

Adaptative Beam Plugin

1 Sofa Datatypes

1.1 RigidBody

1.2 SolidType

2 Beam Element

For the general introduction of beam theory and equations, see p.509 [5]. For detail of the construction local matrix, see the p.70 [2].

3 B-splines , Bézier Splines

B-splines in general and Bézier splines in particular can see in [1] or more detail in [3]. A spline tool can see at [4]. Here assumed several general formula. In general, a Bézier curve order n is determined by $n + 1$ control points (characteristic polygone) $P_{i,0 \leq i \leq n}$. Its trajectory is :

$$B(t) = \sum_{i=0}^n \hat{\mathbf{B}}_{i,n}(t) \cdot P_i$$

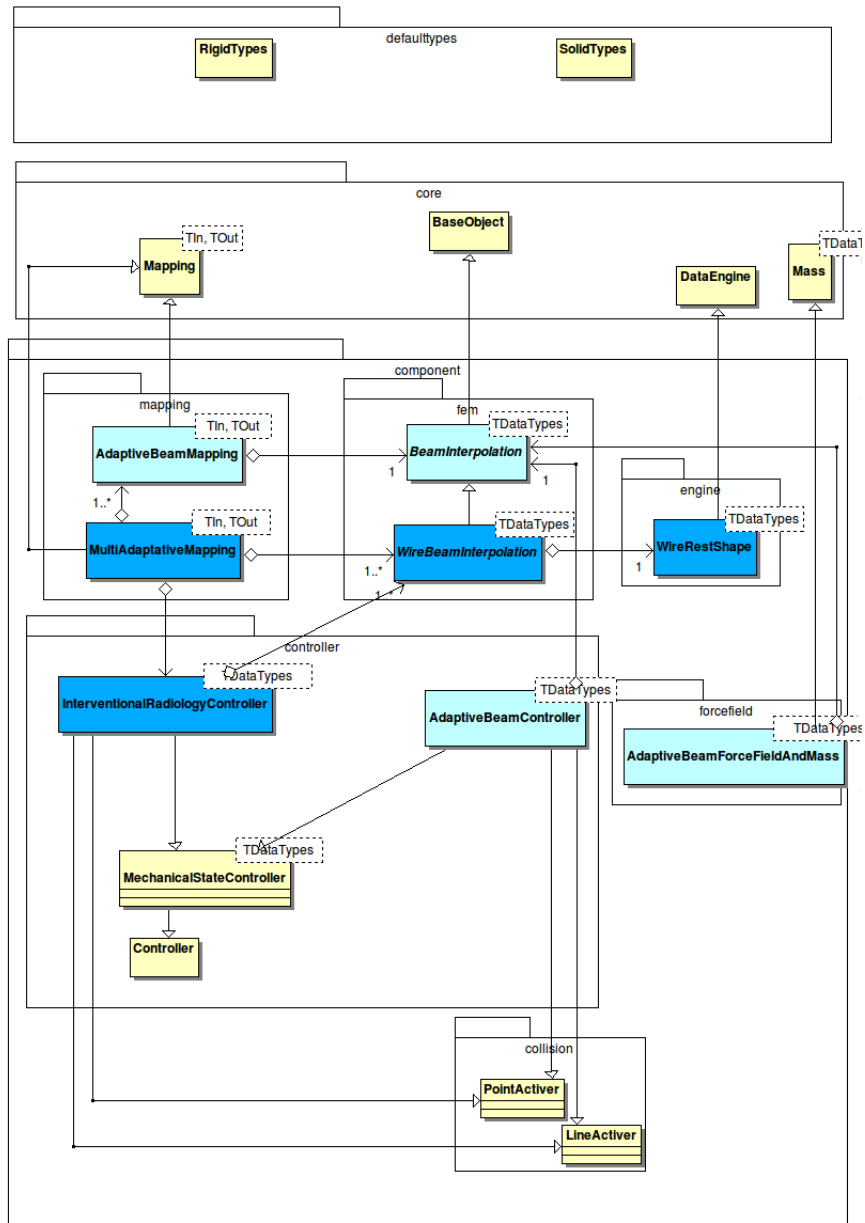
Where $\hat{\mathbf{B}}_{i,n}(t)$ are Bernstein polynomial given by

$$\hat{\mathbf{B}}_{i,n}(t) = \mathbb{C}_n^i \cdot t^i \cdot (1 - t)^{n-i}$$

The most usually used is the cubic Bézier , where trajectory is given by

$$(1 - t)^3 \cdot P_0 + 3 \cdot (1 - t)^2 t \cdot P_1 + 3 \cdot t^2 (1 - t) \cdot P_3 + t^3 \cdot P_3$$

4 Implementation



- 4.1 WireRestShape
- 4.2 BeamInterpolation
- 4.3 AdaptiveBeamForceFieldAndMass
- 4.4 AdaptiveBeamController
- 4.5 AdaptiveBeamMapping
- 4.6 WireBeamInterpolation
- 4.7 InterventionalRadiologyController
- 4.8 MultiAdaptiveMapping

References

- [1] F. ANDERSSON, *Bézier and B-spline Technology*, PhD thesis, Juin 2003.
- [2] J. PRZEMIENIECKI, *Theory of Matrix Structural Analysis*, 1968.
- [3] T. W. SEDERBERG, *COMPUTER AIDED GEOMETRIC DESIGN*, 2011 ed.
- [4] T-SPLINE, <http://www.tsplines.com/>.
- [5] T.BELYTSCHKO, W. K. LIU, AND B. MORAN, *Nonlinear Finite Elements for continua and structures*, 2000.