

PG No. 1 C_1 1 [triclinic] (axial, internal polar quadrupole)

* Harmonics for rank 0

* Harmonics for rank 1

$$\vec{\mathbb{G}}_1^{(2,1)}[q](A, 1)$$

** symmetry

x

** expression

$$-\frac{3\sqrt{10}Q_uyz}{10} - \frac{\sqrt{30}Q_vyz}{10} + \frac{\sqrt{30}Q_{xy}xz}{10} - \frac{\sqrt{30}Q_{xz}xy}{10} - \frac{\sqrt{30}Q_{yz}(y-z)(y+z)}{10}$$

$$\vec{\mathbb{G}}_1^{(2,1)}[q](A, 2)$$

** symmetry

y

** expression

$$\frac{3\sqrt{10}Q_uxz}{10} - \frac{\sqrt{30}Q_vxz}{10} - \frac{\sqrt{30}Q_{xy}yz}{10} + \frac{\sqrt{30}Q_{xz}(x-z)(x+z)}{10} + \frac{\sqrt{30}Q_{yz}xy}{10}$$

$$\vec{\mathbb{G}}_1^{(2,1)}[q](A, 3)$$

** symmetry

z

** expression

$$\frac{\sqrt{30}Q_vxy}{5} - \frac{\sqrt{30}Q_{xy}(x-y)(x+y)}{10} + \frac{\sqrt{30}Q_{xz}yz}{10} - \frac{\sqrt{30}Q_{yz}xz}{10}$$

* Harmonics for rank 2

$$\vec{\mathbb{G}}_2^{(2,-1)}[q](A, 1)$$

** symmetry

$$-\frac{x^2}{2} - \frac{y^2}{2} + z^2$$

** expression

$$\frac{\sqrt{2}Q_{xzy}}{2} - \frac{\sqrt{2}Q_{yzx}}{2}$$

$$\vec{\mathbb{G}}_2^{(2,-1)}[q](A, 2)$$

** symmetry

$$\frac{\sqrt{3}(x-y)(x+y)}{2}$$

** expression

$$\frac{\sqrt{6}Q_{xy}z}{3} - \frac{\sqrt{6}Q_{xz}y}{6} - \frac{\sqrt{6}Q_{yz}x}{6}$$

$$\vec{\mathbb{G}}_2^{(2,-1)}[q](A, 3)$$

** symmetry

$\sqrt{3}yz$

** expression

$$\frac{\sqrt{2}Q_ux}{2} + \frac{\sqrt{6}Q_vx}{6} + \frac{\sqrt{6}Q_{xy}y}{6} - \frac{\sqrt{6}Q_{xz}z}{6}$$

$$\vec{\mathbb{G}}_2^{(2,-1)}[q](A, 4)$$

** symmetry

$\sqrt{3}xz$

** expression

$$-\frac{\sqrt{2}Q_uy}{2} + \frac{\sqrt{6}Q_vy}{6} - \frac{\sqrt{6}Q_{xy}x}{6} + \frac{\sqrt{6}Q_{yz}z}{6}$$

$$\vec{\mathbb{G}}_2^{(2,-1)}[q](A, 5)$$

** symmetry

$\sqrt{3}xy$

** expression

$$-\frac{\sqrt{6}Q_vz}{3} + \frac{\sqrt{6}Q_{xz}x}{6} - \frac{\sqrt{6}Q_{yz}y}{6}$$

$\vec{\mathbb{G}}_2^{(2,1)}[q](A, 1)$

** symmetry

$$-\frac{x^2}{2} - \frac{y^2}{2} + z^2$$

** expression

$$\frac{5\sqrt{42}Q_vxyz}{14} - \frac{5\sqrt{42}Q_{xyz}(x-y)(x+y)}{28} - \frac{\sqrt{42}Q_{xz}y(x^2+y^2-4z^2)}{28} + \frac{\sqrt{42}Q_{yz}x(x^2+y^2-4z^2)}{28}$$

$\vec{\mathbb{G}}_2^{(2,1)}[q](A, 2)$

** symmetry

$$\frac{\sqrt{3}(x-y)(x+y)}{2}$$

** expression

$$-\frac{5\sqrt{42}Q_{uxyz}}{14} + \frac{\sqrt{14}Q_{xy}z(3x^2+3y^2-2z^2)}{28} - \frac{\sqrt{14}Q_{xz}y(9x^2-y^2-6z^2)}{28} + \frac{\sqrt{14}Q_{yz}x(x^2-9y^2+6z^2)}{28}$$

$\vec{\mathbb{G}}_2^{(2,1)}[q](A, 3)$

** symmetry

$$\sqrt{3}yz$$

** expression

$$-\frac{\sqrt{42}Q_ux(x^2+y^2-4z^2)}{28} - \frac{\sqrt{14}Q_vx(x^2-9y^2+6z^2)}{28} - \frac{\sqrt{14}Q_{xy}y(3x^2-2y^2+3z^2)}{14} + \frac{\sqrt{14}Q_{xz}z(3x^2+3y^2-2z^2)}{14}$$

$\vec{\mathbb{G}}_2^{(2,1)}[q](A, 4)$

** symmetry

$$\sqrt{3}xz$$

** expression

$$\frac{\sqrt{42}Q_uy(x^2+y^2-4z^2)}{28} + \frac{\sqrt{14}Q_vy(9x^2-y^2-6z^2)}{28} - \frac{\sqrt{14}Q_{xy}x(2x^2-3y^2-3z^2)}{14} - \frac{\sqrt{14}Q_{yz}z(3x^2+3y^2-2z^2)}{14}$$

$\vec{\mathbb{G}}_2^{(2,1)}[q](A, 5)$

** symmetry

$$\sqrt{3}xy$$

** expression

$$\frac{5\sqrt{42}Q_uz(x-y)(x+y)}{28} - \frac{\sqrt{14}Q_vz(3x^2+3y^2-2z^2)}{28} + \frac{\sqrt{14}Q_{xz}x(2x^2-3y^2-3z^2)}{14} + \frac{\sqrt{14}Q_{yz}y(3x^2-2y^2+3z^2)}{14}$$

* Harmonics for rank 3

$\vec{\mathbb{G}}_3^{(2,-1)}[q](A, 1)$

** symmetry

$$\sqrt{15}xyz$$

** expression

$$\frac{\sqrt{6}Q_u(x-y)(x+y)}{4} + \frac{\sqrt{2}Q_v(x^2+y^2-2z^2)}{4}$$

$\vec{\mathbb{G}}_3^{(2,-1)}[q](A, 2)$

** symmetry

$$\frac{x(2x^2-3y^2-3z^2)}{2}$$

** expression

$$\frac{3\sqrt{10}Q_uyz}{20} + \frac{\sqrt{30}Q_vyz}{20} + \frac{\sqrt{30}Q_{xy}xz}{5} - \frac{\sqrt{30}Q_{xz}xy}{5} + \frac{\sqrt{30}Q_{yz}(y-z)(y+z)}{20}$$

$\vec{\mathbb{G}}_3^{(2,-1)}[q](A, 3)$

** symmetry

$$-\frac{y(3x^2 - 2y^2 + 3z^2)}{2}$$

** expression

$$-\frac{3\sqrt{10}Q_uxz}{20} + \frac{\sqrt{30}Q_vxz}{20} - \frac{\sqrt{30}Q_{xy}yz}{5} - \frac{\sqrt{30}Q_{xz}(x-z)(x+z)}{20} + \frac{\sqrt{30}Q_{yz}xy}{5}$$

$\vec{\mathbb{G}}_3^{(2,-1)}[q](A, 4)$

** symmetry

$$-\frac{z(3x^2 + 3y^2 - 2z^2)}{2}$$

** expression

$$-\frac{\sqrt{30}Q_vxy}{10} + \frac{\sqrt{30}Q_{xy}(x-y)(x+y)}{20} + \frac{\sqrt{30}Q_{xz}yz}{5} - \frac{\sqrt{30}Q_{yz}xz}{5}$$

$\vec{\mathbb{G}}_3^{(2,-1)}[q](A, 5)$

** symmetry

$$\frac{\sqrt{15}x(y-z)(y+z)}{2}$$

** expression

$$\frac{\sqrt{6}Q_uyz}{4} - \frac{3\sqrt{2}Q_vyz}{4} + \frac{\sqrt{2}Q_{yz}(2x^2 - y^2 - z^2)}{4}$$

$\vec{\mathbb{G}}_3^{(2,-1)}[q](A, 6)$

** symmetry

$$-\frac{\sqrt{15}y(x-z)(x+z)}{2}$$

** expression

$$\frac{\sqrt{6}Q_uxz}{4} + \frac{3\sqrt{2}Q_vxz}{4} - \frac{\sqrt{2}Q_{xz}(x^2 - 2y^2 + z^2)}{4}$$

$\vec{\mathbb{G}}_3^{(2,-1)}[q](A, 7)$

** symmetry

$$\frac{\sqrt{15}z(x-y)(x+y)}{2}$$

** expression

$$-\frac{\sqrt{6}Q_uxy}{2} - \frac{\sqrt{2}Q_{xy}(x^2 + y^2 - 2z^2)}{4}$$

$\vec{\mathbb{G}}_3^{(2,1)}[q](A, 1)$

** symmetry

$$\sqrt{15}xyz$$

** expression

$$-\frac{\sqrt{3}Q_u(x-y)(x+y)(x^2 + y^2 - 6z^2)}{6} - \frac{Q_v(x^4 - 12x^2y^2 + 6x^2z^2 + y^4 + 6y^2z^2 - 2z^4)}{6} \\ - \frac{7Q_{xy}xy(x-y)(x+y)}{6} + \frac{7Q_{xz}xz(x-z)(x+z)}{6} - \frac{7Q_{yz}yz(y-z)(y+z)}{6}$$

$\vec{\mathbb{G}}_3^{(2,1)}[q](A, 2)$

** symmetry

$$\frac{x(2x^2 - 3y^2 - 3z^2)}{2}$$

** expression

$$-\frac{\sqrt{5}Q_uyz(6x^2 - y^2 - z^2)}{4} - \frac{\sqrt{15}Q_vyz(6x^2 - y^2 - z^2)}{12} + \frac{\sqrt{15}Q_{xy}xz(4x^2 - 3y^2 - 3z^2)}{12} \\ - \frac{\sqrt{15}Q_{xz}xy(4x^2 - 3y^2 - 3z^2)}{12} - \frac{\sqrt{15}Q_{yz}(y-z)(y+z)(6x^2 - y^2 - z^2)}{12}$$

$\vec{\mathbb{G}}_3^{(2,1)}[q](A, 3)$

** symmetry

$$-\frac{y(3x^2 - 2y^2 + 3z^2)}{2}$$

** expression

$$-\frac{\sqrt{5}Q_{uz}(x^2 - 6y^2 + z^2)}{4} + \frac{\sqrt{15}Q_{vxz}(x^2 - 6y^2 + z^2)}{12} + \frac{\sqrt{15}Q_{xyyz}(3x^2 - 4y^2 + 3z^2)}{12} \\ - \frac{\sqrt{15}Q_{xz}(x-z)(x+z)(x^2 - 6y^2 + z^2)}{12} - \frac{\sqrt{15}Q_{yzxy}(3x^2 - 4y^2 + 3z^2)}{12}$$

$\vec{\mathbb{G}}_3^{(2,1)}[q](A, 4)$

** symmetry

$$-\frac{z(3x^2 + 3y^2 - 2z^2)}{2}$$

** expression

$$-\frac{\sqrt{15}Q_{vxy}(x^2 + y^2 - 6z^2)}{6} + \frac{\sqrt{15}Q_{xy}(x-y)(x+y)(x^2 + y^2 - 6z^2)}{12} - \frac{\sqrt{15}Q_{xzxyz}(3x^2 + 3y^2 - 4z^2)}{12} + \frac{\sqrt{15}Q_{yzxz}(3x^2 + 3y^2 - 4z^2)}{12}$$

$\vec{\mathbb{G}}_3^{(2,1)}[q](A, 5)$

** symmetry

$$\frac{\sqrt{15}x(y-z)(y+z)}{2}$$

** expression

$$\frac{\sqrt{3}Q_{uyz}(12x^2 - 9y^2 + 5z^2)}{12} - \frac{Q_{vyz}(36x^2 + y^2 - 13z^2)}{12} + \frac{7Q_{xyxz}(2x^2 - 3y^2 - z^2)}{12} \\ + \frac{7Q_{xzxy}(2x^2 - y^2 - 3z^2)}{12} - \frac{Q_{yz}(4x^4 - 12x^2y^2 - 12x^2z^2 + 5y^4 - 18y^2z^2 + 5z^4)}{12}$$

$\vec{\mathbb{G}}_3^{(2,1)}[q](A, 6)$

** symmetry

$$-\frac{\sqrt{15}y(x-z)(x+z)}{2}$$

** expression

$$-\frac{\sqrt{3}Q_{uxz}(9x^2 - 12y^2 - 5z^2)}{12} + \frac{Q_{vxz}(x^2 + 36y^2 - 13z^2)}{12} - \frac{7Q_{xyyz}(3x^2 - 2y^2 + z^2)}{12} \\ - \frac{Q_{xz}(5x^4 - 12x^2y^2 - 18x^2z^2 + 4y^4 - 12y^2z^2 + 5z^4)}{12} - \frac{7Q_{yzxy}(x^2 - 2y^2 + 3z^2)}{12}$$

$\vec{\mathbb{G}}_3^{(2,1)}[q](A, 7)$

** symmetry

$$\frac{\sqrt{15}z(x-y)(x+y)}{2}$$

** expression

$$\frac{\sqrt{3}Q_{uxy}(x^2 + y^2 - 6z^2)}{3} + \frac{7Q_{vxy}(x-y)(x+y)}{6} - \frac{Q_{xy}(5x^4 - 18x^2y^2 - 12x^2z^2 + 5y^4 - 12y^2z^2 + 4z^4)}{12} \\ - \frac{7Q_{xzxyz}(3x^2 + y^2 - 2z^2)}{12} - \frac{7Q_{yzxz}(x^2 + 3y^2 - 2z^2)}{12}$$

* Harmonics for rank 4

$\vec{\mathbb{G}}_4^{(2,-1)}[q](A, 1)$

** symmetry

$$\frac{\sqrt{21}(x^4 - 3x^2y^2 - 3x^2z^2 + y^4 - 3y^2z^2 + z^4)}{6}$$

** expression

$$\frac{\sqrt{5}Q_{xyz}(x-y)(x+y)}{2} - \frac{\sqrt{5}Q_{xz}(x-z)(x+z)}{2} + \frac{\sqrt{5}Q_{yzx}(y-z)(y+z)}{2}$$

$\vec{\mathbb{G}}_4^{(2,-1)}[q](A, 2)$

** symmetry

$$-\frac{\sqrt{15}(x^4 - 12x^2y^2 + 6x^2z^2 + y^4 + 6y^2z^2 - 2z^4)}{12}$$

** expression

$$-\frac{6\sqrt{7}Q_{uxyz}}{7} - \frac{\sqrt{7}Q_{xyz}(x-y)(x+y)}{14} + \frac{\sqrt{7}Q_{xxz}(4x^2-3y^2+5z^2)}{14} + \frac{\sqrt{7}Q_{yzx}(3x^2-4y^2-5z^2)}{14}$$

$\vec{\mathbb{G}}_4^{(2,-1)}[q](A, 3)$

** symmetry

$$\frac{\sqrt{5}(x-y)(x+y)(x^2+y^2-6z^2)}{4}$$

** expression

$$\frac{6\sqrt{7}Q_{uxxyz}}{7} + \frac{\sqrt{21}Q_{xyz}(3x^2+3y^2-2z^2)}{14} - \frac{\sqrt{21}Q_{xz}(2x^2-y^2+z^2)}{14} + \frac{\sqrt{21}Q_{yzx}(x^2-2y^2-z^2)}{14}$$

$\vec{\mathbb{G}}_4^{(2,-1)}[q](A, 4)$

** symmetry

$$\frac{\sqrt{35}yz(y-z)(y+z)}{2}$$

** expression

$$\frac{3Q_{ux}(y-z)(y+z)}{4} + \frac{\sqrt{3}Q_vx(y-z)(y+z)}{4} + \frac{\sqrt{3}Q_{xy}y(y^2-3z^2)}{4} - \frac{\sqrt{3}Q_{xz}z(3y^2-z^2)}{4} + \sqrt{3}Q_{yz}xyz$$

$\vec{\mathbb{G}}_4^{(2,-1)}[q](A, 5)$

** symmetry

$$-\frac{\sqrt{35}xz(x-z)(x+z)}{2}$$

** expression

$$\frac{3Q_{uy}(x-z)(x+z)}{4} - \frac{\sqrt{3}Q_vy(x-z)(x+z)}{4} + \frac{\sqrt{3}Q_{xy}x(x^2-3z^2)}{4} + \sqrt{3}Q_{xz}xyz - \frac{\sqrt{3}Q_{yz}z(3x^2-z^2)}{4}$$

$\vec{\mathbb{G}}_4^{(2,-1)}[q](A, 6)$

** symmetry

$$\frac{\sqrt{35}xy(x-y)(x+y)}{2}$$

** expression

$$-\frac{\sqrt{3}Q_vz(x-y)(x+y)}{2} + \sqrt{3}Q_{xy}xyz + \frac{\sqrt{3}Q_{xz}x(x^2-3y^2)}{4} - \frac{\sqrt{3}Q_{yz}y(3x^2-y^2)}{4}$$

$\vec{\mathbb{G}}_4^{(2,-1)}[q](A, 7)$

** symmetry

$$\frac{\sqrt{5}yz(6x^2-y^2-z^2)}{2}$$

** expression

$$\frac{3\sqrt{7}Q_{ux}(2x^2-5y^2-z^2)}{28} + \frac{\sqrt{21}Q_vx(2x^2+3y^2-9z^2)}{28} - \frac{\sqrt{21}Q_{xy}y(2x^2+y^2-5z^2)}{28} + \frac{\sqrt{21}Q_{xz}z(2x^2-5y^2+z^2)}{28}$$

$\vec{\mathbb{G}}_4^{(2,-1)}[q](A, 8)$

** symmetry

$$-\frac{\sqrt{5}xz(x^2-6y^2+z^2)}{2}$$

** expression

$$\frac{3\sqrt{7}Q_{uy}(5x^2-2y^2+z^2)}{28} + \frac{\sqrt{21}Q_vy(3x^2+2y^2-9z^2)}{28} + \frac{\sqrt{21}Q_{xy}x(x^2+2y^2-5z^2)}{28} + \frac{\sqrt{21}Q_{yz}z(5x^2-2y^2-z^2)}{28}$$

$\vec{\mathbb{G}}_4^{(2,-1)}[q](A, 9)$

** symmetry

$$-\frac{\sqrt{5}xy(x^2+y^2-6z^2)}{2}$$

** expression

$$\frac{3\sqrt{7}Q_{uz}(x-y)(x+y)}{7} + \frac{\sqrt{21}Q_vz(3x^2+3y^2-2z^2)}{14} - \frac{\sqrt{21}Q_{xz}x(x^2-5y^2+2z^2)}{28} - \frac{\sqrt{21}Q_{yz}y(5x^2-y^2-2z^2)}{28}$$

$$\tilde{\mathbb{G}}_4^{(2,1)}[q](A, 1)$$

** symmetry

$$\frac{\sqrt{21} (x^4 - 3x^2y^2 - 3x^2z^2 + y^4 - 3y^2z^2 + z^4)}{6}$$

** expression

$$-\frac{3\sqrt{2310}Q_uxyz(x-y)(x+y)}{44} - \frac{3\sqrt{770}Q_vxyz(x^2+y^2-2z^2)}{44} + \frac{\sqrt{770}Q_{xy}z(x-y)(x+y)(x^2+y^2-2z^2)}{22} \\ - \frac{\sqrt{770}Q_{xz}y(x-z)(x+z)(x^2-2y^2+z^2)}{22} - \frac{\sqrt{770}Q_{yz}x(y-z)(y+z)(2x^2-y^2-z^2)}{22}$$

$$\tilde{\mathbb{G}}_4^{(2,1)}[q](A, 2)$$

** symmetry

$$-\frac{\sqrt{15} (x^4 - 12x^2y^2 + 6x^2z^2 + y^4 + 6y^2z^2 - 2z^4)}{12}$$

** expression

$$\frac{21\sqrt{66}Q_uxyz(x-y)(x+y)}{44} - \frac{21\sqrt{22}Q_vxyz(x^2+y^2-2z^2)}{44} + \frac{7\sqrt{22}Q_{xy}z(x-y)(x+y)(x^2+y^2-2z^2)}{44} \\ + \frac{\sqrt{22}Q_{xz}y(17x^4 - 22x^2y^2 - 36x^2z^2 + 3y^4 - 8y^2z^2 + 10z^4)}{44} - \frac{\sqrt{22}Q_{yz}x(3x^4 - 22x^2y^2 - 8x^2z^2 + 17y^4 - 36y^2z^2 + 10z^4)}{44}$$

$$\tilde{\mathbb{G}}_4^{(2,1)}[q](A, 3)$$

** symmetry

$$\frac{\sqrt{5} (x-y)(x+y)(x^2+y^2-6z^2)}{4}$$

** expression

$$-\frac{21\sqrt{22}Q_uxyz(x^2+y^2-2z^2)}{44} - \frac{21\sqrt{66}Q_vxyz(x-y)(x+y)}{44} + \frac{\sqrt{66}Q_{xy}z(9x^4 - 24x^2y^2 - 10x^2z^2 + 9y^4 - 10y^2z^2 + 2z^4)}{44} \\ - \frac{\sqrt{66}Q_{xz}y(x^4 + 2x^2y^2 - 12x^2z^2 + y^4 - 12y^2z^2 + 8z^4)}{44} - \frac{\sqrt{66}Q_{yz}x(x^4 + 2x^2y^2 - 12x^2z^2 + y^4 - 12y^2z^2 + 8z^4)}{44}$$

$$\tilde{\mathbb{G}}_4^{(2,1)}[q](A, 4)$$

** symmetry

$$\frac{\sqrt{35}yz(y-z)(y+z)}{2}$$

** expression

$$-\frac{3\sqrt{154}Q_ux(x^2y^2 - x^2z^2 + y^4 - 9y^2z^2 + 2z^4)}{88} - \frac{\sqrt{462}Q_vx(x^2y^2 - x^2z^2 - 5y^4 + 27y^2z^2 - 4z^4)}{88} \\ - \frac{\sqrt{462}Q_{xy}y(2x^2y^2 - 6x^2z^2 - y^4 + 8y^2z^2 - 3z^4)}{44} + \frac{\sqrt{462}Q_{xz}z(6x^2y^2 - 2x^2z^2 + 3y^4 - 8y^2z^2 + z^4)}{44} - \frac{\sqrt{462}Q_{yz}xyz(2x^2 - y^2 - z^2)}{44}$$

$$\tilde{\mathbb{G}}_4^{(2,1)}[q](A, 5)$$

** symmetry

$$-\frac{\sqrt{35}xz(x-z)(x+z)}{2}$$

** expression

$$-\frac{3\sqrt{154}Q_uy(x^4 + x^2y^2 - 9x^2z^2 - y^2z^2 + 2z^4)}{88} - \frac{\sqrt{462}Q_vy(5x^4 - x^2y^2 - 27x^2z^2 + y^2z^2 + 4z^4)}{88} \\ + \frac{\sqrt{462}Q_{xy}x(x^4 - 2x^2y^2 - 8x^2z^2 + 6y^2z^2 + 3z^4)}{44} + \frac{\sqrt{462}Q_{xz}xyz(x^2 - 2y^2 + z^2)}{44} + \frac{\sqrt{462}Q_{yz}z(3x^4 + 6x^2y^2 - 8x^2z^2 - 2y^2z^2 + z^4)}{44}$$

$$\tilde{\mathbb{G}}_4^{(2,1)}[q](A, 6)$$

** symmetry

$$\frac{\sqrt{35}xy(x-y)(x+y)}{2}$$

** expression

$$-\frac{9\sqrt{154}Q_uz(x^2 - 2xy - y^2)(x^2 + 2xy - y^2)}{88} - \frac{\sqrt{462}Q_vz(x-y)(x+y)(x^2 + y^2 - 2z^2)}{88} + \frac{\sqrt{462}Q_{xy}xyz(x^2 + y^2 - 2z^2)}{44} \\ + \frac{\sqrt{462}Q_{xz}x(x^4 - 8x^2y^2 - 2x^2z^2 + 3y^4 + 6y^2z^2)}{44} + \frac{\sqrt{462}Q_{yz}y(3x^4 - 8x^2y^2 + 6x^2z^2 + y^4 - 2y^2z^2)}{44}$$

$$\tilde{\mathbb{G}}_4^{(2,1)}[q](A, 7)$$

** symmetry

$$\frac{\sqrt{5}yz(6x^2 - y^2 - z^2)}{2}$$

** expression

$$-\frac{3\sqrt{22}Q_{ux}(2x^4 - 3x^2y^2 - 17x^2z^2 - 5y^4 + 39y^2z^2 + 2z^4)}{88} - \frac{\sqrt{66}Q_{vx}(2x^4 - 31x^2y^2 + 11x^2z^2 + 9y^4 + 39y^2z^2 - 12z^4)}{88} \\ - \frac{\sqrt{66}Q_{uyy}(8x^4 - 12x^2y^2 - 12x^2z^2 + y^4 + 2y^2z^2 + z^4)}{44} + \frac{\sqrt{66}Q_{xz}(8x^4 - 12x^2y^2 - 12x^2z^2 + y^4 + 2y^2z^2 + z^4)}{44} - \frac{21\sqrt{66}Q_{yz}xyz(y - z)(y + z)}{44}$$

$\vec{\mathbb{G}}_4^{(2,1)}[q](A, 8)$

** symmetry

$$-\frac{\sqrt{5}xz(x^2 - 6y^2 + z^2)}{2}$$

** expression

$$-\frac{3\sqrt{22}Q_{uy}(5x^4 + 3x^2y^2 - 39x^2z^2 - 2y^4 + 17y^2z^2 - 2z^4)}{88} - \frac{\sqrt{66}Q_{vy}(9x^4 - 31x^2y^2 + 39x^2z^2 + 2y^4 + 11y^2z^2 - 12z^4)}{88} \\ + \frac{\sqrt{66}Q_{xyx}(x^4 - 12x^2y^2 + 2x^2z^2 + 8y^4 - 12y^2z^2 + z^4)}{44} + \frac{21\sqrt{66}Q_{xz}xyz(x - z)(x + z)}{44} - \frac{\sqrt{66}Q_{yz}(x^4 - 12x^2y^2 + 2x^2z^2 + 8y^4 - 12y^2z^2 + z^4)}{44}$$

$\vec{\mathbb{G}}_4^{(2,1)}[q](A, 9)$

** symmetry

$$-\frac{\sqrt{5}xy(x^2 + y^2 - 6z^2)}{2}$$

** expression

$$-\frac{21\sqrt{22}Q_{uz}(x - y)(x + y)(x^2 + y^2 - 2z^2)}{88} - \frac{\sqrt{66}Q_{vz}(3x^4 - 78x^2y^2 + 20x^2z^2 + 3y^4 + 20y^2z^2 - 4z^4)}{88} - \frac{21\sqrt{66}Q_{xy}xyz(x - y)(x + y)}{44} \\ - \frac{\sqrt{66}Q_{xz}(x^4 + 2x^2y^2 - 12x^2z^2 + y^4 - 12y^2z^2 + 8z^4)}{44} + \frac{\sqrt{66}Q_{yz}(x^4 + 2x^2y^2 - 12x^2z^2 + y^4 - 12y^2z^2 + 8z^4)}{44}$$