Casal2 User Manual

Casal2 Development Team

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Contents

1 Introduction

1.1 About Casal2

Casal2 is an open-source integrated statistical catch-at-age assessment tool for modelling the population dynamics of marine populations. Casal2 is designed for quantitative assessments of marine populations, including fish, invertebrates, marine mammals and seabirds.

Casal2 implements a generalised age-structured population model that allows for a great deal of choice in specifying the population dynamics, parameters and those parameters that should be estimated, and the model outputs. Casal2 is designed for flexibility. It allows implementation of age-structured models from single species or stocks, to multiple species or stocks, using user-defined categories such as area, sex, and maturity stage. The categories are are generic, are not predefined, and are easily specified. Casal2 models can be used for a single population with a single anthropogenic event (i.e., a single fish stock with a single fishery), or for multiple species and populations, areas, and/or anthropogenic or exploitation methods, and including predator-prey interactions.

In Casal2 the processes and observations that occur over each year are defined by the user. Processes include recruitment, natural mortality, and anthropogenic mortality. Observations used to fit the models can be from many different sources, including removals-at-size or -age (e.g., a fishery), research survey or other biomass indices, and mark-recapture data. Model parameters can be estimated using penalised maximum likelihood or Bayesian methods.

As well as the point estimates of the parameters, Casal2 can calculate the likelihood or posterior distribution profiles for estimated parameters, and can generate Bayesian posterior distributions using Markov chain Monte Carlo methods. Casal2 can project the population status into the future using both deterministic or stochastic population dynamics. Casal2 can also simulate observations from a given model for both actual or potential observations.

1.2 Citing Casal2

The reference for this document is Casal2 Development Team (2021). Casal2 User Manual, v21.09 (2021-09-07). National Institute of Water & Atmospheric Research Ltd. *NIWA Technical Report 139*. 226 p.

The peer-reviewed journal article reference for Casal2 is (Doonan et al., 2016).

1.3 Casal2 Contributors

The Casal2 project is maintained by the Casal2 Development Team. Casal2 was started by Alistair Dunn. The software architect and lead author of the software code was Scott Rasmussen. Contributors to the development of Casal2 are Scott Rasmussen, Alistair Dunn, Ian Doonan, Craig Marsh, Teresa A'mar, Kath Large, Sophie Mormede, Samik Datta, Matt Dunn, Jingjing Zhang, and Marco Kienzle.

The development of Casal2 was funded by National Institute of Water & Atmospheric Research Ltd. (NIWA), with additional funding from the New Zealand Ministry for Primary Industries.

1.4 Software license

1.5 Where to get Casal2

See https://www.niwa.co.nz/ for information about Casal2. The Casal2 source code is hosted on GitHub, and can be found at http://github.com/NIWAFisheriesModelling/CASAL2.

There are installation packages available for Linux and Microsoft Windows. Release versions of the package includes the Casal2 binary, the Casal2 **R** library, the Casal2 User Manual and associated documentation, example models, and other information. The installation packages can be downloaded at https://github.com/NIWAFisheriesModelling/CASAL2/releases.

1.6 System requirements

Casal2 is available for most x86 compatible machines running 64-bit Linux and Microsoft Windows operating systems. Casal2 has not been compiled nor tested on macOS.

Several of Casal2's tasks are computer intensive and a fast processor is recommended. Depending on the model implemented, some of the Casal2 tasks can take a considerable amount of processing time (minutes to hours), and in extreme cases may even take several days to complete an MCMC estimate.

Output files have the potential to be large, and the output from developing a model, sensitivity analyses, and running multiple MCMC chains can take up significant amounts of disk space. Depending on the number and type of user output requests, the output could range from a few hundred kilobytes to several hundred megabytes. When estimating model fits, several hundred megabytes of RAM may be required, depending on the spatial size of the model, number of categories, and complexity of processes and observations. For larger models, several gigabytes of RAM and disk space may occasionally be required.

1.7 Necessary files

For both 64-bit Linux and Microsoft Windows, we recommend using the install package available on https://github.com/NIWAFisheriesModelling/CASAL2 for Microsoft Windows or the Debian package (.deb) for Linux. Running Casal2 on a system requires the main binary (casal2.exe on Windows, or casa2 on Linux) and the associated dynamically linked libraries (DLL) for Windows or shared objects (.so) for Linux, and cannot be (easily) run by copying the binary to a working directory. Casal2 is not available for 32-bit operating systems or macOS.

Casal2 does not post-process model output. Casal2 writes all output to text files — either the standard out or to files. A package that allows tabulation and graphing of model outputs is recommended. Software such as **R** (R Core Team, 2014) is recommended. The Casal2 **R** package is provided for extracting Casal2 output from reports and output files into **R** (see Section 17). A separate **R** package is also available that provides some examples of diagnostic and plot functionality.

1.8 Getting help

Casal2 is distributed as unsupported software. Please notify the Casal2 Development Team of any issues with or errors in Casal2. Please contact the Casal2 Development Team. See Section 18.2 for the guidelines for reporting issues. Note that Casal2 is a complex program, with many different options and possibilities, and we may not be able to provide any useful help if you submit an error report that does not follow the guidelines.

1.9 Technical details

Casal2 was compiled on Linux using gcc (https://gcc.gnu.org), the C/C++ compiler developed by the GNU Project. The 64-bit Linux version was compiled using gcc version 10.3.0). The source code for Casal2 is available in the GitHub repository at https://github.com/NIWAFisheriesModelling/CASAL2.

The Microsoft Windows (https://www.microsoft.com) version was compiled using TDM-gcc (https://jmeubank.github.io/tdm-gcc/) using gcc 10.3.0 (http://gcc.gnu.org). The Microsoft Windows(https://www.microsoft.com) installer was built using the Inno Setup (https://jrsoftware.org/isdl.php). **Note:** for some previous gcc versions, there have been issues related to threading. This was indicated by failed unit tests which rely on threading such MCMCHamiltonian etc.

Casal2 includes several minimisers; different minimisers may perform better for some models than others. These include both numerical differences minimisers and auto-differentiation minimisers. Numerical differences minimisers will usually work form most problems, albeit more slowly than auto-differentiation based minimisers. The numerical differences minimisers are:

1. Numerical differences: A minimiser that is closely based on the main algorithm of Dennis Jr and Schnabel (1996), that uses finite difference gradients.
2. deltadiff: A multithreaded version of the numerical differences, but with *tan* rescaling instead of *arcsin* and available for use with the Hamiltonian Monte Carlo MCMC algorithm.
3. DESolver: The differential evolution solver (Storn and Price, 1995), based on code by Lester E. Godwin of PushCorp, Inc.

There are two auto-differentiation minimisers, both based on ADOL-C. These are

1. Betadiff: A minimiser using an older version of ADOL-C (v1.8.4) that was used as the automatic differentiation minimiser in CASAL (Bull et al., 2012), with the same minimising algorithm as used for the finite differences minimiser above, but based on the gradient from the auto-differentiation chain.
2. ADOLC: A minimiser using version of ADOL-C (v2.5.1) (Walther et al., 1996);, with a similar minimising algorithm as used for the finite differences minimiser above, but based on the gradient from the auto-differentiation chain.

The random number generator used in Casal2 uses an implementation of the Mersenne twister random number generator (Matsumoto and Nishimura, 1998). This functionality, the command line functionality, matrix operations, and a number of other functions use the Boost C++ library (Version 1.71.0).

Note that the output from Casal2 may differ slightly on the different operating systems and operating system versions due to different precision arithmetic or other platform-dependent (including CPU hardware) implementation details. In particular, the implementation of the standard C++ library math.h differs slightly on different platforms, and hence the results from different platforms may be different.

Unit tests of the underlying Casal2 code are carried out at build time, using the Google Test and Mock unit testing and mocking framework. The unit test framework aims to cover a significant proportion of the key functionality within the Casal2 code base. The unit test code for Casal2 is available as a part of the underlying source code.

2 Model overview

Casal2 is a generalised age-structured population dynamics modelling framework for undertaking age-structured integrated assessments (Maunder, 2013). Casal2— allows multiple sources of information to be combined into a single analysis using a statistical framework so that error sources are fully propagated into the uncertainty in the outcomes. The model follows cohorts as numbers-at-age through time, recording the changes that occur from the population dynamic processes.

Casal2 is run from the console window on Microsoft Windows or from a terminal window on Linux. Casal2 has two sources of information: the *input configuration file* which defines the model structure, provides observations, defines active parameters, and specifies outputs (reports); and the run-time option (e.g., estimate active parameters, run projections, etc..) that is given by command line options and arguments (see Section 3 for specific details). Typically a 'run' will simply run the model (without estimation) and generate the expected values and other models outputs from the parameter values assumed, and an estimation will minimise the model objective function to derive the 'best fit' parameters.

A Casal2 model is defined by its initial conditions and the processes that occur on the population over the years of the model run. Within each year, the annual cycle defines the time steps that occur within a year and the order of processes within each time step. At each point in time, the model updates the *state* of the model, where the state consists of two parts, the *partition*, and any *derived quantities* requested.

The *partition* is a representation of the population at each time step, and can be considered a matrix of the numbers of individuals within each category (i.e., row) and at each age (i.e., column). The partition will change after each process, and hence after each *time-step* of every year. The rows of the partition (categories) and columns (ages) define the population structure. For example, categories can define males and females, area, and/or maturity stage. Note that any user-defined category or category label is possible, for example species, stock, tagged status. The number of categories, what they represent, and how they interact is completely defined by the user. The model records the numbers of individuals within each category and age (e.g., for model with a two sexes, the numbers of males and females at age). In general, cohorts are added via a recruitment event, are aged annually, and are removed from the population via various forms of mortality (e.g., fishing or natural mortality).

A *derived quantity* is the result of a calculation on the partition at some point in time. An example of a derived quantity is spawning stock biomass (SSB) – the sum of the biomass of individuals that are mature (or spawning) at some specific point in the annual cycle. Unlike the partition, which is updated as each new time step, a derived quantity records a single value for each year of the model run. Hence, derived quantities are a vector of values over the time period represented by the model. Each derived quantity can be reported or used as an input into a process. The most common use of a derived quantity is spawning stock biomass (SSB) in the stock-recruitment relationship to determine recruitment of the population into the model. Another example might be a density dependent mortality process for a species that was based on the biomass of a second species in the model.

Observations are the data that was observed for some aspect of the population. They include the observed values, the sampling distribution, relationship with the partition, and the time within the model that these occur (time step and year). For example, indices of abundance or biomass from a research survey, or age compositions from a commercial catch in a fishery. The partition is queried to generate the expected values for the observations, and then the sampling distribution and sample sizes are used to calculate their likelihood. In broad terms, the model parameters are estimated so-as to provide the best fit between expected values and the observations, by minimising an objective

function. Best fit is judged by the lowest objective function value, with the objective function equal to the sum of the negative log-likelihood, priors, and any model constraints (penalties). The evaluation of observations and the calculation of the expected values for each observation type is described in Section 7.

The method that Casal2 uses to find a minimum, the parameters to estimate and their priors is given in the estimation section, see Section 6. This includes the choice of minimiser, MCMC algorithms and associated parameters, ans well as any transformations and penalties used to constrain the model.

Outputs (reports) are defined in the report section. Casal2 has a large number of reports to summarise or generate a variety of output for a given model. See Section 8 for more information.

The model, its population structure, observations, methods of estimation, and output reports are all defined in the input configuration fileṪhe run mode of Casal2 is determined from the command line arguments given when 'running' Casal2.

The input configuration file is a text file with the Casal2 commands and subcommands. The input configuration file completely describes a model implemented in Casal2. See Sections 9, 10, 11, and 12 for details of Casal2's command and subcommand syntax. The default name for this file is `config.csl2`, however any file name can be used if given as an argument to the command line when calling Casal2. Generally, it can be useful to split the input configuration file into a number of smaller files using the `@include` command. We recommend using separate files for the different section for the configuration commands and subcommands to assist readability.

3 Running Casal2

Casal2 is run from a console window (i.e., the command line) on Microsoft Windows or from a terminal window on Linux. Casal2 uses information from input data files -- the *input configuration file* being the input file that is supplied to Casal2.

The input configuration file is required and defines the model structure, processes, observations, parameters (both the fixed parameters and the parameters to be estimated), and the requested reports (outputs).

By convention, the name of the input configuration file ends with the suffix `.csl2`. However, any suffix is acceptable. The default name for the input configuration file is *config.csl2* and if used it does not have to be specified as one of the command line arguments to to Casal2. Note that the input configuration file can include other separate files so the specification can be split into digestible parts.

Command line arguments are used to specify the actions or *tasks* of Casal2, e.g., to run a model with a set of parameter values, to estimate parameter values (either point estimates or MCMC), to project quantities, or to simulate observations.For example, `-r` is the *run* mode, `-e` is the *estimation* mode, and `-m` is the *MCMC* mode. The *command line arguments* are described in Section 3.3.

3.1 Using Casal2

To use Casal2, open a console window (i.e. the command prompt) window on Microsoft Windows or a terminal window on Linux. Navigate to the directory where the model input configuration files are located. Then enter Casal2 with arguments for a specific mode to start the Casal2 mode running; see Section 3.3 for the list of possible arguments. Casal2 will print output to the screen.

For both 64-bit Linux and Microsoft Windows, we recommend using the install package available on `https://github.com/NIWAFisheriesModelling/CASAL2` for Microsoft Windows or the Debian package (.deb) for Linux. Running Casal2 on a system requires the main binary (casal2.exe on Windows, or casal2 on Linux) and the associated dynamically linked libraries (DLL) for Windows or shared objects (.so) for Linux to be installed into appropriate directories, and cannot be (easily) run by copying the binary to a working directory. Casal2 is not available for 32-bit operating systems or macOS.

3.2 Redirecting standard output

Casal2 uses the `standard output` stream to display runtime information. The standard error stream is used by Casal2 to output the program exit status and runtime errors. We suggest redirecting both the standard output and standard error into an appropriate file or files.

With the bash shell (on Linux systems), you can do this using the command structure

```
(casal2 [arguments] > run.out) >& run.err &
```

It may be useful to redirect the standard input, especially if you're using Casal2 inside a batch job, i.e.

```
(casal2 [arguments] > run.out < /dev/null) >& run.err &
```

On Microsoft Windows systems, you can redirect to standard output using

```
casal2 [arguments] > run.out
```

And, on some Microsoft Windows systems (e.g., Windows 10), you can redirect to both standard output and standard error, using the syntax

```
casal2 [arguments] > run.out 2> run.err
```

Casal2 outputs header information to the output. The header consists of the program name and version, the arguments passed to Casal2 from the command line, the date and time that the program was called (derived from the system time), the user name, and the machine name (including the operating system and the process identification number). This information can be used to track output across runs, dates, and versions of Casal2.

3.3 Command line arguments

Casal2 is called using:

`casal2[-c` *`config_file`*`] [`*`task`*`] [`*`options`*`]`

where

`-c` ***`config_file`*** Define the input configuration filefor Casal2 (if this argument is omitted, the default input configuration file is `config.csl2`)

and where *task* must be one of the following ([] indicates a secondary label to call the task, e.g. **`-h`** will execute the same task as **`--help`**),

`-h [--help]` Display help (this page)

`-l [--licence]` Display the reference for the software license (GPL v2)

`-v [--version]` Display the Casal2 version number

`-r [--run]` *Run* the model once using the parameter values in the input configuration file, or optionally with the free parameter values from the file specified with argument `-i` or `-I`.

`-e [--estimate]` Do a point *estimate* using the values in the input configuration file as the starting point for the parameters to be estimated, or optionally with the free parameter values from the file specified with argument `-i` or `-I`.

`-E [--Estimate]` ***`filename`*** Do a point *estimate* and generate an MPD file (ie.e., a file containing the free parameters and the covariance matrix). As with `-e`, this uses the values in the input configuration file as the starting point for the parameters to be estimated, or optionally the free parameter values from the file specified with argument `-i` or `-I`.

`-p[-profiling]` Do a likelihood *profile* using the parameter values in the input configuration file as the starting point, or optionally with the free parameter values from the file specified with argument `-i` or `-I`

`-m [--mcmc]` Do an *MCMC*. An estimate run is fist carried out to estimate the co-variance matrix for the MCMC proposal distribution, using the values in the input configuration file as the starting point for the parameters to be estimated. Optionally the free parameter values from the file specified with argument `-i` or `-I` can be used as the starting point.

`-M [--mcmc-from-estimate]` ***`filename`*** Do an *MCMC* using the covariance and free parameters in the MPD file.

`-R [--resume]` ***`filename`*** Resume a previously stopped*MCMC* using the covariance and free parameters in the MPD file. Additional arguments must be supplied to specify the sample and objective files from the previous MCMC with `--objective-file` and `--sample-file`.

-f [--projection] *n*. Project the model *forward* in time using the parameter values in the input configuration file as the starting point for the estimation, or optionally with the parameter values from the file specified with the argument `-i` or `-I`. Projections are repeated for each parameter set (i.e., each line of data in the free parameter file) *n* times (the default is 1). Typically, the MCMC sample output will be used with `-i`.

-s [--simulation] ***n*** *Simulate n* of observation sets using values in the input configuration file as the parameter values, or optionally with the parameter values from the file specified with the argument `-i` or `-I`.

The following optional arguments [*options*] may be specified

-i [--input] ***filename*** *Input* one or more sets of free (estimated) parameter values from *filename* (see Section 8 for details about the format of *filename*).

-I [--input-force] ***filename*** *Input* one or more sets of parameter values from *filename*. This contains both the free parameters and also force the *overwrite* addressable (non-estimated) values in the input configuration file (see Section 8 for details about the format of *filename*)

-o [--output] ***filename*** *Output* a report of the free (estimated) parameter values in a format suitable for `-i` *filename* (see Section 8 for details about the format of *filename*)

-g [--seed] ***seed*** Initialise the random number *generator* with *seed*, a positive (long) integer value (note, if `-g` is not specified, then Casal2 will generate a random number seed based on the computer clock time)

--loglevel ***arg*** Set the level for information or logging messages from Casal2. Valid options are (from more verbose to less verbose) trace, finest, fine, medium, info, important, and warning. The default is 'info' (see Section 8 for more information).

-t [--tabular] Print `@report` in tabular format (see Section 8 for more information).

--single-step Run with `-r` to pause the model and ask the user to specify parameters and their values to use for the next iteration (see Section 3.6)

-q [--query]*object type* *Query* an object type to print an extract of the object description and parameter definitions. An object can be defined as *block.type*, e.g., `casal2 --query process.recruitment_constant` will query the constant recruitment block.

Combinations of these command line arguments can also be implemented. Examples of some useful ones are below.

`casal -r -i par.file> mulit_run.out` will conduct multiple model runs, one for each row of parameters in `par.file`. This can be useful for investigating the effect of individual parameters in the model or summarising profiled outputs.

`casal -e -i par.file> mulit_estimate.out` will conduct multiple estimation routines. One for each row of parameters in `par.file`. This can be useful for assessing convergence to a global minimum. All base models should be run from multiple starting parameter values to assess model convergence/sensitivity to starting values.

`casal -s 10 -i par.file > mulit_simulation.out` This command instructs Casal2 to simulate 10 sets of simulated data sets for each each row of parameters in `par.file`. The `-s` component adds observation error in simulated data sets through the likelihood distribution assumptions and the `-i` adds parameter uncertainty into the simulated data sets if each row differs.

3.4 Constructing the Casal2 input configuration files

- the description of the population structure, dynamics, and parameters. See Section 5,
- the estimation methods and estimated variables. See Section 6,
- the observations and their associated properties and likelihoods. See Section 7, and
- the results that Casal2 will output. See Section 8.

Note that input configuration file files can *include* other input configuration file files to assist file management, using the command `!include "filename"`. See Section 13 for more details.

3.4.1 Commands

Casal2 has a range of commands that define the model structure, processes, parameters, observations, and how tasks are carried out. There are three types of commands

- Commands that have an argument only and do not have subcommands (for example, `!include filename`)
- Commands that have a label and subcommands (for example `@process` must have a label and has subcommands)
- Commands that do not have either a label or argument, but have subcommands (for example `@model` or `@categories`)

Apart from `!include`, commands start with an `@` in the first column (i.e., may not have a space or tab character before them on the line). After each command, the subcommands are listed and must occur before the next command. Otherwise, the commands and subcommands are free form with each command or subcommand on a separate line (see Section 3.4.3).

Commands that have a label must have a unique label, i.e., the label cannot be used on more than one command of that type. Casal2 checks and will report an error of two commands of the same type have the same label. The labels can contain alpha numeric characters, period ('.'), underscore ('_') and dash ('-'), but cannot start with a double underscore ('__'). Labels that start with a double underscore are reserved, and used for internal reports that Casal2 can automatically generate in some circumstances. Otherwise labels must not contain white space (tabs or spaces) or any characters that are not letters, numbers, dashes, periods, or underscores. For example,

```
@process NaturalMortality
```

or

```
!include MyModelSpecification.csl2
```

3.4.2 Subcommands

Casal2 subcommands define options and parameter values related to a particular command. Subcommands always take an argument which is one of a specific *type*. The *types* for each subcommand are defined in Section 14.1.3, and are summarised below.

Like commands (`@command`), subcommands and their arguments are not order specific, except that that all subcommands of a given command must appear before the next `@command` block. Casal2 may report an error if they are not supplied in this way. However, in some circumstances a different order may result in a valid, but unintended, set of actions, leading to unexpected results.

The argument type for a subcommand can be:

switch true/false

integer an integer number

integer vector a vector of integer numbers

integer range a range of integer numbers separated by a colon, e.g. 1994:1996 is expanded to an integer vector of values (1994 1995 1996)

constant a real number (i.e., a double)

constant vector a vector of real numbers (i.e., a vector of doubles)

estimable a real number that can be estimated (i.e., a double)

estimable vector a vector of real numbers that can be estimated (i.e., a vector of doubles)

addressable a real number that can be referenced but not estimated (i.e., an addressable double)

addressable vector a vector of real numbers that can be referenced but not estimated (i.e., a vector of addressable doubles)

string a categorical (string) value

string vector a vector of categorical values

Switches are characteristics which are either true or false. Enter *true* as `true` or `t`, and *false* as `false` or `f`.

Integers must be entered as whole numbers without decimal points (i.e., if `year` is an integer then it is specified as `2008`, not `2008.0`)

Arguments of type integer vector, constant vector, estimable vector, addressable vector, or categorical vector must contain one or more entries on a row, separated by white space (tabs or spaces). Arguments of type integer range must contain a colon (`:`) and no white space (tabs or spaces).

Parameters are defined in the population section and most (but not all) numeric parameters can be estimated. See Section 14.1.3 for the list of available parameters and if they are allowed to be estimated. Note that parameters will only be estimated if requested using an `@estimate` command, and are otherwise treated as a constant.

Parameters can also be addressable, i.e., they can be referred to within another command or command block by using their addressable name. See Section 14.1.3 to determine of a subcommand is addressable.

3.4.3 The command block format

The command block is a basic unit within the input configuration file. Each command begins with the symbol `@` and then the command name, usually followed by a user defined label or a valid argument. The end of each command block is denoted by the start of the next command block or end of the file. For example, the layout of a input configuration file will be

```
@command label
first_subcommand argument
second_subcommand argument
```

... etc.

```
@another_command label
another_subcommand argument
```

another_subcommand argument

... etc.

Note that subcommands can be in any order within each command block. And command blocks can be in any order within the input files, except @model — this must be the first command block encountered by Casal2.

Blank lines are ignored, as is extra white space (tabs and spaces) between arguments. However, to start command block the @ character must be the first character on the line and must not be preceded by any white space. Each input file must end with a carriage return.

Commands, subcommands, and arguments in the input configuration files are not case sensitive. However, labels and variable values are case sensitive. Note that on Linux (unlike Microsoft Windows) specification of any file names or file paths will be case sensitive.

3.4.4 Commenting out lines

Text on a line that starts with the symbol # is considered to be a comment and is ignored. To comment out a group of commands or subcommands, use # at the beginning of each line to be ignored.

Alternatively, to comment out an entire block or section, use /* at the beginning of a line to start the comment block, then end the block with */. All lines (including line breaks) between /* and */ inclusive are ignored.

```
# This line is a comment and will be ignored
@process NaturalMortality
m 0.2
/* This block of text
is a comment and
will be ignored
*/
```

3.4.5 How to reference parameters

All parameters have an unique name, allowing it to be referenced in other command blocks. When Casal2 processes the input configuration file it translates each command block (see section 3.4.3) and each subcommand block into an object, each with a unique parameter name. For commands, this parameter name is simply the command label. For subcommands, the parameter name format is one of the following:

command[label].subcommand if the command has a label, or

command.subcommand if the command has no label, or

command[label].subcommand{i} if the command has a label and the subcommand arguments are a vector, and we are accessing the *i*th element of that vector.

command[label].subcommand{i:j} if the command has a label, and the subcommand arguments are a vector, and we are accessing the elements from *i* to *j* (inclusive) of that vector.

For example, the parameter name of a process of instantaneous mortality (i.e., natural mortality) is the subcommand m of a @process of type mortality_constant_rate, i.e., the command block may be

```
@process NaturalMortality
type mortality_constant_rate
categories male female
m 0.2 0.2
```

`process[NaturalMortality].m` is the unique reference for the vector of male then females natural mortality values (**note:** order will follow categories order). But to reference just the 'female' rate then the form is `process[NaturalMortality].m{female}`.

3.5 Reading a command block

Here, we illustrate reading a command block using two important commands, `@process` and `@estimate`.

The command `@process` specifies a process that can be used in the model. The are a fixed set of predefined processes (subroutines in C++ code). The way to identify which one is by the `type` subcommand. Processes can take one or more parameters and some will need other data to be applied too. Some parameters are mandatory and others can take a default value if they are not specified. We have categories male and female, and two fisheries, line and pot. The command block starts with a*@process*:

```
@process Fishing
type mortality_instantaneous
```

This sets up a process block using the *mortality_instantaneous* process which simultaneously depletes the population by natural mortality and from two types of fishing. Its label is *Fishing*.

Next we specify the values for natural mortality (*m*) an argument to this process, to 0.17 and specify that fisheries acts on all categories. Note there are two values for natural mortality, one for each sex. The parameters *m* can be estimated, if required. The command block fragment:

```
m 0.17 0.17   # natural mortality  for each category
relative_m_by_age One One # natural mortality multiplier
categories *  # fishing acts on all categories ("*" shorthand for male female)
```

Catches are supplied via a *table* format using three columns: year and two for the fisheries, one for each, which take the labels *line* and *pot*. Column names are on the first line of the table and these columns can be in any order,

```
#catches
table catch         # define catches by fishery in table format
year line pot       #names columns so can identity catch for each fishery
2000 1000 2000      # catches by year
2001 500  1000
2002 1000 5000
end_table           # end of table marker
```

Other information needed are supplied in the methods table which has a fixed number of columns (again these can be in any order), one for each piece of information needed to model a fishery. The method column defines the fishery name which is used in the catch table and also in other observations like age composition from that fishery. The categories that the fishery operates on (all in this case, but it could be just males for one and females for the other) are in the category column, the fishing selectivity to be used is given as a selectivity block name which is define somewhere else in the files, U_max is the maximum exploitation rate in any year that is allowed, next comes the time step the fishing operates in, and lastly the block name of a penalty function that is used to penalise estimable parameter values that result in the supplied catch not being caught. Again, the penalty block is define elsewhere in the files. After the row with the column names, there follows one row for each fishery:

```
table method        # supply arguments and name selectivity etc
method     category  selectivity    u_max    time_step      penalty
pot        *         potFSel        0.7      1              CatchMustBeTaken1
line       *         lineFSel       0.7      1              CatchMustBeTaken1
end_table
```

To estimate natural mortality, you need to supply an *@estimate* block with a reference name back to *m* in the *Fishing* block. For *@estimate*, *type* specifies the prior to be used in the estimation, which in this case is a normal distribution:

```
@estimate estimate.m
type normal # prior type
parameter process[fishing].m  #
    \*Fishing is unique amongst the @process command blocks
      so this defines the unique reference to the parameter m
    *\

mu  0.2 0.2   #argument to prior = mean
sd  0.02 0.02 #another argument to the prior = standard deviation
```

Note that there are two *m*s, one for each sex, so there has to be two priors. The *estiamte* label *estimate.m* is often redundant, but it may be needed in some circumstances.

To estimate a common *m* over both sexes, we estimate one *m*, say the female category, and use the *same* subcommand to apply the same value to the male category *m*,

```
@estimate estimate.m
type normal
parameter process[fishing].m{male}
# {} is used to index one or more elements in a vector
same process[fishing].m{female} # set female values = male estimated values
# The mean of the prior
mu  0.2
# The standard deviation of the prior
sd  0.02
```

3.6 Single-stepping Casal2

Single-stepping means Casal2 can 'pause' after each year in the annual cycle during a model run, write reports, then wait and process user input of updated estimable parameters for the next year (see the command line argument `--single-step`).

This enables Casal2 to implement models for management simulations or scenarios that require feedback and can be used, for example, in operational management procedures (OMPs). The single-stepping process can be automated using **R**, so that Casal2 may be used with **R** to update input harvest values (e.g., catches from a fishery in a fisheries model) to evaluate a particular harvest control rule.

3.7 Validating models across versions

Casal2 has a number of built-in capabilities to validate and verify the code across versions. Unit tests of the underlying Casal2 code are carried out at build time, using the Google Test and Mock unit testing and mocking framework. The unit test framework aims to cover a significant proportion of the key functionality within the Casal2 code base. The unit test code for Casal2 is available as a part of the underlying source code.

Casal2 can also validate or check certain addressables parameters as a part of testing and validation with the assert command. Asserts check the value of a specific addressables (for example, and observations, parameters, or the objective function). Asserts are one aspect of the internal tests Casal2 uses to ensure accuracy across versions and revisions (see Section 14)

3.8 Casal2 exit status values

When Casal2 is run, it will either complete its task successfully or output an error. Casal2 will return a single exit status value 'completed' to the standard output. Error messages will be printed to the console. When input

file configuration errors are found, Casal2 will print error messages, along with the associated filename(s) and line number(s) where the errors were identified, for example,

```
[ERROR] At line 15 in Reports.csl2: Parameter '{' is not supported
```

4 Partition & Categories

Dividing the population into different categories is fundamental to modelling the dynamics of a fish stock. CASAL had a fixed set of hard-wired categories (e.g., factors like sex, area, or stock) and each category type had a predefined set of allowed processes (or transitions in CASAL-speak), e.g., immature fish moving into mature category (Bull et al., 2012). This made sense when CASAL was coded, but now it is seen as a limitation, e.g., changing sex was not allowed and there can only be male and female sexes, not an unknown sex that sometimes occurs in data.

In Casal2 the concept of user defined categories was introduced to allow more flexibility in dividing up the population. Note that Casal2 does not know about sex or area and their properties; these are explicitly built up by the user by specifying processes that act on the categories in the input files. The cost is that users need to follow good practice to achieve clarity and readability of the input files, i.e., poor specifications can result in obscure input files.

4.1 Specifying the partition using categories

A key element of the model is the partition which holds the current state of the population. The partition can be conceptualised as a matrix, where each row represents a category and the columns are the age classes (Figure 4.1). Each row represents all individuals in that category as a numbers-at-age vector. There must be at least one category defined for each model.

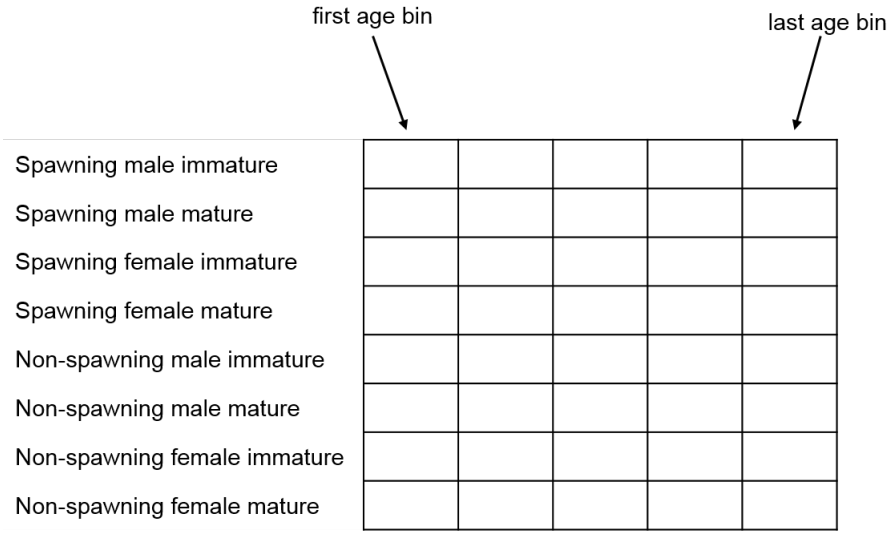

Figure 4.1: A visual representation of a partition.

The categories can include combinations of levels from one or more factors such as sex, maturity state, area, or even species. Casal2 has no predefined categories; *all* categories are defined by the user. Note that the partition only has the current state of the model; past states are not kept (*See* the section on derived quantities about saving past summaries from the partition, p. 49).

To illustrate categories, consider a model of a fish population with two fisheries, one on spawning fish at the spawning grounds and another on the non-spawning population in the rest of the stock area. The mature fish will migrate to the spawning area, where the spawning fishery occurs. At the end of spawning, these fish, along with the recruits from the previous year, migrate back to the non-spawning area. The fish population can be represented by factors sex (levels *male* and *female*), maturity (levels *immature* and *mature*), and area (levels *spawning* and *non-spawning*). So the partition has 8 rows of numbers-at-age, from 2 sexes $\times$ 2 maturity levels $\times$ 2 areas.

These categories are specified in a categories block which starts with a *@categories* line followed on the next line by a *format* subcommand that specifies the factors to use and their order. Factor names are user defined and have no intrinsic meaning to Casal2. The command block is:

```
@categories
format area.sex.mature
names spawn.male.immature spawn.male.mature spawn.female.immature spawn.female.mature
    nonspawn.male.immature nonspawn.male.mature nonspawn.female.immature #all on one line
    nonspawn.female.mature
```

Note the "." syntax to separate the factor names.

Next comes the *names* subcommand which specifies the combinations of levels that makes up each category. In a sense, the *format* subcommand is not needed since the *names* subcommand can define all categories. However, *format* allows a more digestible and shorter syntax to define categories here and in other blocks such as matching observation to categories that provided the data (including combinations of categories, e.g., age compositions that combine both sexes).

For example, the *names* subcommand can be specified by:

```
names spawn,nonspawn.male,female.immature,mature
```

which defines the categories above in a more efficient manner, (again, note the "." to separate the factors and "," to separate the levels within each factor (*see* the next section for more details). A visualisation of the partition is in Figure 4.1.

When using the short-cut syntax in *names*, the order of level combinations is for the levels of the first factor to change the slowest, then the next factor will change faster, and so on with the last factor to changing levels the fastest. The order is important because linking categories to their characteristics, e.g., growth curve or selectivity, is done in other subcommands where these must be specified in the same order.

To exclude unused categories from the partition, the long form must be used in the *names* subcommand, e.g., to exclude *spawn.female.immature* and *spawn.male.immature* since they are never in the spawning area.

To make recruitment to enter the partition in the non-spawning area, use

```
@categories
format area.sex.mature
names spawn.male.mature spawn.female.mature nonspawn.male.immature nonspawn.male.mature
    nonspawn.female.immature
```

4.2 Shorthand syntax for categories

This can be skipped on the first reading.

Some specifications have long lists of categories or years or initial values for parameters and the like, e.g., for YCS from 1900 to 2019, 120 years and 120 initial vales of YCS must be specified; this is hard to do by hand and it can be error prone as well as difficult to match values for each year. Here, the range short cut (*:)* can be used so the the year specification is *1900:2019*, and the multiplier short cut (**)* to give the initial values specification as *1*120*.

There is also shorthand notation for categories since each category can be quite complicated. . First use the `format` subcommand in the *@categories* block to define the factors that make up the sections of the category names. A "." (period) character delineates each factor and this structure allows a shorthand syntax to compose category names.

The `names` subcommand is used to list the category names. Sections within the shorthand syntax for *names* are required to match the order of factors in the *format* subcommand so Casal2 can organise and search on them. In these sections, levels for each factor use the "list specifier" and range characters, e.g.,

```
@categories
format sex.stage.tag # 2 sexes, 2 stages, tag years 2001 to 2005 = 20 categories

names male.immature # Invalid: No tag information
names female # Invalid: no stage of tag information
names female.immature.notag.1 # Invalid: Additional format segment not defined
```

```
names male,female.immature,mature.notag,2001:2005 # Valid shortcut

# Without the shorthand syntax these categories would be written:

names male.immature.notag male.immature.2001 male.immature.2002 male.immature.2003 male.
    immature.2004 male.immature.2005 male.mature.notag male.mature.2001 male.mature.2002 male.
    mature.2003 male.mature.2004 male.mature.2005 female.immature.notag female.immature.2001
    female.immature.2002 female.immature.2003 female.immature.2004 female.immature.2005 female
    .mature.notag female.mature.2001 female.mature.2002 female.mature.2003 female.mature.2004
    female.mature.2005
```

The shorthand syntax available are:

- * Specify all categories
- + Categories join, e.g., *categories* *+ joins all categories together into one unit; *categories male+female* specifies that the observation covers both sexes combined.
- *:* Specify a range of integers ¡int1¿:¡int2¿, e.g., *2000:2005* expands to *2000, 2001, 2002, 2003, 2004, 2005*
- Lists using ",": ¡item1¿,¡item2¿,¡item3¿, e.g., *male,female,unsexed* are the levels for the factor *sex*.
- Repeats a number or label: ¡number — label¿*¡integer¿, e.g., *1*5 –¿ 1 1 1 1 1*
- *format=¡X¿=¡x¿=¡int¿ ¡factor¿=level¿=¡year range¿*, e.g., *tag=2001=1999:2003* the categories with level 2001 in the tag factor are accessible from year 1999 to 2003 inclusive.
- *[]* replace label to a command block with the block defined inline, e.g., *catchability [q = 1e-5]* rather than *catchability CHATq* where *CHATq* labels a command block somewhere in the input files

Example of specifying categories using the short cuts:

This syntax is the long way:

```
@categories
format sex.stage
names male.immature male.mature female.immature female.mature
```

A shorter way to specify the exact same partition structure using *lists*:

```
@categories
format sex.stage
names male,female.immature,mature
```

Casal2 requires categories in processes and observations so that the correct model dynamics can be applied to the correct elements of the partition.

This block illustrates using categories required for the ageing process:

```
# 1. The long-hand way
@ageing my_ageing
categories male.immature male.mature female.immature female.mature

# 2. The first shorthand way
@ageing my_ageing
categories male,female.immature,mature

# 3. Wild Card (all categories)
@ageing my_ageing
categories *
```

```
# 4. The second shorthand way (\textit{obscure}
@ageing my_ageing
categories sex=male sex=female
```

To combine/aggregate categories together, use the "+" special character. For example, this feature can be used to specify that the total biomass of the population is made up of both males and females.

For example,

```
@observation CPUE
type biomass   # observation using an index of biomass
categories male+female
        ...   # other subcommands to link index to the fishery etc
```

This combination/aggregation functionality can be used to compare an observation to the total combined population:

```
@observation CPUE
type biomass
categories *+
 ...   # other subcommands to link index to the fishery etc
```

If the levels `male` and `female` are the only categories in a population (i.e., factor sex), then this is the same syntax as the command block above it.

Shorthand syntax can be useful when applying processes to a select group of categories from the partition.

For example, to apply a spawning migration to the mature categories in the partition giving the partition definition:

```
@categories
format area.maturity.tag
names north,south.immature,mature.notag,2001:2005
```

Then, to migrate a portion of the mature population from the southern area to the northern area:

```
@process spawn_migration
type transition_category   #process to move fish from one category to another
from format=south.mature.* #move all south mature fish, both notag and tagged fish
to format=north.mature.*   # into the relevant north categories
```

Advanced partition syntax

Specific data for a year in a category can be set up so that this category is not to be processed during specific years or in the initialisation phases. Years that each category is available can be specified and these years which will override the default setting of all years in the model. Any category with the default years overridden will no longer be accessible in the initialisation phases.

Examples:

```
@model
start_year 1998   #the model starts in 1996 and
final_year 2010   # goes through to 2010

@categories
format sex.stage.tag
```

```
names male,female.immature,mature.notag,2001:2005 # Valid
# Specify categories with the tag value "2001" are available in years
        #1999, 2000, 2001, 2002, 2003
# And also for categories with the tag value "2005" are available in years
        #2003, 2004, 2005, 2006, 2007
years tag=2001=1999:2003  tag=2005=2003:2007
```

Category	Age					names syntax fragment
	1	2	3	4	5	
male.immature	0	0	0	0	0	male,female.immature,mature
male.mature	0	0	0	0	0	
female.immature	0	0	0	0	0	
female.mature	0	0	0	0	0	
male.immature.2005	0	0	0	0	0	male,female.immature,mature.2005:2010
male.immature.2006	0	0	0	0	0	
male.immature.2007	0	0	0	0	0	
male.immature.2008	0	0	0	0	0	
male.immature.2009	0	0	0	0	0	
male.immature.2010	0	0	0	0	0	
male.mature.2005	0	0	0	0	0	
male.mature.2006	0	0	0	0	0	
male.mature.2007	0	0	0	0	0	
male.mature.2008	0	0	0	0	0	
male.mature.2009	0	0	0	0	0	
male.mature.2010	0	0	0	0	0	
female.immature.2005	0	0	0	0	0	
female.immature.2006	0	0	0	0	0	
female.immature.2007	0	0	0	0	0	
female.immature.2008	0	0	0	0	0	
female.immature.2009	0	0	0	0	0	
female.immature.2010	0	0	0	0	0	
female.mature.2005	0	0	0	0	0	
female.mature.2006	0	0	0	0	0	
female.mature.2007	0	0	0	0	0	
female.mature.2008	0	0	0	0	0	
female.mature.2009	0	0	0	0	0	
female.mature.2010	0	0	0	0	0	
unsexed.immature	0	0	0	0	0	unsexed.immature

Table 4.1: Partition using: *names male,female.immature,mature male,female.immature,mature.2005:2010 unsexed.immature*

Category shortcuts can be used in a sequence to create a complex partition. For example, using the following creates the partition shown in Table 4.1.

```
@categories
format sex.maturation.tag
names male,female.immature,mature male,female.immature,mature.2005-2010 unsexed.immature
#<is equal to>
names male.immature male.mature female.immature female.mature
     male.immature.2005 male.immature.2006 male.immature.2007 male.immature.2008 male.immature
          .2009 male.immature.2010
     male.mature.2005 male.mature.2006 male.mature.2007 male.mature.2008 male.mature.2009 male
          .mature.2010
     female.immature.2005 female.immature.2006 female.immature.2007 female.immature.2008
          female.immature.2009 female.immature.2010
     female.mature.2005 female.mature.2006 female.mature.2007 female.mature.2008 female.mature
          .2009 female.mature.2010
     unsexed.immature
```

Note that the algorithm goes from left to right over the factors in the *format* subcommand. So substituting *unsexed* for *unsexed.immature* is valid and gives a category called *unsexed* in the *sex* factor. But substituting *.immature* (or *.zzz*) for *unsexed.immature* results in one less category and generates an error (i.e., no level provided for factor *sex*).

4.3 Referencing vector and map parameters

To build relationships between command blocks, Casal2 uses a referencing system so that blocks and parameters within blocks can be accessed. In its simplest form, command blocks are referenced by their label. To access specified parameters within a command block, the syntax used is:

```
<syntactic element>     #<>  enclosing a description of the element

# most used version
<block type>[<label of block>].<parameter name>
# e.g., identify a fishery
<block type>[<label of block>].method_<parameter name>

## Examples
# ycs parameter in the process block called recruitment
process[recruitment].ycs
# natural mortality in the process called Fishing
process[Fishing].m
# pot fishery in the process called Fishing
# it is usual to define all fisheries in one
# mortality process block so we need a way to
# identify each one
process[Fishing].method_pot
```

Parameters can be scalars (one value), vectors (several values), or maps. A map consists of two vectors: one containing a key value (for searching or uniquely indexing), and another vector that contains values associated with the index, e.g., specifying YCS values for each year; the years are the key (or index). To reference one or more components of a vector or map use the {} syntax. This is sometime needed when specifying which element(s) in a vector or map are to be estimated.

An example of a map parameter is `ycs_values` in a recruitment process

```
@process   WestRecruitment
# Beverton-Holt function
type       recruitment_beverton_holt
# initial values of the YCS (a vector with 9 values)
ycs_values 1 1 1 1 1 1 1 1
ycs_years 1975:1983
# An alternative method to specify a sequence of values
# use an asterisks to represent a vector of repeating integers
ycs_values 1*8
```

To specify that only the last four years of the YCS parameter `process[WestRecruitment].ycs_values` are to be estimated:

```
@estimate YCS    #YCS is a label to identify this block
#estimate 4 values only: 1980 1981 1982 & 1983
parameter process[WestRecruitment].ycs_values{1980:1983}
```

To estimate a common value for a block of years in a map parameter use the *same* subcommand. We illustrate the idea within the process `@time_varying[label].type=constant`, where we want to fix q over a specified block of years, 1992 to 1995.

First specify the relationships in a `@time_varying` block:

```
@time_varying q_step1
# specify a set value for a year
type          constant
# parameter ref for q in block Fishq
parameter     catchability[Fishq].q
# or 1992:1995 = key into value
years  1992 1993 1994 1995
```

```
value  0.2 0.2 0.2 0.2
# or 0.2*4, initial values of q
```

Next, to estimate only one q value for the time block, pick one element of the map (say 1992), and then force all other years to have the same value:

```
@estimate q_block_1992
# estimate this one
parameter time_varying[q_step1].value{1992}
# set these to the value for 1992
same      time_varying[q_step1].value{1993:1995}
# uniform prior on q
type      uniform
lower_bound 0.1
upper_bound  10
```

Keys are restricted in Casal2 to years and categories. An example using categories as a key in a map:

```
@category
factor sex
names male female

@process recruit
categories male female
# natural mortality values indexed by categories
m  0.17 0.17
...

@estimate M
# prior = uniform
type uniform
# estimate male M, "male" is a level for factor sex
parameter recruitment.[m]{male}
# set female M to the same value as male's
same recruitment.[m]{female}
```

For vector parameters (i.e., no key values), the index is an integer starting with 1 for the first value. An example is the selectivity *all.values.bounded* which can be defined by:

```
@selectivity MatSel
type         all_values_bounded
# lower bound at age 2
L            2
# upper bound at age 4
H            4
# 3 values, one for each age 2, 3, and 4
v            0.1 0.2 0.7

@estimate  mature
# prior = uniform
type       uniform
# estimate the 2nd value only, i.e., age 3
parameter selectivity[MatSel].v{2}
# lower parameter range
lower_bound 0.1
```

```
# upper parameter range
upper_bound 1.0
```

The integer *2* cannot be used to specify the *q* parameter for 1993 in the above example labelled *q_block_1992*. This will pass the syntax test, but it will fail at the validate stage in Casal2.

In-line declaration, avoiding extra command blocks In-line declarations can help shorten models by defining `@` blocks within the subcommand line instead of having a label that points to a command block define somewhere else in the input files.

For example, catchability for an CPUE index series can be defined inline:

```
@observation chatCPUE
type biomass                    # biomass index
catchability [q=6.52606e-005]  # define catchability here
categories male+female          # index cover both sexes together


@estimate chatCPUE_q
parameter catchability[chatTANbiomass.one].q # how to reference q
type uniform_log     # prior
lower_bound 1e-2
upper_bound 1
```

In the above code catchability is defined and estimated without explicitly creating a `@catchability` block.

5 The population section: model structure and the population dynamics

The command and subcommand syntax for the estimation section is given in Section 9.

5.1 Introduction

This section shows how to specify a model for the population dynamics. It describes the model time and age scope, the population processes used (e.g., recruitment, ageing, migration, and mortality), the selectivities, and how to set values for their associated parameters, or starting values if they are going to be estimated.

The basic structure of the population is defined in terms of its partitions and the succession of processes that act on them throughout a year. Casal2 assumes an annual cycle, i.e., rates like natural mortality are assumed to be for a year. To place certain processes or observations (e.g., a research survey) into the right part of the year, the year can be divided into one or more time steps, and each time step needs at least one process. Each time step can represent a specific period of the calendar year, or it can be an abstract sequence of events. Certain processes like natural mortality and growth can have a proportion of the effects of the process assigned to different time steps to crudely mimic seasonal effects, or fisheries that occur in short periods of the year, as well as place a survey within the year relative to the proportion of annual natural mortality that has occurred (see Section 5.4).

The *state* is the current status of the population at any given time and it can change one or more times during the year. The state object must contain sufficient information to determine how the population changes over time, given a model and a complete set of parameters. The partition is key to the state, but it has no ”memory”. Thus, other information must also be kept, such as the mature biomass from a previous year or time step to calculate the recruit numbers into first age class via the spawner-recruitment function. The latter are specified as *derived variables* and they are kept for the whole model run. However, the *derived variables* record only summary information from the partition at a specified time step and year.

Processes can change the partition and, for example, include recruitment, natural mortality, fishing mortality, ageing, migration, and maturation. These processes are repeated for each year of the model.

The specification and ordering of processes in multiple time steps can be used to represent complex dynamics, with the intermingling of multiple species and stocks, migration patterns occurring over multiple areas, and/or multiple sources of anthropogenic impacts using a range of methods which cover different areas and times.

However, the complexity of a stock structure definition is constrained by the available data. It is challenging to use a complex structure to model a population when there are no observations to support that structure. For information on how to define categories and use the shorthand syntax see Section 4.2.

Topics covered are:

- The model scope, such as the ages covered, the years over which the model runs, and the end year for projections;
- Linking processes, such as growth to each category;
- The number of time steps and the processes that are applied in each time step;
- The specification of and the parameters for the population processes: processes that add or remove individuals from a partition, or shift individuals between ages and categories in a partition;
- The initialisation process: the state of the partition at the start of the first year;
- Defining selectivities and linking them to observations;
- The parameters: their definitions, initial values, and other characteristics; and
- Derived quantities, e.g., mature biomass, to include in density-dependent processes such as the spawner-recruit relationship

5.2 Model scope and structure

The model needs scoping for ages and year covered. This is done in the *@model* command block.

Each Casal2 model requires:

- The minimum and maximum population ages

- Whether the maximum age is a plus group
- The start and final year
- The names of all of the categories

The ages used starts at the minimum age through to the maximum age in steps of one. The model is run from the start year through to the final year. It can also be run past the final year to project the state of the population through the final projection year.

An example of how to specify a potential model with two categories is outlined below; the `@model` and `@categories` blocks are:

```
@model
start_year 1981
final_year 2000
projection_final_year 2010
base_weight_units     tonnes
min_age     1
max_age   20
age_plus_group        true
initialisation_phases Equilibrium_phase
time_steps            step1 step2 step3

@categories
format      sex
names       male female
age_lengths male_growth female_growth  #labels for growth blocks
```

This model runs for 20 years, starting in 1981, and will do a projection over 10 years for a population with ages from one and twenty, with age 20 being a plus-group. Each year is divided into three time-steps. The categories are male and female (i.e., there is one category factor, labelled sex) and each category has an age-length relationship.

Whist Casal2 generally uses generic formulation, it does have some specific population concepts, in this case, growth which can vary for each category. Additionally, there is a length-weight concept which is specified in the age-length blocks, here blocks starting with `@age_size male_growth` and `@age_size female_growth` that are placed elsewhere in the input files (not shown).

Casal2 allows categories of the partition to exist for a subset of years of a model. This feature enables more efficient computations when models contain categories that do not persist over all model years. A model may define one-off processes that transition individuals from one category into another in a subset of the model initialisation phases or years (e.g., tagging events). Excluding categories for certain years can be more efficient as Casal2 will not initialise these categories or apply processes to categories in years or time steps in which they do not exist.

The structure of the partition is defined in a configuration block with the `@categories` block (Section 5.2).

Derived quantities are an important component of the state object. An example of a derived quantity is spawning stock biomass (SSB; the biomass of [female] spawning fish calculated at the mid point of the spawning season). Casal2 calculates derived quantities using the command `@derived_quantity`, required for some processes. In fisheries stock assessment models, a recruitment process which includes a stock-recruitment relationship requires the definition of a derived quantity that specifies the mid-season spawning stock biomass. See Section 5.4 for more details.

5.2.1 The implicit annual cycle

There is an implicit annual cycle that orders the sequence of processes within the year, but there is no command block as such. The implementation is by ordering processes within the time-steps. This sequence is repeated for every year. Time steps are used to break the year into separate components and allow observations to be associated with specific time periods and processes. Any number of processes can occur within each time

step, in any order, although there are restrictions for mortality-based processes (see Section 5.3.3); processes can occur multiple times within each time step. Time steps are not implemented during the initialisation phases (effectively there is only one initialisation time step), and the annual cycle in the initialisation phases can be different from the annual cycle specified for the model years (5.2.2).

Figure 5.1 shows an example of the annual cycle using three time-steps.

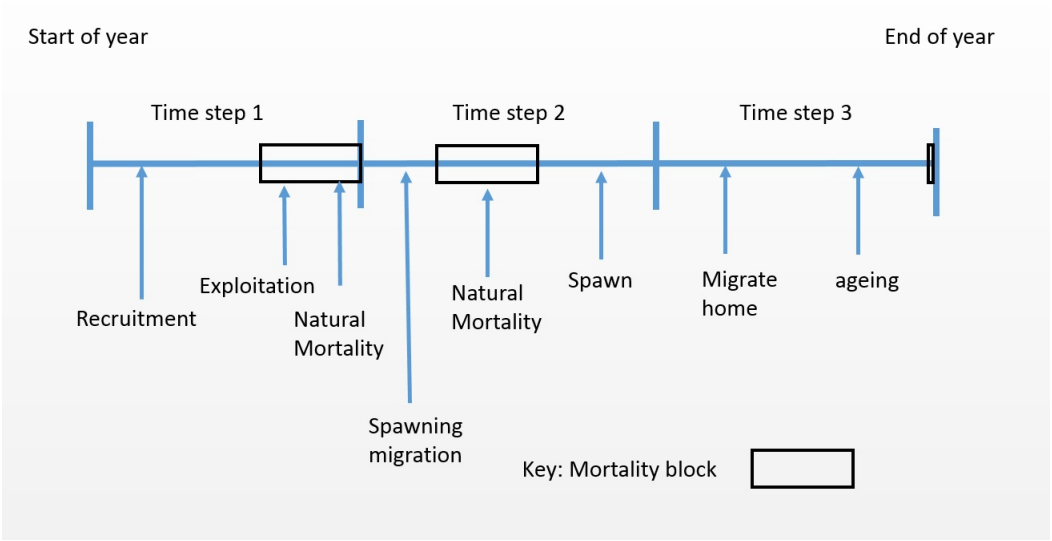

Figure 5.1: A example sequence for an annual cycle.

This would be specified using @time_step block:

```
@model
time\_steps step1 step2 step3
```

This gives the order and labels for each time step, i.e., 3. Processes are sequenced using order within the *@time_step* block:

```
@time_step step1
processes Recruitment Fishing

@time_step step2
processes Spawn_migration Fishing

@time_step step3
processes Home_migration Ageing
```

The *Recruitment*, *Fishing*, *Spawn_migration*, *Home_migration* and *Ageing* are all labels of command blocks that defines a process (see 5.3 for the list of available processes). The order that the processes are executed is in the same order as specified. The process *Fishing* could be the process type `Instantaneous_Mortality` (5.3.3) which takes natural mortality as a parameter as well as specifying the catches in the time-steps, so it is possible to have all catch taken in time-step *step1* with some natural mortality, and no fishing in time-step *step2* where the rest of the natural mortality occurs.

Although *Spawn* represents a biological process, spawning, for the usual modelling it is the time that the spawning stock biomass is calculated since this is needed to calculate recruitment is there is a spawning biomass recruitment relationship. A related concept is maturity which can be in the partition, so there needs to be a transfer of immature fish into the mature category, i.e., a process, but it is only indirectly related to spawning. Hence, in modelling, spawning is not a process that affects the partition directly, but it the time to

calculate the SSB which must be setup as a derived variable (from the partition). Hence, *Spawn* is located in Figure 5.1.

To calculate the SSB a `@derived_quantity` command block is needed in which the ”timing” of the SSB calculation in terms of which time-step and the proportion of natural mortality within it is specified (5.4).

5.2.2 The initialisation phases

Initialisation is the process of determining the model starting state at the start of the first year (`Start_year`. The initial state can be equilibrium/steady state or some other initial state for the model (e.g., exploited), prior to the start year of the model.

There are multiple options for partition initialisation in Casal2, including

- Iterative: run the model for a specified number of years to get the converged state.
- Derived: Use the analytical solution (i.e., faster than iterative) for the initial state, but it does not work for some processes (e.g., density dependant migration)
- Cinitial: Allow the estimation of the initial partition's numbers-at-age
- state_category_by_age: specify the partition's numbers-at-age

Initialisation specifications starts with nominating the initialisation label in the *@model* command block followed by a *@initialisation_phase* command block specifying the type and other settings:

```
@model
...     # other subcommands
initialisation_phase int_label

@initialisation_phase int_label
type iterative  #choose one from the list above
...             # specify option values
```

If needed, the processes used and their order in the initialisation are those specified in the annual cycle, but these can by changed by either excluding some processes or including others by using the `exclude_processes` or `insert_processes` subcommands in the *initialisation_phase* command blocks,

```
@initialisation_phase int_label
type iterative
exclude_processes Fishing
insert_processes step1(recruitment)=initialFishing
            #format=<step>(<insert before label>)-<new block label>
...             # specify option values
```

where *Fishing* is the normal fishing process which defines natural mortality so when excluded, initialisation can use another value that incorporates some unrecorded fishing before the start of the assessment period by setting natural mortality to a higher value in the process *initialFishing*. The place to insert *initialFishing*is in the time-step labelled *step1* before the process *recruitment* which must be in that time-step (process label is enclosed in brackets). To insert at the end of the time-step use *()*, i.e. *step1()=initialFishing*.

Normally,the type *iteration* is used, but more complicated initialisation can by used by sequencing other phases one after another,

```
@model
...     # other subcommands
```

```
initialisation_phase int_label int_label2


@initialisation_phase int_label
type derived    #choose one from the list above
...             # specify option values

@initialisation_phase int_label2
type iterative    #choose one from the list above
...             # specify option values
```

which may be faster overall since less iterations can be used in the second phase. The order of applying each initialisation is that given in the *@model* command block.

The multi-phased initialisation allows for flexibility in the number and type of initialisation, for initialising a non-equilibrium starting state, or applying simple processes before applying more complex ones.

In each initialisation phase, the processes defined for that phase are applied and used as the starting point for the following phase or, if it is the last phase, the start year of the model.

The *first* initialisation phase is always initialised with each age and category set to zero. Care must be taken when using complex category inter-relationships or density-dependent processes that depend on a previously calculated state, as they may fail when used in the first phase of an initialisation.

Multi-phase iterations can also be used to determine if an initialisation has converged. A second initialisation phase can be added for 1 year, with the same processes applied as in the first phase. The state at the end of the first and second phase is then output. If these states are identical, then it is likely that the initialisation has converged to an equilibrium state.

Iterative Initialisation The `iterative` initialisation is a general solution for initialising the model, but can be slow to converge, depending on the model.Its value is that it can work on complex structured models that may be difficult or impossible to implement using analytic approximations.

The number of iterations in the iterative initialisation can increase the model output, and the number of iterations should be chosen to be large enough to allow the population state to fully converge. A period of about two times the maximum age is recommended to ensure convergence. Casal2 can be configured to report convergence statistics that can assist in determining convergence properties.

In addition, the iterative initialisation phase can optionally be stopped early if user-defined convergence criteria is met. For a list of supplied years in the initialisation phase, the convergence criteria is met if the proportional absolute summed difference between the state in year $t-1$ and the state in year t ($\widehat{\lambda}$) is less than the user-defined value of λ, where

$$\widehat{\lambda} = \frac{\sum_{i,j} \left| \text{element}(t)_{i,j} - \text{element}(t-1)_{i,j} \right|}{\sum_{i,j} \text{element}(t)_{i,j}} \tag{5.1}$$

where $\text{element}(t)_{i,j}$ denotes the numbers at time step t in category j and age class i.

Hence, for the initialisation define:

- The number of initialisation phases,
- The number of years in each phase, and
- The processes to apply in each phase, where the default processes are those applied in the annual cycle

An example with one initialisation phase:

```
@model
```

```
...
initialisation_phases Iterative_initialisation

@initialisation_phase Iterative_initialisation
type iterative
years 50                # do 50 iterations
lambda 0.0001
convergence_years 20 40 # test for convergence at 20 and 40 iterations
```

Derived Initialisation The `derived` initialisation is an analytical solution that calculates the equilibrium age structure and the plus group using a geometric series solution. The benefit of this method is it can be solved in `max_age - min_age + 1` years or time-steps units, so it is computationally faster than the iterative initialisation phase. Under some process combinations (e.g., one-way migrations) this initialisation does not calculate the exact equilibrium partition. When using this initialisation, confirm that the partition has reached an equilibrium state by either comparing with an iterative initialisation, or by adding a second iterative initialisation phase with a limited number of iterations for comparison.

An example with one initialisation phase:

```
@model
...
initialisation_phases Equilibrium_initialisation

@initialisation_phase Equilibrium_initialisation
type derived
```

Cinitial Initialisation The `cinitial` initialisation can only be applied after *derived* or *iterative* initialisation phases. This initialisation can be a method for estimating the non-equilibrium state of population if there is exploitation before data is collected. The estimated *cinitial* factors shift the initial population away from an equilibrium state prior to the start year.

After the first initialisation phase we have an equilibrium age-structure denoted by N_{equil}.

Ciniital specifies an age structure denoted by N_{cinit} (in numbers), but this can be combinations of categories, say both sexes by two areas.

$Multiplier = N_{cinit}/N_{equil}^{combined}$

where $N_{equil}^{combined}$ is summed over the same combined categories as *Cinitial*. Then

$N_{init} = N_{equil} * Multiplier$

N_{init} is the numbers-at-age by category for the start of the model run.

It would be helpful to include an observation of age composition data for the first year of the model in order to estimate the non-equilibrium population state.

An example with two initialisation phases:

```
@model
...
initialisation_phases Iterative Cinitial

@initialisation_phase Iterative
type iterative
years 10
lambda 0.0001
convergence_years 10 20

@initialisation_phase Cinitial
```

```
type cinitial
categories spawn.male+nonspawn.male spawn.female+nonspawn.female
table n
spawn.male+nonspawn.male     5e7 5e7 7e6 6e6 5e6 4e6 3e6 2e6 1e6 1e6 1e1 1e1 1e1 1e1
spawn.female+nonspawn.female 5e7 5e7 7e6 6e6 5e6 4e6 3e6 2e6 1e6 1e6 1e1 1e1 1e1 1e1
end_table
```

The Cinitial factors can also be estimated with the syntax

```
@estimate cinit_male
parameter initialisation_phase[Cinitial].spawn.male+nonspawn.male
same initialisation_phase[Cinitial].spawn.female+nonspawn.female
lower_bound  2e2  2e2  2e2  2e2  2e2  2e2  2e2  2e2  2e2  2e2  2e0  2e0  2e0  2e0
upper_bound  2e9  2e9  2e9  2e9  2e9  2e9  2e9  2e9  2e9  2e9  2e9  2e9  2e9  2e9
type uniform
```

State_category_by_age The `state_category_by_age` initialisation uses a user-defined table as the initial partition numbers-at-age for the beginning of the start year. Models can be initialised by specifying the numbers-at-age for each category.

An example with one initialisation phase:

```
@model
...
initialisation_phases Fixed

@initialisation_phase Fixed
type state_category_by_age
categories male female
min_age 3
max_age 10
table n
male   1000 900 800 700 600 500 400 700
female 1000 900 800 700 600 500 400 700
end_table
```

When initialising models with this type, undefined behaviour may result if the model applies processes that require derived quantities to be calculated in the initialisation phase. (e.g., SSB so that recruitment can be calculated for the start year). In the latter case, you would have to use a subsequent initialisation phase *iterator* that has natural mortality set to zero (i.e., *insert_processes* subcommand to introduce zero natural mortality and *exclude_processes* to exclude the mortality process that defines natural mortality) for as many year needed to set up the SSBs.

5.3 Population processes

Population processes are processes that change the model state. These processes produce changes in the partition by adding or removing individuals, or by moving individuals between ages and/or categories.

Current population processes available include:

- recruitment,
- ageing,
- growth,
- maturation,
- mortality events (e.g., natural and fishing), and

- category transition processes, i.e., processes that move individuals between categories while preserving their overall age structure.

There are two types of processes: (1) processes that occur across multiple time steps in the annual cycle, e.g., `mortality_constant_rate` and `mortality_instantaneous`; and (2) processes that occur only within the time step in which they are specified.

5.3.1 Recruitment

Recruitment processes add new individuals to the partition. Recruitment depends on virgin biomass or alternatively recruitment in the virgin state and so these parameters are located in this process (as *b0* and *r0*). The other factors needed are SSB if there is a stock-recruitment relationship and the CV for the prior on YCS (the mean is mandated to be 1 over some specified year range). Thus, a SSB label may have to be included (pointing to a derived quantity).

In the recruitment processes, a number of individuals are added to a single age class (subcommand *age*) within the partition, with the number determined by the type of stock-recruitment process specified. If recruits are added to more than one category, then the proportion of recruits to be added to each category is specified by the `proportions` subcommand. For example, if recruiting to categories labelled `male` and `female`, then the proportions may be set to 0.5 and 0.5, so that half of the recruits are added to the male category and the other half to the female category.

Recruitment can differ between a spawning event or the creation of a cohort/year class. One view for fisheries is that recruitment usually refers to individuals "recruiting" to a fishery. This definition is used because there is usually not a lot of information on younger age classes between the time of spawning and being vulnerable to a survey or fishery for data collection. However, here, recruitment is to a fixed age class for one or more categories.

The offset between spawning and recruitment is parametrised either by the recruitment subcommand `age`, or `min_age`, which is the default value for the `age` subcommand in the recruitment process. The Casal2 parameter `age` is the same as the CASAL parameter `y_enter`. Notice that the minimum age is usually different from zero and so there is usually a one or more year's delay between spawning and recruitment into the partition. There is also a complication from when spawning occurs in the annual cycle and when recruitment occurs.

Casal2 has two recruitment processes, constant recruitment and the Beverton-Holt stock-recruitment relationship (Beverton and Holt, 1957). The number of individuals following recruitment in year y is

$$N_{y,a,j} \leftarrow N_{y,a-1,j} + p_j(R_y) \tag{5.2}$$

where $N_{y,a,j}$ is the numbers in year y and category j at age a, p_j is the proportion added to category j, and R_y is the total number of recruits in year y.

Constant recruitment In the constant recruitment process the total number of recruits added in each year y in age a is R_y, with $R_y = R_0$ for all years

$$R_{y,j} = p_j(R_0) \tag{5.3}$$

Constant recruitment is equivalent to a Beverton-Holt recruitment process with steepness (h) set to 1.

For example, to specify a constant recruitment process where individuals are added to the male and female immature categories at $age = 1$ in equal proportion (`proportions` = 0.5), and the number to add is $R_0 = 5 \times 10^5$, the syntax is

```
@process Recruitment
type constant_recruitment
categories male.immature female.immature
proportions 0.5 0.5
r0 500000
age 1
```

Beverton-Holt recruitment In the Beverton-Holt recruitment process the total number of recruits added each year is R_y. R_y is the product of the average recruitment R_0, the annual year class strength multiplier YCS, and the stock-recruit relationship $SR(SSB_y)$

$$R_{y,a,j} = p_j(R_0 \times YCS_{ycs\_year} \times SR(SSB_{ycs\_year})) \tag{5.4}$$

where

$$ycs\_year = y - \texttt{ssb\_offset} \tag{5.5}$$

and a is age, p_j is the proportion of recruits to enter category j, and `ssb_offset` is the number of years lag between spawning and recruitment.

Recruitment refers to recruitment into the population and may differ from the spawning event. See below on more information about `ssb_offset`. In general this parameter should not be specified by the user.

$SR(SSB_y)$ is the Beverton-Holt stock-recruit relationship parametrised by the steepness h, and based on Mace and Doonan (1988) parametrisation

$$SR(SSB_y) = \frac{SSB_y}{B_0} / \left(1 - \frac{5h-1}{4h}\left(1 - \frac{SSB_y}{B_0}\right)\right) \tag{5.6}$$

The Beverton-Holt recruitment process requires a value for B_0 and SSB_y to calculate the number of recruits. A derived quantity (see Section 5.4) must be defined that provides the annual SSB_y for the recruitment process. B_0 is then defined as the value of the SSB at the end of one of the initialisation phases, which is defined by the parameter `b0_initialisation_phase`.

During initialisation the YCS multipliers are assumed to be equal to 1, and recruitment that happens in the initialisation phases that occur before and during the phase when B_0 is determined are assumed to have steepness $h = 1$ (i.e., in those initialisation phases, recruitment is equal to R_0).

Recruitment in the initialisation phases after the phase where B_0 was determined are calculated using the Beverton-Holt stock-recruit relationship. R_0 and B_0 have a direct relationship when there are no density-dependent processes in the annual cycle. Models can thus be initialised using B_0 or R_0.

An example of the specification of a Beverton-Holt recruitment process, where individuals are added to the category "immature" at $age = 1$, and the number added is $R_0 = 5 \times 10^5$; `SSB_derived_quantity` is a derived quantity that specifies the total spawning stock biomass that contributed to the year class, with B_0 the value of the derived quantity at the end of the initialisation phase labelled `phase1`; and YCS are standardised to have mean one in the period 1995 to 2004, and recruits enter into the model two years following spawning

```
@process Recruitment
type recruitment_beverton_holt
categories immature
proportions 1.0
r0 500000
b0_initialisation_phase phase1
steepness 0.75
age 1
ssb SSB_derived_quantity
```

The property `ssb_offset` should not be manually specified; Casal2 determines `ssb_offset` by the order of ageing, recruitment, spawning, and the recruitment parameter `age`

- if the annual time step order is recruitment, ageing, spawning, then `ssb_offset` should equal `age` + 1, or
- if the annual time step order is spawning, ageing, recruitment, then `ssb_offset` should equal `age` - 1, or
- `ssb_offset` = `age`

There may be scenarios where the user will input these values, e.g., if there are multiple ageing processes in the annual cycle. Casal2 does not have functionality to accommodate this situation, so in this case `ssb_offset` would be manually defined.

There are two variants of this process and they refer to how the stock recruitment residuals or YCS_{ycs_year} are parametrised. This parametrisation can either be in natural space as year class strength (YCS) multipliers, or in log space as recruitment deviations. Due to the difference in terminology, these variants are implemented in two separate processes, `type recruitment_beverton_holt` and `type recruitment_beverton_holt_with_deviations`, respectively.

YCS (YCS_y) The YCS parameter (`ycs_years`) is defined in Equation (5.5). The parameter `ycs_values` is referenced by the `ycs_years` parameter and is important to note when defining `@estimate`, `@project`, and `@time_varying` blocks for the parameter `ycs_values`. An example is at the end of the section.

A common practice when estimating YCS is to standardise using the Haist parametrisation, which was described by V. Haist. Casal2 will standardise YCS only if subcommand `standardise_ycs_years` is defined. The model parameter `ycs_values` is a vector $\mathbf{Y}$, covering the years from `start_year` - `ssb_offset` to `final_year` - `ssb_offset`, as defined by the parameter `ycs_years`. The resulting year class strengths are calculated by $YCS_i = Y_i/\bar{\mathbf{Y}}$, where the mean is calculated over the user-specified years `standardise_ycs_years`.

$$YCS_i = \begin{cases} Y_i/mean_{y\in S}(Y_y) & : y \in S \\ Y_i & : y \notin S \end{cases}$$

where S is the set of years from `standardise_ycs_years`. One effect of this parametrisation is that R_0 is then defined as the mean estimated recruitment over the set of years S, because the mean YCS multiplier over these years will always be one.

Typically `standardise_ycs_years` is defined to span the years over which YCS is reasonably well estimated. For years that are not well estimated, Y_y can be set to 1 for some or all years $y \in S$ (which is equivalent to forcing $R_y = R_0$ x $SR(SSB_y)$) by setting the lower and upper bounds of these Y values to 1. An exception to this might occur for the most recent YCS values, which the user may estimate but not include in the definition of R_0 (because the estimates may be based on too few data). One or more years may be excluded from the range of years for the averaging process of the Haist parametrisation.

The advantage of the Haist parametrisation is that a large penalty is not necessary to force the mean of the YCS parameter to be 1, although a small penalty should still be used to stop the mean of $\mathbf{Y}$ from drifting. These adjustments may improve MCMC performance. Projected YCS values are not affected by this feature. A disadvantage with this parametrisation in a Bayesian analysis is that the prior applies to Y, not YCS.

In the example given above, YCS are standardised to have mean one in the period 1995 to 2004, and recruits enter into the model two years following spawning

```
@process Recruitment
type recruitment_beverton_holt
...            #subcommand above
standardise_ycs_years 1995:2004
ycs_years  1994 1995 1996 1997 1998 1999 2000 2001 2002 2003 2004 2005 2006
ycs_values 0.65 0.87  1.6 1.13 1.02 0.38 2.65 1.35    1    1    1    1    1
```

Recruitment deviations, ε_y **(*type recruitment_beverton_holt_with_deviations*)** Recruitment deviations represent the stock-recruitment relationship residuals in log space, with the link between YCS_y and ε_y

$$YCS_y = exp(\varepsilon_y - b_y \sigma_R^2/2) \tag{5.7}$$

where $\varepsilon_y \sim N(0, \sigma_R^2)$, σ_R^2 is the variance of the stock-recruitment residuals, and b_y is a bias correction defined by Methot Jr and Taylor (2011)

$$b_y = \left\{ \begin{array}{ll} 0, & \text{for } y \leq y_1^b \\ b_{max}(1 - \frac{y - y_1^b}{y_2^b - y_1^b}), & \text{for } y_1^b < y < y_2^b \\ b_{max}, & \text{for } y_2^b \leq y \leq y_3^b \\ b_{max}(1 - \frac{y_3^b - y}{y_4^b - y_3^b}), & \text{for } y_3^b < y < y_4^b \\ 0, & \text{for } y_4^b \leq y \end{array} \right\} \tag{5.8}$$

The ε_y values are normally distributed in log space and thus lognormal when back-transformed to the resulting stock-recruitment relationship YCS_y. Recent work has found that this transformation does not technically lead to the *a priori* assumption that the resulting YCS_y are lognormal.

The ramp function described above for the bias correction has the additional subcommands controlling the ramp

- $y_1^b =$ `last_year_with_no_bias`
- $y_2^b =$ `first_year_with_bias`
- $y_3^b =$ `last_year_with_bias`
- $y_4^b =$ `first_recent_year_with_no_bias`
- $b_{max} =$ `b_max`

```
@process Recruitment
type recruitment_beverton_holt_with_deviations
categories immature
proportions 1.0
r0 500000
last_year_with_no_bias 1940
first_year_with_bias 1950
last_year_with_bias 2016
first_recent_year_with_no_bias 2018
b_max 0.85
b0_initialisation_phase phase1
steepness 0.75
age 1
ssb SSB_derived_quantity
deviation_years  1994-2006
deviation_values 0 -0.2 0.4 0 0 0 0 0 0 0 0 0 0
```

Recruitment when modelling two stocks (or species) To specify a Beverton-Holt recruitment for each stock, the information required is:

1. *YCS*, starting from year (`start_year - ssb_offset`) and extending up to year (`final_year - ssb_offset`)
2. the value of `age` (which is `y_enter` in CASAL)
3. the steepness parameter `h`

4. in a multi category model, the proportion of recruits for each category
5. a label for the derived quantity

When an `@initialisation_phase` (Section 5.2.2) type = `derived` is specified and the recruitment is defined by `b0`, then all categories must be specified in the `@recruitment` block. Usually in a recruitment processes only the categories that receive recruits need to be defined. For example, a population has a spawning area that is different from the area where recruits enter the population. An area-specific model could then be specified which contains spawning categories and recruiting categories. The recruiting categories would be specified in the subcommand `categories`, as these would be the categories receiving recruits.

If `@initialisation_phase`, `type=derived` is used, then all categories that are a part of that recruitment process need to be specified as well. For example,

```
@process Recruitment_stock1
type recruitment_beverton_holt
categories stock1.immature.M stock1.immature.female stock1.spawn.male stock1.spawn.female
proportions 0.5 0.5 0.0 0.0
r0 500000
ssb SSB1
....

@process Recruitment_stock2
type recruitment_beverton_holt
categories stock2.immature.male stock2.immature.female stock2.spawn.male stock2.spawn.female
proportions 0.5 0.5 0.0 0.0
r0 200000
ssb SSB2
....
```

The `proportions = 0.0` for ”spawn.male” and ”spawn.female” are needed due to the way the derived initialisation phase works. The derived initialisation finds a solution for when `r0` = 1.0 based on an infinite geometric series for the plus group, and scales the initial partition by `r0`. Thus, if all categories are not specified, then those that are missed would not be initialised to true values and this could lead to inaccurate model outputs. This set-up extends to multiple-stock fisheries model configurations as well, where all of the categories that make up the stock need to be listed.

5.3.2 Ageing

The ageing process ”ages” individuals, i.e., this process moves all individuals in the named categories j from one age class a to age class $a+1$, or accumulates them if the last age class is a plus group.

The ageing process is defined as,

$$\text{element}(a+1, j) \leftarrow \text{element}(a, j) \tag{5.9}$$

except in the case of the plus group (if defined),

$$\text{element}(a_{\max}, j) \leftarrow \text{element}(a_{\max}, j) + \text{element}(a_{\max-1}, j). \tag{5.10}$$

For example, to apply ageing to the categories `immature` and `mature`, the syntax is

```
@process Ageing
type ageing
categories immature mature
```

Note: the ageing process is *NOT* applied by Casal2 by default — it needs to be explicitly specified. As with all other processes, Casal2 will not apply a process unless it is defined and specified within the annual cycle. Hence, it is possible to specify a model where a category is not aged. *Casal2 will not check or otherwise warn if there is a category defined where ageing is not applied.*

5.3.3 Mortality

There are 8 types of mortality processes available in Casal2:

- constant rate,
- event,
- biomass-event,
- instantaneous,
- instantaneous retained (discards),
- Holling,
- initialisation, and
- a density-dependent relationship based on prey suitability.

These processes remove individuals from the partition, either as a rate, as a total number (abundance), as a biomass of individuals or, as a combination of these. Casal2 does not (yet) implement the Baranov catch equation. However, instantaneous mortality is considered an approximation to the Baranov catch equation.

To apply both natural and biomass-event mortality, the mortality type `mortality_instantaneous` can be specified. Or, you can use `mortality_instantaneous_retained`, where discards are allowed. Mortality blocks are special because they allow both natural mortality and fishing mortality at the same time. Note that all mortality processes occur within the mortality block of a time step. See Section 5.3.3 for more information and definitions on mortality blocks.

Timing evaluation interval; timing the point when observations are fitted or derived quantities are evaluated Observations (see Section 7) and derived quantities (see Section 5.4) need a concept called a *timing evaluation interval* so that the ”time” within a year can be specified for their fit or evaluation. This interval is intimately tied into mortality processes.

There can be one or more mortality processes specified within a time-step, but these must be grouped sequentially, i.e., there cannot be a non-mortality process between any two mortality processes within any one time step. The sequence of mortality processes is called a *timing evaluation interval*. If no mortality processes occurs in a time step, then the *timing evaluation interval* is defined to occur at the end of the time step, i.e., it is a virtual, unspecified, process. Thus each time step has one *timing evaluation interval*.

Casal2 will output an error if more than one *timing evaluation interval* occurs in a single time step.

The ”time” for an observation or derived quantity is based on the proportion of mortality that has occurred within the *timing evaluation interval*. The starting and ending partition are saved so that a partition can be estimated by interpolation between the start and end partitions.

For example, the point of calculation can be set to a point when 75 % of the deaths from natural mortality plus catch has occurred The partition at this point is based on interpolating between the start and end of the interval as the partition is known at those points. Two methods are available: `weighted_sum` and `weighted_product`, and are defined as

- `weighted_sum`: after proportion p through the mortality block, the partition elements are given by $n_{p,j} = (1-p)n_j + p'_j$
- `weighted_product`: after proportion p through the mortality block, the partition elements are given by $n_{p,j} = n_j^{1-p} n_j'^{p}$

where $n_{p,j}$ is the derived quantity at proportion p of the mortality block for category j, n_j is the quantity at the beginning of the mortality block, and n'_j is the quantity at the end of the mortality block.

In the case of a virtual *timing evaluation interval*, the partition at the end of the time-step is used.

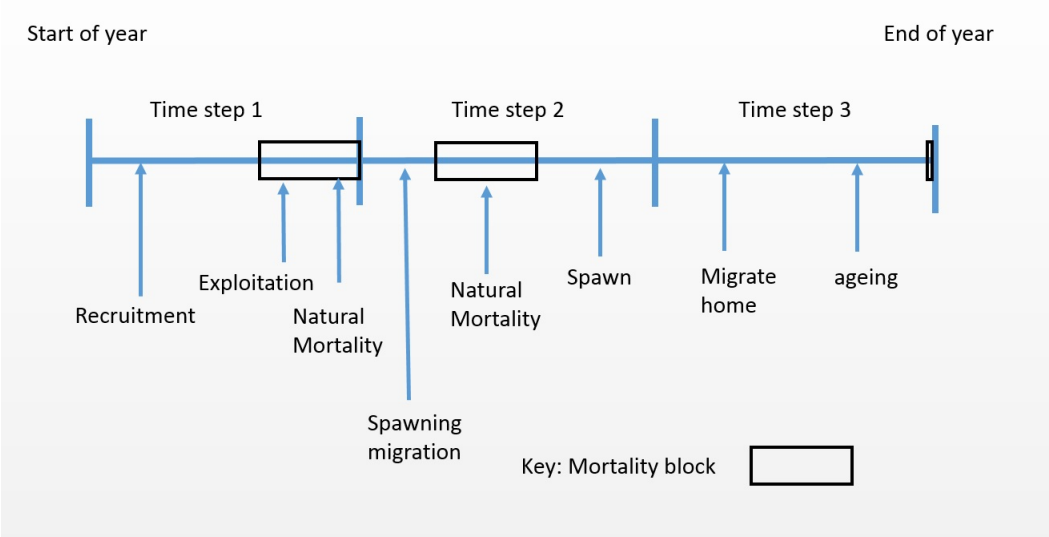

Figure 5.2: A example sequence for an annual cycle.

Constant mortality rate To specify a constant annual mortality rate (e.g. $M = 0.2$) for categories "male" and "female"

```
# A process with label NaturalMortality
@process NaturalMortality
type          mortality_constant_rate
categories    male female
# effectively age related mortality
relative_m_by_age One One
m             0.2 0.2
```

The total number of individuals removed from a category

$$D_{j,t} = \sum_a N_{a,j,t}[1 - \exp(-S_{a,j}M_{a,j}p_t)] \tag{5.11}$$

where $D_{j,t}$ is the total number of deaths in category j in time step t, $N_{a,j,t}$ is the number of individuals in category j of age a in time step t, $S_{a,j}$ is the selectivity value for age a in category j, $M_{a,j}$ is the mortality rate for category j for age a, and p_t is the proportion of the mortality rate to apply in time step t.

The mortality rate process requires the specification of the mortality-by-age curve which is specified using a selectivity. To apply the same mortality rate over all age classes in a category, use a selectivity defined as $S_{a,j} = 1.0$ for all ages a in category j

```
@selectivity One
type constant
c 1
```

Age-specific mortality rates can also be applied. For example, the hypothesis that mortality is higher for younger and older individuals and lowest when individuals are at their optimal fitness could be defined by using a double exponential selectivity (see Section 5.10)

```
@selectivity age_specific_M
type double_exponential
```

```
x0 7.06524
x1 1
x2 17
y0 0.182154
y1 1.43768
y2 1.57169
alpha 1.0

@process      NaturalMortalityByAge
type          mortality_constant_rate
categories    male female
relative_m_by_age age_specific_M age_specific_M
m             1.0 1.0
```

In this definition `m` is set to 1.0 and the rate is described through the selectivity. Otherwise, $M_{age} = S_{age} * m$. This concept can be constructed similarly for other mortality methods such as `instantaneous_mortality`.

Event and biomass-event mortality The event mortality and biomass-event mortality processes are applied in a similar manner, except that they remove a specified abundance (number of individuals) or biomass, respectively. These mortality processes can be used to define mortality events where the numbers of removals are known, e.g., fishing, rather than applying mortality as a rate.

In these cases, the abundance or biomass removed is also constrained by a maximum exploitation rate. Casal2 removes as many individuals or as much biomass as possible, while not exceeding the maximum exploitation rate.

Event mortality processes require a penalty to avoid estimating parameter values that will not allow the defined number of individuals to be removed. The model penalises those parameter estimates that result in an too low a number of individuals in the defined categories (after applying selectivities) to allow for removals at the maximum exploitation rate, with a similar penalty for biomass. See Section 6.8 for more information on how to specify penalties.

The event mortality applied to user-defined categories i, with the numbers removed at age j determined by a selectivity-at-age S_j:

First, calculate the vulnerable abundance for each category j in $1 \ldots J$ for ages $a = 1 \ldots A$ that are subject to event mortality

$$V_{a,j} = S_{a,j} N_{a,j} \tag{5.12}$$

and define the total vulnerable abundance V_{total} as

$$V_{total} = \sum_{j} \sum_{a} V_{a,j} \tag{5.13}$$

The exploitation rate to apply is

$$U = \begin{cases} C/V_{total}, & \text{if } C/V_{total} \leq U_{max} \\ U_{max}, & \text{otherwise} \end{cases} \tag{5.14}$$

The number removed $R_{a,j}$ from each age a in category j is,

$$R_{a,j} = U V_{a,j} \tag{5.15}$$

For example, to specify an **abundance-based** fishing mortality process with catches given for a set of specific years over categories "immature" and "mature", with selectivity "FishingSel", and assuming a maximum possible exploitation rate of 0.7, the syntax is

```
@process     Fishing
type          event_mortality
categories    immature mature
years         2000 2001 2002 2003
U_max         0.70
selectivities FishingSel FishingSel
penalty       event_mortality_penalty
```

and specified similarly for a **biomass-based** fishing mortality process

```
@process      Fishing
type          mortality_event_biomass
categories    immature mature
years         2000 2001 2002 2003
U_max         0.70
selectivities FishingSel FishingSel
penalty      event_mortality_penalty
```

Instantaneous mortality The instantaneous mortality process combines both natural mortality and event biomass mortality into a single process. This allows the simultaneous application of both natural mortality and anthropogenic mortality to occur across multiple time steps. This process applies half the natural mortality in each time step, then the mortalities from all the concurrent removals instantaneously, then the remaining half of the natural mortality. In fisheries models this is the most commonly used mortality process

This process allows for multiple removal events, e.g., a fisheries model with multiple fisheries and/or fleets. A removal method can occur in one time step only, although multiple removals can be defined to cover events during the year.

The equations for instantaneous mortality:

- An exploitation rate (actually a proportion) is calculated for each fishery, as the catch divided by the selected-and-retained biomass,

$$U_f = \frac{C_f}{\sum_a \bar{w}_a S_{f,a} n_a exp(-0.5tM_a)}$$

- The mortality pressure associated with method f is defined as the maximum proportion of fish taken from any element of the partition in the area affected by the method f

$$U_{f,obs} = max_a(\sum_k S_{k,a} U_k)$$

  where the maximum is over all partition elements affected by fishery f, and the summation is over all methods k which affect the jth partition element in the same time step as fishery f.

  In most cases the mortality pressure will be equal to the exploitation rate (i.e., $U_{f,obs} = U_f$), but can be different if: (a) there is another removal method operating in the same time step as removal method f and affecting some of the same partition elements, and/or (b) the selectivity $S_{f,a}$ does not have a maximum value of 1.

  There is a maximum mortality pressure limit of $U_{f,max}$ for each method of removal f. So, no more than proportion $U_{f,max}$ can be taken from any element of the partition affected by removal method f in that time step. Clearly, $0 \leq U_{max} \leq 1$. It is an error if two removal methods, which affect the same partition elements in the same time step, do not have the same U_max.

  For each f, if $U_{f,obs} > U_{f,max}$, then U_f is multiplied by $U_{f,max}/U_{f,obs}$ and the mortality pressures are recalculated. In this case the catch actually taken from the population in the model will differ from the specified catch, C_f.

- The partition is updated using

$$n'_a = n_a exp(-tM_a)\left[1 - \sum_f S_{f,a}U_f\right]$$

For example, to apply natural mortality of 0.20 across three time steps on both male and female categories, with two methods of removals (fisheries `FishingWest` and `FishingEast`) and their respective catches (kg) known for years 1975:1977 (the catches are given in the `catches` table and information on selectivities, penalties, and maximum exploitation rates are given in the `method` table), the syntax is

```
@process instant_mort
type mortality_instantaneous
m 0.20
time_step_proportions 0.42 0.25 0.33
relative_m_by_age One
categories male female
units kgs

table catches
year FishingWest FishingEast
1975 80000 111000
1976 152000 336000
1977 74000 1214000
end table

table method
method       category  selectivity u_max   time_step penalty
FishingWest   stock     westFSel    0.7     step1     CatchPenalty
FishingEast   stock     eastFSel    0.7     step1     CatchPenalty
end_table
```

and for referencing catch parameters for use in projecting, time-varying, and estimating, the syntax is

```
parameter process[mortality_instantaneous].method_"method_label"{2018}
```

where `"method_label"` is the label from the `catch` or `method` table and continuing the example,

```
parameter process[instant_mort].method_FishingWest{2018}
```

To calculate weight by empirical weight-at-age matrices as described in Section 5.7, the method table would include an additional column to reference weight-at-age objects:

```
@age_weight jan_weight_at_age
type data
table data
year 1  2  3  4
1980 3.4 5.6 7.23  8.123
end_table

table method
method       category  selectivity  u_max  time_step  penalty       age_weight
FishingWest  stock     westFSel     0.7    step1      CatchPenalty  jan_weight_at_age
FishingEast  stock     eastFSel     0.7    step1      CatchPenalty  jan_weight_at_age
end_table
```

Instantaneous mortality with retained catch and discards The instantaneous mortality retained process builds on the instantaneous mortality process (5.3.3) which has simultaneous applications of fishing and natural mortality, but with all catch-at-sea being landed, i.e., no discarding. The process `mortality_instantaneous_retained` allows for retained catch, discards, and also a mortality to be applied to discards, i.e., some are allowed to survive. The method for taking catch from the partition and the constraints used are the same as in `mortality_instantaneous`.

This process was implemented to address issues with the pot fishery for blue cod which has a minimum legal size and so some catch is discarded at sea and some of these discards are expected to survive (based on some experimental work). There are length data taken at sea, so the total catch selectivity can be estimated, and length and age data taken from the landed catch (retained), so the retention selectivity can also be estimated.

In this mortality process, discard mortality is specified by defining a selectivity to represent mortality by age or length (e.g., constant or asymptotic descending logistic). This discard selectivity is not be estimated since there is no observation class associated with it. If discard mortality is not provided, it is assumed that all discards die. Landed catch, and both the retained and total catch selectivities must be specified.

Extending the example shown in instantaneous mortality process (5.3.3) to use retained weight instead of catch, the commands are:

```
@process FishingRetainedCatch
type mortality_instantaneous_retained
# natural mortality
m 0.20
# the ratio of natural mortality in each of the three time steps
time_step_proportions 0.42 0.25 0.33
relative_m_by_age One
#for natural mortality by age
categories male female
units kgs

table catches
# two fisheries, West and East
year FishingWest FishingEast
# the catches are now landed catch
1975 80000 111000
1976 152000 336000
1977 74000 1214000
end table

table method
# all discards die
method   category selectivity retained_selectivity u_max time_step      penalty
FishingWest stock    westFSel      westRetainedSel   0.7     step1 CatchPenalty
FishingEast stock    eastFSel      eastRetainedSel   0.7     step1 CatchPenalty
end_table
```

If discard mortality is less than 1.0, use:

```
table method
# 50% discard mortality
method   category selectivity retained_selectivity discard_mortality u_max time_step penalty
FishingWest stock  westFSel    westRetainedSel         DisMort        0.7 step1 CatchPenalty
FishingEast stock  eastFSel    eastRetainedSel         DisMort        0.7 step1 CatchPenalty
end_table

@selectivity DisMort
```

```
Type constant
# 50% mortality of discards
c 0.5
```

See the instantaneous mortality process (5.3.3) for referencing catch parameters and calculating weight using empirical weight-at-age matrices.

The report outputs total catch, actual landed catch, and discards, without and with discard mortality:

```
@report Mortality
type process
process Instantaneous_Mortality_Retained
```

In the following, fisheries are indexed by f, and a indexes both age and category combinations.

The total catch is found by applying a selectivity, $S_{f,a}$, in the same way as in the instantaneous mortality process. Retention, $R_{f,a}$, is defined by specifying a selectivity, which can be a function of length or age. The retained catch is the product of these two values, $R_{f,a} * S_{f,a}$. If sex is in the partition, then there are potentially two retention curves, one for each sex.

In general, there is a retention curve for each category in the partition. This property does not apply to surveys. Discard mortality is also specified as a selectivity, $D_{f,a}$. The fraction of dead fish from fishing activity is $S_{f,a} * [R_{f,a} + (1.0 - R_{f,a}) * D_{f,a}]$. If $D_{f,a}$ is 1.0, then all selected fish are dead, and if it is 0.0, then only the retained fish are dead.

The equations for the `mortality_instantaneous_retained` process:

- Total catch (catch-on-board), C_f, is calculated by (retained catch) * VF / VR, where VF is vulnerable retained biomass, j indexes categories and t is the proportion of M in the time step, and VF is the full vulnerable biomass, $VF = \sum_{a,j} \overline{w}_a S_{a,j} n_{a,j} \exp(-0.5 t M_{a,j})$.
- An exploitation rate (actually a proportion) is calculated for each fishery, as the total catch (retained + discards) divided by the selected biomass (VF above) using selectivity $S_{f,a}$,

$$U_f = \frac{C_f}{\sum_a \bar{w}_a S_{f,a} n_a \exp(-0.5 t M_a)}$$

- The mortality pressure associated with method f is defined as the maximum proportion of fish taken from any element of the partition in the area affected by the method f,

$$U_{f,obs} = max_a(\sum_k S_{k,a} U_k)$$

  where the maximum is over all partition elements affected by fishery f, and the summation is over all methods k which affect the jth partition element in the same time step as fishery f.

  In most cases the mortality pressure will be equal to the exploitation rate (i.e., $U_{f,obs} = U_f$), but can be different if: (a) there is another removal method operating in the same time step as removal method f and affecting some of the same partition elements, and/or (b) the selectivity $S_{f,a}$ does not have a maximum value of 1.

  There is a maximum mortality pressure limit of $U_{f,max}$ for each method of removal f. So, no more than proportion $U_{f,max}$ can be taken from any element of the partition affected by removal method f in that time step. Clearly, $0 \leq U_{max} \leq 1$. It is an error if two removal methods, which affect the same partition elements in the same time step, do not have the same U_max.

  For each f, if $U_{f,obs} > U_{f,max}$, then U_f is multiplied by $U_{f,max}/U_{f,obs}$ and the mortality pressures are recalculated. In this case the catch actually taken from the population in the model will differ from the specified catch, C_f.
- Discard numbers-at-age (including their share of natural mortality) is $S_{a,j}(1 - R_{a,j}) n_{a,j} \exp(-0.5 t M_{a,j})$, and those that die at the end of the time step (updating the partition) are $D_{a,j} S_{a,j} (1 - R_{a,j}) n_{a,j} \exp(-t M_{a,j})$, where $D_{f,a}$ is the fraction that die on return to the sea.
- The partition is updated by removing landed catch, natural mortality, and discard mortality

$$n'_a = n_a \exp(-t M_a) \left[1 - \sum_f S_{f,a} U_f (R_{f,a} + D_{f,a}(1 - R_{f,a}))\right]$$

Holling mortality rate The density-dependent Holling mortality process applies the Holling Type II or Type III functions (Holling, 1959), and is generalised by the Michaelis-Menten equation (Michaelis and Menten, 1913).

This mortality process removes a number or biomass from a set of categories according to the total (selected) abundance (or biomass) and some "predator" abundance (or biomass), and is constrained by a maximum exploitation rate.

The mortality applied to user-defined categories k, with the numbers removed at age l, determined by a selectivity-at-age S_l is applied as follows:

First, calculate the total predator abundance (or biomass) over all predator categories k in $1 \ldots K$ and ages $l = 1 \ldots L$ that are applying the mortality

$$P_{k,l} = S_l^{predator} N_{k,l}^{predator} \tag{5.16}$$

And define the total predator abundance (or biomass) P_{total} as

$$P_{total} = \sum_K \sum_L P_{k,l} \tag{5.17}$$

Then calculate the total vulnerable abundance (or biomass) over all prey categories k in $1 \ldots K$ and ages $l = 1 \ldots L$ that are subject to the mortality

$$V_{k,l} = S_l^{prey} N_{k,l}^{prey} \tag{5.18}$$

Then define the total vulnerable abundance (or biomass) V_{total} as

$$V_{total} = \sum_K \sum_L V_{k,l} \tag{5.19}$$

The number to remove is then determined by

$$R_{total} = P_{total} \frac{a V_{total}^{x-1}}{b + V_{total}^{x-1}} \tag{5.20}$$

where $x = 2$ for the Holling type II function, $x = 3$ for the Holling type III function, or a different value of $x \geq 1$ for the generalised Michaelis-Menten function; $a > 0$ and $b > 0$ are the Holling function parameters.

The exploitation rate to apply is

$$U = \begin{cases} R_{total}/V_{total}, & \text{if } R_{total}/V_{total} \leq U_{max} \\ U_{max}, & \text{otherwise} \end{cases} \tag{5.21}$$

And the number removed R from each age l in category k is

$$R_{k,l} = U V_{k,l} \tag{5.22}$$

The density-dependent Holling mortality process is applied either as a function of biomass or abundance, depending on the value of the `is_abundance` switch.

For example, a biomass Holling type II mortality process on prey `prey` by predator `predator` has the syntax

```
@process HollingMortality
type Holling_mortality_rate
is_abundance F
a 0.08
b 10000
x 2
categories prey
selectivities One
predator_categories predator
predator_selectivities One
u_max 0.8
```

Initialisation-event mortality Initialisation event mortality is a process that can occur only in the initialisation phase. It applies abundance or biomass mortality events specifically in initialisation phases. This option can be useful if the population is not in equilibrium before model start.

This process applies a single catch value for all iterations within the initialisation phase, and mortality will not be applied outside of the initialisation phase. This process should not be embedded in the annual cycle.

This process should be used in conjunction with the `insert_processes` command in the `@initialisation_phase` block.

Example syntax where the `initialisation_mortality_event` has been specified in the initialisation phase `Predation_state` but not in the annual cycle:

```
initialisation_phases Equilibrium_state Predation_state
time_steps Oct_Nov Dec_Mar

@initialisation_phase Equilibrium_state
type derived

@initialisation_phase Predation_state
type iterative
insert_processes Oct_Nov()=predation_Initialisation

@process predation_Initialisation
type initialisation_mortality_event
categories male.HOKI female.HOKI
catch 90000
selectivities Hakesl Hakesl

time_step Oct_Nov
processes Mg1 Instantaneous_Mortality

@time_step Dec_Mar
processes Recruitment Instantaneous_Mortality
```

Prey-suitability mortality The density-dependent prey-suitability mortality process applies predation mortality from a predator group to its prey groups simultaneously. It removes an abundance (or biomass) from each prey group according to the total (selected) abundance (or biomass) of each prey group, the total (selected) abundance (or biomass) of the other prey groups, some "predator" abundance (or biomass), and the preference (electivity) of the predator for each prey group, constrained by a maximum exploitation rate. The predator-prey suitability functions were based on the multispecies Virtual Population Analysis (MSVPA) functions (Jurado-Molina et al., 2005).

The mortality applied to the user-defined prey group g of category k, with the numbers removed at age l determined by a selectivity-at-age S_l is applied as follows:

First, calculate the total predator abundance (or biomass) over all predator categories k in $1 \ldots K$ and ages $l = 1 \ldots L$ that are applying the mortality

$$P_{k,l} = S_l^{predator} N_{k,l}^{predator} \tag{5.23}$$

And define the total predator abundance (or biomass) P_{total} as

$$P_{total} = \sum_K \sum_L P_{k,l} \tag{5.24}$$

Then, given the total vulnerable abundance (or biomass) of prey group g over all categories k in $1 \ldots K$ and ages $l = 1 \ldots L$ that are subject to the mortality

$$V_{g,k,l} = S_l^{prey} N_{k,l}^{prey} \tag{5.25}$$

And define the total vulnerable abundance (or biomass) of each prey group V_{total}^g as

$$V_{total}^g = \sum_K \sum_L V_{g,k,l} \tag{5.26}$$

And the total availability A_{total}^g for each prey group as

$$A_{total}^g = \frac{V_{total}^g}{\sum_G V_{total}^g} \tag{5.27}$$

The vulnerable abundance (or biomass) and availability every prey group g in $1 \ldots G$ is calculated simultaneously. Then the abundance (or biomass) to remove from each prey group g is a function of its electivity E_g, the availability of all other prey groups i in $1 \ldots G$, the electivity of the predator for each prey group E_i, and the total consumption rate of the predator CR and its abundance (or biomass) P_{total}

$$R_{total}^g = P_{total} CR \frac{A_{total}^g E_g}{\sum_G A_{total}^i E_i} \tag{5.28}$$

The exploitation rate to apply to each prey group g is then

$$U_g = \begin{cases} R_{total}^g / V_{total}^g, & \text{if } R_{total}^g / V_{total}^g \leq U_{max} \\ U_{max}, & \text{otherwise} \end{cases} \tag{5.29}$$

And the number removed R^g in each prey group g from each age l in category k is

$$R_{g,k,l} = U_g V_{g,k,l} \tag{5.30}$$

Prey suitability choice occurs only between the prey groups specified by the process. The total predator consumption rate represents the consumption of the predator on those prey groups alone. The electivities must sum to 1. Further, the consumption rate can be modified by a layer to be cell specific.

The density-dependent prey-suitability process is applied as either a biomass or an abundance depending on the value of the `is_abundance` switch.

Individual categories can be aggregated into prey groups using the "+" symbol. To indicate that two (or more) categories are to be aggregated, separate them with a "+" symbol.

For example, to specify two prey groups of two species made up of the males and females in each prey group

```
prey_categories maleSpeciesA + femaleSpeciesA maleSpeciesB + femaleSpeciesB
```

This syntax indicates that there are two prey groups, `maleSpeciesA + femaleSpeciesA` and `maleSpeciesB + femaleSpeciesB`, with each group having its own electivity.

For example, a biomass prey-suitability mortality process with an overall consumption rate of 0.8 of prey `species A` and `species B` (modelled as males and females) by the predator `predatorSpecies` with electivities between `species A` and `species B` of 0.18 and 0.82 has syntax

```
@process PreySuitabilityMortality
type prey-suitability_predation
is_abundance F
consumption_rate 0.8
categories maleSpeciesA + femaleSpeciesA maleSpeciesB + femaleSpeciesB
electivities 0.18 0.82
selectivities One One One One
predator_categories predatorSpecies
predator_selectivities One
u_max 0.8
```

5.3.4 Transition By Category

The transition by category process moves individuals between categories. This process is used to specify transitions such as maturation (individuals move from an immature to mature state) and migration (individuals move from one area to another).

There is a one-to-one relationship between the "from" category and the "to" category, i.e., for every source category there is one target category only

$$N_{a,j} = N_{a,i} \times P_i \times S_{a,i} \tag{5.31}$$

where $N_{a,j}$ is the number of individuals that have moved to category j from category i in age a, $N_{a,i}$ is the number of individuals in category i, P_i is the proportion parameter for category i, and $S_{a,i}$ is the selectivity at age a for category i.

To merge categories repeat the "to" category multiple times.

For example, to specify a simple spawning migration of mature males from a western area to an eastern (spawning) area, the syntax is

```
@process Spawning_migration
type transition_category
from West.males
to East.males
selectivities MatureSel
proportions 1
```

where `MatureSel` is a selectivity that describes the proportion of age or length classes that are mature and thus move to the eastern area.

Transition by category by age A special process type is the transition by category by age process, which allows a transition to occur for a specific subset of ages in specific years only, where each year can have a different number that are moved between categories.

5.3.5 Tag Release events

Tagging processes can be age- or length-based processes, whereby numbers of individuals are moved from an untagged category to a tagged category defined in the `@categories` block. Tag release processes can also account for initial tag-induced mortality on individuals.

Age-based tag release events move a known number of individuals tagged for each age to a tagged category, along with applying additional mortality. Individuals are removed from the non-tagged categories and added to tagged categories. Often the ages of tagged individuals are not known, so length-based tag release events are more commonly used.

Length-based tag release processes are more complicated, as the age-length matrix is calculated and the exploitation for each length bin to then move the correct numbers-at-age based on the known lengths of release. Casal2 also allows for initial tag loss.

The tag-release process:

For each length bin l of the input vector of numbers-at-length $\tilde{N}_l$

$$N_{l,j} = \sum_{a=1} N_{a,l,j} * S_a$$

where $N_{a,l,j}$ is the numbers at age a and length l for category j, and S_a is the selectivity at age a.

Calculate the total numbers-at-length T_l across all source categories at length l, taking into account the selectivities

$$T_l = \sum_{j=1} N_{l,j}$$

Calculate the transition rate for length bin u_l

$$u_l = \tilde{N}_l / T_l$$

Check that the threshold u_{max} is not exceeded, which is analogous to the u_{max} in a mortality processes

$$u_l = \begin{cases} u_{max}, & \text{if } u_l > u_{max} \textbf{ flag a penalty} \\ u_l, & \text{otherwise} \end{cases}$$

Calculate the numbers-at-age in this category that will be moved by multiplying across the age-length matrix and storing the result by age, for each age accumulated across all length bins. Then move the necessary

$$N_{a,j} += N_{a,l} * u_l$$

The syntax for an example of tag release by length process

```
@process 2005Tags_shelf
type tag_by_length
years 2005
from male.untagged+female.untagged
to male.2005  female.2005
selectivities ShelfselMale ShelfselFemale
penalty tagging_penalty
```

```
initial_mortality 0.1
table proportions
year 30 40 50 60 70 80 90 100 110 120 130 140 150 160 170 180 190 200 210 220
2005  0 0 0.0580 0.1546 0.3380 0.1981 0.1643 0.0531 0.0242 0.0097 0 0 0 0 0 0 0 0 0 0
end_table
n 207
U_max 0.999
```

This process moves 207 individuals from a combination of male.untagged and female.untagged categories, based on the combination of growth rates and selectivity, into tagged male and tagged female categories.

5.3.6 Tag loss

Tag Loss is the process which accounts for tags being lost from a tagged individual due to, for example, tag failure or tags getting knocked off. This process is applied as an instantaneous migration rate that can happen over multiple time steps in the annual cycle. This method assumes that when tags are lost the individuals are transferred from the `from` category to the `to` category.

The tag loss rate is applied depending on whether the individuals were tagged with a single tag only (`tag_number_per_animal = 1`), double tagged (`tag_number_per_animal = 2`), or tagged with n tags (`tag_number_per_animal = n`).

The syntax for the tag loss is

```
@process Tag_loss
type tag_loss
categories tagged_fish
tag_loss_rate 0.02
time_step_proportions 0.25 0.75
selectivities One
tag_loss_type single
year 1985
```

5.4 Derived quantities

Some processes require a population value derived from the population state as an argument. These values are `derived quantities`. Derived quantities are values calculated in a specified time step in every year, and thus have a single value for each year of the model. The time within the time-step is at the end unless otherwise specified (using *proportion_mortality*-like subcommand.

Derived quantities can be calculated as either abundance or biomass. Abundance-derived quantities are the sum over the specified categories (after applying a selectivity). Biomass-derived quantities are calculated similarly.

Derived quantities are also calculated during the initialisation phases. Therefore, the time step during each initialisation phase must be specified. If the initialisation time steps are not specified, the derived quantity will be calculated during the initialisation phases.

A common use of an derived quantities is as input into a stock-recruit relationship which requires an equilibrium biomass (B_0) and annual spawning stock biomass values (SSB_y) to calculate recruitment into the first age class. SSB_y is an derived quantity based on the mature biomass, usually at spawning time.

Derived quantities can be associated with a *time evaluation interval*; see section 5.3.3 for more detail on mortality blocks. In this case, the point of calculation can be set to any point within the mortality block, e.g., when 75 % of the deaths from natural mortality plus catch has occurred, which is based on interpolating between the start and end of the block as the partition is known at those points. Two methods are available: `weighted_sum` and `weighted_product`, and are defined as

- `weighted_sum`: after proportion p through the mortality block, the partition elements are given by $n_{p,j} = (1-p)n_j + p'_j$

- `weighted_product`: after proportion p through the mortality block, the partition elements are given by $n_{p,j} = n_j^{1-p} n_j'^{p}$

where $n_{p,j}$ is the derived quantity at proportion p of the mortality block for category j, n_j is the quantity at the beginning of the mortality block, and n'_j is the quantity at the end of the mortality block.

For example, to define a biomass-derived quantity spawning stock biomass, *SSB*, calculated at the end of the first time step (labelled `step_one`), over all "mature" male and female categories and halfway through the mortality block using the `weighted_sum` method, the syntax is

```
@derived_quantity SSB
type          biomass
time_step     step_one
categories    mature.male mature.female
selectivities One
time_step_proportion        0.5
time_step_proportion_method weighted_sum
```

5.5 Age-length relationship

The age-length relationship defines the functional form of the length-at-age (and the weight-at-length; see Section 5.6) of individuals at age/category within the model.

There are four length-age relationship options. The first is the naive "no relationship", where each individual has length 1 regardless of age. The others are: von Bertalanffy relationship, the Schnute relationship, and "data" (mean length-at-age for each model year).

The length-at-age relationship is used to calculate the length frequency given age, and with the length-weight relationship, the weight-at-age of individuals within an age/category. When defining length-at-age, the length-weight relationship must also be defined (see Section 5.6).

Changes in length-at-age during the year, i.e., growth between birthdays, are represented by incrementing age as specified by the `time_step_proportions` parameter.

5.5.1 The 'none' relationship

The length of each individual is 1 for all ages, and the `none` length-weight relationship must also be used.

5.5.2 The von Bertalanffy relationship

$$\bar{s}(age) = L_\infty \left(1 - \exp\left(-k\left(age - t_0\right)\right)\right) \tag{5.32}$$

5.5.3 The Schnute relationship

$$\bar{s}(age) = \begin{cases} \left[y_1^b + \left(y_2^b - y_1^b\right)\dfrac{1-\exp\left(-a(age-\tau_1)\right)}{1-\exp\left(-a(\tau_2-\tau_1)\right)}\right]^{1/b}, & \text{if } a \neq 0 \text{ and } b \neq 0 \\ y_1 \exp\left[\ln\left(y_2/y_1\right)\dfrac{1-\exp\left(-a(age-\tau_1)\right)}{1-\exp\left(-a(\tau_2-\tau_1)\right)}\right], & \text{if } a \neq 0 \text{ and } b = 0 \\ \left[y_1^b + \left(y_2^b - y_1^b\right)\dfrac{age-\tau_1}{\tau_2-\tau_1}\right]^{1/b}, & \text{if } a = 0 \text{ and } b \neq 0 \\ y_1 \exp\left[\ln\left(y_2/y_1\right)\dfrac{age-\tau_1}{\tau_2-\tau_1}\right], & \text{if } a = 0 \text{ and } b = 0 \end{cases} \tag{5.33}$$

The von Bertalanffy relationship has parameters L_∞, k, and t_0. The Schnute relationship (Schnute, 1981) has parameters y_1 and y_2, which are the mean lengths at reference ages τ_1 and τ_2, and a and b; when $b = 1$, this relationship reduces to the von Bertalanffy relationship with $k = a$.

5.5.4 Data: matrix of size at age relationship

There is an option to input empirical length at age by year, which is an alternative to using an age-length growth model such as the von Bertalanffy and Schnute model. Casal2 will interpolate values for missing years across time steps. The calculations of length-at-age throughout the model years occur in the same time step.

```
@age_length   male_AL
type          data
time_step_proportions 0.0 0.0   #use age at start of time-step
length_weight wgt_male          # needed to convert numbers-at-age into catch
distribution  normal            # distribution of lengths around the mean length
cv_first      0.1               # cv of the distribution at the first age
cv_last       0.1               # cv of the distribution at the maximum age
time_step_measurements_were_made step2
internal_gaps mean
external_gaps mean
table data # first line has column labels for year and then all the model ages
year     2     3     4     5     6     7     8      9    10    11    12
1980 30.13 34.90 38.43 40.61 42.45 43.02 43.94 43.63 43.36 43.70 43.84
1981 30.33 34.78 38.03 40.15 42.22 42.89 44.21 44.07 43.99 44.32 44.64
end_table
```

When the values for *cv_last* and *cv_first* are different, the cv used for intermediate ages is, by default, interpolate by that age's mean length. There is a legacy switch for testing the conversion of models from CASAL into Casal2, i.e., use the subcommand, *by_length false* which allows the interpolation to be by age, the default setting for CASAL. CASAL also fixes to by-age interpretation when doing calculating the mean weight (see 5.6.2).

5.6 Length-weight relationship

There are two length-weight relationships options. The first is the naive "no relationship" relationship, where the weight of an individual is always 1, regardless of length. The second relationship is the "basic" relationship, which is the standard length-weight relationship, $W = aL^b$.

5.6.1 The 'none' relationship

$$\text{mean weight} = 1 \tag{5.34}$$

5.6.2 Basic: the standard length-weight relationship

The mean weight $\hat{w}_a$ of an individual of age a is

$$\hat{w}_a = a\hat{l}_a^b \tag{5.35}$$

where $\hat{l}_a$ is the mean length at age a. If a distribution of length-at-age is specified, then the mean weight is calculated over the distribution of lengths

$$\hat{w}_a = (a\hat{l}_a^b)(1+cv^2)^{\frac{b(b-1)}{2}} \tag{5.36}$$

where the cv is the coefficient of variation (CV) of the length-at-age relationship. This adjustment is exact for lognormal distributions, and an approximation for normal distributions if the CV is not large (Bull et al., 2012).

For comparing CASAL with Casal2 results, there is a small difference between the two programs. CASAL adjusted the CVs `by_length` only when CVs are used in distribution calculations (length-based selectivities, length-based processes, and length-based observations), and is not done in the above correction.

Note: the scale of *a* can be specified incorrectly. If the catch is in tonnes and the growth curve is in centimetres, then *a* should convert a length in centimetres to a weight in tonnes. There are reports available that can be used to help check that the units specified are plausible (see Section 8).

```
@length_weight length_weight
type basic
units tonnes
a 0.00000123
b 3.132
```

5.7 Age-weight relationship

Either 'none' or an Empirical weight-at-age matrix. The empirical weight-at-age data can be input. This option is different from the method above as it uses empirical data for weight-at-age, rather than calculating it with the growth functions (age -¿ length -¿ weight). This bypasses the growth machinery which is expected to be present and so using weight-at-age data needs to be declared in blocks that use this method, i.e., biomass observation blocks, fishery mortality blocks, and biomass derived quantities e.g., SSB. The subcommand to use is "`age_weight_label` ageWeight.block.label" within the block, but in mortality fisheries blocks, `age_weight_label` is a column in the *table method* part with the corresponding *ageWeight.block.label* in the body of the table. More than one *@age_weight* blocks can be used, and both weight-at-age data and the usual growth version can be used in the same model (but clearly not in the same block).

This option specifies the weight-at-age values for categories at a point in time.

An example

```
@age_weight age_weight
type Data
units tonnes
table data   #year then ages; 1st row is the column labels
year 1 2 3 4 5 6 7 8 9 10
1986 0.134 0.686 1.639 2.719 3.649 4.901 6.329 6.591 7.238 7.491
1987 0.132 0.724 1.534 2.829 4.092 4.853 5.705 6.143 7.179 8.089
1988 0.122 0.641 1.533 2.641 3.796 5.054 5.652 6.356 6.95 8.857
1989 0.137 0.722 1.606 2.416 3.629 5.027 5.561 6.35 6.933 7.217
1990 0.138 0.773 1.645 2.74 3.711 4.506 5.684 6.929 7.424 7.479
end_table
```

If weight is defined by the empirical weight-at-age data, then the age-length block in the `@categories` block can be omitted.

```
@categories
format stock
names Stock
```

5.8 Weightless model

To model abundance (i.e., to model the population in numbers and not convert to biomass), the `@length_weight` argument is turned off by specifying the keyword `none` in the `@age_length` block

```
@age_length age_size
type schnute
...
length_weight none
```

In this case any "biomass" generated by Casal2 will actually be abundance, and care should be taken with interpretation of the output.

5.9 Maturity, in models without maturing in the partition

When maturity is not a factor in the partition, processes may still depend on maturity. You must then make the assumption that the proportion of mature fish in each element of the partition remains constant over time. A selectivity is used to define the proportion of mature fish in each age class and these can depend on categories (a length selectivity could be used).

This selectivity is specified in the block that requires mature fish, the most common one is for SSB as a derived quantity.

5.10 Selectivities

Selectivity is a term used in Casal2 to mean an ogive that is a function of age. They can be used to specify the selection curve for a fishery or observation (Section 6) or to modify the effects of processes on each age class, e.g., migration rates by age (Section 5). The curves can use length rather than age, in which case they operate on the length distribution for each age (use the subcommand "*by_length true*", *false* is the default). Do not expect too much from length selectivities because in the next time-step or year, the length distribution for each age reverts to being as defined in the *age_length* blocks, e.g., normal, rather than being partially truncated because, e.g., larger fish in an age class have been preferentially caught.

There are a number of different parametric forms as options, including logistic and double normal curves. Selectivities are defined in command block `@selectivity <label>`, where the unique label of the selectivity is used by observations and processes to identify which selectivity to apply.

For example, a logistic selectivity can be defined by:

```
@selectivity trawlSel    #label for the trawl fishery selectivity
type      logistic       # type of curve
a50       4.4            # age at 50% selection
ato95     1.5            # interval (yr) from a50 to the age at 95% selection
                         #  age at 95% selectivity is 5.9 yr; at 5%, 2.9 yr

#at_length true          #if used, then a50 & ato95 refer to length
```

For some selectivities, the function values for some choices of parameters can result in numeric overflow or underflow errors (i.e., the number calculated from parameter values is either too large or too small to be well represented). Casal2 implements range checks on some parameters to test for these errors before calculating function values.

For example, the logistic selectivity is implemented such that if $(a_{50} - x)/a_{to95} > 5$ then the value of the selectivity at $x = 0$, i.e., for $a_{50} = 5$, $a_{to95} = 0.1$, then the value of the selectivity at $x = 1$, without range checking would be 7.1×10^{-52}. With range checking, that value is 0 (as $(a_{50} - x)/a_{to95} = 40 > 5$).

The selectivity options are:

- Constant
- Knife-edge
- All values
- All values bounded
- Increasing
- Logistic
- Inverse logistic (descending logistic?)
- Logistic producing
- Double normal

- Double exponential

See Figure 5.3 for plots of example selectivities (p. 57).

5.10.1 constant

$$f(x) = C \tag{5.37}$$

The constant selectivity has the estimable parameter C.

Input fragment:

```
type constant
c    0.5
```

5.10.2 knife_edge

$$f(x) = \begin{cases} 0, & \text{if } x < E \\ \alpha, & \text{if } x \geq E \end{cases} \tag{5.38}$$

The knife-edge ogive has the estimable parameter E and a non-estimable scaling parameter α, where the default value of $\alpha = 1$.

Input fragment:

```
type  knife_edge
e     8
alpha 0.5
```

5.10.3 all_values

$$f(x) = V_x \tag{5.39}$$

The all-values selectivity has estimable parameters V_{low}, $V_{low+1} \ldots V_{high}$. The selectivity value for each age class must be set.

5.10.4 all_values_bounded

$$f(x) = \begin{cases} 0, & \text{if } x < L \\ V_x, & \text{if } L \leq x \leq H \\ V_H, & \text{if } x > H \end{cases} \tag{5.40}$$

The all-values-bounded selectivity has non-estimable parameters L and H. The estimable parameters are V_L, $V_{L+1} \ldots V_H$. Selectivity values for each age class from $L \ldots H$ must be set.

Selectivities `all_values` and `all_values_bounded` can be included in additional priors using the syntax

```
@selectivity maturity
type all_values
v 0.001 0.1 0.2 0.3 0.4 0.3 0.2 0.1

## encourage ages 3-8 to be smooth.
@additional_prior smooth_maturity
type vector_smooth
parameter selectivity[maturity].values{3:8}
```

5.10.5 increasing

$$f(x) = \begin{cases} 0, & \text{if } x < L \\ f(x-1) + \pi_x(\alpha - f(x-1)), & \text{if } L \le x \le H \\ f(\alpha), & \text{if } x \ge H \end{cases} \tag{5.41}$$

The increasing ogive has non-estimable parameters L and H. The estimable parameters are π_L, $\pi_{L+1} \ldots \pi_H$; if these are estimated, they should always be constrained to be between 0 and 1. α is a scaling parameter, with default value of $\alpha = 1$. The increasing ogive is similar to the all-values-bounded ogive, and is constrained to be non-decreasing.

Input fragment:

```
type  increasing
l     3
h     7
v     0.2 0.3 0.4 0.5 0.6
```

5.10.6 logistic

$$f(x) = \alpha / [1 + 19^{(a_{50} - x)/a_{to95}}] \tag{5.42}$$

The logistic selectivity has estimable parameters a_{50} and a_{to95}. α is a scaling parameter (input files, *alpha*, with default value of $\alpha = 1$. The logistic selectivity takes values 0.5α at $x = a_{50}$ and 0.95α at $x = a_{50} + a_{to95}$.

5.10.7 inverse_logistic

$$f(x) = \alpha - \alpha / [1 + 19^{(a_{50} - x)/a_{to95}}] \tag{5.43}$$

The inverse logistic selectivity has estimable parameters a_{50} and a_{to95}. α is a scaling parameter (*alpha*, with default value of $\alpha = 1$. The logistic selectivity takes values 0.5α at $x = a_{50}$ and 0.95α at $x = a_{50} - a_{to95}$.

Input fragment:

```
type  inverse_logistic
a50   4
ato95 1
alpha 0.5   #default is 1.0
```

5.10.8 logistic_producing

$$f(x) = \begin{cases} 0, & \text{if } x < L \\ \lambda(L), & \text{if } x = L \\ (\lambda(x) - \lambda(x-1)) \,/\, (1 - \lambda(x-1)), & \text{if } L < x < H \\ 1, & \text{if } x \ge H \end{cases} \tag{5.44}$$

The logistic-producing selectivity has non-estimable parameters L and H. The estimable parameters are a_{50} and a_{to95}. α is a scaling parameter, with default value of $\alpha = 1$.

For category transitions, $f(x)$ represents the proportion moving, not the proportion that have moved. This selectivity was designed for use in an age-based model to model maturity. In such a model, a logistic-producing maturation selectivity will, in the absence of other influences, make the proportions mature follow a logistic curve with parameters a_{50} and a_{to95}.

Input fragment:

```
type  logistic_producing
l      2
h      8
a50    4
ato95  1
#alpha 1.0
```

5.10.9 double_normal

$$f(x) = \begin{cases} \alpha 2^{-[(x-\mu)/\sigma_L]^2}, & \text{if } x \le \mu \\ \alpha 2^{-[(x-\mu)/\sigma_R]^2}, & \text{if } x \ge \mu \end{cases} \tag{5.45}$$

The double-normal selectivity has estimable parameters a_1, s_L, and s_R. α is a scaling parameter, with default value of $\alpha = 1$. It has values α at $x = a_1$, and 0.5α at $x = a_1 - s_L$ and $x = a_1 + s_R$.

Input fragment:

```
type  double_normal
mu       6     #age at switch over from left to right normal curves
               #  = mean for both normal curves
sigma_1  1     # standard deviation for left normal
sigma_2  10    # standard deviation for right normal
#alpha 1.0
```

5.10.10 double_exponential

$$f(x) = \begin{cases} \alpha y_0 (y_1/y_0)^{(x-x_0)/(x_1-x_0)}, & \text{if } x \le x_0 \\ \alpha y_0 (y_2/y_0)^{(x-x_0)/(x_2-x_0)}, & \text{if } x > x_0 \end{cases} \tag{5.46}$$

The double-exponential selectivity has non-estimable parameters x_1 and x_2. The estimable parameters are x_0, y_0, y_1, and y_2. α is a scaling parameter, with default value of $\alpha = 1$. This selectivity curve can be "U-shaped". Bounds for x_0 must be such that $x_1 < x_0 < x_2$. With $\alpha = 1$, the selectivity passes through the points (x_1, y), (x_0, y_0), and (x_2, y_2). If both y_1 and y_2 are greater than y_0 the selectivity is "U-shaped" with minimum at (x_0, y_0).

Input fragment:

```
type  double_exponential
x0    15   # age at middle point
y0    0.1  # selection at x0; here a minimum --> U shape
x1    1    # left point
y1    0.5  #  selection at x1
x2    30   # right point
y2    0.8  # selection at x2
#alpha 1.0
```

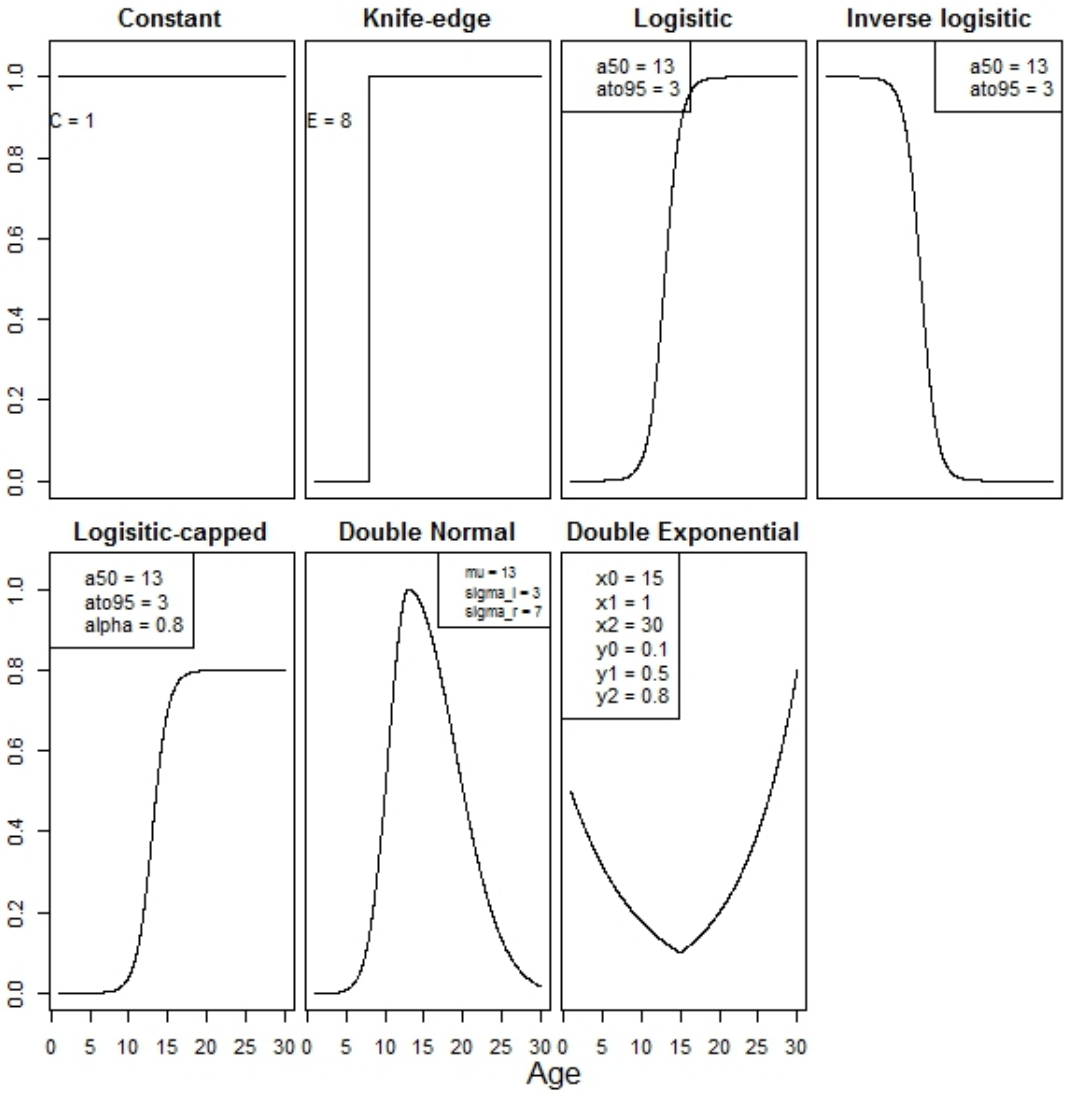

Figure 5.3: Examples of the selectivities

5.11 Time-varying Parameter

Any parameter can be varied annually for blocks of years or in specific years within the model run . For years that are not specified, the parameter will default to the input, or if in an iterative state such as estimation mode, the value being trialled at that iteration.

Method types for a time-varying parameter are:

- `constant`,
- `random_walk`,
- `exogenous`,
- `linear`,
- `annual_shift`, and
- `random_draw`.

This option allows for a parameter to be fixed in a year, or be the result of a deterministic or stochastic equation. **Note:** the stochastic time-varying functionality was added for simulation purposes. **It has not been**

tested in an estimation context.

To implement hierarchical models, the prior parameter values need to be estimated using hyperpriors. To implement a hierarchical model using the time-varying functionality, use MCMC estimation as a way to calculate the integral which is required to obtain unbiased estimates. In an MCMC context, a Gibbs sampler is assumed. That is, every draw is from a conditional distribution and so every draw is a candidate value.

When allowing removals with annually varying catchabilities, selectivities, and/or other model components, simulated observations more closely model real data and associated conclusions become more useful. Implementing time-varying parameters also allows for mean or location parameters of selectivities to change between years based on an explanatory variable. An example of this is in the New Zealand Hoki fishery where the μ and a_{50} parameters are allowed to shift depending on when the fishing season occurs. Descriptive analysis showed that when fishing was earlier relative to other years smaller fish were caught and vice versa. This can be shown in the Examples/2stock directory, implemented at line: `382` in the `population.csl2` file. [Craig to edit]

5.11.1 `constant`

This option allows a parameter to have an different value during specified years to the rest of the model run,and this value can be estimated. To allow survey catchability to be different in the year block 1975 to 1988 from the rest of the series we write:

```
@time_varying q_time_var
type          constant
parameter     catchability[survey_q].q
years         1975:1988
values        0.001      #same for all years
```

To estimate catchability for 1975 and 1976, use the following:

```
@estimate q_time_var
type uniform   #prior
parameter time_varying[q_time_var].values{1975:1976}
lower_bound 1e-6 1e-6
upper_bound 2     2
```

To make the catchability be same over the year block we need to estimate it for one year (say 1975) and use the *same* subcommand to make the others take the same value

```
@estimate q_time_var
type uniform
parameter time_varying[q_time_var].values{1975}
same      time_varying[q_time_var].values{1976:1988}
lower_bound 1e-6
upper_bound 2
```

Caution: do not estimate both the actual parameter and its time-varying counterpart, as the time-varying value will overwrite the actual parameter making the actual value unidentifiable. [Craig to edit]

5.11.2 `random_walk`

A random deviate drawn from a standard normal distribution is added to the previous year's value. This option has an estimable parameter σ_p for each time-varying parameter p. For reproducible modelling when using stochastic functionality, set the random seed (see Section 3.3).

```
@time_varying q_time_var
```

```
type          random_walk
parameter     catchability[survey_q].q
distribution  normal
mean          0
sigma         3
```

If the `parameter` specified in the `@time_varying` block is associated with an `@estimate` block, then the parameter is constrained to stay within the lower and upper bounds of the `@estimate` block.

WARNING: if the parameter does not have an associated `@estimate` block then there is no safeguard against the application of a random deviate resulting in parameter values which cause the model to fail, i.e., generates NA or INF values. To avoid this, specify an `@estimate` block even though the parameter is not actually being estimated; see the example syntax below.

A constraint whilst using this functionality is that a parameter cannot be less than 0.0. If it is then Casal2 sets it equal to 0.01.

```
@estimate survey_q_est
type      uniform
parameter catchability[survey_q].q
lower_bound 1e-6
upper_bound 10
```

This configuration will insure the random walk time-varying process will set the any new candidate values within the lower and upper bound of the `@estimate` block.

5.11.3 annual_shift

A parameter generated in year y (θ'_y) depends on the value specified by the user (θ_y) along with three coefficients a, b, and c

$$\bar{\theta}_y = \frac{\sum_y^Y \theta_y}{Y} \tag{5.47}$$

$$\theta'_y = a\bar{\theta}_y + b\bar{\theta}_y^2 + c\bar{\theta}_y^3 \tag{5.48}$$

5.11.4 exogenous

Parameters are shifted based on an exogenous variable. An example of this is an exploitation selectivity parameters that may vary between years based on known changes in exploitation behaviour such as season, start time, and average depth of exploitation.

$$\delta_y = a(E_y - \bar{E}) \tag{5.49}$$

$$\theta'_y = \theta_y + \delta_y \tag{5.50}$$

where δ_y is the shift or deviation in parameter θ_y in year y to generate the new parameter value in year y (θ'_y). a is an estimable shift parameter, E is the exogenous variable, and E_y is the value of this variable in year y. For more information readers can see Francis et al. (2003).

5.12 Equation Parser

Casal2 has an equation parser, which is currently implemented in Projections (section 5.13), Derived quantities (see Section 5.4), and Reports (section 8).

Examples of syntax for implementing the equation parser are below. For more information on the parser, see https://github.com/nickgammon/parser/blob/master/parser.cpp

```
equation process[Recruitment].r0 * 2 #double the recruitment
```

mathematical functions such as `sqrt()`, `log()`, `exp()`, `cos()`, `sin()`, and `tan()` can be used

```
equation sqrt(process[Recruitment].r0)
```

exponents can be used with `pow()`

```
equation pow(2, 3)
```

the absolute value of an equation using `abs()`

```
equation abs(sqrt(process[Recruitment].r0) * 1.33)
```

`if-else` statements can be used

```
equation if(process[Recruitment].r0 > 23, 44, 55)
## if R0 is greater than 23 return 44 else return 55
```

`if-else` statements can also be linked, more complex syntax

```
# if R0 > 23 return 44
# else if R0 < 23 & r0 > 10 return 55
equation if(process[Recruitment].r0 > 23, 44,
         if(process[Recruitment].r0 > 10, 55, 66))
else R0 must be less than 10 return 66
```

Only single values can be referenced, so an equation cannot be applied to a vector, e.g., `process[Recruit].ycs_values{1974:1980}` cannot be referenced. More information on which parameters can be included in an equation parser is available (Section 14.1.3). Any subcommand that has a `type estimable` could be referenced with the equation parser.

Note: the equation parser will not catch all user configuration errors, such as checking whether a parameter that exists in the system has been populated when it is required.

For example, the wrong year could be misspecified in the case of removals in year y which is based on the state of the population in year $y-1$

```
parameter process[removals].catch
year 2015
equation derived_quantity[percent_b0].values{2020}
```

This example is a valid equation but it will have nonsensical results, since a value for 2020 is to be calculated using values for 2015. Although the equation parser adds flexibility, it is easy to misspecify equations.

5.13 Specifying projections

Given a set of estimated parameter values from a *-e* or a MCMC run, the model can be projected into the future. Projection years are after the model run years, and are defined in the *@model* command block using the `final_projection_year` subcommand, i.e., projection years are `final_year + 1` through to `final_projection_year`.

Parameter values for the projected years can be specified in a stochastic way or fixed at some value (the default is the estimated value if the parameter is not time-varying) and these are specified in the *@projection* block,

```
@project Future_ycs  # label
type       lognormal_empirical  # which method to use
parameter  process[Recruitment].ycs_values
years      2012:2016
multiplier 1
... # any other parameters
```

The subcommands `years` and `parameter` are common to all projection methods. Subcommand `years` specifies the years to apply the new values to for the parameter in `parameter`. Note that the years can be before the *finial_year*, e.g., it is normal to vary the last few YCS in a projection run because they are usually poorly estimated or they have been set to 1. The argument `multiplier` is a constant which is multiplied with the projected value after it has been generated. The `type` subcommand gives the method to use to generate new parameter values.

Casal2 allows any estimable parameter to be specified in a `@project` block and then varied from the estimated value in a projection. The available projection types for these parameters include:

- constant
- lognormal
- empirical-lognormal
- empirical re-sampling
- user-defined

Casal2 has no default projection properties for parameters that are specified by year, e.g., year class strength parameters, time-varying parameters, and as a special case, future catches). For these, projections must have a `@project` command block. For example, Casal2 will produce errors if run in projection mode without a `@project` block for the `ycs_values` parameter being specified.

Note for the year class parameters: the definition of year applies to the `ycs_years`, not the model years. As defined in Section 5.3.1, `ycs_years` are offset between the time of spawning and when individuals are added to the partition.

Future catches are also specified in a *@project* block, one for each fishery (see 5.13.1 for examples). Here, a fishery is reference in the *parameter* subcommand with the *method_* fragment to identify it,

process[¡block label¿].method_¡fisheries label¿,

For a process called *Fishing* that has three fisheries defined, it would be *process[Fishing].method_pot* to specify the fishery labelled *pot*.

The Casal2 command to run the model in projection mode is `Casal2 -f 1`. This functionality allows for the exploration of many scenarios with a single set of parameters. The number of projections should be greater than 1 only if applying a projection type that is stochastic.

The `--tabular` flag should be used when running projections after a Bayesian analysis. This option will output a tabular report (see Section 8.27) which can then be analysed in **R**.

An example of the command line evocation is

casal2 -f 1 -i mcmc.txt –tabular ¿ projection.out.txt

where *mcmc.txt* is output from a MCMC run, one parameter set per row, which will give one projection per row, and *projection.out.txt* will contain one row for each MCMC run in each of the reports specified in (usually) the *Report.csv2* file (quantities as specified in the *report.csl2* file).

For a projection run in Casal2, the model is initialised and run through the model years from `start_year` to `final_year`. During this run mode Casal2 stores all parameter values so that projection classes can allow parameters before `final_year` to be projected. The model then is re-run from `start_year` to `projection_final_year`, where any parameter can either be fixed or drawn from a stochastic distribution or process.

5.13.1 Projection methods

This section lists all the projections classes available, their functionality, and an example of the syntax.

The constant projection type, `constant` A parameter can either be fixed during all projection years or specified individually for each projection year. This is a deterministic assumption, where the parameter is assumed to be known without error during projection years.

```
@project Future_ycs
type      constant
parameter process[Recruitment].ycs_values
years     2012:2016
values    1 2 1 2 0.5  #"values 3" means all years use 3
multiplier 1
```

Sampling from a range of years, type `empirical_sampling` Parameters that have time components associated with them can be sampled uniformly with replacement over a range of years and used as values for the projected years. The year range to sample from is between `start_year` and `final_year`:

```
@project   Future_ycs
type       empirical_sampling
parameter  process[Recruitment].ycs_values
years     2012:2016
start_year 1988     # re-sample from estimated values
final_year 2008     # from 1988 to 2008 inclusive
multiplier 1
```

Sampling from a lognormal distribution, type `lognormal` The parameters are drawn from a Gaussian distribution in log space and exponentiated to result in the lognormal distribution

$$X_p = exp(\varepsilon_p - \sigma^2/2) \tag{5.51}$$

where $\varepsilon_p \overset{iid}{\sim} N(\mu,\sigma)$ and X_p is the projected value for parameter X, and μ and σ are the mean and standard deviation on the log scale.

An example of applying this process to draw future year class parameters from a lognormal distribution with mean 1 and standard deviation 0.8

```
@project Future_ycs
type     lognormal
parameter process[Recruitment].ycs_values
years     2012:2016
mean      0     #mean 1 on un-transformed scale
sigma     0.8   # log scale
multiplier 1
```

Sampling from a lognormal distribution where the variance is estimated from values over a specified year range, type `lognormal_empirical` This method applies a lognormal draw as in the `LogNormal` method above and specifies a year range from which the standard deviation of the distribution is calculated. Then equation (5.51) is used to generate future values with a specified μ and empirically calculated σ,

```
@project Future_ycs
type      lognormal_empirical
parameter process[Recruitment].ycs_values
years     2012:2016
mean      0
start_year 1988   # range of years to take the
final_year 2008   # values for \math{\sigma}
multiplier 1
```

Sample from a user-defined function, `user_defined` This method uses the equation parser to calculate the values to use in the projection. This was set up to define and apply harvest control rules (i.e., apply a management action such as changing catch limits based on the current or previous state).

In fisheries models, this option can be used to calculate the projected catch based on an exploitation rate multiplied by the vulnerable biomass, where the exploitation rate is based on a rule (Figure 5.4).

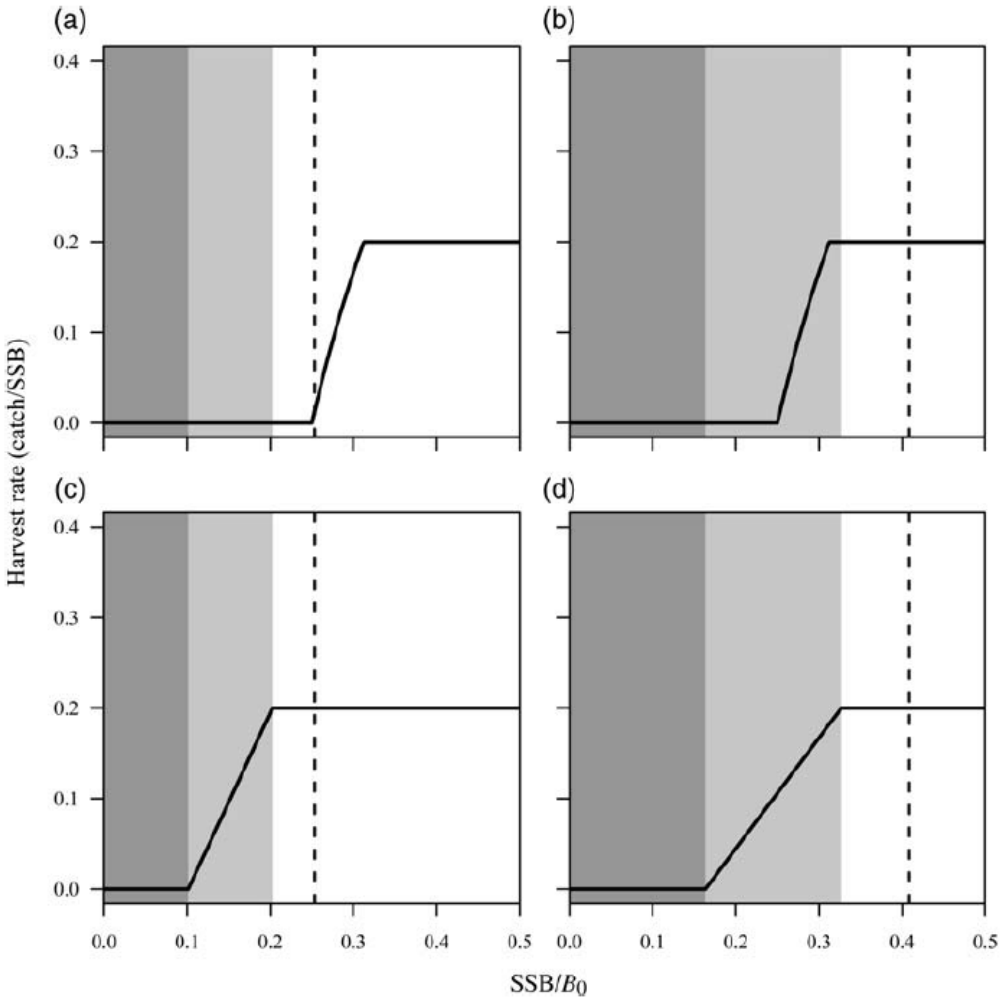

Figure 5.4: Examples of control rules based on current stock status.

```
@project HCR_2015
type       user_defined
parameter process[Instantaneous_Mortality].method_Sub_Ant_F
years 2015
equation if(derived_quantity[SSB].values{2014} / process[Recruitment].b0 <= 0.1, 0.0,
if(derived_quantity[SSB].values{2014} / process[Recruitment].b0 > 0.1 &&
derived_quantity[SSB].values{2014} / process[Recruitment].b0 < 0.2,
derived_quantity[SSB].values{2014} * derived_quantity[SSB].values{2014}
/ process[Recruitment].b0,
derived_quantity[SSB].values{2014} * 0.2))
```

Care should be taken when writing user-defined equations. The above equation is: if $\%B_{2014} \leq 0.1$ then set next year's catch to 0.0, else if $\%B_{2014} > 0.1$ & $\%B_{2014} \leq 0.2$ then set next year's catch equal to $\%B_{2014} \times SSB_{2014}$, else set next year's catch to $0.2SSB_{2014}$.

Specifying catch for projections Catches are unique in that they are known inputs in a table format. For example, to project catches that are in a table

```
# fishing process
@process Fishing
type mortality_instantaneous_retained
m 0.17*6  #0.17    #testing at old values
time_step_proportions 1
relative_m_by_age One*6   #for age based M
categories *
table catches
year FishingLine FishingPot Recreation
1900 0 0 0
1901 13.2 0 22.9
1902 26.4 0 23.5
1903 39.6 0 24
end_table

# projection block
@project future_catch
type      constant
parameter process[Fishing].method_fishingpot
years     2020:2029
values    4000
```

This uses the syntax `block_type[block_label].method_fishinglabel`. **Note:** the fishing label which is defined in the table needs to be lower case form in the `@projection` block. Notice the use of *method_* syntax to identify the right fishery.

6 The estimation section: estimation methods and parameters

The command and subcommand syntax for the estimation section is given in Section 10.

6.1 Role of the estimation section

The role of the estimation section is to define the tasks carried out by Casal2:

1. Define the objective function (see Section 6.2)
2. Define the parameters to be estimated (the free parameters, see Section 6.3)
3. Calculate a point estimate, i.e., the maximum posterior density estimate (MPD) (see Section 6.4)
4. Calculate a posterior profile on selected parameters, i.e., for each of a series of values of a parameter, minimise the objective function, allowing the other estimated parameters to vary (see Section 6.5)
5. Generate MCMC samples from the posterior distribution (see Section 6.6)
6. Calculate the approximate covariance matrix of the parameters as the inverse of the minimizer's approximation to the Hessian, and the corresponding correlation matrix (see Section 6.4)

The estimation section defines the objective function, parameters of the model, and the method of estimation (point estimates, Bayesian posteriors, profiles, etc.). The objective function is based on a goodness-of-fit measure of the model to observations, the assumed priors, and the penalties. See the observation section for a description of the observations, likelihoods, priors, and penalties.

6.2 The objective function

In Bayesian estimation, the objective function is a negative log-posterior,

$$Objective(p) = -\sum_i \log\left[L\left(\mathbf{p}|O_i\right)\right] - \log\left[\pi\left(\mathbf{p}\right)\right] \tag{6.1}$$

where π is the joint prior density of the parameters p.

The contribution to the objective function from the likelihood components is described in Section 7.2. In addition to likelihoods, priors (see Section 6.7) and penalties (see Section 6.8) are components of the objective function. Note that if the priors are specified as uniform, then the prior contribution is zero and the optimisation is now a penalised likelihood and not Bayesian.

Penalties can be used to ensure that the estimated parameter values and derived quantities meet certain restrictions. For example, exploitation rate constraints on mortality events (i.e., fisheries) that are not violated (otherwise there is nothing to prevent the model from having abundances so low that the recorded catches could not have been taken); penalties on category transitions (to ensure there are enough individuals to move); penalties such that estimated values are similar or smooth, etc.

Equation 6.1 can be reduced to a penalised likelihood equation if all priors are assumed to be uniform. This is because uniform priors have no contribution to the objective function so Equation 6.1 reduces to the likelihood components plus penalties.

6.3 Specifying the parameters to be estimated

The parameters to be estimated (estimables) are defined using `@estimate` commands (see Section 10).

For example, a `@estimate` command block

```
@estimate male.m
parameter process[NaturalMortality].m{male}
lower_bound 0.1
upper_bound 0.4
type uniform
```

See Section 3.4.5 for information on how to specify the parameter name. At least one parameter is required to be estimated if doing an estimation `-e`, profile `-p`, or MCMC `-m` run. Initial values for the parameters to be estimated are required, and these values are used as the starting values for the minimiser. However, these values may be overwritten if a set of alternative starting values is provided (i.e., using `casal2 -i`, see Section 3.3).

All parameters are estimated within the specified bounds. For each parameter estimated, the lower and upper bounds and the prior (`type`) (Section 6.7) must be specified. The bounds and the prior should be chosen carefully as they affect the values over which the minimisers search. Some minimisers convert the lower and upper bounds into a minimisation space (for example -1,1 space for the numerical differences algorithm). If estimating only some elements of a vector, either define each element of the vector to be estimated or fix the others by setting the the lower and upper bounds to the same value as the initial value.

6.4 Point estimation

Point estimation is invoked with `casal2 -e`, which attempts to find a minimum of the objective function. Casal2 has multiple minimisation algorithms. There are two automatic differentiation (AD) minimisers: ADOL-C, and BetaDiff (the minimiser used in CASAL). There are also three non-automatic differentiation minimisers: numerical differences, DeltaDiff, and the differential evolution minimiser (`de_solver`). Automatic differentiation minimisers are recommended for more complex models as they are on average much faster and tend to find a more robust minimum when exploring a complex objective surface.

An important input parameter for most minimisers is the `tolerance` parameter. This is the gradient of the objective function, and is used as the stopping rule to define the 'solution' (although a solution may be a local minimum and not the global minimum). Evaluating the robustness of a minimum can be tested with different starting values (i.e., using `-i free_parameter_file.txt`).

Start with the default `tolerance` parameter value of 1e-5 and decrease it while developing a model. For a given model, the parameter estimates when minimising with different tolerance may be different.

6.4.1 The numerical differences minimiser

See Section 10.2.5 for the command syntax.

The numerical differences minimiser uses a quasi-Newton minimiser which is a slightly modified implementation of the main algorithm of Dennis Jr and Schnabel (1996), and uses an *arcsin* transformation to ensure parameters remain within bounds.

The minimiser has three kinds of (non-error) exit status, depending on the minimiser:

- Successful convergence (suggests a local minimum has been found, at least).
- Convergence failure (a local minimum has not been found, although the results may be 'close enough').
- Convergence unclear (the minimiser halted but was unable to determine if convergence occurred. The result may be a local minimum, although this can be checked by restarting the minimiser at the final values of the estimated parameters).

The maximum number of quasi-Newton iterations and objective function evaluations allowed can be specified. If either limit is exceeded, the minimiser exits with a convergence failure. Set the maximum number of evaluations and iterations to values larger than the defaults of 300 and 1000, unless convergence is reached with fewer. An alternative starting point of the minimiser can be specified using `casal2 -i`.

The minimisers are local optimisation algorithms trying to solve a global optimisation problem. What this means is that, even if a 'successful convergence' is reached, the solution may be only a local minimum, and not a global one. To diagnose this problem, start multiple runs from different starting points and comparing the results, or do profiles of one or more key parameters and seeing if any of the profiled estimates finds a better optimum than than the original point estimate.

The approximate covariance matrix of the estimated parameters can be calculated as the inverse of the minimiser's approximation to the Hessian, and the corresponding correlation matrix is also calculated.

Note that

- the Hessian approximation develops over many minimiser steps, so if the minimiser has only run for a small number of iterations the covariance matrix can be a very poor approximation; and
- the inverse Hessian is not a good approximation to the covariance matrix of the estimated parameters, and may not be useful to construct, for example, confidence intervals.

Also note that if an estimated parameter has equal lower and upper bounds, it will have entries of '0' in the covariance matrix and `NaN` or `-1.#IND` (depending on the operating system) in the correlation matrix.

```
@minimiser numerical_diff
type numerical_differences
tolerance 1e-6
iterations 2500
evaluations 4000
```

6.4.2 The DeltaDiff numerical differences minimiser

See Section 10.2.4 for the command syntax.

DeltaDiff applies the same minimiser as Numerical Differences, expect that it uses *tan* rescaling for the parameters rather than *arcsin*. This minimiser may perform better than the Numerical Differences minimiser when parameters are very close to zero bounds.

6.4.3 The differential evolution minimiser

The differential evolution minimiser is a simple population-based, stochastic function minimizer, but is claimed to be quite powerful in solving minimisation problems. It is a method of mathematical optimization of multidimensional functions and belongs to the class of evolution strategy optimizers.

Initially, the procedure randomly generates and evaluates a number of solution vectors (the population size), each with p parameters. Then, for each generation (iteration), the algorithm creates a candidate solution for each existing solution by random mutation and uniform crossover. The random mutation generates a new solution by multiplying the difference between two randomly selected solution vectors by some scale factor, then adding the result to a third vector. Then an element-wise crossover takes place with probability P_{cr}, to generate a potential candidate solution. If this is better than the initial solution vector, it replaces it, otherwise the original solution is retained. The algorithm terminates after either a predefined number of generations (`max_generations`) or when the maximum difference between the scaled individual parameters from the candidate solutions from all populations is less than some predefined amount `tolerance`.

The differential evolution minimiser can be good at finding global minimums in surfaces that may have local minima. However, the speed of the minimiser, and the ability to find a good minima depend on the number of initial 'populations'. Some authors recommend that the number of populations be set at about $10 * p$, where p is the number of free parameters. However, depending on the model, this value can be set to a lower value and still find a robust solution.

There is no proof of convergence for the differential evolution solver, but several papers have found it to be an efficient method of solving multidimensional problems. Some results suggest that it can often find a better minima and may be faster or longer (depending on the actual model specification) at finding a solution when compared with the numerical differences minimiser. Comparisons with automatic differentiation minimisers or other more sophisticated algorithms have not been made.

```
@minimiser DE_solver
type de_solver
tolerance 1e-6
iterations 2500
evaluations 4000
```

6.4.4 The BetaDiff minimiser

An automatic differentiation minimiser for non-linear models, This is the minimiser from the original CASAL package, based on ADOL-C.

```
@minimiser beta_diff
type beta_diff
tolerance 1e-6
iterations 2500
evaluations 4000
```

6.4.5 The ADOL-C minimiser

An automatic differentiation minimiser for non-linear models. See `https://projects.coin-or.org/ADOL-C` for more information.

```
@minimiser ADOLC
type adolc
step_size 1e-6
iterations 2500
evaluations 4000
tolerance 1e-6
```

6.5 Posterior profiles

If profiles are run using the command `casal2 -p`, Casal2 will first calculate a point estimate. For each scalar parameter or, in the case of vectors or selectivities, the element of the parameter to be profiled, Casal2 will fix its value at a sequence of n evenly spaced numbers ($step$) between the specified lower and upper bounds l and u, and calculate a point estimate at each value.

By default $step = 10$, and $(l,u) =$ (lower bound on parameter plus $(range/(2n))$, upper bound on parameter less $(range/(2n))$. Each minimisation starts at the final parameter values from the previous resulting value of the parameter being profiled. Casal2 will report the objective function for each parameter value. The initial point estimate should be compared with the profile results, to check at least that none of the other points along the profile have a better objective function value than the initial 'minimum'.

The parameters to be profiled are specified, and optionally the number of steps, and lower bound and upper bound, for each parameter. In the case of vector parameters, the element(s) of the vector to be profiled are specified.

The initial starting point for the estimation can also be specified using `casal2 -i file`, which may improve the minimiser performance for the profiles.

If the profile results are not reasonable, it may be a result of not using enough iterations in the minimiser or a poor choice of minimiser control variables (e.g., the minimiser tolerance). It may also be useful to try other minimisers and compare the results.

6.6 Bayesian estimation

Casal2 can use Markov chain Monte Carlo (MCMC) functionality to generate a sample from the posterior distribution of the estimated parameters with command `casal2 -m` and output the sampled values to a file, optionally keeping only every nth set of values.

As Casal2 has no post-processing capabilities. Casal2 cannot produce MCMC convergence diagnostics. To calculate these diagnostics, use a package such as BOA, plot/summarize the posterior distributions of the output quantities, and/or use a general-purpose statistical package such as **R**.

Bayesian methodology and MCMC are both large and complex topics. See Gelman et al. (1995) and Gilks et al. (1994) for details of both Bayesian analysis and MCMC methods. In addition, see Punt & Hilborn (2001) for an introduction to quantitative fish stock assessment using Bayesian methods.

This section briefly describes the MCMC algorithms used in Casal2. See Section 10.3 for the Casal2 commands used in an MCMC Bayesian analysis.

Casal2 implements two methods for MCMC. The first is a straightforward implementation of the random walk Metropolis-Hastings algorithm (Gelman et al., 1995, Gilks et al., 1994). The Metropolis-Hastings algorithm attempts to draw a sample from a Bayesian posterior distribution, and calculates the posterior density π, scaled by an unknown constant. The algorithm generates a 'chain' or sequence of values. Typically the beginning of the chain is discarded (the burn-in period) and every Nth element of the remainder is taken as the posterior sample. The second is Hamiltonian Monte Carlo. This uses similar subcommands as the random walk Metropolis-Hastings algorithm. In both cases, the chain is produced by taking an initial point x_0 and repeatedly applying the following rule, where x_i is the current point:

1. Draw a candidate step s from a proposal distribution J, which should be symmetric i.e., $J(-s) = J(s)$
2. Calculate $r = min(\pi(x_i + s)/\pi(x_i), 1)$
3. Let $x_{i+1} = x_i + s$ with probability r, or x_i with probability $1 - r$

An initial point estimate is produced before the chain starts, which is done so as to calculate the approximate covariance matrix of the estimated parameters (as the inverse Hessian), and may also be used as the starting point of the chain.

The starting point of the point estimate minimiser can be specified using the command `casal2 -i`. Don't start it too close to the actual estimate (either by using `casal2 -i`, or by changing the initial parameter values in input configuration file) as it takes a few iterations to determine a reasonable approximation to the Hessian.

There are currently two options for the starting point of the MCMC:

- Start from the point estimate; or
- Restart a chain given a covariance matrix and a previous starting point.

The chain moves in natural space, i.e., no transformations are applied to the estimated parameters. The default proposal distribution is a multivariate Student's t distribution centred on the current point, with covariance matrix equal to a matrix based on the approximate covariance produced by the minimiser, multiplied by a step size factor.

The following steps define how the initial covariance matrix of the proposal distribution is calculated:

1. The covariance matrix is taken as the inverse of the approximate Hessian from the quasi-Newton minimiser.
2. The covariance matrix is modified so as to decrease all correlations greater than `@mcmc.max_correlation` down to `@mcmc.max_correlation`, and similarly to increase all correlations less than `-@mcmc.max_correlation` up to `-@mcmc.max_correlation` (the `@mcmc.max_correlation` parameter defaults to 0.8). This should help to avoid getting 'stuck' in a lower-dimensional subspace.
3. The covariance matrix is then modified either by

   - `@mcmc.adjustment_method=covariance`: that if the variance of the ith parameter is non-zero and less than `@mcmc.min_difference` multiplied by the difference between the parameters' lower and upper bound, then the variance is changed, without changing the associated correlations, to $k =$min_diff$(upper_bound_i - lower_bound_i)$. This is done by setting

     $$\mathrm{Cov}(i,j)' = \mathrm{sqrt}(k)\,\mathrm{Cov}(i,j)/\mathrm{sd}(i)$$

     for $i \neq j$, and $\mathrm{var}(i)' = k$
   - `@mcmc.adjustment_method=correlation`: that if the variance of the ith parameter is non-zero and less than `@mcmc.min_difference` multiplied by the difference between the parameters' lower and upper bounds, then its variance is changed to $k = min\_diff(upper\_bound_i - lower\_bound_i)$. This differs from (i) above in that the effect of this option is that it also modifies the resulting correlations between the ith parameter and all other parameters.

This allows each estimated parameter to move in the MCMC even if its variance is very small according to the inverse Hessian. In both cases, the `@mcmc.min_difference` parameter defaults to 0.0001.

4. The `@mcmc.stepsize` (a scalar factor applied to the covariance matrix to improve the acceptance probability) is set by the user. The default is $2.4d^{-0.5}$ where d is the number of estimated parameters, as recommended by Gelman et al. (Gelman et al., 1995).

The proposal distribution can also change adaptively during the chain, using two different mechanisms. Both are offered as means of improving the convergence properties of the chain. It is important to note that any adaptive behaviour must finish before the end of the burn-in period, i.e., the proposal distribution must be finalised before the kept portion of the chain starts.

The adaptive mechanisms are:

- The step size changes adaptively at one or more sample numbers (See next paragraph for details on the step size adaptation methods)
- The entire covariance matrix changes adaptively at one or more sample numbers. At each adaptation, the covariance matrix is replaced with an empirical covariance matrix, derived from the MCMC chain. The idea is that an empirical covariance is a better approximation of the proposal distribution than the inverse of the Hessian matrix, and can improve convergence and mixing of the chain.

The two options to adapt the step size are `double_half` or `ratio`, which is chosen with the input parameter `adapt_stepsize_method`. The `double_half` method is used in CASAL (see Gelman et al. (Gelman et al., 1995) for justification).

The algorithm for `double_half` is, at each adaptation, the step size is doubled if the acceptance rate since the last adaptation is more than 0.5, or halved if the acceptance rate is less than 0.2. The `ratio` is taken from SPM. It adapts the current step size by the acceptance rate since the last adaptation multiplied by 4.1667 to approach an acceptance rate of ≈ 0.24. See Sherlock and Roberts (2009) for justification on that acceptance rate.

The `stepsize` parameter is now on a completely different scale, and must be rescaled. It is set to a user-specified value (which may or may not be the same as the initial step size). Set the step size adaptations to occur after this, so that the step size can be readjusted to an appropriate value which gives good acceptance probabilities with the new matrix.

All modified versions of the covariance matrix are printed to the standard output, but only the initial covariance matrix (inverse Hessian) is saved to the objectives file. The number of covariance modifications by each iteration is recorded as a column on the objectives file.

The variance-covariance matrix of this sub-sample of chain is calculated. As above, correlations greater than `@mcmc.max_correlation` are reduced to `@mcmc.max_correlation`, correlations less than -`@mcmc.max_correlation` are increased to -`@mcmc.max_correlation`, and very small non-zero variances are increased (`@mcmc.covariance_adjustment` and `@mcmc.min_difference`). The result is the new variance-covariance matrix of the proposal distribution.

The procedure used to choose the sample of points is that, to start, all points on the chain so far are taken. All points in an initial user-specified period are discarded. The assumption is that the chain will have started moving during this period. If this is incorrect and the chain has still not moved by the end of this period, it is a fatal error and Casal2 stops. The remaining set of points must contain at least some user-specified number of transitions. If this is incorrect and the chain has not had at least this number of transitions, then it is also a fatal error. If this test is passed, the set of points is systematically sub-sampled down to 1000 points (and it must be at least this long to start with).

The probability of acceptance for each jump is 0 if the jump would move a parameter value outside of its bounds, 1 if it improves the posterior, or $(newposterior/oldposterior)$ otherwise. How often the position of the chain is recorded is specified with the `keep` parameter. For example, with `keep 10`, only every 10th sample is recorded.

The option to specify that some of the estimated parameters are fixed during the MCMC is available. If the chain starts at the point estimate or at a random location, these fixed parameters are set to their values at the point estimate.

If the start of the chain is specified with the command `casal2 -i`, these fixed parameters are set to the values in the file.

Restarting an MCMC chain: in the case where an MCMC chain was halted or interrupted, the MCMC chain can be restarted from where it finished with

```
casal2 -R MPD_file --objective-file objectives_file --sample-file samples_file
```

where `Objective_file_name` is the file name for the objective function report and `Sample_file_name` is the file name for the sample report from a MCMC chain.

The posterior sample can be used for (projections (Section 5.13)) or simulations (see Section 7.6) with the values supplied with the command `casal2 -i file`.

A multivariate Student's t distribution is used as an alternative to the multivariate normal proposal distribution. If you request multivariate Student's t proposals, change the degrees of freedom from the default of 4. As the degrees of freedom decreases, the t distribution becomes more heavy tailed. This may lead to better convergence properties. Note the default is the multivariate Student's t.

Given a posterior (sub)sample, Casal2 can calculate a list of output quantities for each sample point (see Section 8 specifically tabular report). These quantities can be output to a file (with the command `casal2 -r --tabular`) and read into an external software package where the posterior distributions can be plotted and/or summarised.

The posterior sample can also be used for projections (Section 5.13). The advantage of this is that the parameter uncertainty, as expressed in the posterior distribution, can be included into the risk estimates.

6.7 Priors

In a Bayesian analysis, a prior is required for every parameter that is being estimated. There are no default priors.

When some of these priors are parameterised in terms of mean, c.v., and standard deviation, these refer to the parameters of the distribution before the bounds are applied. The moments of the prior after the bounds are applied may differ.

Casal2 has the following priors (expressed in terms of their contribution to the objective function):

6.7.1 Uniform

$$-\log\left(\pi\left(p\right)\right) = 0 \tag{6.2}$$

6.7.2 Uniform-log

(i.e., $\log(p) \sim$ uniform)

$$-\log\left(\pi\left(p\right)\right) = \log\left(p\right) \tag{6.3}$$

6.7.3 Normal

The normal distribution with mean μ and standard deviation with c.v c

$$-\log\left(\pi\left(p\right)\right) = 0.5\left(\frac{p-\mu}{c\mu}\right)^2 \tag{6.4}$$

6.7.4 Normal with standard deviation

The normal distribution with mean μ and standard deviation σ

$$-\log(\pi(p)) = 0.5\left(\frac{p-\mu}{\sigma}\right)^2 \tag{6.5}$$

6.7.5 Lognormal

The lognormal distribution with mean μ and c.v. c

$$-\log(\pi(p)) = \log(p) + 0.5\left(\frac{\log(p/\mu)}{s} + \frac{s}{2}\right)^2 \tag{6.6}$$

where s is the standard deviation of $\log(p)$ and $s = \sqrt{\log(1+c^2)}$.

6.7.6 Normal-log

The normal-log distribution with mean μ and c.v. c

Similar to the lognormal prior, but with the mean (*mu*) and standard deviation (*sigma*) specified in log space.

where s is the standard deviation of $\log(p)$ and $s = \sqrt{\log(1+c^2)}$.

6.7.7 Beta

The Beta distribution with mean μ and standard deviation σ, and range parameters A and B

$$-\log(\pi(p)) = (1-m)\log(p-A) + (1-n)\log(B-p) \tag{6.7}$$

where $\nu = \frac{\mu-A}{B-A}$, and $\tau = \frac{(\mu-A)(B-\mu)}{\sigma^2} - 1$ and then $\mu = \tau\nu$ and $n = \tau(1-\nu)$. Note that the beta prior is undefined when $\tau \leq 0$.

Vectors of parameters can be independently (but not necessarily identically) distributed according to any of the above forms, in which case the joint negative-log-prior for the vector is the sum of the negative-log-priors of the components. Values of each parameter need to be specified for each element of the vector. Example of syntax to define the estimation of a parameter and the prior assumed:

```
## uniform-log example estimate
@estimate B0
type uniform_log # this command "type" defines the prior type.
parameter process[Recruitment].b0 # "Recruitment" is the label of your process
upper_bound 20000
lower_bound 1000

## Lognormal YCS estimation
@estimate year_class_strengths_1990_1995
type lognormal
parameter process[Recruitment].ycs_values{1990:1995}
# ycs_year  1990 1991 1992 1993 1994 1995
mu    1    1    1    1    1    1
cv  0.9  0.9  0.9  0.9  0.9  0.9
lower_bound 0.01 0.01 0.01 0.01 0.01 0.01
upper_bound 9 9 9 9 9 9
```

6.8 Penalties

Penalties are associated with processes and can be used to enforce parameter value or derived quantity restrictions or model outputs that are invalid by adding a penalty to the objective function. For example, estimated parameter values can be restricted so that a known mortality event removes enough individuals from the population within an event mortality process. Casal2 requires penalty functions for processes that remove or shift a *number* of individuals between categories or from the partition. Many of the penalties that were available in CASAL have been moved to be additional priors in Casal2(see Section 6.9).

For penalties, a multiplier is required to be specified, and the objective function is increased by this multiplier multiplied by the penalty value. In some cases the multiplier may need to be quite large to prohibit some model behaviour.

Penalties are implemented for the processes

- `@process[label].type=event_mortality`,
- `@process[label].type=mortality_instantaneous`,
- `@process[label].type=tag_by_length`,
- `@process[label].type=tag_by_length`, and
- `@process[label].type=category_transition`

For these processes, two types of penalties can be defined: on the natural scale (the default) and on the log scale. Both of these types add a penalty value of the squared difference between the observed value (e.g., the actual number of individuals to be removed in an event mortality process or the actual number of individuals to shift in a category transition process), and the number that were moved (if less than or equal), multiplied by the penalty multiplier.

The natural scale penalty calculates the squared difference on a natural scale, and the log scale penalty calculates the squared difference of the logged values.

For example:

```
@process Mortality
type mortality_instantaneous
penalty CatchMustBeTaken

# define the penalty in an @penalty block
@penalty CatchMustBeTaken
type process
log_scale True
multiplier 10000
```

Penalties are added to the objective function in the following ways;

$$Penalty = (X_1 - X_2)^2 \tag{6.8}$$

or if `log_scale true`

$$Penalty = (log(X_1) - log(X_2))^2 \tag{6.9}$$

where, for example, X_1 is observed catch biomass and X_2 is the estimated catch biomass. Penalties are usually applied in situations when numbers or weight are known. Another example is for tagging, where the number of individuals that were tagged in a given year is known, so a penalty can be used to restrict the model to estimate reasonable values for the numbers of tagged individuals in that year.

6.9 Additional Priors

Additional priors can be thought of as the inverse of penalties . For CASAL models, most of the legacy `@penalty` blocks have now been implemented as `@additional_prior` blocks. They restrict parameters in user-defined spaces .

The types of additional priors available in Casal2 are `vector_smoothing`, `vector_averaging`, `uniform_log`, `lognormal`, `element_difference`, and `Beta`:

- `vector_average`

  This prior can be applied to a vector parameter. Sum of squares of r^{th} differences, optionally on a log scale. This encourages the vector to be like a polynomial of degree $(r-1)$. A range of the vector to be "smoothed" can be specified (and if not, the smoother is applied to the entire vector). However, this restriction must be specified by an index of the vector and must be between 1 and the length of the vector, inclusive.
- `vector_smoothing`

  This prior can be applied to a vector parameter. Square of (mean(vector)-k), or of (mean(log(vector))-l), or of (log(mean(vector)/m)). Restricts the vector to average arithmetically to k or m, or geometrically to exp(l). Typically used for YCS with k=1 or m=1 or l=0, to restrict the YCS to centre on 1. Optionally, indices can be chosen or excluded outside a given set of bounds.
- `lognormal` with mean μ and c.v. c

$$-\log(\pi(p)) = \log(p) + 0.5\left(\frac{\log(p/\mu)}{s} + \frac{s}{2}\right)^2 \tag{6.10}$$

- `uniform_log`

$$-\log(\pi(p)) = \log(p) \tag{6.11}$$

- `element_difference`

$$-\log(\pi(p_1, p_2)) = \sum_{i=1}^{n} (p_{1,i} - p_{2,i})^2 \tag{6.12}$$

- `Beta`

  Beta with mean μ and standard deviation σ, and range parameters A and B, for parameter value = p

$$-\log(\pi(p)) = (1-m)\log(p-A) + (1-n)\log(B-p) \tag{6.13}$$

  where $\nu = \frac{\mu-A}{B-A}$, and $\tau = \frac{(\mu-A)(B-\mu)}{\sigma^2} - 1$ and then $m = \tau\nu$ and $n = \tau(1-\nu)$. The beta prior is undefined when $\tau \leq 0$.

Methods available for the type `vector_average` are `l`, `k`, `m`. For a target vector parameter $\mathbf{X}$ and target mean k, the contribution to the objective score is

- `method k`
  $-\log(\pi(p)) = (\bar{X} - k)^2$
- `method l`
  $-\log(\pi(p)) = \left(\overline{ln(X)} - k\right)^2$
- `method m`
  $-\log(\pi(p)) = (ln(\bar{X}) - k)^2$

where $\overline{ln(X)}$ is the mean of the logged values.

There are a range of parameters and derived values that additional priors can be applied to. Here are a list of non-estimated (all parameters that can be estimated can have an additional prior attached to them) parameters that additional priors can be applied to.

- `selectivity[Selectivity_label].values{i:j}`.

  This subcommand applies a selectivity to the value by age (for ages i through j). This option is available only for certain types of selectivities (`all_values`, `all_values_bounded`, `double_exponential`). See the Hoki stock assessment for an example of applying additional priors on selectivities.

- `catchability[Catchability_label].q`

  This subcommand is for catchabilities that are of type `nuisance` only. Since `nuisance` qs are not free parameters, additional priors can be applied to replicate CASAL models with `@estimate` blocks in nuisance qs. If a CASAL model applied a uniform prior, then this has a null effect and this functionality can be ignored when converting to a Casal2 model.

This list may be useful for users who are trying to apply the equivalent CASAL penalties in a Casal2 model.

6.10 Parameter Transformations

Casal2 has multiple methods to transform a parameter, with some methods developed for legacy purposes. Transformations are implemented to try and achieve 'better' model optimisation. Complex population models can have highly correlated parameters so transforming them to be orthogonal or to be in a different space is a way of addressing correlations, and to allow the minimiser to find a 'global' minimum quicker. To read more about transformations and get a better understanding of why they are used, see Gilks et al. (1995), specifically chapter 6.

There are two main transformation methods available in Casal2, `transform_with_jacobian` and `prior_applies_to_transform`. When using `transform_with_jacobian`, priors are defined on parameters in natural/model space (the usual priors) but when the parameter is passed to the minimiser it gets transformed and a Jacobian is added to the objective function to account for this transformation. The second method is when bounds and prior parameters on the parameters can be specified in transformed space. Note that both `prior_applies_to_transform` and `transform_with_jacobian` cannot be set to `true`.

There are two ways that transformations can be applied. The first is within the `@estimate` block, which is for univariate (simple) transformations only. For more complex transformations a `@estimate_transformation` block must be specified to describe the transformation.

For example:

```
## simple transformation
@estimate log_R0
type lognormal
transformation log
parameter process[Recruitment].r0
transform_with_jacobian true
mu 442413
cv 0.2
lower_bound 3000
upper_bound 24154953


## more complex transformation
@estimate R0
type lognormal
parameter process[Recruitment].r0
mu 442413
```

```
cv 0.2
lower_bound 3000
upper_bound 24154953

@estimate_transformation Log_R0
type log
estimate_label log_R0
transform_with_jacobian true
```

Transform with Jacobian

The support of a random variable X with density $p_X(x)$ is that subset of values for which it has non-zero density,

$$supp(X) = \{x|p_X(x) > 0\} \tag{6.14}$$

If f is a transformation function defined on the support of X, then $Y = f(X)$ is a new random variable (transformed variable).

This section shows the available transformations in Casal2 and the probability density function of Y.

Suppose X is one dimensional and f: $supp(X) \rightarrow \mathbf{R}$ is a one-to-one, monotonic function with a differentiable inverse f^{-1}. Then the density of Y is

$$p_Y(y) = p_X(f^{-1}(y)) \left| \frac{\partial}{\partial y} f^{-1}(y) \right| \tag{6.15}$$

where $\left| \frac{\partial}{\partial y} f^{-1}(y) \right|$ is the Jacobian term. The Jacobian measures how the scale of the transformed variable changes with respect to the underlying variable. This can be expanded to the multivariate case where the Jacobian becomes a matrix of partial derivatives.

In equation 6.15 the term $p_X(f^{-1}(y)) = p_X(X)$ and in a Bayesian context is the prior of the untransformed variable/parameter. **Note:** if this functionality is in use be careful interpreting the covariance matrix as this will be related to the transformed variable not the variable space, e.g., if natural mortality (M) is estimated as $Y = M/2$, then the covariance matrix will be described for Y.

```
@estimate log_R0
type lognormal
transformation log
parameter process[Recruitment].r0
transform_with_jacobian true
mu 442413
cv 0.2
lower_bound 3000
upper_bound 24154953
```

Transform without Jacobian but prior defined in transformed space

This transformation is where the priors are defined in transformed space. This class of transformations contains functionality that was implemented in the CASAL.

If $f()$ is a transformation function defined on the support of X, then $Y = f(X)$ is a new random variable (transformed variable). In this class *a priori* information is specified with regard to $p_Y(y)$ and X can be thought of as a derived quantity.

For example:

```
@estimate log_R0
type lognormal
parameter process[Recruitment].r0
prior_applies_to_transform true
mu 13
cv 0.5
lower_bound 8
upper_bound 17
```

Transformation types

- `log` : natural logarithm transformation
  `is_simple = true`
  `jacobian defined = true`
  $Y = ln(X)$
  $\left|\frac{\partial}{\partial y} f^{-1}(y)\right| = X^{-1}$

- `inverse`
  `is_simple = true`
  `jacobian defined = true`
  $Y = X^{-1}$
  $\left|\frac{\partial}{\partial y} f^{-1}(y)\right| = -X^{-2}$

- `sqrt` : square root transformation
  `is_simple = true`
  `jacobian defined = true`
  $Y = \sqrt{X}$
  $\left|\frac{\partial}{\partial y} f^{-1}(y)\right| = -X^{-1.5}$

- `average_difference` : two parameters θ_1 and θ_2 are transformed to Y_1 and Y_2, where Y_1 is the average of the original parameters and Y_2 is the difference between the mean and each parameter.
  `is_simple = false`
  `jacobian defined = false`
  $Y_1 = \frac{\theta_1+\theta_2}{2}$
  $Y_2 = (Y_1 - \theta_2)2$
  Restore transformations
  $\theta_1 = Y_1 + 0.5Y_2$
  $\theta_2 = \theta_1 - 0.5Y_2$
  $\left|\frac{\partial}{\partial y} f^{-1}(y)\right|$ Hasn't been assessed (i.e it could exist)

- `log_sum` : two parameters θ_1 and θ_2 are transformed to Y_1 and Y_2, where Y_1 is the natural logarithm of the sum of θ_1 and θ_2. Y_2 describes the proportion of the sum with respect to θ_1
  `is_simple = false`
  `jacobian defined = false`
  $Y_1 = ln(\theta_1 + \theta_2)$
  $Y_2 = \theta_1/(\theta_1 + \theta_2)$
  Restore transformations
  $\theta_1 = exp(Y_1)Y_2$
  $\theta_2 = exp(Y_1)(1 - Y_2)$
  $\left|\frac{\partial}{\partial y} f^{-1}(y)\right|$ Hasn't been assessed (i.e it could exist)

- `orthogonal` : two parameters θ_1 and θ_2 are transformed to Y_1 and Y_2, where Y_1 is the multiplication of θ_1 and θ_2. Y_2 is the division of θ_1 and θ_2
  `is_simple = false`
  `jacobian defined = true`
  $Y_1 = \theta_1\theta_2$
  $Y_2 = \theta_1/\theta_2$
  Restore transformations
  $\theta_1 = \sqrt{Y_1Y_2}$
  $\theta_2 = \sqrt{Y_1/Y_2}$
  $\left|\frac{\partial}{\partial y}f^{-1}(y)\right| = 2Y_2$

- `SumToOne` : given two parameters θ_1 and θ_2 that have the constraint $\sum_{i=1}^{2}\theta_i$, estimate θ_1 only given $\theta_2 = 1-\theta_1$
  `is_simple = false`
  `jacobian defined = false`

7 The observation section: observations and their likelihoods

The command and subcommand syntax for the estimation section is given in Section 11.1.

7.1 Observations

The objective function calculates the goodness-of-fit of the model to the observation data. Observations are typically supplied at an instance in time, over a group of aggregated categories. Most observations are sampled over time, i.e., data which were recorded for one or more years, in the same format each year. Examples of time series data types include relative abundance indices, commercial catch length frequencies, and survey numbers-at-age.

Definitions for each type of observation are described below, including how the observed values should be formatted, how Casal2 calculates the expected values, and the likelihoods that are available for each type of observation.

There are two main types of observations available in Casal2. The first type is observations that are associated with a process, and the second are associated with a mortality block (See Section 5.3.3.

Observations for a process are indicated by their type — these use the word process as a part of the type name, e,.g., **`@observation`** *`type`* abundance is an observation of relative abundance that occurs during a mortality block within a time step, and **`@observation`** *`type`* process_abundance is a observation of relative abundance that occurs during a process within a time step.

There are two types of process observations. *process observations* are observations that are associated with a specific process (e.g., `process_proportions_migrating`), and **general process observations** are observations that can be associated with any process (e.g., `process_proportions_at_age`). The observation types are described in different sections.

7.1.1 Mortality block associated observations

All observations within this class are calculated similarly. That is, the expected values are calculated at the beginning of the mortality block and at the end of the mortality block. Casal2 then uses a linear interpolation to approximate the expected values part way through a mortality block using the subcommand `time_step_proportion`. This feature could be useful if a survey occurs part way through an exploitation phase, which may be part way through a fishing season when modelling a fish population. Each observation in this class will evaluate different expectations of the partition (explained in the following descriptions).

The observation `types` available with this class of observations are:

- `abundance`
- `biomass`
- `proportions_at_age`
- `proportions_at_length`
- `proportions_by_category`
- `tag_recapture_by_length`
- `tag_recapture_by_age`

Abundance or biomass observations Abundance (or biomass) observations are observations of either a relative or absolute number (or biomass) of individuals from a set of categories after applying a selectivity. The observation classes are the same, except that a biomass observation will use the biomass as the observed (and expected) value (calculated from mean weight of individuals within each age and category) while an abundance observation is the number of individuals.

Each observation is for a given year and time-step, for some selected age classes of the population (for a range of ages multiplied by a selectivity), for aggregated categories. Furthermore, the label of the catchability coefficient q is required; q can either be estimated of fixed. For absolute abundance or absolute biomass observations, define a catchability where $q = 1$. Catchabilities can be estimated as either free parameters (See Section 10.5.1) or as nuisance parameters (see Section 10.5.2).

The observations can be supplied for any set of categories. For example, for a model with the two categories *male* and *female*, an observation of the total abundance/biomass (male + female) or male-only abundance/biomass could be provided. The subcommand `categories` defines the categories used to aggregate the abundance/biomass. In addition, each category must have an associated selectivity, defined by `selectivities`.

For example,

```
categories male
selectivities male-selectivity
```

defines an observation for males after applying the selectivity male-selectivity. Casal2 then requires that an observation is supplied. The expected values for the observations will be the expected abundance (or biomass) of males, after applying the selectivities, at the year and time-step specified.

Casal2 calculates the expected values by summing over the defined ages (via the age range and selectivity) and categories at both the beginning and end of a mortality block. Casal2 will approximate the expectation part way through the mortality block using the `time_step_proportion`. The default `time_step_proportion` value is 0.5. Casal2 does linear interpolation between the start and end abundance (or biomass) from the mortality block.

For an abundance observation the expected value is

$$E_{i,1} = \sum_{c=1} \sum_{a=1}^{A} S_{a,c} N_{a,c,i,1} \tag{7.1}$$

$$E_{i,2} = \sum_{c=1} \sum_{a=1}^{A} S_{a} N_{a,c,i,2} \tag{7.2}$$

Where $E_{i,1}$ is the expectation at the beginning of time step and $E_{i,2}$ is the expectation at the end of the time-step. S_a is the selectivity for age a and category c. If there is no mortality related to this observation then E_i which is used in the likelihood contribution is $E_{i,1}$. If this was a biomass observation, then $N_{a,c,i,1}$ in Equations (7.1) and (7.2) is replaced with $N_{a,c,i,1}\bar{w}_{a,c}$, where $\bar{w}_{a,c}$ is the mean weight of category c at age a. If the user wishes to apply 100% mortality then $E_i = E_{i,2}$.

For applying quantities of mortality between these values (M_i), the linear interpolation is

$$E_i = |E_{i,1} - E_{i,2}| M_i \tag{7.3}$$

For each year of observations, the observation table `table obs` has a row with year in the first column, the observation per category in the middle column(s), and the error value in the final column:

```
@observation MyAbundance
type abundance
years 1999
...
categories male
table obs
1999 1000 0.10
end_table
...
```

For an observation aggregated over multiple categories:

```
@observation MyAbundance
type abundance
years 1990 1991
...
categories male+female
table obs
1990 1000 0.10
1991 1200 0.12
end_table
...
```

For observations for multiple categories:

```
@observation MyAbundance
type abundance
years 1990 1991
...
categories male female
table obs
1990 550 450 0.10
1991 700 500 0.12
end_table
...
```

To define a biomass observation instead of an abundance observation, use

```
@observation MyBiomass
type biomass
...
```

Proportions-at-age Proportions-at-age observations are observations of the relative number of individuals at age, via some selectivity.

The observation is supplied for a given year and time-step, for some selected age classes of the population (i.e., for a range of ages multiplied by a selectivity), for categories aggregated over a set of spatial cells. Note that the categories defined in the observations must have an associated selectivity, defined by `selectivities`.

The age range must be ages defined in the partition (i.e., between `@model.min_age` and `@model.max_age` inclusive); the upper end of the age range can optionally be a plus group, which must be either the same as or less than the plus group defined for the partition.

Proportions-at-age observations can be supplied as

- a set of proportions for a single category,
- a set of proportions for multiple categories, or
- a set of proportions across aggregated categories.

The method of evaluating expectations are the same for all three types of proportions. The definitions of these proportions and the expected dimensions of observation and error inputs that Casal2 expects for each respective proportion type are described below with examples.

Like all types of observations that are associated with the mortality block, Casal2 will evaluate the numbers at age before and after the mortality block for the specified time step of the observation, and applying the user-defined selectivity. Casal2 then generates the expectations from the partition part way through the mortality block using the subcommand `time_step_proportion`. This approximation is a linear interpolation of the numbers-at-age over the mortality block.

The ageing error is then applied, if the user has specified it. Finally, Casal2 converts the numbers-at-age to proportions-at-age by dividing all numbers in an age bin by the total numbers. The likelihood for the proportions-at-age observation is then calculated.

Defining an observation for a single category is used to model a set of proportions of a single category by age class. For example, to specify that the observations are of the proportions of male within each age class, then the subcommand `categories` for the `@observation[label].type=proportion_by_age` command is

```
categories male
```

Casal2 then requires that there will be a single vector of proportions supplied, with one proportion for each age class within the defined age range, and that these proportions sum to one.

For example, if the age range was 3 to 10, then 8 proportions should be supplied, one proportion for each of the the ages 3, 4, 5, 6, 7, 8, 9, and 10. The expected values will be the expected proportions of males within each of these age classes (after omitting males aged less than 3 and older than 10), after applying a selectivity at the year and time-step specified. The supplied vector of proportions (i.e., in this example, the 8 proportions) must sum to one, which is evaluated with a default tolerance of 0.001.

```
@observation MyProportions
type proportions_at_age
...
categories male
min_age 3
max_age 9
years 1990
table obs
1990 0.01 0.09 0.20 0.20 0.35 0.10 0.05
end_table
...
```

Defining an observation for multiple categories extends the single category observation definition. It is used to model a set of proportions over several categories by age class. For example, to specify that the observations are of the proportions of male or females within each age class, then the subcommand `categories` for the `@observation[label].type=proportion_by_age` command is

```
categories male female
```

Casal2 then requires that there will be a single vector of proportions supplied, with one proportion for each category and age class combination, and that these proportions sum to one across all ages and categories.

For example, if there were two categories and the age range was 3 to 10, then 16 proportions should be supplied (one proportion for each of the ages 3, 4, 5, 6, 7, 8, 9, and 10, for each category male and female). The expected values will be the expected proportions of males and females within each of these age classes (after omitting those aged less than 3 and older than 10), after applying a selectivity at the year and time-step specified. The supplied vector of proportions (i.e., in this example, the 16 proportions) must sum to one, which is evaluated with a default tolerance of 0.001.

For example,

```
@observation MyProportions
type proportions_at_age
...
categories male female
min_age 1
max_age 5
```

```
years 1990 1991
table obs
1990 0.01 0.05 0.10 0.20 0.20 0.01 0.05 0.15 0.20 0.03
1991 0.02 0.06 0.10 0.21 0.18 0.02 0.03 0.17 0.20 0.01
end_table
...
```

Defining an observation across aggregated categories allows categories to be aggregated before the proportions are calculated. It is used to model a set of proportions from several categories that have been combined by age class. To indicate that two (or more) categories are to be aggregated, separate them with a '+' symbol. For example, to specify that the observations are of the proportions of male and females combined within each age class, then the subcommand `categories` for the `@observation[label].type=proportion_by_age` command is

```
categories male + female
```

Casal2 then requires that there will be a single vector of proportions supplied, with one proportion for each age class, and that these proportions sum to one.

For example, if there were two categories and the age range was 3 to 10, then 8 proportions should be supplied (one proportion for each of the the ages 3, 4, 5, 6, 7, 8, 9, and 10, for the sum of males and females within each age class). The expected values will be the expected proportions of males + females within each of these age classes (after omitting those aged less than 3 and older than 10), after applying a selectivity at the year and time-step specified. The supplied vector of proportions (i.e., in this example, the 8 proportions) must sum to one, which is evaluated with a default tolerance of 0.001.

For example,

```
@observation MyProportions
type proportions_at_age
...
years 1990 1991
categories male+female
min_age 1
max_age 5
table obs
1990 0.02 0.13 0.25 0.30 0.30
1991 0.02 0.06 0.18 0.35 0.39
end_table
...
```

The latter form can then be extended to include multiple categories, or multiple aggregated categories. For example, to describe proportions for the three groups: immature males, mature males, and all females (immature and mature females added together) for ages 1 through 4, a total of 12 proportions are required

```
@observation MyProportions
type proportions_at_age
...
categories male_immature male_mature female_immature+female_mature
min_age 1
max_age 4
years 1990
table obs
year 1990 0.05 0.15 0.15 0.05 0.02 0.03 0.08 0.04 0.05 0.15 0.15 0.08
end_table
...
```

Proportions-at-length Functionality for defining combinations of categories and aggregated categories directly translates from proportions-at-age to proportions-at-length. The difference is the observation is over length bins instead of age classes. Casal2 calculates the expected numbers-at-length by converting the numbers-at-age to numbers-at-length by using the age-length relationship and distribution specified for the category specified in the `@age_length` block.

Instead of supplying a minimum and maximum age, the user must supply a vector of length bins. If no length bins are specified, then the observation-specific length bins use the model length bins as the default. If observation-specific length bins are specified, they must be a sequential subset of the model length bins, with no missing or added values. For example, if the model length bins are `0 5 10 15 20 25 ... 100`, then the observation-specific length bins can be `20 25 30 35 40 45 50` but not `20 30 40 50`.

If there is no plus group, i.e., `length_plus=false`, then Casal2 requires a vector of proportions for each year of length $n-1$, where n is the number of lengths supplied. If `length_plus=true` then Casal2 expects a vector of proportions for each year of length n. The last proportion represents the numbers from the last length bin to the maximum length the age-length relationship allows.

```
@observation Observed_Length_frequency_Chat_east
type process_removals_by_length
years 1991 1992
likelihood multinomial
time_step Summer
fishery EastChathamRise
process instant_mort
categories male
length_plus false
length_bins 0 20 40 60 80 110
table obs
1991    0.2   0.25    0.15     0.2     0.2
1992    0.12  0.25    0.28    0.25    0.1
end_table
table error_values
1991 25
1992 37
end_table
```

Proportions-by-category observations Proportions-by-category observations are observations of either the relative number of individuals between categories within age classes, or relative biomass between categories within age classes.

The observation is supplied for a given year and time-step, for selected age classes of the population (i.e., for a range of ages multiplied by a selectivity).

The age range must be ages defined in the partition (i.e., between `@model.min_age` and `@model.max_age` inclusive); the upper end of the age range can optionally be a plus group, which may or may not be the same as the plus group defined for the partition.

Proportions-by-category observations can be supplied for any set of categories as a proportion of themselves and any set of additional categories. For example, for a model with the two categories *male* and *female*, observations of the proportions of males in the population at each age class might be provided. The subcommand `categories` defines the categories for the numerator in the calculation of the proportion, and the subcommand `categories2` supplies the additional categories to be used in the denominator of the calculation. In addition, each category must have an associated selectivity, defined by `selectivities` for the numerator categories and `selectivities2` for the additional categories used in the denominator.

For example,

```
categories male
categories2 female
```

```
selectivities male-selectivity
selectivities2 female-selectivity
```

defines the proportion of males in each age class as a proportion of males + females. Casal2 then requires that there will be a vector of proportions supplied, with one proportion for each age class within the defined age range, i.e., if the age range was 3 to 10, then 8 proportions should be supplied (one proportion for each of the the ages 3, 4, 5, 6, 7, 8, 9, and 10). The expected values will be the expected ratios of male to male + female within each of these age classes, after applying the selectivities at the year and time-step specified.

The observations must be supplied using all or some of the values defined by a categorical layer. Casal2 calculates the expected values by summing over the ages (via the age range and selectivity) and categories for those spatial cells where the categorical layer has the same value as defined for each vector of observations.

For example,

```
@observation MyProportions
type proportions_by_category
years 1990 1991
...
categories male
categories2 female
min_age 1
max_age 5
table obs
1990 0.01 0.05 0.10 0.20 0.20
1991 0.02 0.06 0.10 0.21 0.18
end_table
...
```

Tag Recapture by length Tag data is primarily used to estimate the population abundance of fish. In some models, this estimation can only be made outside the model and the result is used as an estimate of abundance in the model. But in Casal2 the tagging data can, alternatively, be fitted within the model.

Before adding a tag-recapture time series, a tag-release process (Section 5.3.5) needs to be defined. Tagging events list the labels of the tags which are modelled, and define the events where fish are tagged (i.e., Casal2 moves fish into the section of the partition corresponding to a specific tag).

The observations are divided into two parts: (i) the number of fish that were scanned, and (ii) the number of tags that were recaptured. Each number can be specified by categories, or for combinations of categories. The precise content of the scanned and recaptured observations depends on the sampling method.

The available options are:

- age: both the scanned and recaptured are vectors containing numbers-at-age. Only available in an age-based model. The selectivity ogive is redundant and cannot be supplied.
- size: both the scanned and recaptured are vectors containing numbers-at-size. Can be used in either an age- or size-based model. The selectivity ogive is redundant and cannot be supplied.

When defining the tag-recapture time series, the following are also required:

- the time step,
- the years (unlike a tag-release process, the tag-recapture observations can occur over several years),
- the probability that each scanned tagged fish is detected as tagged (may be less than 1 if the observers are not infallible). The expected number of tags detected is calculated by multiplying this number by the number of tagged fish in the sample,
- the tagged category or categories (Make up the recaptures),
- the categories scanned (All the fish sampled for tags),

- A selectivity used in the recapture process,
- the size classes if the observations are size-based in an age-based model.

An example of a tag recapture observation:

```
# For the following partition
@categories
format sex.area.tag
names   male.Area1.2011,notag female.Area1.2011,notag

# individuals tagged in 2011 and recaptured in 2012 in Area1
@observation Tag_2011_Area1_recap_2012
type tag_recapture_by_length
# scanned categories in Area1
categories format=*.Area1.*+
# male and femaled tagged categories
tagged_categories *.Area1.2011+
detection 0.85 ## detection probability
likelihood binomial
selectivities One
tagged_selectivities One
# years to apply observation
years 2012
time_step step2
# proportion of mortality applied before observation is calculated
time_step_proportion 0.5

table scanned
2012 281271 41360 30239 12234
end_table

table recaptured
2012 15 20 12 2
end_table

# robustification value to prevent divide by zero errors
delta 1e-11
# Likelihood dispersion
dispersion 6.3
```

The observed ($O_{y,l}$) and expected ($E_{y,l}$) values in year y and length l of this observation are:

$$O_{y,l} = \frac{R_{y,l}}{S_{y,l}} \tag{7.4}$$

where $R_{y,l}$ is the number of recaptures in year y at length l and $S_{y,l}$ are the scanned values.

$$E_{y,l} = d\frac{\tilde{N}_{y,l,t} + (\tilde{N}_{y,l,t+1} - \tilde{N}_{y,l,t}) \times p}{N_{y,l,t} + (N_{y,l,t+1} - N_{y,l,t}) \times p} \tag{7.5}$$

where $\tilde{N}_{y,l,t}$ is an element in the tagged categories at the beginning of time step t and $\tilde{N}_{y,l,t+1}$ is an element in the tagged categories at the end of time step t, $N_{y,l,t}$ is the sum of the categories that were vulnerable to sampling when the observation occurred, p is the proportion of the time step that the observation was taken, and d is the detection probability.

For observations with multiple tagged categories and multiple categories that were vulnerable to sampling:

$$\tilde{N}_{y,l,t} = \sum_{j=1}^{J} N_{y,l,t,j} \tag{7.6}$$

where $j = \{1,2,3,...,J\}$ are all the tagged categories, the same method is applied to the vulnerable categories to calculate $N_{y,l,t}$. The tagged categories should be defined in the vulnerable categories. In an extreme case where every individual in the population is tagged, this result would be divided by zero. So, to constrain the expectation to be between 0 and 1, the numerator must be in the denominator.

The tag-recapture likelihood (binomial) is specified below. It is a modified version of the more general binomial. Note that this likelihood does not have any user-set precision parameters such as N or $c.v.$, although there are user-specified robustification and dispersion parameters available. The factorials are calculated using the log-gamma function, to allow for non-integer arguments where necessary (and to avoid overflow errors).

7.1.2 General process observations

A list of `types` that are associated with this set of observations:

- `process_abundance`
- `process_biomass`
- `process_proportions_at_age`
- `process_proportions_at_length`
- `process_proportions_by_category`

These observations have the same expectations as the mortality block versions described in Section 5.3.3. With the exception that instead of wrapping a mortality block they can wrap any process type available in Casal2.

7.1.3 Specific process observations

A list of `types` that are associated with this set of observations are:

- `process_removals_by_age`
- `process_removals_by_age_retained`
- `process_removals_by_age_retained_total`
- `process_removals_by_length`
- `process_removals_by_length_retained`
- `process_removals_by_length_retained_total`
- `process_proportions_migrating`

  Process removals by age Removals-at-age observations are observations of the relative number of individuals at age, part way through a process of type `mortality_instantaneous`. This observation is exclusively associated with the process of type `mortality_instantaneous`, and will produce an error if it is associated with any other process type.

  The observation is supplied for a given year and time-step, for selected age classes of the population (i.e., for a range of ages multiplied by a selectivity that is associated with the process).

  The age range must be ages defined in the partition (i.e., between `@model.min_age` and `@model.max_age` inclusive); the upper end of the age range can optionally be a plus group, which must be either the same or less than the plus group defined for the partition.

  The expectations from this observation are generated whilst the process is being executed. The expectation of numbers at age a for category c from exploitation method m ($E[N_{a,c,m}]$) are

$$E[N_{a,c,m}] = N_{a,c}U_{a,m}S_{a,c,m}0.5M_{a,c} \tag{7.7}$$

where $N_{a,c}$ are the numbers-at-age in category c before the process is executed, $U_{a,m}$ is the exploitation rate for age a from method m, $S_{a,c,m}$ is the selectivity, and M is the natural mortality.

The observation class accesses the variable $E[N_{a,c,m}]$ and applies ageing error if the user has specified it. Then the observations are aggregated by method and category depending on how the user specifies the observation, before converting numbers-at-age to proportions-at-age and then calculating the likelihood.

Likelihoods that are available for this observation class are the multinomial, Dirichlet, and the lognormal. See Section 7.2 for information on the respected likelihood.

Process removals by age retained Observations of retained and total catches by age can be included, using the labels `process_removals_by_age_retained` and `process_removals_by_age_retained_total`, respectively. Examples of two such observations are given below, with the associated process `Instantaneous_Mortality_Retained` having the form of the example in Section 5.3.3.

For retained catch:

```
@observation potFishAFtotal
type process_removals_by_age_retained_total
mortality_instantaneous_process Instantaneous_Mortality_Retained
method_of_removal FishingPot
years 2005
time_step 1
categories male
### ageing_error Normal_ageing
min_age 3
max_age 15
plus_group True
table obs
2005 0.00 0.01 0.16 0.27 0.22 0.16 0.11 0.05 0 0 0 0 0
end_table
table error_values
2005 651
end_table
likelihood multinomial
delta 1e-11
```

For total catch:

```
@observation potFishAFretained
type process_removals_by_age_retained
mortality_instantaneous_process Instantaneous_Mortality_Retained
method_of_removal FishingPot
years 2005
time_step 1
categories male
# ageing_error Normal_ageing
min_age 3
max_age 15
plus_group True
table obs
2005 1.65e-10 7.56e-07 1.77e-03 1.96e-01 3.19e-01 2.43e-01 1.60e-01 8.04e-02 0 0 0 0 0
end_table
table error_values
2005 651
end_table
likelihood multinomial
delta 1e-11
```

Process removals by length Removals by length observations are observations of the relative number of individuals at length, part way through a process of type `mortality_instantaneous`. This observation is exclusively associated with the process of type `mortality_instantaneous`, and will produce an error if associated with any other process type.

The observation is supplied for a given year and time-step, for some selected age classes of the population (i.e., for a range of ages multiplied by a selectivity that is associated with the process).

The expectations from this observation are generated whilst the process is being executed. The expectation of numbers at age a for category c from exploitation method m ($E[N_{a,c,m}]$) are

$$E[N_{a,c,m}] = N_{a,c}U_{a,m}S_{a,c,m}0.5M_{a,c} \tag{7.8}$$

where $N_{a,c}$ are the numbers at age in category c before the process is executed, $U_{a,m}$ is the exploitation rate for age a from method m, $S_{a,c,m}$ is the selectivity, and M is the natural mortality.

The observation class accesses the variable $E[N_{a,c,m}]$ from the process and applies the age-length relationship specified in the model. This converts numbers-at-age to numbers-at-age and -length, which are then converted to numbers-at-length. The observations are aggregated by method and category depending on how the user specifies the observation, before converting numbers-at-age to proportions and calculating the likelihood.

Similar to the proportions-at-length observation type, the user must supply a vector of length bins. The observation-specific length bins must be a sequential subset of the model length bins, with no missing or added values. For example, if the model length bins are `0 5 10 15 20 25 ... 100`, then the observation-specific length bins can be `20 25 30 35 40 45 50` but not `20 30 40 50`.

```
@observation observation_fishery_LF
type process_removals_by_length
...
years  1993 1994 1995
method_of_removal FishingEast
mortality_instantaneous_process instant_mort
length_plus false
length_bins 0 20 40 60 80 110
delta 1e-5
table obs
1993    0.0   0.05    0.05    0.10    0.80
1994    0.05  0.1     0.05    0.05    0.75
1995    0.3   0.4     0.2     0.05    0.05
end_table

table error_values
1993 31
1994 34
1995 22
end_table
```

Likelihoods that are available for this observation are the multinomial, Dirichlet and the lognormal. See below for information on the likelihoods.

Process removals by length retained Observations of retained and total catches by length can be included, using the labels `process_removals_by_length_retained` and `process_removals_by_length_retained_total` respectively. Examples of two such observations are given below, with the associated process `Instantaneous_Mortality_Retained` having the form of the example in Section 5.3.3.

Similar to the proportions-at-length observation type, the user must supply a vector of length bins. The observation-specific length bins must be a sequential subset of the model length bins, with no missing or added values. For example, if the model length bins are `0 5 10 15 20 25 ... 100`, then the observation-specific length bins can be `20 25 30 35 40 45 50` but not `20 30 40 50`.

For retained catch:

```
@observation potFishLFtotal   #test syntax get catch LF out
type process_removals_by_length_retained_total
mortality_instantaneous_process Instantaneous_Mortality_Retained
method_of_removal FishingPot
years 2005
time_step 1
categories male
length_bins 30 31 32 33 34 35 36 37 38 39 40 41 42 43 44 45 46 # for LF in catch
length_plus False
table obs
2005 0.05 0.06 0.07 0.08 0.08 0.08 0.08 0.08 0.07 0.06 0.06 0.05 0.04 0.030 0.02 0.02
end_table
table error_values
2005 651
end_table
likelihood multinomial
delta 1e-11
```

For total catch:

```
@observation potFishLFretained   #test syntax get retained LF out
type process_removals_by_length_retained
mortality_instantaneous_process Instantaneous_Mortality_Retained
method_of_removal FishingPot
years 2005
time_step 1
categories male
length_bins 30 31 32 33 34 35 36 37 38 39 40 41 42 43 44 45 46 # for LF in catch
length_plus False
table obs
2005 0.02 0.03 0.04 0.06 0.07 0.08 0.08 0.09 0.08 0.08 0.07 0.06 0.05 0.04 0.03 0.02
end_table
table error_values
2005 651
end_table
likelihood multinomial
delta 1e-11
```

Proportions migrating This observation is of the proportion migrating from one area to another. This observation is exclusively associated with the process type `transition_category`, and will produce an error when associated with any other process type. This observation is used to inform migration rates in migration processes. This observation class is used in the hoki stock assessment see Francis et al. (2003) for more information on how these observations are collected and a situation that uses it.

This observation calculates an expectation E_a of proportions for each age class a that have migrated, by

$$E_a = \frac{N_a - N'_a}{N_a} \tag{7.9}$$

where N_a are the numbers of individuals in age a before the migration process occurs, and N'_a are the number of individuals after the migration process occurs.

The likelihoods that are allowed for this observation are the lognormal, multinomial, and Dirichlet.

A section of the hoki stock assessment model:

```
@observation pspawn_1993
type process_proportions_migrating
years 1993
time_step step4
process Wspmg ## migration process that the observation is associated with
age_plus true
min_age 4
max_age 9
likelihood lognormal
categories male.west+female.west ## Categories to evaluate the prportion for
ageing_error Normal_offset ## label for an @ageing_error block
table obs
#age    4    5    6    7    8    9
1993 0.64 0.58 0.65 0.66 0.71 0.60
end_table

table error_values
## if lognormal these are c.v.'s
1993 0.25
end_table
```

7.2 Likelihoods

7.2.1 Likelihoods for proportions-at-age observations

Casal2 implements three likelihoods for proportions-at-age observations, the multinomial likelihood, the Dirichlet, and the lognormal likelihood.

The multinomial likelihood

For the observed proportions at age O_i for age classes i, with sample size N, and the expected proportions at the same age classes E_i, the negative log-likelihood is:

$$-\log(L) = -\log(N!) + \sum_i \log((NO_i)!) - NO_i \log(Z(E_i, \delta)) \tag{7.10}$$

where $\sum_i O_i = 1$ and $\sum_i E_i = 1$. $Z(\theta, \delta)$ is a robustifying function to prevent division by zero errors, with parameter $\delta > 0$.

$$Z(\theta, \delta) = \begin{cases} \theta, & \text{where } \theta \geq r \\ \delta/(2 - \theta/\delta), & \text{otherwise} \end{cases} \tag{7.11}$$

The default value of δ is 1×10^{-11}.

The Dirichlet likelihood

For the observed proportions at age O_i for age classes i, with sample size N, and the expected proportions at the same age classes E_i, the negative log-likelihood is:

$$-\log(L) = -\log(\Gamma \sum_i (\alpha_i)) + \sum_i \log(\Gamma(\alpha_i)) - \sum_i (\alpha_i - 1) \log(Z(O_i, \delta)) \tag{7.12}$$

where $\alpha_i = Z(NE_i, \delta)$, $\sum_i O_i = 1$, and $\sum_i E_i = 1$. $Z(\theta, \delta)$ is a robustifying function to prevent division by zero

errors, with parameter $\delta > 0$.

$$Z(\theta,\delta) = \begin{cases} \theta, & \text{where } \theta \geq r \\ \delta/(2-\theta/\delta), & \text{otherwise} \end{cases} \tag{7.13}$$

The default value of δ is 1×10^{-11}.

The lognormal likelihood

For the observed proportions at age O_i for age classes i, with c.v. c_i, and the expected proportions at the same age classes E_i, the negative log-likelihood is defined as;

$$-\log(L) = \sum_i \left(\log(\sigma_i) + 0.5 \left(\frac{\log(O_i/Z(E_i,\delta))}{\sigma_i} + 0.5\sigma_i \right)^2 \right) \tag{7.14}$$

where

$$\sigma_i = \sqrt{\log\left(1+c_i^2\right)} \tag{7.15}$$

and the c_i's are the c.v.s for each age class i, and $Z(\theta,\delta)$ is a robustifying function to prevent division by zero errors, with parameter $\delta > 0$.

$$Z(\theta,\delta) = \begin{cases} \theta, & \text{where } \theta \geq r \\ \delta/(2-\theta/\delta), & \text{otherwise} \end{cases} \tag{7.16}$$

The default value of δ is 1×10^{-11}.

7.2.2 Likelihoods for abundance and biomass observations

Abundance and biomass observations are expected as an annual time series in Casal2, where they select the same categories over that time series. The parameters and inputs needed to use this observation class are: a observation O_i, c.v. c_i, catchability coefficient q, where i indexed the year. Casal2 calculates an expectation E_i and scales it by q before comparing it to O_i. This means that the value chosen for q will determine whether the observation is relative ($q \neq 1$) or absolute $q = 1$. Before we describe each of the likelihoods we will discuss the methods available to handle qs:

- The qs can be treated as 'nuisance' parameters. For each set of values of the free parameters, the model uses the values of the qs which minimise the objective function. These optimal qs are calculated algebraically (see Section 7.4). If one of the qs falls outside the bounds specified by the user, it is set equal to the closest bound. This approach reduces the size of the parameter vector and hence should improve the performance of the estimation method. However, it is not correct when calculating a sample from the posterior in a Bayesian analysis (except asymptotically, see Walters and Ludwig (1994)) and we offer the following alternative;
- The qs can be treated as ordinary free parameters.

For both options, it is necessary to evaluate the contribution of O_i to the negative log likelihood for a given value of q. Each observation O_i varies about qE_i, which expresses the variability of O_i in terms of its c.v. c_i (or in one case, its standard deviation si). Here are the likelihoods, which are expressed on the objective-function scale of -log(L):

The lognormal likelihood

The negative log likelihood for the lognormal is

$$-\log(L) = \sum_i \left(\log(\sigma_i) + 0.5 \left(\frac{\log(O_i / qZ(E_i, \delta))}{\sigma_i} + 0.5\sigma_i \right)^2 \right) \tag{7.17}$$

where

$$\sigma_i = \sqrt{\log\left(1 + c_i^2\right)} \tag{7.18}$$

and $Z(\theta, \delta)$ is a robustifying function to prevent division by zero errors, with parameter $\delta > 0$.

$$Z(\theta, \delta) = \begin{cases} \theta, & \text{where } \theta \geq r \\ \delta / (2 - \theta/\delta), & \text{otherwise} \end{cases} \tag{7.19}$$

The default value of δ is 1×10^{-11}.

This formulation reflects the distributional assumptions that O_i has the lognormal distribution, that the mean of O_i is qE_i and the c.v. of O_i is c_i.

The normal likelihood

For observations O_i, c.v. c_i, and expected values qE_i, the negative log-likelihood is defined as;

$$-\log(L) = \sum_i \left(\log(c_i E_i) + 0.5 \left(\frac{O_i - E_i}{Z(c_i E_i, \delta)} \right)^2 \right) \tag{7.20}$$

and $Z(\theta, \delta)$ is a robustifying function to prevent division by zero errors, with parameter $\delta > 0$.

$$Z(\theta, \delta) = \begin{cases} \theta, & \text{where } \theta \geq r \\ \delta / (2 - \theta/\delta), & \text{otherwise} \end{cases} \tag{7.21}$$

The default value of δ is 1×10^{-11}.

This reflects the distributional assumptions that O_i has the normal distribution, that the mean of O_i is qE_i and the c.v. of O_i is c_i.

7.2.3 Likelihoods for tag recapture by age and length observations

The binomial likelihood This likelihood is for situations where the size frequencies or age frequencies of the recaptured tagged fish and of the scanned fish are known. Available in both age or size based models.

The likelihood is defined as a binomial, but based on sizes, rather than ages

$$\begin{aligned} -\log(L)' = -\sum_i [& \log(n_i!) - \log((n_i - m_i)!) - \log((m_i)!) + m_i \log\left(Z\left(\frac{M_i}{N_i}, \delta \right) \right) \\ & + (n_i - m_i) \log\left(Z\left(1 - \frac{M_i}{N_i}, \delta \right) \right)] \end{aligned} \tag{7.22}$$

where

n_i = number of fish at size or age i that were scanned

m_i = number of fish at size or age i that were recaptured

N_i = number of fish at size or age i in the available population (tagged and untagged)

M_i = number of fish at size or age i in the available population that have the tag after a detection probability p_d has been applied, $M_i = M_i' p_d$, where M_i' is the expected available population that have the tag.

$Z(x,\delta)$ is a robustifying function with parameter $r > 0$ (to prevent division by zero errors).

$$Z(x,\delta) = \begin{cases} x & \text{where } x \geq \delta \\ \frac{\delta}{(2-x/\delta)} & \text{otherwise} \end{cases}$$

If a dispersion parameter (τ) is described in the observation then the final negative log likelihood $-log(L)$ contribution is

$$-log(L) = -log(L)'/\tau$$

7.2.4 Likelihoods for proportions-by-category observations

Casal2 implements two likelihoods for proportions-by-category observations, the binomial likelihood, and the normal approximation to the binomial (binomial-approx).

The binomial likelihood

For observed proportions O_i for age class i, where E_i are the expected proportions for age class i, and N_i is the effective sample size for age class i, then the negative log-likelihood is

$$\begin{aligned} -\log(L) = -\sum_i [\, & \log(N_i!) - \log((N_i(1-O_i))!) - \log((N_i O_i)!) + N_i O_i \log(Z(E_i,\delta)) \\ & + N_i(1-O_i)\log(Z(1-E_i,\delta))\,] \end{aligned} \tag{7.23}$$

where $Z(\theta,\delta)$ is a robustifying function to prevent division by zero errors, with parameter $\delta > 0$.

$$Z(\theta,\delta) = \begin{cases} \theta, & \text{where } \theta \geq r \\ \delta/(2-\theta/\delta), & \text{otherwise} \end{cases} \tag{7.24}$$

The default value of δ is 1×10^{-11}.

The normal approximation to the binomial likelihood

For observed proportions O_i for age class i, where E_i are the expected proportions for age class i, and N_i is the effective sample size for age class i, then the negative log-likelihood is defined as;

$$-\log(L) = \sum_i \log\left(\sqrt{Z(E_i,\delta)Z(1-E_i,\delta)/N_i}\right) + \frac{1}{2}\left(\frac{O_i - E_i}{\sqrt{Z(E_i,\delta)Z(1-E_i,\delta)/N_i}}\right)^2 \tag{7.25}$$

where $Z(\theta,\delta)$ is a robustifying function to prevent division by zero errors, with parameter $\delta > 0$.

$$Z(\theta,\delta) = \begin{cases} \theta, & \text{where } \theta \geq r \\ \delta/(2-\theta/\delta), & \text{otherwise} \end{cases} \tag{7.26}$$

The default value of δ is 1×10^{-11}.

7.3 Process error

Additional 'process error' can be defined for any set of observations. Additional process error has the effect of increasing the observation error in the data, and hence of decreasing the relative weight given to the data in the fitting process.

For observations where the likelihood is parameterised by the c.v., the process error can be specified for a given set of observations as a c.v., in which case all the c.v.s c_i are changed to

$$c_i' = \sqrt{c_i^2 + c_{process\_error}^2} \tag{7.27}$$

Note that $c_{process\_error} \geq 0$, and that $c_{process\_error} = 0$ is equivalent to no process error.

Similarly, if the likelihood is parameterised by the effective sample size N,

$$N_i' = \frac{1}{1/N_i + 1/N_{process\_error}} \tag{7.28}$$

Note that this requires that $N_{process\_error} > 0$, but the special case of $N_{process\_error} = 0$ is valid, and $N_{process\_error} = 0$ represents no process error (i.e., defined to be equivalent to $N_{process\_error} = \infty$).

For both the c.v. and N process errors, the process error has more effect on small errors than on large ones. Note that a large value for the N process error means a small process error.

7.4 Calculating nuisance q parameters

This section describes the theory used to calculate nuisance (analytical) catchability coefficients qs (see Section 7.2.2). From the user's point of view, the essence is that you can use nuisance qs in the following situations:

- With maximum likelihood estimation
- With Bayesian estimation, providing that the additional prior on q is one of the following:
  - None (default)
  - Uniform-log
  - Lognormal with observations distributed lognormal, robustified lognormal

The scenarios in which the nuisance catchability q can be used in a Bayesian analysis (Table 7.1):

Table 7.1: Equations used to calculate nuisance qs. (*=no analytic solution found.)

Distribution	Maximum Likelihood	None	Uniform-log	Normal	lognormal
Normal	(7.29)	(7.29)	(7.31)	*	*
Lognormal	(7.32)	(7.32)	(7.36)	*	(7.37)

Note that qs are calculated for robustified lognormal likelihoods as if they were ordinary lognormal likelihoods.

Let $\sigma_i = \sqrt{log(1+c_i^2)}$ throughout, and let n be the number of observations in the time series. The case of multiple time series sharing the same q, and the modifications required for the assumption of curvature, are addressed at the end of this subsection.

First, consider maximum likelihood estimation. When the (Oi) are assumed to be normally distributed

$$-log(L) = \sum_i log(c_i q E_i) + 0.5 \sum_i \left(\frac{O_i - qE_i}{c_i q E_i} \right)^2 \tag{7.29}$$

The value of q which minimises the objective function is found by solving for q under the following condition, $\partial/\partial q(-log(L)) = 0$

$$\frac{\partial}{\partial q}(-log(L)) = \frac{n}{q} + \frac{1}{q^2}\sum_i \frac{O_i}{c_i^2 E_i} - \frac{1}{q^3}\sum_i \left(\frac{O_i}{c_i E_i}\right)^2 \tag{7.30}$$

hence

$$\hat{q} = \frac{-S_1 + \sqrt{S_1^2 + 4nS_2}}{2n} \tag{7.31}$$

where $S_1 = \sum_i (O_i/c_i^2 E_i)$ and $S_2 = \sum_i (O_i/c_i E_i)^2$

When the (O_i) are assumed to be lognormally distributed,

$$-log(L) = \sum_i log(\sigma_i) + 0.5\sum_i \left(\frac{log(O_i) - log(qE_i) + 0.5\sigma_i^2}{\sigma_i}\right)^2 \tag{7.32}$$

$$\frac{\partial}{\partial q}(-log(L)) = \frac{-1}{q}\sum_i \left(\frac{log(O_i/E_i) - log(q) + 0.5\sigma_i^2}{\sigma_i^2}\right) \tag{7.33}$$

$$\hat{q} = exp\frac{0.5n + S_3}{S_4} \tag{7.34}$$

where $S_3 = \sum_i (log(O_i/E_I)/\sigma_i^2)$ and $S_4 = \sum_i (1/\sigma_i^2)$.

Next, consider Bayesian estimation, where a prior for q must be specified.

The effects of the prior on the equations are to replace likelihood L by posterior P throughout, to add $-log(\pi(q))$ to the equation for $-log(P)$ and $\partial/\partial q(-log(-\pi(q)))$ to the equation for $\partial/\partial q(-log(P))$

This last term is 0 for a uniform prior on q, $1/q$ for a log-uniform prior, and $\frac{1}{q}\left(1.5 + \frac{log(q) - log(\mu_q)}{\sigma_q^2}\right.$ for a lognormal prior, where μ_q and c_q are the mean and c.v. of the prior on q, respectively, and $\sigma_q = \sqrt{log(1+c_q^2)}$. Since the prior is uniform, the equation for $\hat{q}$ is the same as the maximum likelihood estimation.

When the (O_i) are assumed to be normally distributed and the prior is log-uniform equation (7.31) becomes,

$$\hat{q} = \frac{-S_1 + \sqrt{S_1^2 + 4(n+1)S_2}}{2(n+1)} \tag{7.35}$$

but $\hat{q}$ with either a normal or lognormal prior cannot be solved for.

When the O_i are assumed to be lognormally distributed and the prior is log-uniform, equation (7.34) becomes

$$\hat{q} = exp\frac{0.5n - 1 + S_3}{S_4} \tag{7.36}$$

and if the prior is lognormal,

$$\hat{q} = exp\frac{0.5n - 1.5 + log(\mu_q)/\sigma_q^2 + S_3}{S_4 + 1/\sigma_q^2} \tag{7.37}$$

However, it is not possible to solve for $\hat{q}$ with a normal prior.

An example of specifying the syntax and an equivalent additional prior

```
@catchability chatTANq
type nuisance
upper_bound 0.6
lower_bound 0.0001

@additional_prior chatTANq_prior
type lognormal
parameter catchabilityp[chatTANq].q
mu 0.3
cv 0.2
```

7.5 Ageing error

Casal2 can apply ageing error to expected age frequencies estimated by the model. The ageing error is applied as a misclassification matrix, which has the effect of 'smearing' the expected age frequencies. This is mimicking the error involved in identifying the age of individuals. For example, fish species are aged by reading the ear bones (otoliths) which can be quite difficult depending on the species. These age frequencies are used in calculating the fits to the observed values, and hence the contribution to the total objective function.

Ageing error is optional, and if it is used, it may be omitted for any individual time series. Different ageing error models may be applied for different observation commands. See Section 11.3 for reporting the misclassification matrix at the end of model run.

The ageing error models implemented are

- None: The default model is to apply no ageing error.
- Off by one: Proportion p_1 of individuals of each age a are misclassified as age $a-1$ and proportion p_2 are misclassified as age $a+1$. Individuals of age $a < k$ are not misclassified. If there is no plus group in the population model, then proportion p_2 of the oldest age class will 'fall off the edge and disappear'.
- Normal: Individuals of age a are classified as ages which are normally distributed with mean a and constant c.v. c. As above, if there is no plus group in the population model, some individuals of the older age classes may disappear. If c is high enough, some of the younger age classes may 'fall off the other edge'. Individuals of age $a < k$ are not misclassified.
- Data: A matrix that defines the misclassification matrix for ageing error.

The expected values (fits) reported by Casal2 for observations with ageing error will have had the ageing error applied.

7.6 Simulating observations

Casal2 can generate simulated observations for a given model with a set of parameter values using `casal2 -s` n to simulate n sets of observations). Simulated observations are randomly generated values, which are generated with the error distributions defined for each observation, around fits calculated from one or more sets of the 'true' parameter values. Simulating from a set of parameters can be used to generate observations from an operating model or as a form of parametric bootstrap.

The procedure Casal2 uses for simulating observations is to use the 'true' parameter values which are fed via the `-i`/`-I` file input which generate expected values. Then, if a set of observations use ageing error, ageing error is applied. Finally, a random value for each observed value is generated based on (i) the expected values, (ii) the type of likelihood specified, and (iii) the variability parameters (e.g., `error_value` and `process_error`).

Methods for generating the random error, and hence the simulated values, have three components which the user can change. These are the (i) the likelihood choice and observation error, (ii) parameter uncertainty through the use of `-i`/`-I`, and (iii) time-varying parameters.

- Normal likelihood parameterised by c.v.: Let E_i be the fitted value for observation i, and c_i be the corresponding c.v. (adjusted by the process error if applicable). Each simulated observation value S_i is generated as an independent normal deviate with mean E_i and standard deviation $E_i c_i$.
- Log-normal likelihood: Let E_i be the fitted value for observation i and c_i be the corresponding c.v. (adjusted by the process error if applicable). Each simulated observation value S_i is generated as an independent lognormal deviate with mean and standard deviation (on the natural scale, not the log-scale) of E_i and $E_i c_i$ respectively. The robustification parameter δ is ignored.
- Multinomial likelihood: Let E_i be the fitted value for observation i, for i between 1 and n, and let N be the sample size (adjusted by process error if applicable, and then rounded up to the next whole number). The robustification parameter δ is ignored. Then,
  1. A sample of N values from 1 to n is generated using the multinomial distribution, using sample probabilities proportional to the values of E_i.
  2. Each simulated observation value S_i is calculated as the proportion of the N sampled values equalling i
  3. The simulated observation values S_i are then rescaled so that their sum is equal to 1
- Binomial and the normal approximation to the binomial likelihoods: Let E_i be the fitted value for observation i, for i between 1 and n, and N_i the corresponding equivalent sample size (adjusted by process error if applicable, and then rounded up to the next whole number). The robustification parameter δ is ignored. Then,
  1. A sample of N_i independent binary variates is generated, equalling 1 with probability E_i
  2. The simulated observation value S_i is calculated as the sum of these binary variates divided by N_i

An important note when simulating: Casal2 will **not** automatically report simulated observations when using a `casal2 -s 1 -i input_pars.out` run. A report must be defined using the `simulated_observation` report (`@report[label].type=observation`). For completeness the report is described along with some best practices here, but there is additional information in Section 8.

A typical report for simulating an observation looks like

```
@report CPUE_index_sim # report label
type simulated_observation # report tyoe
observation CPUEandes # observation to simulate
file_name sim/CPUEandes # file to write simualted data to
```

note that in the subcommand `file_name` there is a directory component `sim`. It is recommended when doing simulations that you create directories that can be documented on what configurations caused that set of simulated datasets. This will become useful if you are looking at multiple simulated models assumptions.

Simulated reports will be produced with the following extension `.1_1`. The first number of the extension relates to the row of the `-i`/`-I` file and the second number (separated by `_`) represents the simulation iteration defined by the `n` argument in the configuration input `casal2 -s n`. Examples of the extension follow,

- `.1_1` indicates simulated data produced from the first row of parameters and is the first random draw
- `.1_2` indicates simulated data produced from the first row of parameters and is the second random draw
- `.2_10` indicates simulated data produced from the second row of parameters and is the 10^{th} random draw

7.7 Pseudo-observations

Casal2 can generate expected values for observations without them contributing to the total objective function. These are called pseudo-observations, and can be used to either generate the expected values from Casal2 for reporting or diagnostic purposes. To define an observation as a pseudo-observation, use the command `@observation[label].likelihood=none`. Any observation type can be used as a pseudo-observation. Casal2 can also generate simulated observations from pseudo-observations. Note that

- Output will be generated only if a report command `@report[label].type=observation` is specified.
- The observed values should be supplied (even if they are 'dummy' observations). These observation values will be processed by Casal2 as if they were actual observation values, and must be in the same format as actual observation values.
- The subcommands `likelihood`, `obs`, `error_value`, and `process_error` have no effect when generating the expected values for the pseudo-observation.
- When simulating observations, the subcommand `simulation_likelihood` to indicate the likelihood to use. In this case, the `obs`, `error_value`, and `process_error` are used to determine the appropriate terms to use for the likelihood when simulating.

7.8 Residuals

Casal2 will print the default residual values (i.e., observed less fitted) only when the report type `@report.type=observation` is used. For an observation O and F the corresponding fit (=qE for relative observations), then

- Residuals = O - F

Pearson and normalised residuals can be generated using the Casal2 **R** package. For specific **R** functions see Section 17.

The definitions used in the calculations are

- *Pearson residuals* attempt to express the residual relative to the variability of the observation, and are defined as (O-F)/std.dev.(O), where std.dev.(O) is calculated as
  - F $\times$ cv for normal, lognormal, robustified lognormal, and normal-log error distributions.
  - s for normal-by-standard deviation error distributions.
  - $\sqrt{\frac{Z(F,r)(1-Z(F,r))}{N}}$ for multinomial or binomial likelihoods.
  - $\sqrt{\frac{(F+r)(1-F+r)}{N}}$ for binomial-approx likelihood likelihoods.
- *Normalised residuals* to express the residual on a standard normal scale, and are defined as:
  - Equal to the Pearson residuals for normal error distributions.
  - (log(O/F)+0.5σ^2)/σ for lognormal (including robustified lognormal) error distributions, where $\sigma = \sqrt{log(1+cv^2)}$.
  - log(O/F)/σ for normal-log error distributions, again with $\sigma = \sqrt{log(1+cv^2)}$.
  - And are otherwise undefined.

where $Z(F,r)$ is the robustifying term on F (fit or expectation of the observation). This robustifying function is described earlier in the likelihood section.

8 The report section: output and reports

The command and subcommand syntax for the estimation section is given in Section 12.1.

The report section specifies the printouts and other output from the model. Casal2 does not, in general, produce any output unless specified by a valid `@report` block.

8.1 Report command block format

Reports from Casal2 can be defined to print partition and states objects at a particular point in time, observation summaries, estimated and derived parameter values, and objective function values.

```
@report observation_age ## label of report
type observation     ## Type of report
observation age_1990  ## label corresponding to an @observation report, shown below

@observation age_1990
type proportion_at_age
year 1990
plus_group
etc., ...
```

8.2 Report output format

Reports from Casal2 have a standard style (with the exception of `output_parameters` and `simulated_observation`, see below). The standard style is that reports are prefixed with an asterisk followed by a user-defined label and type of report in brackets (e.g., `*label (type)`), with the report ending with the line `*end`. For example,

```
*My_report(type)
...
... # report content
...
*end
```

This report block output format should make it easier for other software packages to read and process Casal2 output. The `extract` functions in the **R** Casal2 package use this information to identify and read Casal2 output.

The `output_parameters` report does not print either a header or `*end` at the end of the report block. This is because the `output_parameters` report is designed to provide a single line vector of the estimated parameter values, or multiple lines for more than one set, which can be read by Casal2 with the command `casal2 -i`. This is a specialised report for the `casal2 -o filename` command.

For estimated values in standard output use the `type=estimate_value` report.

Reports can be defined in a `@report` command block but may not be output, e.g., a report to print the partition for a year and/or time step that does not exist, or reporting the covariance matrix when not estimation run mode.

Certain reports are associated with certain Casal2 run modes. These reports are ignored by Casal2 and the program will not generate any output for these reports, although they must still conform to Casal2 syntax requirements.

Not all reports will be generated in all run modes. Some reports are only available in some run modes. For example, when simulating, only the simulation reports will be output.

8.3 Print default reports

This is a report type that generates a range of other default reports, The report queries model and generates default reports for all catchabilities, observations, processes, selectivities, derived parameters, and projections.

This report will print out in run modes `-r, -e, -f`.

8.4 Print the partition at the end of an initialisation

This report prints the partition following the initialisation phase, which includes the numbers of individuals in each age class and category in the partition. This report will print out in run modes `-r, -e, -f`.

8.5 Print the partition

This report prints the numbers of individuals in each age class and category in the partition for each given year or given years and time step. This report is evaluated at the end of the time step in the given year(s). This report will print out in run modes `-r, -e, -f`.

8.6 Print the partition biomass

This report prints the biomass in each age class and category in the partition for each given year or given years and time step. This report is evaluated at the end of the time step in the given year(s). This report will print out in run modes `-r, -e, -f`.

8.7 Print the age length and length weight values

This report prints the length and weight value for each age class and category in the partition for each given year or given years and time step. This report is evaluated at the end of the time step in the given year(s). This report will print out in run modes `-r, -e, -f`.

```
@report length_weight_at_age
type partition_mean_weight
time_step step2
years 1900:2013
```

8.8 Print a process summary

Depending on the process, different summaries are produced. These reports typically detail the type of process, its parameters and other options, and any associated details. This report will print out in run modes `-r, -e, -f`.

8.9 Print derived quantities

This report prints the description of the derived quantity, and the values of the derived quantity as recorded in the model state, for each year of the model, and for all years in the initialisation phase. This report will print out in run modes `-r, -e, -f`.

8.10 Print the estimated parameters

This report prints a summary of the estimated parameters using the type `estimate_summary`, including the parameter name, lower and upper bounds, the label of the prior, and its value. This report will print out in run modes `-r, -e`.

8.11 Print the MPD (the free parameters and covariance matrix)

This report prints the estimated parameter values out as a vector along with the covariance matrix. The `MPD` report prints these in a format suitable for use as the starting point for an MCMC. This report will print out in run modes `-r, -e`.

8.12 Print the estimate values (the free parameters in the free parameter file format)

This report prints the estimated parameter values out as a vector. The `estimate_values` report prints the name of the parameter, followed by the value for that run. This report will print out in run modes `-r, -e`.

8.13 Print the objective function

This report prints the total objective function value, the value of all observation likelihood components, the values of all priors, and the value of any penalties that have been incurred. If an individual model run does not incur a penalty, then the penalty will not be reported. This report will print out in run modes `-r, -e, -f`.

8.14 Print the covariance matrix

This report prints the covariance matrix if in estimation run mode and if the covariance has been requested by `@minimiser[label].covariance=true`.

8.15 Print the correlation matrix

This report prints the correlation matrix if in estimation run mode and if the covariance has been requested by `@minimiser[label].covariance=true`.

8.16 Print the Hessian matrix

This report prints the Hessian matrix if in estimation run mode and if the covariance has been requested by `@minimiser[label].covariance=true`.

8.17 Print the catchability values

This report prints the catchability for a requested catchability.

8.18 Print observations, fits, and residuals

This report prints, for each category or combination of categories, the expected values, residuals (observed − expected), the error value, process error, the total error (i.e., the error value as modified by any additional process error), and the contribution to the total objective function of that individual datum in the observation.

Constants in the likelihood components are often ignored in the objective function score of individual observation values. Hence, the total score from an observation equals the contribution of the objective function scores from each individual observation value plus a constant term (if applicable). In likelihood components without a constant term, the total score from an observation will equal the contribution of the objective function scores from each individual observation value.

If Casal2 is in simulation run mode, then the contribution to the objective function of each observation is reported as zero.

```
@report Tan_at_age_obs
type observation
observation TAN_AT_AGE
```

8.19 Print simulated observations

This report prints a complete set of observation values in the form specified by `@report[label].type=observation`, with observed values replaced by randomly generated simulated values. The output is in a form suitable for use within a Casal2 input configuration file, reproducing the command and subcommands from the input configuration file. This report will print out in run mode `-s`.

8.20 Print the ageing error misclassification matrix

This report prints the ageing error misclassification matrix used to offset observations within during model the model fitting procedure.

8.21 Print selectivities

This report prints the values of a selectivity for each age in the partition, for a given year and at then end of a given time step.

8.22 Print the random number seed

This report prints the random number seed used by Casal2 to initialise the generated random number sequence. Additional runs which use the same random number seed and the same model will produce identical outputs.

8.23 Print the results of an MCMC

This report prints the MCMC samples, objective function values, and proposal covariance matrix following an MCMC. This report will print out in run mode `-m`.

8.24 Print the MCMC samples as they are calculated

This report prints the MCMC samples for each new *i*th sample as they are calculated while doing an MCMC. The output file will be appended with each new sample as it is calculated by Casal2. This report will print out in run mode `-m`.

8.25 Print the MCMC objective function values as they are calculated

This report prints the MCMC objective function values, along with the proposal covariance matrix, for each new *i*th sample as they are calculated while doing an MCMC. The output file will be appended with each new set of objective function values as it is calculated by Casal2. This report will print out in run mode `-m`.

8.26 Print time varying parameters

This report prints all `@time_varying` blocks with the values and years in which they were specified. This report will print out in run modes `-r, -e, -m`.

```
@report time_varying_parameters
type time_varying
```

8.27 Tabular reporting format

An alternative reporting framework to the standard output is the tabular reporting format. Tabular reporting is used with multi-line `-i` input files (like the MCMC sample or `-o` outputs). Tabular reports will print out a row that will correspond with each row of the `-i` input files.

Tabular reporting is specified using the `--tabular` argument (`casal2 -r --tabular -i file_name`).

Derived quantities, processes, observations, and `estimate_values` are the only report types that can be output with this format. For each input file the output will begin with the names of each column followed by a multi-line report ending with the `*end` syntax.

These tables can be read with **R** using the Casal2 **R** package. An example usage is reading in files of MCMC posterior values of derived quantities, which can then be plotted.

9 Population command and subcommand syntax

The description of the methods for the population section is given in Section 5.

In the following section, the sub-section headers use a notation of the form "**@observation[label].type=abundance**" which, in this case, represents the input command fragment

```
@observation label # where label is a unique label for that observation
type=abundance
...
```

The specific subcommands for a command are given within each command.

9.1 Model structure

`@Model` *`label`* Define an object of type *Model*. See Section 5.2 for more information.

`type` Type of model (only type=age is currently implemented)
Type: String
Default: age

`base_weight_units` Define the units for the base weight measurement unit (grams, kilograms (kgs), or tonnes). This will be the default unit of any weight input values
Type: String
Default: tonnes

`threads` The number of threads to use for this model
Type: Non-negative integer
Default: 1
Lower Bound: 1 (inclusive)

9.1.1 Model of type Age

`@Model[label].type=Age`.

`start_year` Define the first year of the model, immediately following initialisation
Type: Non-negative integer
Default: No default
Value: Defines the first year of the model, must be ≥ 1000, e.g. 1990

`final_year` Define the final year of the model, excluding years in the projection period
Type: Non-negative integer
Default: No default
Value: Defines the last year of the model, i.e., the model is run from start_year to final_year

`min_age` Minimum age of individuals in the population
Type: Non-negative integer
Default: 0
Value: $0 \leq \text{age}_{\text{min}} \leq \text{age}_{\text{max}}$

`max_age` Maximum age of individuals in the population

Type: Non-negative integer
Default: 0
Value: $0 \leq \text{age}_{\text{min}} \leq \text{age}_{\text{max}}$

`age_plus` Define the oldest age or extra length midpoint (plus group size) as a plus group
Type: Boolean
Default: true
Value: true, false

`initialisation_phases` Define the labels of the phases of the initialisation
Type: Vector of strings
Default: true
Value: A list of valid labels defined by `@initialisation_phase`

`time_steps` Define the labels of the time steps, in the order that they are applied, to form the annual cycle
Type: Vector of strings
Default: No default
Value: A list of valid labels defined by `@time_step`

`projection_final_year` Define the final year of the model when running projections
Type: Non-negative integer
Default: 0
Value: A value greater than final_year

`length_bins` The minimum length in each length bin
Type: Vector of real numbers (estimable)
Default: true
Value: $0 \leq \text{length}_{\text{min}} \leq \text{length}_{\text{max}}$

`length_plus` Specify whether there is a length plus group or not
Type: Boolean
Default: true
Value: true, false

`length_plus_group` Mean length of length plus group
Type: Real number (estimable)
Default: 0
Value: $\text{length}_{\text{max}} <$ length_plus_group

9.2 Initialisation

`@Initialisation_Phase` *`label`* Define an object of type *Initialisation_Phase*. See Section 5.2.2 for more information.

`label` The label of the initialisation phase

Type: String
Default: No default

`type` The type of initialisation
Type: String
Default: iterative

9.2.1 Initialisation_Phase of type Cinitial

`@Initialisation_Phase[label].type=Cinitial`. See Section 5.2.2 for more information.

`categories` The list of categories for the Cinitial initialisation
Type: Vector of strings
Default: No default

`table` The table of data specifying the initial values by age
Type: Data table with label = n
Default: No default
Value: A *nxm* matrix, where n = the categories and m = the number of ages defined in the model. Rows of values specify the initial value of the partition. The table ends with 'end_table'
Note: See 16.2 for more details on specifying data tables

9.2.2 Initialisation_Phase of type Derived

`@Initialisation_Phase[label].type=Derived`. See Section 5.2.2 for more information.

`insert_processes` Specifies the additional processes that are not in the annual cycle, but should be be inserted into this initialisation phase
Type: Vector of strings
Default: true

`exclude_processes` Specifies the processes in the annual cycle that should be excluded from this initialisation phase
Type: Vector of strings
Default: true

`casal_initialisation_switch` Run an extra annual cycle to evaluate equilibrium SSBs. Warning: if true, this may not correctly evaluate the equilibrium state. Set to true if replicating a CASAL model
Type: Boolean
Default: false

9.2.3 Initialisation_Phase of type Iterative

`@Initialisation_Phase[label].type=Iterative`. See Section 5.2.2 for more information.

`years` The number of iterations (years) over which to execute this initialisation phase
Type: Non-negative integer
Default: No default

`insert_processes` The processes in the annual cycle to be include in this initialisation phase
Type: Vector of strings
Default: true

`exclude_processes` The processes in the annual cycle to be excluded from this initialisation phase
Type: Vector of strings
Default: true

`convergence_years` The iteration (year) when the test for convergence (λ) is evaluated
Type: Vector of non-negative integers
Default: true

`lambda` The maximum value of the absolute sum of differences (lambda) between the partition at year-1 and year that indicates successful convergence
Type: Real number
Default: 0.0

9.2.4 Initialisation_Phase of type State_Category_By_Age

`@Initialisation_Phase[label].type=State_Category_By_Age`. See Section 5.2.2 for more information.

`categories` The list of categories for the category state initialisation
Type: Vector of strings
Default: No default

`min_age` The minimum age of values supplied in the definition of the category state
Type: Non-negative integer
Default: No default

`max_age` The maximum age of values supplied in the definition of the category state
Type: Non-negative integer
Default: No default

`table` The table of data specifying the initial values by age
Type: Data table with label = n
Default: No default
Value: A *nxm* matrix, where $n =$ the categories and $m =$ the number of ages defined in the model. Rows of values specify the initial value of the partition. The table ends with 'end_table'
Note: See 16.2 for more details on specifying data tables

9.3 Categories

`@Categories` *`label`* Define an object of type *Categories*. See Section 4.2 for more information.

`format` The format that the category names use
Type: String
Default: No default

`names` The names of the categories
Type: Vector of strings
Default: No default

`age_lengths` The age-length relationship labels for each category
Type: Vector of strings
Default: true
Value: Valid labels of age-weight relationships

`age_weight` The age-weight relationships labels for each category
Type: Vector of strings
Default: true
Value: Valid labels of age-weight relationships

9.4 Time-steps

`@Time_Step` *`label`* Define an object of type *Time_Step*. See Section 5.2.1 for more information.

`label` The label of the time step
Type: String
Default: No default

`processes` The labels of the processes that occur in this time step, in the order that they occur
Type: Vector of strings
Default: No default

9.5 Processes

`@Process` *`label`* Define an object of type *Process*. See Section 5.3 for more information.

`label` The label of the process
Type: String
Default: No default

`type` The type of process
Type: String
Default: No default

9.5.1 Process of type Ageing

`@Process[label].type=Ageing`. See Section 5.3.2 for more information.

`categories` The labels of the categories to age

Type: Vector of strings
Default: No default

9.5.2 Process of type Load_Partition

`@Process[label].type=Load_Partition`. See Section **??** for more information.

`table` The table of data specifying the n in each partition category and age
Type: Data table with label =
Default: No default
Value:
Note: See 16.2 for more details on specifying data tables

9.5.3 Process of type Maturation

`@Process[label].type=Maturation`. See Section **??** for more information.

`from` The list of categories to mature from
Type: Vector of strings
Default: No default

`to` The list of categories to mature to
Type: Vector of strings
Default: No default

`selectivities` The list of selectivities to use for maturation
Type: Vector of strings
Default: No default

`years` The years to be associated with the maturity rates
Type: Vector of non-negative integers
Default: No default

`rates` The rates to mature for each year
Type: Vector of real numbers (estimable)
Default: No default

9.5.4 Process of type Mortality_Constant_Rate

`@Process[label].type=Mortality_Constant_Rate`. See Section 5.3.3 for more information.

`categories` The list of category labels
Type: Vector of strings
Default: No default

`m` The mortality rates

Type: Real number (estimable)
Default: No default
Lower Bound: 0.0 (inclusive)

`time_step_proportions` The time step proportions for the mortality rates
Type: Vector of real numbers
Default: false
Lower Bound: 0.0 (inclusive)
Upper Bound: 1.0 (inclusive)
Value: The time step proportions must sum to one. If only one value is supplied, then the each time step is allocated an equal proportion. Otherwise the number of values must equal the number of time steps

`relative_m_by_age` The list of mortality by age ogive labels for the categories
Type: Vector of strings
Default: No default

9.5.5 Process of type Mortality_Event

`@Process[label].type=Mortality_Event`. See Section 5.3.3 for more information.

`categories` The categories
Type: Vector of strings
Default: No default

`years` The years in which to apply the mortality process
Type: Vector of non-negative integers
Default: No default

`catches` The number of removals (catches) to apply for each year
Type: Vector of real numbers (estimable)
Default: No default

`u_max` The maximum exploitation rate (U_max)
Type: Real number
Default: 0.99
Lower Bound: 0.0 (inclusive)
Upper Bound: 1.0 (inclusive)

`selectivities` The list of selectivities
Type: Vector of strings
Default: No default

`penalty` The label of the penalty to apply if the total number of removals cannot be taken
Type: String
Default: No default

9.5.6 Process of type Mortality_Event_Biomass

`@Process[label].type=Mortality_Event_Biomass`. See Section 5.3.3 for more information.

`categories` The category labels
Type: Vector of strings
Default: No default

`selectivities` The labels of the selectivities for each of the categories
Type: Vector of strings
Default: No default

`years` The years in which to apply the mortality process
Type: Vector of non-negative integers
Default: No default

`catches` The biomass of removals (catches) to apply for each year
Type: Vector of real numbers (estimable)
Default: No default

`u_max` The maximum exploitation rate (U_max)
Type: Real number (estimable)
Default: 0.99
Lower Bound: 0.0 (inclusive)
Upper Bound: 1.0 (inclusive)

`penalty` The label of the penalty to apply if the total biomass of removals cannot be taken
Type: String
Default: No default

9.5.7 Process of type Mortality_Holling_Rate

`@Process[label].type=Mortality_Holling_Rate`. See Section 5.3.3 for more information.

`prey_categories` The prey categories labels
Type: Vector of strings
Default: No default

`predator_categories` The predator categories labels
Type: Vector of strings
Default: No default

`is_abundance` Is vulnerable amount of prey and predator an abundance [true] or biomass [false]
Type: Boolean
Default: true

`a` Parameter a

Type: Real number (estimable)
Default: No default
Lower Bound: 0.0 (inclusive)

`b` Parameter b
Type: Real number (estimable)
Default: No default
Lower Bound: 0.0 (inclusive)

`x` This parameter controls the functional form: Holling function type 2 (x=2) or 3 (x=3), or generalised (Michaelis Menten, x¿=1)
Type: Real number (estimable)
Default: No default
Lower Bound: 1.0 (inclusive)

`u_max` The maximum exploitation rate (*U_max*)
Type: Real number
Default: 0.99
Lower Bound: 0.0 (inclusive)
Upper Bound: 1.0 (exclusive)

`prey_selectivities` The selectivities for prey categories
Type: Vector of strings
Default: true

`predator_selectivities` The selectivities for predator categories
Type: Vector of strings
Default: true

`penalty` The label of penalty
Type: String
Default: No default

`years` The years in which to apply the mortality process
Type: Vector of non-negative integers
Default: No default

`table` The table of data specifying the predator selectivities
Type: Data table with label =
Default: No default
Value:
Note: See 16.2 for more details on specifying data tables

`table` The table of data specifying the prey selectivities

Type: Data table with label =
Default: No default
Value:
Note: See 16.2 for more details on specifying data tables

9.5.8 Process of type Mortality_Initialisation_Event

`@Process[label].type=Mortality_Initialisation_Event`. See Section 5.3.3 for more information.

`categories` The categories
Type: Vector of strings
Default: No default

`catch` The number of removals (catches) to apply for each year
Type: Real number (estimable)
Default: No default

`u_max` The maximum exploitation rate (U_max)
Type: Real number
Default: 0.99
Lower Bound: 0.0 (inclusive)
Upper Bound: 1.0 (exclusive)

`selectivities` The list of selectivities
Type: Vector of strings
Default: No default

`penalty` The label of the penalty to apply if the total number of removals cannot be taken
Type: String
Default: No default

`table` The table of data specifying the catches for each fishery, the categories, years, and the U_max
Type: Data table with label =
Default: No default
Value:
Note: See 16.2 for more details on specifying data tables

9.5.9 Process of type Mortality_Initialisation_Event_Biomass

`@Process[label].type=Mortality_Initialisation_Event_Biomass`. See Section 5.3.3 for more information.

`categories` The categories
Type: Vector of strings
Default: No default

`catch` The number of removals (catches) to apply for each year
Type: Real number (estimable)
Default: No default

`u_max` The maximum exploitation rate (*U_max*)
Type: Real number
Default: 0.99
Lower Bound: 0.0 (inclusive)
Upper Bound: 1.0 (inclusive)

`selectivities` The list of selectivities
Type: Vector of strings
Default: No default

`penalty` The label of the penalty to apply if the total number of removals cannot be taken
Type: String
Default: No default

9.5.10 Process of type Mortality_Instantaneous

`@Process[label].type=Mortality_Instantaneous`. See Section 5.3.3 for more information.

`categories` The categories for instantaneous mortality
Type: Vector of strings
Default: No default

`m` The natural mortality rates for each category
Type: Real number (estimable)
Default: No default
Lower Bound: 0.0 (inclusive)

`time_step_proportions` The time step proportions for natural mortality
Type: Vector of real numbers
Default: true
Lower Bound: 0.0 (inclusive)
Upper Bound: 1.0 (inclusive)
Value: Proportions must sum to one

`relative_m_by_age` The M-by-age selectivities to apply to each of the categories for natural mortality
Type: Vector of strings
Default: No default

`table` The table of data specifying the catches for each fishery, the categories, years, and the

U_max
Type: Data table with label =
Default: No default
Value:
Note: See 16.2 for more details on specifying data tables

9.5.11 Process of type Mortality_Instantaneous_Retained

`@Process[label].type=Mortality_Instantaneous_Retained`. See Section 5.3.3 for more information.

`categories` The categories for instantaneous mortality
Type: Vector of strings
Default: No default

`m` The natural mortality rates for each category
Type: Real number (estimable)
Default: No default
Lower Bound: 0.0 (inclusive)

`time_step_proportions` The time step proportions for natural mortality
Type: Vector of real numbers
Default: No default
Lower Bound: 0.0 (inclusive)
Upper Bound: 1.0 (inclusive)
Value: Proportions must sum to one

`relative_m_by_age` The M-by-age selectivities to apply on the categories for natural mortality
Type: Vector of strings
Default: No default

`table` The table of data specifying the catches for each fishery, the categories, years, and the U_max
Type: Data table with label =
Default: No default
Value:
Note: See 16.2 for more details on specifying data tables

9.5.12 Process of type Mortality_Prey_Suitability

`@Process[label].type=Mortality_Prey_Suitability`. See Section 5.3.3 for more information.

`prey_categories` The prey categories labels
Type: Vector of strings
Default: No default

`predator_categories` The predator categories labels

Type: Vector of strings
Default: No default

`consumption_rate` The predator consumption rate
Type: Real number (estimable)
Default: No default
Lower Bound: 0.0 (inclusive)
Upper Bound: 1.0 (inclusive)

`electivities` The prey electivities
Type: Vector of real numbers (estimable)
Default: No default
Lower Bound: 0.0 (inclusive)
Upper Bound: 1.0 (inclusive)

`u_max` The maximum exploitation rate (U_max)
Type: Real number
Default: 0.99
Lower Bound: 0.0 (inclusive)
Upper Bound: 1.0 (exclusive)

`prey_selectivities` The selectivities for prey categories
Type: Vector of strings
Default: No default

`predator_selectivities` The selectivities for predator categories
Type: Vector of strings
Default: No default

`penalty` The label of the penalty
Type: String
Default: No default

`years` The year that process occurs
Type: Vector of non-negative integers
Default: No default

9.5.13 Process of type null_process

`@Process[label].type=null_process`.

The null_process type has no additional subcommands. Note that this process does nothing. It is included primarily as a means of replacing other processes with ”no action” to allow for testing of alternative model structures.

9.5.14 Process of type Recruitment_Beverton_Holt

`@Process[label].type=Recruitment_Beverton_Holt`. See Section 5.3.1 for more information.

`categories` The category labels
Type: Vector of strings
Default: No default

`r0` R0, the mean recruitment used to scale annual recruits or initialise the model
Type: Real number (estimable)
Default: No default
Lower Bound: 0.0 (inclusive)
Value: Use either R0 or B0, but not both

`b0` B0, the SSB corresponding to R0, and used to scale annual recruits or initialise the model
Type: Real number (estimable)
Default: No default
Lower Bound: 0.0 (inclusive)
Value: Use either R0 or B0, but not both

`proportions` The proportion for each category
Type: Real number (estimable)
Default: No default

`age` The age at recruitment
Type: Non-negative integer
Default: No default

`ssb_offset` The spawning biomass year offset
Type: Non-negative integer
Default: No default

`steepness` Steepness (h)
Type: Real number (estimable)
Default: 1.0
Lower Bound: 0.2 (inclusive)
Upper Bound: 1.0 (inclusive)

`ssb` The SSB label (i.e., the derived quantity label)
Type: String
Default: No default

`b0_initialisation_phase` The initialisation phase label that B0 is from
Type: String
Default: No default

`ycs_values` The YCS values
Type: Vector of real numbers (estimable)
Default: No default

`ycs_years` The recruitment years. A vector of years that relates to the year of the spawning event that created this cohort
Type: Vector of non-negative integers
Default: false

`standardise_ycs_years` The years that are included for year class standardisation
Type: Vector of non-negative integers
Default: true

9.5.15 Process of type Recruitment_Beverton_Holt_With_Deviations

`@Process[label].type=Recruitment_Beverton_Holt_With_Deviations`. See Section 5.3.1 for more information.

`categories` The category labels
Type: Vector of strings
Default: No default

`r0` R0, the mean recruitment used to scale annual recruits or initialise the model
Type: Real number (estimable)
Default: No default
Lower Bound: 0.0 (inclusive)
Value: Use either R0 or B0, but not both

`b0` B0, the SSB corresponding to R0, and used to scale annual recruits or initialise the model
Type: Real number (estimable)
Default: No default
Lower Bound: 0.0 (inclusive)
Value: Use either R0 or B0, but not both

`proportions` The proportion for each category
Type: Real number (estimable)
Default: No default

`age` The age at recruitment
Type: Non-negative integer
Default: true

`ssb_offset` The spawning biomass year offset
Type: Non-negative integer
Default: No default

`steepness` Steepness (h)

Type: Real number (estimable)
Default: 1.0
Lower Bound: 0.2 (inclusive)
Upper Bound: 1.0 (inclusive)

`ssb` The SSB label (i.e., the derived quantity label)
Type: String
Default: No default
Value: (
A valid derived quantity)

`sigma_r` The standard deviation of recruitment, σ_R
Type: Real number (estimable)
Default: No default
Lower Bound: 0.0 (inclusive)

`b_max` The maximum bias adjustment
Type: Real number (estimable)
Default: 0.85
Lower Bound: 0.0 (inclusive)
Upper Bound: 1.0 (inclusive)

`last_year_with_no_bias` The last year with no bias adjustment
Type: Non-negative integer
Default: false

`first_year_with_bias` The first year with full bias adjustment
Type: Non-negative integer
Default: false

`last_year_with_bias` The last year with full bias adjustment
Type: Non-negative integer
Default: false

`first_recent_year_with_no_bias` The first recent year with no bias adjustment
Type: Non-negative integer
Default: false

`b0_initialisation_phase` The initialisation phase label that B0 is from
Type: String
Default: No default

`deviation_values` The recruitment deviation values
Type: Vector of real numbers (estimable)
Default: No default

`deviation_years` The recruitment years. A vector of years that relates to the year of the

spawning event that created this cohort
Type: Vector of non-negative integers
Default: false

9.5.16 Process of type Recruitment_Constant

`@Process[label].type=Recruitment_Constant`. See Section 5.3.1 for more information.

`categories` The categories
Type: Vector of strings
Default: No default

`proportions` The proportion for each category
Type: Real number (estimable)
Default: true

`age` The age at recruitment
Type: Non-negative integer
Default: No default

`r0` R0, the recruitment used for annual recruits and initialise the model
Type: Real number (estimable)
Default: No default
Lower Bound: 0.0 (inclusive)

9.5.17 Process of type Survival_Constant_Rate

`@Process[label].type=Survival_Constant_Rate`. See Section **??** for more information.

`categories` The list of categories
Type: Vector of strings
Default: No default

`s` The survival rates
Type: Real number (estimable)
Default: No default
Lower Bound: 0.0 (inclusive)
Upper Bound: 1.0 (inclusive)

`time_step_proportions` The time step proportions for the survival rate S
Type: Vector of real numbers
Default: true
Lower Bound: 0.0 (exclusive)
Upper Bound: 1.0 (inclusive)
Value: The proportions must sum to one

`selectivities` The selectivity labels for each category

Type: Vector of strings
Default: No default

9.5.18 Process of type Tag_By_Age

`@Process[label].type=Tag_By_Age`. See Section 5.3.5 for more information.

`from` The categories that are selected for tagging (i.e, transition from)
Type: Vector of strings
Default: No default

`to` The categories that have tags (i.e., transition to)
Type: Vector of strings
Default: No default

`min_age` The minimum age tagged
Type: Non-negative integer
Default: No default

`max_age` The maximum age tagged
Type: Non-negative integer
Default: No default

`penalty` The penalty label
Type: String
Default: No default

`u_max` The maximum exploitation rate (U_max)
Type: Real number
Default: 0.99
Lower Bound: 0.0 (inclusive)
Upper Bound: 1.0 (exclusive)

`years` The years to execute the tagging in
Type: Vector of non-negative integers
Default: No default

`initial_mortality` The initial mortality value
Type: Real number (estimable)
Default: 0.0
Lower Bound: 0.0 (inclusive)

`initial_mortality_selectivity` The initial mortality selectivity label
Type: String
Default: No default

`loss_rate` The loss rate

Type: Vector of real numbers (estimable)
Default: No default

`loss_rate_selectivities` The loss rate selectivity label
Type: Vector of strings
Default: true

`selectivities` The selectivity labels
Type: Vector of strings
Default: No default

`n` N
Type: Vector of real numbers (estimable)
Default: true

`table` The table of data specifying the n to tag from and to each category, years, and the U_max
Type: Data table with label =
Default: No default
Value:
Note: See 16.2 for more details on specifying data tables

9.5.19 Process of type Tag_By_Length

`@Process[label].type=Tag_By_Length`. See Section 5.3.5 for more information.

`from` The categories that are selected for tagging (i.e, transition from)
Type: Vector of strings
Default: No default

`to` The categories that have tags (i.e., transition to)
Type: Vector of strings
Default: No default

`penalty` The penalty label
Type: String
Default: No default

`u_max` The maximum exploitation rate (*U_max*)
Type: Real number
Default: 0.99
Lower Bound: 0.0 (inclusive)
Upper Bound: 1.0 (exclusive)

`years` The years to execute the tagging events in
Type: Vector of non-negative integers
Default: No default

`initial_mortality` The initial mortality to apply to tags as a proportion
Type: Real number (estimable)
Default: 0.0
Lower Bound: 0.0 (inclusive)
Upper Bound: 1.0 (inclusive)

`initial_mortality_selectivity`
Type: String
Default: No default
Value: A valid selectivity label

`selectivities`
Type: Vector of strings
Default: No default
Value: Valid selectivity labels

`n` The total number of tags to apply
Type: Vector of real numbers (estimable)
Default: No default

`tolerance` Tolerance for checking the specified proportions sum to one
Type: Real number
Default: 1e-5
Lower Bound: 0 (inclusive)
Upper Bound: 1.0 (inclusive)

`table` The table of data specifying the n to tag from and to each category, years, and the U_max
Type: Data table with label =
Default: No default
Value:
Note: See 16.2 for more details on specifying data tables

9.5.20 Process of type Tag_Loss

`@Process[label].type=Tag_Loss`. See Section 5.3.6 for more information.

`categories` The list of categories
Type: Vector of strings
Default: No default
Value: Valid category labels

`tag_loss_rate` The tag loss rates
Type: Vector of real numbers (estimable)
Default: No default
Lower Bound: 0.0 (inclusive)
Value: The instantaneous rate of tag loss

`time_step_ratio` The time step ratios for tag loss
Type: Vector of real numbers (estimable)
Default: true
Lower Bound: 0.0 (inclusive)
Upper Bound: 1.0 (inclusive)

`tag_loss_type` The type of tag loss
Type: String
Default: No default

`selectivities` The selectivities
Type: Vector of strings
Default: No default

`year` The year the first tagging release process was executed
Type: Non-negative integer
Default: No default

9.5.21 Process of type Transition_Category

`@Process[label].type=Transition_Category`. See Section 5.3.4 for more information.

`from` The categories to transition from
Type: Vector of strings
Default: No default
Value: Valid category labels

`to` The categories to transition to
Type: Vector of strings
Default: No default
Value: Valid category labels

`proportions` The proportions to transition for each category
Type: Real number (estimable)
Default: No default
Lower Bound: 0.0 (inclusive)
Upper Bound: 1.0 (inclusive)

`selectivities` The selectivities to apply to each proportion
Type: Vector of strings
Default: No default
Value: Valid selectivity labels

9.5.22 Process of type Transition_Category_By_Age

`@Process[label].type=Transition_Category_By_Age`. See Section 5.3.4 for more information.

`from` The categories to transition from
Type: Vector of strings
Default: No default
Value: Valid category labels

`to` The categories to transition to
Type: Vector of strings
Default: No default
Value: Valid category labels

`min_age` The minimum age to transition
Type: Non-negative integer
Default: No default
Value: Valid category labels

`max_age` The maximum age to transition
Type: Non-negative integer
Default: No default

`penalty` The penalty label
Type: String
Default: No default
Value: A valid penalty label

`u_max` The maximum exploitation rate (U_max)
Type: Real number (estimable)
Default: 0.99
Lower Bound: 0.0 (inclusive)
Upper Bound: 1.0 (exclusive)

`years` The years to execute the transition in
Type: Vector of non-negative integers
Default: No default

`table` The table of data specifying the n to transition from and to each category, years, and the U_max
Type: Data table with label =
Default: No default
Value:
Note: See 16.2 for more details on specifying data tables

9.6 Time varying parameters

`@Time_Varying` *`label`* Define an object of type *Time_Varying*. See Section 5.11 for more information.

`label` The label of the time-varying object

Type: String
Default: No default

`type` The type of the time-varying object
Type: String
Default: No default

`parameter` The name of the parameter to vary in each year
Type: String
Default: No default

`years` The years in which to vary the parameter
Type: Vector of non-negative integers
Default: No default

9.6.1 Time_Varying of type Annual_Shift

`@Time_Varying[label].type=Annual_Shift`. See Section 5.11.3 for more information.

`a` Parameter A
Type: Real number (estimable)
Default: No default

`b` Parameter B
Type: Real number (estimable)
Default: No default

`c` Parameter C
Type: Real number (estimable)
Default: No default

`scaling_years` The scaling years
Type: Vector of non-negative integers
Default: The years in which to vary the parameter

`values` The values
Type: Vector of real numbers (estimable)
Default: No default

9.6.2 Time_Varying of type Constant

`@Time_Varying[label].type=Constant`. See Section 5.11.1 for more information.

`values` The value to assign to addressable
Type: Vector of real numbers (estimable)
Default: No default

9.6.3 Time_Varying of type Exogenous

`@Time_Varying[label].type=Exogenous`. See Section 5.11.4 for more information.

`a` The shift parameter
Type: Real number (estimable)
Default: No default

`exogenous_variable` The values of exogenous variable for each year
Type: Vector of real numbers (estimable)
Default: No default

9.6.4 Time_Varying of type Linear

`@Time_Varying[label].type=Linear`. See Section **??** for more information.

`slope` The slope of the linear trend (i.e., the additive amount per year)
Type: Real number (estimable)
Default: No default

`intercept` The intercept of the linear trend (, i.e. the value in the first year)
Type: Real number (estimable)
Default: No default

9.6.5 Time_Varying of type Random_Draw

`@Time_Varying[label].type=Random_Draw`. See Section **??** for more information.

`mean` The mean (μ) of the random draw distribution
Type: Real number (estimable)
Default: 0

`sigma` The standard deviation (σ) of the random draw distribution
Type: Real number (estimable)
Default: 1.0
Value: A positive real number

`lower_bound` The lower bound for the random draw
Type: Real number (estimable)
Default: No default

`upper_bound` The upper bound for the random draw
Type: Real number (estimable)
Default: No default

`distribution` The distribution type
Type: String
Default: normal
Value: Only the normal and lognormal are implemented

9.6.6 Time_Varying of type Random_Walk

`@Time_Varying[label].type=Random_Walk`. See Section 5.11.2 for more information.

`mean` The mean (μ) of the random walk distribution
Type: Real number (estimable)
Default: 0.0

`sigma` The standard deviation (σ) of the random walk distribution
Type: Real number (estimable)
Default: 1.0
Value: A positive real number

`lower_bound` The lower bound for the random walk
Type: Real number (estimable)
Default: No default

`upper_bound` The upper bound for the random walk
Type: Real number (estimable)
Default: No default

`rho` The autocorrelation parameter (ρ) of the random walk distribution
Type: Real number (estimable)
Default: 1

`distribution` The distribution type
Type: String
Default: normal
Value: Only the normal distribution is implemented

9.7 Derived quantities

`@Derived_Quantity` *`label`* Define an object of type *Derived_Quantity*. See Section 5.4 for more information.

`label` The label of the derived quantity
Type: String
Default: No default

`type` The type of derived quantity
Type: String
Default: No default

`time_step` The time step in which to calculate the derived quantity
Type: String
Default: No default

`categories` The list of categories to use when calculating the derived quantity
Type: Vector of strings
Default: No default

`selectivities` The list of selectivities to use when calculating the derived quantity
Type: Vector of strings
Default: No default

`time_step_proportion` The proportion through the mortality block of the time step when the derived quantity is calculated
Type: Real number (estimable)
Default: 0.5
Lower Bound: 0.0 (inclusive)
Upper Bound: 1.0 (inclusive)

`time_step_proportion_method` The method for interpolating for the proportion through the mortality block
Type: String
Default: weighted_sum

`values`
Type: Vector of addressables
Default: No default

9.7.1 Derived_Quantity of type Abundance

`@Derived_Quantity[label].type=Abundance`. See Section 5.4 for more information.

The Abundance type has no additional subcommands.

9.7.2 Derived_Quantity of type Biomass

`@Derived_Quantity[label].type=Biomass`. See Section 5.4 for more information.

`age_weight_labels` The labels for the age-weights that correspond to each category for the biomass calculation
Type: Vector of strings
Default: No default

9.8 Age-length relationship

`@Age_Length` *`label`* Define an object of type *Age_Length*. See Section 5.5 for more information.

`label` The label of the age length relationship
Type: String
Default: No default

`type` The type of age length relationship

Type: String
Default: No default

`time_step_proportions` The fraction of the year applied in each time step that is added to the age for the purposes of evaluating the length, i.e., a value of 0.5 for a time step will evaluate the length of individuals at age+0.5 in that time step
Type: Vector of real numbers
Default: true
Lower Bound: 0.0 (inclusive)
Upper Bound: 1.0 (inclusive)

`distribution` The assumed distribution for the growth curve
Type: String
Default: normal

`cv_first` The CV for the first age class
Type: Real number (estimable)
Default: 0.0
Lower Bound: 0.0 (inclusive)

`cv_last` The CV for last age class
Type: Real number (estimable)
Default: 0.0
Lower Bound: 0.0 (inclusive)
Note: If not supplied, the value is assumed to be equal to cv_first

`compatibility_option` Backwards compatibility option: either casal2 (the default) or casal to use the (less accurate) cumulative normal function from CASAL
Type: String
Default: casal2

`by_length` Specifies if the linear interpolation of CVs is a linear function of mean length at age, or at age
Type: Boolean
Default: true
Note: The default is almost always the most appropriate choice. This option is provided for compatibility with a similar option in CASAL

9.8.1 Age_Length of type Data

`@Age_Length[label].type=Data`. See Section 5.5.4 for more information.

`external_gaps` The method to use for external data gaps
Type: String
Default: mean

`internal_gaps` The method to use for internal data gaps

Type: String
Default: mean

`length_weight` The label from an associated length-weight block
Type: String
Default: No default

`time_step_measurements_were_made` The time step label for which size-at-age data are provided
Type: String
Default: No default

`table` The table of data specifying the length at age values
Type: Data table with label = data
Default: No default
Value: A $n \times m$ matrix, where $n =$ the years of the model, and $m =$ the number of ages defined in the model. Rows of values specify the length for each age for every year. The table ends with 'end_table'
Note: See 16.2 for more details on specifying data tables

9.8.2 Age_Length of type None

`@Age_Length[label].type=None`. See Section 5.5.1 for more information.

The None type has no additional subcommands.

9.8.3 Age_Length of type Schnute

`@Age_Length[label].type=Schnute`. See Section 5.5.3 for more information.

`y1` The y_1 parameter
Type: Real number (estimable)
Default: No default

`y2` The y_2 parameter
Type: Real number (estimable)
Default: No default

`tau1` The τ_1 parameter
Type: Real number (estimable)
Default: No default

`tau2` The τ_2 parameter
Type: Real number (estimable)
Default: No default

`a` The a parameter
Type: Real number (estimable)
Default: No default
Lower Bound: 0.0 (inclusive)

`b` The *b* parameter
Type: Real number (estimable)
Default: No default
Lower Bound: 0.0 (exclusive)

`length_weight` The label of the associated length-weight relationship
Type: String
Default: No default

9.8.4 Age_Length of type Von_Bertalanffy

`@Age_Length[label].type=Von_Bertalanffy`. See Section 5.5.2 for more information.

`linf` The *L_infinity* parameter
Type: Real number (estimable)
Default: No default
Lower Bound: 0.0 (inclusive)

`k` The *k* parameter
Type: Real number (estimable)
Default: No default
Lower Bound: 0.0 (inclusive)

`t0` The *t_0* parameter
Type: Real number (estimable)
Default: No default

`length_weight` The label of the associated length-weight relationship
Type: String
Default: No default

9.9 Length-weight

`@Length_Weight` *`label`* Define an object of type *Length_Weight*. See Section 5.6 for more information.

`label` The label of the length-weight relationship
Type: String
Default: No default

`type` The type of the length-weight relationship
Type: String
Default: No default

9.9.1 Length_Weight of type Basic

`@Length_Weight[label].type=Basic`. See Section 5.6.2 for more information.

`a` The a parameter ($W = aL^b$)
Type: Real number (estimable)
Default: No default
Lower Bound: 0.0 (exclusive)

`b` The b parameter ($W = aL^b$)
Type: Real number (estimable)
Default: No default
Lower Bound: 0.0 (exclusive)

`units` The units for weights (grams, kilograms (kgs), or tonnes)
Type: String
Default: No default

9.9.2 Length_Weight of type None

`@Length_Weight[label].type=None`. See Section 5.6.1 for more information.

The None type has no additional subcommands.

9.10 Age-weight

`@Age_Weight` *`label`* Define an object of type *Age_Weight*. See Section 5.7 for more information.

`label` Label of the age weight relationship
Type: String
Default: No default

`type` The type of age weight
Type: String
Default: No default

9.10.1 Age_Weight of type Data

`@Age_Weight[label].type=Data`. See Section 5.7 for more information.

`equilibrium_method` If used in an SSB calculation, what is the method to calculate equilibrium SSB
Type: String
Default: terminal_year

`units` The units of measure (grams, kilograms (kgs), or tonnes)
Type: String
Default: kgs

`table` The table of data specifying the age at weight values
Type: Data table with label = data
Default: No default
Value: A $n \times m$ matrix, where $n =$ the years of the model, and $m =$ the number of ages defined in the model. Rows of values specify the weight for each age for every year. The table ends with 'end_table'
Note: See 16.2 for more details on specifying data tables

9.10.2 Age_Weight of type None

`@Age_Weight[label].type=None`. See Section 5.7 for more information.

The None type has no additional subcommands.

9.11 Selectivities

`@Selectivity` *`label`* Define an object of type *Selectivity*. See Section 5.10 for more information.

`label` The label for the selectivity
Type: String
Default: No default

`type` The type of selectivity
Type: String
Default: No default

`length_based` Is the selectivity length based?
Type: Boolean
Default: false

`intervals` The number of quantiles to evaluate a length-based selectivity over the age-length distribution
Type: Non-negative integer
Default: 5

`values`
Type: Vector of addressables
Default: No default

`length_values`
Type: Vector of addressables
Default: No default

9.11.1 Selectivity of type All_Values

`@Selectivity[label].type=All_Values`. See Section 5.10.3 for more information.

`v` The v parameter

Type: Vector of real numbers (estimable)
Default: No default

9.11.2 Selectivity of type All_Values_Bounded

`@Selectivity[label].type=All_Values_Bounded`. See Section 5.10.4 for more information.

`l` The low value (L)
Type: Non-negative integer
Default: No default

`h` The high value (H)
Type: Non-negative integer
Default: No default

`v` The v parameter
Type: Vector of real numbers (estimable)
Default: No default

9.11.3 Selectivity of type Constant

`@Selectivity[label].type=Constant`. See Section 5.10.1 for more information.

`c` The constant value
Type: Real number (estimable)
Default: No default

9.11.4 Selectivity of type Double_Exponential

`@Selectivity[label].type=Double_Exponential`. See Section 5.10.10 for more information.

`x0` The $x0$ parameter
Type: Real number (estimable)
Default: No default

`x1` The $x1$ parameter
Type: Real number (estimable)
Default: No default

`x2` The $x2$ parameter
Type: Real number (estimable)
Default: No default

`y0` The $y0$ parameter
Type: Real number (estimable)
Default: No default
Lower Bound: 0.0 (inclusive)

`y1` The $y1$ parameter
Type: Real number (estimable)
Default: No default
Lower Bound: 0.0 (inclusive)

`y2` The $y2$ parameter
Type: Real number (estimable)
Default: No default
Lower Bound: 0.0 (inclusive)

`alpha` The maximum value of the selectivity
Type: Real number (estimable)
Default: 1.0
Lower Bound: 0.0 (exclusive)

9.11.5 Selectivity of type Double_Normal

`@Selectivity[label].type=Double_Normal`. See Section 5.10.9 for more information.

`mu` The mean (μ
Type: Real number (estimable)
Default: No default

`sigma_l` The left-hand variance (sigma_l) parameter
Type: Real number (estimable)
Default: No default
Lower Bound: 0.0 (exclusive)

`sigma_r` The right-hand variance (sigma_r) parameter
Type: Real number (estimable)
Default: No default
Lower Bound: 0.0 (exclusive)

`alpha` The maximum value of the selectivity
Type: Real number (estimable)
Default: 1.0
Lower Bound: 0.0 (exclusive)

9.11.6 Selectivity of type Increasing

`@Selectivity[label].type=Increasing`. See Section 5.10.5 for more information.

`l` The low value (L)
Type: Non-negative integer
Default: No default

`h` The high value (H)

Type: Non-negative integer
Default: No default

`v` The v parameter
Type: Vector of real numbers (estimable)
Default: No default

`alpha` The maximum value of the selectivity
Type: Real number (estimable)
Default: 1.0
Lower Bound: 0.0 (exclusive)

9.11.7 Selectivity of type Inverse_Logistic

`@Selectivity[label].type=Inverse_Logistic`. See Section 5.10.7 for more information.

`a50` The a50 parameter
Type: Real number (estimable)
Default: No default

`ato95` The ato95 parameter
Type: Real number (estimable)
Default: No default
Lower Bound: 0.0 (exclusive)

`alpha` The maximum value of the selectivity
Type: Real number (estimable)
Default: 1.0
Lower Bound: 0.0 (exclusive)

9.11.8 Selectivity of type Knife_Edge

`@Selectivity[label].type=Knife_Edge`. See Section 5.10.2 for more information.

`e` The edge value
Type: Real number (estimable)
Default: No default

`alpha` The maximum value of the selectivity
Type: Real number (estimable)
Default: 1.0

9.11.9 Selectivity of type Logistic

`@Selectivity[label].type=Logistic`. See Section 5.10.6 for more information.

`a50` The a50 parameter

Type: Real number (estimable)
Default: No default

`ato95` The ato95 parameter
Type: Real number (estimable)
Default: No default
Lower Bound: 0.0 (exclusive)

`alpha` The maximum value of the selectivity
Type: Real number (estimable)
Default: 1.0
Lower Bound: 0.0 (exclusive)

9.11.10 Selectivity of type Logistic_Producing

`@Selectivity[label].type=Logistic_Producing`. See Section 5.10.8 for more information.

`l` The low value (L)
Type: Non-negative integer
Default: No default

`h` The high value (H)
Type: Non-negative integer
Default: No default

`a50` The a50 parameter
Type: Real number (estimable)
Default: No default

`ato95` the ato95 parameter
Type: Real number (estimable)
Default: No default
Lower Bound: 0.0 (exclusive)

`alpha` The maximum value of the selectivity
Type: Real number (estimable)
Default: 1.0
Lower Bound: 0.0 (exclusive)

9.12 Projections

`@Project` *`label`* Define an object of type *Project*. See Section 5.13 for more information.

`label` Label
Type: String
Default: No default

`type` Type

Type: String
Default: No default

`years` Years to recalculate the values
Type: Vector of non-negative integers
Default: No default

`parameter` Parameter to project
Type: String
Default: No default

`multiplier` Multiplier that is applied to the projected value
Type: Real number (estimable)
Default: 1.0
Lower Bound: 0.0 (exclusive)

9.12.1 Project of type Constant

`@Project[label].type=Constant`. See Section 5.13.1 for more information.

`values` The values to assign to the addressable
Type: Vector of real numbers (estimable)
Default: No default

9.12.2 Project of type Empirical_Sampling

`@Project[label].type=Empirical_Sampling`. See Section 5.13.1 for more information.

`start_year` The start year of sampling
Type: Non-negative integer
Default: No default

`final_year` The final year of sampling
Type: Non-negative integer
Default: No default

9.12.3 Project of type Log_Normal

`@Project[label].type=Log_Normal`. See Section 5.13.1 for more information.

`mean` The mean of the lognormal process
Type: Real number (estimable)
Default: 0.0

`sigma` The standard deviation (sigma) of the lognormal sampling
Type: Real number (estimable)
Default: No default
Lower Bound: 0.0 (inclusive)

9.12.4 Project of type Log_Normal_Empirical

`@Project[label].type=Log_Normal_Empirical`. See Section 5.13.1 for more information.

`mean` The mean of the Gaussian process
Type: Real number (estimable)
Default: 0.0

`start_year` The start year of sampling
Type: Non-negative integer
Default: No default

`final_year` The final year of sampling
Type: Non-negative integer
Default: No default

9.12.5 Project of type User_Defined

`@Project[label].type=User_Defined`. See Section 5.13.1 for more information.

`equation` The equation to do a test run of
Type: Vector of strings
Default: No default

10 Estimation command and subcommand syntax

The description of the methods for the estimation section is given in Section 6.

In the following section, the sub-section headers use a notation of the form "**@observation[label].type=abundance**" which, in this case, represents the input command fragment

```
@observation label # where label is a unique label for that observation
type=abundance
...
```

The specific subcommands for a command are given within each command.

10.1 Estimation methods

`@Estimate` *`label`* Define an object of type *Estimate*. See Section 6 for more information.

`label` The label of the estimate
Type: String
Default: No default

`type` The type of prior for the estimate
Type: String
Default: No default

`parameter` The name of the parameter to estimate
Type: String
Default: No default

`lower_bound` The lower bound for the parameter
Type: Real number (estimable)
Default: No default

`upper_bound` The upper bound for the parameter
Type: Real number (estimable)
Default: No default

`same` List of other parameters that are constrained to have the same value as this parameter
Type: Vector of strings
Default: No default

`estimation_phase` The first estimation phase to allow this to be estimated
Type: Non-negative integer
Default: 1
Value: Phases must be number sequentially and start at one

`mcmc` Indicates if this parameter is estimated at the point estimate but fixed during MCMC estimation run
Type: Boolean
Default: false

`transformation` Type of simple transformation to apply to estimate
Type: String
Default: No default

`transform_with_jacobian` Apply Jacobian during transformation
Type: Boolean
Default: false

`prior_applies_to_transform` Does the prior apply to the transformed parameter?
Type: Boolean
Default: false

10.1.1 Estimate of prior type Beta

`@Estimate[label].type=Beta`. See Section 6.7.7 for more information.

`mu` Beta prior mean (mu) parameter
Type: Real number (estimable)
Default: No default

`sigma` Beta prior standard deviation (sigma) parameter

Type: Real number (estimable)
Default: No default
Lower Bound: 0.0 (exclusive)

`a` Beta prior lower bound of the range (A) parameter
Type: Real number (estimable)
Default: No default

`b` Beta prior upper bound of the range (B) parameter
Type: Real number (estimable)
Default: No default

10.1.2 Estimate of prior type Lognormal

`@Estimate[label].type=Lognormal`. See Section 6.7.5 for more information.

`mu` The lognormal prior mean (mu) parameter
Type: Real number (estimable)
Default: No default
Lower Bound: 0.0 (exclusive)

`cv` The lognormal variance (cv) parameter
Type: Real number (estimable)
Default: No default
Lower Bound: 0.0 (exclusive)

10.1.3 Estimate of prior type Normal

`@Estimate[label].type=Normal`. See Section 6.7.3 for more information.

`mu` The normal prior mean (mu) parameter
Type: Real number (estimable)
Default: No default

`cv` The normal standard deviation (sigma) parameter
Type: Real number (estimable)
Default: No default
Lower Bound: 0.0 (exclusive)

10.1.4 Estimate of prior type Normal_By_Stdev

`@Estimate[label].type=Normal_By_Stdev`. See Section 6.7.4 for more information.

`mu` The normal prior mean (mu) parameter
Type: Real number (estimable)
Default: No default

`sigma` The normal standard deviation (sigma) parameter

Type: Real number (estimable)
Default: No default
Lower Bound: 0.0 (exclusive)

`lognormal_transformation` Add a Jacobian if the derived outcome of the estimate is assumed to be lognormal, e.g., used for recruitment deviations in the recruitment process. See the User Manual for more information
Type: Boolean
Default: false

10.1.5 Estimate of prior type Normal_Log

`@Estimate[label].type=Normal_Log`. See Section 6.7.6 for more information.

`mu` The normal-log prior mean (mu) parameter
Type: Real number (estimable)
Default: No default

`sigma` The normal-log prior standard deviation (sigma) parameter
Type: Real number (estimable)
Default: No default
Lower Bound: 0.0 (exclusive)

10.1.6 Estimate of type Uniform

`@Estimate[label].type=Uniform`. See Section 6.7.1 for more information.

The Uniform type has no additional subcommands.

10.1.7 Estimate of type Uniform_Log

`@Estimate[label].type=Uniform_Log`. See Section 6.7.2 for more information.

The Uniform_Log type has no additional subcommands.

10.2 Point estimation

`@Minimiser` *`label`* Define an object of type *Minimiser*. See Section 6.4 for more information.

`label` The minimiser label
Type: String
Default: No default

`type` The type of minimiser to use
Type: String
Default: No default

`active` Indicates if this minimiser is active
Type: Boolean
Default: false

`covariance` Indicates if a covariance matrix should be generated
Type: Boolean
Default: true

10.2.1 Minimiser of type ADOLC

`@Minimiser[label].type=ADOLC`. See Section 6.4.5 for more information.

`iterations` The maximum number of iterations
Type: Integer
Default: 1000
Lower Bound: 1 (inclusive)

`evaluations` The maximum number of evaluations
Type: Integer
Default: 4000
Lower Bound: 1 (inclusive)

`tolerance` The tolerance of the gradient for convergence
Type: Real number
Default: 1e-5
Lower Bound: 0.0 (exclusive)

`step_size` The minimum step size before minimisation fails
Type: Real number
Default: 1e-7
Lower Bound: 0.0 (exclusive)

10.2.2 Minimiser of type Betadiff

`@Minimiser[label].type=Betadiff`. See Section 6.4.4 for more information.

`iterations` The maximum number of iterations
Type: Integer
Default: 1000
Lower Bound: 1 (inclusive)

`evaluations` The maximum number of evaluations
Type: Integer
Default: 4000
Lower Bound: 1 (inclusive)

`tolerance` The tolerance of the gradient for convergence
Type: Real number
Default: 1e-5
Lower Bound: 0.0 (exclusive)

10.2.3 Minimiser of type DESolver

`@Minimiser[label].type=DESolver`. See Section 6.4.3 for more information.

`population_size` The number of candidate solutions to have in the population
Type: Non-negative integer
Default: No default
Lower Bound: 1 (inclusive)

`crossover_probability` The minimiser's crossover probability
Type: Real number
Default: 0.9
Lower Bound: 0.0 (inclusive)
Upper Bound: 1.0 (inclusive)

`difference_scale` The scale to apply to new solutions when comparing candidates
Type: Real number
Default: 0.02

`max_generations` The maximum number of iterations to run
Type: Non-negative integer
Default: No default

`tolerance` The total variance between the population and best candidate before acceptance
Type: Real number
Default: 1e-5
Lower Bound: 0.0 (exclusive)

10.2.4 Minimiser of type Deltadiff

`@Minimiser[label].type=Deltadiff`. See Section 6.4.2 for more information.

`iterations` Maximum number of iterations
Type: Integer
Default: 1000
Lower Bound: 1 (inclusive)

`evaluations` Maximum number of evaluations
Type: Integer
Default: 4000
Lower Bound: 1 (inclusive)

`tolerance` Tolerance of the gradient for convergence
Type: Real number
Default: 1e-5
Lower Bound: 0 (exclusive)

`step_size` Minimum Step-size before minimisation fails

Type: Real number
Default: 1e-7
Lower Bound: 0 (exclusive)

10.2.5 Minimiser of type Numerical_Differences

`@Minimiser[label].type=Numerical_Differences`. See Section 6.4.1 for more information.

`iterations` The maximum number of iterations
Type: Integer
Default: 1000
Lower Bound: 1 (inclusive)

`evaluations` The maximum number of evaluations
Type: Integer
Default: 4000
Lower Bound: 1 (inclusive)

`tolerance` The tolerance of the gradient for convergence
Type: Real number
Default: 1e-5
Lower Bound: 0.0 (exclusive)

`step_size` The minimum step size before minimisation fails
Type: Real number
Default: 1e-7
Lower Bound: 0.0 (exclusive)

10.3 Markov chain Monte Carlo (MCMC)

`@MCMC` *`label`* Define an object of type *MCMC*. See Section 6.6 for more information.

`label` The label of the MCMC
Type: String
Default: No default

`type` The MCMC method
Type: String
Default: No default

`length` The number of iterations for the MCMC (including the burn in period)
Type: Non-negative integer
Default: No default
Lower Bound: 1 (inclusive)

`burn_in` The number of iterations for the burn_in period of the MCMC

Type: Non-negative integer
Default: 0
Lower Bound: 0 (inclusive)

`active` Indicates if this is the active MCMC algorithm
Type: Boolean
Default: true

`step_size` Initial step-size (as a multiplier of the approximate covariance matrix)
Type: Real number
Default: 0.02
Lower Bound: 0 (inclusive)

`start` The covariance multiplier for the starting point of the MCMC
Type: Real number
Default: 0.0
Lower Bound: 0.0 (inclusive)

`keep` The spacing between recorded values in the MCMC
Type: Non-negative integer
Default: 1
Lower Bound: 1 (inclusive)

`max_correlation` The maximum absolute correlation in the covariance matrix of the proposal distribution
Type: Real number
Default: 0.8
Lower Bound: 0.0 (exclusive)
Upper Bound: 1.0 (inclusive)

`covariance_adjustment_method` The method for adjusting small variances in the covariance proposal matrix
Type: String
Default: correlation

`correlation_adjustment_diff` The minimum non-zero variance times the range of the bounds in the covariance matrix of the proposal distribution
Type: Real number
Default: 0.0001
Lower Bound: 0.0 (exclusive)

`proposal_distribution` The shape of the proposal distribution (either the t or the normal distribution)
Type: String
Default: t

`df` The degrees of freedom of the multivariate t proposal distribution
Type: Non-negative integer
Default: 4
Lower Bound: 0 (exclusive)

`adapt_stepsize_at` The iteration numbers in which to check and resize the MCMC stepsize
Type: Vector of non-negative integers
Default: true
Lower Bound: 0 (inclusive)
Value: Must be less than the burn_in

`adapt_stepsize_method` The method to use to adapt the step size
Type: String
Default: ratio

`adapt_covariance_matrix_at` The iteration number in which to adapt the covariance matrix
Type: Non-negative integer
Default: 0
Lower Bound: 0 (inclusive)
Value: Must be less than the burn_in

10.3.1 MCMC of type Hamiltonian_Monte_Carlo

`@MCMC[label].type=Hamiltonian_Monte_Carlo`.

`leapfrog_steps` Number of leapfrog steps
Type: Non-negative integer
Default: 1
Lower Bound: 0 (exclusive)

`leapfrog_delta` Amount to leapfrog per step
Type: Real number
Default: 1e-7
Lower Bound: 0 (exclusive)

`gradient_step_size` Step size to use when calculating gradient
Type: Real number
Default: 1e-7
Lower Bound: 1e-13 (inclusive)

10.3.2 MCMC of type Random_Walk_Metropolis_Hastings

`@MCMC[label].type=Random_Walk`. See Section 6.6 for more information.

The Random_Walk type has no additional subcommands.

10.4 Profiles

`@Profile` *`label`* Define an object of type *Profile*. See Section 6.5 for more information.

`label` The label of the profile
Type: String
Default: No default

`steps` The number of steps between the lower and upper bound
Type: Non-negative integer
Default: No default
Value: A positive integer ≥ 2

`lower_bound` The lower value of the range
Type: Real number (estimable)
Default: No default

`upper_bound` The upper value of the range
Type: Real number (estimable)
Default: No default

`parameter` The free parameter to profile
Type: String
Default: No default

`same` A free parameter that is constrained to have the same value as the parameter being profiled
Type: String
Default: No default

10.5 Defining catchability constants

`@Catchability` *`label`* Define an object of type *Catchability*.

`label` Label of the catchability
Type: String
Default: No default

`type` The type of catchability
Type: String
Default: No default

10.5.1 Catchability of type Free

`@Catchability[label].type=Free`.

`q` The value of the catchability
Type: Real number (estimable)
Default: No default
Lower Bound: 0.0 (inclusive)

10.5.2 Catchability of type Nuisance

`@Catchability[label].type=Nuisance`.

`lower_bound` The upper bound for nuisance catchability
Type: Real number (estimable)
Default: No default

`upper_bound` The lower bound for nuisance catchability
Type: Real number (estimable)
Default: No default

`q` The value of the catchability
Type: Addressable
Default: No default

10.6 Defining penalties

`@Penalty` *`label`* Define an object of type *Penalty*. See Section 6.8 for more information.

`label` The label of the penalty
Type: String
Default: No default

`type` The type of penalty
Type: String
Default: No default

10.6.1 Penalty of type Process

`@Penalty[label].type=Process`. See Section 6.8 for more information.

`multiplier` The penalty multiplier
Type: Real number (estimable)
Default: 1.0

`log_scale` Indicates if the sums of squares will be calculated on the log scale
Type: Boolean
Default: false

10.7 Defining priors on parameter ratios, differences, and means

`@Additional_Prior` *`label`* Define an object of type *Additional_Prior*. See Section 6.9 for more information.

`label` The label for the additional prior
Type: String
Default: No default

`parameter` The name of the parameter for the additional prior
Type: String
Default: No default

`type` The additional prior type
Type: String
Default: No default

10.7.1 Additional_Prior of type Beta

`@Additional_Prior[label].type=Beta`. See Section 6.9 for more information.

`mu` Beta distribution mean μ parameter
Type: Real number (estimable)
Default: No default

`sigma` Beta distribution variance σ parameter
Type: Real number (estimable)
Default: No default
Lower Bound: 0.0 (exclusive)

`a` Beta distribution lower bound, of the range A parameter
Type: Real number
Default: No default

`b` Beta distribution upper bound of the range B parameter
Type: Real number
Default: No default

10.7.2 Additional_Prior of type Element_Difference

`@Additional_Prior[label].type=Element_Difference`. See Section 6.9 for more information.

`second_parameter` The name of the second parameter for comparing
Type: String
Default: No default

`multiplier` Multiply the penalty by this factor
Type: Real number
Default: 1

10.7.3 Additional_Prior of type Log_Normal

`@Additional_Prior[label].type=Log_Normal`. See Section 6.9 for more information.

`mu` The lognormal prior mean (mu) parameter

Type: Real number (estimable)
Default: No default
Lower Bound: 0.0 (exclusive)

`cv` The lognormal CV parameter
Type: Real number (estimable)
Default: No default
Lower Bound: 0.0 (exclusive)

10.7.4 Additional_Prior of type Uniform_Log

`@Additional_Prior[label].type=Uniform_Log`. See Section 6.9 for more information.

The Uniform_Log type has no additional subcommands.

10.7.5 Additional_Prior of type Vector_Average

`@Additional_Prior[label].type=Vector_Average`. See Section 6.9 for more information.

`method` Which calculation method to use: k, l, or m
Type: String
Default: k

`k` The k value to use in the calculation
Type: Real number
Default: No default

`multiplier` Multiplier for the penalty amount
Type: Real number
Default: 1

10.7.6 Additional_Prior of type Vector_Smoothing

`@Additional_Prior[label].type=Vector_Smoothing`. See Section 6.9 for more information.

`log_scale` Should the sums of squares be calculated on the log scale?
Type: Boolean
Default: false

`multiplier` Multiply the penalty by this factor
Type: Real number
Default: 1

`lower_bound` The first element to apply the penalty to in the vector
Type: Non-negative integer
Default: 0

`upper_bound` The last element to apply the penalty to in the vector

Type: Non-negative integer
Default: 0

`r` The rth difference that the penalty is applied to
Type: Non-negative integer
Default: 2

10.8 Defining estimation of transformations

`@Estimate_Transformation` *`label`* Define an object of type *Estimate_Transformation*. See Section 6.10 for more information.

`label` Label for the transformation block
Type: String
Default: No default

`type` The type of transformation
Type: String
Default: No default

`transform_with_jacobian` Apply Jacobian during transformation
Type: Boolean
Default: true

10.8.1 Estimate_Transformation of type Average_Difference

`@Estimate_Transformation[label].type=Average_Difference`. See Section 6.10 for more information.

`theta2` The label of the @estimate block relating to the θ_2 parameter in the transformation
Type: String
Default: No default

`theta1` The label of @estimate block relating to the θ_1 parameter in the transformation
Type: String
Default: No default

10.8.2 Estimate_Transformation of type Inverse

`@Estimate_Transformation[label].type=Inverse`. See Section 6.10 for more information.

`estimate_label` The label of estimate block to apply transformation
Type: String
Default: No default

10.8.3 Estimate_Transformation of type Log

`@Estimate_Transformation[label].type=Log`. See Section 6.10 for more information.

`estimate_label` The label of estimate block to apply transformation
Type: String
Default: No default

10.8.4 Estimate_Transformation of type Log_Sum

`@Estimate_Transformation[label].type=Log_Sum`. See Section 6.10 for more information.

`estimate_label` The label of estimate block to apply transformation
Type: String
Default: No default

`theta1` The label of @estimate block relating to the θ_1 parameter in the transformation
Type: String
Default: No default

10.8.5 Estimate_Transformation of type Orthogonal

`@Estimate_Transformation[label].type=Orthogonal`. See Section 6.10 for more information.

`theta2` The label of the @estimate block relating to the θ_2 parameter in the transformation
Type: String
Default: No default

`theta1` The label of @estimate block relating to the θ_1 parameter in the transformation
Type: String
Default: No default

10.8.6 Estimate_Transformation of type Square_Root

`@Estimate_Transformation[label].type=Square_Root`. See Section 6.10 for more information.

`estimate_label` The label of the estimate block to apply transformation
Type: String
Default: No default

10.8.7 Estimate_Transformation of type Sum_To_One

`@Estimate_Transformation[label].type=Sum_To_One`. See Section 6.10 for more information.

`estimate_labels` The label for the estimates for the sum to one transformation
Type: Vector of strings
Default: No default

`upper_bound` The empirical upper bounds for the transformed parameters. There should be one

less bound than parameters
Type: Vector of real numbers (estimable)
Default: true

`lower_bound` The empirical lower bound for the transformed parameters. There should be one less bound than parameters
Type: Vector of real numbers (estimable)
Default: true

11 Observation command and subcommand syntax

The description of the methods for the observation section is given in Section 7.

In the following section, the sub-section headers use a notation of the form "**@observation[label].type=abundance**" which, in this case, represents the input command fragment

```
@observation label # where label is a unique label for that observation
type=abundance
...
```

The specific subcommands for a command are given within each command.

11.1 Observation types

The description of the observations is given in Section 7. The observation types available are:

Observations of proportions of individuals by age class

Observations of proportions of individuals by category and age class

Relative and absolute abundance observations

Relative and absolute biomass observations

Each type of observation requires a set of subcommands and arguments specific to that process.

`@Observation` *`label`* Define an object of type *Observation*. See Section 7 for more information.

`label` The label of the observation
Type: String
Default: No default

`type` The type of observation
Type: String
Default: No default

`likelihood` The type of likelihood to use
Type: String
Default: No default

`categories` The category labels to use

Type: Vector of strings
Default: true

`delta` The robustification value (delta) for the likelihood
Type: Real number (estimable)
Default: 1e-11
Lower Bound: 0.0 (inclusive)

`simulation_likelihood` The simulation likelihood to use
Type: String
Default: No default

`likelihood_multiplier` The likelihood multiplier
Type: Real number (estimable)
Default: 1.0
Lower Bound: 0.0 (inclusive)

`error_value_multiplier` The error value multiplier for likelihood
Type: Real number (estimable)
Default: 1.0
Lower Bound: 0.0 (inclusive)

`table` The table of data specifying the observed values
Type: Data table with label = obs
Default: No default
Value: A $n * m$ matrix, where $n =$ the years and $m =$ either the number of ages, lengths, or abundance/biomass observation for each year defined in the model. Each row starts with the year. The table ends with 'end_table'
Note: See 16.2 for more details on specifying data tables. The exact number of columns depends on the observation type

`table` The table of data specifying the observed error values
Type: Data table with label = error_values
Default: No default
Value: A $n * m$ matrix, where $n =$ the years and $m =$ either the number of ages, lengths, or abundance/biomass observation for each year defined in the model. Each row starts with the year. The table ends with 'end_table'
Note: See 16.2 for more details on specifying data tables. The exact number of columns depends on the likelihood type

11.1.1 Observation of type Abundance

`@Observation[label].type=Abundance`. See Section 7.1.1 for more information.

`time_step` The label of the time step that the observation occurs in
Type: String
Default: No default

`catchability` The label of the catchability coefficient (q)
Type: String
Default: No default

`selectivities` The labels of the selectivities
Type: Vector of strings
Default: true

`process_error` The process error
Type: Real number (estimable)
Default: 0.0
Lower Bound: 0.0 (inclusive)

`years` The years for which there are observations
Type: Vector of non-negative integers
Default: No default

11.1.2 Observation of type Biomass

`@Observation[label].type=Biomass`. See Section 7.1.1 for more information.

`time_step` The label of the time step that the observation occurs in
Type: String
Default: No default

`catchability` The label of the catchability coefficient (q)
Type: String
Default: No default

`selectivities` The labels of the selectivities
Type: Vector of strings
Default: true

`process_error` The process error
Type: Real number (estimable)
Default: 0.0
Lower Bound: 0.0 (inclusive)

`age_weight_labels` The labels for the `@`*age_weight* block which corresponds to each category, to use the weight calculation method for biomass calculations)
Type: Vector of strings
Default: No default

`years` The years of the observed values
Type: Vector of non-negative integers
Default: No default

11.1.3 Observation of type Process_Removals_By_Age

`@Observation[label].type=Process_Removals_By_Age`. See Section 7.1.3 for more information.

`min_age` The minimum age
Type: Non-negative integer
Default: No default

`max_age` The maximum age
Type: Non-negative integer
Default: No default

`plus_group` Is the maximum age the age plus group
Type: Boolean
Default: true

`time_step` The label of time-step that the observation occurs in
Type: Vector of strings
Default: No default

`tolerance` The tolerance
Type: Real number (estimable)
Default: 0.001
Lower Bound: 0.0 (exclusive)
Upper Bound: 1.0 (exclusive)

`years` The years for which there are observations
Type: Vector of non-negative integers
Default: No default

`process_errors` The label of process error to use
Type: Vector of real numbers (estimable)
Default: true

`ageing_error` The label of the ageing error to use
Type: String
Default: No default

`method_of_removal` The label of the observed method of removals
Type: Vector of strings
Default: No default

`mortality_instantaneous_process` The label of the mortality instantaneous process for the observation
Type: String
Default: No default

11.1.4 Observation of type Process_Removals_By_Age_Retained

`@Observation[label].type=Process_Removals_By_Age_Retained`. See Section 7.1.3 for more information.

`min_age` The minimum age
Type: Non-negative integer
Default: No default

`max_age` The maximum age
Type: Non-negative integer
Default: No default

`plus_group` Is the maximum age the age plus group?
Type: Boolean
Default: true

`time_step` The label of the time step that the observation occurs in
Type: Vector of strings
Default: No default

`tolerance` The tolerance
Type: Real number (estimable)
Default: 0.001
Lower Bound: 0.0 (exclusive)
Upper Bound: 1.0 (exclusive)

`years` The years for which there are observations
Type: Vector of non-negative integers
Default: No default

`process_errors` The label of the process error to use
Type: Vector of real numbers (estimable)
Default: true

`ageing_error` The label of the ageing error to use
Type: String
Default: No default

`method_of_removal` The label of observed method of removals
Type: Vector of strings
Default: No default

`mortality_instantaneous_process` The label of the mortality instantaneous process for the

observation
Type: String
Default: No default

11.1.5 Observation of type Process_Removals_By_Age_Retained_Total

`@Observation[label].type=Process_Removals_By_Age_Retained_Total`. See Section 7.1.3 for more information.

`min_age` The minimum age
Type: Non-negative integer
Default: No default

`max_age` The maximum age
Type: Non-negative integer
Default: No default

`plus_group` Is the maximum age the age plus group?
Type: Boolean
Default: true

`time_step` The label of the time step that the observation occurs in
Type: Vector of strings
Default: No default

`tolerance` The tolerance
Type: Real number (estimable)
Default: 0.001
Lower Bound: 0.0 (exclusive)
Upper Bound: 1.0 (exclusive)

`years` The years for which there are observations
Type: Vector of non-negative integers
Default: No default

`process_errors` The label of the process error to use
Type: Vector of real numbers (estimable)
Default: true

`ageing_error` The label of the ageing error to use
Type: String
Default: No default

`method_of_removal` The label of observed method of removals
Type: Vector of strings
Default: No default

`mortality_instantaneous_process` The label of the mortality instantaneous process for the observation
Type: String
Default: No default

11.1.6 Observation of type Process_Removals_By_Length

`@Observation[label].type=Process_Removals_By_Length`. See Section 7.1.3 for more information.

`time_step` The time step to execute in
Type: String
Default: No default

`tolerance` The tolerance for rescaling proportions
Type: Real number (estimable)
Default: 0.001
Lower Bound: 0.0 (exclusive)
Upper Bound: 1.0 (exclusive)

`years` The years for which there are observations
Type: Vector of non-negative integers
Default: No default

`process_errors` The process error
Type: Vector of real numbers (estimable)
Default: true

`method_of_removal` The label of observed method of removals
Type: String
Default: No default

`length_bins` The length bins
Type: Vector of real numbers (estimable)
Default: No default

`length_plus` Is the last length bin a plus group? (defaults to @model value)
Type: Boolean
Default: model

`mortality_instantaneous_process` The label of the mortality instantaneous process for the observation
Type: String
Default: No default

11.1.7 Observation of type Process_Removals_By_Length_Retained

`@Observation[label].type=Process_Removals_By_Length_Retained`. See Section 7.1.3 for more information.

`time_step` The time step to execute in
Type: String
Default: No default

`tolerance` The tolerance for rescaling proportions
Type: Real number (estimable)
Default: 0.001
Lower Bound: 0.0 (exclusive)
Upper Bound: 1.0 (exclusive)

`years` The years for which there are observations
Type: Vector of non-negative integers
Default: No default

`process_errors` The process error
Type: Vector of real numbers (estimable)
Default: true

`method_of_removal` The label of observed method of removals
Type: String
Default: No default

`length_bins` The length bins
Type: Vector of real numbers (estimable)
Default: No default

`length_plus` Is the last length bin a plus group? (defaults to @model value)
Type: Boolean
Default: model

`mortality_instantaneous_process` The label of the mortality instantaneous process for the observation
Type: String
Default: No default

11.1.8 Observation of type Process_Removals_By_Length_Retained_Total

`@Observation[label].type=Process_Removals_By_Length_Retained_Total`. See Section 7.1.3 for more information.

`time_step` The time step to execute in
Type: String
Default: No default

`tolerance` The tolerance for rescaling proportions
Type: Real number (estimable)
Default: 0.001
Lower Bound: 0.0 (exclusive)
Upper Bound: 1.0 (exclusive)

`years` The years for which there are observations
Type: Vector of non-negative integers
Default: No default

`process_errors` The process error
Type: Vector of real numbers (estimable)
Default: true

`method_of_removal` The label of observed method of removals
Type: String
Default: No default

`length_bins` The length bins
Type: Vector of real numbers (estimable)
Default: No default

`length_plus` Is the last length bin a plus group? (defaults to @model value)
Type: Boolean
Default: model

`mortality_instantaneous_process` The label of the mortality instantaneous process for the observation
Type: String
Default: No default

11.1.9 Observation of type Process_Removals_By_Weight

`@Observation[label].type=Process_Removals_By_Weight`. See Section **??** for more information.

`mortality_instantaneous_process` The label of the mortality instantaneous process for the observation
Type: String
Default: No default

`method_of_removal` The label of observed method of removals
Type: String
Default: No default

`time_step` The time step to execute in

Type: String
Default: No default

`tolerance` The tolerance for rescaling proportions
Type: Real number (estimable)
Default: 0.001
Lower Bound: 0.0 (exclusive)
Upper Bound: 1.0 (exclusive)

`years` The years for which there are observations
Type: Vector of non-negative integers
Default: No default

`process_errors` The process error
Type: Vector of real numbers (estimable)
Default: true

`length_weight_cv` The CV for the length-weight relationship
Type: Real number (estimable)
Default: 0.10
Lower Bound: 0.0 (exclusive)

`length_weight_distribution` The distribution of the length-weight relationship
Type: String
Default: normal

`length_bins` The length bins
Type: Vector of real numbers (estimable)
Default: No default

`length_bins_n` The average number in each length bin
Type: Vector of real numbers (estimable)
Default: No default

`units` The units for the weight bins (grams, kilograms (kgs), or tonnes)
Type: String
Default: kgs

`fishbox_weight` The target weight of each box
Type: Real number (estimable)
Default: 20.0
Lower Bound: 0.0 (exclusive)

`weight_bins` The weight bins
Type: Vector of real numbers (estimable)
Default: No default

11.1.10 Observation of type Proportions_At_Age

`@Observation[label].type=Proportions_At_Age`. See Section 7.1.1 for more information.

`min_age` The minimum age
Type: Non-negative integer
Default: No default

`max_age` The maximum age
Type: Non-negative integer
Default: No default

`plus_group` Is the maximum age the age plus group?
Type: Boolean
Default: true

`time_step` The label of the time step that the observation occurs in
Type: String
Default: No default

`tolerance` The tolerance on the constraint that for each year the sum of proportions in each age must equal 1, e.g., if tolerance = 0.1 then 1 - Sum(Proportions) can be as great as 0.1
Type: Real number (estimable)
Default: 0.001
Lower Bound: 0.0 (exclusive)
Upper Bound: 1.0 (exclusive)

`years` The years of the observed values
Type: Vector of non-negative integers
Default: No default

`selectivities` The labels of the selectivities
Type: Vector of strings
Default: true

`process_errors` The process error
Type: Vector of real numbers (estimable)
Default: true

`ageing_error` The label of ageing error to use
Type: String
Default: No default

11.1.11 Observation of type Proportions_At_Length

`@Observation[label].type=Proportions_At_Length`. See Section 7.1.1 for more information.

`time_step` The label of the time step that the observation occurs in
Type: String
Default: No default

`tolerance` The tolerance for rescaling proportions
Type: Real number (estimable)
Default: 0.001
Lower Bound: 0.0 (exclusive)

`years` The years for which there are observations
Type: Vector of non-negative integers
Default: No default

`selectivities` The labels of the selectivities
Type: Vector of strings
Default: true

`process_errors` The process error
Type: Vector of real numbers (estimable)
Default: true

`length_bins` The length bins
Type: Vector of real numbers (estimable)
Default: true

11.1.12 Observation of type Proportions_By_Category

`@Observation[label].type=Proportions_By_Category`. See Section 7.1.1 for more information.

`min_age` The minimum age
Type: Non-negative integer
Default: No default

`max_age` The maximum age
Type: Non-negative integer
Default: No default

`time_step` The label of the time step that the observation occurs in
Type: String
Default: No default

`plus_group` Use the age plus group?

Type: Boolean
Default: true

`years` The years for which there are observations
Type: Vector of non-negative integers
Default: No default

`selectivities` The labels of the selectivities
Type: Vector of strings
Default: true

`categories2` The target categories
Type: Vector of strings
Default: No default

`selectivities2` The target selectivities
Type: Vector of strings
Default: No default

11.1.13 Observation of type Proportions_Mature_By_Age

`@Observation[label].type=Proportions_Mature_By_Age`. See Section **??** for more information.

`min_age` The minimum age
Type: Non-negative integer
Default: No default

`max_age` The maximum age
Type: Non-negative integer
Default: No default

`time_step` The label of time-step that the observation occurs in
Type: String
Default: No default

`plus_group` Use the age plus group?
Type: Boolean
Default: true

`years` The years for which there are observations
Type: Vector of non-negative integers
Default: No default

`ageing_error` The label of ageing error to use
Type: String
Default: No default

`total_categories` All category labels that were vulnerable to sampling at the time of this observation (not including the categories already given)
Type: Vector of strings
Default: true

`time_step_proportion` The proportion through the mortality block of the time step when the observation is evaluated
Type: Real number (estimable)
Default: 0.5
Lower Bound: 0.0 (inclusive)
Upper Bound: 1.0 (inclusive)

11.1.14 Observation of type Proportions_Migrating

`@Observation[label].type=Proportions_Migrating`. See Section 7.1.3 for more information.

`min_age` The minimum age
Type: Non-negative integer
Default: No default

`max_age` The maximum age
Type: Non-negative integer
Default: No default

`time_step` The label of the time step that the observation occurs in
Type: String
Default: No default

`plus_group` Is the maximum age the age plus group?
Type: Boolean
Default: true

`years` The years for which there are observations
Type: Vector of non-negative integers
Default: No default

`process_errors` The process error
Type: Vector of real numbers (estimable)
Default: true

`ageing_error` The label of the ageing error to use
Type: String
Default: No default

`process` The process label

Type: String
Default: No default

11.1.15 Observation of type Tag_Recapture_By_Age

`@Observation[label].type=Tag_Recapture_By_Age`. See Section **??** for more information.

`min_age` The minimum age
Type: Non-negative integer
Default: No default

`max_age` The maximum age
Type: Non-negative integer
Default: No default

`plus_group` Is the maximum age the age plus group?
Type: Boolean
Default: true

`years` The years for which there are observations
Type: Vector of non-negative integers
Default: No default

`categories2` The available categories in the partition
Type: Vector of strings
Default: No default

`selectivities` The labels of the selectivities
Type: Vector of strings
Default: true

`time_step` The label of the time step that the observation occurs in
Type: String
Default: No default

`selectivities2` The categories of tagged individuals for the observation
Type: Vector of strings
Default: No default

`detection` The probability of detecting a recaptured individual
Type: Real number (estimable)
Default: No default
Lower Bound: 0.0 (inclusive)
Upper Bound: 1.0 (inclusive)

`time_step_proportion` The proportion through the mortality block of the time step when the

observation is evaluated
Type: Real number (estimable)
Default: 0.5
Lower Bound: 0.0 (inclusive)
Upper Bound: 1.0 (inclusive)

11.1.16 Observation of type Tag_Recapture_By_Length

`@Observation[label].type=Tag_Recapture_By_Length`. See Section 7.1.1 for more information.

`years` The years for which there are observations
Type: Vector of non-negative integers
Default: No default

`time_step` The time step to execute in
Type: String
Default: No default

`length_bins` The length bins
Type: Vector of real numbers (estimable)
Default: true

`selectivities` The labels of the selectivities used for untagged categories
Type: Vector of strings
Default: true

`tagged_selectivities` The labels of the tag category selectivities
Type: Vector of strings
Default: No default

`detection` The probability of detecting a recaptured individual
Type: Real number (estimable)
Default: No default
Lower Bound: 0.0 (inclusive)
Upper Bound: 1.0 (inclusive)

`dispersion` The overdispersion parameter (phi)
Type: Real number (estimable)
Default: 1.0
Lower Bound: 0.0 (inclusive)

`time_step_proportion` The proportion through the mortality block of the time step when the

observation is evaluated
Type: Real number (estimable)
Default: 0.5
Lower Bound: 0.0 (inclusive)
Upper Bound: 1.0 (inclusive)

11.2 Likelihoods

`@Likelihood` *`label`* Define an object of type *Likelihood*. See Section 7.2 for more information.

11.2.1 Likelihood of type Binomial

`@Likelihood[label].type=Binomial`.

The Binomial type has no additional subcommands.

11.2.2 Likelihood of type Binomial_Approx

`@Likelihood[label].type=Binomial_Approx`.

The Binomial_Approx type has no additional subcommands.

11.2.3 Likelihood of type Dirichlet

`@Likelihood[label].type=Dirichlet`.

The Dirichlet type has no additional subcommands.

11.2.4 Likelihood of type Log_Normal

`@Likelihood[label].type=Log_Normal`.

The Log_Normal type has no additional subcommands.

11.2.5 Likelihood of type Log_Normal_With_Q

`@Likelihood[label].type=Log_Normal_With_Q`.

The Log_Normal_With_Q type has no additional subcommands.

11.2.6 Likelihood of type Multinomial

`@Likelihood[label].type=Multinomial`.

The Multinomial type has no additional subcommands.

11.2.7 Likelihood of type Normal

`@Likelihood[label].type=Normal`.

The Normal type has no additional subcommands.

11.2.8 Likelihood of type Pseudo

`@Likelihood[label].type=Pseudo`.

The Pseudo type has no additional subcommands.

11.3 Defining ageing error

The methods for including ageing error into estimation for observations are:

- None
- Data
- Normal
- Off-by-one

Each type of ageing error has a set of subcommands and arguments specific to its type.

`@Ageing_Error` *`label`* Define an object of type *Ageing_Error*. See Section 7.5 for more information.

`label` The label of the ageing error
Type: String
Default: No default

`type` The type of ageing error
Type: String
Default: No default

11.3.1 Ageing_Error of type Data

`@Ageing_Error[label].type=Data`.

`table` The table of data specifying the ageing misclassification matrix
Type: A table giving the misclassification matrix
Default: No default
Value: The table has *n* rows and columns, where n is the number of ages in the model

11.3.2 Ageing_Error of type None

`@Ageing_Error[label].type=None`.

The None type has no additional subcommands.

11.3.3 Ageing_Error of type Normal

`@Ageing_Error[label].type=Normal`.

`cv` CV of the misclassification matrix
Type: Real number (estimable)
Default: No default
Lower Bound: 0.0 (exclusive)

`k` k defines the minimum age of individuals which can be misclassified, i.e., individuals of age less than k have no ageing error
Type: Non-negative integer
Default: 0
Lower Bound: 0 (inclusive)

11.3.4 Ageing_Error of type Off_By_One

`@Ageing_Error[label].type=Off_By_One`.

`p1` The proportion misclassified as one year younger, e.g., the proportion of age k individuals that were misclassified as age (k-1)
Type: Real number (estimable)
Default: No default
Lower Bound: 0.0 (inclusive)
Upper Bound: 1.0 (inclusive)

`p2` The proportion misclassified as one year older, e.g., the proportion of age k individuals that were misclassified as age (k+1))
Type: Real number (estimable)
Default: No default
Lower Bound: 0.0 (inclusive)
Upper Bound: 1.0 (inclusive)

`k` The minimum age of animals which can be misclassified, i.e., animals of age less than k are assumed to be correctly classified
Type: Non-negative integer
Default: 0
Lower Bound: 0 (inclusive)

11.4 Simulating observations

`@Simulate` *`label`* Define an object of type *Simulate*. See Section 7.6 for more information.

`label` The label for the simulation command
Type: String
Default: No default

`type` The type of simulation
Type: String
Default: No default
Value: Only the type constant is implemented

`years` The years to simulate values for
Type: Vector of non-negative integers
Default: No default

`parameter` The parameter to generate simulated values for
Type: String
Default: No default

11.4.1 Simulate of type Constant

`@Simulate[label].type=Constant`. See Section **??** for more information.

`value` The value to assign to the parameter in the simulations
Type: Real number (estimable)
Default: No default

12 Report command and subcommand syntax

The description of each report is given in Section 8.

12.1 Report commands and subcommands

`@Report` *`label`* Define an object of type *Report*. See Section 8 for more information.

`label` The report label
Type: String
Default: No default

`type` The report type
Type: String
Default: No default

`file_name` The file name. If not supplied, then output is directed to standard out
Type: String
Default: No default

`write_mode` Specify if any previous file with the same name should be overwritten, appended to, or is generated using a sequential suffix
Type: String
Default: overwrite

`format` Report output format
Type: String
Default: r
Value: Either **R** for formatting for reading into **R** or `none` for no formatting

12.1.1 Report of type Addressable

`@Report[label].type=Addressable`. See Section **??** for more information.

`parameter` The addressable parameter name
Type: String
Default: No default

`years` Define the years that the report is generated for
Type: Vector of non-negative integers
Default: No default

`time_step` Defines the time-step that the report applies to

Type: String
Default: No default
Value: A valid time step label

12.1.2 Report of type Age_Length

`@Report[label].type=Age_Length`. See Section 8.7 for more information.

`time_step` The time step label
Type: String
Default: No default
Value: A valid time step label

`years` The years for the report
Type: Vector of non-negative integers
Default: All years

`age_length` The age-length label
Type: String
Default: No default

`category` The category label
Type: String
Default: No default
Value: A valid category label

12.1.3 Report of type Ageing_Error_Matrix

`@Report[label].type=Ageing_Error_Matrix`. See Section 8.20 for more information.

`ageing_error` The ageing error label
Type: String
Default: No default

12.1.4 Report of type Catchability

`@Report[label].type=Catchability`. See Section 8.17 for more information.

`catchability` The catchability label
Type: String
Default: No default
Value: If not specified, then the label of the report is assumed to be the category label

12.1.5 Report of type Category_Info

`@Report[label].type=Category_Info`. See Section **??** for more information.

The Category_Info report has no additional subcommands.

12.1.6 Report of type Category_List

`@Report[label].type=Category_List`. See Section **??** for more information.

The Category_List report has no additional subcommands.

12.1.7 Report of type Correlation_Matrix

`@Report[label].type=Correlation_Matrix`. See Section 8.15 for more information.

The Correlation_Matrix report has no additional subcommands.

12.1.8 Report of type Covariance_Matrix

`@Report[label].type=Covariance_Matrix`. See Section 8.14 for more information.

The Covariance_Matrix type has no additional subcommands.

12.1.9 Report of type Default

`@Report[label].type=Default`. See Section 8.3 for more information.

`catchabilities` Report catchabilities
Type: Boolean
Default: false
Note: Reports all valid catchabilities

`derived_quantities` Report derived quantities
Type: Boolean
Default: false
Note: Reports all valid derived quantities

`observations` Report observations
Type: Boolean
Default: false
Note: Reports all valid observations

`processes` Report processes
Type: Boolean
Default: false
Note: Reports all valid processes

`projects` Report projects
Type: Boolean
Default: false
Note: Reports all valid projections

`selectivities` Report selectivities
Type: Boolean
Default: false
Note: Reports all valid selectivities

12.1.10 Report of type Derived_Quantity

`@Report[label].type=Derived_Quantity`. See Section 8.9 for more information.

`derived_quantity` The derived quantity label
Type: String
Default: No default
Value: If not specified, then the label of the report is assumed to be the derived quantity label

12.1.11 Report of type Equation_Test

`@Report[label].type=Equation_Test`. See Section **??** for more information.

`equation` The equation to do a test run of
Type: Vector of strings
Default: No default

12.1.12 Report of type Estimate_Summary

`@Report[label].type=Estimate_Summary`. See Section 8.10 for more information.

Value: A summary of the estimated (free parameters)

The Estimate_Summary type has no additional subcommands.

12.1.13 Report of type Estimate_Value

`@Report[label].type=Estimate_Value`. See Section 8.12 for more information.

Value: The free parameters and their values, in a format suitable for use with `-i`

The Estimate_Value report has no additional subcommands.

12.1.14 Report of type Estimation_Result

`@Report[label].type=Estimation_Result`. See Section **??** for more information.

Value: A summary of the results of the minimisation

The Estimation_Result report has no additional subcommands.

12.1.15 Report of type Hessian_Matrix

`@Report[label].type=Hessian_Matrix`. See Section 8.16 for more information.

The Hessian_Matrix report has no additional subcommands.

12.1.16 Report of type Initialisation_Partition

`@Report[label].type=Initialisation_Partition`. See Section 8.4 for more information.

The Initialisation_Partition report has no additional subcommands.

12.1.17 Report of type Initialisation_Partition_Mean_Weight

`@Report[label].type=Initialisation_Partition_Mean_Weight`. See Section **??** for more information.

The Initialisation_Partition_Mean_Weight report has no additional subcommands.

12.1.18 Report of type MCMC_Covariance

`@Report[label].type=MCM_CCovariance`. See Section **??** for more information.

The MCMC_Covariance report has no additional subcommands.

12.1.19 Report of type MCMC_Objective

`@Report[label].type=MCMC_Objective`. See Section 8.25 for more information.

The MCMC_Objective report has no additional subcommands.

12.1.20 Report of type MCMC_Sample

`@Report[label].type=MCMC_Sample`. See Section 8.24 for more information.

The MCMC_Sample report has no additional subcommands.

12.1.21 Report of type MPD

`@Report[label].type=MPD`. See Section 8.11 for more information. Value: An MPD report, consisting of the free parameters and the covariance matrix

The MPD report has no additional subcommands.

12.1.22 Report of type Objective_Function

`@Report[label].type=Objective_Function`. See Section 8.13 for more information.

The Objective_Function type has no additional subcommands.

12.1.23 Report of type Observation

`@Report[label].type=Observation`. See Section 8.18 for more information.

`observation` The observation label
Type: String
Default: No default

`normalised_residuals` Print Normalised Residuals?
Type: Boolean
Default: true
Note: Only generated if valid for associated likelihood

`pearsons_residuals` Print Pearsons Residuals?
Type: Boolean
Default: true
Note: Only generated if valid for associated likelihood

12.1.24 Report of type Output_Parameters

`@Report[label].type=Output_Parameters`. See Section **??** for more information.

The Output_Parameters report has no additional subcommands.

12.1.25 Report of type Partition

`@Report[label].type=Partition`. See Section 8.5 for more information.

`time_step` Time Step label
Type: String
Default: No default

`years` Years
Type: Vector of non-negative integers
Default: All years

12.1.26 Report of type Partition_Biomass

`@Report[label].type=Partition_Biomass`. See Section 8.6 for more information.

`time_step` The time step label
Type: String
Default: No default

`years` The years for the report
Type: Vector of non-negative integers
Default: All years

12.1.27 Report of type Partition_Mean_Length

`@Report[label].type=Partition_Mean_Length`. See Section **??** for more information.

`time_step` The time step label
Type: String
Default: No default

`years` The years for the report
Type: Vector of non-negative integers
Default: All years

12.1.28 Report of type Partition_Mean_Weight

`@Report[label].type=Partition_Mean_Weight`. See Section **??** for more information.

`time_step` The time step label
Type: String
Default: No default

`years` The years for the report

Type: Vector of non-negative integers
Default: All years

12.1.29 Report of type Partition_Year_Cross_Age_Matrix

`@Report[label].type=Partition_Year_Cross_Age_Matrix`. See Section **??** for more information.

The Partition_Year_Cross_Age_Matrix report has no additional subcommands.

12.1.30 Report of type Process

`@Report[label].type=Process`. See Section 8.8 for more information.

`process` The process label that is reported
Type: String
Default: No default
Value: A valid process label
Value: If not specified, then the label of the report is assumed to be the process label

12.1.31 Report of type Project

`@Report[label].type=Project`. See Section **??** for more information.

`project` The project label that is reported
Type: String
Default: No default
Value: If not specified, then the label of the report is assumed to be the projection label

12.1.32 Report of type Random_Number_Seed

`@Report[label].type=Random_Number_Seed`. See Section 8.22 for more information.

The Random_Number_Seed type has no additional subcommands.

12.1.33 Report of type Selectivity

`@Report[label].type=Selectivity`. See Section 8.21 for more information.

`selectivity` Selectivity name
Type: String
Default: No default
Value: If not specified, then the label of the report is assumed to be the selectivity label

12.1.34 Report of type Simulated_Observation

`@Report[label].type=Simulated_Observation`. See Section 8.19 for more information.

`observation` The observation label
Type: String
Default: No default
Value: If not specified, then the label of the report is assumed to be the observation label

12.1.35 Report of type Time_Varying

`@Report[label].type=Time_Varying`. See Section 8.26 for more information.

`time_varying` The time varying label that is reported
Type: String
Default: No default
Value: If not specified, then the label of the report is assumed to be the time varying label

13 Including commands from other files

`@include` *`file`* Include an external file

`file` The name of the external input configuration file to include
Type: string
Default: No default
Value: A valid input configuration file
Note: If `file_name` includes a space character, then it must be enclosed in quotes, for example `@include "my file.csl2"`. Also note that the `@include` does not denote the end of the previous command block as is the case for all other commands

14 Validating model values using asserts

Casal2 can validate or check certain addressables parameters as a part of testing and validation with the assert command. Asserts check the value of a specific addressables (for example, and observations, parameters, or the objective function). Asserts are one aspect of the internal tests Casal2 uses to ensure accuracy across versions and revisions (see Section 3.7)

14.1 Assert syntax

`@Assert` *`label`* Define an object of type *Assert*. See Section 3.7 for more information.

`label` The label for the assert
Type: String
Default: No default

`type` The type of the assert
Type: String
Default: No default

14.1.1 Assert of type Addressable

`@Assert[label].type=Addressable`.

`parameter` The addressable to check
Type: String
Default: No default

`years` The years to check addressable
Type: Vector of non-negative integers
Default: No default

`time_step` The time step to execute after
Type: String
Default: No default

`values` The values to check against the addressable
Type: Vector of non-negative integers
Default: No default

`error_type` Report assert failures as either an error or warning
Type: String
Default: error

14.1.2 Assert of type Objective_Function

`@Assert[label].type=Objective_Function. value` Expected value of the objective function
Type: Real number (estimable)
Default: No default

`error_type` Report assert failures as either an error or warning
Type: String
Default: error

14.1.3 Assert of type Partition

`@Assert[label].type=Partition. category` Category to check population values for
Type: String
Default: No default

`values` Values expected in the partition
Type: Vector of real numbers (estimable)
Default: No default

`error_type` Report assert failures as either an error or warning
Type: String
Default: error

15 Tips for setting up Casal2 model based on an existing CASAL model

Many users of Casal2 may be be starting with a functioning CASAL model. This section focuses on transitioning from CASAL to Casal2.

There are a range of reasons why Casal2 will output different values when comparing model output to CASAL models. There are also reasons why values will differ that are not so obvious such as, reasons caused from using different compilers on different machines where over/underflow might occur. It is assumed that the latter reasons should be rare, and the 'overall' behaviour when it comes to estimation will be the same between CASAL and Casal2.

Reasons why there may be different values reported between CASAL and Casal2 include:

- Report rounding. There are settings with respect to output in CASAL that set the number of significant figures for writing to files. So if values look truncated, this might be the reason.
- Priors on parameters that are turned off with `upper_bound` = `lower_bound`. In both CASAL and Casal2 the estimation of parameters can be turned off by setting the bounds equal. CASAL will evaluate the prior value and add this to the objective function. This contribution is a constant value so it will not affect parameter inference. It may however be confusing when comparing output between the two models.
- Default values. There are a lot of switches in these programs, and options like the `delta` in Casal2 or `r` parameter in CASAL for robustifying likelihoods can cause differences.
- The order of processes. CASAL has a predefined sequence in which it executes processes within a time step (i.e., ageing, recruitment, maturation, migration, growth, natural and fishing mortality, disease mortality, tag release events, tag shedding rate, and semelparous mortality), where as Casal2 is completely user defined.
- Length-based processes or observations. Casal2 has updated the cumulative normal distribution calculation (CASAL used the approximated no closed form solution) with better approximations.
- Age-based observations. Casal2 does not have the `sum_to_one` subcommand implemented, and CASAL makes this adjustment implicitly. Check that this flag is set to 'false' in the CASAL model for a more accurate comparison.
- Tag penalties. CASAL applies a penalty to the sum of squares on total tagged fish in a 'tagging episode' from the model compared to observed number of tagged fish. Casal2 applies a penalty on the transition rate by length. If tags are applied in a length bin that does not have individuals, e.g., a model configuration which tags 2 individuals of length l when there are no individuals in that length bin will include a penalty.

Many of the flags and options in CASAL and Casal2 are the same or similar. The syntax section of this document (Section 9) provides more details about the Casal2 functionality and behaviour. Check that the programs produce the same results with a **range** of parameter values using the deterministic run command (`casal2 -r`), before doing an estimation run (`casal2 -e`).

The first outputs to check when comparing Casal2 and CASAL versions of the same model are the stock dynamics outputs, ignoring the fits to observations. That is, check the initial age structure, the SSB and YCS values and patterns, R0, B0, etc. If these outputs differ, then the fits to the observations will likely also be different.

There are a few linkages with certain stock dynamics outputs to check to determine if processes are misspecified. Differences between the proportions in the initial age structure, assuming an equilibrium state, are due to M, natural mortality. Differences in the initial equilibrium recruitment

value, R_0, are due to growth (`@age_length` or `@length_weight`). Many models estimate B_0 so that R_0 is a back calculation through the growth curve.

If the initial age structure is the same, next check the derived quantities such as the SSB values. Differences in these values are generally caused by how fishing and recruitment processes are specified. Check which *YCS* values are estimated or standardised, the definition and designation of selectivities, etc.

Once the stock dynamics outputs match, check the results with a few different sets of starting parameter values by using the `-i` command line option. Next, check the fits to the observation data by comparing the expected values. Assuming the observations in both models match, the differences in the objective function value come from the expected values and the likelihood configurations. This is where subcommands such as the robustification values and the default values may differ between CASAL and Casal2.

Once the stock dynamics outputs and the fits to the observation data are the same, do an estimation run (`casal2 -e`). If CASAL and Casal2 do not optimise to the same parameter values, then use the parameter values from CASAL and do a deterministic run with Casal2 using the CASAL estimated parameter values (`casal2 -r -i CASAL_mpd_pars.txt`). Then check the stock dynamics outputs and the fits to the observation data and determine where the differences in the parameter estimates and outputs are.

The next question is, how close do the parameter estimates, expected values, and objective function values have to be to say that the models are equivalent? This is an ongoing topic of discussion. Previously, subjective qualitative measures have been used to decide whether the models are equivalent. A recorded comparison for the hake stock assessment can be found at Appendix B in Horn (2017).

16 Syntax conventions and examples

16.1 Input File Specification

The file format used for Casal2 is based on the command block formats used in CASAL and SPM. It is a text file that contains definitions organised into blocks.

Every object specified in a configuration file is part of a block. At the top level blocks have a one-to-one relationships with components in the system.

Example:

```
@block1 label
parameter value
parameter value_1 value 2

@block2 label
parameter value
table table_name
column_1 column_2
data_1 data_2
data_3 data_4
end_table
```

Some general notes about configuration files:

- White space can be used freely. Tabs and spaces are both valid.
- A block ends only at the beginning of a new block or at the end of the final configuration file.
- Configuration files can include other configuration files.
- Included files are placed in-line, so a block can be continued in a new file.
- The configuration files support in-line declarations of objects.

16.2 Keywords And Reserved Characters

In order to allow efficient creation of input files, the Casal2 file format has special keywords and characters that cannot be used for labels.

Labels cannot start with a double underscore — labels with a double underscore are reserved, and are used by Casal2 for automatic reports and other internal constructs.

`@Block` Definitions Each block in the configuration file must start with the block definition character, which is the "`@`" character.

Example:

```
@block1 <label>
type <type>

@block2 <label>
type <type>
```

The 'type' Keyword The 'type' keyword is used for declaring the sub-type of a defined block. Any block object that has multiple sub-types will use the `type` keyword.

Example:

```
@block1 <label>
type <sub_type>

@block2 <label>
type <sub_type>
```

 # (Single Line Comments) Comments are supported in the configuration file on one line (to the end of that line) or over multiple lines. Comments on single lines start with the "#" character.

Example:

```
@block <label>
type <sub_type> # Descriptive comment
# parameter <value_1> *** This whole line is commented out
parameter <value_1> # <value_2> *** value_2 is commented out
```

/* */ (Multiple Line Comments) Multiple line comments are supported by surrounding the comments in /* and */

Example:

```
@block <label>
type <sub_type>
parameter <value_1>
parameter <value_1> <value_2>

/*
Do not load this process
@block <label>
type <sub_type>
parameter <value_1>
parameter <value_1> <value_2>
*/
```

{} (Indexing Parameters) Individual elements of a vector can be referenced using the { } syntax. For example, when estimating `ycs_values` a range or block of YCS values can be referenced.

Example:

```
@estimate YCS
parameter process[Recruitment].ycs_values{1975:2012}
type uniform
lower_bound
upper_bound
```

':' (Range Specifier) The range specifier ":" allows specifying a range of values instead of specifying each value explicitly. Ranges can be either incremental or decremental.

Example:

```
@process my_recruitment_process
type constant_recruitment
# With the range specifier
years_to_run 1999:2009
```

```
@process my_mortality_process
type natural_mortality
# Without the range specifier
years_to_run 2000 2001 2002 2003 2004 2005 2006 2007
```

',' (List Specifier) When a parameter supports multiple values in a single entry, the list specifier "," can be used to define multiple values as a single parameter.

Example:

```
@categories
format sex.stage
# With the list specifier
names male,female.immature,mature

@categories
format sex.stage
# Without the list specifier
names male.immature male.mature female.immature female.mature
```

'table' and 'end_table' Keyword The table keyword `table` is used to define a block of values used as parameters (e.g., catch data, observations data, etc.). In many cases an appropriate table label will need to be supplied (i.e., 'obs', 'error_value', or simply 'table', depending on where used) The first line following the `table` declaration must either (1) contain a list of columns to be used, or (2) in the case of observations the data in the specified format. The subsequent lines are rows of the table. Each row must have the same number of values as the number of columns specified. The table definition must end with the "`end_table`" keyword on its own line.

Example:

```
@block <label>
type <sub_type>
parameter <value_1>
table <table_label>
<column_label_1> <column_label_2> ...  <column_label_N>
<row1_value_1>   <row1_value_2>   ...  <row1_value_N>
<row2_value_1>   <row2_value_2>   ...  <row2_value_N>
end_table
```

[ ] (in-line Declarations) When an object takes the label of a target object as a parameter, the label can be replaced with an in-line declaration. An in-line declaration "[ ]" is a complete declaration of an object on one line. This feature is designed to allow simplifying the configuration definition.

Example:

```
@model
# With in-line declaration with label specified for time step
time_steps step_one=[type=iterative; processes=recruitment ageing]

@model
# With in-line declaration with default label (model.1)
time_steps [type=iterative; processes=recruitment ageing]
```

```
# Without in-line declaration
@model
time_steps step_one

@time_step step_one
processes recruitment ageing
```

Categories The Casal2 population representation is essentially a 2-dimensional structure. The partition is:

Categories x Ages or Lengths

Each category allows for a different range of ages or lengths and accessibility during different time periods.

Because each category can be quite complicated, the syntax for defining categories has been structured to allow for complex definitions using a simple shorthand structure.

The ”format” parameter allows for defining the structure of the category labels. Using a ”.” (period) character between each segment allows for shorthand lookups of categories.

The ”names” parameter is a list of the category names. The syntax of these names is required to match the ”format” parameter so Casal2 can organise and search on them. Using the ”list specifier” and range characters this parameter can be shortened.

Example:

```
@categories
format sex.stage.tag
names male.immature.notag male.immature.2001 male.mature.notag male.mature.2001

names male.immature # Invalid: No tag information
names female # Invalid: no stage of tag information
names female.immature.notag.1 # Invalid: Additional format segment not defined

names male,female.immature,mature.notag,2001:2005 # Valid
# Without the shorthand syntax these categories would be written:
names male.immature.notag male.immature.2001 male.immature.2002
male.immature.2003 male.immature.2004 male.immature.2005 male.mature.notag
  male.mature.2001 male.mature.2002 male.mature.2003 male.mature.2004
  male.mature.2005 female.immature.notag female.immature.2001
  female.immature.2002 female.immature.2003 female.immature.2004
  female.immature.2005 female.mature.notag female.mature.2001
  female.mature.2002 female.mature.2003 female.mature.2004 female.mature.2005
```

16.3 Examples of shorthand syntax and use of reserved and key characters

Categories Casal2 allows for many user-defined categories so shorthand syntax has been added to aid in the definition of complex configuration labelling and partition structures. For example, when defining categories a comma ”,” can be used to shorten lists of categories.

This syntax is the long way:

```
@categories
format sex.stage
names male.immature male.mature female.immature female.mature
```

For the exact same partition structure specified in a shorter way:

```
@categories
format sex.stage
names male,female.immature,mature
```

Casal2 requires categories in processes and observations so that the correct model dynamics can be applied to the correct elements of the partition.

An example of a process where categories are required as an input command is for ageing

```
# 1. The standard way
@ageing my_ageing
categories male.immature male.mature female.immature female.mature

# 2. The first shorthand way
@ageing my_ageing
categories male,female.immature,mature

# 3. Wild Card (all categories)
@ageing my_ageing
categories *

# 4. The second shorthand way
@ageing my_ageing
categories sex=male sex=female
```

To combine/aggregate categories together, use the "+" special character. For example, this feature can be used to specify that the total biomass of the population is made up of both males and females.

For example,

```
@observation CPUE
type biomass
catchability Fishq
time_step one
categories male+female
selectivities FishSel
likelihood lognormal
time_step_proportion 1.0
years 1992:2001
table obs
1992    1.50    0.35
1993    1.10    0.35
1994    0.93    0.35
1995    1.33    0.35
1996    1.53    0.35
1997    0.90    0.35
1998    0.68    0.35
1999    0.75    0.35
2000    0.57    0.35
2001    1.23    0.35
end_table
```

This combination/aggregation functionality can be used to compare an observation to the total combined population:

```
@observation CPUE
type biomass
catchability Fishq
time_step one
categories *+
selectivities FishSel
likelihood lognormal
time_step_proportion 1.0
years 1992:2001
table obs
1992    1.50    0.35
1993    1.10    0.35
1994    0.93    0.35
1995    1.33    0.35
1996    1.53    0.35
1997    0.90    0.35
1998    0.68    0.35
1999    0.75    0.35
2000    0.57    0.35
2001    1.23    0.35
end_table
```

If `male` and `female` are the only categories in a population, then this is the same syntax as the command block above it.

Shorthand syntax can be useful when applying processes to a select group of categories from the partition.

For example, to apply a spawning migration to the mature categories in the partition and the partition was defined:

```
@categories
format area.maturity.tag
names north.immature.notag,2011 north.mature.notag,2011 south.immature.notag,2011
south.mature.notag,2011
```

Then, to migrate a portion of the mature population from the southern area to the northern area:

```
@process spawn_migration
type transition_category
from format=south.mature.*
to format=north.mature.*
proportions 1.0
selectivities One
```

Parameters Casal2 also allows parameters that are of type vector or map to be referenced and estimated fully or partially. An example of a parameter that is type vector is `ycs_values` in a recruitment process.

For example, a recruitment block:

```
@process WestRecruitment
type recruitment_beverton_holt
r0 400000
years
```

```
ycs_values 1 1 1 1 1 1 1 1
ycs_years 1975:1983
# An alternative method to specify a sequence of values
# use an asterix to represent a vector of repeating integers
ycs_values 1*8
steepness 0.9
age 1
```

To estimate the last four years of the parameter `process[WestRecruitment].ycs_values` only can be specified as

```
@estimate
parameter process[WestRecruitment].ycs_values{1980:1983}
type uniform
lower_bound 0.1 0.1 0.1 0.1
upper_bound  10  10  10  10
```

Note that the first element of a vector is indexed by 1. This syntax can be applied to parameters that are of type map as well. For information on what type a parameter is see the syntax section.

An example of a parameter that is of type map is `@time_varying[label].type=constant`.

For a `@time_varying` block

```
@time_varying q_step1
type constant
parameter catchability[Fishq].q
years  1992 1993 1994 1995
value  0.2 0.2 0.2 0.2
```

For example, to estimate only one element of the map (say 1992), and force all other years to be the same as the one estimate, can be done in the `@estimate` block using `same`:

```
@estimate
parameter time_varying[q_step1].value{1992}
same time_varying[q_step1].value{1993:1995}
type uniform
lower_bound 0.1 0.1 0.1 0.1
upper_bound  10  10  10  10
```

In-line declaration In-line declarations can help shorten models by passing `@` blocks (see Section 4.3).

For example,

```
@observation chatCPUE
type biomass
catchability [q=6.52606e-005]
time_step one
categories male+female
selectivities chatFselMale chatFselFemale
likelihood lognormal
time_step_proportion 1.0
years 1992:2001
```

```
table obs
1992    1.50    0.35
1993    1.10    0.35
1994    0.93    0.35
1995    1.33    0.35
1996    1.53    0.35
1997    0.90    0.35
1998    0.68    0.35
1999    0.75    0.35
2000    0.57    0.35
2001    1.23    0.35
end_table

@estimate
parameter catchability[chatTANbiomass.one].q
type uniform_log
lower_bound 1e-2
upper_bound 1
```

In the above code catchability is defined and estimated without explicitly creating a `@catchability` block.

When an in-line declaration is made, the new object will be created with the name of the creator's `label.index`, where `index` is the word "`one`" through "`nine`" if it is 1 through 9, and the number if it is 10+.

For example,

```
@mortality halfm
selectivities [type=constant; c=1]

would create
@selectivity halfm.one
```

If there are 10 categories, each with its own selectivity, the 10^{th} selectivity is labelled

```
@selectivity halfm.10
```

16.4 Processes

Processes are special in how they can be defined. Typically, specifying a process is

```
@process Recruitment
type recruitment_beverton_holt
```

However, for convenience and clarity, this block can also be specified as

```
@recruitment Recruitment
type beverton_holt
```

The difference is that the keyword `process` can be replaced with the first word of the process type. In the example above this is the `recruitment` process. This option can be used to create more succinct model configurations.

More examples:

```
@mortality Fishing_and_M
type instantaneous


@transition Migration
type category
```

16.5 An example of a simple model

This example describes a single species and area model, with recruitment, maturation, natural and fishing mortality, and an annual age increment. The population structure has ages $1-30^{+}$ with a single category.

The default Casal2 configuration filename is `config.csl2`. In this example, `config.csl2` specifies the files to include to run the Casal2 model from the current directory using the *!include* command.

```
## Include the input configuration files required
################################################

# Example input configuration file:
```

It is recommended to separate the sections of a Casal2 model for enhancing readability and error checking, and including the files in a version control system.

The file `population.csl2` contains the population information. The model years are from 1975 through 2012, with 3 time steps. The model is initialised over a 120 year period prior to 1975 and applies the following processes

- A Beverton-Holt recruitment process, recruiting a constant number of individuals to the first age class (i.e., $age = 1$).
- A constant mortality process representing natural mortality(M). This process is repeated in all 3 time steps, so that a proportion of M is applied in each time step.
- An ageing process, where all individuals are aged by one year, and with a plus group accumulator age class at $age = 30$.

Following initialisation, the model runs from the years 1975 to 2012 iterating through 3 time steps.

The first time step applies processes of recruitment, and $\frac{1}{2}M_1 + F + \frac{1}{2}M_1$ processes, where M_1 is the proportion of M applied in the first time step. The exploitation process (fishing) is applied in the years 1975 - 2012. Catches are defined in the catches table and attributes for each fishery, such as selectivity and time step they are implemented, are in the fisheries table in the `@process` block.

The second time step applies an age increment and the remaining natural mortality.

The third time step applies .

The first 28 lines of the main section of the `population.csl2`:

```
########################################
# The Population definition for the model
########################################

# The model definition. (This must be the first @command in the config files)
@model
start_year 1975
final_year 2012
projection_final_year 2025
min_age 1
```

```
max_age 30
age_plus true
base_weight_units tonnes
initialisation_phases Equilibrium_state
time_steps Sep_Feb Mar_May Jun_Aug

# Categories
@categories
format stock ## Single sex and area population
names HAK4
age_lengths age_size

@initialisation_phase Equilibrium_state
type derived

# Define the processes in the Annual Cycle
@time_step Sep_Feb
processes Recruitment Instantaneous_Mortality
```

To run the model to verify that the model runs without any syntax errors, use the command `casal2 -r`. Since Casal2 reads in the default filename `config.csl2`, this filename can be overridden. For example, if the model is in file `Mymodel.txt`, then this filename would be specified using the `-c` option, `casal2 -r -c Mymodel.txt`.

To estimate the parameters defined in the file `estimation.csl2` (the catchability constant q, recruitment R_0, and the selectivity parameters a_{50} and a_{to95}), use `casal2 -e`. The output has been redirected to file `estimate.log` using the command `casal2 -e > estimate.log`. Reports for the user-defined reports `reports.csl2` from the final iteration of the estimation are output to the file `estimate.log`, and successful convergence is printed to the screen

```
Total elapsed time: 1 second
Completed
```

The main output from the estimation run is summarised in the file `estimate.log`, and the final MPD parameter values can also be redirected as a separate report, in this case named `paramaters.out`, using the command `casal2 -e -o paramaters.out > estimate.log`.

A profile on the R_0 parameter can be run, using `casal2 -p > profile.log`. See the examples folder for the example of the output.

17 Post-processing output using R

R (https://www.r-project.org/) is the main application used to process and visualise output from a Casal2 model. **R** is free and can be downloaded from https://cran.r-project.org/. Once you have installed **R** you can install the casal2 **R** package from the file (casal2_1.0.tar.gz) which is part of the Casal2 download.

The Casal2 **R** package has functionality to parse Casal2 output into a list. It also has diagnostic, plotting, and summarising functions.

There are three types of output that Casal2 can produce, depending on the type of analysis run. These outputs are: Standard, MCMC, and Derived Quantity.

The Standard outputs are the reports that are produced in most Casal2 run modes, with the exception of -s and -m. The Standard output can be split into two additional categories, a single parameter run (casal2 -r) or a multi-parameter run (casal2 -r -i many_pars.out), or running in projection mode (-f 1). The Standard outputs can be read into **R** using the extract.mpd() function.

The second type of output is generated when doing an MCMC analysis (casal2 -m), which can generate two files, mcmc_objective.out and mcmc_samples.out. The MCMC outputs can be used to summarise convergence properties or chain behaviour, and can also be used to view marginal posteriors and quantify parameter uncertainty.

The third output type is the Derived Quantity outputs, also referred to as tabular output. The Derived Quantity output can be generated after an MCMC analysis is done, to produce the marginal posteriors for derived quantities. A commonly reported derived quantity in fisheries stock assessment modelling is the time series of spawning stock biomass. To get the posterior distributions for these derived quantities use the --tabular flag (e.g., casal2 -r -i mcmc_samples.out --tabular > Tabular_report.out). This output can then be read into **R** using the extract.tabular() function.

Casal2's reported output is written so that each @report will start with a '*' and end with '*end'. This format can be used as the basis to construct functions that read Casal2 output to identify and read individual reports for post-processing.

The Casal2 **R** extract() functions differ by how the expected output is structured and they each create a different casal2 object. The summary() and plot() functions will generate different plots for the different casal2 objects. Objects produced by the extract() function can be queried with class(object).

The list of casal2 **R** functions include:

- extract.mpd(), which parses the Casal2 default output into a list
- extract.mcmc(), which parses the Casal2 MCMC output into a list
- extract.tabular(), which parses the Casal2 tabular output into a list
- extract.parameters(), which parses the Casal2 parameter files into a list
- generate.starting.pars(), which reads in a file that contains the @estimate blocks and generates 'N' starting values to test convergence
- burn.in.tabular(), which omits the first 'N' rows from a casal2TAB object
- plot.derived_quantities(), which plots the derived quantities
- plot.selectivities(), which plots the selectivities
- plot.ycs(), which plots the true YCS strengths
- plot.pressure(), which plots the fishing pressures

- `summary()`, which summarises a model run
- `extract.csl2.file()`, which reads a Casal2 .csl2 (configuration) file into a list
- `write.csl2.file()`, which writes a Casal2 .csl2 (configuration) file to a file
- `ReadSimulatedData()`, which parses Casal2 output from a `casal2 -s` run
- `Method.TA1.8()`, which returns a weighting factor for age or length composition data. See Francis (2011) for more detail
- `apply.dataweighting.to.csl2()`, which parses a Casal2 .csl2 (configuration) file that contains `@observation` blocks, applies a weighting factor to an age or length composition data set, and generates a new `.csl2` file with modified effective sample size values

The required and optional arguments for these functions can be queried after loading the Casal2 **R** library with `library(casal2)` and using the standard **R** help syntax `?` (e.g., `?param.profile()`). Many of the help files have example code and data to demonstrate function syntax.

Standard diagnostic functions and plots for model output `plot.derived_quantity()`

When comparing model output either: different parameters for the same model structure are being compared (Situation 1), or outputs from multiple model structures are being compared (Situation 2). These functions can be useful for both comparison types.

- `plot.selectivities()`
- `plot.pressure()`
- `plot.fit()`
- `plot.ycs()`

Data weighting An important component of fisheries stock assessment modelling is addressing data conflicts through the use of data weighting. There are a range of methods that can be used (Francis (2011)). The Casal2 **R** function is `Method.TA1.8()`. An additional function `apply.dataweighting.to.csl2()` automatically applies a weighting factor to a specific age or length composition data in an `@observation` block, and generates a new `.csl2` file with modified effective sample size values.

```
library(casal2)

## read in the reported output from a "casal2 -e" run
## ensure there is a @report block for the observation of interest.
mpd <- extract.mpd(file = "estimate.log")

## calculate weighting factor from Francis method
WeightingFactor <- Method.TA1.8(model = mpd, observation_labels = "chatTANage")

## Apply the weighting factor to the block in the Observation.csl2 file
## this call generates a new file (Observation.csl2.0) with the re-weighted effective sample
    sizes
apply.dataweighting.to.csl2(weighting_factor = WeightingFactor,
                            Observation_csl2_file = "Observations.csl2",
                            Observation_label = "chatTANage",
                            Observation_out_filename = "Observation.csl2.0")
```

Automating the data weighting process:

```
library(casal2)

mpd <- extract.mpd(file = "estimate.log")
```

```
ModelFactor <- Method.TA1.8(mpd, observation_labels = c("ObserverProportionsAtAge"))

## make a back-up copy of the file Observation.csl2 before running this section

while(abs(ModelFactor - 1) > 0.01) {
  shell("betadiff & casal2 -e > estimate.log 2> log.out")

  new_mpd <- extract.mpd(file = "estimate.log")

  ModelFactor <- Method.TA1.8(new_mpd, observation_labels = c("ObserverProportionsAtAge"))

  apply.dataweighting.to.csl2(weighting_factor = ModelFactor,
                              Observation_csl2_file = "Observation.csl2",
                              Observation_out_filename = "Observation.csl2",
                              Observation_label = c("ObserverProportionsAtAge"))
  print(ModelFactor)
}
```

Troubleshooting the `casal2` R package If you get this error when using one of the `extract()` functions

```
Read 1 item
Warning messages:
1: In scan(filename, what = "", sep = "\n", fileEncoding = fileEncoding) :
embedded nul(s) found in input
2: In extract.mpd(file = "results.txt", fileEncoding = "") :
File is empty, no reports found
```

You may be able to resolve this issue by using an alternative UTF format by specifying this format with the `fileEncoding` parameter

```
MyOutput <- extract.mpd(file = "Estimate.log", path = getwd(), fileEncoding = "UTF-16LE")
```

18 Troubleshooting

Casal2 can implement complex models that provide many opportunities for error — either because the parameter files do not correctly specify the model, or because the model specified does not appear to work as expected. When in doubt, ask an experienced user. Debugging versions of Casal2 are available that can help to track down cryptic errors.

If you cannot resolve an issue using these guidelines then please contact the development team. To report an issue please follow the guidelines described in Section 18.2.1.

For most issues, Casal2 attempts to produce informative error messages. There are optional command line arguments that will give more verbose reporting, and should enable additional information to help resolve a problem. However, when Casal2 generates an error and the error message does not make sense, please let the Development Team know. Even if you manage to fix the problem yourself, we may be able to implement a more helpful error message or modify the user manual, and make life easier for the next person to encounter the problem. You can do this by submitting an issue in the GitHub repository at `https://github.com/NIWAFisheriesModelling/CASAL2/issues`.

18.1 Logging

Casal2's internal logging system can be invoked at the command line with argument `--loglevel` followed by one of the options: `trace`, `finest`, `fine`, `medium`.

The optimal level of logging will depend on what run mode you are using and the granularity of information that you would like to see. The ordering for the options is that `medium` is the most coarse, and `trace` being the finest level, with `fine` and `finest` in-between. We suggest that if you are running Casal2 in an iterative state such as for estimation (`casal2 -e`) or MCMC you use `medium` level. This is because the logging can print a lot of information for a single model run, so an estimation which could comprise thousands of model runs can produce very large text files with the finer logging option specified. For a single iteration run such as `casal2 -r` each of the logging options can be useful during different phases of model development.

For example, to enable logging with trace level output:

- On Windows: `casal2 -r --loglevel trace > output.log 2> log.out`
- On Linux: `casal2 -r --loglevel trace > output.log 2&> log.out`

This argument will output Casal2's reports to the file "output.log", and the "`2>`" or "`2&>`" syntax will print the error logged information to the file "log.out". You should be able to see where Casal2 failed, and is exited by going to the end of the "log.out" file and looking at the last few messages.

18.2 Reporting errors

If you find a bug or error in Casal2, please submit an issue in the GitHub repository at `https://github.com/NIWAFisheriesModelling/CASAL2/issues`.

Please follow the guidelines below so that the bug or error can be reproduced. It is helpful to be as detailed and specific as possible when describing the observed behaviour as well as the expected behaviour. If possible, try to reduce the input configuration file to demonstrate the error with a reduced set of commands and model structure, and aim to have as little else going on in the model as possible. This will make it faster to isolate the problem and provide a solution or fix.

18.2.1 Guidelines for reporting an error with Casal2

1. Ensure you are using the most recent version of Casal2, as the bug or error you are having may have already been resolved.
2. Provide the version of Casal2 you are using, e.g., "Casal2 v21.09 (2021-09-07)". The version is output by Casal2 with the command `casal2 -v`.
3. Provide the system you are using, e.g., "x64 Intel CPU with Microsoft Windows 10".
4. Provide a brief description of the problem, e.g., "a segmentation fault was produced".
5. If the problem is reproducible, please describe in detail the steps required to cause it, and include the Casal2 configuration files, other input files, and any output files generated. Specify the *exact* command line arguments that were used, e.g., "Using the command `casal2 -e` produced a segmentation fault. The input configuration files are attached."
6. If the problem is not reproducible (it happened only once, or occasionally for no apparent reason), please describe in detail the circumstances in which it occurred and the behaviour observed, e.g., "Casal2 crashed, but I have not been able to reproduce the issue. It seemed to be related to a local network crash but I cannot be sure."
7. If the problem produced any error messages, please give the *exact* text displayed, e.g., "`segmentation fault (core dumped)`".
8. Attach all relevant input and output files so that the problem can be reproduced; these files can be compressed into a single file e.g., a zip file, and uploaded to GitHub.

19 Casal2 software license

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