010}'   \frac{1}{2} \frac{1}{2} \frac{1}{2}\}$ | $\begin{bmatrix} 1 & 0 & 0 & \frac{1}{2} \\ 0 & -1 & 0 & \frac{1}{2} \\ 0 & 0 & 1 & \frac{1}{2} \end{bmatrix}$ | -1  | -1 |
| 16  | $\{m_{001}'   \frac{1}{2} \frac{1}{2} \frac{1}{2}\}$ | $\begin{bmatrix} 1 & 0 & 0 & \frac{1}{2} \\ 0 & 1 & 0 & \frac{1}{2} \\ 0 & 0 & -1 & \frac{1}{2} \end{bmatrix}$ | -1  | -1 |