

SAMB for “UPt2Si2”

Generated on 2023-06-01 18:04 by MultiPie 1.1.2

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- Group: No. 129 D_{4h}^7 $P4/nmm$ [tetragonal]
 - Associated point group: No. 15 D_{4h} $4/mmm$ [tetragonal]
 - Generation condition
 - model type: **tight_binding**
 - time-reversal type: **electric**
 - irrep: **[A1g]**
 - **spinless**
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- Unit cell:
 - $a = 4.1972$, $b = 4.1972$, $c = 9.6906$, $\alpha = 90.0$, $\beta = 90.0$, $\gamma = 90.0$
- Lattice vectors:
 - $\mathbf{a}_1 = (4.1972 \ 0 \ 0)$
 - $\mathbf{a}_2 = (0 \ 4.1972 \ 0)$
 - $\mathbf{a}_3 = (0 \ 0 \ 9.6906)$

Table 1: High-symmetry line: Γ -X.

| | symbol | position | | symbol | position |
|--|----------|---|--|--------|---|
| | Γ | $\begin{pmatrix} 0 & 0 & 0 \end{pmatrix}$ | | X | $\begin{pmatrix} \frac{1}{2} & 0 & 0 \end{pmatrix}$ |

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- Kets: dimension = 46

Table 2: Hilbert space for full matrix.

| No. | ket | No. | ket | No. | ket | No. | ket | No. | ket |
|-----|---------------|-----|----------------|-----|----------------|-----|----------------|-----|--------------|
| 1 | $f_{xyz}@U_1$ | 2 | $f_{ax}@U_1$ | 3 | $f_{ay}@U_1$ | 4 | $f_{az}@U_1$ | 5 | $f_{bx}@U_1$ |
| 6 | $f_{by}@U_1$ | 7 | $f_{bz}@U_1$ | 8 | $f_{xyz}@U_2$ | 9 | $f_{ax}@U_2$ | 10 | $f_{ay}@U_2$ |
| 11 | $f_{az}@U_2$ | 12 | $f_{bx}@U_2$ | 13 | $f_{by}@U_2$ | 14 | $f_{bz}@U_2$ | 15 | $d_u@Pt1_1$ |
| 16 | $d_v@Pt1_1$ | 17 | $d_{yz}@Pt1_1$ | 18 | $d_{zx}@Pt1_1$ | 19 | $d_{xy}@Pt1_1$ | 20 | $d_u@Pt1_2$ |
| 21 | $d_v@Pt1_2$ | 22 | $d_{yz}@Pt1_2$ | 23 | $d_{zx}@Pt1_2$ | 24 | $d_{xy}@Pt1_2$ | 25 | $d_u@Pt2_1$ |
| 26 | $d_v@Pt2_1$ | 27 | $d_{yz}@Pt2_1$ | 28 | $d_{zx}@Pt2_1$ | 29 | $d_{xy}@Pt2_1$ | 30 | $d_u@Pt2_2$ |
| 31 | $d_v@Pt2_2$ | 32 | $d_{yz}@Pt2_2$ | 33 | $d_{zx}@Pt2_2$ | 34 | $d_{xy}@Pt2_2$ | 35 | $p_x@Si1_1$ |
| 36 | $p_y@Si1_1$ | 37 | $p_z@Si1_1$ | 38 | $p_x@Si1_2$ | 39 | $p_y@Si1_2$ | 40 | $p_z@Si1_2$ |
| 41 | $p_x@Si2_1$ | 42 | $p_y@Si2_1$ | 43 | $p_z@Si2_1$ | 44 | $p_x@Si2_2$ | 45 | $p_y@Si2_2$ |
| 46 | $p_z@Si2_2$ | | | | | | | | |

- Sites in (primitive) unit cell:

Table 3: Site-clusters.

| site | position | mapping |
|---------------------------------|---|-----------------------|
| S ₁ U ₁ | $\begin{pmatrix} \frac{1}{4} & \frac{1}{4} & 0.7484 \end{pmatrix}$ | [1,2,7,8,11,12,13,14] |
| U ₂ | $\begin{pmatrix} \frac{3}{4} & \frac{3}{4} & 0.2516 \end{pmatrix}$ | [3,4,5,6,9,10,15,16] |
| S ₂ Pt1 ₁ | $\begin{pmatrix} \frac{3}{4} & \frac{1}{4} & 0 \end{pmatrix}$ | [1,2,5,6,11,12,15,16] |
| Pt1 ₂ | $\begin{pmatrix} \frac{1}{4} & \frac{3}{4} & 0 \end{pmatrix}$ | [3,4,7,8,9,10,13,14] |
| S ₃ Pt2 ₁ | $\begin{pmatrix} \frac{1}{4} & \frac{1}{4} & 0.3785 \end{pmatrix}$ | [1,2,7,8,11,12,13,14] |
| Pt2 ₂ | $\begin{pmatrix} \frac{3}{4} & \frac{3}{4} & 0.6215 \end{pmatrix}$ | [3,4,5,6,9,10,15,16] |
| S ₄ Si1 ₁ | $\begin{pmatrix} \frac{3}{4} & \frac{1}{4} & \frac{1}{2} \end{pmatrix}$ | [1,2,5,6,11,12,15,16] |
| Si1 ₂ | $\begin{pmatrix} \frac{1}{4} & \frac{3}{4} & \frac{1}{2} \end{pmatrix}$ | [3,4,7,8,9,10,13,14] |
| S ₅ Si2 ₁ | $\begin{pmatrix} \frac{1}{4} & \frac{1}{4} & 0.133 \end{pmatrix}$ | [1,2,7,8,11,12,13,14] |
| Si2 ₂ | $\begin{pmatrix} \frac{3}{4} & \frac{3}{4} & 0.867 \end{pmatrix}$ | [3,4,5,6,9,10,15,16] |

- Bonds in (primitive) unit cell:

Table 4: Bond-clusters.

| | bond | tail | head | n | # | $\mathbf{b@c}$ | mapping |
|----------------|-----------------|------------------|------------------|-----|---|--|---------|
| B ₁ | b ₁ | Pt1 ₁ | Si2 ₁ | 1 | 1 | $\begin{pmatrix} \frac{1}{2} & 0 & 0.133 \end{pmatrix} @ \begin{pmatrix} 0 & \frac{1}{4} & 0.0665 \end{pmatrix}$ | [1,12] |
| | b ₂ | Pt1 ₁ | Si2 ₁ | 1 | 1 | $\begin{pmatrix} -\frac{1}{2} & 0 & 0.133 \end{pmatrix} @ \begin{pmatrix} \frac{1}{2} & \frac{1}{4} & 0.0665 \end{pmatrix}$ | [2,11] |
| | b ₃ | Pt1 ₂ | Si2 ₂ | 1 | 1 | $\begin{pmatrix} \frac{1}{2} & 0 & -0.133 \end{pmatrix} @ \begin{pmatrix} \frac{1}{2} & \frac{3}{4} & 0.9335 \end{pmatrix}$ | [3,10] |
| | b ₄ | Pt1 ₂ | Si2 ₂ | 1 | 1 | $\begin{pmatrix} -\frac{1}{2} & 0 & -0.133 \end{pmatrix} @ \begin{pmatrix} 0 & \frac{3}{4} & 0.9335 \end{pmatrix}$ | [4,9] |
| | b ₅ | Pt1 ₁ | Si2 ₂ | 1 | 1 | $\begin{pmatrix} 0 & \frac{1}{2} & -0.133 \end{pmatrix} @ \begin{pmatrix} \frac{3}{4} & \frac{1}{2} & 0.9335 \end{pmatrix}$ | [5,16] |
| | b ₆ | Pt1 ₁ | Si2 ₂ | 1 | 1 | $\begin{pmatrix} 0 & -\frac{1}{2} & -0.133 \end{pmatrix} @ \begin{pmatrix} \frac{3}{4} & 0 & 0.9335 \end{pmatrix}$ | [6,15] |
| | b ₇ | Pt1 ₂ | Si2 ₁ | 1 | 1 | $\begin{pmatrix} 0 & \frac{1}{2} & 0.133 \end{pmatrix} @ \begin{pmatrix} \frac{1}{4} & 0 & 0.0665 \end{pmatrix}$ | [7,14] |
| | b ₈ | Pt1 ₂ | Si2 ₁ | 1 | 1 | $\begin{pmatrix} 0 & -\frac{1}{2} & 0.133 \end{pmatrix} @ \begin{pmatrix} \frac{1}{4} & \frac{1}{2} & 0.0665 \end{pmatrix}$ | [8,13] |
| B ₂ | b ₉ | Pt2 ₁ | Si1 ₁ | 1 | 1 | $\begin{pmatrix} -\frac{1}{2} & 0 & 0.1215 \end{pmatrix} @ \begin{pmatrix} 0 & \frac{1}{4} & 0.43925 \end{pmatrix}$ | [1,12] |
| | b ₁₀ | Pt2 ₁ | Si1 ₁ | 1 | 1 | $\begin{pmatrix} \frac{1}{2} & 0 & 0.1215 \end{pmatrix} @ \begin{pmatrix} \frac{1}{2} & \frac{1}{4} & 0.43925 \end{pmatrix}$ | [2,11] |
| | b ₁₁ | Pt2 ₂ | Si1 ₂ | 1 | 1 | $\begin{pmatrix} -\frac{1}{2} & 0 & -0.1215 \end{pmatrix} @ \begin{pmatrix} \frac{1}{2} & \frac{3}{4} & 0.56075 \end{pmatrix}$ | [3,10] |
| | b ₁₂ | Pt2 ₂ | Si1 ₂ | 1 | 1 | $\begin{pmatrix} \frac{1}{2} & 0 & -0.1215 \end{pmatrix} @ \begin{pmatrix} 0 & \frac{3}{4} & 0.56075 \end{pmatrix}$ | [4,9] |
| | b ₁₃ | Pt2 ₂ | Si1 ₁ | 1 | 1 | $\begin{pmatrix} 0 & -\frac{1}{2} & -0.1215 \end{pmatrix} @ \begin{pmatrix} \frac{3}{4} & \frac{1}{2} & 0.56075 \end{pmatrix}$ | [5,16] |
| | b ₁₄ | Pt2 ₂ | Si1 ₁ | 1 | 1 | $\begin{pmatrix} 0 & \frac{1}{2} & -0.1215 \end{pmatrix} @ \begin{pmatrix} \frac{3}{4} & 0 & 0.56075 \end{pmatrix}$ | [6,15] |
| | b ₁₅ | Pt2 ₁ | Si1 ₂ | 1 | 1 | $\begin{pmatrix} 0 & -\frac{1}{2} & 0.1215 \end{pmatrix} @ \begin{pmatrix} \frac{1}{4} & 0 & 0.43925 \end{pmatrix}$ | [7,14] |
| | b ₁₆ | Pt2 ₁ | Si1 ₂ | 1 | 1 | $\begin{pmatrix} 0 & \frac{1}{2} & 0.1215 \end{pmatrix} @ \begin{pmatrix} \frac{1}{4} & \frac{1}{2} & 0.43925 \end{pmatrix}$ | [8,13] |

- SAMB:

$$\boxed{\text{No. 1}} \quad \hat{\mathbb{Q}}_0^{(A_{1g})} [\mathbf{M}_1, \mathbf{S}_1]$$

$$\hat{\mathbb{Z}}_1 = \mathbb{X}_1[\mathbb{Q}_0^{(a, A_{1g})}] \otimes \mathbb{Y}_1[\mathbb{Q}_0^{(s, A_{1g})}]$$

$$\hat{\mathbb{Z}}_1(\mathbf{k}) = \mathbb{X}_1[\mathbb{Q}_0^{(a, A_{1g})}] \otimes \mathbb{U}_1[\mathbb{Q}_0^{(s, A_{1g})}]$$

$$\boxed{\text{No. 2}} \quad \hat{\mathbb{Q}}_2^{(A_{1g})} [\mathbf{M}_1, \mathbf{S}_1]$$

$$\hat{\mathbb{Z}}_2 = \mathbb{X}_2[\mathbb{Q}_2^{(a, A_{1g})}] \otimes \mathbb{Y}_1[\mathbb{Q}_0^{(s, A_{1g})}]$$

$$\hat{\mathbb{Z}}_2(\mathbf{k}) = \mathbb{X}_2[\mathbb{Q}_2^{(a, A_{1g})}] \otimes \mathbb{U}_1[\mathbb{Q}_0^{(s, A_{1g})}]$$

$$\boxed{\text{No. 3}} \quad \hat{\mathbb{Q}}_4^{(A_{1g}, 1)} [\mathbf{M}_1, \mathbf{S}_1]$$

$$\hat{\mathbb{Z}}_3 = \mathbb{X}_3[\mathbb{Q}_4^{(a, A_{1g}, 1)}] \otimes \mathbb{Y}_1[\mathbb{Q}_0^{(s, A_{1g})}]$$

$$\hat{\mathbb{Z}}_3(\mathbf{k}) = \mathbb{X}_3[\mathbb{Q}_4^{(a, A_{1g}, 1)}] \otimes \mathbb{U}_1[\mathbb{Q}_0^{(s, A_{1g})}]$$

$$\boxed{\text{No. 4}} \quad \hat{\mathbb{Q}}_4^{(A_{1g}, 2)} [\mathbf{M}_1, \mathbf{S}_1]$$

$$\hat{\mathbb{Z}}_4 = \mathbb{X}_4[\mathbb{Q}_4^{(a, A_{1g}, 2)}] \otimes \mathbb{Y}_1[\mathbb{Q}_0^{(s, A_{1g})}]$$

$$\hat{\mathbb{Z}}_4(\mathbf{k}) = \mathbb{X}_4[\mathbb{Q}_4^{(a, A_{1g}, 2)}] \otimes \mathbb{U}_1[\mathbb{Q}_0^{(s, A_{1g})}]$$

$$\boxed{\text{No. 5}} \quad \hat{\mathbb{Q}}_6^{(A_{1g}, 1)} [\mathbf{M}_1, \mathbf{S}_1]$$

$$\hat{\mathbb{Z}}_5 = \mathbb{X}_5[\mathbb{Q}_6^{(a, A_{1g}, 1)}] \otimes \mathbb{Y}_1[\mathbb{Q}_0^{(s, A_{1g})}]$$

$$\hat{\mathbb{Z}}_5(\mathbf{k}) = \mathbb{X}_5[\mathbb{Q}_6^{(a, A_{1g}, 1)}] \otimes \mathbb{U}_1[\mathbb{Q}_0^{(s, A_{1g})}]$$

$$\boxed{\text{No. 6}} \quad \hat{\mathbb{Q}}_6^{(A_{1g}, 2)} [\mathbf{M}_1, \mathbf{S}_1]$$

$$\hat{\mathbb{Z}}_6 = \mathbb{X}_6[\mathbb{Q}_6^{(a, A_{1g}, 2)}] \otimes \mathbb{Y}_1[\mathbb{Q}_0^{(s, A_{1g})}]$$

$$\hat{\mathbb{Z}}_6(\mathbf{k}) = \mathbb{X}_6[\mathbb{Q}_6^{(a, A_{1g}, 2)}] \otimes \mathbb{U}_1[\mathbb{Q}_0^{(s, A_{1g})}]$$

$$\boxed{\text{No. 7}} \quad \hat{\mathbb{Q}}_0^{(A_{1g})} [\mathbf{M}_2, \mathbf{S}_2]$$

$$\hat{\mathbb{Z}}_7 = \mathbb{X}_7[\mathbb{Q}_0^{(a, A_{1g})}] \otimes \mathbb{Y}_2[\mathbb{Q}_0^{(s, A_{1g})}]$$

$$\hat{\mathbb{Z}}_7(\mathbf{k}) = \mathbb{X}_7[\mathbb{Q}_0^{(a, A_{1g})}] \otimes \mathbb{U}_2[\mathbb{Q}_0^{(s, A_{1g})}]$$

$$\boxed{\text{No. 8}} \quad \hat{\mathbb{Q}}_2^{(A_{1g})} [\text{M}_2, \text{S}_2]$$

$$\hat{\mathbb{Z}}_8 = \mathbb{X}_8[\mathbb{Q}_2^{(a, A_{1g})}] \otimes \mathbb{Y}_2[\mathbb{Q}_0^{(s, A_{1g})}]$$

$$\hat{\mathbb{Z}}_8(\mathbf{k}) = \mathbb{X}_8[\mathbb{Q}_2^{(a, A_{1g})}] \otimes \mathbb{U}_2[\mathbb{Q}_0^{(s, A_{1g})}]$$

$$\boxed{\text{No. 9}} \quad \hat{\mathbb{Q}}_4^{(A_{1g}, 1)} [\text{M}_2, \text{S}_2]$$

$$\hat{\mathbb{Z}}_9 = \mathbb{X}_9[\mathbb{Q}_4^{(a, A_{1g}, 1)}] \otimes \mathbb{Y}_2[\mathbb{Q}_0^{(s, A_{1g})}]$$

$$\hat{\mathbb{Z}}_9(\mathbf{k}) = \mathbb{X}_9[\mathbb{Q}_4^{(a, A_{1g}, 1)}] \otimes \mathbb{U}_2[\mathbb{Q}_0^{(s, A_{1g})}]$$

$$\boxed{\text{No. 10}} \quad \hat{\mathbb{Q}}_4^{(A_{1g}, 2)} [\text{M}_2, \text{S}_2]$$

$$\hat{\mathbb{Z}}_{10} = \mathbb{X}_{10}[\mathbb{Q}_4^{(a, A_{1g}, 2)}] \otimes \mathbb{Y}_2[\mathbb{Q}_0^{(s, A_{1g})}]$$

$$\hat{\mathbb{Z}}_{10}(\mathbf{k}) = \mathbb{X}_{10}[\mathbb{Q}_4^{(a, A_{1g}, 2)}] \otimes \mathbb{U}_2[\mathbb{Q}_0^{(s, A_{1g})}]$$

$$\boxed{\text{No. 11}} \quad \hat{\mathbb{Q}}_0^{(A_{1g})} [\text{M}_2, \text{S}_3]$$

$$\hat{\mathbb{Z}}_{11} = \mathbb{X}_7[\mathbb{Q}_0^{(a, A_{1g})}] \otimes \mathbb{Y}_3[\mathbb{Q}_0^{(s, A_{1g})}]$$

$$\hat{\mathbb{Z}}_{11}(\mathbf{k}) = \mathbb{X}_7[\mathbb{Q}_0^{(a, A_{1g})}] \otimes \mathbb{U}_3[\mathbb{Q}_0^{(s, A_{1g})}]$$

$$\boxed{\text{No. 12}} \quad \hat{\mathbb{Q}}_2^{(A_{1g})} [\text{M}_2, \text{S}_3]$$

$$\hat{\mathbb{Z}}_{12} = \mathbb{X}_8[\mathbb{Q}_2^{(a, A_{1g})}] \otimes \mathbb{Y}_3[\mathbb{Q}_0^{(s, A_{1g})}]$$

$$\hat{\mathbb{Z}}_{12}(\mathbf{k}) = \mathbb{X}_8[\mathbb{Q}_2^{(a, A_{1g})}] \otimes \mathbb{U}_3[\mathbb{Q}_0^{(s, A_{1g})}]$$

$$\boxed{\text{No. 13}} \quad \hat{\mathbb{Q}}_4^{(A_{1g}, 1)} [\text{M}_2, \text{S}_3]$$

$$\hat{\mathbb{Z}}_{13} = \mathbb{X}_9[\mathbb{Q}_4^{(a, A_{1g}, 1)}] \otimes \mathbb{Y}_3[\mathbb{Q}_0^{(s, A_{1g})}]$$

$$\hat{\mathbb{Z}}_{13}(\mathbf{k}) = \mathbb{X}_9[\mathbb{Q}_4^{(a, A_{1g}, 1)}] \otimes \mathbb{U}_3[\mathbb{Q}_0^{(s, A_{1g})}]$$

$$\boxed{\text{No. 14}} \quad \hat{\mathbb{Q}}_4^{(A_{1g}, 2)} [\text{M}_2, \text{S}_3]$$

$$\hat{\mathbb{Z}}_{14} = \mathbb{X}_{10}[\mathbb{Q}_4^{(a, A_{1g}, 2)}] \otimes \mathbb{Y}_3[\mathbb{Q}_0^{(s, A_{1g})}]$$

$$\hat{\mathbb{Z}}_{14}(\mathbf{k}) = \mathbb{X}_{10}[\mathbb{Q}_4^{(a, A_{1g}, 2)}] \otimes \mathbb{U}_3[\mathbb{Q}_0^{(s, A_{1g})}]$$

$$\boxed{\text{No. 15}} \quad \hat{\mathbb{Q}}_0^{(A_{1g})} [\text{M}_3, \text{S}_4]$$

$$\hat{\mathbb{Z}}_{15} = \mathbb{X}_{11}[\mathbb{Q}_0^{(a, A_{1g})}] \otimes \mathbb{Y}_4[\mathbb{Q}_0^{(s, A_{1g})}]$$

$$\hat{\mathbb{Z}}_{15}(\mathbf{k}) = \mathbb{X}_{11}[\mathbb{Q}_0^{(a, A_{1g})}] \otimes \mathbb{U}_4[\mathbb{Q}_0^{(s, A_{1g})}]$$

$$\boxed{\text{No. 16}} \quad \hat{\mathbb{Q}}_2^{(A_{1g})} [\text{M}_3, \text{S}_4]$$

$$\hat{\mathbb{Z}}_{16} = \mathbb{X}_{12}[\mathbb{Q}_2^{(a, A_{1g})}] \otimes \mathbb{Y}_4[\mathbb{Q}_0^{(s, A_{1g})}]$$

$$\hat{\mathbb{Z}}_{16}(\mathbf{k}) = \mathbb{X}_{12}[\mathbb{Q}_2^{(a, A_{1g})}] \otimes \mathbb{U}_4[\mathbb{Q}_0^{(s, A_{1g})}]$$

$$\boxed{\text{No. 17}} \quad \hat{\mathbb{Q}}_0^{(A_{1g})} [\text{M}_3, \text{S}_5]$$

$$\hat{\mathbb{Z}}_{17} = \mathbb{X}_{11}[\mathbb{Q}_0^{(a, A_{1g})}] \otimes \mathbb{Y}_5[\mathbb{Q}_0^{(s, A_{1g})}]$$

$$\hat{\mathbb{Z}}_{17}(\mathbf{k}) = \mathbb{X}_{11}[\mathbb{Q}_0^{(a, A_{1g})}] \otimes \mathbb{U}_5[\mathbb{Q}_0^{(s, A_{1g})}]$$

$$\boxed{\text{No. 18}} \quad \hat{\mathbb{Q}}_2^{(A_{1g})} [\text{M}_3, \text{S}_5]$$

$$\hat{\mathbb{Z}}_{18} = \mathbb{X}_{12}[\mathbb{Q}_2^{(a, A_{1g})}] \otimes \mathbb{Y}_5[\mathbb{Q}_0^{(s, A_{1g})}]$$

$$\hat{\mathbb{Z}}_{18}(\mathbf{k}) = \mathbb{X}_{12}[\mathbb{Q}_2^{(a, A_{1g})}] \otimes \mathbb{U}_5[\mathbb{Q}_0^{(s, A_{1g})}]$$

$$\boxed{\text{No. 19}} \quad \hat{\mathbb{Q}}_0^{(A_{1g})} [\text{M}_4, \text{B}_1]$$

$$\hat{\mathbb{Z}}_{19} = \frac{\sqrt{3}\mathbb{X}_{13}[\mathbb{Q}_1^{(a, A_{2u})}] \otimes \mathbb{Y}_6[\mathbb{Q}_1^{(b, A_{2u})}]}{3} + \frac{\sqrt{3}\mathbb{X}_{15}[\mathbb{Q}_{1,0}^{(a, Eu)}] \otimes \mathbb{Y}_7[\mathbb{Q}_{1,0}^{(b, Eu)}]}{3} + \frac{\sqrt{3}\mathbb{X}_{16}[\mathbb{Q}_{1,1}^{(a, Eu)}] \otimes \mathbb{Y}_8[\mathbb{Q}_{1,1}^{(b, Eu)}]}{3}$$

$$\begin{aligned}
\hat{Z}_{19}(\mathbf{k}) = & \frac{\sqrt{3}\mathbb{X}_{13}[\mathbb{Q}_1^{(a,A_{2u})}] \otimes \mathbb{U}_6[\mathbb{Q}_1^{(u,A_{2u})}] \otimes \mathbb{F}_1[\mathbb{Q}_0^{(k,A_{1g})}]}{6} + \frac{\sqrt{3}\mathbb{X}_{13}[\mathbb{Q}_1^{(a,A_{2u})}] \otimes \mathbb{U}_7[\mathbb{Q}_3^{(u,B_{2u})}] \otimes \mathbb{F}_2[\mathbb{Q}_2^{(k,B_{1g})}]}{6} - \frac{\sqrt{3}\mathbb{X}_{13}[\mathbb{Q}_1^{(a,A_{2u})}] \otimes \mathbb{U}_8[\mathbb{T}_0^{(u,A_{1g})}] \otimes \mathbb{F}_5[\mathbb{T}_1^{(k,A_{2u})}]}{6} \\
& - \frac{\sqrt{3}\mathbb{X}_{13}[\mathbb{Q}_1^{(a,A_{2u})}] \otimes \mathbb{U}_9[\mathbb{T}_2^{(u,B_{1g})}] \otimes \mathbb{F}_8[\mathbb{T}_3^{(k,B_{2u})}]}{6} + \frac{\sqrt{3}\mathbb{X}_{15}[\mathbb{Q}_{1,0}^{(a,E_u)}] \otimes \mathbb{U}_6[\mathbb{Q}_1^{(u,A_{2u})}] \otimes \mathbb{F}_4[\mathbb{Q}_{2,1}^{(k,E_g)}]}{6} + \frac{\sqrt{3}\mathbb{X}_{15}[\mathbb{Q}_{1,0}^{(a,E_u)}] \otimes \mathbb{U}_7[\mathbb{Q}_3^{(u,B_{2u})}] \otimes \mathbb{F}_4[\mathbb{Q}_{2,1}^{(k,E_g)}]}{6} \\
& - \frac{\sqrt{3}\mathbb{X}_{15}[\mathbb{Q}_{1,0}^{(a,E_u)}] \otimes \mathbb{U}_8[\mathbb{T}_0^{(u,A_{1g})}] \otimes \mathbb{F}_6[\mathbb{T}_{1,0}^{(k,E_u)}]}{6} - \frac{\sqrt{3}\mathbb{X}_{15}[\mathbb{Q}_{1,0}^{(a,E_u)}] \otimes \mathbb{U}_9[\mathbb{T}_2^{(u,B_{1g})}] \otimes \mathbb{F}_6[\mathbb{T}_{1,0}^{(k,E_u)}]}{6} + \frac{\sqrt{3}\mathbb{X}_{16}[\mathbb{Q}_{1,1}^{(a,E_u)}] \otimes \mathbb{U}_6[\mathbb{Q}_1^{(u,A_{2u})}] \otimes \mathbb{F}_3[\mathbb{Q}_{2,0}^{(k,E_g)}]}{6} \\
& - \frac{\sqrt{3}\mathbb{X}_{16}[\mathbb{Q}_{1,1}^{(a,E_u)}] \otimes \mathbb{U}_7[\mathbb{Q}_3^{(u,B_{2u})}] \otimes \mathbb{F}_3[\mathbb{Q}_{2,0}^{(k,E_g)}]}{6} - \frac{\sqrt{3}\mathbb{X}_{16}[\mathbb{Q}_{1,1}^{(a,E_u)}] \otimes \mathbb{U}_8[\mathbb{T}_0^{(u,A_{1g})}] \otimes \mathbb{F}_7[\mathbb{T}_{1,1}^{(k,E_u)}]}{6} + \frac{\sqrt{3}\mathbb{X}_{16}[\mathbb{Q}_{1,1}^{(a,E_u)}] \otimes \mathbb{U}_9[\mathbb{T}_2^{(u,B_{1g})}] \otimes \mathbb{F}_7[\mathbb{T}_{1,1}^{(k,E_u)}]}{6}
\end{aligned}$$

$$\boxed{\text{No. 20}} \quad \hat{\mathbb{Q}}_2^{(A_{1g})} [\mathbb{M}_4, \mathbb{B}_1]$$

$$\hat{Z}_{20} = \frac{\sqrt{6}\mathbb{X}_{13}[\mathbb{Q}_1^{(a,A_{2u})}] \otimes \mathbb{Y}_6[\mathbb{Q}_1^{(b,A_{2u})}]}{3} - \frac{\sqrt{6}\mathbb{X}_{15}[\mathbb{Q}_{1,0}^{(a,E_u)}] \otimes \mathbb{Y}_7[\mathbb{Q}_{1,0}^{(b,E_u)}]}{6} - \frac{\sqrt{6}\mathbb{X}_{16}[\mathbb{Q}_{1,1}^{(a,E_u)}] \otimes \mathbb{Y}_8[\mathbb{Q}_{1,1}^{(b,E_u)}]}{6}$$

$$\begin{aligned}
\hat{Z}_{20}(\mathbf{k}) = & \frac{\sqrt{6}\mathbb{X}_{13}[\mathbb{Q}_1^{(a,A_{2u})}] \otimes \mathbb{U}_6[\mathbb{Q}_1^{(u,A_{2u})}] \otimes \mathbb{F}_1[\mathbb{Q}_0^{(k,A_{1g})}]}{6} + \frac{\sqrt{6}\mathbb{X}_{13}[\mathbb{Q}_1^{(a,A_{2u})}] \otimes \mathbb{U}_7[\mathbb{Q}_3^{(u,B_{2u})}] \otimes \mathbb{F}_2[\mathbb{Q}_2^{(k,B_{1g})}]}{6} - \frac{\sqrt{6}\mathbb{X}_{13}[\mathbb{Q}_1^{(a,A_{2u})}] \otimes \mathbb{U}_8[\mathbb{T}_0^{(u,A_{1g})}] \otimes \mathbb{F}_5[\mathbb{T}_1^{(k,A_{2u})}]}{6} \\
& - \frac{\sqrt{6}\mathbb{X}_{13}[\mathbb{Q}_1^{(a,A_{2u})}] \otimes \mathbb{U}_9[\mathbb{T}_2^{(u,B_{1g})}] \otimes \mathbb{F}_8[\mathbb{T}_3^{(k,B_{2u})}]}{6} - \frac{\sqrt{6}\mathbb{X}_{15}[\mathbb{Q}_{1,0}^{(a,E_u)}] \otimes \mathbb{U}_6[\mathbb{Q}_1^{(u,A_{2u})}] \otimes \mathbb{F}_4[\mathbb{Q}_{2,1}^{(k,E_g)}]}{6} - \frac{\sqrt{6}\mathbb{X}_{15}[\mathbb{Q}_{1,0}^{(a,E_u)}] \otimes \mathbb{U}_7[\mathbb{Q}_3^{(u,B_{2u})}] \otimes \mathbb{F}_4[\mathbb{Q}_{2,1}^{(k,E_g)}]}{6} \\
& + \frac{\sqrt{6}\mathbb{X}_{15}[\mathbb{Q}_{1,0}^{(a,E_u)}] \otimes \mathbb{U}_8[\mathbb{T}_0^{(u,A_{1g})}] \otimes \mathbb{F}_6[\mathbb{T}_{1,0}^{(k,E_u)}]}{12} + \frac{\sqrt{6}\mathbb{X}_{15}[\mathbb{Q}_{1,0}^{(a,E_u)}] \otimes \mathbb{U}_9[\mathbb{T}_2^{(u,B_{1g})}] \otimes \mathbb{F}_6[\mathbb{T}_{1,0}^{(k,E_u)}]}{12} - \frac{\sqrt{6}\mathbb{X}_{16}[\mathbb{Q}_{1,1}^{(a,E_u)}] \otimes \mathbb{U}_6[\mathbb{Q}_1^{(u,A_{2u})}] \otimes \mathbb{F}_3[\mathbb{Q}_{2,0}^{(k,E_g)}]}{12} \\
& + \frac{\sqrt{6}\mathbb{X}_{16}[\mathbb{Q}_{1,1}^{(a,E_u)}] \otimes \mathbb{U}_7[\mathbb{Q}_3^{(u,B_{2u})}] \otimes \mathbb{F}_3[\mathbb{Q}_{2,0}^{(k,E_g)}]}{12} + \frac{\sqrt{6}\mathbb{X}_{16}[\mathbb{Q}_{1,1}^{(a,E_u)}] \otimes \mathbb{U}_8[\mathbb{T}_0^{(u,A_{1g})}] \otimes \mathbb{F}_7[\mathbb{T}_{1,1}^{(k,E_u)}]}{12} - \frac{\sqrt{6}\mathbb{X}_{16}[\mathbb{Q}_{1,1}^{(a,E_u)}] \otimes \mathbb{U}_9[\mathbb{T}_2^{(u,B_{1g})}] \otimes \mathbb{F}_7[\mathbb{T}_{1,1}^{(k,E_u)}]}{12}
\end{aligned}$$

$$\boxed{\text{No. 21}} \quad \hat{\mathbb{Q}}_2^{(A_{1g})} [\mathbb{M}_4, \mathbb{B}_1]$$

$$\begin{aligned}
\hat{Z}_{21} = & \frac{\sqrt{21}\mathbb{X}_{14}[\mathbb{Q}_3^{(a,A_{2u})}] \otimes \mathbb{Y}_6[\mathbb{Q}_1^{(b,A_{2u})}]}{7} - \frac{\sqrt{21}\mathbb{X}_{17}[\mathbb{Q}_{3,0}^{(a,E_u,1)}] \otimes \mathbb{Y}_7[\mathbb{Q}_{1,0}^{(b,E_u)}]}{14} - \frac{\sqrt{21}\mathbb{X}_{18}[\mathbb{Q}_{3,1}^{(a,E_u,1)}] \otimes \mathbb{Y}_8[\mathbb{Q}_{1,1}^{(b,E_u)}]}{14} \\
& - \frac{\sqrt{35}\mathbb{X}_{19}[\mathbb{Q}_{3,0}^{(a,E_u,2)}] \otimes \mathbb{Y}_7[\mathbb{Q}_{1,0}^{(b,E_u)}]}{14} - \frac{\sqrt{35}\mathbb{X}_{20}[\mathbb{Q}_{3,1}^{(a,E_u,2)}] \otimes \mathbb{Y}_8[\mathbb{Q}_{1,1}^{(b,E_u)}]}{14}
\end{aligned}$$

$$\begin{aligned}
\hat{Z}_{23}(\mathbf{k}) = & \frac{\sqrt{105}\mathbb{X}_{14}[\mathbb{Q}_3^{(a,A_{2u})}] \otimes \mathbb{U}_6[\mathbb{Q}_1^{(u,A_{2u})}] \otimes \mathbb{F}_1[\mathbb{Q}_0^{(k,A_{1g})}]}{42} + \frac{\sqrt{105}\mathbb{X}_{14}[\mathbb{Q}_3^{(a,A_{2u})}] \otimes \mathbb{U}_7[\mathbb{Q}_3^{(u,B_{2u})}] \otimes \mathbb{F}_2[\mathbb{Q}_2^{(k,B_{1g})}]}{42} - \frac{\sqrt{105}\mathbb{X}_{14}[\mathbb{Q}_3^{(a,A_{2u})}] \otimes \mathbb{U}_8[\mathbb{T}_0^{(u,A_{1g})}] \otimes \mathbb{F}_5[\mathbb{T}_1^{(k,A_{2u})}]}{42} \\
& - \frac{\sqrt{105}\mathbb{X}_{14}[\mathbb{Q}_3^{(a,A_{2u})}] \otimes \mathbb{U}_9[\mathbb{T}_2^{(u,B_{1g})}] \otimes \mathbb{F}_8[\mathbb{T}_3^{(k,B_{2u})}]}{42} - \frac{\sqrt{105}\mathbb{X}_{17}[\mathbb{Q}_{3,0}^{(a,E_u,1)}] \otimes \mathbb{U}_6[\mathbb{Q}_1^{(u,A_{2u})}] \otimes \mathbb{F}_4[\mathbb{Q}_{2,1}^{(k,E_g)}]}{84} - \frac{\sqrt{105}\mathbb{X}_{17}[\mathbb{Q}_{3,0}^{(a,E_u,1)}] \otimes \mathbb{U}_7[\mathbb{Q}_3^{(u,B_{2u})}] \otimes \mathbb{F}_4[\mathbb{Q}_{2,1}^{(k,E_g)}]}{84} \\
& + \frac{\sqrt{105}\mathbb{X}_{17}[\mathbb{Q}_{3,0}^{(a,E_u,1)}] \otimes \mathbb{U}_8[\mathbb{T}_0^{(u,A_{1g})}] \otimes \mathbb{F}_6[\mathbb{T}_{1,0}^{(k,E_u)}]}{84} + \frac{\sqrt{105}\mathbb{X}_{17}[\mathbb{Q}_{3,0}^{(a,E_u,1)}] \otimes \mathbb{U}_9[\mathbb{T}_2^{(u,B_{1g})}] \otimes \mathbb{F}_6[\mathbb{T}_{1,0}^{(k,E_u)}]}{84} - \frac{\sqrt{105}\mathbb{X}_{18}[\mathbb{Q}_{3,1}^{(a,E_u,1)}] \otimes \mathbb{U}_6[\mathbb{Q}_1^{(u,A_{2u})}] \otimes \mathbb{F}_3[\mathbb{Q}_{2,0}^{(k,E_g)}]}{84} \\
& + \frac{\sqrt{105}\mathbb{X}_{18}[\mathbb{Q}_{3,1}^{(a,E_u,1)}] \otimes \mathbb{U}_7[\mathbb{Q}_3^{(u,B_{2u})}] \otimes \mathbb{F}_3[\mathbb{Q}_{2,0}^{(k,E_g)}]}{84} + \frac{\sqrt{105}\mathbb{X}_{18}[\mathbb{Q}_{3,1}^{(a,E_u,1)}] \otimes \mathbb{U}_8[\mathbb{T}_0^{(u,A_{1g})}] \otimes \mathbb{F}_7[\mathbb{T}_{1,1}^{(k,E_u)}]}{84} \\
& - \frac{\sqrt{105}\mathbb{X}_{18}[\mathbb{Q}_{3,1}^{(a,E_u,1)}] \otimes \mathbb{U}_9[\mathbb{T}_2^{(u,B_{1g})}] \otimes \mathbb{F}_7[\mathbb{T}_{1,1}^{(k,E_u)}]}{84} + \frac{3\sqrt{7}\mathbb{X}_{19}[\mathbb{Q}_{3,0}^{(a,E_u,2)}] \otimes \mathbb{U}_6[\mathbb{Q}_1^{(u,A_{2u})}] \otimes \mathbb{F}_4[\mathbb{Q}_{2,1}^{(k,E_g)}]}{28} + \frac{3\sqrt{7}\mathbb{X}_{19}[\mathbb{Q}_{3,0}^{(a,E_u,2)}] \otimes \mathbb{U}_7[\mathbb{Q}_3^{(u,B_{2u})}] \otimes \mathbb{F}_4[\mathbb{Q}_{2,1}^{(k,E_g)}]}{28} \\
& - \frac{3\sqrt{7}\mathbb{X}_{19}[\mathbb{Q}_{3,0}^{(a,E_u,2)}] \otimes \mathbb{U}_8[\mathbb{T}_0^{(u,A_{1g})}] \otimes \mathbb{F}_6[\mathbb{T}_{1,0}^{(k,E_u)}]}{28} - \frac{3\sqrt{7}\mathbb{X}_{19}[\mathbb{Q}_{3,0}^{(a,E_u,2)}] \otimes \mathbb{U}_9[\mathbb{T}_2^{(u,B_{1g})}] \otimes \mathbb{F}_6[\mathbb{T}_{1,0}^{(k,E_u)}]}{28} + \frac{3\sqrt{7}\mathbb{X}_{20}[\mathbb{Q}_{3,1}^{(a,E_u,2)}] \otimes \mathbb{U}_6[\mathbb{Q}_1^{(u,A_{2u})}] \otimes \mathbb{F}_3[\mathbb{Q}_{2,0}^{(k,E_g)}]}{28} \\
& - \frac{3\sqrt{7}\mathbb{X}_{20}[\mathbb{Q}_{3,1}^{(a,E_u,2)}] \otimes \mathbb{U}_7[\mathbb{Q}_3^{(u,B_{2u})}] \otimes \mathbb{F}_3[\mathbb{Q}_{2,0}^{(k,E_g)}]}{28} - \frac{3\sqrt{7}\mathbb{X}_{20}[\mathbb{Q}_{3,1}^{(a,E_u,2)}] \otimes \mathbb{U}_8[\mathbb{T}_0^{(u,A_{1g})}] \otimes \mathbb{F}_7[\mathbb{T}_{1,1}^{(k,E_u)}]}{28} + \frac{3\sqrt{7}\mathbb{X}_{20}[\mathbb{Q}_{3,1}^{(a,E_u,2)}] \otimes \mathbb{U}_9[\mathbb{T}_2^{(u,B_{1g})}] \otimes \mathbb{F}_7[\mathbb{T}_{1,1}^{(k,E_u)}]}{28}
\end{aligned}$$

$$\boxed{\text{No. 24}} \quad \hat{\mathbb{Q}}_0^{(A_{1g})} [\mathbb{M}_4, \mathbb{B}_1]$$

$$\hat{Z}_{24} = \mathbb{X}_{23}[\mathbb{Q}_3^{(a,B_{2u})}] \otimes \mathbb{Y}_9[\mathbb{Q}_3^{(b,B_{2u})}]$$

$$\begin{aligned}
\hat{Z}_{24}(\mathbf{k}) = & \frac{\mathbb{X}_{23}[\mathbb{Q}_3^{(a,B_{2u})}] \otimes \mathbb{U}_6[\mathbb{Q}_1^{(u,A_{2u})}] \otimes \mathbb{F}_2[\mathbb{Q}_2^{(k,B_{1g})}]}{2} + \frac{\mathbb{X}_{23}[\mathbb{Q}_3^{(a,B_{2u})}] \otimes \mathbb{U}_7[\mathbb{Q}_3^{(u,B_{2u})}] \otimes \mathbb{F}_1[\mathbb{Q}_0^{(k,A_{1g})}]}{2} \\
& - \frac{\mathbb{X}_{23}[\mathbb{Q}_3^{(a,B_{2u})}] \otimes \mathbb{U}_8[\mathbb{T}_0^{(u,A_{1g})}] \otimes \mathbb{F}_8[\mathbb{T}_3^{(k,B_{2u})}]}{2} - \frac{\mathbb{X}_{23}[\mathbb{Q}_3^{(a,B_{2u})}] \otimes \mathbb{U}_9[\mathbb{T}_2^{(u,B_{1g})}] \otimes \mathbb{F}_5[\mathbb{T}_1^{(k,A_{2u})}]}{2}
\end{aligned}$$

$$\boxed{\text{No. 25}} \quad \hat{\mathbb{Q}}_2^{(A_{1g})} [\mathbb{M}_4, \mathbb{B}_1]$$

$$\hat{Z}_{25} = -\frac{\sqrt{2}\mathbb{X}_{21}[\mathbb{G}_{2,0}^{(a,E_u)}] \otimes \mathbb{Y}_7[\mathbb{Q}_{1,0}^{(b,E_u)}]}{2} + \frac{\sqrt{2}\mathbb{X}_{22}[\mathbb{G}_{2,1}^{(a,E_u)}] \otimes \mathbb{Y}_8[\mathbb{Q}_{1,1}^{(b,E_u)}]}{2}$$

$$\begin{aligned}
\hat{Z}_{25}(\mathbf{k}) = & -\frac{\sqrt{2}\mathbb{X}_{21}[\mathbb{G}_{2,0}^{(a,E_u)}] \otimes \mathbb{U}_6[\mathbb{Q}_1^{(u,A_{2u})}] \otimes \mathbb{F}_4[\mathbb{Q}_{2,1}^{(k,E_g)}]}{4} - \frac{\sqrt{2}\mathbb{X}_{21}[\mathbb{G}_{2,0}^{(a,E_u)}] \otimes \mathbb{U}_7[\mathbb{Q}_3^{(u,B_{2u})}] \otimes \mathbb{F}_4[\mathbb{Q}_{2,1}^{(k,E_g)}]}{4} \\
& + \frac{\sqrt{2}\mathbb{X}_{21}[\mathbb{G}_{2,0}^{(a,E_u)}] \otimes \mathbb{U}_8[\mathbb{T}_0^{(u,A_{1g})}] \otimes \mathbb{F}_6[\mathbb{T}_{1,0}^{(k,E_u)}]}{4} + \frac{\sqrt{2}\mathbb{X}_{21}[\mathbb{G}_{2,0}^{(a,E_u)}] \otimes \mathbb{U}_9[\mathbb{T}_2^{(u,B_{1g})}] \otimes \mathbb{F}_6[\mathbb{T}_{1,0}^{(k,E_u)}]}{4} + \frac{\sqrt{2}\mathbb{X}_{22}[\mathbb{G}_{2,1}^{(a,E_u)}] \otimes \mathbb{U}_6[\mathbb{Q}_1^{(u,A_{2u})}] \otimes \mathbb{F}_3[\mathbb{Q}_{2,0}^{(k,E_g)}]}{4} \\
& - \frac{\sqrt{2}\mathbb{X}_{22}[\mathbb{G}_{2,1}^{(a,E_u)}] \otimes \mathbb{U}_7[\mathbb{Q}_3^{(u,B_{2u})}] \otimes \mathbb{F}_3[\mathbb{Q}_{2,0}^{(k,E_g)}]}{4} - \frac{\sqrt{2}\mathbb{X}_{22}[\mathbb{G}_{2,1}^{(a,E_u)}] \otimes \mathbb{U}_8[\mathbb{T}_0^{(u,A_{1g})}] \otimes \mathbb{F}_7[\mathbb{T}_{1,1}^{(k,E_u)}]}{4} + \frac{\sqrt{2}\mathbb{X}_{22}[\mathbb{G}_{2,1}^{(a,E_u)}] \otimes \mathbb{U}_9[\mathbb{T}_2^{(u,B_{1g})}] \otimes \mathbb{F}_7[\mathbb{T}_{1,1}^{(k,E_u)}]}{4}
\end{aligned}$$

$$\boxed{\text{No. 26}} \quad \hat{\mathbb{Q}}_2^{(A_{1g})} [\text{M}_4, \text{B}_1]$$

$$\hat{\mathbb{Z}}_{26} = -\mathbb{X}_{24}[\mathbb{G}_2^{(a, B_{2u})}] \otimes \mathbb{Y}_9[\mathbb{Q}_3^{(b, B_{2u})}]$$

$$\begin{aligned} \hat{\mathbb{Z}}_{26}(\mathbf{k}) = & -\frac{\mathbb{X}_{24}[\mathbb{G}_2^{(a, B_{2u})}] \otimes \mathbb{U}_6[\mathbb{Q}_1^{(u, A_{2u})}] \otimes \mathbb{F}_2[\mathbb{Q}_2^{(k, B_{1g})}]}{2} - \frac{\mathbb{X}_{24}[\mathbb{G}_2^{(a, B_{2u})}] \otimes \mathbb{U}_7[\mathbb{Q}_3^{(u, B_{2u})}] \otimes \mathbb{F}_1[\mathbb{Q}_0^{(k, A_{1g})}]}{2} \\ & + \frac{\mathbb{X}_{24}[\mathbb{G}_2^{(a, B_{2u})}] \otimes \mathbb{U}_8[\mathbb{T}_0^{(u, A_{1g})}] \otimes \mathbb{F}_8[\mathbb{T}_3^{(k, B_{2u})}]}{2} + \frac{\mathbb{X}_{24}[\mathbb{G}_2^{(a, B_{2u})}] \otimes \mathbb{U}_9[\mathbb{T}_2^{(u, B_{1g})}] \otimes \mathbb{F}_5[\mathbb{T}_1^{(k, A_{2u})}]}{2} \end{aligned}$$

$$\boxed{\text{No. 27}} \quad \hat{\mathbb{Q}}_0^{(A_{1g})} [\text{M}_4, \text{B}_2]$$

$$\hat{\mathbb{Z}}_{27} = \frac{\sqrt{3}\mathbb{X}_{13}[\mathbb{Q}_1^{(a, A_{2u})}] \otimes \mathbb{Y}_{10}[\mathbb{Q}_1^{(b, A_{2u})}]}{3} + \frac{\sqrt{3}\mathbb{X}_{15}[\mathbb{Q}_{1,0}^{(a, Eu)}] \otimes \mathbb{Y}_{11}[\mathbb{Q}_{1,0}^{(b, Eu)}]}{3} + \frac{\sqrt{3}\mathbb{X}_{16}[\mathbb{Q}_{1,1}^{(a, Eu)}] \otimes \mathbb{Y}_{12}[\mathbb{Q}_{1,1}^{(b, Eu)}]}{3}$$

$$\begin{aligned} \hat{\mathbb{Z}}_{27}(\mathbf{k}) = & \frac{\sqrt{3}\mathbb{X}_{13}[\mathbb{Q}_1^{(a, A_{2u})}] \otimes \mathbb{U}_{10}[\mathbb{Q}_1^{(u, A_{2u})}] \otimes \mathbb{F}_9[\mathbb{Q}_0^{(k, A_{1g})}]}{6} + \frac{\sqrt{3}\mathbb{X}_{13}[\mathbb{Q}_1^{(a, A_{2u})}] \otimes \mathbb{U}_{11}[\mathbb{Q}_3^{(u, B_{2u})}] \otimes \mathbb{F}_{10}[\mathbb{Q}_2^{(k, B_{1g})}]}{6} - \frac{\sqrt{3}\mathbb{X}_{13}[\mathbb{Q}_1^{(a, A_{2u})}] \otimes \mathbb{U}_{12}[\mathbb{T}_0^{(u, A_{1g})}] \otimes \mathbb{F}_{13}[\mathbb{T}_1^{(k, A_{2u})}]}{6} \\ & - \frac{\sqrt{3}\mathbb{X}_{13}[\mathbb{Q}_1^{(a, A_{2u})}] \otimes \mathbb{U}_{13}[\mathbb{T}_2^{(u, B_{1g})}] \otimes \mathbb{F}_{16}[\mathbb{T}_3^{(k, B_{2u})}]}{6} + \frac{\sqrt{3}\mathbb{X}_{15}[\mathbb{Q}_{1,0}^{(a, Eu)}] \otimes \mathbb{U}_{10}[\mathbb{Q}_1^{(u, A_{2u})}] \otimes \mathbb{F}_{12}[\mathbb{Q}_{2,1}^{(k, Eg)}]}{6} + \frac{\sqrt{3}\mathbb{X}_{15}[\mathbb{Q}_{1,0}^{(a, Eu)}] \otimes \mathbb{U}_{11}[\mathbb{Q}_3^{(u, B_{2u})}] \otimes \mathbb{F}_{12}[\mathbb{Q}_{2,1}^{(k, Eg)}]}{6} \\ & - \frac{\sqrt{3}\mathbb{X}_{15}[\mathbb{Q}_{1,0}^{(a, Eu)}] \otimes \mathbb{U}_{12}[\mathbb{T}_0^{(u, A_{1g})}] \otimes \mathbb{F}_{14}[\mathbb{T}_{1,0}^{(k, Eu)}]}{6} - \frac{\sqrt{3}\mathbb{X}_{15}[\mathbb{Q}_{1,0}^{(a, Eu)}] \otimes \mathbb{U}_{13}[\mathbb{T}_2^{(u, B_{1g})}] \otimes \mathbb{F}_{14}[\mathbb{T}_{1,0}^{(k, Eu)}]}{6} + \frac{\sqrt{3}\mathbb{X}_{16}[\mathbb{Q}_{1,1}^{(a, Eu)}] \otimes \mathbb{U}_{10}[\mathbb{Q}_1^{(u, A_{2u})}] \otimes \mathbb{F}_{11}[\mathbb{Q}_{2,0}^{(k, Eg)}]}{6} \\ & - \frac{\sqrt{3}\mathbb{X}_{16}[\mathbb{Q}_{1,1}^{(a, Eu)}] \otimes \mathbb{U}_{11}[\mathbb{Q}_3^{(u, B_{2u})}] \otimes \mathbb{F}_{11}[\mathbb{Q}_{2,0}^{(k, Eg)}]}{6} - \frac{\sqrt{3}\mathbb{X}_{16}[\mathbb{Q}_{1,1}^{(a, Eu)}] \otimes \mathbb{U}_{12}[\mathbb{T}_0^{(u, A_{1g})}] \otimes \mathbb{F}_{15}[\mathbb{T}_{1,1}^{(k, Eu)}]}{6} + \frac{\sqrt{3}\mathbb{X}_{16}[\mathbb{Q}_{1,1}^{(a, Eu)}] \otimes \mathbb{U}_{13}[\mathbb{T}_2^{(u, B_{1g})}] \otimes \mathbb{F}_{15}[\mathbb{T}_{1,1}^{(k, Eu)}]}{6} \end{aligned}$$

$$\boxed{\text{No. 28}} \quad \hat{\mathbb{Q}}_2^{(A_{1g})} [\text{M}_4, \text{B}_2]$$

$$\hat{\mathbb{Z}}_{28} = \frac{\sqrt{6}\mathbb{X}_{13}[\mathbb{Q}_1^{(a, A_{2u})}] \otimes \mathbb{Y}_{10}[\mathbb{Q}_1^{(b, A_{2u})}]}{3} - \frac{\sqrt{6}\mathbb{X}_{15}[\mathbb{Q}_{1,0}^{(a, Eu)}] \otimes \mathbb{Y}_{11}[\mathbb{Q}_{1,0}^{(b, Eu)}]}{6} - \frac{\sqrt{6}\mathbb{X}_{16}[\mathbb{Q}_{1,1}^{(a, Eu)}] \otimes \mathbb{Y}_{12}[\mathbb{Q}_{1,1}^{(b, Eu)}]}{6}$$

$$\begin{aligned} \hat{\mathbb{Z}}_{28}(\mathbf{k}) = & \frac{\sqrt{6}\mathbb{X}_{13}[\mathbb{Q}_1^{(a, A_{2u})}] \otimes \mathbb{U}_{10}[\mathbb{Q}_1^{(u, A_{2u})}] \otimes \mathbb{F}_9[\mathbb{Q}_0^{(k, A_{1g})}]}{6} + \frac{\sqrt{6}\mathbb{X}_{13}[\mathbb{Q}_1^{(a, A_{2u})}] \otimes \mathbb{U}_{11}[\mathbb{Q}_3^{(u, B_{2u})}] \otimes \mathbb{F}_{10}[\mathbb{Q}_2^{(k, B_{1g})}]}{6} - \frac{\sqrt{6}\mathbb{X}_{13}[\mathbb{Q}_1^{(a, A_{2u})}] \otimes \mathbb{U}_{12}[\mathbb{T}_0^{(u, A_{1g})}] \otimes \mathbb{F}_{13}[\mathbb{T}_1^{(k, A_{2u})}]}{6} \\ & - \frac{\sqrt{6}\mathbb{X}_{13}[\mathbb{Q}_1^{(a, A_{2u})}] \otimes \mathbb{U}_{13}[\mathbb{T}_2^{(u, B_{1g})}] \otimes \mathbb{F}_{16}[\mathbb{T}_3^{(k, B_{2u})}]}{6} - \frac{\sqrt{6}\mathbb{X}_{15}[\mathbb{Q}_{1,0}^{(a, Eu)}] \otimes \mathbb{U}_{10}[\mathbb{Q}_1^{(u, A_{2u})}] \otimes \mathbb{F}_{12}[\mathbb{Q}_{2,1}^{(k, Eg)}]}{12} - \frac{\sqrt{6}\mathbb{X}_{15}[\mathbb{Q}_{1,0}^{(a, Eu)}] \otimes \mathbb{U}_{11}[\mathbb{Q}_3^{(u, B_{2u})}] \otimes \mathbb{F}_{12}[\mathbb{Q}_{2,1}^{(k, Eg)}]}{12} \\ & + \frac{\sqrt{6}\mathbb{X}_{15}[\mathbb{Q}_{1,0}^{(a, Eu)}] \otimes \mathbb{U}_{12}[\mathbb{T}_0^{(u, A_{1g})}] \otimes \mathbb{F}_{14}[\mathbb{T}_{1,0}^{(k, Eu)}]}{12} + \frac{\sqrt{6}\mathbb{X}_{15}[\mathbb{Q}_{1,0}^{(a, Eu)}] \otimes \mathbb{U}_{13}[\mathbb{T}_2^{(u, B_{1g})}] \otimes \mathbb{F}_{14}[\mathbb{T}_{1,0}^{(k, Eu)}]}{12} - \frac{\sqrt{6}\mathbb{X}_{16}[\mathbb{Q}_{1,1}^{(a, Eu)}] \otimes \mathbb{U}_{10}[\mathbb{Q}_1^{(u, A_{2u})}] \otimes \mathbb{F}_{11}[\mathbb{Q}_{2,0}^{(k, Eg)}]}{12} \\ & + \frac{\sqrt{6}\mathbb{X}_{16}[\mathbb{Q}_{1,1}^{(a, Eu)}] \otimes \mathbb{U}_{11}[\mathbb{Q}_3^{(u, B_{2u})}] \otimes \mathbb{F}_{11}[\mathbb{Q}_{2,0}^{(k, Eg)}]}{12} + \frac{\sqrt{6}\mathbb{X}_{16}[\mathbb{Q}_{1,1}^{(a, Eu)}] \otimes \mathbb{U}_{12}[\mathbb{T}_0^{(u, A_{1g})}] \otimes \mathbb{F}_{15}[\mathbb{T}_{1,1}^{(k, Eu)}]}{12} - \frac{\sqrt{6}\mathbb{X}_{16}[\mathbb{Q}_{1,1}^{(a, Eu)}] \otimes \mathbb{U}_{13}[\mathbb{T}_2^{(u, B_{1g})}] \otimes \mathbb{F}_{15}[\mathbb{T}_{1,1}^{(k, Eu)}]}{12} \end{aligned}$$

$$\hat{Z}_{29} = \frac{\sqrt{21}\mathbb{X}_{14}[\mathbb{Q}_3^{(a,A_{2u})}] \otimes \mathbb{Y}_{10}[\mathbb{Q}_1^{(b,A_{2u})}]}{7} - \frac{\sqrt{21}\mathbb{X}_{17}[\mathbb{Q}_{3,0}^{(a,E_u,1)}] \otimes \mathbb{Y}_{11}[\mathbb{Q}_{1,0}^{(b,E_u)}]}{14} - \frac{\sqrt{21}\mathbb{X}_{18}[\mathbb{Q}_{3,1}^{(a,E_u,1)}] \otimes \mathbb{Y}_{12}[\mathbb{Q}_{1,1}^{(b,E_u)}]}{14} \\ - \frac{\sqrt{35}\mathbb{X}_{19}[\mathbb{Q}_{3,0}^{(a,E_u,2)}] \otimes \mathbb{Y}_{11}[\mathbb{Q}_{1,0}^{(b,E_u)}]}{14} - \frac{\sqrt{35}\mathbb{X}_{20}[\mathbb{Q}_{3,1}^{(a,E_u,2)}] \otimes \mathbb{Y}_{12}[\mathbb{Q}_{1,1}^{(b,E_u)}]}{14}$$

No. 30 $\hat{\mathbb{Q}}_4^{(A_{1g},1)} [\mathbf{M}_4, \mathbf{B}_2]$

$$\hat{\mathbb{Z}}_{30} = \frac{\sqrt{3}\mathbb{X}_{14}[\mathbb{Q}_3^{(a,A_{2u})}] \otimes \mathbb{Y}_{10}[\mathbb{Q}_1^{(b,A_{2u})}]}{3} + \frac{\sqrt{3}\mathbb{X}_{17}[\mathbb{Q}_{3,0}^{(a,E_u,1)}] \otimes \mathbb{Y}_{11}[\mathbb{Q}_{1,0}^{(b,E_u)}]}{3} + \frac{\sqrt{3}\mathbb{X}_{18}[\mathbb{Q}_{3,1}^{(a,E_u,1)}] \otimes \mathbb{Y}_{12}[\mathbb{Q}_{1,1}^{(b,E_u)}]}{3}$$

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$$\boxed{\text{No. 31}} \quad \hat{\mathbb{Q}}_4^{(A_{1g},2)} [M_4, B_2]$$

$$\begin{aligned} \hat{\mathbb{Z}}_{31} = & \frac{\sqrt{105}\mathbb{X}_{14}[\mathbb{Q}_3^{(a,A_{2u})}] \otimes \mathbb{Y}_{10}[\mathbb{Q}_1^{(b,A_{2u})}]}{21} - \frac{\sqrt{105}\mathbb{X}_{17}[\mathbb{Q}_{3,0}^{(a,E_u,1)}] \otimes \mathbb{Y}_{11}[\mathbb{Q}_{1,0}^{(b,E_u)}]}{42} \\ & - \frac{\sqrt{105}\mathbb{X}_{18}[\mathbb{Q}_{3,1}^{(a,E_u,1)}] \otimes \mathbb{Y}_{12}[\mathbb{Q}_{1,1}^{(b,E_u)}]}{42} + \frac{3\sqrt{7}\mathbb{X}_{19}[\mathbb{Q}_{3,0}^{(a,E_u,2)}] \otimes \mathbb{Y}_{11}[\mathbb{Q}_{1,0}^{(b,E_u)}]}{14} + \frac{3\sqrt{7}\mathbb{X}_{20}[\mathbb{Q}_{3,1}^{(a,E_u,2)}] \otimes \mathbb{Y}_{12}[\mathbb{Q}_{1,1}^{(b,E_u)}]}{14} \\ \hat{\mathbb{Z}}_{31}(\mathbf{k}) = & \frac{\sqrt{105}\mathbb{X}_{14}[\mathbb{Q}_3^{(a,A_{2u})}] \otimes \mathbb{U}_{10}[\mathbb{Q}_1^{(u,A_{2u})}] \otimes \mathbb{F}_9[\mathbb{Q}_0^{(k,A_{1g})}]}{42} + \frac{\sqrt{105}\mathbb{X}_{14}[\mathbb{Q}_3^{(a,A_{2u})}] \otimes \mathbb{U}_{11}[\mathbb{Q}_3^{(u,B_{2u})}] \otimes \mathbb{F}_{10}[\mathbb{Q}_2^{(k,B_{1g})}]}{42} \\ & - \frac{\sqrt{105}\mathbb{X}_{14}[\mathbb{Q}_3^{(a,A_{2u})}] \otimes \mathbb{U}_{12}[\mathbb{T}_0^{(u,A_{1g})}] \otimes \mathbb{F}_{13}[\mathbb{T}_1^{(k,A_{2u})}]}{42} - \frac{\sqrt{105}\mathbb{X}_{14}[\mathbb{Q}_3^{(a,A_{2u})}] \otimes \mathbb{U}_{13}[\mathbb{T}_2^{(u,B_{1g})}] \otimes \mathbb{F}_{16}[\mathbb{T}_3^{(k,B_{2u})}]}{42} \\ & - \frac{\sqrt{105}\mathbb{X}_{17}[\mathbb{Q}_{3,0}^{(a,E_u,1)}] \otimes \mathbb{U}_{10}[\mathbb{Q}_1^{(u,A_{2u})}] \otimes \mathbb{F}_{12}[\mathbb{Q}_{2,1}^{(k,E_g)}]}{84} - \frac{\sqrt{105}\mathbb{X}_{17}[\mathbb{Q}_{3,0}^{(a,E_u,1)}] \otimes \mathbb{U}_{11}[\mathbb{Q}_3^{(u,B_{2u})}] \otimes \mathbb{F}_{12}[\mathbb{Q}_{2,1}^{(k,E_g)}]}{84} \\ & + \frac{\sqrt{105}\mathbb{X}_{17}[\mathbb{Q}_{3,0}^{(a,E_u,1)}] \otimes \mathbb{U}_{12}[\mathbb{T}_0^{(u,A_{1g})}] \otimes \mathbb{F}_{14}[\mathbb{T}_{1,0}^{(k,E_u)}]}{84} + \frac{\sqrt{105}\mathbb{X}_{17}[\mathbb{Q}_{3,0}^{(a,E_u,1)}] \otimes \mathbb{U}_{13}[\mathbb{T}_2^{(u,B_{1g})}] \otimes \mathbb{F}_{14}[\mathbb{T}_{1,0}^{(k,E_u)}]}{84} \\ & - \frac{\sqrt{105}\mathbb{X}_{18}[\mathbb{Q}_{3,1}^{(a,E_u,1)}] \otimes \mathbb{U}_{10}[\mathbb{Q}_1^{(u,A_{2u})}] \otimes \mathbb{F}_{11}[\mathbb{Q}_{2,0}^{(k,E_g)}]}{84} + \frac{\sqrt{105}\mathbb{X}_{18}[\mathbb{Q}_{3,1}^{(a,E_u,1)}] \otimes \mathbb{U}_{11}[\mathbb{Q}_3^{(u,B_{2u})}] \otimes \mathbb{F}_{11}[\mathbb{Q}_{2,0}^{(k,E_g)}]}{84} \\ & + \frac{\sqrt{105}\mathbb{X}_{18}[\mathbb{Q}_{3,1}^{(a,E_u,1)}] \otimes \mathbb{U}_{12}[\mathbb{T}_0^{(u,A_{1g})}] \otimes \mathbb{F}_{15}[\mathbb{T}_{1,1}^{(k,E_u)}]}{84} - \frac{\sqrt{105}\mathbb{X}_{18}[\mathbb{Q}_{3,1}^{(a,E_u,1)}] \otimes \mathbb{U}_{13}[\mathbb{T}_2^{(u,B_{1g})}] \otimes \mathbb{F}_{15}[\mathbb{T}_{1,1}^{(k,E_u)}]}{84} \\ & + \frac{3\sqrt{7}\mathbb{X}_{19}[\mathbb{Q}_{3,0}^{(a,E_u,2)}] \otimes \mathbb{U}_{10}[\mathbb{Q}_1^{(u,A_{2u})}] \otimes \mathbb{F}_{12}[\mathbb{Q}_{2,1}^{(k,E_g)}]}{28} + \frac{3\sqrt{7}\mathbb{X}_{19}[\mathbb{Q}_{3,0}^{(a,E_u,2)}] \otimes \mathbb{U}_{11}[\mathbb{Q}_3^{(u,B_{2u})}] \otimes \mathbb{F}_{12}[\mathbb{Q}_{2,1}^{(k,E_g)}]}{28} \\ & - \frac{3\sqrt{7}\mathbb{X}_{19}[\mathbb{Q}_{3,0}^{(a,E_u,2)}] \otimes \mathbb{U}_{12}[\mathbb{T}_0^{(u,A_{1g})}] \otimes \mathbb{F}_{14}[\mathbb{T}_{1,0}^{(k,E_u)}]}{28} - \frac{3\sqrt{7}\mathbb{X}_{19}[\mathbb{Q}_{3,0}^{(a,E_u,2)}] \otimes \mathbb{U}_{13}[\mathbb{T}_2^{(u,B_{1g})}] \otimes \mathbb{F}_{14}[\mathbb{T}_{1,0}^{(k,E_u)}]}{28} + \frac{3\sqrt{7}\mathbb{X}_{20}[\mathbb{Q}_{3,1}^{(a,E_u,2)}] \otimes \mathbb{U}_{10}[\mathbb{Q}_1^{(u,A_{2u})}] \otimes \mathbb{F}_{11}[\mathbb{Q}_{2,0}^{(k,E_g)}]}{28} \\ & - \frac{3\sqrt{7}\mathbb{X}_{20}[\mathbb{Q}_{3,1}^{(a,E_u,2)}] \otimes \mathbb{U}_{11}[\mathbb{Q}_3^{(u,B_{2u})}] \otimes \mathbb{F}_{11}[\mathbb{Q}_{2,0}^{(k,E_g)}]}{28} - \frac{3\sqrt{7}\mathbb{X}_{20}[\mathbb{Q}_{3,1}^{(a,E_u,2)}] \otimes \mathbb{U}_{12}[\mathbb{T}_0^{(u,A_{1g})}] \otimes \mathbb{F}_{15}[\mathbb{T}_{1,1}^{(k,E_u)}]}{28} + \frac{3\sqrt{7}\mathbb{X}_{20}[\mathbb{Q}_{3,1}^{(a,E_u,2)}] \otimes \mathbb{U}_{13}[\mathbb{T}_2^{(u,B_{1g})}] \otimes \mathbb{F}_{15}[\mathbb{T}_{1,1}^{(k,E_u)}]}{28} \end{aligned}$$

$$\boxed{\text{No. 32}} \quad \hat{\mathbb{Q}}_0^{(A_{1g})} [M_4, B_2]$$

$$\begin{aligned} \hat{\mathbb{Z}}_{32} = & \mathbb{X}_{23}[\mathbb{Q}_3^{(a,B_{2u})}] \otimes \mathbb{Y}_{13}[\mathbb{Q}_3^{(b,B_{2u})}] \\ \hat{\mathbb{Z}}_{32}(\mathbf{k}) = & \frac{\mathbb{X}_{23}[\mathbb{Q}_3^{(a,B_{2u})}] \otimes \mathbb{U}_{10}[\mathbb{Q}_1^{(u,A_{2u})}] \otimes \mathbb{F}_{10}[\mathbb{Q}_2^{(k,B_{1g})}]}{2} + \frac{\mathbb{X}_{23}[\mathbb{Q}_3^{(a,B_{2u})}] \otimes \mathbb{U}_{11}[\mathbb{Q}_3^{(u,B_{2u})}] \otimes \mathbb{F}_9[\mathbb{Q}_0^{(k,A_{1g})}]}{2} \\ & - \frac{\mathbb{X}_{23}[\mathbb{Q}_3^{(a,B_{2u})}] \otimes \mathbb{U}_{12}[\mathbb{T}_0^{(u,A_{1g})}] \otimes \mathbb{F}_{16}[\mathbb{T}_3^{(k,B_{2u})}]}{2} - \frac{\mathbb{X}_{23}[\mathbb{Q}_3^{(a,B_{2u})}] \otimes \mathbb{U}_{13}[\mathbb{T}_2^{(u,B_{1g})}] \otimes \mathbb{F}_{13}[\mathbb{T}_1^{(k,A_{2u})}]}{2} \end{aligned}$$

$$\boxed{\text{No. 33}} \quad \hat{\mathbb{Q}}_2^{(A_{1g})} [M_4, B_2]$$

$$\hat{\mathbb{Z}}_{33} = -\frac{\sqrt{2}\mathbb{X}_{21}[\mathbb{G}_{2,0}^{(a,E_u)}] \otimes \mathbb{Y}_{11}[\mathbb{Q}_{1,0}^{(b,E_u)}]}{2} + \frac{\sqrt{2}\mathbb{X}_{22}[\mathbb{G}_{2,1}^{(a,E_u)}] \otimes \mathbb{Y}_{12}[\mathbb{Q}_{1,1}^{(b,E_u)}]}{2}$$

$$\begin{aligned}
\hat{Z}_{33}(\mathbf{k}) = & -\frac{\sqrt{2}\mathbb{X}_{21}[\mathbb{G}_{2,0}^{(a,Eu)}] \otimes \mathbb{U}_{10}[\mathbb{Q}_1^{(u,A_{2u})}] \otimes \mathbb{F}_{12}[\mathbb{Q}_{2,1}^{(k,E_g)}]}{4} - \frac{\sqrt{2}\mathbb{X}_{21}[\mathbb{G}_{2,0}^{(a,Eu)}] \otimes \mathbb{U}_{11}[\mathbb{Q}_3^{(u,B_{2u})}] \otimes \mathbb{F}_{12}[\mathbb{Q}_{2,1}^{(k,E_g)}]}{4} + \frac{\sqrt{2}\mathbb{X}_{21}[\mathbb{G}_{2,0}^{(a,Eu)}] \otimes \mathbb{U}_{12}[\mathbb{T}_0^{(u,A_{1g})}] \otimes \mathbb{F}_{14}[\mathbb{T}_{1,0}^{(k,E_u)}]}{4} \\
& + \frac{\sqrt{2}\mathbb{X}_{21}[\mathbb{G}_{2,0}^{(a,Eu)}] \otimes \mathbb{U}_{13}[\mathbb{T}_2^{(u,B_{1g})}] \otimes \mathbb{F}_{14}[\mathbb{T}_{1,0}^{(k,E_u)}]}{4} + \frac{\sqrt{2}\mathbb{X}_{22}[\mathbb{G}_{2,1}^{(a,Eu)}] \otimes \mathbb{U}_{10}[\mathbb{Q}_1^{(u,A_{2u})}] \otimes \mathbb{F}_{11}[\mathbb{Q}_{2,0}^{(k,E_g)}]}{4} - \frac{\sqrt{2}\mathbb{X}_{22}[\mathbb{G}_{2,1}^{(a,Eu)}] \otimes \mathbb{U}_{11}[\mathbb{Q}_3^{(u,B_{2u})}] \otimes \mathbb{F}_{11}[\mathbb{Q}_{2,0}^{(k,E_g)}]}{4} \\
& - \frac{\sqrt{2}\mathbb{X}_{22}[\mathbb{G}_{2,1}^{(a,Eu)}] \otimes \mathbb{U}_{12}[\mathbb{T}_0^{(u,A_{1g})}] \otimes \mathbb{F}_{15}[\mathbb{T}_{1,1}^{(k,E_u)}]}{4} + \frac{\sqrt{2}\mathbb{X}_{22}[\mathbb{G}_{2,1}^{(a,Eu)}] \otimes \mathbb{U}_{13}[\mathbb{T}_2^{(u,B_{1g})}] \otimes \mathbb{F}_{15}[\mathbb{T}_{1,1}^{(k,E_u)}]}{4}
\end{aligned}$$

$$\boxed{\text{No. 34}} \quad \hat{\mathbb{Q}}_2^{(A_{1g})} [\mathbb{M}_4, \mathbb{B}_2]$$

$$\hat{Z}_{34} = -\mathbb{X}_{24}[\mathbb{G}_2^{(a,B_{2u})}] \otimes \mathbb{Y}_{13}[\mathbb{Q}_3^{(b,B_{2u})}]$$

$$\begin{aligned}
\hat{Z}_{34}(\mathbf{k}) = & -\frac{\mathbb{X}_{24}[\mathbb{G}_2^{(a,B_{2u})}] \otimes \mathbb{U}_{10}[\mathbb{Q}_1^{(u,A_{2u})}] \otimes \mathbb{F}_{10}[\mathbb{Q}_2^{(k,B_{1g})}]}{2} - \frac{\mathbb{X}_{24}[\mathbb{G}_2^{(a,B_{2u})}] \otimes \mathbb{U}_{11}[\mathbb{Q}_3^{(u,B_{2u})}] \otimes \mathbb{F}_9[\mathbb{Q}_0^{(k,A_{1g})}]}{2} \\
& + \frac{\mathbb{X}_{24}[\mathbb{G}_2^{(a,B_{2u})}] \otimes \mathbb{U}_{12}[\mathbb{T}_0^{(u,A_{1g})}] \otimes \mathbb{F}_{16}[\mathbb{T}_3^{(k,B_{2u})}]}{2} + \frac{\mathbb{X}_{24}[\mathbb{G}_2^{(a,B_{2u})}] \otimes \mathbb{U}_{13}[\mathbb{T}_2^{(u,B_{1g})}] \otimes \mathbb{F}_{13}[\mathbb{T}_1^{(k,A_{2u})}]}{2}
\end{aligned}$$

Table 5: Atomic SAMB group.

| group | bra | ket |
|----------------|---|---|
| M ₁ | $f_{xyz}, f_{ax}, f_{ay}, f_{az}, f_{bx}, f_{by}, f_{bz}$ | $f_{xyz}, f_{ax}, f_{ay}, f_{az}, f_{bx}, f_{by}, f_{bz}$ |
| M ₂ | $d_u, d_v, d_{yz}, d_{zx}, d_{xy}$ | $d_u, d_v, d_{yz}, d_{zx}, d_{xy}$ |
| M ₃ | p_x, p_y, p_z | p_x, p_y, p_z |
| M ₄ | $d_u, d_v, d_{yz}, d_{zx}, d_{xy}$ | p_x, p_y, p_z |

Table 6: Atomic SAMB.

| symbol | type | group | form |
|----------------|-------------------------------|-------|---|
| \mathbb{X}_1 | $\mathbb{Q}_0^{(a,A_{1g})}$ | M_1 | $\begin{pmatrix} \frac{\sqrt{7}}{7} & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & \frac{\sqrt{7}}{7} & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & \frac{\sqrt{7}}{7} & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & \frac{\sqrt{7}}{7} & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & \frac{\sqrt{7}}{7} & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & \frac{\sqrt{7}}{7} & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & \frac{\sqrt{7}}{7} \end{pmatrix}$ |
| \mathbb{X}_2 | $\mathbb{Q}_2^{(a,A_{1g})}$ | M_1 | $\begin{pmatrix} 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & -\frac{\sqrt{21}}{21} & 0 & 0 & \frac{\sqrt{35}}{14} & 0 & 0 \\ 0 & 0 & -\frac{\sqrt{21}}{21} & 0 & 0 & -\frac{\sqrt{35}}{14} & 0 \\ 0 & 0 & 0 & \frac{2\sqrt{21}}{21} & 0 & 0 & 0 \\ 0 & \frac{\sqrt{35}}{14} & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & -\frac{\sqrt{35}}{14} & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 \end{pmatrix}$ |
| \mathbb{X}_3 | $\mathbb{Q}_4^{(a,A_{1g},1)}$ | M_1 | $\begin{pmatrix} -\frac{\sqrt{66}}{11} & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & \frac{\sqrt{66}}{22} & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & \frac{\sqrt{66}}{22} & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & \frac{\sqrt{66}}{22} & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & -\frac{\sqrt{66}}{66} & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & -\frac{\sqrt{66}}{66} & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & -\frac{\sqrt{66}}{66} \end{pmatrix}$ |
| \mathbb{X}_4 | $\mathbb{Q}_4^{(a,A_{1g},2)}$ | M_1 | $\begin{pmatrix} 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & -\frac{\sqrt{2310}}{308} & 0 & 0 & -\frac{3\sqrt{154}}{308} & 0 & 0 \\ 0 & 0 & -\frac{\sqrt{2310}}{308} & 0 & 0 & \frac{3\sqrt{154}}{308} & 0 \\ 0 & 0 & 0 & \frac{\sqrt{2310}}{154} & 0 & 0 & 0 \\ 0 & -\frac{3\sqrt{154}}{308} & 0 & 0 & \frac{\sqrt{2310}}{132} & 0 & 0 \\ 0 & 0 & \frac{3\sqrt{154}}{308} & 0 & 0 & \frac{\sqrt{2310}}{132} & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & -\frac{\sqrt{2310}}{66} \end{pmatrix}$ |

continued ...

Table 6

| symbol | type | group | form |
|----------------|---------------------------------|-------|--|
| \mathbb{X}_5 | $\mathbb{Q}_6^{(a, A_{1g}, 1)}$ | M_1 | $\begin{pmatrix} \frac{2\sqrt{462}}{77} & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & \frac{5\sqrt{462}}{462} & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & \frac{5\sqrt{462}}{462} & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & \frac{5\sqrt{462}}{462} & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & -\frac{3\sqrt{462}}{154} & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & -\frac{3\sqrt{462}}{154} & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & -\frac{3\sqrt{462}}{154} \end{pmatrix}$ |
| \mathbb{X}_6 | $\mathbb{Q}_6^{(a, A_{1g}, 2)}$ | M_1 | $\begin{pmatrix} 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & -\frac{5\sqrt{66}}{132} & 0 & 0 & -\frac{\sqrt{110}}{44} & 0 & 0 \\ 0 & 0 & -\frac{5\sqrt{66}}{132} & 0 & 0 & \frac{\sqrt{110}}{44} & 0 \\ 0 & 0 & 0 & \frac{5\sqrt{66}}{66} & 0 & 0 & 0 \\ 0 & -\frac{\sqrt{110}}{44} & 0 & 0 & -\frac{\sqrt{66}}{44} & 0 & 0 \\ 0 & 0 & \frac{\sqrt{110}}{44} & 0 & 0 & -\frac{\sqrt{66}}{44} & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & \frac{\sqrt{66}}{22} \end{pmatrix}$ |
| \mathbb{X}_7 | $\mathbb{Q}_0^{(a, A_{1g})}$ | M_2 | $\begin{pmatrix} \frac{\sqrt{5}}{5} & 0 & 0 & 0 & 0 \\ 0 & \frac{\sqrt{5}}{5} & 0 & 0 & 0 \\ 0 & 0 & \frac{\sqrt{5}}{5} & 0 & 0 \\ 0 & 0 & 0 & \frac{\sqrt{5}}{5} & 0 \\ 0 & 0 & 0 & 0 & \frac{\sqrt{5}}{5} \end{pmatrix}$ |
| \mathbb{X}_8 | $\mathbb{Q}_2^{(a, A_{1g})}$ | M_2 | $\begin{pmatrix} \frac{\sqrt{14}}{7} & 0 & 0 & 0 & 0 \\ 0 & -\frac{\sqrt{14}}{7} & 0 & 0 & 0 \\ 0 & 0 & \frac{\sqrt{14}}{14} & 0 & 0 \\ 0 & 0 & 0 & \frac{\sqrt{14}}{14} & 0 \\ 0 & 0 & 0 & 0 & -\frac{\sqrt{14}}{7} \end{pmatrix}$ |
| \mathbb{X}_9 | $\mathbb{Q}_4^{(a, A_{1g}, 1)}$ | M_2 | $\begin{pmatrix} \frac{\sqrt{30}}{10} & 0 & 0 & 0 & 0 \\ 0 & \frac{\sqrt{30}}{10} & 0 & 0 & 0 \\ 0 & 0 & -\frac{\sqrt{30}}{15} & 0 & 0 \\ 0 & 0 & 0 & -\frac{\sqrt{30}}{15} & 0 \\ 0 & 0 & 0 & 0 & -\frac{\sqrt{30}}{15} \end{pmatrix}$ |

continued ...

Table 6

| symbol | type | group | form |
|-------------------|-------------------------------|-------|--|
| \mathbb{X}_{10} | $\mathbb{Q}_4^{(a,A_{1g},2)}$ | M_2 | $\begin{pmatrix} \frac{\sqrt{42}}{14} & 0 & 0 & 0 & 0 \\ 0 & -\frac{\sqrt{42}}{14} & 0 & 0 & 0 \\ 0 & 0 & -\frac{\sqrt{42}}{21} & 0 & 0 \\ 0 & 0 & 0 & -\frac{\sqrt{42}}{21} & 0 \\ 0 & 0 & 0 & 0 & \frac{2\sqrt{42}}{21} \end{pmatrix}$ |
| \mathbb{X}_{11} | $\mathbb{Q}_0^{(a,A_{1g})}$ | M_3 | $\begin{pmatrix} \frac{\sqrt{3}}{3} & 0 & 0 \\ 0 & \frac{\sqrt{3}}{3} & 0 \\ 0 & 0 & \frac{\sqrt{3}}{3} \end{pmatrix}$ |
| \mathbb{X}_{12} | $\mathbb{Q}_2^{(a,A_{1g})}$ | M_3 | $\begin{pmatrix} -\frac{\sqrt{6}}{6} & 0 & 0 \\ 0 & -\frac{\sqrt{6}}{6} & 0 \\ 0 & 0 & \frac{\sqrt{6}}{3} \end{pmatrix}$ |
| \mathbb{X}_{13} | $\mathbb{Q}_1^{(a,A_{2u})}$ | M_4 | $\begin{pmatrix} 0 & 0 & \frac{\sqrt{10}}{5} \\ 0 & 0 & 0 \\ 0 & \frac{\sqrt{30}}{10} & 0 \\ \frac{\sqrt{30}}{10} & 0 & 0 \\ 0 & 0 & 0 \end{pmatrix}$ |
| \mathbb{X}_{14} | $\mathbb{Q}_3^{(a,A_{2u})}$ | M_4 | $\begin{pmatrix} 0 & 0 & \frac{\sqrt{15}}{5} \\ 0 & 0 & 0 \\ 0 & -\frac{\sqrt{5}}{5} & 0 \\ -\frac{\sqrt{5}}{5} & 0 & 0 \\ 0 & 0 & 0 \end{pmatrix}$ |
| \mathbb{X}_{15} | $\mathbb{Q}_{1,0}^{(a,E_u)}$ | M_4 | $\begin{pmatrix} -\frac{\sqrt{10}}{10} & 0 & 0 \\ \frac{\sqrt{30}}{10} & 0 & 0 \\ 0 & 0 & 0 \\ 0 & 0 & \frac{\sqrt{30}}{10} \\ 0 & \frac{\sqrt{30}}{10} & 0 \end{pmatrix}$ |
| \mathbb{X}_{16} | $\mathbb{Q}_{1,1}^{(a,E_u)}$ | M_4 | $\begin{pmatrix} 0 & -\frac{\sqrt{10}}{10} & 0 \\ 0 & -\frac{\sqrt{30}}{10} & 0 \\ 0 & 0 & \frac{\sqrt{30}}{10} \\ 0 & 0 & 0 \\ \frac{\sqrt{30}}{10} & 0 & 0 \end{pmatrix}$ |

continued ...

Table 6

| symbol | type | group | form |
|-------------------|--------------------------------|-------|---|
| \mathbb{X}_{17} | $\mathbb{Q}_{3,0}^{(a,E_u,1)}$ | M_4 | $\begin{pmatrix} -\frac{\sqrt{15}}{10} & 0 & 0 \\ \frac{3\sqrt{5}}{10} & 0 & 0 \\ 0 & 0 & 0 \\ 0 & 0 & -\frac{\sqrt{5}}{5} \\ 0 & -\frac{\sqrt{5}}{5} & 0 \end{pmatrix}$ |
| \mathbb{X}_{18} | $\mathbb{Q}_{3,1}^{(a,E_u,1)}$ | M_4 | $\begin{pmatrix} 0 & -\frac{\sqrt{15}}{10} & 0 \\ 0 & -\frac{3\sqrt{5}}{10} & 0 \\ 0 & 0 & -\frac{\sqrt{5}}{5} \\ 0 & 0 & 0 \\ -\frac{\sqrt{5}}{5} & 0 & 0 \end{pmatrix}$ |
| \mathbb{X}_{19} | $\mathbb{Q}_{3,0}^{(a,E_u,2)}$ | M_4 | $\begin{pmatrix} -\frac{1}{2} & 0 & 0 \\ -\frac{\sqrt{3}}{6} & 0 & 0 \\ 0 & 0 & 0 \\ 0 & 0 & -\frac{\sqrt{3}}{3} \\ 0 & \frac{\sqrt{3}}{3} & 0 \end{pmatrix}$ |
| \mathbb{X}_{20} | $\mathbb{Q}_{3,1}^{(a,E_u,2)}$ | M_4 | $\begin{pmatrix} 0 & -\frac{1}{2} & 0 \\ 0 & \frac{\sqrt{3}}{6} & 0 \\ 0 & 0 & -\frac{\sqrt{3}}{3} \\ 0 & 0 & 0 \\ \frac{\sqrt{3}}{3} & 0 & 0 \end{pmatrix}$ |
| \mathbb{X}_{21} | $\mathbb{G}_{2,0}^{(a,E_u)}$ | M_4 | $\begin{pmatrix} -\frac{\sqrt{2}}{2} & 0 & 0 \\ -\frac{\sqrt{6}}{6} & 0 & 0 \\ 0 & 0 & 0 \\ 0 & 0 & \frac{\sqrt{6}}{6} \\ 0 & -\frac{\sqrt{6}}{6} & 0 \end{pmatrix}$ |
| \mathbb{X}_{22} | $\mathbb{G}_{2,1}^{(a,E_u)}$ | M_4 | $\begin{pmatrix} 0 & \frac{\sqrt{2}}{2} & 0 \\ 0 & -\frac{\sqrt{6}}{6} & 0 \\ 0 & 0 & -\frac{\sqrt{6}}{6} \\ 0 & 0 & 0 \\ \frac{\sqrt{6}}{6} & 0 & 0 \end{pmatrix}$ |

continued ...

Table 6

| symbol | type | group | form |
|-------------------|------------------------------|-------|---|
| \mathbb{X}_{23} | $\mathbb{Q}_3^{(a, B_{2u})}$ | M_4 | $\begin{pmatrix} 0 & 0 & 0 \\ 0 & 0 & \frac{\sqrt{3}}{3} \\ 0 & -\frac{\sqrt{3}}{3} & 0 \\ \frac{\sqrt{3}}{3} & 0 & 0 \\ 0 & 0 & 0 \end{pmatrix}$ |
| \mathbb{X}_{24} | $\mathbb{G}_2^{(a, B_{2u})}$ | M_4 | $\begin{pmatrix} 0 & 0 & 0 \\ 0 & 0 & \frac{\sqrt{6}}{3} \\ 0 & \frac{\sqrt{6}}{6} & 0 \\ -\frac{\sqrt{6}}{6} & 0 & 0 \\ 0 & 0 & 0 \end{pmatrix}$ |

Table 7: Cluster SAMB.

| symbol | type | cluster | form |
|-------------------|-------------------------------|---------|---|
| \mathbb{Y}_1 | $\mathbb{Q}_0^{(s, A_{1g})}$ | S_1 | $\begin{pmatrix} \frac{\sqrt{2}}{2} & \frac{\sqrt{2}}{2} \end{pmatrix}$ |
| \mathbb{Y}_2 | $\mathbb{Q}_0^{(s, A_{1g})}$ | S_2 | $\begin{pmatrix} \frac{\sqrt{2}}{2} & \frac{\sqrt{2}}{2} \end{pmatrix}$ |
| \mathbb{Y}_3 | $\mathbb{Q}_0^{(s, A_{1g})}$ | S_3 | $\begin{pmatrix} \frac{\sqrt{2}}{2} & \frac{\sqrt{2}}{2} \end{pmatrix}$ |
| \mathbb{Y}_4 | $\mathbb{Q}_0^{(s, A_{1g})}$ | S_4 | $\begin{pmatrix} \frac{\sqrt{2}}{2} & \frac{\sqrt{2}}{2} \end{pmatrix}$ |
| \mathbb{Y}_5 | $\mathbb{Q}_0^{(s, A_{1g})}$ | S_5 | $\begin{pmatrix} \frac{\sqrt{2}}{2} & \frac{\sqrt{2}}{2} \end{pmatrix}$ |
| \mathbb{Y}_6 | $\mathbb{Q}_1^{(b, A_{2u})}$ | B_1 | $\begin{pmatrix} \frac{\sqrt{2}}{4} & \frac{\sqrt{2}}{4} & -\frac{\sqrt{2}}{4} & -\frac{\sqrt{2}}{4} & -\frac{\sqrt{2}}{4} & -\frac{\sqrt{2}}{4} & \frac{\sqrt{2}}{4} & \frac{\sqrt{2}}{4} \end{pmatrix}$ |
| \mathbb{Y}_7 | $\mathbb{Q}_{1,0}^{(b, E_u)}$ | B_1 | $\begin{pmatrix} \frac{1}{2} & -\frac{1}{2} & \frac{1}{2} & -\frac{1}{2} & 0 & 0 & 0 & 0 \end{pmatrix}$ |
| \mathbb{Y}_8 | $\mathbb{Q}_{1,1}^{(b, E_u)}$ | B_1 | $\begin{pmatrix} 0 & 0 & 0 & 0 & \frac{1}{2} & -\frac{1}{2} & \frac{1}{2} & -\frac{1}{2} \end{pmatrix}$ |
| \mathbb{Y}_9 | $\mathbb{Q}_3^{(b, B_{2u})}$ | B_1 | $\begin{pmatrix} \frac{\sqrt{2}}{4} & \frac{\sqrt{2}}{4} & -\frac{\sqrt{2}}{4} & -\frac{\sqrt{2}}{4} & \frac{\sqrt{2}}{4} & \frac{\sqrt{2}}{4} & -\frac{\sqrt{2}}{4} & -\frac{\sqrt{2}}{4} \end{pmatrix}$ |
| \mathbb{Y}_{10} | $\mathbb{Q}_1^{(b, A_{2u})}$ | B_2 | $\begin{pmatrix} \frac{\sqrt{2}}{4} & \frac{\sqrt{2}}{4} & -\frac{\sqrt{2}}{4} & -\frac{\sqrt{2}}{4} & -\frac{\sqrt{2}}{4} & -\frac{\sqrt{2}}{4} & \frac{\sqrt{2}}{4} & \frac{\sqrt{2}}{4} \end{pmatrix}$ |
| \mathbb{Y}_{11} | $\mathbb{Q}_{1,0}^{(b, E_u)}$ | B_2 | $\begin{pmatrix} \frac{1}{2} & -\frac{1}{2} & \frac{1}{2} & -\frac{1}{2} & 0 & 0 & 0 & 0 \end{pmatrix}$ |
| \mathbb{Y}_{12} | $\mathbb{Q}_{1,1}^{(b, E_u)}$ | B_2 | $\begin{pmatrix} 0 & 0 & 0 & 0 & \frac{1}{2} & -\frac{1}{2} & \frac{1}{2} & -\frac{1}{2} \end{pmatrix}$ |
| \mathbb{Y}_{13} | $\mathbb{Q}_3^{(b, B_{2u})}$ | B_2 | $\begin{pmatrix} \frac{\sqrt{2}}{4} & \frac{\sqrt{2}}{4} & -\frac{\sqrt{2}}{4} & -\frac{\sqrt{2}}{4} & \frac{\sqrt{2}}{4} & \frac{\sqrt{2}}{4} & -\frac{\sqrt{2}}{4} & -\frac{\sqrt{2}}{4} \end{pmatrix}$ |

Table 8: Uniform SAMB.

[illegible]

continued ...

[illegible]

continued ...

[illegible]

continued ...

[illegible]

continued ...

Table 8

| symbol | type | cluster | form |
|-------------------|------------------------------|---------|--|
| \mathbb{U}_{13} | $\mathbb{T}_2^{(u, B_{1g})}$ | B_2 | $\begin{pmatrix} 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & \frac{\sqrt{2}i}{4} & -\frac{\sqrt{2}i}{4} & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & -\frac{\sqrt{2}i}{4} & \frac{\sqrt{2}i}{4} & 0 & 0 \\ 0 & 0 & 0 & 0 & -\frac{\sqrt{2}i}{4} & \frac{\sqrt{2}i}{4} & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & \frac{\sqrt{2}i}{4} & -\frac{\sqrt{2}i}{4} & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \end{pmatrix}$ |

Table 9: Structure SAMB.

| symbol | type | cluster | form |
|-------------------|-------------------------------|---------|---|
| \mathbb{F}_1 | $\mathbb{Q}_0^{(k, A_{1g})}$ | B_1 | $\frac{\sqrt{2}c_{001}}{2} + \frac{\sqrt{2}c_{002}}{2} + \frac{\sqrt{2}c_{005}}{2} + \frac{\sqrt{2}c_{006}}{2}$ |
| \mathbb{F}_2 | $\mathbb{Q}_2^{(k, B_{1g})}$ | B_1 | $\frac{\sqrt{2}c_{001}}{2} + \frac{\sqrt{2}c_{002}}{2} - \frac{\sqrt{2}c_{005}}{2} - \frac{\sqrt{2}c_{006}}{2}$ |
| \mathbb{F}_3 | $\mathbb{Q}_{2,0}^{(k, E_g)}$ | B_1 | $-c_{005} + c_{006}$ |
| \mathbb{F}_4 | $\mathbb{Q}_{2,1}^{(k, E_g)}$ | B_1 | $c_{001} - c_{002}$ |
| \mathbb{F}_5 | $\mathbb{T}_1^{(k, A_{2u})}$ | B_1 | $\frac{\sqrt{2}s_{001}}{2} + \frac{\sqrt{2}s_{002}}{2} - \frac{\sqrt{2}s_{005}}{2} - \frac{\sqrt{2}s_{006}}{2}$ |
| \mathbb{F}_6 | $\mathbb{T}_{1,0}^{(k, Eu)}$ | B_1 | $s_{001} - s_{002}$ |
| \mathbb{F}_7 | $\mathbb{T}_{1,1}^{(k, Eu)}$ | B_1 | $s_{005} - s_{006}$ |
| \mathbb{F}_8 | $\mathbb{T}_3^{(k, B_{2u})}$ | B_1 | $\frac{\sqrt{2}s_{001}}{2} + \frac{\sqrt{2}s_{002}}{2} + \frac{\sqrt{2}s_{005}}{2} + \frac{\sqrt{2}s_{006}}{2}$ |
| \mathbb{F}_9 | $\mathbb{Q}_0^{(k, A_{1g})}$ | B_2 | $\frac{\sqrt{2}c_{009}}{2} + \frac{\sqrt{2}c_{010}}{2} + \frac{\sqrt{2}c_{013}}{2} + \frac{\sqrt{2}c_{014}}{2}$ |
| \mathbb{F}_{10} | $\mathbb{Q}_2^{(k, B_{1g})}$ | B_2 | $\frac{\sqrt{2}c_{009}}{2} + \frac{\sqrt{2}c_{010}}{2} - \frac{\sqrt{2}c_{013}}{2} - \frac{\sqrt{2}c_{014}}{2}$ |
| \mathbb{F}_{11} | $\mathbb{Q}_{2,0}^{(k, E_g)}$ | B_2 | $-c_{013} + c_{014}$ |
| \mathbb{F}_{12} | $\mathbb{Q}_{2,1}^{(k, E_g)}$ | B_2 | $c_{009} - c_{010}$ |
| \mathbb{F}_{13} | $\mathbb{T}_1^{(k, A_{2u})}$ | B_2 | $\frac{\sqrt{2}s_{009}}{2} + \frac{\sqrt{2}s_{010}}{2} - \frac{\sqrt{2}s_{013}}{2} - \frac{\sqrt{2}s_{014}}{2}$ |
| \mathbb{F}_{14} | $\mathbb{T}_{1,0}^{(k, Eu)}$ | B_2 | $s_{009} - s_{010}$ |
| \mathbb{F}_{15} | $\mathbb{T}_{1,1}^{(k, Eu)}$ | B_2 | $s_{013} - s_{014}$ |

continued ...

Table 9

| symbol | type | cluster | form |
|-------------------|------------------------------|---------|---|
| \mathbb{F}_{16} | $\mathbb{T}_3^{(k, B_{2u})}$ | B_2 | $\frac{\sqrt{2}s_{009}}{2} + \frac{\sqrt{2}s_{010}}{2} + \frac{\sqrt{2}s_{013}}{2} + \frac{\sqrt{2}s_{014}}{2}$ |

Table 10: Polar harmonics.

| No. | symbol | rank | irrep. | mul. | comp. | form |
|-----|---------------------|------|----------|------|-------|--|
| 1 | $Q_0^{(A_{1g})}$ | 0 | A_{1g} | — | — | 1 |
| 2 | $Q_1^{(A_{2u})}$ | 1 | A_{2u} | — | — | z |
| 3 | $Q_{1,0}^{(E_u)}$ | 1 | E_u | — | 0 | x |
| 4 | $Q_{1,1}^{(E_u)}$ | 1 | E_u | — | 1 | y |
| 5 | $Q_2^{(A_{1g})}$ | 2 | A_{1g} | — | — | $-\frac{x^2}{2} - \frac{y^2}{2} + z^2$ |
| 6 | $Q_2^{(B_{1g})}$ | 2 | B_{1g} | — | — | $\frac{\sqrt{3}(x-y)(x+y)}{2}$ |
| 7 | $Q_{2,0}^{(E_g)}$ | 2 | E_g | — | 0 | $\sqrt{3}yz$ |
| 8 | $Q_{2,1}^{(E_g)}$ | 2 | E_g | — | 1 | $\sqrt{3}xz$ |
| 9 | $Q_3^{(A_{2u})}$ | 3 | A_{2u} | — | — | $-\frac{z(3x^2+3y^2-2z^2)}{2}$ |
| 10 | $Q_3^{(B_{2u})}$ | 3 | B_{2u} | — | — | $\frac{\sqrt{15}z(x-y)(x+y)}{2}$ |
| 11 | $Q_{3,0}^{(E_u,1)}$ | 3 | E_u | 1 | 0 | $\frac{x(2x^2-3y^2-3z^2)}{2}$ |
| 12 | $Q_{3,1}^{(E_u,1)}$ | 3 | E_u | 1 | 1 | $-\frac{y(3x^2-2y^2+3z^2)}{2}$ |
| 13 | $Q_{3,0}^{(E_u,2)}$ | 3 | E_u | 2 | 0 | $\frac{\sqrt{15}x(y-z)(y+z)}{2}$ |
| 14 | $Q_{3,1}^{(E_u,2)}$ | 3 | E_u | 2 | 1 | $\frac{\sqrt{15}y(x-z)(x+z)}{2}$ |
| 15 | $Q_4^{(A_{1g},1)}$ | 4 | A_{1g} | 1 | — | $\frac{\sqrt{21}(x^4-3x^2y^2-3x^2z^2+y^4-3y^2z^2+z^4)}{2}$ |
| 16 | $Q_4^{(A_{1g},2)}$ | 4 | A_{1g} | 2 | — | $-\frac{\sqrt{15}(x^4-12x^2y^2+6x^2z^2+y^4+6y^2z^2-2z^4)}{12}$ |
| 17 | $Q_6^{(A_{1g},1)}$ | 6 | A_{1g} | 1 | — | $\frac{\sqrt{2} \cdot (2x^6-15x^4y^2-15x^4z^2-15x^2y^4+180x^2y^2z^2-15x^2z^4+2y^6-15y^4z^2-15y^2z^4+2z^6)}{8}$ |
| 18 | $Q_6^{(A_{1g},2)}$ | 6 | A_{1g} | 2 | — | $-\frac{\sqrt{14}(x^6-15x^4z^2+15x^2z^4+y^6-15y^4z^2+15y^2z^4-2z^6)}{8}$ |

Table 11: Axial harmonics.

| No. | symbol | rank | irrep. | mul. | comp. | form |
|-----|----------------------------|------|----------|------|-------|--------------|
| 1 | $\mathbb{G}_2^{(B_{2u})}$ | 2 | B_{2u} | — | — | $\sqrt{3}XY$ |
| 2 | $\mathbb{G}_{2,0}^{(E_u)}$ | 2 | E_u | — | 0 | $\sqrt{3}YZ$ |
| 3 | $\mathbb{G}_{2,1}^{(E_u)}$ | 2 | E_u | — | 1 | $\sqrt{3}XZ$ |

-
- Group info.: Generator = $\{2_{001}|\frac{1}{2}\frac{1}{2}0\}$, $\{4_{001}^+|\frac{1}{2}00\}$, $\{2_{010}|0\frac{1}{2}0\}$, $\{-1|0\}$

Table 12: Conjugacy class (point-group part).

| rep. SO | symmetry operations |
|---------------------------------------|---|
| $\{1 0\}$ | $\{1 0\}$ |
| $\{2_{001} \frac{1}{2}\frac{1}{2}0\}$ | $\{2_{001} \frac{1}{2}\frac{1}{2}0\}$ |
| $\{2_{100} \frac{1}{2}00\}$ | $\{2_{100} \frac{1}{2}00\}$, $\{2_{010} 0\frac{1}{2}0\}$ |
| $\{2_{110} \frac{1}{2}\frac{1}{2}0\}$ | $\{2_{110} \frac{1}{2}\frac{1}{2}0\}$, $\{2_{1-10} 0\}$ |
| $\{4_{001}^+ \frac{1}{2}00\}$ | $\{4_{001}^+ \frac{1}{2}00\}$, $\{4_{001}^- 0\frac{1}{2}0\}$ |
| $\{-1 0\}$ | $\{-1 0\}$ |
| $\{m_{001} \frac{1}{2}\frac{1}{2}0\}$ | $\{m_{001} \frac{1}{2}\frac{1}{2}0\}$ |
| $\{m_{100} \frac{1}{2}00\}$ | $\{m_{100} \frac{1}{2}00\}$, $\{m_{010} 0\frac{1}{2}0\}$ |
| $\{m_{110} \frac{1}{2}\frac{1}{2}0\}$ | $\{m_{110} \frac{1}{2}\frac{1}{2}0\}$, $\{m_{1-10} 0\}$ |
| $\{-4_{001}^+ \frac{1}{2}00\}$ | $\{-4_{001}^+ \frac{1}{2}00\}$, $\{-4_{001}^- 0\frac{1}{2}0\}$ |

Table 13: Symmetry operations.

| No. | SO | No. | SO | No. | SO | No. | SO | No. | SO |
|-----|-----------|-----|---------------------------------------|-----|-----------------------------|-----|-----------------------------|-----|---------------------------------------|
| 1 | $\{1 0\}$ | 2 | $\{2_{001} \frac{1}{2}\frac{1}{2}0\}$ | 3 | $\{2_{100} \frac{1}{2}00\}$ | 4 | $\{2_{010} 0\frac{1}{2}0\}$ | 5 | $\{2_{110} \frac{1}{2}\frac{1}{2}0\}$ |

continued ...

Table 13

| No. | SO | No. | SO | No. | SO | No. | SO | No. | SO |
|-----|--------------------------------|-----|-------------------------------|-----|---------------------------------------|-----|------------------|-----|---------------------------------------|
| 6 | $\{2_{1-10} 0\}$ | 7 | $\{4_{001}^+ \frac{1}{2}00\}$ | 8 | $\{4_{001}^- 0\frac{1}{2}0\}$ | 9 | $\{-1 0\}$ | 10 | $\{m_{001} \frac{1}{2}\frac{1}{2}0\}$ |
| 11 | $\{m_{100} \frac{1}{2}00\}$ | 12 | $\{m_{010} 0\frac{1}{2}0\}$ | 13 | $\{m_{110} \frac{1}{2}\frac{1}{2}0\}$ | 14 | $\{m_{1-10} 0\}$ | 15 | $\{-4_{001}^+ \frac{1}{2}00\}$ |
| 16 | $\{-4_{001}^- 0\frac{1}{2}0\}$ | | | | | | | | |

Table 14: Character table (point-group part).

| | 1 | 2 ₀₀₁ | 2 ₁₀₀ | 2 ₁₁₀ | 4 ₀₀₁ ⁺ | -1 | m ₀₀₁ | m ₁₀₀ | m ₁₁₀ | -4 ₀₀₁ ⁺ |
|------------------------|---|------------------|------------------|------------------|-------------------------------|----|------------------|------------------|------------------|--------------------------------|
| <i>A</i> _{1g} | 1 | 1 | 1 | 1 | 1 | 1 | 1 | 1 | 1 | 1 |
| <i>A</i> _{2g} | 1 | 1 | -1 | -1 | 1 | 1 | 1 | -1 | -1 | 1 |
| <i>B</i> _{1g} | 1 | 1 | 1 | -1 | -1 | 1 | 1 | 1 | -1 | -1 |
| <i>B</i> _{2g} | 1 | 1 | -1 | 1 | -1 | 1 | 1 | -1 | 1 | -1 |
| <i>E</i> _g | 2 | -2 | 0 | 0 | 0 | 2 | -2 | 0 | 0 | 0 |
| <i>A</i> _{1u} | 1 | 1 | 1 | 1 | 1 | -1 | -1 | -1 | -1 | -1 |
| <i>A</i> _{2u} | 1 | 1 | -1 | -1 | 1 | -1 | -1 | 1 | 1 | -1 |
| <i>B</i> _{1u} | 1 | 1 | 1 | -1 | -1 | -1 | -1 | -1 | 1 | 1 |
| <i>B</i> _{2u} | 1 | 1 | -1 | 1 | -1 | -1 | -1 | 1 | -1 | 1 |
| <i>E</i> _u | 2 | -2 | 0 | 0 | 0 | -2 | 2 | 0 | 0 | 0 |

Table 15: Parity conversion.

| \leftrightarrow | \leftrightarrow | \leftrightarrow | \leftrightarrow | \leftrightarrow |
|---|---|---|---|---|
| <i>A</i> _{1g} (<i>A</i> _{1u}) | <i>B</i> _{1g} (<i>B</i> _{1u}) | <i>E</i> _g (<i>E</i> _u) | <i>A</i> _{2g} (<i>A</i> _{2u}) | <i>B</i> _{2g} (<i>B</i> _{2u}) |
| <i>A</i> _{1u} (<i>A</i> _{1g}) | <i>B</i> _{1u} (<i>B</i> _{1g}) | <i>E</i> _u (<i>E</i> _g) | <i>A</i> _{2u} (<i>A</i> _{2g}) | <i>B</i> _{2u} (<i>B</i> _{2g}) |

Table 16: Symmetric product, $[\Gamma \otimes \Gamma']_+$.

| | A_{1g} | A_{2g} | B_{1g} | B_{2g} | E_g | A_{1u} | A_{2u} | B_{1u} | B_{2u} | E_u |
|----------|----------|----------|----------|----------|----------------------------|----------|----------|----------|----------|-------------------------------------|
| A_{1g} | A_{1g} | A_{2g} | B_{1g} | B_{2g} | E_g | A_{1u} | A_{2u} | B_{1u} | B_{2u} | E_u |
| A_{2g} | | A_{1g} | B_{2g} | B_{1g} | E_g | A_{2u} | A_{1u} | B_{2u} | B_{1u} | E_u |
| B_{1g} | | | A_{1g} | A_{2g} | E_g | B_{1u} | B_{2u} | A_{1u} | A_{2u} | E_u |
| B_{2g} | | | | A_{1g} | E_g | B_{2u} | B_{1u} | A_{2u} | A_{1u} | E_u |
| E_g | | | | | $A_{1g} + B_{1g} + B_{2g}$ | E_u | E_u | E_u | E_u | $A_{1u} + A_{2u} + B_{1u} + B_{2u}$ |
| A_{1u} | | | | | | A_{1g} | A_{2g} | B_{1g} | B_{2g} | E_g |
| A_{2u} | | | | | | | A_{1g} | B_{2g} | B_{1g} | E_g |
| B_{1u} | | | | | | | | A_{1g} | A_{2g} | E_g |
| B_{2u} | | | | | | | | | A_{1g} | E_g |
| E_u | | | | | | | | | | $A_{1g} + B_{1g} + B_{2g}$ |

Table 17: Anti-symmetric product, $[\Gamma \otimes \Gamma]_-$.

| A_{1g} | A_{2g} | B_{1g} | B_{2g} | E_g | A_{1u} | A_{2u} | B_{1u} | B_{2u} | E_u |
|----------|----------|----------|----------|----------|----------|----------|----------|----------|----------|
| - | - | - | - | A_{2g} | - | - | - | - | A_{2g} |

Table 18: Virtual-cluster sites.

| No. | position | No. | position | No. | position | No. | position |
|-----|--|-----|--|-----|---|-----|---|
| 1 | $\begin{pmatrix} 2 & 1 & 1 \end{pmatrix}$ | 2 | $\begin{pmatrix} -2 & -1 & 1 \end{pmatrix}$ | 3 | $\begin{pmatrix} 2 & -1 & -1 \end{pmatrix}$ | 4 | $\begin{pmatrix} -2 & 1 & -1 \end{pmatrix}$ |
| 5 | $\begin{pmatrix} 1 & 2 & -1 \end{pmatrix}$ | 6 | $\begin{pmatrix} -1 & -2 & -1 \end{pmatrix}$ | 7 | $\begin{pmatrix} -1 & 2 & 1 \end{pmatrix}$ | 8 | $\begin{pmatrix} 1 & -2 & 1 \end{pmatrix}$ |
| 9 | $\begin{pmatrix} -2 & -1 & -1 \end{pmatrix}$ | 10 | $\begin{pmatrix} 2 & 1 & -1 \end{pmatrix}$ | 11 | $\begin{pmatrix} -2 & 1 & 1 \end{pmatrix}$ | 12 | $\begin{pmatrix} 2 & -1 & 1 \end{pmatrix}$ |
| 13 | $\begin{pmatrix} -1 & -2 & 1 \end{pmatrix}$ | 14 | $\begin{pmatrix} 1 & 2 & 1 \end{pmatrix}$ | 15 | $\begin{pmatrix} 1 & -2 & -1 \end{pmatrix}$ | 16 | $\begin{pmatrix} -1 & 2 & -1 \end{pmatrix}$ |

Table 19: Virtual-cluster basis.

| symbol | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | 10 |
|--------------------------------|-------------------------|-------------------------|-------------------------|-------------------------|-------------------------|-------------------------|-------------------------|-------------------------|-------------------------|-------------------------|
| $\mathbb{Q}_0^{(A_{1g})}$ | $\frac{1}{4}$ | $\frac{1}{4}$ | $\frac{1}{4}$ | $\frac{1}{4}$ | $\frac{1}{4}$ | $\frac{1}{4}$ | $\frac{1}{4}$ | $\frac{1}{4}$ | $\frac{1}{4}$ | $\frac{1}{4}$ |
| $\mathbb{Q}_1^{(A_{2u})}$ | $\frac{1}{4}$ | $\frac{1}{4}$ | $-\frac{1}{4}$ | $-\frac{1}{4}$ | $-\frac{1}{4}$ | $-\frac{1}{4}$ | $\frac{1}{4}$ | $\frac{1}{4}$ | $-\frac{1}{4}$ | $-\frac{1}{4}$ |
| $\mathbb{Q}_{1,0}^{(E_u)}$ | $\frac{\sqrt{10}}{10}$ | $-\frac{\sqrt{10}}{10}$ | $\frac{\sqrt{10}}{10}$ | $-\frac{\sqrt{10}}{10}$ | $\frac{\sqrt{10}}{20}$ | $-\frac{\sqrt{10}}{20}$ | $-\frac{\sqrt{10}}{20}$ | $\frac{\sqrt{10}}{20}$ | $-\frac{\sqrt{10}}{10}$ | $\frac{\sqrt{10}}{10}$ |
| $\mathbb{Q}_{1,1}^{(E_u)}$ | $-\frac{\sqrt{10}}{10}$ | $\frac{\sqrt{10}}{10}$ | $-\frac{\sqrt{10}}{20}$ | $\frac{\sqrt{10}}{20}$ | $\frac{\sqrt{10}}{20}$ | $-\frac{\sqrt{10}}{20}$ | $\frac{\sqrt{10}}{10}$ | $-\frac{\sqrt{10}}{10}$ | $-\frac{\sqrt{10}}{20}$ | $\frac{\sqrt{10}}{20}$ |
| $\mathbb{Q}_2^{(B_{1g})}$ | $\frac{1}{4}$ | $\frac{1}{4}$ | $\frac{1}{4}$ | $\frac{1}{4}$ | $-\frac{1}{4}$ | $-\frac{1}{4}$ | $-\frac{1}{4}$ | $-\frac{1}{4}$ | $\frac{1}{4}$ | $\frac{1}{4}$ |
| $\mathbb{Q}_2^{(B_{2g})}$ | $\frac{1}{4}$ | $\frac{1}{4}$ | $-\frac{1}{4}$ | $-\frac{1}{4}$ | $\frac{1}{4}$ | $\frac{1}{4}$ | $-\frac{1}{4}$ | $-\frac{1}{4}$ | $\frac{1}{4}$ | $\frac{1}{4}$ |
| $\mathbb{Q}_{2,0}^{(E_g)}$ | $\frac{\sqrt{10}}{20}$ | $-\frac{\sqrt{10}}{20}$ | $\frac{\sqrt{10}}{20}$ | $-\frac{\sqrt{10}}{20}$ | $-\frac{\sqrt{10}}{10}$ | $\frac{\sqrt{10}}{10}$ | $\frac{\sqrt{10}}{10}$ | $-\frac{\sqrt{10}}{10}$ | $\frac{\sqrt{10}}{20}$ | $-\frac{\sqrt{10}}{20}$ |
| $\mathbb{Q}_{2,1}^{(E_g)}$ | $\frac{\sqrt{10}}{10}$ | $-\frac{\sqrt{10}}{10}$ | $-\frac{\sqrt{10}}{10}$ | $\frac{\sqrt{10}}{10}$ | $-\frac{\sqrt{10}}{20}$ | $\frac{\sqrt{10}}{20}$ | $-\frac{\sqrt{10}}{20}$ | $\frac{\sqrt{10}}{20}$ | $\frac{\sqrt{10}}{10}$ | $-\frac{\sqrt{10}}{10}$ |
| $\mathbb{Q}_3^{(B_{1u})}$ | $\frac{1}{4}$ | $\frac{1}{4}$ | $\frac{1}{4}$ | $\frac{1}{4}$ | $-\frac{1}{4}$ | $-\frac{1}{4}$ | $-\frac{1}{4}$ | $-\frac{1}{4}$ | $-\frac{1}{4}$ | $-\frac{1}{4}$ |
| $\mathbb{Q}_3^{(B_{2u})}$ | $\frac{1}{4}$ | $\frac{1}{4}$ | $-\frac{1}{4}$ | $-\frac{1}{4}$ | $\frac{1}{4}$ | $\frac{1}{4}$ | $-\frac{1}{4}$ | $-\frac{1}{4}$ | $-\frac{1}{4}$ | $-\frac{1}{4}$ |
| $\mathbb{Q}_{3,0}^{(E_{u,1})}$ | $\frac{\sqrt{10}}{20}$ | $-\frac{\sqrt{10}}{20}$ | $\frac{\sqrt{10}}{20}$ | $-\frac{\sqrt{10}}{20}$ | $-\frac{\sqrt{10}}{10}$ | $\frac{\sqrt{10}}{10}$ | $\frac{\sqrt{10}}{10}$ | $-\frac{\sqrt{10}}{10}$ | $-\frac{\sqrt{10}}{20}$ | $\frac{\sqrt{10}}{20}$ |
| $\mathbb{Q}_{3,1}^{(E_{u,1})}$ | $-\frac{\sqrt{10}}{10}$ | $\frac{\sqrt{10}}{10}$ | $\frac{\sqrt{10}}{10}$ | $-\frac{\sqrt{10}}{10}$ | $\frac{\sqrt{10}}{20}$ | $-\frac{\sqrt{10}}{20}$ | $\frac{\sqrt{10}}{20}$ | $-\frac{\sqrt{10}}{20}$ | $\frac{\sqrt{10}}{10}$ | $-\frac{\sqrt{10}}{10}$ |
| $\mathbb{Q}_4^{(A_{2g})}$ | $\frac{1}{4}$ | $\frac{1}{4}$ | $-\frac{1}{4}$ | $-\frac{1}{4}$ | $-\frac{1}{4}$ | $-\frac{1}{4}$ | $\frac{1}{4}$ | $\frac{1}{4}$ | $\frac{1}{4}$ | $\frac{1}{4}$ |
| $\mathbb{Q}_{4,0}^{(E_{g,1})}$ | $-\frac{\sqrt{10}}{10}$ | $\frac{\sqrt{10}}{10}$ | $-\frac{\sqrt{10}}{10}$ | $\frac{\sqrt{10}}{10}$ | $-\frac{\sqrt{10}}{20}$ | $\frac{\sqrt{10}}{20}$ | $\frac{\sqrt{10}}{20}$ | $-\frac{\sqrt{10}}{20}$ | $-\frac{\sqrt{10}}{10}$ | $\frac{\sqrt{10}}{10}$ |
| $\mathbb{Q}_{4,1}^{(E_{g,1})}$ | $\frac{\sqrt{10}}{20}$ | $-\frac{\sqrt{10}}{20}$ | $-\frac{\sqrt{10}}{20}$ | $\frac{\sqrt{10}}{20}$ | $\frac{\sqrt{10}}{10}$ | $-\frac{\sqrt{10}}{10}$ | $\frac{\sqrt{10}}{10}$ | $-\frac{\sqrt{10}}{10}$ | $\frac{\sqrt{10}}{20}$ | $-\frac{\sqrt{10}}{20}$ |

continued ...

Table 19

| symbol | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | 10 |
|---------------------------|-------------------------|------------------------|------------------------|-------------------------|------------------------|-------------------------|---------------|---------------|----------------|----------------|
| | $-\frac{\sqrt{10}}{20}$ | $\frac{\sqrt{10}}{20}$ | $\frac{\sqrt{10}}{10}$ | $-\frac{\sqrt{10}}{10}$ | $\frac{\sqrt{10}}{10}$ | $-\frac{\sqrt{10}}{10}$ | | | | |
| $\mathbb{Q}_5^{(A_{1u})}$ | $\frac{1}{4}$ | $\frac{1}{4}$ | $\frac{1}{4}$ | $\frac{1}{4}$ | $\frac{1}{4}$ | $\frac{1}{4}$ | $\frac{1}{4}$ | $\frac{1}{4}$ | $-\frac{1}{4}$ | $-\frac{1}{4}$ |
| | $-\frac{1}{4}$ | $-\frac{1}{4}$ | $-\frac{1}{4}$ | $-\frac{1}{4}$ | $-\frac{1}{4}$ | $-\frac{1}{4}$ | | | | |