



CASAL2 User Manual

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1. Introduction

1.1. About CASAL2

CASAL2 is NIWA's open-source integrated assessment tool for modelling the population dynamics of marine species, including fishery stock assessments. CASAL2 expands functionality and increases maintainability relative to its predecessor, CASAL. CASAL2 can be used for quantitative assessments of marine populations, including fish, invertebrates, marine mammals and seabirds.

The CASAL2 software implements a generalised age-structured population model that allows for a great deal of choice in specifying the population dynamics, parameter estimation, and model outputs. CASAL2 is designed for flexibility. It can implement an age-structured model for a single population or multiple populations using user-defined categories such as area, sex, and maturity. These structural elements are generic and not predefined, and are easily constructed. CASAL2 models can be used for a single population with a single anthropogenic event (in a fish population model this would be a single fishery), or for multiple species and populations, areas, and/or anthropogenic or exploitation methods, and including predator-prey interactions.

In CASAL2 the processes in a time period and within an annual cycle are defined by the user. Observation data used for model fitting can be from many different sources, like, removals-at-size or -age from an anthropogenic or exploitation event (e.g., fishery or other human impact), research survey and other biomass indices, and mark-recapture data. Model parameters can be estimated using penalised maximum likelihood or Bayesian methods.

As well as the point estimates of the parameters, CASAL2 can calculate the likelihood or posterior distribution profiles, and can generate Bayesian posterior distributions using Markov chain Monte Carlo methods. CASAL2 can project population status using deterministic or stochastic population dynamics. CASAL2 can also simulate observations from a set of given model structures.

1.2. Citing CASAL2

The reference for this document is I. Doonan, A. Dunn, K. Large, C. Marsh, S. Rasmussen (2020). CASAL2 User Manual, v2020-07-07 (rev. b86d98a). National Institute of Water & Atmospheric Research Ltd. *NIWA Technical Report 139*. 253 p.

The peer-reviewed journal article reference for CASAL2 is ([Doonan et al., 2016](#)).

1.3. Software license

This program and the accompanying materials are made available under the terms of the GNU General Public License version 2 which accompanies this software (see [Section 17](#)).

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1.4. Where to get CASAL2

In the first instance, see <http://www.niwa.co.nz/> for information about CASAL2. The CASAL2 source code is hosted on GitHub, and can be found at <https://github.com/NIWAFisheriesModelling/CASAL2>.

There are installation packages available for Linux and Microsoft Windows. The package includes the CASAL2 executable, the **R** library, the User Manual and other documentation, example models, and other information. The installation packages can be downloaded at <https://github.com/NIWAFisheriesModelling/CASAL2/releases>.

1.5. System requirements

CASAL2 is available for most IBM compatible machines running 64-bit Linux and Microsoft Windows operating systems.

Several of CASAL2's tasks are computer intensive and a fast processor is recommended. Depending on the model implemented, some of the CASAL2 tasks can take a considerable amount of processing time (minutes to hours), and in extreme cases may take several days to complete an MCMC estimate.

Output files can be large, and the output from developing a model, sensitivity analyses, and running multiple MCMC chains can take up significant amounts of disk space. Depending on the number and type of user output requests, the output could range from a few hundred kilobytes to several hundred megabytes. When estimating model fits, several hundred megabytes of RAM may be required, depending on the spatial size of the model, number of categories, and complexity of processes and observations. For larger models, several gigabytes of RAM and disk space may occasionally be required.

1.6. Necessary files

For both 64-bit Linux and Microsoft Windows, only the binary executable `casal2` or `casal2.exe` is required to run CASAL2. No other software is required. CASAL2 is not available for 32-bit operating systems.

CASAL2 provides few functions for post-processing model output, and a package that allows tabulation and graphing of model outputs is recommended. Software such as **R** ([R Core Team, 2014](#)) is recommended for post-processing CASAL2 output. The CASAL2 **R** package is provided for parsing the CASAL2 output into **R** (see [Section 15](#)), as well as providing some diagnostic and plotting functionality.

1.7. Getting help

TODO review with the Project Manager and Project Lead

CASAL2 is distributed as unsupported software. Please notify the CASAL2 Development Team of any issues with or errors in CASAL2. Please contact the `Casal2 Development Team`. See [Section 16.2](#) for the template for reporting issues.

1.8. Technical details

CASAL2 was compiled on Linux using `gcc` (<http://gcc.gnu.org>), the C/C++ compiler developed by the GNU Project (<http://gcc.gnu.org>). The 64-bit Linux version was compiled using `gcc` version 4.8.5 20150623 on CentOS 7.7 Linux (<http://www.ubuntu.com/>).

The Microsoft Windows (<http://www.microsoft.com>) version was compiled using MingW (<http://www.mingw.org>) `gcc` 8.1.0 (<http://gcc.gnu.org>). The Microsoft Windows(<http://www.mingw.org>)

`//www.microsoft.com`) installer was built using the Inno Setup 5 (<http://www.jrsoftware.org/isdl.php>).

CASAL2 includes number of different minimisers; different minimisers may perform better for some models than others. The first three minimisers are non-automatic differentiation minimisers: the first is closely based on the main algorithm of [Dennis Jr and Schnabel \(1996\)](#), and uses finite difference gradients; the second is an implementation of the differential evolution solver ([Storn and Price, 1995](#)), based on code by Lester E. Godwin of PushCorp, Inc.; and the third is Dlib ([King, 2009](#)).

The three automatic differentiation minimisers are: ADOL-C, an auto differentiation minimiser ([Walther et al., 1996](#)); CppAD, an auto differentiation minimiser similar to ADOL-C ([Wächter and Biegler, 2006](#)); and the third is a modified version of an older version of ADOL-C (v1.8.4) that was used as the automatic differentiation minimiser in the first version of CASAL ([Bull et al., 2012](#)).

The random number generator used in CASAL2 uses an implementation of the Mersenne twister random number generator ([Matsumoto and Nishimura, 1998](#)). This functionality, the command line functionality, matrix operations, and a number of other functions use the Boost C++ library (Version 1.58.0).

The output from CASAL2 may differ slightly on the different operating systems and operating system versions due to different precision arithmetic or other platform-dependent implementation details. The source code for CASAL2 is available in the GitHub repository at <https://github.com/NIWAFisheriesModelling/CASAL2>.

Unit tests of the underlying CASAL2 code are carried out at build time, using the Google Test and Mock unit testing and mocking framework. The unit test framework aims to cover a significant proportion of the key functionality within the CASAL2 code base. The unit test code for CASAL2 is available as a part of the underlying source code.

2. Model overview

CASAL2 is a generalized age-structured population dynamics modelling framework of the integrated assessment type (Maunder and Punt, 2013). It allows several sources of information to be combined into a single analysis using a statistical framework so that error sources are fully propagated into the uncertainty in the results. The model follows cohorts as numbers-at-age through time recording changes from processes acting on them such as nature mortality and fishing.

CASAL2 is run from the console window on Microsoft Windows or from a terminal window on Linux. CASAL2 has two sources of information: the *input configuration file* which defines the model structure, provides observations, defines active parameters, and specifies outputs (reports); and run time actions (e.g., estimation of active parameters or projections) which are given by command line options and arguments (see Section 3 for details).

The model is defined in terms of the *state* at various points in the annual cycle within each year. The annual cycle defines the time steps within a year and the order of processes. The state consists of two parts, the *partition*, and any defined *derived quantities*. The partition will typically change in each *time-step* of every year, depending on the *processes* defined for those time-steps in the model.

The *partition* is a representation of the population at each time step, and can be considered a matrix of the numbers of individuals within each category (i.e., row) and at each age. Categories define the important population structure, such as whether a fish is male or female, in a specific area, and its maturity state, but other divisions are also possible like stock, or even species. How many categories there are and what they represent are entirely defined by the user as CASAL2 does not have any hard-wired fisheries concepts. The latter is one reason for re-writing CASAL (CASAL2's precursor), but the increased flexibility does come at a cost of more complex input files complexity.

A *derived quantity* is a calculation of a selected part of the partition at some point in time, an example is spawning stock biomass (SSB). Unlike the partition, which is updated as each new time step, a derived quantity records a single value for each year of the model run. Hence, derived quantities build up a vector of values over the time period represented by the model. The derived quantity is then available to be reported or as an input into another process at some point in a subsequent year. The most common use is using SSB from a previous year in the stock-recruitment relationship to determine numbers into the first age of the partition. Another example might be having age-at-maturity inversely related to the largest size of recruitment in the previous four years.

Observations, their sampling distributions, relationship with the partition, and time sampled (time step and year) are specified in the input configuration file. Examples are abundance indices from a research trawl survey or age compositions from the commercial catch. The relevant state can now be linked to the observation which then can generate expected values for the observations. In broad terms, the model parameters can be optimised to provide the best fit between expected values and the observations. Best fit is judged by the lowest negative log-likelihood, for which a special case would be the sums-of-squares. The manner in which observations are evaluated and how the expected values are calculated by the model is described in Section 6.

The model scope and population structure are specified in the input configuration file and this is similar to that in CASAL (Bull et al., 2012), but with a different syntax. The model records the numbers of individuals by category and age (e.g., for a sex category, the numbers of males and females at age). In general, cohorts are added via a recruitment event, are aged annually, and are removed from the population via various forms of mortality (e.g., fishing or natural mortality). The population is assumed to be closed (i.e., no immigration or emigration from the modelled area). REPEAT?

By convention, the input configuration file is a file named `config.csl2` which reads in four other

files so that assessment specifications are more digestible (one comprehensive file can be used instead and users do not have to use the name `config.csl2`). These subordinate files cover (again by convention): the model structure, population dynamics, etc. (Section 4); the methods of estimation, priors, penalties, and the model parameters to be estimated (Section 5); the observation data, their associated likelihoods, and their timing (Section 6); and the outputs from the model (default is no outputs) (Section 7). The input configuration file completely describes a model implemented in CASAL2. See Sections 8, 9, 10, and 11 for details and specification of CASAL2's command and subcommand syntax within the input configuration file.

3. Running CASAL2

CASAL2 is run from a console window (i.e., the command line) on Microsoft Windows or from a terminal window on Linux. CASAL2 uses information from input data files -- the *input configuration file* being the input file that is supplied to CASAL2.

The input configuration file is required and defines the model structure, processes, observations, parameters (both the fixed parameters and the parameters to be estimated), and the requested reports (outputs).

By convention, the name of the input configuration file ends with the suffix `.csl2`. However, any suffix is acceptable. The default name for the input configuration file is `config.csl2` and if used it does not have to be specified to CASAL2. Note that the input configuration file can include other separate files so the specification can be split into digestible parts.

Command line arguments are used to specify the actions or *tasks* of CASAL2, e.g., to run a model with a set of parameter values, to estimate parameter values (either point estimates or MCMC), to project quantities, or to simulate observations. For example, `-r` is the *run* mode, `-e` is the *estimation* mode, and `-m` is the *MCMC* mode. The *command line arguments* are described in Section 3.3.

3.1. Using CASAL2

To use CASAL2, open a console window (i.e. the command prompt) window on Microsoft Windows or a terminal window on Linux. Navigate to the directory where the model input configuration files are located. Then enter `casal2` with arguments for a specific mode to start the CASAL2 mode running; see Section 3.3 for the list of possible arguments. CASAL2 will print output to the screen.

The CASAL2 executable and shared libraries (files with extension `.dll` or `.so`) must either be in the same directory as the input configuration files or in one of the directories in your operating system's `PATH` environment variable. The CASAL2 installer will update `PATH`; see your operating system documentation for help displaying or modifying `PATH`.

3.2. Redirecting standard output

CASAL2 uses the standard output stream to display runtime information. The standard error stream is used by CASAL2 to output the program exit status and runtime errors. We suggest redirecting both the standard output and standard error into files.

With the bash shell (on Linux systems), you can do this using the command structure

```
(casal2 [arguments] > run.out) >& run.err &
```

It may be useful to redirect the standard input, especially if you're using CASAL2 inside a batch job, i.e.

```
(casal2 [arguments] > run.out < /dev/null) >& run.err &
```

On Microsoft Windows systems, you can redirect to standard output using

```
casal2 [arguments] > run.out
```

And, on some Microsoft Windows systems (e.g., Windows 10), you can redirect to both standard output and standard error, using the syntax

```
casal2 [arguments] > run.out 2> run.err
```

CASAL2 outputs header information to the output (Figure 3.1). The header consists of the program name and version, the arguments passed to CASAL2 from the command line, the date and time that the program was called (derived from the system time), the user name, and the machine name (including the operating system and the process identification number). This information can be used to track outputs as well as identifying the version of CASAL2 used to run the model.



Figure 3.1: Example of output file header information.

3.3. Command line arguments

CASAL2 is called using:

```
casal2[-c config_file] [task] [options]
```

where

-c *config_file* Define the input configuration file for CASAL2 (if this argument is omitted, the default input configuration file is `config.csl2`)

and where *task* must be one of the following ([] indicates a secondary label to call the task, e.g. **-h** will execute the same task as **--help**),

-h [--help] Display help (this page)

-l [--licence] Display the reference for the software license (GPL v2)

-v [--version] Display the CASAL2 version number

-r [--run] Run the model once using the parameter values in the input configuration file, or optionally with the parameter values from the file specified with argument **-i *filename***

-e [--estimate] Do a point *estimate* using the values in the input configuration file as the starting point for the parameters to be estimated, or optionally with the starting parameter values from the file specified with the argument **-i *filename***. By default, it generates the file `mpd.out` with the estimated parameters and the covariance matrix; use **[--no-mpd]** to stop creating this file

- [-p-profiling]** Do a likelihood *profile* using the parameter values in the input configuration file as the starting point, or optionally with the starting parameter values from the file specified with the argument `-i filename`
- m [--mcmc]** Do an *MCMC* chain. The the co-variance matrix is first estimated using the values in the input configuration file as the starting point for the parameters to be estimated, or optionally with the starting parameter values from the file specified with the argument `-i filename`. Use `-skip-estimation` to skip estimating the co-variance matrix and to read it in from `mpd.out`.
- f [--projection] arg.** Project the model *forward* in time using the parameter values in the input configuration file as the starting point for the estimation, or optionally with the parameter values from the file specified with the argument `-i filename`. Repeat each parameter set *arg* times (default 1). Normally, the MCMC sample are used via `-i`
- s [--simulation] number** Simulate the *number* of observation sets using values in the input configuration file as the parameter values, or optionally with the parameter values from the file specified with the argument `-i filename`

and where the following optional arguments [*options*] may be specified

- i [--input] filename** Input one or more sets of free (estimated) parameter values from *filename* (see Section 11 for details about the format of *filename*)
- o [--output] filename** Output a report of the free (estimated) parameter values in a format suitable for `-i filename` (see Section 11 for details about the format of *filename*)
- g [--seed] seed** Initialise the random number *generator* with *seed*, a positive (long) integer value (note, if `-g` is not specified, then CASAL2 will generate a random number seed based on the computer clock time)
- loglevel** *arg* = {trace, finest, fine, medium} (see Section 7)
- tabular** Run with `-r` or `-f` command to print `@report` in tabular format (see Section 7)
- single-step** Run with `-r` to pause the model and ask the user to specify parameters and their values to use for the next iteration (see Section 3.6)
- [--resume]** Resume a MCMC chain
- [--objective-file] arg.** Objective file for resuming an MCMC is *arg*
- [--sample-file] arg.** Sample file for resuming an MCMC is *arg*
- [--skip-estimation]** For `[-mcmc]` run, skip estimating the covariance matrix; take it from the file `mpd.out`. This is a way use a re-calculated covariance matrix based on a previous MCMC run and start a new chain
- [--no-mpd]** For `-e [--estimate]` run, do not create the MPD file, `mpd.out`
- q [--query] object type** Query an object type to print an extract of the object description and parameter definitions. An object can be defined as *block.type*, e.g. `casal2 --query process.recruitment_constant` will query the constant recruitment block.

3.4. Constructing the CASAL2 input configuration files

By convention, the input configuration file is a stub that names four other files that cover four broad sections:

- the description of the population structure, dynamics, and parameters (population.csl2, Section 4),
- the estimation methods and estimated variables (estimation.csl2, Section 5),
- the observations and their associated properties and likelihoods (observation.csl2, Section 6), and
- the results that CASAL2 will output (reports.csl2, Section 7).

The way to do the above is to use the command `!include "filename"` (Figure 3.2). This command specifies that another file, `filename`, be read and processed, exactly as if its contents had been inserted into the main input configuration file at that point. The file name must be the complete file name with extension, and can use either the relative or absolute path as part of its name. Included files can also contain `!include` commands. See Section 12 for more detail.



Figure 3.2: Example of using the input configuration file command `!include "filename"`.

The command and subcommand syntax to be used in each of these configuration sections are listed in Sections 8 (Population), 9 (Estimation), 10 (Observation) and 11 (Report).

3.4.1. Commands

CASAL2 has a range of commands that define the model structure, processes, parameters, observations, and how tasks are carried out. There are three types of commands

- Commands that have an argument and do not have subcommands (for example, `!include filename`)
- Commands that have a label and subcommands (for example `@process` must have a label and has subcommands)
- Commands that do not have either a label or argument, but have subcommands (for example `@model`)

Apart from `!include`, commands start with an `@` in column 1. Otherwise, inputs are free form. The `@` is important as it signals the start of a command block which is the basic unit in the input files (see sub-section ??).

Commands that have a label must have a unique label, i.e., the label cannot be used on more than one command of that type so that it can be referenced in other parts of the input configuration file. The labels can contain alpha numeric characters, period ('.'), underscore ('_') and dash ('-'). Labels

must not contain whitespace (tabs or spaces) or other characters that are not letters, numbers, dash, period, or an underscore. For example,

```
@process NaturalMortality
or
!include MyModelSpecification.csl2
```

3.4.2. Subcommands

CASAL2 subcommands define options and parameter values related to a particular command. Subcommands always take an argument which is one of a specific *type*. The argument *types* acceptable for each subcommand are defined in Section 12, and are summarised below.

Like commands (@command), subcommands and their arguments are not order specific, except that that all subcommands of a given command must appear before the next @command block. CASAL2 may report an error if they are not supplied in this way. However, in some circumstances a different order may result in a valid, but unintended, set of actions, leading to possible errors in the expected results.

The argument type for a subcommand can be:

switch	true/false
integer	an integer number
integer vector	a vector of integer numbers
integer range	a range of integer numbers separated by a colon, e.g. 1994:1996 is expanded to an integer vector of values (1994 1995 1996)
constant	a real number (i.e., a double)
constant vector	a vector of real numbers (i.e., a vector of doubles)
estimable	a real number that can be estimated (i.e., a double)
estimable vector	a vector of real numbers that can be estimated (i.e., a vector of doubles)
addressable	a real number that can be referenced but not estimated (i.e., an addressable double)
addressable vector	a vector of real numbers that can be referenced but not estimated (i.e., a vector of addressable doubles)
string	a categorical (string) value
string vector	a vector of categorical values.

Switches are characteristics which are either true or false. Enter *true* as true or t, and *false* as false or f.

Integers must be entered as whole numbers without decimal points (i.e., if year is an integer then it is specified as 2008, not 2008.0)

Arguments of type integer vector, constant vector, estimable vector, addressable vector, or categorical vector must contain one or more entries on a row, separated by whitespace (tabs or spaces). Arguments of type integer range must contain a colon (:) and no whitespace (tabs or spaces).

Parameters are defined in the population section and can be specified as estimable with the subcommand type estimable or estimable vector. These parameters will be estimated if specified as such in the estimation section. If an estimable parameter is not specified in the estimation section it will instead be treated as a constant (or constant vector). In other words, only estimable parameters can be estimated and the parameter command must explicitly specify that the parameter is estimable with the estimable or estimable vector subcommand type. CHECK THIS?????

Parameters defined as addressable with the subcommand type addressable or addressable

vector are usually derived quantities and are not directly estimable. As such, they can be referenced by various processes, or have priors and/or penalties associated with them, but they do not directly contribute to any estimation within the model. WHAT IS ADDRESSABLE???

3.4.3. The command block format

The command block is a basic continuous unit within the input file(s). It begins with a line that starts with the symbol @, juxtaposition against a single command and followed, if required, by any unique label or argument. There is no indicator of the end of a command block. Each command block is delimited by the end of the file or the start of the next command block (which is marked by the @ on the first character of a line). The !include command is the only exception to this rule (see Section 12 for details of the use of !include). The !include command can be used to include contents of another file within the scope of the command block.

Within the command block, any subcommands needed and their arguments are presented, e.g.,

@command	@command argument	@command label
subcommand argument	subcommand argument	subcommand argument
subcommand argument	subcommand argument	subcommand argument
.	.	.
.	.	.
etc.	etc.	etc.

Subcommands can be in any order within the command block. Command blocks can be in any order within the input files, except @model which must be the first command block encountered by CASAL2 since this scopes the basic model dimensions (but excluding the !include command).

Blank lines are ignored, as is extra whitespace (tabs and spaces) between arguments. However, to start command block the @ character must be the first character on the line and must not be preceded by any whitespace. Each input file must end with a carriage return.

Commands, subcommands, and arguments in the input configuration files are not case sensitive. However, labels and variable values are case sensitive. On Linux, filenames and paths are case sensitive (i.e., when using !include filename, the argument filename will be case sensitive).

3.4.4. Commenting out lines

Text on a line that starts with the symbol # is considered to be a comment and is ignored. To comment out a group of commands or subcommands, use # at the beginning of each line to be ignored.

Alternatively, to comment out an entire block or section, use /* at the beginning of a line to start the comment block, then end the block with */. All lines (including line breaks) between /* and */ inclusive are ignored.

```
# This line is a comment and will be ignored
@process NaturalMortality
m 0.2
/*
This block of text
is a comment and
```

```
will be ignored
*/
```

3.4.5. How to reference parameters

Parameters need an unique name so it can be referenced in other command blocks, e.g., specifying it to be estimated, to apply a penalty, specifying values to use in projections, making it time varying, or profiling.

When CASAL2 processes the input configuration file it translates each command block and each subcommand block into a CASAL2 object, each with a unique parameter name. For commands, this parameter name is simply the command label. For subcommands, the parameter name format is one of the following:

```
command[label].subcommand if the command has a label, or
command.subcommand if the command has no label, or
command[label].subcommand{i} if the command has a label and the subcommand arguments
are a vector, and we are accessing the ith element of that vector.
command[label].subcommand{i:j} if the command has a label, and the subcommand arguments
are a vector, and we are accessing the elements from i to j (inclusive) of that vector.
```

For example, the parameter name of the natural mortality rates subcommand `m` of the command `@process` with the label `NaturalMortality` and there is a different rate for males and females has the form to reference both rates as a vector is

```
process[NaturalMortality].m, but to reference just the male rate then the form is
process[NaturalMortality].m{male}.
```

All labels (parameter names) are user specified. As such, naming conventions are non-restrictive and can be model specific.

3.5. Reading a command block

Here, we illustrate reading a command block using two important commands, `@process` and `@estimate`.

The command `@process` specifies a process that can be used in the model. There are a fixed set of predefined processes (subroutines in C++ code). The way to identify which one is by the `type` subcommand. Processes can take one or more parameters and some will need other data to be applied too. Some parameters are mandatory and others can take a default value if they are not specified. We have categories `male` and `female`, and two fisheries, `line` and `pot`. The command block starts with a `@process`:

```
@process Fishing
type mortality_instantaneous
```

This sets up a process block using the `mortality_instantaneous` process which simultaneously depletes the population by natural mortality and from two types of fishing. Its label is `Fishing`. Next we specify the values for natural mortality (`m`) an argument to this process, to 0.17 and specify that fisheries acts on all categories. Note there are two values for natural mortality, one for each sex. The parameters `m` can be estimated, if required. The command block fragment is:

```
m 0.17 0.17 #natural mortality for each category
categories * # fishing acts on all categories ("*" shorthand for male female)
```

Catches are supplied via a *table* format using three columns: year and two for the fisheries, one for each, which take the labels *line* and *pot*. Column names are on the first line of the table and these columns can be in any order. e.g

```
#catches
table catch          # define catches by fishery in table format
year line pot        #names columns so can identity catch for each fishery
2000 1000 2000       # catches by year
2001 500 1000
2002 1000 5000
end_table            # end of table marker
```

Other information needed are supplied in the methods table which has a fixed number of columns (again these can be in any order), one for each piece of information needed to model a fishery. The method column defines the fishery name which is used in the catch table and also in other observations like age composition from that fishery. The categories that the fishery operates on (all in this case, but it could be just males for one and females for the other) are in the category column, the fishing selectivity to be used is given as a selectivity block name which is define somewhere else in the files, *u_max* is the maximum exploitation rate in any year that is allowed, next comes the time step the fishing operates in, and lastly the block name of a penalty function that is used to penalise estimable parameter values that result in the supplied catch not being caught. Again, the penalty block is define elsewhere in the files. After the row with the column names, there follows one row for each fishery. e.g

```
table method          # supply arguments and name selectivity etc
method category selectivity u_max time_step penalty
pot * potFSel 0.7 1 CatchMustBeTaken1
line * lineFSel 0.7 1 CatchMustBeTaken1
end_table
```

To estimate natural morality, you need to supply an *@estimate* block with a reference name back to *m* in the *Fishing* block. For *@estimate*, *type* specifies the prior to be used in the estimation, which in this case is a normal distribution. The block is:

```
@estimate estimate.m
type normal normal
parameter process[fishing].m #
  \*Fishing is unique amongst the @process command blocks
  so this defines the unique reference to the parameter m
  *\

mu 0.2 0.2 #argument to prior = mean
sd 0.02 0.02 #another argument to the prior = standard deviation
```

Note that there are two *ms*, one for each sex, so there has to be two priors. The *estiamte* label *estimate.m* is often redundant, but it may be needed , e.g., in a transformation command block.

To estimate a common *m* over both sexes, we estimate one *m*, say male, and use the *same* subcommand to apply the same value to the female *m*, e.g.,

```
@estimate estimate.m
```

```
type normal
parameter process[fishing].m{1} #male M since males are first in the category order
same process[fishing].m{2}      #{} is used to index one or more elements in a vector
mu 0.2 #argument to prior = mean
sd 0.02 #another argument to the prior = standard deviation
```

There are section detailing the equations involve and a separate syntax section that gives the possible types and their subcommands. Note that the syntax sections are auto-generated from the code base (i.e., from the constructors) so they give the definitive set of subcommands and their names.

3.6. Single-stepping CASAL2 SHIFT TO SOMEWHERE ELSE

Single-stepping means CASAL2 can ‘pause’ after each year in the annual cycle during a model run, write reports, then wait and process user input of updated estimable parameters for the next year (see the command line argument `--single-step`).

This enables CASAL2 to implement models for management simulations or scenarios that require feedback and can be used, for example, in operational management procedures (OMPs). The single-stepping process can be automated using **R**, so that CASAL2 may be used with **R** to update input harvest values (e.g., catches from a fishery in a fisheries model) to evaluate a particular harvest control rule.

3.7. CASAL2 exit status values

When CASAL2 is run, it will complete its task successfully or output errors. CASAL2 will return a single exit status value ‘completed’ to the standard output. Error messages will be printed to the console. When input file configuration errors are found, CASAL2 will print error messages, along with the associated filename(s) and line number(s) where the errors were identified, for example,

```
#1: At line 15 in Reports.csl2: Parameter '{}' is not supported
```

4. The population section

4.1. Introduction

The population section specifies the model of the population dynamics. It describes the model structure, the population partitions and categories, the population processes (e.g., recruitment, ageing, migration, and mortality), the selectivities, and the associated parameters.

The population section includes:

- The population structure, the categories and ages in an age-based model;
- The initialisation process, the state of the partition at the start of the first year;
- The years over which the model runs, the start and end years of the model;
- The annual cycle, the number of time steps and the processes that are applied in each time step;
- The specification of and the parameters for the population processes, processes that add or remove individuals from a partition, or shift individuals between ages and categories in a partition;
- The selectivities;
- The parameters, their definitions, initial values, prior distributions, and other characteristics; and
- Derived quantities, e.g., mature biomass to include in density-dependent processes such as the spawner-recruit relationship

4.2. Population structure

The basic structure of the population section of a CASAL2 model is defined in terms of an annual cycle, time steps, states, and transitions.

The annual cycle defines what processes happen in each model year, and in what sequence. CASAL2 assumes an annual cycle.

Each year is defined by one or more time steps, with at least one process occurring in each time step. Each time step can represent a specific period of the calendar year, or it can be an abstract sequence of events.

The division of the year into time steps allows the user to specify the exact order in which processes and observations occur throughout the year. The user specifies the time step in which each process occurs. If more than one process occurs in the same time step, the order in which to apply each process is specified in the `@time_step` block.

The mortality processes are grouped into a mortality block: in every time step, a mortality block (a group of consecutive mortality-based processes) exists in which individuals are removed from the partition (see Section 4.4.2).

The state is the current status of the population at any given time. The state can change one or more times in each time step in each year. The state object must contain sufficient information to determine how the population changes over time, given a model and a complete set of parameters.

The state can undergo a number of possible changes during the annual cycle, called transitions. Transitions are applied by processes. Transitions include recruitment, natural mortality, fishing

mortality, ageing, migration, tagging events, and maturation. These transitions are repeated for each year of the model, although some processes can be specified to occur in a subset of years only.

The key element of the state is the partition. The partition separates the total number of individuals in the population into different ages, lengths, and/or categories. The categories include sex, maturity state, area, and species. CASAL2 has no predefined categories; *all* categories are defined by the user, which differs from CASAL (Bull et al., 2012).

The partitions can be conceptualised as a matrix, where each row represents a category and the columns are the age classes (Figure 4.1). Each row represents all individuals that category.

The names of categories are user defined. There must be at least one category defined for each model. The model ages are a sequence from age_{min} to age_{max} , with the last age optionally a plus group. The age-length relationship for each category must also be defined for an age-based model, although this relationship could be defined as "none". An example of four categories based on sex and area is:

```
@categories
format mature.sex
names      spawn.male  spawn.female  nonspawn.male  nonspawn.female
age_lengths male_AL    female_AL     male_AL        female_AL
```

Consider a model of a fish population with a mature fishery and a non-spawning fishery. Assume that the non-spawning fishery occurs in the non-spawning area. The mature fish then migrate to the spawning area, where the spawning fishery occurs. At the end of spawning, these fish, along with the recruits from the previous year, migrate back to the non-spawning area. The fish population can be represented with partitions by age, sex, maturity, and area (spawning and non-spawning areas). So the partition has 8 rows of numbers-at-age, for 2 sexes \times (mature or immature) \times 2 areas.

	first age bin							last age bin
Spawning male immature								
Spawning male mature								
Spawning female immature								
Spawning female mature								
Non-spawning male immature								
Non-spawning male mature								
Non-spawning female immature								
Non-spawning female mature								

Figure 4.1: A visual representation of a partition.

For this example four time steps are defined and labelled 1 through 4: *step1* for the non-spawning fishery period, *step2* for the migration to the spawning area, *step3* for the spawning fishery period, and *step4* for recruitment and migration back to the non-spawning area. The default order of processes within a time step has migrations occurring before fisheries (TODO: check this), so that the processes in steps 2 and 3 could have occurred in one time step. Other details that describe the

population structure are also linked to time steps, such as proportion of natural mortality occurring in each time step and in which time step the observations occur.

The definition and ordering of processes in multiple time steps can be used to represent complex dynamics, with the intermingling of multiple species and stocks, migration patterns occurring over multiple areas, and/or multiple sources of anthropogenic impact using a range of methods which cover different areas and times. However, the complexity of a stock structure definition is constrained by the available data. It is challenging to use a complex structure to model a population when there are no observations to support that structure. For information on how to define categories and use the shorthand syntax see Section 14.2.

The model is run from the start year through the final year. It can also be run past the final year to project the state of the population through the final projection year.

To specify a model with two categories, male and female, population ages 1-20, with the last age a plus group, three time steps, and sex-specific age-length relationships, the `@model` and `@categories` blocks are:

```
@model
start_year 1901
final_year 2000
projection_final_year 2010
base_weight_units tonnes
min_age 1
max_age 20
age_plus_group true
initialisation_phases Equilibrium_phase
time_steps step1 step2 step3

@categories
format sex
names male female
age_lengths male_growth female_growth
```

4.3. The state object and the partition

The key component of the state object is the partition, a matrix that stores the numbers of individuals at age or length for each category. A category represents a group of individuals that have the same attributes, e.g., life histories characteristics, growth rates, etc.

- Sex (male or female)
- Area
- Maturity (immature or mature)
- Growth path
- Tagging event
- Stock
- Species

A stock is defined as a population of individuals which recruits to that population. Maturity can either be defined as a separate category in the partition, or calculated from the population at the time required; see Section 4.11 for the treatment of maturity when maturity is not a category in the partition.

Each CASAL2 model requires:

- The minimum and maximum population ages
- Whether the maximum age is a plus group
- The names of all of the categories

The age range is sequential by 1 starting with the minimum age through the maximum age.

CASAL2 allows categories of the partition to exist for a subset of years of a model. This feature enables more efficient computations when models contain categories that do not persist over all model years. A model may define one-off processes that transition individuals from one category into another in a subset of the model initialisation phases or years (e.g., tagging events). Excluding categories for certain years can be more efficient as CASAL2 will not initialise these categories or apply processes to categories in years or time steps in which they do not exist.

The structure of the partition is defined in a configuration block with the `@categories` block (Section 4.2).

Derived quantities are another important component of the state object. An example of a derived quantity is spawning stock biomass (SSB; the biomass of [female] spawning fish calculated at the mid point of the spawning season). CASAL2 calculates derived quantities using the command `@derived_quantity`, which may be required for some processes. In fisheries stock assessment models, a recruitment process which includes a stock-recruitment relationship requires the definition of a derived quantity that specifies the mid-season spawning stock biomass.

4.4. Time sequences

The time sequence of the model is defined in:

- The annual cycle
- The mortality blocks
- The initialisation phases
- The model run years
- The projection years

4.4.1. The annual cycle

The annual cycle is implemented as a set of processes that occur in a user-defined order within each year. Time steps are used to break the annual cycle into separate components and allow observations to be associated with specific time periods and processes. Any number of processes can occur within each time step, in any order, although there are restrictions for mortality-based processes (see Section 4.4.2); processes can occur multiple times within each time step. Time steps are not implemented during the initialisation phases (effectively there is only one initialisation time step), and the annual cycle in the initialisation phases can be different from the annual cycle specified for the model years.

4.4.2. The mortality blocks

There is an associated *mortality block* for every time step in the annual cycle. Mortality blocks are a key concept in CASAL2.

Mortality blocks are used to define the "point" in the model time sequence when observations (see Section 6) are evaluated, and derived quantities (see Section 4.6) are evaluated.

A mortality block is defined as a consecutive sequence of mortality processes within a time step. The mortality processes are described in Subsection 4.5.3.

CASAL2 requires that each time step has exactly one mortality block. Either all of the mortality processes in a time step must be sequential (i.e., there can not be a non-mortality process between any two mortality processes within any one time step); or, if no mortality processes occur in a time step, then the mortality block is defined to occur at the end of the time step.

CASAL2 will output an error if more than one mortality block occurs in a single time step. Use separate time steps to define a sequence of mortality blocks.



Figure 4.2: A example sequence for an annual cycle.

4.4.3. The initialisation phases

Initialisation is the process of determining the model starting state. The initial state can be equilibrium/steady state or some other initial state for the model (e.g., exploited), prior to the start year of the model.

There are multiple options for partition initialisation in CASAL2, including

- Iterative
- Derived
- Cinitial
- Fixed

Model initialisation can also occur in several phases, each of which can use a different method. The initialisations are performed in sequence. At the end of all of the initialisation phases, CASAL2 then

runs through the model years applying the user-defined processes in each time step in the annual cycle.

The multi-phased initialisation allows for flexibility in the number and type of initialisations, for initialising a non-equilibrium starting state, or applying simple processes before applying more complex ones.

Each phase of the initialisation defaults to have the same processes and in the same order as defined in the annual cycle. An initialisation phase can include other processes with the `insert_processes` subcommand.

In each initialisation phase, the processes defined for that phase are applied and used as the starting point for the following phase or, if it is the last phase, the start year of the model.

The *first* initialisation phase is always initialised with each age and category set to zero. Care must be taken when using complex category inter-relationships or density-dependent processes that depend on a previously calculated state, as they may fail when used in the first phase of an initialisation.

Multi-phase iterations can also be used to determine if an initialisation has converged. A second initialisation phase can be added for 1 year, with the same processes applied as in the first phase. The state at the end of the first and second phase is then output. If these states are identical, then it is likely that the initialisation has converged to an equilibrium state.

The subcommands for including or excluding processes are `insert_processes` and `exclude_processes`.

For the `insert_processes` the syntax is:

```
insert_processes time_step_label(process_label_in_annual_cycle) = label_new_process
```

For example, this subcommand could be used in a `@time_step` labelled `Oct_Nov`, which includes the `@process` labelled `predationInit`, and before the `@process` labelled `Instantaneous_Mortality`,

```
insert_processes Oct_Nov(Instantaneous_Mortality)=predationInit
```

To include a process at the end of the time step:

```
insert_processes Oct_Nov()=predationInit
```

To exclude a process from an initialisation phase, use the subcommand `exclude_processes` in a command `@initialisation_phase`,

```
exclude_processes Instantaneous_Mortality
```

This command removes the process labelled `Instantaneous_Mortality` during that particular initialisation phase.

4.4.3.1. Iterative Initialisation

The *Iterative* initialisation is a general solution for initialising the model. The iterative method can be slow to converge, depending on the model, but can work on even complex structured models that may be difficult or impossible to implement using analytic approximations.

The number of iterations in the iterative initialisation can increase the model output, and the number of iterations should be chosen to be large enough to allow the population state to fully converge. A period of about two generation times is recommended to ensure convergence. CASAL2 can be configured to report convergence statistics that can assist in determining convergence properties.

In addition, the iterative initialisation phase can optionally be stopped early if user-defined convergence criteria is met. For a list of supplied years in the initialisation phase, the convergence criteria is met if the proportional absolute summed difference between the state in year $t - 1$ and the state in year t ($\hat{\lambda}$) is less than the user-defined value of λ , where

$$\hat{\lambda} = \frac{\sum_i \sum_j |\text{element}(i, j)_t - \text{element}(i, j)_{t-1}|}{\sum_i \sum_j \text{element}(i, j)_t} \quad (4.1)$$

Hence, for initialisation define:

- The number of initialisation phases,
- The number of years in each phase, and
- The processes to apply in each phase, where the default processes are those applied in the annual cycle

An example with one initialisation phase:

```
@model
...
initialisation_phases Iterative_initialisation

@initialisation_phase Iterative_initialisation
type iterative
years 50
lambda 0.0001
convergence_years 20 40
```

4.4.3.2. Derived Initialisation

The Derived initialisation is an analytical solution that calculates the equilibrium age structure and the plus group using a geometric series solution. The benefit of this method is it can be solved in $\text{max_age} - \text{min_age} + 1$ years/steps/units?, so it is computationally faster than the iterative initialisation phase. Under some process combinations (e.g., one-way migrations) this initialisation does not calculate the exact equilibrium partition. When using this initialisation, confirm that the partition has reached an equilibrium state by either comparing with an iterative initialisation, or by adding a second iterative initialisation phase with a limited number of iterations for comparison.

An example with one initialisation phase:

```
@model
...
initialisation_phases Equilibrium_initialisation

@initialisation_phase Equilibrium_initialisation
type derived
```

4.4.3.3. Cinitia Initialisation

The `Cinitia` initialisation is used only as a second or greater phase initialisation, and can only be applied after `Derived` or `Iterative` initialisation phases. This initialisation can be a method for estimating the non-equilibrium state of population if there is exploitation before the data start. The estimated `Cinitia` factors shift the initial population away from an equilibrium state prior to the start year. It would be helpful to include an observation of age composition data for the first year of the model in order to estimate the non-equilibrium population state.

An example with two initialisation phases:

```
@model
...
initialisation_phases Iterative Cinitia

@initialisation_phase Iterative
type iterative
years 10
lambda 0.0001
convergence_years 10 20

@initialisation_phase Cinitia
type cinitia
categories spawn.male+nonspawn.male spawn.female+nonspawn.female
table n
spawn.male+nonspawn.male      5e7 5e7 7e6 6e6 5e6 4e6 3e6 2e6 1e6 1e6 1e1 1e1 1e1 1e1
spawn.female+nonspawn.female 5e7 5e7 7e6 6e6 5e6 4e6 3e6 2e6 1e6 1e6 1e1 1e1 1e1 1e1
end_table
```

The `Cinitia` factors can also be estimated with the syntax

```
@estimate cinit_male
parameter initialisation_phase[Cinitia].spawn.male+nonspawn.male
same initialisation_phase[Cinitia].spawn.female+nonspawn.female
lower_bound 2e2 2e2 2e2 2e2 2e2 2e2 2e2 2e2 2e2 2e2 2e0 2e0 2e0 2e0
upper_bound 2e9 2e9 2e9 2e9 2e9 2e9 2e9 2e9 2e9 2e9 2e9 2e9 2e9 2e9
type uniform
```

4.4.3.4. Fixed Initialisation

The `Fixed` initialisation uses a user-defined table as the initial partition numbers-at-age prior to the start year. Models can be initialised by specifying the numbers-at-age for each category. When initialising models with this type, undefined behaviour may be result if the model applies processes that require derived quantities to be calculated in the initialisation phase.

An example with one initialisation phase:

```
@model
...
initialisation_phases Fixed

@initialisation_phase Fixed
type state_category_by_age
categories male female
```

```

min_age 3
max_age 10
table n
male 1000 900 800 700 600 500 400 700
female 1000 900 800 700 600 500 400 700
end_table

```

4.4.4. Model run years

Following initialisation, the model then runs over the user-defined years, from `start_year` to `final_year`. For this part of the model, the annual cycle can be broken into multiple time steps per year, and observations can be associated with specific time steps.

Processes are applied in the order specified within each time step. These processes can be the same or different from the processes specified for the initialisation phases.

The run years define the years over which the model is to run and the annual cycle within each year. The model runs from the start of year `initial` to the end of year `final`. The projection then extends the run time up to the end of year `project_final_year`.

The model properties must be specified:

- The number of time steps and the processes applied in each
- The first year, the model start year
- The last year, the model final year
- The last projection year, the model projection final year

An example of the syntax:

```

@model
start_year 1972
final_year 2016
projection_final_year 2021
## Define the ages in the partition
min_age 1
max_age 30
age_plus true
base_weight_units tonnes
initialisation_phases Equilibrium_state
## Define the annual cycle
time_steps Sep_Feb Mar_May Jun_Aug

## Define the "rows" in the partition
## This is a single sex and area population
@categories
format stock
names HAK4
age_lengths age_size

@initialisation_phase Equilibrium_state
type derived

## Define the processes in the annual cycle
## A list of labels in each time step that correspond to a process

```

```
@time_step Sep_Feb
processes Recruitment Instantaneous_Mortality
```

```
@time_step Mar_May
processes Instantaneous_Mortality
```

```
@time_step Jun_Aug
processes Ageing Instantaneous_Mortality
```

4.4.5. Projection years

The Projection functionality runs the model forwards, using stochastic and/or deterministic values for some population parameters, such as recruitments and catches.

The CASAL2 command to run the model in projection mode is `casal2 -f 1`. The number that follows the `-f` parameter indicates the number of projections to generate for each set of parameters supplied. This functionality allows for the exploration of many scenarios with a single set of parameters. The number of projections should be greater than 1 only if applying a projection type that is stochastic.

The `--tabular` flag should be used when running projections after a Bayesian analysis. This option will output a tabular report (see Section 7.21) which can then be analysed in **R**.

Projection years are after the model run years, and are defined as the `final_year + 1` through the `final_projection_year`.

For a projection run in CASAL2 the model is initialised and run through the model years from `start_year` to `final_year`. During this run mode CASAL2 stores all parameter values so that projection classes can allow parameters before `final_year` to be projected. The model then is re-run from `start_year` to `projection_final_year`, where any parameter can either be fixed or drawn from a stochastic distribution or process.

An example of when a parameter is projected before the projection phase has started is for year class parameters. The last few year class parameters may be poorly estimated, which depends on the quality and coverage of the composition data that could inform these parameters or the use of a recruitment index. Thus, users may assume that these parameters are unknown and apply projection methods for the future values.

CASAL2 has no default projection properties for parameters that are specified by year, e.g., year class strength parameters. The projections for these parameters must be specified using the `@project` command block. CASAL2 will produce errors if run in projection mode without a `@project` block for the `ycs_values` parameter being specified.

CASAL2 allows any estimable parameter to be specified in a `@project` block and then used in a projection. The available projection types for these parameters include:

- constant
- lognormal
- empirical-lognormal
- empirical re-sampling
- user-defined

The projection classes available, and examples of their syntax, are in Section 4.13.

The subcommands `years` and `parameter` are common to all projection methods. The argument `multiplier` is a constant which is multiplied with the projected value after it has been generated.

Note for the year class parameters: the definition of year applies to the `ycs_years`, not the model years. As defined in Section 4.5.1.2, `ycs_years` are offset between the time of spawning and when individuals are added to the partition.

4.5. Population processes

Population processes are processes that change the model state. These processes produce changes in the partition by adding and removing individuals, or by moving individuals between ages and/or categories.

The population processes include:

- recruitment,
- ageing,
- growth,
- maturation,
- mortality events (e.g., natural and fishing), and
- category transition processes, i.e., processes that move individuals between categories while preserving their age structure.

There are two types of processes: (1) processes that occur across multiple time steps in the annual cycle, e.g., `mortality_constant_rate` and `mortality_instantaneous`; and (2) processes that occur only within the time step in which they are defined. These processes are applied in the user-defined order when initialising the model, and then for a user-defined order in each year in the annual cycle.

4.5.1. Recruitment

Recruitment processes are defined as processes that add new individuals to the partition. CASAL2 has two options for recruitment processes, constant recruitment and the Beverton-Holt stock-recruitment relationship (Beverton and Holt, 1957).

In the recruitment processes, a number of individuals are added to a single age class within the partition, with the number determined by the type of recruitment process specified. If more than one category (of recruits?) is defined, then the proportion of recruits to be added to each category is specified by the `proportions` property, or multiple recruitment processes can be defined. For example, if recruiting to categories labelled `male` and `female`, then the proportions may be set to 0.5 and 0.5, so that half of the recruits are added to the male category and the other half to the female category.

Recruitment can differ between a spawning event or the creation of a cohort/year class. In a fisheries context, recruitment usually refers to individuals "recruiting" to a fishery. This definition is used because there is usually not a lot of information on younger age classes between the time of spawning and being vulnerable to a survey or fishery for data collection. Thus, the model configuration may specify the population for which data are available.

The offset between spawning and recruitment is parameterised either by the recruitment variable `age`, or `min_age`, which is the default value for the `age` property in the recruitment process. The

CASAL2 parameter `age` is the same as the CASAL parameter `y_enter`.

For the constant and Beverton-Holt recruitment processes, the number of individuals following recruitment in year y is

$$N_{y,a,j} \leftarrow N_{y,a-1,j} + p_j(R_y) \quad (4.2)$$

where $N_{y,a,j}$ is the numbers in year y and category j at age a , p_j is the proportion added to category j , and R_y is the total number of recruits in year y .

4.5.1.1. Constant recruitment

In the constant recruitment process the total number of recruits added in each year y in age a is R_y , with $R_y = R_0$ for all years

$$R_{y,j} = p_j(R_0) \quad (4.3)$$

Constant recruitment is equivalent to a Beverton-Holt recruitment process with steepness (h) set to 1.

For example, to specify a constant recruitment process where individuals are added to the male and female immature categories at $age = 1$ in equal proportion (`proportions = 0.5`), and the number to add is $R_0 = 5 \times 10^5$, the syntax is

```
@process Recruitment
type constant_recruitment
categories male.immature female.immature
proportions 0.5 0.5
r0 500000
age 1
```

4.5.1.2. Beverton-Holt recruitment

In the Beverton-Holt recruitment process the total number of recruits added each year is R_y . R_y is the product of the average recruitment R_0 , the annual year class strength multiplier YCS , and the stock-recruit relationship $SR(SSB_y)$

$$R_{y,a,j} = p_j(R_0 \times YCS_{y_{cs_year}} \times SR(SSB_{y_{cs_year}})) \quad (4.4)$$

where

$$y_{cs_year} = y - ssb_offset \quad (4.5)$$

and a is age, p_j is the proportion of recruits to enter category j , and `ssb_offset` is the number of years lag between spawning and recruitment.

Recruitment refers to recruitment into the population and may differ from the spawning event. See below on more information about `ssb_offset`. In general this parameter should not be specified by the user.

$SR(SSB_y)$ is the Beverton-Holt stock-recruit relationship parametrised by the steepness h , and based on [Mace and Doonan \(1988\)](#) parametrisation

$$SR(SSB_y) = \frac{SSB_y}{B_0} / \left(1 - \frac{5h-1}{4h} \left(1 - \frac{SSB_y}{B_0} \right) \right) \quad (4.6)$$

The Beverton-Holt recruitment process requires a value for B_0 and SSB_y to calculate the number of recruits. A derived quantity (see Section 4.6) must be defined that provides the annual SSB_y for the recruitment process. B_0 is then defined as the value of the SSB at the end of one of the initialisation phases, which is defined by the parameter `b0_initialisation_phase`.

During initialisation the YCS multipliers are assumed to be equal to 1, and recruitment that happens in the initialisation phases that occur before and during the phase when B_0 is determined are assumed to have steepness $h = 1$ (i.e., in those initialisation phases, recruitment is equal to R_0).

Recruitment in the initialisation phases after the phase where B_0 was determined are calculated using the Beverton-Holt stock-recruit relationship. R_0 and B_0 have a direct relationship when there are no density-dependent processes in the annual cycle. Models can thus be initialised using B_0 or R_0 .

The property `ssb_offset` should not be manually specified; CASAL2 determines `ssb_offset` by the order of ageing, recruitment, spawning, and the recruitment parameter `age`

- if the annual time step order is recruitment, ageing, spawning, then `ssb_offset` should equal `age + 1`, or
- if the annual time step order is spawning, ageing, recruitment, then `ssb_offset` should equal `age - 1`, or
- `ssb_offset = age`

There may be scenarios where the user will input these values, e.g., if there are multiple ageing processes in the annual cycle. CASAL2 does not have functionality to accommodate this situation, so in this case `ssb_offset` would be manually defined.

There are two variants of this process and they refer to how the stock recruitment residuals or $YCS_{y_{cs_year}}$ are parametrised. This parametrisation can either be in natural space as year class strength (YCS) multipliers, or in log space as recruitment deviations. Due to the difference in terminology, these variants are implemented in two separate processes, `recruitment_beverton_holt` and `recruitment_beverton_holt_with_deviations`, respectively.

YCS (YCS_y)

The YCS parameter (`y_{cs_years}`) is defined in Equation (4.5). The parameter `y_{cs_values}` is referenced by the `y_{cs_years}` parameter and is important to note when defining `@estimate`, `@project`, and `@time_varying` blocks for the parameter `y_{cs_values}`. An example is at the end of the section.

A common practice when estimating YCS is to standardise using the Haist parametrisation, which was described by V. Haist. CASAL2 will standardise YCS only if subcommand `standardise_y_{cs_years}` is defined. The model parameter `y_{cs_values}` is a vector \mathbf{Y} , covering the

years from `start_year - ssb_offset` to `final_year - ssb_offset`, as defined by the parameter `ycs_years`. The resulting year class strengths are calculated by $YCS_i = Y_i / \bar{Y}$, where the mean is calculated over the user-specified years `standardise_ycs_years`.

$$YCS_i = \begin{cases} Y_i / \text{mean}_{y \in S}(Y_y) & : y \in S \\ Y_i & : y \notin S \end{cases}$$

where S is the set of years from `standardise_ycs_years`. One effect of this parametrisation is that R_0 is then defined as the mean estimated recruitment over the set of years S , because the mean YCS multiplier over these years will always be one.

Typically `standardise_ycs_years` is defined to span the years over which YCS is reasonably well estimated. For years that are not well estimated, Y_y can be set to 1 for some or all years $y \in S$ (which is equivalent to forcing $R_y = R_0 \times SR(SSB_y)$) by setting the lower and upper bounds of these Y values to 1. An exception to this might occur for the most recent YCS values, which the user may estimate but not include in the definition of R_0 (because the estimates may be based on too few data). One or more years may be excluded from the range of years for the averaging process of the Haist parametrisation.

The advantage of the Haist parametrisation is that a large penalty is not necessary to force the mean of the YCS parameter to be 1, although a small penalty should still be used to stop the mean of Y from drifting. These adjustments may improve MCMC performance. Projected YCS values are not affected by this feature. A disadvantage with this parametrisation in a Bayesian analysis is that the prior applies to Y , not YCS .

An example of the specification of a Beverton-Holt recruitment process, where individuals are added to the category "immature" at $age = 1$, and the number added is $R_0 = 5 \times 10^5$; `SSB_derived_quantity` is a derived quantity that specifies the total spawning stock biomass that contributed to the year class, with B_0 the value of the derived quantity at the end of the initialisation phase labelled `phase1`; and YCS are standardised to have mean one in the period 1995 to 2004, and recruits enter into the model two years following spawning

```
@process Recruitment
type recruitment_beverton_holt
categories immature
proportions 1.0
r0 500000
b0_initialisation_phase phase1
steepness 0.75
age 1
ssb SSB_derived_quantity
standardise_ycs_years 1995:2004
ycs_years 1994 1995 1996 1997 1998 1999 2000 2001 2002 2003 2004 2005 2006
ycs_values 0.65 0.87 1.6 1.13 1.0235 0.385 2.653 1.35 1 1 1 1 1
```

Recruitment deviations, ϵ_y

Recruitment deviations represent the stock-recruitment relationship residuals in log space, with the link between YCS_y and ϵ_y

$$YCS_y = \exp(\epsilon_y - b_y \sigma_R^2 / 2) \quad (4.7)$$

where $\varepsilon_y \sim N(0, \sigma_R^2)$, σ_R^2 is the variance of the stock-recruitment residuals, and b_y is a bias correction defined by [Methot Jr and Taylor \(2011\)](#)

$$b_y = \left\{ \begin{array}{ll} 0, & \text{for } y \leq y_1^b \\ b_{\max}(1 - \frac{y-y_1^b}{y_2^b-y_1^b}), & \text{for } y_1^b < y < y_2^b \\ b_{\max}, & \text{for } y_2^b \leq y \leq y_3^b \\ b_{\max}(1 - \frac{y_3^b-y}{y_4^b-y_3^b}), & \text{for } y_3^b < y < y_4^b \\ 0, & \text{for } y_4^b \leq y \end{array} \right\} \quad (4.8)$$

The ε_y values are normally distributed in log space and thus lognormal when back-transformed to the resulting stock-recruitment relationship YCS_y . Recent work has found that this transformation does not technically lead to the *a priori* assumption that the resulting YCS_y are lognormal. See [Appendix A](#) for more discussion.

The ramp function described above for the bias correction has the additional subcommands controlling the ramp

- $y_1^b = \text{last_year_with_no_bias}$
- $y_2^b = \text{first_year_with_bias}$
- $y_3^b = \text{last_year_with_bias}$
- $y_4^b = \text{first_recent_year_with_no_bias}$
- $b_{\max} = \text{b_max}$

```
@process Recruitment
type recruitment_beverton_holt_with_deviations
categories immature
proportions 1.0
r0 500000
last_year_with_no_bias 1940
first_year_with_bias 1950
last_year_with_bias 2016
first_recent_year_with_no_bias 2018
b_max 0.85
b0_initialisation_phase phase1
steepness 0.75
age 1
ssb SSB_derived_quantity
deviation_years 1994 1995 1996 1997 1998 1999 2000 2001 2002 2003 2004 2005 2006
deviation_values 0 -0.2 0.4 0 0 0 0 0 0 0 0 0 0
```

To specify a Beverton-Holt recruitment for each stock, the information required is:

1. YCS , starting from year (`start_year - ssb_offset`) and extending up to year (`final_year - ssb_offset`)
2. the value of age (which is `y_enter` in CASAL)
3. the steepness parameter `h`
4. in a multi category model, the proportion of recruits for each category
5. a label for the derived quantity

When an `@initialisation_phase` (Section 4.4.3) `type = derived` is specified and the recruitment is defined by `b0`, then all categories must be specified in the `@recruitment` block. Usually in a recruitment processes only the categories that receive recruits need to be defined. For example, a population has a spawning area that is different from the area where recruits enter the population. An area-specific model could then be specified which contains spawning categories and recruiting categories. The recruiting categories would be specified in the subcommand `categories`, as these would be the categories receiving recruits.

If `@initialisation_phase, type=derived` is used, then all categories that are a part of that recruitment process need to be specified as well

```
@process Recruitment
type recruitment_beverton_holt
categories recruits.male recruits.female spawn.male spawn.female
proportions 0.5 0.5 0.0 0.0
r0 500000
ssb SSB
....
```

The `proportions = 0.0` for "spawn.male" and "spawn.female" are needed due to the way the derived initialisation phase works. The derived initialisation finds a solution for when `r0 = 1.0` based on an infinite geometric series for the plus group, and scales the initial partition by `r0`. Thus, if all categories are not specified, then those that are missed would not be initialised to true values and this could lead to inaccurate model outputs. This set-up extends to multiple-stock fisheries model configurations as well, where all of the categories that make up the stock need to be listed.

4.5.2. Ageing

The ageing process "ages" individuals, i.e., this process moves all individuals in the named categories j from one age class a to age class $a + 1$, or accumulates them if the last age class is a plus group.

The ageing process is defined as,

$$\text{element}(a + 1, j) \leftarrow \text{element}(a, j) \quad (4.9)$$

except in the case of the plus group (if defined),

$$\text{element}(a_{\max}, j) \leftarrow \text{element}(a_{\max}, j) + \text{element}(a_{\max-1}, j). \quad (4.10)$$

For example, to apply ageing to the categories `immature` and `mature`, the syntax is

```
@process Ageing
type ageing
categories immature mature
```

Note: the ageing process is *NOT* applied by CASAL2 by default. As with other processes, CASAL2 will not apply a process unless it is defined and specified as a process within the annual cycle. Hence, it is possible to specify a model where a category is not aged. CASAL2 *will NOT check or otherwise warn if there is a category defined where ageing is not applied.*

4.5.3. Mortality

There are 8 types of mortality processes available in CASAL2:

- constant rate,
- event,
- biomass-event,
- instantaneous,
- instantaneous retained,
- Hollings,
- initialisation, and
- a density-dependent relationship based on prey suitability.

These processes remove individuals from the partition, either as a rate, as a total number (abundance), as a biomass of individuals or, as a combination of these. CASAL2 does not (yet) implement the Baranov catch equation. However, instantaneous mortality is considered an approximation to the Baranov catch equation.

To apply both natural and biomass-event mortality, the mortality type `mortality_instantaneous` can be specified. Note that all mortality processes occur within the mortality block of a time step. See Section 4.4.2 for more information and definitions on mortality blocks.

4.5.3.1. Constant mortality rate

To specify a constant annual mortality rate (e.g. $M = 0.2$) for categories "male" and "female"

```
@process NaturalMortality
type mortality_constant_rate
categories male female
selectivities One One
m 0.2 0.2
```

The total number of individuals removed from a category

$$D_{j,t} = \sum_a N_{a,j,t} [1 - \exp(-S_{a,j} M_{a,j} p_t)] \quad (4.11)$$

where $D_{j,t}$ is the total number of deaths in category j in time step t , $N_{a,j,t}$ is the number of individuals in category j of age a in time step t , $S_{a,j}$ is the selectivity value for age a in category j , $M_{a,j}$ is the mortality rate for category j for age a , and p_t is the proportion of the mortality rate to apply in time step t .

The mortality rate process requires a selectivity. To apply the same mortality rate over all age classes in a category, use a selectivity defined as $S_{a,j} = 1.0$ for all ages a in category j

```
@selectivity One
type constant
c 1
```

Age-specific mortality rates can also be applied. For example, the hypothesis that mortality is higher for younger and older individuals and lowest when individuals are at their optimal fitness could be defined by using a double exponential selectivity (see Section 4.12)

```
@selectivity age_specific_M
type double_exponential
x0 7.06524
x1 1
x2 17
y0 0.182154
y1 1.43768
y2 1.57169
alpha 1.0

@process NaturalMortalityByAge
type mortality_constant_rate
categories male female
selectivities age_specific_M age_specific_M
m 1.0 1.0
```

In this definition `m` is set to 1.0 and the rate is described through the selectivity. This concept can be constructed similarly for other mortality methods such as `instantaneous_mortality`.

4.5.3.2. Event and biomass-event mortality

The event mortality and biomass-event mortality processes are applied in a similar manner, except that they remove a specified abundance (number of individuals) or biomass, respectively. These mortality processes can be used to define mortality events where the numbers of removals are known, e.g., fishing, rather than applying mortality as a rate.

In these cases, the abundance or biomass removed is also constrained by a maximum exploitation rate. CASAL2 removes as many individuals or as much biomass as possible, while not exceeding the maximum exploitation rate.

Event mortality processes require a penalty to avoid estimating parameter values that will not allow the defined number of individuals to be removed. The model penalises those parameter estimates that result in an too low a number of individuals in the defined categories (after applying selectivities) to allow for removals at the maximum exploitation rate, with a similar penalty for biomass. See Section 5.8 for more information on how to specify penalties.

The event mortality applied to user-defined categories i , with the numbers removed at age j determined by a selectivity-at-age S_j :

First, calculate the vulnerable abundance for each category j in $1 \dots J$ for ages $a = 1 \dots A$ that are subject to event mortality

$$V_{a,j} = S_{a,j} N_{a,j} \quad (4.12)$$

and define the total vulnerable abundance V_{total} as

$$V_{total} = \sum_j \sum_a V_{a,j} \quad (4.13)$$

The exploitation rate to apply is

$$U = \begin{cases} C/V_{total}, & \text{if } C/V_{total} \leq U_{max} \\ U_{max}, & \text{otherwise} \end{cases} \quad (4.14)$$

The number removed $R_{a,j}$ from each age a in category j is,

$$R_{a,j} = UV_{a,j} \quad (4.15)$$

For example, to specify an **abundance-based** fishing mortality process with catches given for a set of specific years over categories "immature" and "mature", with selectivity "FishingSel", and assuming a maximum possible exploitation rate of 0.7, the syntax is

```
@process Fishing
type event_mortality
categories immature mature
years 2000 2001 2002 2003
U_max 0.70
selectivities FishingSel FishingSel
penalty event_mortality_penalty
```

and specified similarly for a **biomass-based** fishing mortality process

```
@process Fishing
type mortality_event_biomass
categories immature mature
years 2000 2001 2002 2003
U_max 0.70
selectivities FishingSel FishingSel
penalty event_mortality_penalty
```

4.5.3.3. Instantaneous mortality

The instantaneous mortality process combines both natural mortality and event biomass mortality into a single process. This allows the simultaneous application of both natural mortality and anthropogenic mortality to occur across multiple time steps. This process applies half the natural mortality in each time step, then the mortalities from all the concurrent removals instantaneously, then half of the natural mortality. In fisheries models this is the most commonly used mortality process.

This process allows for multiple removal events, e.g., a fisheries model with multiple fisheries and/or fleets. A removal method can occur in one time step only, although multiple removals can be defined to cover events during the year.

The equations for instantaneous mortality:

TODO redo equations, as notation is not consistent with that above, e.g., $S_{a,j}$

- An exploitation rate (actually a proportion) is calculated for each fishery, as the catch divided by the selected-and-retained biomass,

$$U_f = \frac{C_f}{\sum_a \bar{w}_a S_{f,a} n_a \exp(-0.5tM_a)}$$

- The mortality pressure associated with method f is defined as the maximum proportion of fish taken from any element of the partition in the area affected by the method f

$$U_{f,obs} = \max_a \left(\sum_k S_{k,a} U_k \right)$$

where the maximum is over all partition elements affected by fishery f , and the summation is over all methods k which affect the j th partition element in the same time step as fishery f .

In most cases the mortality pressure will be equal to the exploitation rate (i.e., $U_{f,obs} = U_f$), but can be different if: (a) there is another removal method operating in the same time step as removal method f and affecting some of the same partition elements, and/or (b) the selectivity $S_{f,a}$ does not have a maximum value of 1.

There is a maximum mortality pressure limit of $U_{f,max}$ for each method of removal f . So, no more than proportion $U_{f,max}$ can be taken from any element of the partition affected by removal method f in that time step. Clearly, $0 \leq U_{max} \leq 1$. It is an error if two removal methods, which affect the same partition elements in the same time step, do not have the same U_{max} .

For each f , if $U_{f,obs} > U_{f,max}$, then U_f is multiplied by $U_{f,max}/U_{f,obs}$ and the mortality pressures are recalculated. In this case the catch actually taken from the population in the model will differ from the specified catch, C_f .

- The partition is updated using

$$n'_a = n_a \exp(-tM_a) \left[1 - \sum_f S_{f,a} U_f \right]$$

For example, to apply natural mortality of 0.20 across three time steps on both male and female categories, with two methods of removals (fisheries FishingWest and FishingEast) and their respective catches (kg) known for years 1975:1977 (the catches are given in the `catches` table and information on selectivities, penalties, and maximum exploitation rates are given in the `method` table), the syntax is

TODO where is `time_step_ratio` and its usage defined?

```
@process instant_mort
type mortality_instantaneous
m 0.20
time_step_ratio 0.42 0.25 0.33
selectivities One
categories male female
units kgs

table catches
year FishingWest FishingEast
1975 80000 111000
1976 152000 336000
1977 74000 1214000
end table

table method
method category selectivity u_max time_step penalty
FishingWest stock westFSel 0.7 step1 CatchPenalty
FishingEast stock eastFSel 0.7 step1 CatchPenalty
end_table
```

and for referencing catch parameters for use in projecting, time-varying, and estimating, the syntax is

```
parameter process[mortality_instantaneous].method_"method_label"{2018}
```

where "method_label" is the label from the catch or method table and continuing the example,

```
parameter process[instant_mort].method_FishingWest{2018}
```

To calculate weight by empirical weight-at-age matrices as described in Section 4.9, the method table would include an additional column to reference weight-at-age objects:

```
@age_weight jan_weight_at_age
type data
table data
year 1 2 3 4
1980 3.4 5.6 7.23 8.123
end_table

table method
method      category  selectivity  u_max  time_step  penalty      age_weight
FishingWest stock     westFSel     0.7    step1      CatchPenalty jan_weight_at_age
FishingEast stock     eastFSel     0.7    step1      CatchPenalty jan_weight_at_age
end_table
```

4.5.3.4. Instantaneous mortality with retained catch and discards

The instantaneous mortality retained process builds on the instantaneous mortality process (4.5.3.3) which has simultaneous applications of fishing and natural mortality, but with all catch-at-sea being landed, i.e., no discarding. The process `mortality_instantaneous_retained` allows for retained catch, discards, and also a mortality to be applied to discards, i.e., some are allowed to survive. The method for taking catch from the partition and the constraints used are the same as in `mortality_instantaneous`.

This process was implemented to address issues with the pot fishery for blue cod which has a minimum legal size and so some catch is discarded at sea and some of these discards are expected to survive (based on some experimental work). There are length data taken at sea, so the total catch selectivity can be estimated, and length and age data taken from the landed catch (retained), so the retention selectivity can also be estimated.

In this mortality process, discard mortality is specified by defining a selectivity to represent mortality by age or length (e.g., constant or asymptotic descending logistic). This discard selectivity is not be estimated since there is no observation class associated with it. If discard mortality is not provided, it is assumed that all discards die. Landed catch, and both the retained and total catch selectivities must be specified.

Extending the example shown in instantaneous mortality process (4.5.3.3) to use retained weight instead of catch, the commands are:

```
@process FishingRetainedCatch
type mortality_instantaneous_retained
# natural mortality
```

```

m 0.20
# the ratio of natural mortality in each of the three time steps
time_step_ratio 0.42 0.25 0.33
selectivities One
#for natural mortality by age
categories male female
units kgs

table catches
# two fisheries, West and East
year FishingWest FishingEast
# the catches are now landed catch
1975 80000 111000
1976 152000 336000
1977 74000 1214000
end table

table method
# all discards die
method      category selectivity retained_selectivity u_max time_step penalty
FishingWest stock    westFSel   westRetainedSel    0.7  step1  CatchPenalty
FishingEast stock    eastFSel   eastRetainedSel    0.7  step1  CatchPenalty
end_table

```

If discard mortality is less than 1.0, use:

```

table method
# 50% discard mortality
method      category selectivity retained_selectivity discard_mortality u_max time_step penalty
FishingWest stock    westFSel   westRetainedSel    DisMort    0.7  step1  CatchPer
FishingEast stock    eastFSel   eastRetainedSel    DisMort    0.7  step1  CatchPer
end_table

@selectivity DisMort
Type constant
# 50% mortality of discards
c 0.5

```

See the instantaneous mortality process (4.5.3.3) for referencing catch parameters and calculating weight using empirical weight-at-age matrices.

The report outputs total catch, actual landed catch, and discards, without and with discard mortality:

```

@report Mortality
type process
process Instantaneous_Mortality_Retained

```

TODO redo notation, as it is not consistent with that above, e.g., $S_{a,j}$ and R_y

In the following, fisheries are indexed by f , and a indexes both age and category combinations.

The total catch is found by applying a selectivity, $S_{f,a}$, in the same way as in the instantaneous mortality process. Retention, $R_{f,a}$, is defined by specifying a selectivity, which can be a function

of length or age. The retained catch is the product of these two values, $R_{f,a} * S_{f,a}$. If sex is in the partition, then there are potentially two retention curves, one for each sex.

In general, there is a retention curve for each category in the partition. This property does not apply to surveys. Discard mortality is also specified as a selectivity, $D_{f,a}$. The fraction of dead fish from fishing activity is $S_{f,a} * [R_{f,a} + (1.0 - R_{f,a}) * D_{f,a}]$. If $D_{f,a}$ is 1.0, then all selected fish are dead, and if it is 0.0, then only the retained fish are dead.

The equations for the `mortality_instantaneous_retained` process:

- Total catch (catch-on-board), C_f , is calculated by (retained catch) * VF / VR, where VF is vulnerable retained biomass, j indexes categories and t is the proportion of M in the time step, and VR is the full vulnerable biomass, $VF = \sum_{a,j} \bar{w}_a S_{a,j} n_{a,j} \exp(-0.5tM_{a,j})$.
- An exploitation rate (actually a proportion) is calculated for each fishery, as the total catch (retained + discards) divided by the selected biomass (VF above) using selectivity $S_{f,a}$,

$$U_f = \frac{C_f}{\sum_a \bar{w}_a S_{f,a} n_a \exp(-0.5tM_a)}$$

- The mortality pressure associated with method f is defined as the maximum proportion of fish taken from any element of the partition in the area affected by the method f ,

$$U_{f,obs} = \max_a \left(\sum_k S_{k,a} U_k \right)$$

where the maximum is over all partition elements affected by fishery f , and the summation is over all methods k which affect the j th partition element in the same time step as fishery f .

In most cases the mortality pressure will be equal to the exploitation rate (i.e., $U_{f,obs} = U_f$), but can be different if: (a) there is another removal method operating in the same time step as removal method f and affecting some of the same partition elements, and/or (b) the selectivity $S_{f,a}$ does not have a maximum value of 1.

There is a maximum mortality pressure limit of $U_{f,max}$ for each method of removal f . So, no more than proportion $U_{f,max}$ can be taken from any element of the partition affected by removal method f in that time step. Clearly, $0 \leq U_{max} \leq 1$. It is an error if two removal methods, which affect the same partition elements in the same time step, do not have the same U_{max} .

For each f , if $U_{f,obs} > U_{f,max}$, then U_f is multiplied by $U_{f,max}/U_{f,obs}$ and the mortality pressures are recalculated. In this case the catch actually taken from the population in the model will differ from the specified catch, C_f .

- Discard numbers-at-age (including their share of natural mortality) is $S_{a,j}(1 - R_{a,j})n_{a,j} \exp(-0.5tM_{a,j})$, and those that die at the end of the time step (updating the partition) are $D_{a,j}S_{a,j}(1 - R_{a,j})n_{a,j} \exp(-tM_{a,j})$, where $D_{f,a}$ is the fraction that die on return to the sea.
- The partition is updated by removing landed catch, natural mortality, and discard mortality

$$n'_a = n_a \exp(-tM_a) \left[1 - \sum_f S_{f,a} U_f (R_{f,a} + D_{f,a}(1 - R_{f,a})) \right]$$

4.5.3.5. Holling mortality rate

The density-dependent Hollings mortality process applies the Holling Type II or Type III functions (Holling, 1959), and is generalised by the Michaelis-Menten equation (Michaelis and Menten, 1913).

This mortality process removes a number or biomass from a set of categories according to the total (selected) abundance (or biomass) and some "predator" abundance (or biomass), and is constrained by a maximum exploitation rate.

The mortality applied to user-defined categories k , with the numbers removed at age l , determined by a selectivity-at-age S_l is applied as follows:

First, calculate the total predator abundance (or biomass) over all predator categories k in $1 \dots K$ and ages $l = 1 \dots L$ that are applying the mortality

$$P_{k,l} = S_l^{predator} N_{k,l}^{predator} \quad (4.16)$$

And define the total predator abundance (or biomass) P_{total} as

$$P_{total} = \sum_K \sum_L P_{k,l} \quad (4.17)$$

Then calculate the total vulnerable abundance (or biomass) over all prey categories k in $1 \dots K$ and ages $l = 1 \dots L$ that are subject to the mortality

$$V_{k,l} = S_l^{prey} N_{k,l}^{prey} \quad (4.18)$$

Then define the total vulnerable abundance (or biomass) V_{total} as

$$V_{total} = \sum_K \sum_L V_{k,l} \quad (4.19)$$

The number to remove is then determined by

$$R_{total} = P_{total} \frac{a V_{total}^{x-1}}{b + V_{total}^{x-1}} \quad (4.20)$$

where $x = 2$ for the Holling type II function, $x = 3$ for the Holling type III function, or a different value of $x \geq 1$ for the generalised Michaelis-Menten function; $a > 0$ and $b > 0$ are the Holling function parameters.

The exploitation rate to apply is

$$U = \begin{cases} R_{total}/V_{total}, & \text{if } R_{total}/V_{total} \leq U_{max} \\ U_{max}, & \text{otherwise} \end{cases} \quad (4.21)$$

And the number removed R from each age l in category k is

$$R_{k,l} = U V_{k,l} \quad (4.22)$$

The density-dependent Holling mortality process is applied either as a function of biomass or abundance, depending on the value of the `is_abundance` switch.

For example, a biomass Holling type II mortality process on prey `prey` by predator `predator` has the syntax

```
@process HollingMortality
type Holling_mortality_rate
is_abundance F
a 0.08
b 10000
x 2
categories prey
selectivities One
predator_categories predator
predator_selectivities One
u_max 0.8
```

4.5.3.6. Initialisation-event mortality

Initialisation event mortality is a process that can occur only in the initialisation phase. It applies abundance or biomass mortality events specifically in initialisation phases. This option can be useful if the population is not in equilibrium before model start.

This process applies a single catch value for all iterations within the initialisation phase, and mortality will not be applied outside of the initialisation phase. This process should not be embedded in the annual cycle.

This process should be used in conjunction with the `insert_processes` command in the `@initialisation_phase` block.

Example syntax where the `initialisation_mortality_event` has been specified in the initialisation phase `Predation_state` but not in the annual cycle:

```
initialisation_phases Equilibrium_state Predation_state
time_steps Oct_Nov Dec_Mar
```

```
@initialisation_phase Equilibrium_state
type derived
```

```
@initialisation_phase Predation_state
type iterative
insert_processes Oct_Nov()=predation_Initialisation
```

```
@process predation_Initialisation
type initialisation_mortality_event
categories male.HOKI female.HOKI
catch 90000
selectivities Hakesl Hakesl
```

```
time_step Oct_Nov
processes Mgl Instantaneous_Mortality
```

```
@time_step Dec_Mar
processes Recruitment Instantaneous_Mortality
```

4.5.3.7. Prey-suitability mortality

The density-dependent prey-suitability mortality process applies predation mortality from a predator group to its prey groups simultaneously. It removes an abundance (or biomass) from each prey group according to the total (selected) abundance (or biomass) of each prey group, the total (selected) abundance (or biomass) of the other prey groups, some "predator" abundance (or biomass), and the preference (electivity) of the predator for each prey group, constrained by a maximum exploitation rate. The predator-prey suitability functions were based on the multispecies Virtual Population Analysis (MSVPA) functions (Jurado-Molina et al., 2005).

The mortality applied to the user-defined prey group g of category k , with the numbers removed at age l determined by a selectivity-at-age S_l is applied as follows:

First, calculate the total predator abundance (or biomass) over all predator categories k in $1 \dots K$ and ages $l = 1 \dots L$ that are applying the mortality

$$P_{k,l} = S_l^{predator} N_{k,l}^{predator} \quad (4.23)$$

And define the total predator abundance (or biomass) P_{total} as

$$P_{total} = \sum_K \sum_L P_{k,l} \quad (4.24)$$

Then, given the total vulnerable abundance (or biomass) of prey group g over all categories k in $1 \dots K$ and ages $l = 1 \dots L$ that are subject to the mortality

$$V_{g,k,l} = S_l^{prey} N_{k,l}^{prey} \quad (4.25)$$

And define the total vulnerable abundance (or biomass) of each prey group V_{total}^g as

$$V_{total}^g = \sum_K \sum_L V_{g,k,l} \quad (4.26)$$

And the total availability A_{total}^g for each prey group as

$$A_{total}^g = \frac{V_{total}^g}{\sum_G V_{total}^g} \quad (4.27)$$

The vulnerable abundance (or biomass) and availability every prey group g in $1 \dots G$ is calculated simultaneously. Then the abundance (or biomass) to remove from each prey group g is a function of its electivity E_g , the availability of all other prey groups i in $1 \dots G$, the electivity of the predator for each prey group E_i , and the total consumption rate of the predator CR and its abundance (or biomass) P_{total}

$$R_{total}^g = P_{total} CR \frac{A_{total}^g E_g}{\sum_G A_{total}^i E_i} \quad (4.28)$$

The exploitation rate to apply to each prey group g is then

$$U_g = \begin{cases} R_{total}^g / V_{total}^g, & \text{if } R_{total}^g / V_{total}^g \leq U_{max} \\ U_{max}, & \text{otherwise} \end{cases} \quad (4.29)$$

And the number removed R^g in each prey group g from each age l in category k is

$$R_{g,k,l} = U_g V_{g,k,l} \quad (4.30)$$

Prey suitability choice occurs only between the prey groups specified by the process. The total predator consumption rate represents the consumption of the predator on those prey groups alone. The electivities must sum to 1. Further, the consumption rate can be modified by a layer to be cell specific.

The density-dependent prey-suitability process is applied as either a biomass or an abundance depending on the value of the `is_abundance` switch.

Individual categories can be aggregated into prey groups using the "+" symbol. To indicate that two (or more) categories are to be aggregated, separate them with a "+" symbol.

For example, to specify two prey groups of two species made up of the males and females in each prey group

```
prey_categories maleSpeciesA + femaleSpeciesA maleSpeciesB + femaleSpeciesB
```

This syntax indicates that there are two prey groups, `maleSpeciesA + femaleSpeciesA` and `maleSpeciesB + femaleSpeciesB`, with each group having its own electivity.

For example, a biomass prey-suitability mortality process with an overall consumption rate of 0.8 of prey species A and species B (modelled as males and females) by the predator `predatorSpecies` with electivities between species A and species B of 0.18 and 0.82 has syntax

```
@process PreySuitabilityMortality
type prey-suitability_predation
is_abundance F
consumption_rate 0.8
categories maleSpeciesA + femaleSpeciesA maleSpeciesB + femaleSpeciesB
electivities 0.18 0.82
selectivities One One One One
predator_categories predatorSpecies
predator_selectivities One
u_max 0.8
```

4.5.4. Transition By Category

The transition by category process moves individuals between categories. This process is used to specify transitions such as maturation (individuals move from an immature to mature state) and migration (individuals move from one area to another).

4.5.4.1. Annual transition by category

A special process type is the annual transition by category process, which allows a transition to occur in a specific subset of years only, where each year can have a different rate.

In both cases, there is a one-to-one relationship between the "from" category and the "to" category, i.e., for every source category there is one target category only

$$N_{a,j} = N_{a,i} \times P_i \times S_{a,i} \quad (4.31)$$

where $N_{a,j}$ is the number of individuals that have moved to category j from category i in age a , $N_{a,i}$ is the number of individuals in category i , P_i is the proportion parameter for category i , and $S_{a,i}$ is the selectivity at age a for category i .

To merge categories repeat the "to" category multiple times.

For example, to specify a simple spawning migration of mature males from a western area to an eastern (spawning) area, the syntax is

```
@process Spawning_migration
type transition_category
from West.males
to East.males
selectivities MatureSel
proportions 1
```

where `MatureSel` is a selectivity that describes the proportion of age or length classes that are mature and thus move to the eastern area.

4.5.5. Tag Release events

Tagging processes can be age- or length-based processes, whereby numbers of individuals are moved from an untagged category to a tagged category defined in the `@categories` block. Tag release processes can also account for initial tag-induced mortality on individuals.

Age-based tag release events move a known number of individuals tagged for each age to a tagged category, along with applying additional mortality. Individuals are removed from the non-tagged categories and added to tagged categories. Often the ages of tagged individuals are not known, so length-based tag release events are more commonly used.

Length-based tag release processes are more complicated, as the age-length matrix is calculated and the exploitation for each length bin to then move the correct numbers-at-age based on the known lengths of release. CASAL2 also allows for initial tag loss.

The tag-release process:

For each length bin l of the input vector of numbers-at-length \tilde{N}_l

$$N_{l,j} = \sum_{a=1} N_{a,l,j} * S_a$$

where $N_{a,l,j}$ is the numbers at age a and length l for category j , and S_a is the selectivity at age a .

Calculate the total numbers-at-length T_l across all source categories at length l , taking into account the selectivities

$$T_l = \sum_{j=1} N_{l,j}$$

Calculate the transition rate for length bin u_l

$$u_l = \tilde{N}_l / T_l$$

Check that the threshold u_{max} is not exceeded, which is analogous to the u_{max} in a mortality processes

$$u_l = \begin{cases} u_{max}, & \text{if } u_l > u_{max} \text{ flag a penalty} \\ u_l, & \text{otherwise} \end{cases}$$

Calculate the numbers-at-age in this category that will be moved by multiplying across the age-length matrix and storing the result by age, for each age accumulated across all length bins. Then move the necessary

$$N_{a,j+} = N_{a,l} * u_l$$

The syntax for an example of tag release by length process

```
@process 2005Tags_shelf
type tag_by_length
years 2005
from male.untagged+female.untagged
to male.2005 female.2005
selectivities ShelfselMale ShelfselFemale
penalty tagging_penalty
initial_mortality 0.1
table proportions
year 30 40 50 60 70 80 90 100 110 120 130 140 150 160 170 180 190 200 210 220
2005 0 0 0.0580 0.1546 0.3380 0.1981 0.1643 0.0531 0.0242 0.0097 0 0 0 0 0 0 0 0 0 0
end_table
n 207
U_max 0.999
```

This process moves 207 individuals from a combination of male.untagged and female.untagged categories, based on the combination of growth rates and selectivity, into tagged male and tagged female categories.

4.5.6. Tag Loss

Tag Loss is the process which accounts for tags being lost from a tagged individual due to, for example, tag failure or tags getting knocked off. This process is applied as an instantaneous migration rate that can happen over multiple time steps in the annual cycle. This method assumes that when tags are lost the individuals are transferred from the `from` category to the `to` category.

The tag loss rate is applied depending on whether the individuals were tagged with a single tag only (`tag_number_per_animal = 1`), double tagged (`tag_number_per_animal = 2`), or tagged with n tags (`tag_number_per_animal = n`).

The syntax for the tag loss is

```
@process Tag_loss
type tag_loss
categories tagged_fish
tag_loss_rate 0.02
time_step_ratio 0.25 0.75
selectivities One
tag_loss_type single
year 1985
```

4.6. Derived quantities

Some processes require a population value derived from the population state as an argument. These values are derived quantities. Derived quantities are values calculated at the end of a specified time step in every year, and thus have a single value for each year of the model.

Derived quantities can be calculated as either a function of abundance or biomass. Abundance-derived quantities are the sum over the categories (after applying a selectivity). Biomass-derived quantities are calculated similarly.

Derived quantities are also calculated during the initialisation phases. Therefore, the time step during each phase must be specified. If the initialisation time steps are not specified, the derived quantity will be calculated during the initialisation phases in every year, at the end of the annual cycle.

Derived quantities are required by some processes, e.g., the Beverton-Holt recruitment process which requires an equilibrium biomass (B_0) and annual spawning stock biomass values (SSB_y) to calculate the stock-recruit relationship. These derived quantities are defined as the abundance or biomass of a part of the population at some point in the annual cycle for selected ages and categories.

Derived quantities are associated with a mortality block; see section 4.4.2 for more detail on mortality blocks. Derived quantities can be calculated partway through a mortality blocks.

Two derived quantity methods interpolate derived quantities partway through a mortality block. These methods are `weighted_sum` and `weighted_product`, and are defined as

- `weighted_sum`: after proportion p of the mortality block, the partition elements are given by $n_{p,j} = (1 - p)n_j + p'_j$
- `weighted_product`: after proportion p of the mortality block, the partition elements are given by $n_{p,j} = n_j^{1-p} n'_j{}^p$

where $n_{p,j}$ is the derived quantity at proportion p of the mortality block for category j , n_j is the quantity at the beginning of the mortality block, and n'_j is the quantity at the end of the mortality block.

For example, to define a biomass-derived quantity spawning stock biomass, SSB , calculated at the end of the first time step (labelled `step_one`), over all "mature" male and female categories and halfway through the mortality block using the `weighted_sum` method, the syntax is

```
@derived_quantity SSB
type biomass
```

```

time_step step_one
categories mature.male mature.female
selectivities One
time_step_proportion 0.5
time_step_proportion_method weighted_sum

```

4.7. Age-length relationship

The age-length relationship defines the functional form of the length-at-age (and the weight-at-length; see Section 4.8) of individuals at age/category within the model.

There are three length-age relationship options. The first is the naive "no relationship", where each individual has length 1 regardless of age. The second is the von Bertalanffy relationship, and the third is the Schnute relationship.

The length-at-age relationship is used to calculate the length frequency given age, and with the length-weight relationship, the weight-at-age of individuals within an age/category. When defining length-at-age, the length-weight relationship must also be defined (see Section 4.8).

Changes in length-at-age during the year, i.e., growth between birthdays, are represented by incrementing age as specified by the `time_step_proportions` parameter.

4.7.0.1. The "no relationship" relationship, `none`

The length of each individual is 1 for all ages, and the `none` length-weight relationship must also be used.

4.7.0.2. The von Bertalanffy relationship, `von_bertalanffy`

$$\bar{s}(\text{age}) = L_{\infty} (1 - \exp(-k(\text{age} - t_0))) \quad (4.32)$$

4.7.0.3. The Schnute relationship, `schnute`

$$\bar{s}(\text{age}) = \begin{cases} \left[y_1^b + (y_2^b - y_1^b) \frac{1 - \exp(-a(\text{age} - \tau_1))}{1 - \exp(-a(\tau_2 - \tau_1))} \right]^{1/b}, & \text{if } a \neq 0 \text{ and } b \neq 0 \\ y_1 \exp \left[\ln(y_2/y_1) \frac{1 - \exp(-a(\text{age} - \tau_1))}{1 - \exp(-a(\tau_2 - \tau_1))} \right], & \text{if } a \neq 0 \text{ and } b = 0 \\ \left[y_1^b + (y_2^b - y_1^b) \frac{\text{age} - \tau_1}{\tau_2 - \tau_1} \right]^{1/b}, & \text{if } a = 0 \text{ and } b \neq 0 \\ y_1 \exp \left[\ln(y_2/y_1) \frac{\text{age} - \tau_1}{\tau_2 - \tau_1} \right], & \text{if } a = 0 \text{ and } b = 0 \end{cases} \quad (4.33)$$

The von Bertalanffy relationship has parameters L_{∞} , k , and t_0 . The Schnute relationship (Schnute, 1981) has parameters y_1 and y_2 , which are the mean lengths at reference ages τ_1 and τ_2 , and a and b ; when $b = 1$, this relationship reduces to the von Bertalanffy relationship with $k = a$.

4.7.0.4. data

There is an option to input empirical length at age by year, which is an alternative to using an age-length growth model such as the von Bertalanffy and Schnute model. CASAL2 will interpolate values for missing years across time steps. The calculations of length-at-age throughout the model years occur in the same time step.

```
@age_length male_AL
type data
time_step_proportions 0.0 0.0
length_weight wgt_male
distribution normal
cv_first 0.1
cv_last 0.1
time_step_measurements_were_made step2
internal_gaps mean
external_gaps mean
table data
year 2 3 4 5 6 7 8 9 10 11 12 13 14 15
1980 30.13 34.9 38.43 40.61 42.45 43.02 43.94 43.63 43.36 43.7 43.84 43.51 43.45 43.45
1981 30.33 34.78 38.03 40.15 42.22 42.89 44.21 44.07 43.99 44.32 44.64 44.28 44.04 43.93
end_table
```

4.8. Length-weight relationship

There are two length-weight relationships options. The first is the naive "no relationship" relationship, where the weight of an individual is always 1, regardless of length. The second relationship is the "basic" relationship, which is the standard length-weight relationship, $W = aL^b$.

4.8.0.1. The "no relationship" relationship, none

$$\text{mean weight} = 1 \quad (4.34)$$

4.8.0.2. The standard length-weight relationship, basic

The mean weight \hat{w}_a of an individual of age a is

$$\hat{w}_a = a\hat{l}_a^b \quad (4.35)$$

where \hat{l}_a is the mean length at age a . If a distribution of length-at-age is specified, then the mean weight is calculated over the distribution of lengths

$$\hat{w}_a = (a\hat{l}_a^b)(1 + cv^2)^{\frac{b(b-1)}{2}} \quad (4.36)$$

where the cv is the coefficient of variation (CV) of the length-at-age relationship. This adjustment is exact for lognormal distributions, and an approximation for normal distributions if the CV is not large (Bull et al., 2012).

For comparing CASAL with CASAL2 results, there is a small difference between the two programs. CASAL adjusted the CVs by `length` only when CVs are used in distribution calculations (length-based selectivities, length-based processes, and [length-based?] observations), and is not done in the above correction.

Note: the scale of a can be specified incorrectly. If the catch is in tonnes and the growth curve is in centimetres, then a should convert a length in centimetres to a weight in tonnes. There are reports available that can be used to help check that the units specified are plausible (see Section 7).

```
@length_weight length_weight
type basic
units tonnes
a 0.00000123
b 3.132
```

4.9. Age-weight relationship

Empirical weight-at-age data can be input. This option is different from the method above as it uses empirical data for weight-at-age, rather than calculating it with the growth functions (age -> length -> weight).

This option specifies the weight-at-age values for categories at a point in time. These values can be used in weight-based derived quantities, processes, and observations.

An example

```
TODO: how does this block start? @age_weight age_weight?
type Data
units tonnes
table data
year 1 2 3 4 5 6 7 8 9 10
1986 0.134 0.686 1.639 2.719 3.649 4.901 6.329 6.591 7.238 7.491
1987 0.132 0.724 1.534 2.829 4.092 4.853 5.705 6.143 7.179 8.089
1988 0.122 0.641 1.533 2.641 3.796 5.054 5.652 6.356 6.95 8.857
1989 0.137 0.722 1.606 2.416 3.629 5.027 5.561 6.35 6.933 7.217
1990 0.138 0.773 1.645 2.74 3.711 4.506 5.684 6.929 7.424 7.479
end_table
```

If weight is defined by the empirical weight-at-age data, then the age-length block in the `@categories` block can be omitted.

```
@categories
format stock
names Stock
```

If a weight- or biomass-based derived quantity, process, or observation has a `age_weight_label` subcommand then the `@age_weight` class can be used to calculate the mean weight-at-age.

4.10. Weightless model

To model abundance (i.e., to model the population in numbers and not convert to biomass), the `@length_weight` argument is turned off by specifying the keyword `none` in the `@age_length` block

```
@age_length age_size
type schnute
...
length_weight none
```

In this case any "biomass" generated by CASAL2 will actually be abundance, and care should be taken with interpretation of the output.

4.11. Maturity, in models without maturing in the partition

If maturity is not a characteristic of the partition it can be derived using selectivities. The mature individuals in a population can be calculated by applying a maturity selectivity to the partition. These numbers can then be used in processes, in calculating mature biomass (using derived quantities), and in reports for the mature partition as an output.

4.12. Selectivities

A selectivity is a function that can have a different value for each age class. Selectivities are used to fit to observations (Section 5) or to modify the effects of processes on each age class (Section 4).

There are a number of different parametric forms as options, including logistic, knife edge, and double normal selectivities. Selectivities are defined in command block (@selectivity), where the unique label of the selectivity is used by observations and processes to identify which selectivity to apply.

Selectivities are indexed by age, with indices from `min_age` to `max_age`. S logistic age-based selectivity with 50% selected at age 5 and 95% selected at age 7 would be defined by the `type=logistic` with parameters $a_{50} = 5$ and $a_{t095} = (7 - 5) = 2$. The value of the selectivity at age $x = 7$ is 0.95, and the value at age $x = 3$ is 0.05.

For some selectivities the function values for some choices of parameters can result in numeric overflow or underflow errors (i.e., the number calculated from parameter values is either too large or too small to be well represented). CASAL2 implements range checks on some parameters to test for these errors before calculating function values.

For example, the logistic selectivity is implemented such that if $(a_{50} - x)/a_{t095} > 5$ then the value of the selectivity at $x = 0$, i.e., for $a_{50} = 5$, $a_{t095} = 0.1$, then the value of the selectivity at $x = 1$, without range checking would be 7.1×10^{-52} . With range checking, that value is 0 (as $(a_{50} - x)/a_{t095} = 40 > 5$).

The selectivities options are:

- Constant
- Knife-edge
- All values
- All values bounded
- Increasing
- Logistic
- Inverse logistic (descending logistic?)
- Logistic producing

- Double normal
- Double exponential

4.12.1. constant

$$f(x) = C \quad (4.37)$$

The constant selectivity has the estimable parameter C .

4.12.2. knife_edge

$$f(x) = \begin{cases} 0, & \text{if } x < E \\ \alpha, & \text{if } x \geq E \end{cases} \quad (4.38)$$

The knife-edge ogive has the estimable parameter E and a non-estimable scaling parameter α , where the default value of $\alpha = 1$.

4.12.3. all_values

$$f(x) = V_x \quad (4.39)$$

The all-values selectivity has estimable parameters $V_{low}, V_{low+1} \dots V_{high}$. The selectivity value for each age class must be set.

4.12.4. all_values_bounded

$$f(x) = \begin{cases} 0, & \text{if } x < L \\ V_x, & \text{if } L \leq x \leq H \\ V_H, & \text{if } x > H \end{cases} \quad (4.40)$$

The all-values-bounded selectivity has non-estimable parameters L and H . The estimable parameters are $V_L, V_{L+1} \dots V_H$. Selectivity values for each age class from $L \dots H$ must be set.

4.12.5. increasing

$$f(x) = \begin{cases} 0, & \text{if } x < L \\ f(x-1) + \pi_x(\alpha - f(x-1)), & \text{if } L \leq x \leq H \\ f(\alpha), & \text{if } x \geq H \end{cases} \quad (4.41)$$

The increasing ogive has non-estimable parameters L and H . The estimable parameters are $\pi_L, \pi_{L+1} \dots \pi_H$; if these are estimated, they should always be constrained to be between 0 and 1. α is a scaling parameter, with default value of $\alpha = 1$. The increasing ogive is similar to the all-values-bounded ogive, and is constrained to be non-decreasing.

4.12.6. logistic

$$f(x) = \alpha / [1 + 19^{(a_{50}-x)/a_{t095}}] \quad (4.42)$$

The logistic selectivity has estimable parameters a_{50} and a_{t095} . α is a scaling parameter, with default value of $\alpha = 1$. The logistic selectivity takes values 0.5α at $x = a_{50}$ and 0.95α at $x = a_{50} + a_{t095}$.

4.12.7. inverse_logistic

$$f(x) = \alpha - \alpha / [1 + 19^{(a_{50}-x)/a_{t095}}] \quad (4.43)$$

The inverse logistic selectivity has estimable parameters a_{50} and a_{t095} . α is a scaling parameter, with default value of $\alpha = 1$. The logistic selectivity takes values 0.5α at $x = a_{50}$ and 0.95α at $x = a_{50} - a_{t095}$.

4.12.8. logistic_producing

$$f(x) = \begin{cases} 0, & \text{if } x < L \\ \lambda(L), & \text{if } x = L \\ (\lambda(x) - \lambda(x-1)) / (1 - \lambda(x-1)), & \text{if } L < x < H \\ 1, & \text{if } x \geq H \end{cases} \quad (4.44)$$

The logistic-producing selectivity has non-estimable parameters L and H . The estimable parameters are a_{50} and a_{t095} . α is a scaling parameter, with default value of $\alpha = 1$.

For category transitions, $f(x)$ represents the proportion moving, not the proportion that have moved. This selectivity was designed for use in an age-based model to model maturity. In such a model, a logistic-producing maturation selectivity will, in the absence of other influences, make the proportions mature follow a logistic curve with parameters a_{50} and a_{t095} .

4.12.9. double_normal

$$f(x) = \begin{cases} \alpha 2^{-[(x-\mu)/\sigma_L]^2}, & \text{if } x \leq \mu \\ \alpha 2^{-[(x-\mu)/\sigma_R]^2}, & \text{if } x \geq \mu \end{cases} \quad (4.45)$$

The double-normal selectivity has estimable parameters a_1 , s_L , and s_R . α is a scaling parameter, with default value of $\alpha = 1$. It has values α at $x = a_1$, and 0.5α at $x = a_1 - s_L$ and $x = a_1 + s_R$.

4.12.10. double_exponential

$$f(x) = \begin{cases} \alpha y_0 (y_1/y_0)^{(x-x_0)/(x_1-x_0)}, & \text{if } x \leq x_0 \\ \alpha y_0 (y_2/y_0)^{(x-x_0)/(x_2-x_0)}, & \text{if } x > x_0 \end{cases} \quad (4.46)$$

The double-exponential selectivity has non-estimable parameters x_1 and x_2 . The estimable parameters are x_0 , y_0 , y_1 , and y_2 . α is a scaling parameter, with default value of $\alpha = 1$. This selectivity curve can be "U-shaped". Bounds for x_0 must be such that $x_1 < x_0 < x_2$. With $\alpha = 1$, the selectivity passes through the points (x_1, y_1) , (x_0, y_0) , and (x_2, y_2) . If both y_1 and y_2 are greater than y_0 the selectivity is "U-shaped" with minimum at (x_0, y_0) .



Figure 4.3: Examples of the selectivities

Selectivities `all_values` and `all_values_bounded` can be included in additional priors using the syntax

```
@selectivity maturity
type all_values
v 0.001 0.1 0.2 0.3 0.4 0.3 0.2 0.1

## encourage ages 3-8 to be smooth.
@additional_prior smooth_maturity
type vector_smooth
parameter selectivity[maturity].values{3:8}
```

4.13. Projections

This section lists all the projections classes available, their functionality, and an example of the syntax.

4.13.1. The constant projection class, `constant`

A parameter can either be fixed during all projection years or specified individually for each projection year. This is a deterministic assumption, where the parameter is assumed to be known without error during projection years.

```
@project Future_ycs
type constant
parameter process[Recruitment].ycs_values
years 2012:2016
values 1 2 1 2 0.5
multiplier 1
```

4.13.2. Sampling from a range of years, `empirical_resampling`

Parameters that have time components associated with them can be re-sampled uniformly with replacement over a range of years and used as values for the projected years. The year range to sample from is between `start_year` and `final_year`:

```
@project Future_ycs
type empirical_sampling
parameter process[Recruitment].ycs_values
years 2012:2016
start_year 1988
final_year 2008
multiplier 1
```

4.13.3. Sampling from a lognormal distribution, `lognormal`

The parameters are drawn from a Gaussian distribution in log space and exponentiated to result in the lognormal distribution

$$X_p = \exp(\epsilon_p - \sigma^2/2) \tag{4.47}$$

where $\epsilon_p \stackrel{iid}{\sim} N(\mu, \sigma)$ and X_p is the projected value for parameter X , and μ and σ are the mean and standard deviation on the log scale.

An example of applying this process to draw future year class parameters from a lognormal distribution with mean 1 and standard deviation 0.8

```
@project Future_ycs
type lognormal
parameter process[Recruitment].ycs_values
years 2012:2016
```

```
mean 0
sigma 0.8
multiplier 1
```

4.13.4. Sampling from a lognormal distribution defined by values from a range of years, `lognormal_empirical`

This class applies a lognormal draw as in the `LogNormal` class and specifies a year range which is re-sampled uniformly without replacement. These re-sampled values are then used to calculate the standard deviation of the distribution. Then equation (4.47) is used to generate future values with a specified μ and empirically calculated σ ,

```
@project Future_ycs
type lognormal_empirical
parameter process[Recruitment].ycs_values
years 2012:2016
mean 0
start_year 1988
final_year 2008
multiplier 1
```

4.13.5. Sample using a user-defined function, `user_defined`

This class uses the equation parser to define the future values of a parameter during projection mode. This was set up to define and apply harvest control rules (i.e., apply a management action such as changing the TACC based on the current or previous state).

In fisheries models, this option can be used to calculate the projected catch based on an exploitation rate multiplied by the vulnerable biomass, where the exploitation rate is based on a rule (Figure 4.4).



Figure 4.4: Examples of control rules based on current stock status.

```
@project HCR_2015
type user_defined
parameter process[Instantaneous_Mortality].method_Sub_Ant_F
years 2015
equation if(derived_quantity[SSB].values{2014} / process[Recruitment].b0 <= 0.1, 0.0,
if(derived_quantity[SSB].values{2014} / process[Recruitment].b0 > 0.1 &&
derived_quantity[SSB].values{2014} / process[Recruitment].b0 < 0.2,
derived_quantity[SSB].values{2014} * derived_quantity[SSB].values{2014}
/ process[Recruitment].b0,
derived_quantity[SSB].values{2014} * 0.2))
```

Care should be taken when writing user-defined equations. The above equation is: if $\%B_{2014} \leq 0.1$ then set next year's catch to 0.0, else if $\%B_{2014} > 0.1$ & $\%B_{2014} \leq 0.2$ then set next year's catch equal to $\%B_{2014} \times SSB_{2014}$, else set next year's catch to $0.2SSB_{2014}$.

4.13.6. Projections with catches specified

Catches are unique in that they are known inputs in a table format. For example, to project catches that are in a table

```
# fishing process
@process Fishing
type mortality_instantaneous_retained
m 0.17*6 #0.17 #testing at old values
time_step_ratio 1
selectivities One*6 #for age based M
categories *
table catches
year FishingLine FishingPot Recreation
1900 0 0 0
1901 13.2 0 22.9
1902 26.4 0 23.5
1903 39.6 0 24
end_table

# projection block
@project future_catch
type constant
parameter process[Fishing].method_fishingpot
years 2020:2029
values 4000
```

This uses the syntax `block_type[block_label].method_fishinglabel`. **Note:** the fishing label which is defined in the table needs to be lower case form in the `@projection` block.

4.14. Time-varying Parameters

CASAL2 has the functionality to vary any parameter annually between the start and final year of a model run. This can be for blocks of years or specific years. For years that are not specified the parameter will default to the input, or if in an iterative state such as estimation mode, the value being trialled at that iteration.

Method types for a time-varying parameter are:

- constant,
- random_walk,
- exogenous,
- linear,
- annual_shift, and
- random_draw.

This option allows for a parameter to be known in a year, or be the result of a deterministic or stochastic equation. **Note:** the stochastic time-varying functionality was added for simulation purposes. It has not been tested in an estimation context.

To implement hierarchical models, estimated the prior parameter values with hyperpriors. To implement a hierarchical model using the time-varying functionality, use MCMC estimation to calculate the integral which is required to obtain unbiased estimates. In an MCMC context a Gibbs sampler is assumed. That is, every draw is from a conditional distribution and so every draw is a candidate value.

When allowing removals with annually varying catchabilities, selectivities, and/or other model components, simulated observations more closely model real data and associated conclusions

become more useful. Implementing time-varying parameters also allows for mean or location parameters of selectivities to change between years based on an explanatory variable. An example of this is in the New Zealand Hoki fishery where the μ and a_{50} parameters are allowed to shift depending on when the fishing season occurs. Descriptive analysis showed that when fishing was earlier relative to other years smaller fish were caught and vice versa. This can be shown in the CASAL2/Examples/2stock directory, implemented at line: 382 in the `population.csl2` file.

4.14.1. constant

This option allows a parameter to have an alternative value during certain years, which can be estimated.

```
@time_varying q_time_var
type constant
parameter catchability[survey_q].q
years 1975:1988
values 0.001
```

These year values can be estimated using the syntax

```
@estimate q_time_var
type uniform
parameter time_varying[q_time_var].values(1975:1976)
lower_bound 1e-6 1e-6
upper_bound 2 2
```

Caution: do not estimate both the actual parameter and its time-varying counterpart, as the time-varying value will overwrite the actual parameter making the actual value unidentifiable.

4.14.2. random_walk

A random deviate drawn from a standard normal distribution is added to the previous value. This option has an estimable parameter σ_p for each time-varying parameter p . For reproducible modelling when using stochastic functionality, set the random seed (see Section 3.3).

```
@time_varying q_time_var
type random_walk
parameter catchability[survey_q].q
distribution normal
mean 0
sigma 3
```

If the parameter specified in the `@time_varying` block is associated with an `@estimate` block, then the parameter is constrained to stay within the lower and upper bounds of the `@estimate` block.

WARNING: if the parameter does not have an associated `@estimate` block then there is no safeguard against the application of a random deviate resulting in parameter values which cause the model to fail, i.e., generates NA or INF values. To avoid this, specify an `@estimate` block even though the parameter is not actually being estimated; see the example syntax below.

A constraint whilst using this functionality is that a parameter cannot be less than 0.0. If it is then CASAL2 sets it equal to 0.01.

```
@estimate survey_q_est
type uniform
parameter catchability[survey_q].q
lower_bound 1e-6
upper_bound 10
```

This configuration will insure the random walk time-varying process will set the any new candidate values within the lower and upper bound of the @estimate block.

4.14.3. annual_shift

A parameter generated in year y (θ'_y) depends on the value specified by the user (θ_y) along with three coefficients a , b , and c

$$\bar{\theta}_y = \frac{\sum_y^Y \theta_y}{Y} \quad (4.48)$$

$$\theta'_y = a\bar{\theta}_y + b\bar{\theta}_y^2 + c\bar{\theta}_y^3 \quad (4.49)$$

4.14.4. exogenous

Parameters are shifted based on an exogenous variable. An example of this is an exploitation selectivity parameters that may vary between years based on known changes in exploitation behaviour such as season, start time, and average depth of exploitation.

$$\delta_y = a(E_y - \bar{E}) \quad (4.50)$$

$$\theta'_y = \theta_y + \delta_y \quad (4.51)$$

where δ_y is the shift or deviation in parameter θ_y in year y to generate the new parameter value in year y (θ'_y). a is an estimable shift parameter, E is the exogenous variable, and E_y is the value of this variable in year y . For more information readers can see [Francis et al. \(2003\)](#).

4.15. Equation Parser

CASAL2 has equation parser functionality, which is currently implemented in Projections (section 4.13), Derived quantities (section 4.6), and Reports (section 7).

Examples of syntax for implementing the equation parser are below. For more information on the parser, see <https://github.com/nickgammon/parser/blob/master/parser.cpp>

TODO what does this first example do?

```
equation process[Recruitment].r0 * (2-1)
```

mathematical functions such as `sqrt()`, `log()`, `exp()`, `cos()`, `sin()`, and `tan()` can be used

```
equation sqrt(process[Recruitment].r0)
```

exponents can be used with `pow()`

```
equation pow(2, 3)
```

the absolute value of an equation using `abs()`

```
equation abs(sqrt(process[Recruitment].r0) * 1.33)
```

if-else statements can be used

```
equation if(process[Recruitment].r0 > 23, 44, 55)
## if R0 is greater than 23 return 44 else return 55
```

if-else statements can also be linked, more complex syntax

```
equation if(process[Recruitment].r0 > 23, 44,
            if(process[Recruitment].r0 > 10, 55, 66))
## if R0 is greater than 23 return 44 else if R0 less than 23 but greater than 10 return 55,
else R0 must be less than 10 return 66
```

Only single values can be referenced, so an equation cannot be applied to a vector, e.g., `process[Recruit].yrs_values{1974:1980}` cannot be referenced. More information on which parameters can be included in an equation parser is available (Section 12). Any subcommand that has a type `estimable` could be referenced with the equation parser.

Note: the equation parser will not catch all user configuration errors, such as checking whether a parameter that exists in the system has been populated when it is required.

For example, the wrong year could be misspecified in the case of removals in year y which is based on the state of the population in year $y - 1$

```
parameter process[removals].catch
year 2015
equation derived_quantity[percent_b0].values{2020}
```

This example is a valid equation but it will have nonsensical results, since a value for 2020 is to be calculated using values for 2015. Although the equation parser adds flexibility, it is easy to misspecify equations.

5. The estimation section

5.1. Role of the estimation section

The role of the estimation section is to define the tasks carried out by CASAL2:

1. Define the objective function (see Section 5.2)
2. Define the parameters to be estimated (see Section 5.3)
3. Calculate a point estimate, i.e., the maximum posterior density estimate (MPD) (see Section 5.4)
4. Calculate a posterior profile on selected parameters, i.e., for each of a series of values of a parameter, minimise the objective function, allowing the other estimated parameters to vary (see Section 5.5)
5. Generate MCMC samples from the posterior distribution (see Section 5.6)
6. Calculate the approximate covariance matrix of the parameters as the inverse of the minimizer's approximation to the Hessian, and the corresponding correlation matrix (see Section 5.4)

The estimation section defines the objective function, parameters of the model, and the method of estimation (point estimates, Bayesian posteriors, profiles, etc.). The objective function is based on a goodness-of-fit measure of the model to observations, the assumed priors, and the penalties. See the observation section for a description of the observations, likelihoods, priors, and penalties.

5.2. The objective function

In Bayesian estimation, the objective function is a negative log-posterior,

$$Objective(p) = -\sum_i \log [L(\mathbf{p}|O_i)] - \log [\pi(\mathbf{p})] \quad (5.1)$$

where π is the joint prior density of the parameters p .

The contribution to the objective function from the likelihood components is described in Section 6.2. In addition to likelihoods, priors (see Section 5.7) and penalties (see Section 5.8) are components of the objective function. Note that if the priors are specified as uniform, then the prior contribution is zero and the optimisation is now a penalised likelihood and not Bayesian.

Penalties can be used to ensure that the estimated parameter values and derived quantities meet certain restrictions. For example, exploitation rate constraints on mortality events (i.e., fisheries) that are not violated (otherwise there is nothing to prevent the model from having abundances so low that the recorded catches could not have been taken); penalties on category transitions (to ensure there are enough individuals to move); penalties such that estimated values are similar or smooth, etc.

Equation 5.1 can be reduced to a penalised likelihood equation if all priors are assumed to be uniform. This is because uniform priors have no contribution to the objective function so Equation 5.1 reduces to the likelihood components plus penalties.

5.3. Specifying the parameters to be estimated

The parameters to be estimated (estimables) are defined using `@estimate` commands (see Section 9).

For example, a `@estimate` command block

```
@estimate male.m
parameter process[NaturalMortality].m{male}
lower_bound 0.1
upper_bound 0.4
type uniform
```

See Section 3.4.5 for information on how to specify the parameter name. At least one parameter is required to be estimated if doing an estimation `-e`, profile `-p`, or MCMC `-m` run. Initial values for the parameters to be estimated are required, and these values are used as the starting values for the minimiser. However, these values may be overwritten if a set of alternative starting values is provided (i.e., using `casal2 -i`, see Section 3.3).

All parameters are estimated within the specified bounds. For each parameter estimated, the lower and upper bounds and the prior (`type`) (Section 5.7) must be specified. The bounds and the prior should be chosen carefully as they affect the values over which the minimisers search. Some minimisers convert the lower and upper bounds into a minimisation space (for example `-1,1` space for the numerical differences algorithm). If estimating only some elements of a vector, either define each element of the vector to be estimated (see 3.4.5) or fix the others by setting the lower and upper bounds to the same value as the initial value.

5.4. Point estimation

Point estimation is invoked with `casal2 -e`, which attempts to find a minimum of the objective function. CASAL2 has multiple minimisation algorithms. There are three automatic differentiation (AD) minimisers: ADOL-C, CppAD, and BetaDiff (the minimiser used in CASAL). There are also three non-automatic differentiation minimisers: numerical differences, differential evolution minimiser (`de_solver`), and the dlib minimiser (see Section 1.8). AD minimisers are recommended for more complex models as they are on average much faster and tend to find a more robust minimum when exploring a complex objective surface.

An important input parameter for most minimisers is the `tolerance` parameter. This is one of the stopping rules that minimisers use to define when they have found a 'solution' (although a solution may be a local minimum and not the global minimum). To evaluate the robustness of a solution, use a set of different starting values, with the `-i parameter_file.txt` option.

Start with the default `tolerance` parameter value of 0.002 and decrease it while developing a model. For a given model, the parameter estimates when minimising with tolerance value 0.0000002 may be quite different from those with the default tolerance value. This is not robust model behaviour and more investigative and diagnostic work may be required to determine what parameters are causing this behaviour. *Note:* this issue will also affect the covariance matrix. When a different tolerance value and/or minimiser is used, a different approximate Hessian matrix which is inverted to solve for the covariance matrix may be produced. The effect that this behaviour has on MCMC samples is not well-determined.

5.4.1. The numerical differences minimiser

The minimiser has three kinds of (non-error) exit status, depending on the minimiser:

- Successful convergence (suggests a local minimum has been found, at least).
- Convergence failure (a local minimum has not been found, although the results may be 'close enough').
- Convergence unclear (the minimiser halted but was unable to determine if convergence occurred. The result may be a local minimum, although this can be checked by restarting the minimiser at the final values of the estimated parameters).

The maximum number of quasi-Newton iterations and objective function evaluations allowed can be specified. If either limit is exceeded, the minimiser exits with a convergence failure. Set the maximum number of evaluations and iterations to values larger than the defaults of 300 and 1000, unless convergence is reached with fewer. An alternative starting point of the minimiser can be specified using `casal2 -i`.

The minimisers are local optimisation algorithms trying to solve a global optimisation problem. What this means is that, even if a 'successful convergence' is reached, the solution may be only a local minimum, and not a global one. To diagnose this problem, start multiple runs from different starting points and comparing the results, or do profiles of one or more key parameters and seeing if any of the profiled estimates finds a better optimum than the original point estimate.

The approximate covariance matrix of the estimated parameters can be calculated as the inverse of the minimiser's approximation to the Hessian, and the corresponding correlation matrix is also calculated.

Note that

- the Hessian approximation develops over many minimiser steps, so if the minimiser has only run for a small number of iterations the covariance matrix can be a very poor approximation; and
- the inverse Hessian is not a good approximation to the covariance matrix of the estimated parameters, and may not be useful to construct, for example, confidence intervals.

Also note that if an estimated parameter has equal lower and upper bounds, it will have entries of '0' in the covariance matrix and NaN or -1.#IND (depending on the operating system) in the correlation matrix.

```
@minimiser numerical_diff
type numerical_differences
tolerance 1e-6
iterations 2500
evaluations 4000
```

5.4.2. The differential evolution minimiser

The differential evolution minimiser is a simple population-based, stochastic function minimizer, but is claimed to be quite powerful in solving minimisation problems. It is a method of mathematical optimization of multidimensional functions and belongs to the class of evolution strategy optimizers (TODO reference?).

Initially, the procedure randomly generates and evaluates a number of solution vectors (the population size), each with p parameters. Then, for each generation (iteration), the algorithm creates a candidate solution for each existing solution by random mutation and uniform crossover. The random mutation generates a new solution by multiplying the difference between two randomly selected solution vectors by some scale factor, then adding the result to a third vector. Then an element-wise crossover takes place with probability P_{cr} , to generate a potential candidate solution. If this is better than the initial solution vector, it replaces it, otherwise the original solution is retained. The algorithm terminates after either a predefined number of generations (`max_generations`) or when the maximum difference between the scaled individual parameters from the candidate solutions from all populations is less than some predefined amount `tolerance`.

The differential evolution minimiser can be good at finding global minimums in surfaces that may have local minima. However, the speed of the minimiser, and the ability to find a good minima depend on the number of initial 'populations'. Some authors recommend that the number of populations be set at about $10 * p$, where p is the number of free parameters. However, depending on the model, this value can be set to a lower value and still find a robust solution.

There is no proof of convergence for the differential evolution solver, but several papers have found it to be an efficient method of solving multidimensional problems. Some results suggest that it can often find a better minima and may be faster or longer (depending on the actual model specification) at finding a solution when compared with the numerical differences minimiser. Comparisons with automatic differentiation minimisers or other more sophisticated algorithms have not been made.

```
@minimiser DE_solver
type de_solver
tolerance 1e-6
iterations 2500
evaluations 4000
```

5.4.3. The BetaDiff minimiser

An automatic differentiation minimiser for non-linear models, This is the minimiser from the original CASAL package, based on ADOL-C.

```
@minimiser beta_diff
type beta_diff
tolerance 1e-6
iterations 2500
evaluations 4000
```

5.4.4. The ADOL-C minimiser

An automatic differentiation minimiser for non-linear models. See <https://projects.coin-or.org/ADOL-C> for more information.

```
@minimiser ADOLC
type adolc
step_size 1e-6
iterations 2500
evaluations 4000
tolerance 1e-6
```

5.4.5. The CppAD minimiser

An automatic differentiation minimiser for non-linear models using the MUMPS solver. See <https://coin-or.github.io/CppAD/doc/cppad.htm> and https://www.coin-or.org/CppAD/Doc/ipoft_solve.htm for more information.

```
@minimiser CPPAD
type cppad
```

CppAD has an implicit tolerance value of $1e-9$.

Some results suggest that this solver may be one of the quickest solvers for models that have a reasonably well-defined solution, i.e., the data are informative with respect to determining the estimated parameters.

5.4.6. The Dlib minimiser

Non-automatic differentiation minimiser. See <http://dlib.net/> for more information.

```
@minimiser Dlib
type dlib
tolerance 1e-6
iterations 2500
evaluations 4000
```

5.5. Posterior profiles

If profiles are run using the command `casal2 -p`, CASAL2 will first calculate a point estimate. For each scalar parameter or, in the case of vectors or selectivities, the element of the parameter to be profiled, CASAL2 will fix its value at a sequence of n evenly spaced numbers (*step*) between the specified lower and upper bounds l and u , and calculate a point estimate at each value.

By default $step = 10$, and $(l, u) = (\text{lower bound on parameter plus } (range/(2n)), \text{upper bound on parameter less } (range/(2n)))$. Each minimisation starts at the final parameter values from the previous resulting value of the parameter being profiled. CASAL2 will report the objective function for each parameter value. The initial point estimate should be compared with the profile results, to check at least that none of the other points along the profile have a better objective function value than the initial 'minimum'.

The parameters to be profiled are specified, and optionally the number of steps, and lower bound and upper bound, for each parameter. In the case of vector parameters, the element(s) of the vector to be profiled are specified.

The initial starting point for the estimation can also be specified using `casal2 -i file`, which may improve the minimiser performance for the profiles.

If the profile results are not reasonable, it may be a result of not using enough iterations in the minimiser or a poor choice of minimiser control variables (e.g., the minimiser tolerance). It may also be useful to try other minimisers and compare the results.

5.6. Bayesian estimation

CASAL2 can use Markov chain Monte Carlo (MCMC) functionality to generate a sample from the posterior distribution of the estimated parameters with command `casal2 -m` and output the sampled values to a file, optionally keeping only every n th set of values.

As CASAL2 has no post-processing capabilities. CASAL2 cannot produce MCMC convergence diagnostics. To calculate these diagnostics, use a package such as BOA, plot/summarize the posterior distributions of the output quantities, and/or use a general-purpose statistical package such as R.

Bayesian methodology and MCMC are both large and complex topics. See Gelman et al. (1995) and Gilks et al. (1994) for details of both Bayesian analysis and MCMC methods. In addition, see Punt & Hilborn (2001) for an introduction to quantitative fish stock assessment using Bayesian methods.

This section briefly describes the MCMC algorithms used in CASAL2. See Section 9.3 for a description of the sequence of CASAL2 commands used in a full Bayesian analysis.

CASAL2 uses a straightforward implementation of the Metropolis-Hastings algorithm (Gelman et al., 1995, Gilks et al., 1994). The Metropolis-Hastings algorithm attempts to draw a sample from a Bayesian posterior distribution, and calculates the posterior density π , scaled by an unknown constant. The algorithm generates a 'chain' or sequence of values. Typically the beginning of the chain is discarded (the burn-in period) and every N th element of the remainder is taken as the posterior sample.

The chain is produced by taking an initial point x_0 and repeatedly applying the following rule, where x_i is the current point:

1. Draw a candidate step s from a proposal distribution J , which should be symmetric i.e., $J(-s) = J(s)$
2. Calculate $r = \min(\pi(x_i + s)/\pi(x_i), 1)$
3. Let $x_{i+1} = x_i + s$ with probability r , or x_i with probability $1 - r$

An initial point estimate is produced before the chain starts, which is done so as to calculate the approximate covariance matrix of the estimated parameters (as the inverse Hessian), and may also be used as the starting point of the chain.

The starting point of the point estimate minimiser can be specified using the command `casal2 -i`. Don't start it too close to the actual estimate (either by using `casal2 -i`, or by changing the initial parameter values in input configuration file) as it takes a few iterations to determine a reasonable approximation to the Hessian.

There are currently two options for the starting point of the MCMC:

- Start from the point estimate; or
- Restart a chain given a covariance matrix and a previous starting point.

The chain moves in natural space, i.e., no transformations are applied to the estimated parameters. The default proposal distribution is a multivariate Student's t distribution centred on the current point, with covariance matrix equal to a matrix based on the approximate covariance produced by the minimiser, multiplied by a stepsize factor.

The following steps define how the initial covariance matrix of the proposal distribution is calculated:

1. The covariance matrix is taken as the inverse of the approximate Hessian from the quasi-Newton minimiser.
2. The covariance matrix is modified so as to decrease all correlations greater than `@mcmc.max_correlation` down to `@mcmc.max_correlation`, and similarly to increase all correlations less than `-@mcmc.max_correlation` up to `-@mcmc.max_correlation` (the `@mcmc.max_correlation` parameter defaults to 0.8). This should help to avoid getting 'stuck' in a lower-dimensional subspace.
3. The covariance matrix is then modified either by
 - `@mcmc.adjustment_method=covariance`: that if the variance of the i th parameter is non-zero and less than `@mcmc.min_difference` multiplied by the difference between the parameters' lower and upper bound, then the variance is changed, without changing the associated correlations, to $k = \min_diff(upper_bound_i - lower_bound_i)$. This is done by setting

$$\text{Cov}(i, j)' = \text{sqrt}(k) \text{Cov}(i, j) / \text{sd}(i)$$

for $i \neq j$, and $\text{var}(i)' = k$

- `@mcmc.adjustment_method=correlation`: that if the variance of the i th parameter is non-zero and less than `@mcmc.min_difference` multiplied by the difference between the parameters' lower and upper bounds, then its variance is changed to $k = \min_diff(upper_bound_i - lower_bound_i)$. This differs from (i) above in that the effect of this option is that it also modifies the resulting correlations between the i th parameter and all other parameters.

This allows each estimated parameter to move in the MCMC even if its variance is very small according to the inverse Hessian. In both cases, the `@mcmc.min_difference` parameter defaults to 0.0001.

4. The `@mcmc.stepsize` (a scalar factor applied to the covariance matrix to improve the acceptance probability) is set by the user. The default is $2.4d^{-0.5}$ where d is the number of estimated parameters, as recommended by Gelman et al. (Gelman et al., 1995). However, a smaller value may often be better.

The proposal distribution can also change adaptively during the chain, using two different mechanisms. Both are offered as means of improving the convergence properties of the chain. It is important to note that any adaptive behaviour must finish before the end of the burn-in period, i.e., the proposal distribution must be finalised before the kept portion of the chain starts.

The adaptive mechanisms are:

- The stepsize changes adaptively at one or more sample numbers (See next paragraph for details on the stepsize adaptation methods)
- The entire covariance matrix changes adaptively at one or more sample numbers. At each adaptation, the covariance matrix is replaced with an empirical covariance matrix, derived from the MCMC chain. The idea is that an empirical covariance is a better approximation of the proposal distribution than the inverse of the Hessian matrix, and can improve convergence and mixing of the chain.

The two options to adapt the step size are `double_half` or `ratio`, which is chosen with the input parameter `adapt_stepsize_method`. The `double_half` method is used in CASAL (see Gelman et al. (Gelman et al., 1995) for justification).

The algorithm for `double_half` is, at each adaptation, the stepsize is doubled if the acceptance rate since the last adaptation is more than 0.5, or halved if the acceptance rate is less than 0.2. The `ratio` is taken from SPM. It adapts the current step size by the acceptance rate since the last adaptation multiplied by 4.1667 to reach an acceptance rate of ≈ 0.24 . See [Sherlock and Roberts \(2009\)](#) for justification on that acceptance rate.

The stepsize parameter is now on a completely different scale, and must be rescaled. It is set to a user-specified value (which may or may not be the same as the initial stepsize). Set the stepsize adaptations to occur after this, so that the stepsize can be readjusted to an appropriate value which gives good acceptance probabilities with the new matrix.

All modified versions of the covariance matrix are printed to the standard output, but only the initial covariance matrix (inverse Hessian) is saved to the objectives file. The number of covariance modifications by each iteration is recorded as a column on the objectives file.

The variance-covariance matrix of this sub-sample of chain is calculated. As above, correlations greater than `@mcmc.max_correlation` are reduced to `@mcmc.max_correlation`, correlations less than `-@mcmc.max_correlation` are increased to `-@mcmc.max_correlation`, and very small non-zero variances are increased (`@mcmc.covariance_adjustment` and `@mcmc.min_difference`). The result is the new variance-covariance matrix of the proposal distribution.

The procedure used to choose the sample of points is that, to start, all points on the chain so far are taken. (TODO reword this paragraph) All points in an initial user-specified period are discarded. The assumption is that the chain will have started moving during this period. If this is incorrect and the chain has still not moved by the end of this period, it is a fatal error and CASAL2 stops. The remaining set of points must contain at least some user-specified number of transitions. If this is incorrect and the chain has not had at least this number of transitions, then it is also a fatal error. If this test is passed, the set of points is systematically sub-sampled down to 1000 points (and it must be at least this long to start with).

The probability of acceptance for each jump is 0 if the jump would move a parameter value outside of its bounds, 1 if it improves the posterior, or $(\text{newposterior}/\text{oldposterior})$ otherwise. How often the position of the chain is recorded is specified with the `keep` parameter. For example, with `keep 10`, only every 10th sample is recorded.

The option to specify that some of the estimated parameters are fixed during the MCMC is available. If the chain starts at the point estimate or at a random location, these fixed parameters are set to their values at the point estimate.

If the start of the chain is specified with the command `casal2 -i`, these fixed parameters are set to the values in the file.

Restarting an MCMC chain: in the case where an MCMC chain was halted or interrupted, the MCMC chain can be restarted from where it finished with

```
casal2 -m --resume --objective-file Objective_file_name --sample-file Sample_file_name
```

where `Objective_file_name` is the file name for the objective function report and `Sample_file_name` is the file name for the sample report from a MCMC chain.

The posterior sample can be used for (projections (Section 4.4.5)) or simulations (Section 6.6) with the values supplied with the command `casal2 -i file`.

A multivariate Student's t distribution is used as an alternative to the multivariate normal proposal distribution. If you request multivariate Student's t proposals, change the degrees of freedom from the default of 4. As the degrees of freedom decreases, the t distribution becomes more heavy tailed.

This may lead to better convergence properties. Note the default is the multivariate Student's t .

Given a posterior (sub)sample, CASAL2 can calculate a list of output quantities for each sample point (see Section 7 specifically tabular report). These quantities can be output to a file (with the command `casal2 -r -tabular`) and read into an external software package where the posterior distributions can be plotted and/or summarised.

The posterior sample can also be used for projections (Section 4.4.5). The advantage of this is that the parameter uncertainty, as expressed in the posterior distribution, can be included into the risk estimates.

5.7. Priors

In a Bayesian analysis, a prior is required for every parameter that is being estimated. There are no default priors.

When some of these priors are parameterised in terms of mean, c.v., and standard deviation, these refer to the parameters of the distribution before the bounds are applied. The moments of the prior after the bounds are applied may differ.

CASAL2 has the following priors (expressed in terms of their contribution to the objective function):

1. Uniform

$$-\log(\pi(p)) = 0 \quad (5.2)$$

2. Uniform-log (i.e., $\log(p) \sim \text{uniform}$)

$$-\log(\pi(p)) = \log(p) \quad (5.3)$$

3. Normal with mean μ and c.v. c

$$-\log(\pi(p)) = 0.5 \left(\frac{p - \mu}{c\mu} \right)^2 \quad (5.4)$$

4. Normal with mean μ and standard deviation σ

$$-\log(\pi(p)) = 0.5 \left(\frac{p - \mu}{\sigma} \right)^2 \quad (5.5)$$

5. Lognormal with mean μ and c.v. c

$$-\log(\pi(p)) = \log(p) + 0.5 \left(\frac{\log(p/\mu)}{s} + \frac{s}{2} \right)^2 \quad (5.6)$$

where s is the standard deviation of $\log(p)$ and $s = \sqrt{\log(1 + c^2)}$.

6. Beta with mean μ and standard deviation σ , and range parameters A and B

$$-\log(\pi(p)) = (1-m)\log(p-A) + (1-n)\log(B-p) \quad (5.7)$$

where $v = \frac{\mu-A}{B-A}$, and $\tau = \frac{(\mu-A)(B-\mu)}{\sigma^2} - 1$ and then $\mu = \tau v$ and $n = \tau(1-v)$. Note that the beta prior is undefined when $\tau \leq 0$.

Vectors of parameters can be independently (but not necessarily identically) distributed according to any of the above forms, in which case the joint negative-log-prior for the vector is the sum of the negative-log-priors of the components. Values of each parameter need to be specified for each element of the vector. Example of syntax to define the estimation of a parameter and the prior assumed:

```
## uniform-log example estimate
@estimate B0
type uniform_log # this command "type" defines the prior type.
parameter process[Recruitment].b0 # "Recruitment" is the label of your process
upper_bound 20000
lower_bound 1000

## Lognormal YCS estimation
@estimate year_class_strengths_1990_1995
type lognormal
parameter process[Recruitment].ycs_values{1990:1995}
# ycs_year 1990 1991 1992 1993 1994 1995
mu      1      1      1      1      1      1
cv    0.9  0.9  0.9  0.9  0.9  0.9
lower_bound 0.01 0.01 0.01 0.01 0.01 0.01
upper_bound 9 9 9 9 9 9
```

5.8. Penalties

Penalties are associated with processes and can be used to enforce parameter value or derived quantity restrictions or model outputs that are invalid by adding a penalty to the objective function. For example, estimated parameter values can be restricted so that a known mortality event removes enough individuals from the population within an event mortality process. CASAL2 requires penalty functions for processes that remove or shift a *number* of individuals between categories or from the partition. Many of the penalties that were available in CASAL have been moved to be additional priors in CASAL2(see Section 5.9).

For most penalties, a multiplier is required to be specified, and the objective function is increased by this multiplier multiplied by the penalty value. In some cases the multiplier may need to be quite large to prohibit some model behaviour.

Penalties are implemented for the processes

- @process[label].type=event_mortality,
- @process[label].type=mortality_instantaneous,
- @process[label].type=tag_by_length,
- @process[label].type=tag_by_length, and

- `@process[label].type=category_transition`

For these processes, two types of penalties can be defined: on the natural scale (the default) and on the log scale. Both of these types add a penalty value of the squared difference between the observed value (e.g., the actual number of individuals to be removed in an event mortality process or the actual number of individuals to shift in a category transition process), and the number that were moved (if less than or equal), multiplied by the penalty multiplier.

The natural scale penalty calculates the squared difference on a natural scale, and the log scale penalty calculates the squared difference of the logged values.

For example:

```
@process Mortality
type mortality_instantaneous
penalty CatchMustBeTaken

# define the penalty in an @penalty block
@penalty CatchMustBeTaken
type process
log_scale True
multiplier 10000
```

Penalties are added to the objective function in the following ways;

$$Penalty = (X_1 - X_2)^2 \quad (5.8)$$

or if `log_scale true`

$$Penalty = (\log(X_1) - \log(X_2))^2 \quad (5.9)$$

where, for example, X_1 is observed catch biomass and X_2 is the estimated catch biomass. Penalties are usually applied in situations when numbers or weight are known. Another example is for tagging, where the number of individuals that were tagged in a given year is known, so a penalty can be used to restrict the model to estimate reasonable values for the numbers of tagged individuals in that year.

5.9. Additional Priors

Additional priors can be thought of as the inverse of penalties (TODO please rephrase). For CASAL models, most of the legacy `@penalty` blocks have now been implemented as `@additional_prior` blocks. They restrict parameters in user-defined spaces (TODO please rephrase).

The types of additional priors available in CASAL2 are `vector_smoothing`, `vector_averaging`, `uniform_log`, `lognormal`, `element_difference`, and `Beta`:

- `vector_averaging`

This prior can be applied to a vector parameter. Sum of squares of r^{th} differences, optionally on a log scale. This encourages the vector to be like a polynomial of degree $(r - 1)$. A range of the vector to be "smoothed" can be specified (and if not, the smoother is applied to the entire vector). However, this restriction must be specified by an index of the vector and must be between 1 and the length of the vector, inclusive.

- `vector_smoothing`

This prior can be applied to a vector parameter. Square of $(\text{mean}(\text{vector})-k)$, or of $(\text{mean}(\log(\text{vector}))-l)$, or of $(\log(\text{mean}(\text{vector})/m))$. Restricts the vector to average arithmetically to k or m , or geometrically to $\exp(l)$. Typically used for YCS with $k=1$ or $m=1$ or $l=0$, to restrict the YCS to centre on 1. Optionally, indices can be chosen or excluded outside a given set of bounds.

- `lognormal` with mean μ and c.v. c

$$-\log(\pi(p)) = \log(p) + 0.5 \left(\frac{\log(p/\mu)}{s} + \frac{s}{2} \right)^2 \quad (5.10)$$

- `uniform_log`

$$-\log(\pi(p)) = \log(p) \quad (5.11)$$

- `element_difference`

$$-\log(\pi(p_1, p_2)) = \sum_{i=1}^n (p_{1,i} - p_{2,i})^2 \quad (5.12)$$

- `Beta`

Beta with mean μ and standard deviation σ , and range parameters A and B , for parameter value = p

$$-\log(\pi(p)) = (1-m)\log(p-A) + (1-n)\log(B-p) \quad (5.13)$$

where $v = \frac{\mu-A}{B-A}$, and $\tau = \frac{(\mu-A)(B-\mu)}{\sigma^2} - 1$ and then $m = \tau v$ and $n = \tau(1-v)$. The beta prior is undefined when $\tau \leq 0$.

Methods available for the type `vector_average` are `l`, `k`, `m`. For a target vector parameter \mathbf{X} and target mean k , the contribution to the objective score is

- `method k`

$$-\log(\pi(p)) = (\bar{X} - k)^2$$

- `method l`

$$-\log(\pi(p)) = \left(\overline{\ln(X)} - k \right)^2$$

- `method m`

$$-\log(\pi(p)) = (\ln(\bar{X}) - k)^2$$

where $\overline{\ln(X)}$ is the mean of the logged values.

There are a range of parameters and derived values that additional priors can be applied to. Here are a list of non-estimated (all parameters that can be estimated can have an additional prior attached to them) parameters that additional priors can be applied to.

- `selectivity[Selectivity_label].values{i:j}.`

This subcommand applies a selectivity (???) to the actual selectivity value by age (for ages i through j). This option is available only for certain types of selectivities (`all_values`, `all_values_bounded`, `double_exponential`). See the Hoki stock assessment for an example of applying additional priors on selectivities.

- `catchability[Catchability_label].q`

This subcommand is for catchabilities that are of type nuisance only. Since nuisance qs are not free parameters, additional priors can be applied to replicate CASAL models with `@estimate` blocks in nuisance qs . If a CASAL model applied a uniform prior, then this has a null effect and this functionality can be ignored when converting to a CASAL2 model.

This list may be useful for users who are trying to apply the equivalent CASAL penalties in a CASAL2 model.

5.10. Parameter Transformations

CASAL2 has multiple methods to transform a parameter, with some methods developed for legacy purposes. Transformations are implemented to try and achieve 'better' model optimisation. Complex population models can have highly correlated parameters so transforming them to be orthogonal or to be in a different space is a way of addressing correlations, and to allow the minimiser to find a 'global' minimum quicker. To read more about transformations and get a better understanding of why they are used, see [Gilks et al. \(1995\)](#), specifically chapter 6.

There are two main transformation methods available in CASAL2, `transform_with_jacobian` and `prior_applies_to_transform`. When using `transform_with_jacobian`, priors are defined on parameters in natural/model space (the usual priors) but when the parameter is passed to the minimiser it gets transformed and a Jacobian is added to the objective function to account for this transformation. The second method is when bounds and prior parameters on the parameters can be specified in transformed space. Note that both `prior_applies_to_transform` and `transform_with_jacobian` cannot be set to true.

There are two ways that transformations can be applied. The first is within the `@estimate` block, which is for univariate (simple) transformations only. For more complex transformations a `@estimate_transformation` block must be specified to describe the transformation.

For example:

```
## simple transformation
@estimate log_R0
type lognormal
transformation log
parameter process[Recruitment].r0
transform_with_jacobian true
mu 442413
cv 0.2
lower_bound 3000
upper_bound 24154953

## more complex transformation
@estimate R0
type lognormal
```

```

parameter process[Recruitment].r0
mu 442413
cv 0.2
lower_bound 3000
upper_bound 24154953

@estimate_transformation Log_R0
type log
estimate_label log_R0
transform_with_jacobian true

```

Transform with Jacobian

The support of a random variable X with density $p_X(x)$ is that subset of values for which it has non-zero density,

$$\text{supp}(X) = \{x | p_X(x) > 0\} \quad (5.14)$$

If f is a transformation function defined on the support of X , then $Y = f(X)$ is a new random variable (transformed variable).

This section shows the available transformations in CASAL2 and the probability density function of Y .

Suppose X is one dimensional and $f: \text{supp}(X) \rightarrow \mathbf{R}$ is a one-to-one, monotonic function with a differentiable inverse f^{-1} . Then the density of Y is

$$p_Y(y) = p_X(f^{-1}(y)) \left| \frac{\partial}{\partial y} f^{-1}(y) \right| \quad (5.15)$$

where $\left| \frac{\partial}{\partial y} f^{-1}(y) \right|$ is the Jacobian term. The Jacobian measures how the scale of the transformed variable changes with respect to the underlying variable. This can be expanded to the multivariate case where the Jacobian becomes a matrix of partial derivatives.

In equation 5.15 the term $p_X(f^{-1}(y)) = p_X(X)$ and in a Bayesian context is the prior of the untransformed variable/parameter. **Note:** if this functionality is in use be careful interpreting the covariance matrix as this will be related to the transformed variable not the variable space, e.g., if natural mortality (M) is estimated as $Y = M/2$, then the covariance matrix will be described for Y .

```

@estimate log_R0
type lognormal
transformation log
parameter process[Recruitment].r0
transform_with_jacobian true
mu 442413
cv 0.2
lower_bound 3000
upper_bound 24154953

```


Transform without Jacobian but prior defined in transformed space

This transformation is where the priors are defined in transformed space. This class of transformations contains functionality that was implemented in the CASAL.

If $f()$ is a transformation function defined on the support of X , then $Y = f(X)$ is a new random variable (transformed variable). In this class *a priori* information is specified with regard to $p_Y(y)$ and X can be thought of as a derived quantity.

For example:

```
@estimate log_R0
type lognormal
parameter process[Recruitment].r0
prior_applies_to_transform true
mu 13
cv 0.5
lower_bound 8
upper_bound 17
```

Transformation types

- **log : natural logarithm transformation**

```
is_simple = true
jacobian defined = true
 $Y = \ln(X)$ 
 $\left| \frac{\partial}{\partial y} f^{-1}(y) \right| = X^{-1}$ 
```

- **inverse**

```
is_simple = true
jacobian defined = true
 $Y = X^{-1}$ 
 $\left| \frac{\partial}{\partial y} f^{-1}(y) \right| = -X^{-2}$ 
```

- **sqrt : square root transformation**

```
is_simple = true
jacobian defined = true
 $Y = \sqrt{X}$ 
 $\left| \frac{\partial}{\partial y} f^{-1}(y) \right| = -X^{-1.5}$ 
```

- **average_difference : two parameters θ_1 and θ_2 are transformed to Y_1 and Y_2 , where Y_1 is the average of the original parameters and Y_2 is the difference between the mean and each parameter.**

```
is_simple = false
jacobian defined = false
 $Y_1 = \frac{\theta_1 + \theta_2}{2}$ 
 $Y_2 = (Y_1 - \theta_2)2$ 
```

Restore transformations

$$\theta_1 = Y_1 + 0.5Y_2$$

$$\theta_2 = \theta_1 - 0.5Y_2$$

$$\left| \frac{\partial}{\partial y} f^{-1}(y) \right| \text{ Hasn't been assessed (i.e it could exist) (TODO ?????)}$$

- `log_sum` : two parameters θ_1 and θ_2 are transformed to Y_1 and Y_2 , where Y_1 is the natural logarithm of the sum of θ_1 and θ_2 . Y_2 describes the proportion of the sum with respect to θ_1

`is_simple = false`

`jacobian defined = false`

$$Y_1 = \ln(\theta_1 + \theta_2)$$

$$Y_2 = \theta_1 / (\theta_1 + \theta_2)$$

Restore transformations

$$\theta_1 = \exp(Y_1)Y_2$$

$$\theta_2 = \exp(Y_1)(1 - Y_2)$$

$$\left| \frac{\partial}{\partial y} f^{-1}(y) \right| \text{ Hasn't been assessed (i.e it could exist) (TODO ?????)}$$

- `orthogonal` : two parameters θ_1 and θ_2 are transformed to Y_1 and Y_2 , where Y_1 is the multiplication of θ_1 and θ_2 . Y_2 is the division of θ_1 and θ_2

`is_simple = false`

`jacobian defined = true`

$$Y_1 = \theta_1 \theta_2$$

$$Y_2 = \theta_1 / \theta_2$$

Restore transformations

$$\theta_1 = \sqrt{Y_1 Y_2}$$

$$\theta_2 = \sqrt{Y_1 / Y_2}$$

$$\left| \frac{\partial}{\partial y} f^{-1}(y) \right| = 2Y_2$$

- `SumToOne` : given two parameters θ_1 and θ_2 that have the constraint $\sum_{i=1}^2 \theta_i$, estimate θ_1 only

given $\theta_2 = 1 - \theta_1$

`is_simple = false`

`jacobian defined = false`

6. The observation section

6.1. Observations

The objective function calculates the goodness-of-fit of the model to the observation data. Observations are typically supplied at an instance in time, over a group of aggregated categories. Most observations are sampled over time, i.e., data which were recorded for one or more years, in the same format each year. Examples of time series data types include relative abundance indices, commercial catch length frequencies, and survey numbers-at-age.

Definitions for each type of observation are described below, including how the observed values should be formatted, how CASAL2 calculates the expected values, and the likelihoods that are available for each type of observation.

There are two main types of observations available in CASAL2. The first type is observations that are associated with a **mortality block**. The second type is observations that are associated with a specific process. These observations use the `type` subcommand.

If an observation begins with `process` it is an observation that is associated with a process. If an observation does **not** begin with `process` it is associated with the mortality block of the defined time step. For example, the observation type `process_abundance` is a process-based observation, whereas `process_abundance abundance` is an observation that is associated with a mortality block.

There are two types of process observations. **Specific process observations** are observations that are associated with a specific process (e.g., `process_proportions_migrating`), and **general process observations** are observations that can be associated with any process (e.g., `process_proportions_at_age`). The observation types are described in different sections.

6.1.1. Mortality block associated observations

All observations within this class are calculated similarly. That is, the expected values are calculated at the beginning of the mortality block and at the end of the mortality block. CASAL2 then uses a linear interpolation to approximate the expected values part way through a mortality block using the subcommand `time_step_proportion`. This feature could be useful if a survey occurs part way through an exploitation phase, which may be part way through a fishing season when modelling a fish population. Each observation in this class will evaluate different expectations of the partition (explained in the following descriptions).

The observation types available with this class of observations are:

- `abundance`
- `biomass`
- `proportions_at_age`
- `proportions_at_length`
- `proportions_by_category`
- `tag_recapture_by_length`
- `tag_recapture_by_age`

Abundance or biomass observations

Abundance (or biomass) observations are observations of either a relative or absolute number (or biomass) of individuals from a set of categories after applying a selectivity. The observation classes are the same, except that a biomass observation will use the biomass as the observed (and expected) value (calculated from mean weight of individuals within each age and category) while an abundance observation is the number of individuals.

Each observation is for a given year and time-step, for some selected age classes of the population (for a range of ages multiplied by a selectivity), for aggregated categories. Furthermore, the label of the catchability coefficient q is required; q can either be estimated or fixed. For absolute abundance or absolute biomass observations, define a catchability where $q = 1$.

The observations can be supplied for any set of categories. For example, for a model with the two categories *male* and *female*, an observation of the total abundance/biomass (male + female) or male-only abundance/biomass could be provided. The subcommand `categories` defines the categories used to aggregate the abundance/biomass. In addition, each category must have an associated selectivity, defined by `selectivities`.

For example,

```
categories male
selectivities male-selectivity
```

defines an observation for males after applying the selectivity `male-selectivity`. CASAL2 then requires that an observation is supplied. The expected values for the observations will be the expected abundance (or biomass) of males, after applying the selectivities, at the year and time-step specified.

CASAL2 calculates the expected values by summing over the defined ages (via the age range and selectivity) and categories at both the beginning and end of a mortality block. CASAL2 will approximate the expectation part way through the mortality block using the `time_step_proportion`. The default `time_step_proportion` value is 0.5. CASAL2 does linear interpolation between the start and end abundance (or biomass) from the mortality block.

For an abundance observation the expected value is

$$E_{i,1} = \sum_{c=1}^A \sum_{a=1}^A S_{a,c} N_{a,c,i,1} \quad (6.1)$$

$$E_{i,2} = \sum_{c=1}^A \sum_{a=1}^A S_a N_{a,c,i,2} \quad (6.2)$$

Where $E_{i,1}$ is the expectation at the beginning of time step and $E_{i,2}$ is the expectation at the end of the time-step. S_a is the selectivity for age a and category c . If there is no mortality related to this observation then E_i which is used in the likelihood contribution is $E_{i,1}$. If this was a biomass observation, then $N_{a,c,i,1}$ in Equations (6.1) and (6.2) is replaced with $N_{a,c,i,1} \bar{w}_{a,c}$, where $\bar{w}_{a,c}$ is the mean weight of category c at age a . If the user wishes to apply 100% mortality then $E_i = E_{i,2}$.

For applying quantities of mortality between these values (M_i), the linear interpolation is

$$E_i = |E_{i,1} - E_{i,2}| M_i \quad (6.3)$$

```
@observation MyAbundance
type abundance
years 1999
...
categories male
obs 1000
...
```

Or, for an observation aggregated over multiple categories,

```
@observation MyAbundance
type abundance
years 1990 1991
...
categories male+female
table obs
1990 1000
1991 1200
end_table
...
```

To define a biomass observation instead of an abundance observation, use

```
@observation MyBiomass
type biomass
...
```

Proportions-at-age

Proportions-at-age observations are observations of the relative number of individuals at age, via some selectivity.

The observation is supplied for a given year and time-step, for some selected age classes of the population (i.e., for a range of ages multiplied by a selectivity), for categories aggregated over a set of spatial cells. Note that the categories defined in the observations must have an associated selectivity, defined by `selectivities`.

The age range must be ages defined in the partition (i.e., between `@model.min_age` and `@model.max_age` inclusive); the upper end of the age range can optionally be a plus group, which must be either the same as or less than the plus group defined for the partition.

Proportions-at-age observations can be supplied as

- a set of proportions for a single category,
- a set of proportions for multiple categories, or
- a set of proportions across aggregated categories.

The method of evaluating expectations are the same for all three types of proportions. The definitions of these proportions and the expected dimensions of observation and error inputs that CASAL2 expects for each respective proportion type are described below with examples.

Like all types of observations that are associated with the mortality block, CASAL2 will evaluate the numbers at age before and after the mortality block for the specified time step of the observation,

and applying the user-defined selectivity. CASAL2 then generates the expectations from the partition part way through the mortality block using the subcommand `time_step_proportion`. This approximation is a linear interpolation of the numbers-at-age over the mortality block.

The ageing error is then applied, if the user has specified it. Finally, CASAL2 converts the numbers-at-age to proportions-at-age by dividing all numbers in an age bin by the total numbers. The likelihood for the proportions-at-age observation is then calculated.

Defining an observation for a single category is used to model a set of proportions of a single category by age class. For example, to specify that the observations are of the proportions of male within each age class, then the subcommand `categories` for the `@observation[label].type=proportion_by_age` command is

```
categories male
```

CASAL2 then requires that there will be a single vector of proportions supplied, with one proportion for each age class within the defined age range, and that these proportions sum to one.

For example, if the age range was 3 to 10, then 8 proportions should be supplied, one proportion for each of the the ages 3, 4, 5, 6, 7, 8, 9, and 10. The expected values will be the expected proportions of males within each of these age classes (after omitting males aged less than 3 and older than 10), after applying a selectivity at the year and time-step specified. The supplied vector of proportions (i.e., in this example, the 8 proportions) must sum to one, which is evaluated with a default tolerance of 0.001.

```
@observation MyProportions
type proportions_at_age
...
categories male
min_age 3
max_age 9
years 1990
table obs
1990 0.01 0.09 0.20 0.20 0.35 0.10 0.05
end_table
...
```

Defining an observation for multiple categories extends the single category observation definition. It is used to model a set of proportions over several categories by age class. For example, to specify that the observations are of the proportions of male or females within each age class, then the subcommand `categories` for the `@observation[label].type=proportion_by_age` command is

```
categories male female
```

CASAL2 then requires that there will be a single vector of proportions supplied, with one proportion for each category and age class combination, and that these proportions sum to one across all ages and categories.

For example, if there were two categories and the age range was 3 to 10, then 16 proportions should be supplied (one proportion for each of the the ages 3, 4, 5, 6, 7, 8, 9, and 10, for each category male and female). The expected values will be the expected proportions of males and females within each of these age classes (after omitting those aged less than 3 and older than 10), after applying

a selectivity at the year and time-step specified. The supplied vector of proportions (i.e., in this example, the 16 proportions) must sum to one, which is evaluated with a default tolerance of 0.001.

For example,

```
@observation MyProportions
type proportions_at_age
...
categories male female
min_age 1
max_age 5
years 1990 1991
table obs
1990 0.01 0.05 0.10 0.20 0.20 0.01 0.05 0.15 0.20 0.03
1991 0.02 0.06 0.10 0.21 0.18 0.02 0.03 0.17 0.20 0.01
end_table
...
```

Defining an observation across aggregated categories allows categories to be aggregated before the proportions are calculated. It is used to model a set of proportions from several categories that have been combined by age class. To indicate that two (or more) categories are to be aggregated, separate them with a '+' symbol. For example, to specify that the observations are of the proportions of male and females combined within each age class, then the subcommand `categories` for the `@observation[label].type=proportion_by_age` command is

```
categories male + female
```

CASAL2 then requires that there will be a single vector of proportions supplied, with one proportion for each age class, and that these proportions sum to one.

For example, if there were two categories and the age range was 3 to 10, then 8 proportions should be supplied (one proportion for each of the the ages 3, 4, 5, 6, 7, 8, 9, and 10, for the sum of males and females within each age class). The expected values will be the expected proportions of males + females within each of these age classes (after omitting those aged less than 3 and older than 10), after applying a selectivity at the year and time-step specified. The supplied vector of proportions (i.e., in this example, the 8 proportions) must sum to one, which is evaluated with a default tolerance of 0.001.

For example,

```
@observation MyProportions
type proportions_at_age
...
years 1990 1991
categories male+female
min_age 1
max_age 5
table obs
1990 0.02 0.13 0.25 0.30 0.30
1991 0.02 0.06 0.18 0.35 0.39
end_table
...
```

The latter form can then be extended to include multiple categories, or multiple aggregated categories. For example, to describe proportions for the three groups: immature males, mature

males, and all females (immature and mature females added together) for ages 1 through 4, a total of 12 proportions are required

```
@observation MyProportions
type proportions_at_age
...
categories male_immature male_mature female_immature+female_mature
min_age 1
max_age 4
years 1990
table obs
year 1990 0.05 0.15 0.15 0.05 0.02 0.03 0.08 0.04 0.05 0.15 0.15 0.08
end_table
...
```

Proportions-at-length

Functionality for defining combinations of categories and aggregated categories directly translates from proportions-at-age to proportions-at-length. The difference is the observation is over length bins instead of age classes. CASAL2 calculates the expected numbers-at-length by converting the numbers-at-age to numbers-at-length by using the age-length relationship and distribution specified for the category specified in the @age_length block.

Instead of supplying a minimum and maximum age, the user must supply a vector of length bins. If no length bins are specified, then the observation-specific length bins use the model length bins as the default. If observation-specific length bins are specified, they must be a sequential subset of the model length bins, with no missing or added values. For example, if the model length bins are 0 5 10 15 20 25 ... 100, then the observation-specific length bins can be 20 25 30 35 40 45 50 but not 20 30 40 50.

If there is no plus group, i.e., length_plus=false, then CASAL2 requires a vector of proportions for each year of length $n - 1$, where n is the number of lengths supplied. If length_plus=true then CASAL2 expects a vector of proportions for each year of length n . The last proportion represents the numbers from the last length bin to the maximum length the age-length relationship allows.

```
@observation Observed_Length_frequency_ChathamRise
type process_removals_by_length
years 1991 1992
likelihood multinomial
time_step Summer
fishery EastChathamRise
process instant_mort
categories male
length_plus false
length_bins 0 20 40 60 80 110
table obs
1991 0.2 0.25 0.15 0.2 0.2
1992 0.12 0.25 0.28 0.25 0.1
end_table
table error_values
1991 25
1992 37
end_table
```


Proportions-by-category observations

TODO 'between categories' or 'within categories'?

Proportions-by-category observations are observations of either the relative number of individuals between categories within age classes, or relative biomass between categories within age classes.

The observation is supplied for a given year and time-step, for selected age classes of the population (i.e., for a range of ages multiplied by a selectivity).

The age range must be ages defined in the partition (i.e., between `@model.min_age` and `@model.max_age` inclusive); the upper end of the age range can optionally be a plus group, which may or may not be the same as the plus group defined for the partition.

Proportions-by-category observations can be supplied for any set of categories as a proportion of themselves and any set of additional categories. For example, for a model with the two categories *male* and *female*, observations of the proportions of males in the population at each age class might be provided. The subcommand `categories` defines the categories for the numerator in the calculation of the proportion, and the subcommand `categories2` supplies the additional categories to be used in the denominator of the calculation. In addition, each category must have an associated selectivity, defined by `selectivities` for the numerator categories and `selectivities2` for the additional categories used in the denominator.

For example,

```
categories male
categories2 female
selectivities male-selectivity
selectivities2 female-selectivity
```

defines the proportion of males in each age class as a proportion of males + females. CASAL2 then requires that there will be a vector of proportions supplied, with one proportion for each age class within the defined age range, i.e., if the age range was 3 to 10, then 8 proportions should be supplied (one proportion for each of the ages 3, 4, 5, 6, 7, 8, 9, and 10). The expected values will be the expected ratios of male to male + female within each of these age classes, after applying the selectivities at the year and time-step specified.

The observations must be supplied using all or some of the values defined by a categorical layer. CASAL2 calculates the expected values by summing over the ages (via the age range and selectivity) and categories for those spatial cells where the categorical layer has the same value as defined for each vector of observations.

For example,

```
@observation MyProportions
type proportions_by_category
years 1990 1991
...
categories male
categories2 female
min_age 1
max_age 5
table obs
1990 0.01 0.05 0.10 0.20 0.20
1991 0.02 0.06 0.10 0.21 0.18
end_table
...
```

Tag Recapture by length

Tag data is primarily used to estimate the population abundance of fish. In some models, this estimation can only be made outside the model and the result is used as an estimate of abundance in the model. But in CASAL2 the tagging data can, alternatively, be fitted within the model.

Before adding a tag-recapture time series, a tag-release process (Section 4.5.5) needs to be defined. Tagging events list the labels of the tags which are modelled, and define the events where fish are tagged (i.e., CASAL2 moves fish into the section of the partition corresponding to a specific tag).

The observations are divided into two parts: (i) the number of fish that were scanned, and (ii) the number of tags that were recaptured. Each number can be specified by categories, or for combinations of categories. The precise content of the scanned and recaptured observations depends on the sampling method.

The available options are:

- age: both the scanned and recaptured are vectors containing numbers-at-age. Only available in an age-based model. The selectivity ogive is redundant and cannot be supplied.
- size: both the scanned and recaptured are vectors containing numbers-at-size. Can be used in either an age- or size-based model. The selectivity ogive is redundant and cannot be supplied.

When defining the tag-recapture time series, the following are also required:

- the time step,
- the years (unlike a tag-release process, the tag-recapture observations can occur over several years),
- the probability that each scanned tagged fish is detected as tagged (may be less than 1 if the observers are not infallible). The expected number of tags detected is calculated by multiplying this number by the number of tagged fish in the sample,
- the tagged category or categories (Make up the recaptures),
- the categories scanned (All the fish sampled for tags),
- A selectivity used in the recapture process,
- the size classes if the observations are size-based in an age-based model.

An example of a tag recapture observation:

```
## For the following partition
@categories
format sex.area.tag
names    male.Areal.2011,notag female.Areal.2011,notag

@observation Tag_2011_Areal_recap_2012 ## individuals tagged in 2011 and recaptured in 2012
## in Areal
type tag_recapture_by_length
categories format=*.Areal.*+ ## scanned categories in Areal
tagged_categories *.Areal.2011+ ## male and female tagged categories
detection 0.85 ## detection probability
likelihood binomial ## likelihood choice
selectivities One ## label of selectivity for tagged
tagged_selectivities One ## label of selectivity for scanned
years 2012 ## years to apply observation
```

```

time_step step2 ## time_step to apply observation
time_step_proportion 0.5 ## proportion of mortality applied before observation is calculated

table scanned
2012 281271 41360 30239 12234
end_table

table recaptured
2012 15 20 12 2
end_table

delta 1e-11 ## robustification value
dispersion 6.3 ## dispersion factor

```

The observed ($O_{y,l}$) and expected ($E_{y,l}$) values in year y and length l of this observation are:

$$O_{y,l} = \frac{R_{y,l}}{S_{y,l}} \quad (6.4)$$

where $R_{y,l}$ is the number of recaptures in year y at length l and $S_{y,l}$ are the scanned values.

$$E_{y,l} = d \frac{\tilde{N}_{y,l,t} + (\tilde{N}_{y,l,t+1} - \tilde{N}_{y,l,t}) \times p}{N_{y,l,t} + (N_{y,l,t+1} - N_{y,l,t}) \times p} \quad (6.5)$$

where $\tilde{N}_{y,l,t}$ is an element in the tagged categories at the beginning of time step t and $\tilde{N}_{y,l,t+1}$ is an element in the tagged categories at the end of time step t , $N_{y,l,t}$ is the sum of the categories that were vulnerable to sampling when the observation occurred, p is the proportion of the time step that the observation was taken, and d is the detection probability.

For observations with multiple tagged categories and multiple categories that were vulnerable to sampling:

$$\tilde{N}_{y,l,t} = \sum_{j=1}^J N_{y,l,t,j} \quad (6.6)$$

where $j = \{1, 2, 3, \dots, J\}$ are all the tagged categories, the same method is applied to the vulnerable categories to calculate $N_{y,l,t}$. The tagged categories should be defined in the vulnerable categories. In an extreme case where every individual in the population is tagged, this result would be divided by zero. So, to constrain the expectation to be between 0 and 1, the numerator must be in the denominator.

The tag-recapture likelihood (binomial) is specified below. It is a modified version of the more general binomial. Note that this likelihood does not have any user-set precision parameters such as N or $c.v.$, although there are user-specified robustification and dispersion parameters available. The factorials are calculated using the log-gamma function, to allow for non-integer arguments where necessary (and to avoid overflow errors).

6.1.2. General process observations

A list of `types` that are associated with this set of observations:

- process_abundance
- process_biomass
- process_proportions_at_age
- process_proportions_at_length
- process_proportions_by_category

These observations have the same expectations as the mortality block versions described in Section 4.4.2. With the exception that instead of wrapping a mortality block they can wrap any process type available in CASAL2.

6.1.3. Specific process observations

A list of types that are associated with this set of observations are:

- process_removals_by_age
- process_removals_by_age_retained
- process_removals_by_age_retained_total
- process_removals_by_length
- process_removals_by_length_retained
- process_removals_by_length_retained_total
- process_proportions_migrating

Process removals by age

Removals-at-age observations are observations of the relative number of individuals at age, part way through a process of type `mortality_instantaneous`. This observation is exclusively associated with the process of type `mortality_instantaneous`, and will produce an error if it is associated with any other process type.

The observation is supplied for a given year and time-step, for selected age classes of the population (i.e., for a range of ages multiplied by a selectivity that is associated with the process).

The age range must be ages defined in the partition (i.e., between `@model.min_age` and `@model.max_age` inclusive); the upper end of the age range can optionally be a plus group, which must be either the same or less than the plus group defined for the partition.

The expectations from this observation are generated whilst the process is being executed. The expectation of numbers at age a for category c from exploitation method m ($E[N_{a,c,m}]$) are

$$E[N_{a,c,m}] = N_{a,c} U_{a,m} S_{a,c,m} 0.5 M_{a,c} \quad (6.7)$$

where $N_{a,c}$ are the numbers-at-age in category c before the process is executed, $U_{a,m}$ is the exploitation rate for age a from method m , $S_{a,c,m}$ is the selectivity, and M is the natural mortality.

The observation class accesses the variable $E[N_{a,c,m}]$ and applies ageing error if the user has specified it. Then the observations are aggregated by method and category depending on how the user specifies the observation, before converting numbers-at-age to proportions-at-age and then calculating the likelihood.

Likelihoods that are available for this observation class are the multinomial, Dirichlet, and the lognormal. See Section 6.2 for information on the respected likelihood.

Process removals by age retained

Observations of retained and total catches by age can be included, using the labels `process_removals_by_age_retained` and `process_removals_by_age_retained_total`, respectively. Examples of two such observations are given below, with the associated process `Instantaneous_Mortality_Retained` having the form of the example in Section 4.5.3.4.

For retained catch:

```
@observation potFishAFtotal #test syntax get catch AF out
type process_removals_by_age_retained_total
mortality_instantaneous_process Instantaneous_Mortality_Retained
method_of_removal FishingPot
years 2005
time_step 1
categories male
### ageing_error Normal_ageing
min_age 3
max_age 15
plus_group True
table obs
2005 0.0002814574 0.0095351205 0.1661896098 0.2701718827 0.2214454177 0.1661869474 0.1107930285 0.
end_table
table error_values
2005 651
end_table
likelihood multinomial
delta 1e-11
```

For total catch:

```
@observation potFishAFretained #test syntax --> fits to discards not catch
type process_removals_by_age_retained
mortality_instantaneous_process Instantaneous_Mortality_Retained
method_of_removal FishingPot
years 2005
time_step 1
categories male
# ageing_error Normal_ageing
min_age 3
max_age 15
plus_group True
table obs
2005 1.650990e-10 7.566419e-07 1.771126e-03 1.962050e-01 3.192775e-01 2.413644e-01 1.609208e-01 8.
end_table
table error_values
```

```

2005 651
end_table
likelihood multinomial
delta 1e-11

```

Process removals by length

Removals by length observations are observations of the relative number of individuals at length, part way through a process of type `mortality_instantaneous`. This observation is exclusively associated with the process of type `mortality_instantaneous`, and will produce an error if associated with any other process type.

The observation is supplied for a given year and time-step, for some selected age classes of the population (i.e., for a range of ages multiplied by a selectivity that is associated with the process).

The expectations from this observation are generated whilst the process is being executed. The expectation of numbers at age a for category c from exploitation method m ($E[N_{a,c,m}]$) are

$$E[N_{a,c,m}] = N_{a,c} U_{a,m} S_{a,c,m} 0.5 M_{a,c} \quad (6.8)$$

where $N_{a,c}$ are the numbers at age in category c before the process is executed, $U_{a,m}$ is the exploitation rate for age a from method m , $S_{a,c,m}$ is the selectivity, and M is the natural mortality.

The observation class accesses the variable $E[N_{a,c,m}]$ from the process and applies the age-length relationship specified in the model. This converts numbers-at-age to numbers-at-age and -length, which are then converted to numbers-at-length. The observations are aggregated by method and category depending on how the user specifies the observation, before converting numbers-at-age to proportions and calculating the likelihood.

Similar to the proportions-at-length observation type, the user must supply a vector of length bins. The observation-specific length bins must be a sequential subset of the model length bins, with no missing or added values. For example, if the model length bins are 0 5 10 15 20 25 ... 100, then the observation-specific length bins can be 20 25 30 35 40 45 50 but not 20 30 40 50.

```

@observation observation_fishery_LF
type process_removals_by_length
...
years 1993 1994 1995
method_of_removal FishingEast
mortality_instantaneous_process instant_mort
length_plus false
length_bins 0 20 40 60 80 110
delta 1e-5
table obs
1993    0.0    0.05    0.05    0.10    0.80
1994    0.05   0.1     0.05    0.05    0.75
1995    0.3    0.4     0.2     0.05    0.05
end_table

table error_values

```

```

1993 31
1994 34
1995 22
end_table

```

Likelihoods that are available for this observation are the multinomial, Dirichlet and the lognormal. See Section 6.2 for information on the likelihoods.

Process removals by length retained

Observations of retained and total catches by length can be included, using the labels `process_removals_by_length_retained` and `process_removals_by_length_retained_total` respectively. Examples of two such observations are given below, with the associated process `Instantaneous_Mortality_Retained` having the form of the example in Section 4.5.3.4.

Similar to the proportions-at-length observation type, the user must supply a vector of length bins. The observation-specific length bins must be a sequential subset of the model length bins, with no missing or added values. For example, if the model length bins are 0 5 10 15 20 25 ... 100, then the observation-specific length bins can be 20 25 30 35 40 45 50 but not 20 30 40 50.

For retained catch:

```

@observation potFishLFtotal #test syntax get catch LF out
type process_removals_by_length_retained_total
mortality_instantaneous_process Instantaneous_Mortality_Retained
method_of_removal FishingPot
years 2005
time_step 1
categories male
length_bins 30 31 32 33 34 35 36 37 38 39 40 41 42 43 44 45 46 # for LF in catch
length_plus False
table obs
2005 0.05344612 0.06432242 0.07357780 0.08050385 0.08473451 0.08619620 0.08502982 0.08152921 0.076
end_table
table error_values
2005 651
end_table
likelihood multinomial
delta 1e-11

```

For total catch:

```

@observation potFishLFretained #test syntax get retained LF out
type process_removals_by_length_retained
mortality_instantaneous_process Instantaneous_Mortality_Retained
method_of_removal FishingPot
years 2005
time_step 1
categories male
length_bins 30 31 32 33 34 35 36 37 38 39 40 41 42 43 44 45 46 # for LF in catch
length_plus False
table obs
2005 0.02462879 0.03536036 0.04759163 0.06025858 0.07205340 0.08169356 0.08817806 0.09095124 0.089

```

```
end_table
table error_values
2005 651
end_table
likelihood multinomial
delta 1e-11
```

Proportions migrating

This observation is of the proportion migrating from one area to another. This observation is exclusively associated with the process type `transition_category`, and will produce an error when associated with any other process type. This observation is used to inform migration rates in migration processes. This observation class is used in the Hoki stock assessment see [Francis et al. \(2003\)](#) for more information on how these observations are collected and a situation that uses it.

This observation calculates an expectation E_a of proportions for each age class a that have migrated, by

$$E_a = \frac{N_a - N'_a}{N_a} \quad (6.9)$$

where N_a are the numbers of individuals in age a before the migration process occurs, and N'_a are the number of individuals after the migration process occurs.

The likelihoods that are allowed for this observation are the lognormal, multinomial, and Dirichlet.

A section of the Hoki stock assessment model:

```
@observation pspawn_1993
type process_proportions_migrating
years 1993
time_step step4
process Wspmg ## migration process that the observation is associated with
age_plus true
min_age 4
max_age 9
likelihood lognormal
categories male.west+female.west ## Categories to evaluate the prportion for
ageing_error Normal_offset ## label for an @ageing_error block
table obs
#age    4    5    6    7    8    9
1993 0.64 0.58 0.65 0.66 0.71 0.60
end_table

table error_values
## if lognormal these are c.v.'s
1993 0.25
end_table
```


6.2. Likelihoods

6.2.1. Likelihoods for proportions-at-age observations

CASAL2 implements three likelihoods for proportions-at-age observations, the multinomial likelihood, the Dirichlet, and the lognormal likelihood.

The multinomial likelihood

For the observed proportions at age O_i for age classes i , with sample size N , and the expected proportions at the same age classes E_i , the negative log-likelihood is:

$$-\log(L) = -\log(N!) + \sum_i \log((NO_i)!) - NO_i \log(Z(E_i, \delta)) \quad (6.10)$$

where $\sum_i O_i = 1$ and $\sum_i E_i = 1$. $Z(\theta, \delta)$ is a robustifying function to prevent division by zero errors, with parameter $\delta > 0$.

$$Z(\theta, \delta) = \begin{cases} \theta, & \text{where } \theta \geq r \\ \delta / (2 - \theta / \delta), & \text{otherwise} \end{cases} \quad (6.11)$$

The default value of δ is 1×10^{-11} .

The Dirichlet likelihood

For the observed proportions at age O_i for age classes i , with sample size N , and the expected proportions at the same age classes E_i , the negative log-likelihood is:

$$-\log(L) = -\log(\Gamma \sum_i (\alpha_i)) + \sum_i \log(\Gamma(\alpha_i)) - \sum_i (\alpha_i - 1) \log(Z(O_i, \delta)) \quad (6.12)$$

where $\alpha_i = Z(NE_i, \delta)$, $\sum_i O_i = 1$, and $\sum_i E_i = 1$. $Z(\theta, \delta)$ is a robustifying function to prevent division by zero errors, with parameter $\delta > 0$.

$$Z(\theta, \delta) = \begin{cases} \theta, & \text{where } \theta \geq r \\ \delta / (2 - \theta / \delta), & \text{otherwise} \end{cases} \quad (6.13)$$

The default value of δ is 1×10^{-11} .

The lognormal likelihood

For the observed proportions at age O_i for age classes i , with c.v. c_i , and the expected proportions at the same age classes E_i , the negative log-likelihood is defined as;

$$-\log(L) = \sum_i \left(\log(\sigma_i) + 0.5 \left(\frac{\log(O_i/Z(E_i, \delta))}{\sigma_i} + 0.5\sigma_i \right)^2 \right) \quad (6.14)$$

where

$$\sigma_i = \sqrt{\log(1 + c_i^2)} \quad (6.15)$$

and the c_i 's are the c.v.s for each age class i , and $Z(\theta, \delta)$ is a robustifying function to prevent division by zero errors, with parameter $\delta > 0$.

$$Z(\theta, \delta) = \begin{cases} \theta, & \text{where } \theta \geq r \\ \delta/(2 - \theta/\delta), & \text{otherwise} \end{cases} \quad (6.16)$$

The default value of δ is 1×10^{-11} .

6.2.2. Likelihoods for abundance and biomass observations

Abundance and biomass observations are expected as an annual time series in CASAL2, where they select the same categories over that time series. The parameters and inputs needed to use this observation class are: a observation O_i , c.v. c_i , catchability coefficient q , where i indexed the year. CASAL2 calculates an expectation E_i and scales it by q before comparing it to O_i . This means that the value chosen for q will determine whether the observation is relative ($q \neq 1$) or absolute $q = 1$. Before we describe each of the likelihoods we will discuss the methods available to handle qs :

- The qs can be treated as 'nuisance' parameters. For each set of values of the free parameters, the model uses the values of the qs which minimise the objective function. These optimal qs are calculated algebraically (see Section 6.4). If one of the qs falls outside the bounds specified by the user, it is set equal to the closest bound. This approach reduces the size of the parameter vector and hence should improve the performance of the estimation method. However, it is not correct when calculating a sample from the posterior in a Bayesian analysis (except asymptotically, see [Walters and Ludwig \(1994\)](#)) and we offer the following alternative;
- The qs can be treated as ordinary free parameters.

For both options, it is necessary to evaluate the contribution of O_i to the negative log likelihood for a given value of q . Each observation O_i varies about qE_i , which expresses the variability of O_i in terms of its c.v. c_i (or in one case, its standard deviation s_i). Here are the likelihoods, which are expressed on the objective-function scale of $-\log(L)$:

The lognormal likelihood

The negative log likelihood for the lognormal is

$$-\log(L) = \sum_i \left(\log(\sigma_i) + 0.5 \left(\frac{\log(O_i/qZ(E_i, \delta))}{\sigma_i} + 0.5\sigma_i \right)^2 \right) \quad (6.17)$$

where

$$\sigma_i = \sqrt{\log(1 + c_i^2)} \quad (6.18)$$

and $Z(\theta, \delta)$ is a robustifying function to prevent division by zero errors, with parameter $\delta > 0$.

$$Z(\theta, \delta) = \begin{cases} \theta, & \text{where } \theta \geq r \\ \delta/(2 - \theta/\delta), & \text{otherwise} \end{cases} \quad (6.19)$$

The default value of δ is 1×10^{-11} .

This formulation reflects the distributional assumptions that O_i has the lognormal distribution, that the mean of O_i is qE_i and the c.v. of O_i is c_i .

The normal likelihood

For observations O_i , c.v. c_i , and expected values qE_i , the negative log-likelihood is defined as;

$$-\log(L) = \sum_i \left(\log(c_i E_i) + 0.5 \left(\frac{O_i - E_i}{Z(c_i E_i, \delta)} \right)^2 \right) \quad (6.20)$$

and $Z(\theta, \delta)$ is a robustifying function to prevent division by zero errors, with parameter $\delta > 0$.

$$Z(\theta, \delta) = \begin{cases} \theta, & \text{where } \theta \geq r \\ \delta/(2 - \theta/\delta), & \text{otherwise} \end{cases} \quad (6.21)$$

The default value of δ is 1×10^{-11} .

This reflects the distributional assumptions that O_i has the normal distribution, that the mean of O_i is qE_i and the c.v. of O_i is c_i .

6.2.3. Likelihoods for tag recapture by age and length observations

The binomial likelihood

This likelihood is for situations where the size frequencies or age frequencies of the recaptured tagged fish and of the scanned fish are known. Available in both age or size based models.

The likelihood is defined as a binomial, but based on sizes, rather than ages

$$-\log(L)' = -\sum_i [\log(n_i!) - \log((n_i - m_i)!) - \log((m_i)!) + m_i \log\left(Z\left(\frac{M_i}{N_i}, \delta\right)\right) + (n_i - m_i) \log\left(Z\left(1 - \frac{M_i}{N_i}, \delta\right)\right)] \quad (6.22)$$

where

n_i = number of fish at size or age i that were scanned

m_i = number of fish at size or age i that were recaptured

N_i = number of fish at size or age i in the available population (tagged and untagged)

M_i = number of fish at size or age i in the available population that have the tag after a detection probability p_d has been applied, $M_i = M'_i p_d$, where M'_i is the expected available population that have the tag.

$Z(x, \delta)$ is a robustifying function with parameter $r > 0$ (to prevent division by zero errors).

$$Z(x, \delta) = \begin{cases} x & \text{where } x \geq \delta \\ \frac{\delta}{(2-x/\delta)} & \text{otherwise} \end{cases}$$

If a dispersion parameter (τ) is described in the observation then the final negative log likelihood $-\log(L)$ contribution is

$$-\log(L) = -\log(L)' / \tau$$

6.2.4. Likelihoods for proportions-by-category observations

CASAL2 implements two likelihoods for proportions-by-category observations, the binomial likelihood, and the normal approximation to the binomial (binomial-approx).

The binomial likelihood

For observed proportions O_i for age class i , where E_i are the expected proportions for age class i , and N_i is the effective sample size for age class i , then the negative log-likelihood is

$$-\log(L) = -\sum_i [\log(N_i!) - \log((N_i(1 - O_i))!) - \log((N_i O_i)!) + N_i O_i \log(Z(E_i, \delta)) + N_i(1 - O_i) \log(Z(1 - E_i, \delta))] \quad (6.23)$$

where $Z(\theta, \delta)$ is a robustifying function to prevent division by zero errors, with parameter $\delta > 0$.

$$Z(\theta, \delta) = \begin{cases} \theta, & \text{where } \theta \geq r \\ \delta / (2 - \theta / \delta), & \text{otherwise} \end{cases} \quad (6.24)$$

The default value of δ is 1×10^{-11} .

The normal approximation to the binomial likelihood

For observed proportions O_i for age class i , where E_i are the expected proportions for age class i , and N_i is the effective sample size for age class i , then the negative log-likelihood is defined as;

$$-\log(L) = \sum_i \log \left(\sqrt{Z(E_i, \delta) Z(1 - E_i, \delta) / N_i} \right) + \frac{1}{2} \left(\frac{O_i - E_i}{\sqrt{Z(E_i, \delta) Z(1 - E_i, \delta) / N_i}} \right)^2 \quad (6.25)$$

where $Z(\theta, \delta)$ is a robustifying function to prevent division by zero errors, with parameter $\delta > 0$.

$$Z(\theta, \delta) = \begin{cases} \theta, & \text{where } \theta \geq r \\ \delta / (2 - \theta / \delta), & \text{otherwise} \end{cases} \quad (6.26)$$

The default value of δ is 1×10^{-11} .

6.3. Process error

Additional 'process error' can be defined for any set of observations. Additional process error has the effect of increasing the observation error in the data, and hence of decreasing the relative weight given to the data in the fitting process.

For observations where the likelihood is parameterised by the c.v., the process error can be specified for a given set of observations as a c.v., in which case all the c.v.s c_i are changed to

$$c'_i = \sqrt{c_i^2 + c_{process_error}^2} \quad (6.27)$$

Note that $c_{process_error} \geq 0$, and that $c_{process_error} = 0$ is equivalent to no process error.

Similarly, if the likelihood is parameterised by the effective sample size N ,

$$N'_i = \frac{1}{1/N_i + 1/N_{process_error}} \quad (6.28)$$

Note that this requires that $N_{process_error} > 0$, but the special case of $N_{process_error} = 0$ is valid, and $N_{process_error} = 0$ represents no process error (i.e., defined to be equivalent to $N_{process_error} = \infty$).

For both the c.v. and N process errors, the process error has more effect on small errors than on large ones. Note that a large value for the N process error means a small process error.

6.4. Calculating nuisance q parameters

This section describes the theory used to calculate nuisance (analytical) catchability coefficients q s (see Section 6.2.2). From the user's point of view, the essence is that you can use nuisance q s in the following situations:

- With maximum likelihood estimation

- With Bayesian estimation, providing that the additional prior on q is one of the following:
 - None (default)
 - Uniform-log
 - Lognormal with observations distributed lognormal, robustified lognormal

The scenarios in which the nuisance catchability q can be used in a Bayesian analysis (Table 6.1):

Table 6.1: Equations used to calculate nuisance qs . (*=no analytic solution found.)

Distribution of observations	Maximum Likelihood	None	Uniform-log	Normal	lognormal
Normal	(6.29)	(6.29)	(6.31)	*	*
Lognormal	(6.32)	(6.32)	(6.36)	*	(6.37)

Note that qs are calculated for robustified lognormal likelihoods as if they were ordinary lognormal likelihoods.

Let $\sigma_i = \sqrt{\log(1 + c_i^2)}$ throughout, and let n be the number of observations in the time series. The case of multiple time series sharing the same q , and the modifications required for the assumption of curvature, are addressed at the end of this subsection.

First, consider maximum likelihood estimation. When the (O_i) are assumed to be normally distributed

$$-\log(L) = \sum_i \log(c_i q E_i) + 0.5 \sum_i \left(\frac{O_i - q E_i}{c_i q E_i} \right)^2 \quad (6.29)$$

The value of q which minimises the objective function is found by solving for q under the following condition, $\partial/\partial q(-\log(L)) = 0$

$$\frac{\partial}{\partial q}(-\log(L)) = \frac{n}{q} + \frac{1}{q^2} \sum_i \frac{O_i}{c_i^2 E_i} - \frac{1}{q^3} \sum_i \left(\frac{O_i}{c_i E_i} \right)^2 \quad (6.30)$$

hence

$$\hat{q} = \frac{-S_1 + \sqrt{S_1^2 + 4nS_2}}{2n} \quad (6.31)$$

where $S_1 = \sum_i (O_i/c_i^2 E_i)$ and $S_2 = \sum_i (O_i/c_i E_i)^2$

When the (O_i) are assumed to be lognormally distributed,

$$-\log(L) = \sum_i \log(\sigma_i) + 0.5 \sum_i \left(\frac{\log(O_i) - \log(q E_i) + 0.5 \sigma_i^2}{\sigma_i} \right)^2 \quad (6.32)$$

$$\frac{\partial}{\partial q}(-\log(L)) = \frac{-1}{q} \sum_i \left(\frac{\log(O_i/E_i) - \log(q) + 0.5 \sigma_i^2}{\sigma_i^2} \right) \quad (6.33)$$

$$\hat{q} = \exp \frac{0.5n + S_3}{S_4} \quad (6.34)$$

where $S_3 = \sum_i (\log(O_i/E_I)/\sigma_i^2)$ and $S_4 = \sum_i (1/\sigma_i^2)$.

Next, consider Bayesian estimation, where a prior for q must be specified.

The effects of the prior on the equations are to replace likelihood L by posterior P throughout, to add $-\log(\pi(q))$ to the equation for $-\log(P)$ and $\partial/\partial q(-\log(-\pi(q)))$ to the equation for $\partial/\partial q(-\log(P))$

This last term is 0 for a uniform prior on q , $1/q$ for a log-uniform prior, and $\frac{1}{q} \left(1.5 + \frac{\log(q) - \log(\mu_q)}{\sigma_q^2} \right)$ for a lognormal prior, where μ_q and c_q are the mean and c.v. of the prior on q , respectively, and $\sigma_q = \sqrt{\log(1 + c_q^2)}$. Since the prior is uniform, the equation for \hat{q} is the same as the maximum likelihood estimation.

When the (O_i) are assumed to be normally distributed and the prior is log-uniform equation (6.31) becomes,

$$\hat{q} = \frac{-S_1 + \sqrt{S_1^2 + 4(n+1)S_2}}{2(n+1)} \quad (6.35)$$

but \hat{q} with either a normal or lognormal prior cannot be solved for.

When the O_i are assumed to be lognormally distributed and the prior is log-uniform, equation (6.34) becomes

$$\hat{q} = \exp \frac{0.5n - 1 + S_3}{S_4} \quad (6.36)$$

and if the prior is lognormal,

$$\hat{q} = \exp \frac{0.5n - 1.5 + \log(\mu_q)/\sigma_q^2 + S_3}{S_4 + 1/\sigma_q^2} \quad (6.37)$$

However, it is not possible to solve for \hat{q} with a normal prior.

An example of specifying the syntax and an equivalent additional prior

```
@catchability chatTANq
type nuisance
upper_bound 0.6
lower_bound 0.0001

@additional_prior chatTANq_prior
type lognormal
parameter catchabilityp[chatTANq].q
mu 0.3
cv 0.2
```

6.5. Ageing error

CASAL2 can apply ageing error to expected age frequencies estimated by the model. The ageing error is applied as a misclassification matrix, which has the effect of 'smearing' the expected age frequencies. This is mimicking the error involved in identifying the age of individuals. For example, fish species are aged by reading the ear bones (otoliths) which can be quite difficult depending on the species. These age frequencies are used in calculating the fits to the observed values, and hence the contribution to the total objective function.

Ageing error is optional, and if it is used, it may be omitted for any individual time series. Different ageing error models may be applied for different observation commands. See Section 7.14 for reporting the misclassification matrix at the end of model run.

The ageing error models implemented are

- None: The default model is to apply no ageing error.
- Off by one: Proportion p_1 of individuals of each age a are misclassified as age $a - 1$ and proportion p_2 are misclassified as age $a + 1$. Individuals of age $a < k$ are not misclassified. If there is no plus group in the population model, then proportion p_2 of the oldest age class will 'fall off the edge and disappear'.
- Normal: Individuals of age a are classified as ages which are normally distributed with mean a and constant c.v. c . As above, if there is no plus group in the population model, some individuals of the older age classes may disappear. If c is high enough, some of the younger age classes may 'fall off the other edge'. Individuals of age $a < k$ are not misclassified.

The expected values (fits) reported by CASAL2 for observations with ageing error will have had the ageing error applied.

6.6. Simulating observations

CASAL2 can generate simulated observations for a given model with a set of parameter values using `casal2 -s 1` (To simulate one set of simulated observations). Simulated observations are randomly generated values, which are generated with the error distributions defined for each observation, around fits calculated from one or more sets of the 'true' parameter values. Simulating from a set of parameters can be used to generate observations from an operating model or as a form of parametric bootstrap.

The procedure CASAL2 uses for simulating observations is to use the 'true' parameter values and generate the expected values. Then, if a set of observations use ageing error, ageing error is applied. Finally, a random value for each observed value is generated based on (i) the expected values, (ii) the type of likelihood specified, and (iii) the variability parameters (e.g., `error_value` and `process_error`).

Methods for generating the random error, and hence the simulated values, depend on the specific likelihood type of each observation.

- Normal likelihood parameterised by c.v.: Let E_i be the fitted value for observation i , and c_i be the corresponding c.v. (adjusted by the process error if applicable). Each simulated observation value S_i is generated as an independent normal deviate with mean E_i and standard deviation $E_i c_i$.
- Log-normal likelihood: Let E_i be the fitted value for observation i and c_i be the corresponding c.v. (adjusted by the process error if applicable). Each simulated observation value S_i is

generated as an independent lognormal deviate with mean and standard deviation (on the natural scale, not the log-scale) of E_i and $E_i c_i$ respectively. The robustification parameter δ is ignored.

- Multinomial likelihood: Let E_i be the fitted value for observation i , for i between 1 and n , and let N be the sample size (adjusted by process error if applicable, and then rounded up to the next whole number). The robustification parameter δ is ignored. Then,
 1. A sample of N values from 1 to n is generated using the multinomial distribution, using sample probabilities proportional to the values of E_i .
 2. Each simulated observation value S_i is calculated as the proportion of the N sampled values equalling i
 3. The simulated observation values S_i are then rescaled so that their sum is equal to 1
- Binomial and the normal approximation to the binomial likelihoods: Let E_i be the fitted value for observation i , for i between 1 and n , and N_i the corresponding equivalent sample size (adjusted by process error if applicable, and then rounded up to the next whole number). The robustification parameter δ is ignored. Then,
 1. A sample of N_i independent binary variates is generated, equalling 1 with probability E_i
 2. The simulated observation value S_i is calculated as the sum of these binary variates divided by N_i

An important note when simulating: CASAL2 will **not** automatically report simulated observations when using a `casal2 -s 1` run. A report must be defined using the `simulated_observation_report (@report[label].type=observation)`. See Section 7 for more information on how to write this report.

6.7. Pseudo-observations

CASAL2 can generate expected values for observations without them contributing to the total objective function. These are called pseudo-observations, and can be used to either generate the expected values from CASAL2 for reporting or diagnostic purposes. To define an observation as a pseudo-observation, use the command `@observation[label].likelihood=none`. Any observation type can be used as a pseudo-observation. CASAL2 can also generate simulated observations from pseudo-observations. Note that

- Output will be generated only if a report command `@report[label].type=observation` is specified.
- The observed values should be supplied (even if they are 'dummy' observations). These observation values will be processed by CASAL2 as if they were actual observation values, and must be in the same format as actual observation values.
- The subcommands `likelihood`, `obs`, `error_value`, and `process_error` have no effect when generating the expected values for the pseudo-observation.
- When simulating observations, the subcommand `simulation_likelihood` to indicate the likelihood to use. In this case, the `obs`, `error_value`, and `process_error` are used to determine the appropriate terms to use for the likelihood when simulating.

6.8. Residuals

CASAL2 will print the default residual values (i.e., observed less fitted) only when the report type `@report.type=observation` is used. For an observation O and F the corresponding fit ($=qE$ for relative observations), then

- Residuals = $O - F$

Pearson and normalised residuals can be generated using the CASAL2 **R** package. For specific **R** functions see Section 15.

The definitions used in the calculations are

- *Pearson residuals* attempt to express the residual relative to the variability of the observation, and are defined as $(O-F)/\text{std.dev.}(O)$, where $\text{std.dev.}(O)$ is calculated as
 - $F \times \text{cv}$ for normal, lognormal, robustified lognormal, and normal-log error distributions.
 - s for normal-by-standard deviation error distributions.
 - $\sqrt{\frac{Z(F,r)(1-Z(F,r))}{N}}$ for multinomial or binomial likelihoods.
 - $\sqrt{\frac{(F+r)(1-F+r)}{N}}$ for binomial-approx likelihood likelihoods.
- *Normalised residuals* to express the residual on a standard normal scale, and are defined as:
 - Equal to the Pearson residuals for normal error distributions.
 - $(\log(O/F)+0.5\sigma^2)/\sigma$ for lognormal (including robustified lognormal) error distributions, where $\sigma = \sqrt{\log(1+cv^2)}$.
 - $\log(O/F)/\sigma$ for normal-log error distributions, again with $\sigma = \sqrt{\log(1+cv^2)}$.
 - And are otherwise undefined.

where $Z(F,r)$ is the robustifying term on F (fit or expectation of the observation). This robustifying function is described earlier in the likelihood section.

7. The report section

The report section specifies the printouts and other output from the model. CASAL2 does not, in general, produce any output unless specified by a valid `@report` block.

7.1. Report command block format

Reports from CASAL2 can be defined to print partition and states objects at a particular point in time, observation summaries, estimated and derived parameter values, and objective function values.

```
@report observation_age ## label of report
type observation ## Type of report
observation age_1990 ## label corresponding to an @observation report, shown below

@observation age_1990
type proportion_at_age
year 1990
plus_group
etc ...
```

7.2. Report block output format

Reports from CASAL2 have a standard style (with one exception, the `output_parameters` report, see below). The standard style is that reports are prefixed with an asterisk followed by a user-defined label and type of report in brackets (e.g., `*label (type)`), with the report ending with the line `*end`. For example,

```
*My_report (type)
...
*end
```

This report block output format should make it easier for other software packages to read and process CASAL2 output. The `extract` functions in the **R** CASAL2 package use this information to identify and read CASAL2 output.

The `output_parameters` report does not print either a header or `*end` at the end of the report block. This is because the `output_parameters` report is designed to provide a single line vector of the estimated parameter values, or multiple lines for more than one set, which can be read by CASAL2 with the command `casal2 -i`. This is a specialised report for the `casal2 -o filename` command.

For estimated values in standard output use the `type=estimate_value` report.

Reports can be defined in a `@report` command block but may not be output, e.g., a report to print the partition for a year and/or timestep that does not exist, or reporting the covariance matrix when not estimation run mode.

Certain reports are associated with certain CASAL2 run modes. These reports are ignored by CASAL2 and the program will not generate any output for these reports, although they must still conform to CASAL2 syntax requirements.

Not all reports will be generated in all run modes. Some reports are only available in some run modes. For example, when simulating, only the simulation reports will be output.

7.3. Print the partition at the end of an initialisation

This report prints the partition following the initialisation phase, which includes the numbers of individuals in each age class and category in the partition. This report will print out in run modes `-r`, `-e`, `-f`.

7.4. Print the partition

This report prints the numbers of individuals in each age class and category in the partition for each given year or given years and timestep. This report is evaluated at the end of the timestep in the given year(s). This report will print out in run modes `-r`, `-e`, `-f`.

7.5. Print the age length and length weight values

This report prints the length and weight value for each age class and category in the partition for each given year or given years and timestep. This report is evaluated at the end of the timestep in the given year(s). This report will print out in run modes `-r`, `-e`, `-f`.

```
@report length_weight_at_age
type partition_mean_weight
time_step step2
years 1900:2013
```

7.6. Print a process summary

Depending on the process, different summaries are produced. These reports typically detail the type of process, its parameters and other options, and any associated details. This report will print out in run modes `-r`, `-e`, `-f`.

7.7. Print derived quantities

This report prints the description of the derived quantity, and the values of the derived quantity as recorded in the model state, for each year of the model, and for all years in the initialisation phase. This report will print out in run modes `-r`, `-e`, `-f`.

7.8. Print the estimated parameters

This report prints a summary of the estimated parameters using the type `estimate_summary`, including the parameter name, lower and upper bounds, the label of the prior, and its value. This report will print out in run modes `-r`, `-e`.

7.9. Print the estimated parameters in a vector format

This report prints the estimated parameter values out as a vector. The `estimate_values` report prints the name of the parameter, followed by the value for that run. This report will print out in run modes `-r`, `-e`.

7.10. Print the objective function

This report prints the total objective function value, the value of all observation likelihood components, the values of all priors, and the value of any penalties that have been incurred. If an individual model run does not incur a penalty, then the penalty will not be reported. This report will print out in run modes `-r`, `-e`, `-f`.

7.11. Print the covariance matrix

This report prints the Hessian and covariance matrices if in estimation run mode and if the covariance has been requested by `@minimiser[label].covariance=true`.

7.12. Print observations, fits, and residuals

This report prints, for each category or combination of categories, the expected values, residuals (observed – expected), the error value, process error, the total error (i.e., the error value as modified by any additional process error), and the contribution to the total objective function of that individual datum in the observation.

Constants in the likelihood components are often ignored in the objective function score of individual observation values. Hence, the total score from an observation equals the contribution of the objective function scores from each individual observation value plus a constant term (if applicable). In likelihood components without a constant term, the total score from an observation will equal the contribution of the objective function scores from each individual observation value.

If CASAL2 is in simulation run mode, then the contribution to the objective function of each observation is reported as zero.

```
@report Tan_at_age_obs
type observation
observation TAN_AT_AGE
```

7.13. Print simulated observations

This report prints a complete set of observation values in the form specified by `@report[label].type=observation`, with observed values replaced by randomly generated simulated values. The output is in a form suitable for use within a CASAL2 input configuration file, reproducing the command and subcommands from the input configuration file. This report will print out in run mode `-s`.

7.14. Print the ageing error misclassification matrix

This report prints the ageing error misclassification matrix used to offset observations within during model the model fitting procedure.

7.15. Print selectivities

This report prints the values of a selectivity for each age in the partition, for a given year and at then end of a given timestep.

7.16. Print the random number seed

This report prints the random number seed used by CASAL2 to initialise the generated random number sequence. Additional runs which use the same random number seed and the same model will produce identical outputs.

7.17. Print the results of an MCMC

This report prints the MCMC samples, objective function values, and proposal covariance matrix following an MCMC. This report will print out in run mode `-m`.

7.18. Print the MCMC samples as they are calculated

This report prints the MCMC samples for each new *i*th sample as they are calculated while doing an MCMC. The output file will be appended with each new sample as it is calculated by CASAL2. This report will print out in run mode `-m`.

7.19. Print the MCMC objective function values as they are calculated

This report prints the MCMC objective function values, along with the proposal covariance matrix, for each new *i*th sample as they are calculated while doing an MCMC. The output file will be appended with each new set of objective function values as it is calculated by CASAL2. This report will print out in run mode `-m`.

7.20. Print time varying parameters

This report prints all `@time_varying` blocks with the values and years in which they were specified. This report will print out in run modes `-r`, `-e`, `-m`.

```
@report time_varying_parameters
type time_varying
```

7.21. Tabular reporting format

An alternative reporting framework to the standard output is the tabular reporting format. Tabular reporting is used with multi-line `-i` input files (like the MCMC sample or `-o` outputs). Tabular reports will print out a row that will correspond with each row of the `-i` input files.

Tabular reporting is specified using the `--tabular` argument (`casal2 -r --tabular -i file_name`).

Derived quantities, processes, observations, and `estimate_values` are the only report types that can be output with this format. For each input file the output will begin with the names of each column followed by a multi-line report ending with the `*end` syntax.

These tables can be read with **R** using the `CASAL2` package. An example usage is reading in files of MCMC posterior values of derived quantities, which can then be plotted. This command is the same as running `casal -v` in CASAL.

8. Population command and subcommand syntax

In the syntax sections, the sub-section headers use a notation like "**@observation[label].type=abundance**" which, in this case, represents the input command fragment

```
@observation label #where label is a generic placeholder
type=abundance
...
```

and the sub-section will describe all of its own specific sub-commands. Common sub-commands are described after the command header.

8.1. Model structure

@model1 label Define an object of type *model*

start_year The first year of the model, immediately following initialisation

Type: non-negative integer

Default: No Default

Value: R, Defines the first year of the model, ≥ 1 , e.g. 1990,

final_year The final year of the model, excluding years in the projection period

Type: non-negative integer

Default: No Default

Value: Defines the last year of the model, i.e., the model is run from start_year to final_year

min_age The minimum age of individuals in the population

Type: non-negative integer

Default: 0

Value: R, $0 \leq \text{age}_{\min} \leq \text{age}_{\max}$,

max_age The maximum age of individuals in the population

Type: non-negative integer

Default: 0

Value: R, $0 \leq \text{age}_{\min} \leq \text{age}_{\max}$,

age_plus The oldest age or extra length midpoint ,plus group size, as a plus group

Type: boolean

Default: true

Value: true, false

initialisation_phases The labels of the phases of the initialisation

Type: string vector

Default: true

Value: R, A list of valid labels defined by @initialisation_phase,

time_steps The labels of the time steps, in the order that they are applied, to form the annual

- cycle**
Type: string vector
Default: No Default
Value: R,A list of valid labels defined by @time_step,
- projection_final_year** The final year of the model in projection mode
Type: non-negative integer
Default: 0
Value: R,Defines the last year of the projection period, i.e., the projection period runs from final_year+1 to projection_final_year. For the default, 0, no projections are run.,
- type** The type of model ,the partition structure,,: age, length, or hybrid
Type: string
Default: age
Allowed Values: age, length, hybrid
- length_bins** The minimum length in each length bin
Type: constant vector
Default: true
Value: R, $0 \leq \text{length}_{\min} \leq \text{length}_{\max}$,
- length_plus** Is there a length plus group or not?
Type: boolean
Default: true
Value: true, false
- length_plus_group** The mean length of length plus group
Type: constant
Default: 0
Value: R,length_{max} , length_plus_group,
- base_weight_units** The units for the base weight. This will be the default unit of any weight input parameters
Type: string
Default: tonnes
Value: grams, kgs or tonnes
Allowed Values: grams, tonnes, kgs

8.2. Initialisation

- @initialisation_phase label** Define an object of type *initialisation_phase*
- label** The label of the initialisation phase
Type: string
Default: No Default

`type` The type of initialisation
Type: string
Default: iterative

8.2.1. `@initialisation__phase[label].type=cinitial`

`categories` The list of categories for the Cinitial initialisation
Type: string vector
Default: No Default

8.2.2. `@initialisation__phase[label].type=derived`

`insert_processes` Additional processes not defined in the annual cycle that are to be inserted into this initialisation phase
Type: string vector
Default: true

`exclude_processes` Processes in the annual cycle to be excluded from this initialisation phase
Type: string vector
Default: true

`casal_initialisation_switch` Run an extra annual cycle to evaluate equilibrium SSBs. Warning - if true, this may not correctly evaluate the equilibrium state. Set to true if replicating a CASAL model
Type: boolean
Default: false

8.2.3. `@initialisation__phase[label].type=iterative`

`years` The number of iterations ,years, over which to execute this initialisation phase
Type: non-negative integer
Default: No Default

`insert_processes` The processes in the annual cycle to be included in this initialisation phase
Type: string vector
Default: true

`exclude_processes` The processes in the annual cycle to be excluded from this initialisation phase
Type: string vector
Default: true

`convergence_years` The iteration ,year, when the test for convergence ,lambda, is evaluated

Type: non-negative integer vector

Default: true

`lambda` The maximum value of the absolute sum of differences `,lambda`, between the partition at year-1 and year that indicates successful convergence

Type: constant

Default: 0.0

8.2.4. `@initialisation__phase[label].type=state_category_by_age`

`categories` The list of categories for the category state initialisation

Type: string vector

Default: No Default

`min_age` The minimum age of values supplied in the definition of the category state

Type: non-negative integer

Default: No Default

`max_age` The maximum age of values supplied in the definition of the category state

Type: non-negative integer

Default: No Default

8.3. Categories

`@categories` *label* Define an object of type *categories*

`format` The format that the category names use

Type: string

Default: No Default

`names` The names of the categories to be used in the model

Type: string vector

Default: No Default

`years` The years that individual categories will be active for. This overrides the model values

Type: string vector

Default: true

`age_lengths` R, The labels of `age_length` objects that are assigned to categories,

Type: string vector

Default: true

`length_weight` R, The labels of the `length_weight` objects that are assigned to categories,

Type: string vector

Default: true

`age_weight` R, The labels of the `age_weight` objects that are assigned to categories,
Type: string vector
Default: true

8.4. Time-steps

@time_step *label* Define an object of type *time_step*

`label` The label of the timestep
Type: string
Default: No Default

`processes` The labels of the processes for this time step in the order that they occur
Type: string vector
Default: No Default

8.5. Processes

@process *label* Define an object of type *process*

`label` The label of the process
Type: string
Default: No Default

`type` The type of process
Type: string
Default: ""

8.5.1. @process[label].type=ageing

`categories` The labels of the categories
Type: string vector
Default: No Default

8.5.2. @process[label].type=growth_basic

`categories` The labels of the categories
Type: string vector
Default: No Default

`number_of_growth_episodes` The number of growth episodes per year
Type: non-negative integer
Default: No Default

`growth_time_steps` The time step in which each growth episode occurs
 Type: string vector
 Default: No Default

`cv` The CV for the growth model
 Type: constant
 Default: 0.0
 Lower Bound: 0.0 (inclusive)

`sigma_min` The lower bound on sigma for the growth model
 Type: constant
 Default: 0.0
 Lower Bound: 0.0 (inclusive)

8.5.3. **@process[label].type=maturation**

`from` The list of categories to mature from
 Type: string vector
 Default: No Default

`to` The list of categories to mature to
 Type: string vector
 Default: No Default

`selectivities` The list of selectivities to use for maturation
 Type: string vector
 Default: No Default

`years` The years to be associated with the maturity rates
 Type: non-negative integer vector
 Default: No Default

`rates` The rates to mature for each year
 Type: estimable vector
 Default: No Default

8.5.4. **@process[label].type=mortality_constant_rate**

`categories` The list of categories labels
 Type: string vector
 Default: No Default

`m` The mortality rates

Type: estimable
Default: No Default
Lower Bound: 0.0 (inclusive)

`time_step_ratio` The time step ratios for the mortality rates
Type: constant vector
Default: true
Lower Bound: 0.0 (inclusive)
Upper Bound: 1.0 (inclusive)

8.5.5. `@process[label].type=mortality_event`

`categories` The categories
Type: string vector
Default: No Default

`years` The years in which to apply the mortality process
Type: non-negative integer vector
Default: No Default

`catches` The number of removals ,catches, to apply for each year
Type: estimable vector
Default: No Default

`u_max` The maximum exploitation rate , U_{max} ,
Type: estimable
Default: 0.99
Lower Bound: 0.0 (inclusive)
Upper Bound: 1.0 (inclusive)

`selectivities` The list of selectivities
Type: string vector
Default: No Default

`penalty` The label of the penalty to apply if the total number of removals cannot be taken
Type: string
Default: ""

8.5.6. `@process[label].type=mortality_event_biomass`

`categories` The category labels
Type: string vector
Default: No Default

`selectivities` The labels of the selectivities for each of the categories
 Type: string vector
 Default: No Default

`years` The years in which to apply the mortality process
 Type: non-negative integer vector
 Default: No Default

`catches` The biomass of removals ,catches, to apply for each year
 Type: estimable vector
 Default: No Default

`u_max` The maximum exploitation rate , U_{max} ,
 Type: estimable
 Default: 0.99
 Lower Bound: 0.0 (exclusive)
 Upper Bound: 1.0 (exclusive)

`penalty` The label of the penalty to apply if the total biomass of removals cannot be taken
 Type: string
 Default: ""

8.5.7. `@process[label].type=mortality_holling_rate`

`prey_categories` The prey categories labels
 Type: string vector
 Default: No Default

`predator_categories` The predator categories labels
 Type: string vector
 Default: No Default

`is_abundance` Is vulnerable amount of prey and predator an abundance [true] or biomass [false]
 Type: boolean
 Default: true

`a` Parameter a
 Type: estimable
 Default: No Default
 Lower Bound: 0.0 (inclusive)

`b` Parameter b

Type: estimable
Default: No Default
Lower Bound: 0.0 (inclusive)

`x` This parameter controls the functional form: Holling function type 2 , $x=2$, or 3 , $x=3$, or generalised ,Michaelis Menten, $x=1$,
Type: estimable
Default: No Default
Lower Bound: 1.0 (inclusive)

`u_max` The maximum exploitation rate , U_{max} ,
Type: constant
Default: No Default
Lower Bound: 0.0 (inclusive)
Upper Bound: 1.0 (inclusive)

`prey_selectivities` The selectivities for prey categories
Type: string vector
Default: true

`predator_selectivities` The selectivities for predator categories
Type: string vector
Default: true

`penalty` The label of penalty
Type: string
Default: ""

`years` The years in which to apply the mortality process
Type: non-negative integer vector
Default: No Default

8.5.8. @process[label].type=mortality_initialisation_event

`categories` The categories
Type: string vector
Default: No Default

`catch` The number of removals ,catches, to apply for each year
Type: estimable
Default: No Default

`u_max` The maximum exploitation rate , U_{max} ,

Type: estimable
 Default: 0.99
 Lower Bound: 0.0 (inclusive)
 Upper Bound: 1.0 (inclusive)

`selectivities` The list of selectivities
 Type: string vector
 Default: No Default

`penalty` The label of the penalty to apply if the total number of removals cannot be taken
 Type: string
 Default: ""

8.5.9. `@process[label].type=mortality_initialisation_event_biomass`

`categories` The categories
 Type: string vector
 Default: No Default

`catch` The number of removals ,catches, to apply for each year
 Type: estimable
 Default: No Default

`u_max` The maximum exploitation rate , U_{max} ,
 Type: estimable
 Default: 0.99
 Lower Bound: 0.0 (inclusive)
 Upper Bound: 1.0 (inclusive)

`selectivities` The list of selectivities
 Type: string vector
 Default: No Default

`penalty` The label of the penalty to apply if the total number of removals cannot be taken
 Type: string
 Default: ""

8.5.10. `@process[label].type=mortality_instantaneous`

`categories` The categories for instantaneous mortality
 Type: string vector
 Default: No Default

`m` The natural mortality rates for each category

Type: estimable
Default: No Default
Lower Bound: 0.0 (inclusive)

`time_step_ratio` The time step ratios for natural mortality
Type: constant vector
Default: true
Lower Bound: 0.0 (inclusive)
Upper Bound: 1.0 (inclusive)

`selectivities` The selectivities to apply on the categories for natural mortality
Type: string vector
Default: No Default

8.5.11. @process[label].type=mortality_instantaneous_retained

`categories` The categories for instantaneous mortality
Type: string vector
Default: No Default

`m` The natural mortality rates for each category
Type: estimable
Default: No Default
Lower Bound: 0.0 (inclusive)

`time_step_ratio` The time step ratios for natural mortality
Type: constant vector
Default: true
Lower Bound: 0.0 (inclusive)
Upper Bound: 1.0 (inclusive)

`selectivities` The selectivities to apply on the categories for natural mortality
Type: string vector
Default: No Default

8.5.12. @process[label].type=mortality_preysuitability

`prey_categories` The prey categories labels
Type: string vector
Default: No Default

`predator_categories` The predator categories labels
Type: string vector
Default: No Default

consumption_rate The predator consumption rate
Type: estimable
Default: No Default
Lower Bound: 0.0 (inclusive)
Upper Bound: 1.0 (inclusive)

electivities The prey electivities
Type: estimable vector
Default: No Default
Lower Bound: 0.0 (inclusive)
Upper Bound: 1.0 (inclusive)

u_max U max
Type: constant
Default: No Default
Lower Bound: 0.0 (inclusive)
Upper Bound: 1.0 (inclusive)

prey_selectivities The selectivities for prey categories
Type: string vector
Default: No Default

predator_selectivities The selectivities for predator categories
Type: string vector
Default: No Default

penalty The label of the penalty
Type: string
Default: ""

years The year that process occurs
Type: non-negative integer vector
Default: No Default

8.5.13. @process[label].type=recruitment_beverton_holt

categories The category labels
Type: string vector
Default: No Default

r0 R0
Type: estimable
Default: false
Lower Bound: 0.0 (inclusive)

- b0** **B0**
Type: estimable
Default: false
Lower Bound: 0.0 (inclusive)
- proportions** The proportion for each category
Type: estimable
Default: No Default
- age** The age at recruitment
Type: non-negative integer
Default: true
- ssb_offset** The spawning biomass year offset
Type: non-negative integer
Default: true
- steepness** Steepness ,h,
Type: estimable
Default: 1.0
Lower Bound: 0.2 (inclusive)
Upper Bound: 1.0 (inclusive)
- ssb** The SSB label ,derived quantity,
Type: string
Default: No Default
- b0_initialisation_phase** The initialisation phase label that B0 is from
Type: string
Default: ""
- yces_values** The YCS values
Type: estimable vector
Default: No Default
- yces_years** The recruitment years. A vector of years that relates to the year of the spawning event that created this cohort
Type: non-negative integer vector
Default: false
- standardise_yces_years** The years that are included for year class standardisation
Type: non-negative integer vector
Default: true

8.5.14. @process[label].type=recruitment_beverton_holt_with_deviations

categories The category labels

Type: string vector

Default: No Default

r0 R0

Type: estimable

Default: false

Lower Bound: 0.0 (inclusive)

b0 B0

Type: estimable

Default: false

Lower Bound: 0.0 (inclusive)

proportions The proportion for each category

Type: estimable

Default: No Default

age The age at recruitment

Type: non-negative integer

Default: true

ssb_offset The spawning biomass year offset

Type: non-negative integer

Default: true

steepness Steepness ,h,

Type: estimable

Default: 1.0

Lower Bound: 0.2 (inclusive)

ssb The SSB Label ,derived quantity,

Type: string

Default: No Default

sigma_r sigma R

Type: estimable

Default: No Default

Lower Bound: 0.0 (inclusive)

b_max The maximum bias adjustment

Type: estimable
Default: 0.85
Lower Bound: 0.0 (inclusive)
Upper Bound: 1.0 (inclusive)

`last_year_with_no_bias` The last year with no bias adjustment
Type: non-negative integer
Default: false

`first_year_with_bias` The first year with full bias adjustment
Type: non-negative integer
Default: false

`last_year_with_bias` The last year with full bias adjustment
Type: non-negative integer
Default: false

`first_recent_year_with_no_bias` The first recent year with no bias adjustment
Type: non-negative integer
Default: false

`b0_initialisation_phase` The initialisation phase label that B0 is from
Type: string
Default: ""

`deviation_values` The recruitment deviation values
Type: estimable vector
Default: No Default

`deviation_years` The recruitment years. A vector of years that relates to the year of the spawning event that created this cohort
Type: non-negative integer vector
Default: false

8.5.15. @process[label].type=recruitment_constant

`categories` The categories
Type: string vector
Default: No Default

`proportions` The proportions
Type: estimable
Default: true

`length_bins` The length bins that recruits are uniformly distributed over at the time of

recruitment
Type: constant vector
Default: No Default

r0 R0
Type: estimable
Default: No Default
Lower Bound: 0.0 (inclusive)

8.5.16. **@process[label].type=survival_constant_rate**

categories The list of categories
Type: string vector
Default: No Default

s The survival rates
Type: estimable
Default: No Default
Lower Bound: 0.0 (inclusive)
Upper Bound: 1.0 (inclusive)

time_step_ratio The time step ratios for S
Type: constant vector
Default: true
Lower Bound: 0.0 (exclusive)
Upper Bound: 1.0 (inclusive)

selectivities The selectivity label
Type: string vector
Default: No Default

8.5.17. **@process[label].type=tag_by_age**

from The categories to transition from
Type: string vector
Default: No Default

to The categories to transition to
Type: string vector
Default: No Default

min_age The minimum age to transition
Type: non-negative integer
Default: No Default

`max_age` The maximum age to transition
Type: non-negative integer
Default: No Default

`penalty` The penalty label
Type: string
Default: ""

`u_max` U Max
Type: constant
Default: 0.99
Lower Bound: 0.0 (exclusive)
Upper Bound: 1.0 (inclusive)

`years` The years to execute the transition in
Type: non-negative integer vector
Default: No Default

`initial_mortality` The initial mortality value
Type: constant
Default: 0.0
Lower Bound: 0.0 (inclusive)

`initial_mortality_selectivity` The initial mortality selectivity label
Type: string
Default: ""

`loss_rate` The loss rate
Type: constant vector
Default: No Default

`loss_rate_selectivities` The loss rate selectivity label
Type: string vector
Default: true

`selectivities` The selectivity labels
Type: string vector
Default: No Default

`n` N
Type: constant vector
Default: true

8.5.18. @process[label].type=tag_by_length

from The categories to transition from

Type: string vector

Default: No Default

to The categories to transition to

Type: string vector

Default: No Default

penalty The penalty label

Type: string

Default: ""

u_max U Max

Type: constant

Default: 0.99

Lower Bound: 0.0 (exclusive)

Upper Bound: 1.0 (inclusive)

initial_mortality

Type: constant

Default: 0.0

Lower Bound: 0.0 (inclusive)

initial_mortality_selectivity

Type: string

Default: ""

selectivities

Type: string vector

Default: No Default

n

Type: constant vector

Default: true

8.5.19. @process[label].type=tag_loss

categories The list of categories

Type: string vector

Default: No Default

tag_loss_rate The tag loss rates

Type: constant vector
Default: No Default
Lower Bound: 0.0 (inclusive)
Upper Bound: 1.0 (inclusive)

`time_step_ratio` The time step ratios for tag loss
Type: constant vector
Default: true
Lower Bound: 0.0 (inclusive)
Upper Bound: 1.0 (inclusive)

`tag_loss_type` The type of tag loss
Type: string
Default: No Default

`selectivities` The selectivities
Type: string vector
Default: No Default

`year` The year the first tagging release process was executed
Type: non-negative integer
Default: No Default

8.5.20. `@process[label].type=transition_category`

`from` The from category
Type: string vector
Default: No Default

`to` The to category
Type: string vector
Default: No Default

`proportions` The proportions
Type: estimable
Default: No Default
Lower Bound: 0.0 (inclusive)
Upper Bound: 1.0 (inclusive)

`selectivities` The selectivity names
Type: string vector
Default: No Default

8.5.21. @process[label].type=transition_category_by_age

from The categories to transition from

Type: string vector

Default: No Default

to The categories to transition to

Type: string vector

Default: No Default

min_age The minimum age to transition

Type: non-negative integer

Default: No Default

max_age The maximum age to transition

Type: non-negative integer

Default: No Default

penalty The penalty label

Type: string

Default: ""

u_max U max

Type: constant

Default: 0.99

Lower Bound: 0.0 (exclusive)

Upper Bound: 1.0 (inclusive)

years The years to execute the transition in

Type: non-negative integer vector

Default: No Default

8.6. Time varying parameters

@time_varying *label* Define an object of type *time_varying*

label The time-varying label

Type: string

Default: No Default

type The time-varying type

Type: string

Default: ""

years The years in which to vary the values

Type: non-negative integer vector

Default: No Default

parameter The name of the parameter to time vary

Type: string

Default: No Default

8.6.1. **@time__varying[label].type=annual_shift**

values The values

Type: constant vector

Default: No Default

a Parameter A

Type: constant

Default: No Default

b Parameter B

Type: constant

Default: No Default

c Parameter C

Type: constant

Default: No Default

scaling_years The scaling years

Type: non-negative integer vector

Default: true

8.6.2. **@time__varying[label].type=constant**

values The value to assign to addressable

Type: estimable vector

Default: No Default

8.6.3. **@time__varying[label].type=exogenous**

a The shift parameter

Type: estimable

Default: No Default

exogeneous_variable The values of exogeneous variable for each year

Type: constant vector
Default: No Default

8.6.4. @time__varying[label].type=linear

slope The slope of the linear trend ,additive unit per year,
Type: estimable
Default: No Default

intercept The intercept of the linear trend value for the first year
Type: estimable
Default: No Default

8.6.5. @time__varying[label].type=random_draw

mean The mean ,mu,
Type: estimable
Default: 0

sigma The standard deviation ,sigma,
Type: estimable
Default: 1

distribution The distribution
Type: string
Default: normal
Allowed Values: normal, lognormal

8.6.6. @time__varying[label].type=random_walk

mean The mean ,mu,
Type: estimable
Default: 0

sigma The standard deviation ,sigma,
Type: estimable
Default: 1

upper_bound The upper bound for the random walk
Type: constant
Default: 1

upper_bound The lower bound for the random walk

Type: constant

Default: 1

`rho` The autocorrelation parameter ,rho,

Type: constant

Default: 1

`distribution` The distribution

Type: string

Default: normal

8.7. Derived quantities

@derived_quantity *label* Define an object of type *derived_quantity*

`label` The label of the derived quantity

Type: string

Default: No Default

`type` The type of derived quantity

Type: string

Default: No Default

`time_step` The time step in which to calculate the derived quantity after

Type: string

Default: No Default

`categories` The list of categories to use when calculating the derived quantity

Type: string vector

Default: No Default

`selectivities` A list of one selectivity

Type: string vector

Default: No Default

`time_step_proportion` The proportion through the mortality block of the time step when calculated

Type: constant

Default: 0.5

Lower Bound: 0.0 (inclusive)

Upper Bound: 1.0 (inclusive)

`time_step_proportion_method` The method for interpolating for the proportion through the

mortality block

Type: string

Default: weighted_sum

Allowed Values: weighted_sum, weighted_product

values

Type: Addressable vector

Default: No Default

8.7.1. @derived__quantity[label].type=abundance

8.7.2. @derived__quantity[label].type=biomass

8.8. Age-length relationship

@age_length label Define an object of type *age_length*

label The label of the age length relationship

Type: string

Default: No Default

type The type of age length relationship

Type: string

Default: No Default

time_step_proportions The fraction of the year applied in each time step that is added to the age for the purposes of evaluating the length, i.e., a value of 0.5 for a time step will evaluate the length of individuals at age+0.5 in that time step

Type: constant vector

Default: true

Lower Bound: 0.0 (inclusive)

Upper Bound: 1.0 (inclusive)

distribution The assumed distribution for the growth curve

Type: string

Default: normal

cv_first The CV for the first age class

Type: estimable

Default: 0.0

Lower Bound: 0.0 (inclusive)

cv_last The CV for last age class

Type: estimable

Default: 0.0

Lower Bound: 0.0 (inclusive)

`casal_switch` If true, use the ,less accurate, equation for the cumulative normal function as was used in the legacy version of CASAL.

Type: boolean

Default: false

`by_length` Specifies if the linear interpolation of CVs is a linear function of mean length at age. Default is by age only

Type: boolean

Default: true

8.8.1. `@age__length[label].type=data`

`external_gaps` The method to use for external data gaps

Type: string

Default: mean

Allowed Values: mean, nearest_neighbour

`internal_gaps` The method to use for internal data gaps

Type: string

Default: mean

Allowed Values: mean, nearest_neighbour, interpolate

`length_weight` The label from an associated length-weight block

Type: string

Default: No Default

`time_step_measurements_were_made` The time step label for which size-at-age data are provided

Type: string

Default: No Default

8.8.2. `@age__length[label].type=none`

8.8.3. `@age__length[label].type=schnute`

`y1` The y_1 parameter

Type: estimable

Default: No Default

`y2` The y_2 parameter

Type: estimable

Default: No Default

`tau1` The τ_1 parameter

Type: estimable
Default: No Default

`tau2` The τ_2 parameter
Type: estimable
Default: No Default

`a` The a parameter
Type: estimable
Default: No Default
Lower Bound: 0.0 (inclusive)

`b` The b parameter
Type: estimable
Default: No Default
Lower Bound: 0.0 (exclusive)

`length_weight` The label of the associated length-weight relationship
Type: string
Default: No Default

8.8.4. `@age__length[label].type=von_bertalanffy`

`linf` The $L_{infinity}$ parameter
Type: estimable
Default: No Default
Lower Bound: 0.0 (inclusive)

`k` The k parameter
Type: estimable
Default: No Default
Lower Bound: 0.0 (inclusive)

`t0` The t_0 parameter
Type: estimable
Default: No Default

`length_weight` The label of the associated length-weight relationship
Type: string
Default: No Default

8.9. Length-weight

`@length_weight label` Define an object of type *length_weight*

`label` The label of the length-weight relationship
Type: string
Default: No Default

`type` The type of the length-weight relationship
Type: string
Default: No Default

8.9.1. `@length__weight[label].type=basic`

a The a parameter, $W = aL^b$,
Type: estimable
Default: No Default
Lower Bound: 0.0 (exclusive)

b The b parameter, $W = aL^b$,
Type: estimable
Default: No Default
Lower Bound: 0.0 (exclusive)

`units` The units of measure ,tonnes, kgs, grams,
Type: string
Default: No Default
Allowed Values: tonnes, kgs, grams

8.9.2. `@length__weight[label].type=none`

8.10. Selectivities

`@selectivity label` Define an object of type *selectivity*

`label` The label for this selectivity
Type: string
Default: No Default

`type` The type of selectivity
Type: string
Default: No Default

`length_based` Is the selectivity length based?
Type: boolean
Default: false

`intervals` The number of quantiles to evaluate a length-based selectivity over the age-length

distribution

Type: non-negative integer

Default: 5

partition_type The type of partition that this selectivity will support. Defaults to the same as the model

Type: string

Default: model

Allowed Values: model, age, length, hybrid

values

Type: Addressable vector

Default: No Default

length_values

Type: Addressable vector

Default: No Default

8.10.1. @selectivity[label].type=all_values

v The v parameter

Type: estimable vector

Default: No Default

8.10.2. @selectivity[label].type=all_values_bounded

l The low value ,L,

Type: non-negative integer

Default: No Default

h The high value ,H,

Type: non-negative integer

Default: No Default

v The v parameter

Type: estimable vector

Default: No Default

8.10.3. @selectivity[label].type=constant

c The constant value

Type: estimable

Default: No Default

8.10.4. @selectivity[label].type=double_exponential

x0 The X0 parameter

Type: estimable

Default: No Default

x1 The X1 parameter

Type: constant

Default: No Default

x2 The X2 parameter

Type: constant

Default: No Default

y0 The Y0 parameter

Type: estimable

Default: No Default

Lower Bound: 0.0 (inclusive)

y1 The Y1 parameter

Type: estimable

Default: No Default

Lower Bound: 0.0 (inclusive)

y2 The Y2 parameter

Type: estimable

Default: No Default

Lower Bound: 0.0 (inclusive)

alpha alpha

Type: estimable

Default: 1.0

Lower Bound: 0.0 (exclusive)

8.10.5. @selectivity[label].type=double_normal

mu The mean ,mu,

Type: estimable

Default: No Default

sigma_l The sigma L parameter

Type: estimable
Default: No Default
Lower Bound: 0.0 (exclusive)

sigma_r The sigma R parameter
Type: estimable
Default: No Default
Lower Bound: 0.0 (exclusive)

alpha alpha
Type: estimable
Default: 1.0
Lower Bound: 0.0 (exclusive)

8.10.6. @selectivity[label].type=increasing

l The low value ,L,
Type: non-negative integer
Default: No Default

h The high value ,H,
Type: non-negative integer
Default: No Default

v The v parameter
Type: estimable vector
Default: No Default

alpha alpha
Type: constant
Default: 1.0
Lower Bound: 0.0 (exclusive)

8.10.7. @selectivity[label].type=inverse_logistic

a50 a50
Type: estimable
Default: No Default

ato95 ato95
Type: estimable
Default: No Default
Lower Bound: 0.0 (exclusive)

alpha alpha
Type: estimable
Default: 1.0
Lower Bound: 0.0 (exclusive)

8.10.8. @selectivity[label].type=knife_edge

e The edge value
Type: estimable
Default: No Default

alpha alpha
Type: estimable
Default: 1.0

8.10.9. @selectivity[label].type=logistic

a50 a50
Type: estimable
Default: No Default

ato95 ato95
Type: estimable
Default: No Default
Lower Bound: 0.0 (exclusive)

alpha alpha
Type: estimable
Default: 1.0
Lower Bound: 0.0 (exclusive)

8.10.10. @selectivity[label].type=logistic_producing

l The low value ,L,
Type: non-negative integer
Default: No Default

h The high value ,H,
Type: non-negative integer
Default: No Default

a50 a50

Type: estimable
Default: No Default

ato95 ato95
Type: estimable
Default: No Default
Lower Bound: 0.0 (exclusive)

alpha alpha
Type: estimable
Default: 1.0
Lower Bound: 0.0 (exclusive)

8.11. Projections

@project *label* Define an object of type *project*

label Label
Type: string
Default: No Default

type Type
Type: string
Default: ""

years Years to recalculate the values
Type: non-negative integer vector
Default: true

parameter Parameter to project
Type: string
Default: No Default

multiplier Multiplier that is applied to the projected value
Type: constant
Default: 1.0
Lower Bound: 0.0 (exclusive)

8.11.1. @project[label].type=constant

values The values to assign to the addressable
Type: constant vector
Default: No Default

8.11.2. @project[label].type=empirical_sampling

start_year The start year of sampling
Type: non-negative integer
Default: false

final_year The final year of sampling
Type: non-negative integer
Default: false

8.11.3. @project[label].type=log_normal

mean The mean of the lognormal process
Type: constant
Default: 0.0

sigma The standard deviation ,sigma, of the lognormal process
Type: constant
Default: No Default
Lower Bound: 0.0 (inclusive)

8.11.4. @project[label].type=log_normal_empirical

mean The mean of gaussian process
Type: constant
Default: 0.0

start_year The start year of sampling
Type: non-negative integer
Default: false

final_year The final year of sampling
Type: non-negative integer
Default: false

8.11.5. @project[label].type=user_defined

equation The equation to do a test run of
Type: string vector
Default: No Default

8.12. Time-varying Parameters

@time_varying *label* Define an object of type *time_varying*

label The time-varying label

Type: string

Default: No Default

type The time-varying type

Type: string

Default: ""

years The years in which to vary the values

Type: non-negative integer vector

Default: No Default

parameter The name of the parameter to time vary

Type: string

Default: No Default

8.12.1. @time__varying[label].type=annual_shift

values The values

Type: constant vector

Default: No Default

a Parameter A

Type: constant

Default: No Default

b Parameter B

Type: constant

Default: No Default

c Parameter C

Type: constant

Default: No Default

scaling_years The scaling years

Type: non-negative integer vector

Default: true

8.12.2. @time__varying[label].type=constant

values The value to assign to addressable

Type: estimable vector

Default: No Default

8.12.3. @time__varying[label].type=exogenous

a The shift parameter

Type: estimable

Default: No Default

exogeneous_variable The values of exogeneous variable for each year

Type: constant vector

Default: No Default

8.12.4. @time__varying[label].type=linear

slope The slope of the linear trend ,additive unit per year,

Type: estimable

Default: No Default

intercept The intercept of the linear trend value for the first year

Type: estimable

Default: No Default

8.12.5. @time__varying[label].type=random_draw

mean The mean ,mu,

Type: estimable

Default: 0

sigma The standard deviation ,sigma,

Type: estimable

Default: 1

distribution The distribution

Type: string

Default: normal

Allowed Values: normal, lognormal

8.12.6. @time__varying[label].type=random_walk

mean The mean ,mu,
Type: estimable
Default: 0

sigma The standard deviation ,sigma,
Type: estimable
Default: 1

upper_bound The upper bound for the random walk
Type: constant
Default: 1

upper_bound The lower bound for the random walk
Type: constant
Default: 1

rho The autocorrelation parameter ,rho,
Type: constant
Default: 1

distribution The distribution
Type: string
Default: normal

9. Estimation command and subcommand syntax

In the syntax sections, the sub-section headers use a notation like "**@observation[label].type=abundance**" which, in this case, represents the input command fragment

```
@observation label #where label is a generic placeholder
type=abundance
...
```

and the sub-section will describe all of its own specific sub-commands. Common sub-commands are described after the command header.

9.1. Estimation methods

@estimate label Define an object of type *estimate*

label The label of the estimate
Type: string
Default: ""

- `type` The prior type for the estimate
Type: string
Default: No Default
- `parameter` The name of the parameter to estimate in the model
Type: string
Default: No Default
- `lower_bound` The lower bound for the parameter
Type: constant
Default: No Default
- `upper_bound` The upper bound for the parameter
Type: constant
Default: No Default
- `same` List of parameters that are constrained to have the same value as this parameter
Type: string vector
Default: ""
- `estimation_phase` The first estimation phase to allow this to be estimated
Type: non-negative integer
Default: 1
- `mcmc` Indicates if this parameter is estimated at the point estimate but fixed during MCMC estimation run
Type: boolean
Default: false
- `transformation` Type of simple transformation to apply to estimate
Type: string
Default: ""
- `transform_with_jacobian` Apply jacobian during transformation
Type: boolean
Default: false
- `prior_applies_to_transform` Does the prior apply to the transformed parameter? a legacy switch, see Manual for more information
Type: boolean
Default: false

9.1.1. @estimate[label].type=beta

mu Beta prior mean ,mu, parameter

Type: estimable

Default: No Default

sigma Beta prior variance ,sigma, parameter

Type: estimable

Default: No Default

Lower Bound: 0.0 (exclusive)

a Beta prior lower bound of the range ,A, parameter

Type: constant

Default: No Default

b Beta prior upper bound of the range ,B, parameter

Type: constant

Default: No Default

9.1.2. @estimate[label].type=lognormal

mu The lognormal prior mean ,mu, parameter

Type: estimable

Default: No Default

Lower Bound: 0.0 (exclusive)

cv The lognormal variance ,cv, parameter

Type: estimable

Default: No Default

Lower Bound: 0.0 (exclusive)

9.1.3. @estimate[label].type=normal

mu The normal prior mean ,mu, parameter

Type: estimable

Default: No Default

cv The normal variance ,standard deviation, parameter

Type: estimable

Default: No Default

Lower Bound: 0.0 (exclusive)

9.1.4. @estimate[label].type=normal_by_stdev

`mu` The normal prior mean ,mu, parameter

Type: estimable

Default: No Default

`sigma` The normal variance ,sigma, parameter

Type: estimable

Default: No Default

Lower Bound: 0.0 (exclusive)

`lognormal_transformation` Add a Jacobian if the derived outcome of the estimate is assumed to be lognormal, e.g., used for recruitment deviations in the recruitment process. See the User Manual for more information

Type: boolean

Default: false

9.1.5. @estimate[label].type=normal_log

`mu` The normal-log prior mean ,mu, parameter

Type: estimable

Default: No Default

`sigma` The normal-log prior variance ,standard deviation, parameter

Type: estimable

Default: No Default

Lower Bound: 0.0 (exclusive)

9.1.6. @estimate[label].type=uniform**9.1.7. @estimate[label].type=uniform_log****9.2. Point estimation**

@minimiser *label* Define an object of type *minimiser*

`label` The minimiser label

Type: string

Default: No Default

`type` The type of minimiser to use

Type: string

Default: No Default

`active` Indicates if this minimiser is active

Type: boolean
Default: false

covariance Indicates if a covariance matrix should be generated
Type: boolean
Default: true

9.2.1. @minimiser[label].type=adolc

iterations The maximum number of iterations
Type: integer
Default: 1000
Lower Bound: 1 (inclusive)

evaluations The maximum number of evaluations
Type: integer
Default: 4000
Lower Bound: 1 (inclusive)

tolerance The tolerance of the gradient for convergence
Type: constant
Default: 0.02
Lower Bound: 0.0 (exclusive)

step_size The minimum step size before minimisation fails
Type: constant
Default: 1e-7
Lower Bound: 0.0 (exclusive)

9.2.2. @minimiser[label].type=betadiff

iterations The maximum number of iterations
Type: integer
Default: 1000
Lower Bound: 1 (inclusive)

evaluations The maximum number of evaluations
Type: integer
Default: 4000
Lower Bound: 1 (inclusive)

tolerance The tolerance of the gradient for convergence
Type: constant
Default: 2e-3
Lower Bound: 0.0 (exclusive)

9.2.3. @minimiser[label].type=cppad

retape Retape?

Type: string

Default: "true"

Allowed Values: true, false

print_level The level of debug to stdout

Type: non-negative integer

Default: 5u

Lower Bound: 0u (inclusive)

Upper Bound: 12u (inclusive)

sb String buffer output?

Type: string

Default: "yes"

Allowed Values: yes, no

pidi Print iteration diagnostic information?

Type: string

Default: "yes"

Allowed Values: yes, no

max_iter The maximum number of iterations

Type: non-negative integer

Default: 4000

Lower Bound: 1u (inclusive)

tol The tolerance for convergence

Type: constant

Default: 1e-9

Lower Bound: 0.0 (exclusive)

acceptable_tol The acceptable tolerance

Type: constant

Default: 1e-6

Lower Bound: 0.0 (exclusive)

acceptable_obj_change_tol

Type: constant

Default: 1e+20

Lower Bound: 0.0 (exclusive)

derivative_test How to test for derivatives

Type: string
Default: "first-order"
Allowed Values: none, first-order, second-order, only-second-order

`point_perturbation_radius` The point perturbation radius
Type: constant
Default: 0.0
Lower Bound: 0.0 (inclusive)

9.2.4. `@minimiser[label].type=de_solver`

`population_size` The number of candidate solutions to have in the population
Type: non-negative integer
Default: No Default

`crossover_probability` The minimiser's crossover probability
Type: constant
Default: 0.9
Lower Bound: 0.0 (inclusive)
Upper Bound: 1.0 (inclusive)

`difference_scale` The scale to apply to new solutions when comparing candidates
Type: constant
Default: 0.02

`max_generations` The maximum number of iterations to run
Type: non-negative integer
Default: No Default

`tolerance` The total variance between the population and best candidate before acceptance
Type: constant
Default: 0.01
Lower Bound: 0.0 (exclusive)

`method` The type of candidate generation method to use
Type: string
Default: ""
Value: not_yet_implemented

9.2.5. `@minimiser[label].type=d_lib`

`minimisation_type` The type of minimisation to use
Type: string
Default: `min_using_approximate_derivatives`
Allowed Values: `min_using_approximate_derivatives`, `minimisation`, `min_box_constrained`,

min_trust_region, min_bobyqa, min_global

search_strategy The type of search strategy to use

Type: string

Default: bfgs

Allowed Values: bfgs, lbfgs, cg, newton

tolerance The tolerance of the gradient for convergence

Type: constant

Default: 1e-7

Lower Bound: 0.0 (exclusive)

lbfgs_max_size The maximum size for the LBFGS search strategy

Type: non-negative integer

Default: 1

bobyqa_interpolation_points BOBYQA interpolation points

Type: non-negative integer

Default: 5u

bobyqa_initial_trust_radius BOBYQA initial trust radius

Type: constant

Default: 1e-2

bobyqa_stopping_trust_radius BOBYQA stopping trust radius

Type: constant

Default: 1e-6

bobyqa_max_evaluations BOBYQA max objective evaluations

Type: constant

Default: 4000

Lower Bound: 1 (inclusive)

verbose Print debug of objective function calls?

Type: boolean

Default: false

9.2.6. @minimiser[label].type=numerical_differences

iterations The maximum number of iterations

Type: integer

Default: 1000

Lower Bound: 1 (inclusive)

evaluations The maximum number of evaluations

Type: integer
 Default: 4000
 Lower Bound: 1 (inclusive)

`tolerance` The tolerance of the gradient for convergence
 Type: constant
 Default: 0.02
 Lower Bound: 0.0 (exclusive)

`step_size` The minimum step size before minimisation fails
 Type: constant
 Default: 1e-7
 Lower Bound: 0.0 (exclusive)

9.3. Markov chain Monte Carlo (MCMC)

@mcmc *label* Define an object of type *mcmc*

`label` The label of the MCMC
 Type: string
 Default: No Default

`type` The type of MCMC
 Type: string
 Default: ""

`length` The number of iterations in for the MCMC chain
 Type: non-negative integer
 Default: No Default

`active` Indicates if this is the active MCMC algorithm
 Type: boolean
 Default: true

`step_size` Initial stepsize ,as a multiplier of the approximate covariance matrix,
 Type: constant
 Default: 0.02

9.3.1. @mcmc[label].type=independence_metropolis

`start` The covariance multiplier for the starting point of the MCMC
 Type: constant
 Default: 0.0
 Lower Bound: 0.0 (inclusive)

- keep** The spacing between recorded values in the MCMC
Type: non-negative integer
Default: 1u
Lower Bound: 1u (inclusive)
- max_correlation** The maximum absolute correlation in the covariance matrix of the proposal distribution
Type: constant
Default: 0.8
Lower Bound: 0.0 (exclusive)
Upper Bound: 1.0 (inclusive)
- covariance_adjustment_method** The method for adjusting small variances in the covariance proposal matrix
Type: string
Default: correlation
Allowed Values: covariance, correlation, none
- correlation_adjustment_diff** The minimum non-zero variance times the range of the bounds in the covariance matrix of the proposal distribution
Type: constant
Default: 0.0001
Lower Bound: 0.0 (exclusive)
- proposal_distribution** The shape of the proposal distribution ,either the t or the normal distribution,
Type: string
Default: t
- df** The degrees of freedom of the multivariate t proposal distribution
Type: non-negative integer
Default: 4
Lower Bound: 0 (exclusive)
- adapt_stepsize_at** The iteration numbers in which to check and resize the MCMC stepsize
Type: non-negative integer vector
Default: true
Lower Bound: 0 (inclusive)
- adapt_covariance_matrix_at** The iteration numbers in which to check and resize the MCMC stepsize
Type: non-negative integer vector
Default: true
Lower Bound: 0 (inclusive)
- adapt_stepsize_method** The method to use to adapt the step size

Type: string
Default: ratio
Allowed Values: ratio, double_half

9.4. Profiles

@profile *label* Define an object of type *profile*

label The label of the profile
Type: string
Default: ""

steps The number of steps between the lower and upper bound
Type: non-negative integer
Default: No Default

lower_bound The lower bounds
Type: constant
Default: No Default

upper_bound The upper bounds
Type: constant
Default: No Default

parameter The system parameter to profile
Type: string
Default: No Default

same A parameter that is constrained to have the same value as the parameter being profiled
Type: string
Default: ""

9.5. Defining catchability constants

@catchability *label* Define an object of type *catchability*

label Label of the catchability
Type: string
Default: No Default

type The type of catchability
Type: string
Default: No Default

9.5.1. @catchability[label].type=free

q The value of the catchability
Type: estimable
Default: No Default
Lower Bound: 0.0 (inclusive)

9.5.2. @catchability[label].type=nuisance

lower_bound The upper bound for nuisance catchability
Type: constant
Default: No Default

upper_bound The lower bound for nuisance catchability
Type: constant
Default: No Default

q
Type: Addressable
Default: No Default

9.6. Defining penalties

@penalty label Define an object of type *penalty*

label The label of the penalty
Type: string
Default: No Default

type The type of penalty
Type: string
Default: No Default

9.6.1. @penalty[label].type=process

multiplier The penalty multiplier
Type: constant
Default: 1.0
Lower Bound: 0.0 (exclusive)

log_scale Indicates if the sums of squares is calculated on the log scale
Type: boolean
Default: false

9.7. Defining priors on parameter ratios, differences, and means

@additional_prior *label* Define an object of type *additional_prior*

parameter The name of the parameter to generate additional prior on

Type: string

Default: No Default

label The label for the additional prior

Type: string

Default: No Default

type The type of additional prior

Type: string

Default: No Default

9.7.1. @additional__prior[label].type=beta

mu Beta distribution mean ,mu, parameter

Type: constant

Default: No Default

sigma Beta distribution variance ,sigma, parameter

Type: constant

Default: No Default

Lower Bound: 0.0 (inclusive)

a Beta distribution lower bound of the range ,A, parameter

Type: constant

Default: No Default

b Beta distribution upper bound of the range ,B, parameter

Type: constant

Default: No Default

9.7.2. @additional__prior[label].type=element_difference

second_parameter The name of the second parameter for comparing

Type: string

Default: No Default

multiplier Multiply the penalty by this factor

Type: constant

Default: 1

9.7.3. @additional__prior[label].type=log_normal

`mu` The lognormal prior mean ,mu, parameter

Type: constant

Default: No Default

Lower Bound: 0.0 (exclusive)

`cv` The lognormal variance ,cv, parameter

Type: constant

Default: No Default

Lower Bound: 0.0 (exclusive)

9.7.4. @additional__prior[label].type=uniform_log**9.7.5. @additional__prior[label].type=vector_average**

`method` Which calculation method to use: k, l, or m

Type: string

Default: k

`k` The k value to use in the calculation

Type: constant

Default: No Default

`multiplier` The multiplier for the penalty amount

Type: constant

Default: 1

9.7.6. @additional__prior[label].type=vector_smoothing

`log_scale` Should the sums of squares be calculated on the log scale?

Type: boolean

Default: false

`multiplier` Multiply the penalty by this factor

Type: constant

Default: 1

`lower_bound` The first element to apply the penalty to in the vector

Type: non-negative integer

Default: 0u

`upper_bound` The last element to apply the penalty to in the vector

Type: non-negative integer

Default: 0u

`r` Penalty applied to r th differences
 Type: non-negative integer
 Default: 2u

9.8. Defining estimation of transformations

@estimate_transformation *label* Define an object of type *estimate_transformation*

`label` Label for the transformation block
 Type: string
 Default: No Default

`type` The type of transformation
 Type: string
 Default: No Default

`transform_with_jacobian` Apply Jacobian during transformation
 Type: boolean
 Default: true

9.8.1. @estimate__transformation[label].type=average_difference

`theta2` The label of the @estimate block relating to the θ_2 parameter in the transformation. See the User Manual for more information
 Type: string
 Default: No Default

`theta1` The label of @estimate block relating to the θ_1 parameter in the transformation. See the User Manual for more information
 Type: string
 Default: No Default

9.8.2. @estimate__transformation[label].type=inverse

`estimate_label` The label of estimate block to apply transformation. Defined as θ_1 in the documentation
 Type: string
 Default: No Default

9.8.3. @estimate__transformation[label].type=log

`estimate_label` Label of estimate block to apply transformation. Defined as θ_1 in the documentation

Type: string

Default: No Default

9.8.4. @estimate__transformation[label].type=log_sum

`theta2` The label of the @estimate block relating to the θ_2 parameter in the transformation. See the User Manual for more information

Type: string

Default: No Default

`theta1` The label of @estimate block relating to the θ_1 parameter in the transformation. See the User Manual for more information

Type: string

Default: No Default

9.8.5. @estimate__transformation[label].type=orthogonal

`theta2` The label of the @estimate block relating to the θ_2 parameter in the transformation. See the User Manual for more information

Type: string

Default: No Default

`theta1` The label of @estimate block relating to the θ_1 parameter in the transformation. See the User Manual for more information

Type: string

Default: No Default

9.8.6. @estimate__transformation[label].type=simplex

`lower_bound` The empirical lower bound for the simplex transformed. This should be -Inf but some of the minimisers do not allow that

Type: constant

Default: true

`upper_bound` The empirical upper bound for the simplex transformed. This should be Inf but some of the minimisers do not allow that

Type: constant

Default: true

9.8.7. @estimate__transformation[label].type=square_root

estimate_label The label of the estimate block to apply transformation. Defined as θ_1 in the documentation
Type: string
Default: No Default

9.8.8. @estimate__transformation[label].type=sum_to_one

estimate_labels The label for the estimates for the sum to one transformation
Type: string vector
Default: No Default

upper_bound The empirical upper bounds for the transformed parameters. There should be one less bound than parameters
Type: constant vector
Default: true

lower_bound The empirical lower bound for the transformed parameters. There should be one less bound than parameters
Type: constant vector
Default: true

10. Observation command and subcommand syntax

In the syntax sections, the sub-section headers use a notation like "**@observation[label].type=abundance**" which, in this case, represents the input command fragment

```
@observation label #where label is a generic placeholder
type=abundance
...
```

and the sub-section will describe all of its own specific sub-commands. Common sub-commands are described after the command header.

10.1. Observation types

The observation types available are:

- Observations of proportions of individuals by age class
- Observations of proportions of individuals by category and age class
- Relative and absolute abundance observations
- Relative and absolute biomass observations

Each type of observation requires a set of subcommands and arguments specific to that process.

@observation *label* Define an object of type *observation*

label The label of the observation

Type: string

Default: No Default

type The type of observation

Type: string

Default: No Default

likelihood The type of likelihood to use

Type: string

Default: No Default

categories The category labels to use

Type: string vector

Default: true

delta The robustification value ,delta, for the likelihood

Type: constant

Default: DELTA

Lower Bound: 0.0 (inclusive)

simulation_likelihood The simulation likelihood to use

Type: string

Default: ""

likelihood_multiplier The likelihood score multiplier

Type: constant

Default: 1.0

Lower Bound: 0.0 (inclusive)

error_value_multiplier The error value multiplier for likelihood

Type: constant

Default: 1.0

Lower Bound: 0.0 (inclusive)

10.1.1. @observation[label].type=abundance

time_step The label of the time step that the observation occurs in

Type: string

Default: No Default

catchability The label of the catchability coefficient ,q,

Type: string
 Default: No Default

`selectivities` The labels of the selectivities
 Type: string vector
 Default: true

`process_error` The process error
 Type: estimable
 Default: 0.0
 Lower Bound: 0.0 (inclusive)

`years` The years for which there are observations
 Type: non-negative integer vector
 Default: No Default

`obs` The observed values
 Type: string vector
 Default: No Default

`error_value` The error values of the observed values ,note that the units depend on the likelihood,
 Type: constant vector
 Default: No Default

10.1.2. `@observation[label].type=biomass`

`time_step` The label of the time step that the observation occurs in
 Type: string
 Default: No Default

`catchability` The label of the catchability coefficient ,q,
 Type: string
 Default: No Default

`selectivities` The labels of the selectivities
 Type: string vector
 Default: true

`process_error` The process error
 Type: estimable
 Default: 0.0
 Lower Bound: 0.0 (inclusive)

`years` The years of the observed values

Type: non-negative integer vector

Default: No Default

obs The observed values

Type: string vector

Default: No Default

error_value The error values of the observed values ,note that the units depend on the likelihood,

Type: constant vector

Default: No Default

age_weight_labels R,The labels for the `@age_weight` block which corresponds to each category, to use the weight calculation method for biomass calculations,

Type: string vector

Default: ""

10.1.3. `@observation[label].type=process_removals_by_age`

min_age The minimum age

Type: non-negative integer

Default: No Default

max_age The maximum age

Type: non-negative integer

Default: No Default

plus_group Is the maximum age the age plus group

Type: boolean

Default: true

time_step The label of time-step that the observation occurs in

Type: string vector

Default: No Default

tolerance The tolerance

Type: constant

Default: double

Lower Bound: 0.0 (exclusive)

Upper Bound: 1.0 (exclusive)

years The years for which there are observations

Type: non-negative integer vector

Default: No Default

`process_errors` The label of process error to use
 Type: estimable vector
 Default: true

`ageing_error` The label of the ageing error to use
 Type: string
 Default: ""

`method_of_removal` The label of the observed method of removals
 Type: string vector
 Default: ""

`mortality_instantaneous_process` The label of the mortality instantaneous process for the observation
 Type: string
 Default: No Default

10.1.4. `@observation[label].type=process_removals_by_age_retained`

`min_age` The minimum age
 Type: non-negative integer
 Default: No Default

`max_age` The maximum age
 Type: non-negative integer
 Default: No Default

`plus_group` Is the maximum age the age plus group?
 Type: boolean
 Default: true

`time_step` The label of the time step that the observation occurs in
 Type: string vector
 Default: No Default

`tolerance` The tolerance
 Type: constant
 Default: double
 Lower Bound: 0.0 (exclusive)
 Upper Bound: 1.0 (exclusive)

`years` The years for which there are observations
 Type: non-negative integer vector
 Default: No Default

`process_errors` The label of the process error to use
Type: estimable vector
Default: true

`ageing_error` The label of the ageing error to use
Type: string
Default: ""

`method_of_removal` The label of observed method of removals
Type: string vector
Default: ""

`mortality_instantaneous_process` The label of the mortality instantaneous process for the observation
Type: string
Default: No Default

10.1.5. `@observation[label].type=process_removals_by_age_retained_total`

`min_age` The minimum age
Type: non-negative integer
Default: No Default

`max_age` The maximum age
Type: non-negative integer
Default: No Default

`plus_group` Is the maximum age the age plus group?
Type: boolean
Default: true

`time_step` The label of the time step that the observation occurs in
Type: string vector
Default: No Default

`tolerance` The tolerance
Type: constant
Default: double
Lower Bound: 0.0 (exclusive)
Upper Bound: 1.0 (exclusive)

`years` The years for which there are observations
Type: non-negative integer vector
Default: No Default

`process_errors` The label of the process error to use
 Type: estimable vector
 Default: true

`ageing_error` The label of the ageing error to use
 Type: string
 Default: ""

`method_of_removal` The label of observed method of removals
 Type: string vector
 Default: ""

`mortality_instantaneous_process` The label of the mortality instantaneous process for the observation
 Type: string
 Default: No Default

10.1.6. @observation[label].type=process_removals_by_length

`time_step` The time step to execute in
 Type: string
 Default: No Default

`tolerance` The tolerance for rescaling proportions
 Type: constant
 Default: double
 Lower Bound: 0.0 (exclusive)
 Upper Bound: 1.0 (exclusive)

`years` The years for which there are observations
 Type: non-negative integer vector
 Default: No Default

`process_errors` The process error
 Type: estimable vector
 Default: true

`method_of_removal` The label of observed method of removals
 Type: string
 Default: ""

`length_bins` The length bins
 Type: constant vector
 Default: No Default

`length_plus` Is the last length bin a plus group? ,defaults to @model value,
Type: boolean
Default: model

`mortality_instantaneous_process` The label of the mortality instantaneous process for the
observation
Type: string
Default: No Default

10.1.7. @observation[label].type=process_removals_by_length_retained

`time_step` The time step to execute in
Type: string
Default: No Default

`tolerance` The tolerance for rescaling proportions
Type: constant
Default: double
Lower Bound: 0.0 (exclusive)
Upper Bound: 1.0 (exclusive)

`years` The years for which there are observations
Type: non-negative integer vector
Default: No Default

`process_errors` The process error
Type: estimable vector
Default: true

`method_of_removal` The label of observed method of removals
Type: string
Default: ""

`length_bins` The length bins
Type: constant vector
Default: No Default

`length_plus` Is the last length bin a plus group? ,defaults to @model value,
Type: boolean
Default: model

`mortality_instantaneous_process` The label of the mortality instantaneous process for the
observation
Type: string
Default: No Default

10.1.8. @observation[label].type=process_removals_by_length_retained_total

time_step The time step to execute in
Type: string
Default: No Default

tolerance The tolerance for rescaling proportions
Type: constant
Default: double
Lower Bound: 0.0 (exclusive)
Upper Bound: 1.0 (exclusive)

years The years for which there are observations
Type: non-negative integer vector
Default: No Default

process_errors The process error
Type: estimable vector
Default: true

method_of_removal The label of observed method of removals
Type: string
Default: ""

length_bins The length bins
Type: constant vector
Default: No Default

length_plus Is the last length bin a plus group? ,defaults to @model value,
Type: boolean
Default: model

mortality_instantaneous_process The label of the mortality instantaneous process for the
observation
Type: string
Default: No Default

10.1.9. @observation[label].type=proportions_at_age

min_age The minimum age
Type: non-negative integer
Default: No Default

`max_age` The maximum age
Type: non-negative integer
Default: No Default

`plus_group` Is the maximum age the age plus group?
Type: boolean
Default: true

`time_step` The label of the time step that the observation occurs in
Type: string
Default: No Default

`tolerance` The tolerance on the constraint that for each year the sum of proportions in each age must equal 1, e.g., if tolerance = 0.1 then $1 - \text{Sum,Proportions}$, can be as great as 0.1
Type: constant
Default: double
Lower Bound: 0.0 (exclusive)
Upper Bound: 1.0 (exclusive)

`years` The years of the observed values
Type: non-negative integer vector
Default: No Default

`selectivities` The labels of the selectivities
Type: string vector
Default: true

`process_errors` The process error
Type: constant vector
Default: true

`ageing_error` The label of ageing error to use
Type: string
Default: ""

10.1.10. @observation[label].type=proportions_at_length

`time_step` The label of the time step that the observation occurs in
Type: string
Default: No Default

`tolerance` The tolerance for rescaling proportions
Type: constant
Default: double
Lower Bound: 0.0 (exclusive)

`years` The years for which there are observations
Type: non-negative integer vector
Default: No Default

`selectivities` The labels of the selectivities
Type: string vector
Default: true

`process_errors` The process error
Type: constant vector
Default: true

`length_bins` The length bins
Type: constant vector
Default: true

10.1.11. `@observation[label].type=proportions_by_category`

`min_age` The minimum age
Type: non-negative integer
Default: No Default

`max_age` The maximum age
Type: non-negative integer
Default: No Default

`time_step` The label of the time step that the observation occurs in
Type: string
Default: No Default

`plus_group` Use the age plus group?
Type: boolean
Default: true

`years` The years for which there are observations
Type: non-negative integer vector
Default: No Default

`selectivities` The labels of the selectivities
Type: string vector
Default: true

`categories2` The target categories

Type: string vector
Default: No Default

`selectivities2` The target selectivities
Type: string vector
Default: No Default

10.1.12. `@observation[label].type=proportions_mature_by_age`

`min_age` The minimum age
Type: non-negative integer
Default: No Default

`max_age` The maximum age
Type: non-negative integer
Default: No Default

`time_step` The label of time-step that the observation occurs in
Type: string
Default: No Default

`plus_group` Use the age plus group?
Type: boolean
Default: true

`years` The years for which there are observations
Type: non-negative integer vector
Default: No Default

`ageing_error` The label of ageing error to use
Type: string
Default: ""

`total_categories` All category labels that were vulnerable to sampling at the time of this observation ,not including the categories already given,
Type: string vector
Default: true

`time_step_proportion` The proportion through the mortality block of the time step when the observation is evaluated
Type: constant
Default: double
Lower Bound: 0.0 (inclusive)
Upper Bound: 1.0 (inclusive)

10.1.13. @observation[label].type=proportions_migrating

min_age The minimum age

Type: non-negative integer

Default: No Default

max_age The maximum age

Type: non-negative integer

Default: No Default

time_step The label of the time step that the observation occurs in

Type: string

Default: No Default

plus_group Is the maximum age the age plus group?

Type: boolean

Default: true

years The years for which there are observations

Type: non-negative integer vector

Default: No Default

process_errors The process error

Type: constant vector

Default: true

ageing_error The label of the ageing error to use

Type: string

Default: ""

process The process label

Type: string

Default: No Default

10.1.14. @observation[label].type=tag_recapture_by_age

min_age The minimum age

Type: non-negative integer

Default: No Default

max_age The maximum age

Type: non-negative integer

Default: No Default

plus_group Is the maximum age the age plus group?

Type: boolean

Default: true

years The years for which there are observations

Type: non-negative integer vector

Default: No Default

categories2 The available categories in the partition

Type: string vector

Default: No Default

selectivities The labels of the selectivities

Type: string vector

Default: true

time_step The label of the time step that the observation occurs in

Type: string

Default: No Default

selectivities2 The categories of tagged individuals for the observation

Type: string vector

Default: No Default

detection The probability of detecting a recaptured individual

Type: constant

Default: No Default

Lower Bound: 0.0 (inclusive)

Upper Bound: 1.0 (inclusive)

time_step_proportion The proportion through the mortality block of the time step when the observation is evaluated

Type: constant

Default: double

Lower Bound: 0.0 (inclusive)

Upper Bound: 1.0 (inclusive)

10.1.15. @observation[label].type=tag_recapture_by_length

years The years for which there are observations

Type: non-negative integer vector

Default: No Default

time_step The time step to execute in

Type: string

Default: No Default

`length_bins` The length bins

Type: constant vector

Default: true

`selectivities` The labels of the selectivities used for untagged categories

Type: string vector

Default: true

`tagged_selectivities` The labels of the tag category selectivities

Type: string vector

Default: No Default

`detection` The probability of detecting a recaptured individual

Type: constant

Default: No Default

Lower Bound: 0.0 (inclusive)

Upper Bound: 1.0 (inclusive)

`dispersion` The overdispersion parameter ϕ ,

Type: constant

Default: double

Lower Bound: 0.0 (inclusive)

`time_step_proportion` The proportion through the mortality block of the time step when the observation is evaluated

Type: constant

Default: double

Lower Bound: 0.0 (inclusive)

Upper Bound: 1.0 (inclusive)

10.2. Likelihoods

@likelihood *label* Define an object of type *likelihood*

10.2.1. `@likelihood[label].type=binomial`

10.2.2. `@likelihood[label].type=binomial_approx`

10.2.3. `@likelihood[label].type=dirichlet`

10.2.4. `@likelihood[label].type=log_normal`

10.2.5. `@likelihood[label].type=log_normal_with_q`

10.2.6. `@likelihood[label].type=multinomial`

10.2.7. `@likelihood[label].type=normal`

10.2.8. `@likelihood[label].type=pseudo`

10.3. Defining ageing error

The methods for including ageing error into estimation with observations are:

- None
- Data
- Normal
- Off-by-one

Each type of ageing error requires a set of subcommands and arguments specific to its type.

@ageing_error *label* Define an object of type *ageing_error*

label The label of the ageing error

Type: string

Default: No Default

type The type of ageing error

Type: string

Default: No Default

10.3.1. `@ageing__error[label].type=data`

10.3.2. `@ageing__error[label].type=none`

10.3.3. `@ageing__error[label].type=normal`

cv CV of the misclassification matrix

Type: estimable

Default: No Default

Lower Bound: 0.0 (exclusive)

k **k** defines the minimum age of individuals which can be misclassified, i.e., individuals of age less than **k** have no ageing error
Type: non-negative integer
Default: 0u
Lower Bound: 0u (inclusive)

10.3.4. @ageing__error[label].type=off_by_one

p1 The proportion misclassified as one year younger, e.g., the proportion of age 3 individuals that were misclassified as age 2
Type: estimable
Default: No Default
Lower Bound: 0.0 (inclusive)
Upper Bound: 1.0 (inclusive)

p2 The proportion misclassified as one year older, e.g., the proportion of age 3 individuals that were misclassified as age 4
Type: estimable
Default: No Default
Lower Bound: 0.0 (inclusive)
Upper Bound: 1.0 (inclusive)

k The minimum age of animals which can be misclassified, i.e., animals of age less than **k** are assumed to be correctly classified
Type: non-negative integer
Default: 0u
Lower Bound: 0.0 (inclusive)
Upper Bound: 1.0 (inclusive)

10.4. Simulating observations

@simulate label Define an object of type *simulate*

label Label
Type: string
Default: No Default

type Type
Type: string
Default: ""

years Years to recalculate the values
Type: non-negative integer vector
Default: true

parameter Parameter to simulate

Type: string
Default: No Default

10.4.1. **@simulate[label].type=constant**

value The value to assign to the addressable
Type: constant
Default: No Default

11. Report command and subcommand syntax

11.1. Report commands and subcommands

@report *label* Define an object of type *report*

label The label for the report
Type: string
Default: No Default

type The type of report
Type: string
Default: No Default

file_name The filename for this report to be in a separate file
Type: string
Default: ""

write_mode The write mode
Type: string
Default: overwrite
Allowed Values: overwrite, append, incremental_suffix

11.1.1. **@report[label].type=addressable**

parameter The parameter to print
Type: string
Default: No Default

years The years to print the addressable for
Type: non-negative integer vector
Default: No Default

time_step The time Step label

Type: string
Default: ""

11.1.2. @report[label].type=age_length

time_step The time step label
Type: string
Default: ""

years The years for the report
Type: non-negative integer vector
Default: true

age_length The age-length label
Type: string
Default: No Default

category The category label
Type: string
Default: No Default

11.1.3. @report[label].type=ageing_error_matrix

ageing_error The ageing error label
Type: string
Default: No Default

11.1.4. @report[label].type=catchability

11.1.5. @report[label].type=category_info

11.1.6. @report[label].type=category_list

11.1.7. @report[label].type=correlation_matrix

11.1.8. @report[label].type=covariance_matrix

11.1.9. @report[label].type=derived_quantity

11.1.10. @report[label].type=equation_test

equation The equation to do a test run of
Type: string vector
Default: No Default

11.1.11. @report[label].type=estimate_summary

11.1.12. @report[label].type=estimate_value

11.1.13. @report[label].type=estimation_result

11.1.14. @report[label].type=hessian_matrix

11.1.15. @report[label].type=initialisation_partition

11.1.16. @report[label].type=initialisation_partition_mean_weight

11.1.17. @report[label].type=mcmc_covariance

11.1.18. @report[label].type=mcmc_objective

11.1.19. @report[label].type=mcmc_sample

11.1.20. @report[label].type=m_p_d

11.1.21. @report[label].type=objective_function

11.1.22. @report[label].type=observation

observation The observation label

Type: string

Default: No Default

normalised_residuals Print Normalised Residuals?

Type: boolean

Default: false

pearsons_residuals Print Pearsons Residuals?

Type: boolean

Default: false

11.1.23. @report[label].type=output_parameters

11.1.24. @report[label].type=partition

time_step The time step label

Type: string

Default: ""

years The years for the report
Type: non-negative integer vector
Default: true

11.1.25. @report[label].type=partition_biomass

time_step The time step label
Type: string
Default: ""

years The years for the report
Type: non-negative integer vector
Default: true

11.1.26. @report[label].type=partition_mean_length

time_step The time step label
Type: string
Default: ""

years The years for the report
Type: non-negative integer vector
Default: true

11.1.27. @report[label].type=partition_mean_weight

time_step The time step label
Type: string
Default: ""

years The years for the report
Type: non-negative integer vector
Default: true

11.1.28. @report[label].type=partition_year_cross_age_matrix

11.1.29. @report[label].type=process

process The process label that is reported
Type: string
Default: ""

11.1.30. **@report [label] .type=project**

project The project label that is reported
Type: string
Default: ""

11.1.31. **@report [label] .type=random_number_seed**

11.1.32. **@report [label] .type=selectivity**

selectivity The selectivity name
Type: string
Default: No Default

11.1.33. **@report [label] .type=simulated_observation**

observation The observation label
Type: string
Default: No Default

11.1.34. **@report [label] .type=standard_header**

11.1.35. **@report [label] .type=time_varying**

12. Including commands from other files

@include *file* Include an external file

file The name of the external file to include

Type: string

Default: No default

Value: A valid external file

Condition: The file name must be enclosed in double quotes

Example: @include "my_file.csl2"

Note: @include does not denote the end of the previous command block as is the case for all other commands

13. Tips for setting up Casal2 model based on an existing CASAL model

Many users of CASAL2 may be starting with a functioning CASAL model. This section focuses on transitioning from CASAL to CASAL2.

There are a range of reasons why CASAL2 will output different values when comparing model output to CASAL models. There are also reasons why values will differ that are not so obvious such as, reasons caused from using different compilers on different machines where over/underflow might occur. It is assumed that the latter reasons should be rare, and the 'overall' behaviour when it comes to estimation will be the same between CASAL and CASAL2.

Reasons why there may be different values reported between CASAL and CASAL2 include:

- Report rounding. There are settings with respect to output in CASAL that set the number of significant figures for writing to files. So if values look truncated, this might be the reason.
- Priors on parameters that are turned off with `upper_bound = lower_bound`. In both CASAL and CASAL2 the estimation of parameters can be turned off by setting the bounds equal. CASAL will evaluate the prior value and add this to the objective function. This contribution is a constant value so it will not affect parameter inference. It may however be confusing when comparing output between the two models.
- Default values. There are a lot of switches in these programs, and options like the `delta` in CASAL2 or `r` parameter in CASAL for robustifying likelihoods can cause differences.
- The order of processes. CASAL has a predefined sequence in which it executes processes within a time step (i.e., ageing, recruitment, maturation, migration, growth, natural and fishing mortality, disease mortality, tag release events, tag shedding rate, and semelparous mortality), whereas CASAL2 is completely user defined.
- Length-based processes or observations. CASAL2 has updated the cumulative normal distribution calculation (CASAL used the approximated no closed form solution) with better approximations.
- Age-based observations. CASAL2 does not have the `sum_to_one` subcommand implemented, and CASAL makes this adjustment implicitly. Check that this flag is set to 'false' in the CASAL model for a more accurate comparison.
- Tag penalties. CASAL applies a penalty to the sum of squares on total tagged fish in a 'tagging episode' from the model compared to observed number of tagged fish. CASAL2 applies a penalty on the transition rate by length. If tags are applied in a length bin that does not have individuals, e.g., a model configuration which tags 2 individuals of length l when there are no individuals in that length bin will include a penalty.

Many of the flags and options in CASAL and CASAL2 are the same or similar. The syntax section of this document (Sections 8) provides more details about the CASAL2 functionality and behaviour. Check that the programs produce the same results with a **range** of parameter values using the deterministic run command (`casal2 -r`), before doing an estimation run (`casal2 -e`).

The first outputs to check when comparing CASAL2 and CASAL versions of the same model are the stock dynamics outputs, ignoring the fits to observations. That is, check the initial age structure, the SSB and YCS values and patterns, R_0 , B_0 , etc. If these outputs differ, then the fits to the observations will likely also be different.

There are a few linkages with certain stock dynamics outputs to check to determine if processes are misspecified. Differences between the proportions in the initial age structure, assuming an equilibrium state, are due to M , natural mortality. Differences in the initial equilibrium recruitment

value, R_0 , are due to growth (@age_length or @length_weight). Many models estimate B_0 so that R_0 is a back calculation through the growth curve.

If the initial age structure is the same, next check the derived quantities such as the SSB values. Differences in these values are generally caused by how fishing and recruitment processes are specified. Check which *YCS* values are estimated or standardised, the definition and designation of selectivities, etc.

Once the stock dynamics outputs match, check the results with a few different sets of starting parameter values by using the `-i` command line option. Next, check the fits to the observation data by comparing the expected values. Assuming the observations in both models match, the differences in the objective function value come from the expected values and the likelihood configurations. This is where subcommands such as the robustification values and the default values may differ between CASAL and CASAL2.

Once the stock dynamics outputs and the fits to the observation data are the same, do an estimation run (`casal2 -e`). If CASAL and CASAL2 do not optimise to the same parameter values, then use the parameter values from CASAL and do a deterministic run with CASAL2 using the CASAL estimated parameter values (`casal2 -r -i CASAL_mpd_pars.txt`). Then check the stock dynamics outputs and the fits to the observation data and determine where the differences in the parameter estimates and outputs are.

The next question is, how close do the parameter estimates, expected values, and objective function values have to be to say that the models are equivalent? This is an ongoing topic of discussion. Previously, subjective qualitative measures have been used to decide whether the models are equivalent. A recorded comparison for the hake stock assessment can be found at Appendix B in [Horn \(2017\)](#).

14. Syntax conventions, examples and niceties

14.1. Input File Specification

The file format used for CASAL2 is based on the command block formats used in CASAL and SPM. It is a text file that contains definitions organised into blocks.

Every object specified in a configuration file is part of a block. At the top level blocks have a one-to-one relationships with components in the system.

Example:

```
@block1 label
parameter value
parameter value_1 value 2

@block2 label
parameter value
table table_name
column_1 column_2
data_1 data_2
data_3 data_4
end_table
```

Some general notes about configuration files:

- Whitespace can be used freely. Tabs and spaces are both valid.
- A block ends only at the beginning of a new block or at the end of the final configuration file.
- Configuration files can include other configuration files.
- Included files are placed in-line, so a block can be continued in a new file.
- The configuration files support in-line declarations of objects.

14.1.1. Keywords And Reserved Characters

In order to allow efficient creation of input files, the CASAL2 file format has special keywords and characters that cannot be used for labels.

@Block Definitions

Each block in the configuration file must start with the block definition character, which is the "@" character.

Example:

```
@block1 <label>
type <type>

@block2 <label>
type <type>
```

The 'type' Keyword

The 'type' keyword is used for declaring the sub-type of a defined block. Any block object that has multiple sub-types will use the `type` keyword.

Example:

```
@block1 <label>
type <sub_type>
```

```
@block2 <label>
type <sub_type>
```

(Single Line Comments)

Comments are supported in the configuration file on one line (to the end of that line) or over multiple lines. Comments on single lines start with the "#" character.

Example:

```
@block <label>
type <sub_type> # Descriptive comment
# parameter <value_1> *** This whole line is commented out
parameter <value_1> # <value_2> *** value_2 is commented out
```

/* */ (Multiple Line Comments)

Multiple line comments are supported by surrounding the comments in `/*` and `*/`

Example:

```
@block <label>
type <sub_type>
parameter <value_1>
parameter <value_1> <value_2>

/*
Do not load this process
@block <label>
type <sub_type>
parameter <value_1>
parameter <value_1> <value_2>
*/
```

{ } (Indexing Parameters)

Individual elements of a vector can be referenced using the { } syntax. For example, when estimating `ycs_values` a range or block of YCS values can be referenced.

Example:

```
@estimate YCS
parameter process[Recruitment].ycs_values{1975:2012}
type uniform
lower_bound
upper_bound
```

':' (Range Specifier)

The range specifier ":" allows specifying a range of values instead of specifying each value explicitly. Ranges can be either incremental or decremental.

Example:

```
@process my_recruitment_process
type constant_recruitment
# With the range specifier
years_to_run 1999:2009

@process my_mortality_process
type natural_mortality
# Without the range specifier
years_to_run 2000 2001 2002 2003 2004 2005 2006 2007
```

',' (List Specifier)

When a parameter supports multiple values in a single entry, the list specifier "," can be used to define multiple values as a single parameter.

Example:

```
@categories
format sex.stage
# With the list specifier
names male,female.immature,mature

@categories
format sex.stage
# Without the list specifier
names male,immature male,mature female,immature female,mature
```

'table' and 'end_table' Keyword

The table keyword `table` is used to define a tabular block of values used as a parameter. The first line following the `table` declaration must contain a list of columns to be used. The subsequent lines are rows of the table. Each row must have the same number of values as the number of columns specified. The table definition must end with the `"end_table"` keyword on its own line.

Example:

```
@block <label>
type <sub_type>
parameter <value_1>
table <table_label>
<column_label_1> <column_label_2> ... <column_label_N>
<row1_value_1> <row1_value_2> ... <row1_value_N>
<row2_value_1> <row2_value_2> ... <row2_value_N>
end_table
```

[] (in-line Declarations)

When an object takes the label of a target object as a parameter, the label can be replaced with an in-line declaration. An in-line declaration "[]" is a complete declaration of an object on one line. This feature is designed to allow simplifying the configuration definition.

Example:

```
@model
# With in-line declaration with label specified for time step
time_steps step_one=[type=iterative; processes=recruitment ageing]

@model
# With in-line declaration with default label (model.1)
time_steps [type=iterative; processes=recruitment ageing]

# Without in-line declaration
@model
time_steps step_one

@time_step step_one
processes recruitment ageing
```

Categories

The CASAL2 population representation is essentially a 2-dimensional structure. The partition is:

Categories x Ages or Lengths

Each category allows for a different range of ages or lengths and accessibility during different time periods.

Because each category can be quite complicated, the syntax for defining categories has been structured to allow for complex definitions using a simple shorthand structure.

The "format" parameter allows for defining the structure of the category labels. Using a "." (period) character between each segment allows for shorthand lookups of categories.

The "names" parameter is a list of the category names. The syntax of these names is required to match the "format" parameter so CASAL2 can organise and search on them. Using the "list specifier" and range characters this parameter can be shortened.

Example:

```
@categories
format sex.stage.tag
names male.immature.notag male.immature.2001 male.mature.notag male.mature.2001

names male.immature # Invalid: No tag information
names female # Invalid: no stage of tag information
names female.immature.notag.1 # Invalid: Additional format segment not defined

names male,female.immature,mature.notag,2001:2005 # Valid
# Without the shorthand syntax these categories would be written:
names male.immature.notag male.immature.2001 male.immature.2002 male.immature.2003 male.immature.2004
```


Specific data for a year in a category can be set up so that this category is not to be processed during specific years or in the initialisation phases. A list of years can be provided for each category to indicate in which year(s) it is to be available. These years which will override the default setting of all years in the model. Any category with the default years overridden will no longer be accessible in the initialisation phases.

Examples:

```
@model
start_year 1998
final_year 2010

@categories
format sex.stage.tag
names male,female.immature,mature.notag,2001:2005 # Valid
# Categories with the tag value "2001" are available in years 1999, 2000, 2001, 2002, 2003
# Categories with the tag value "2005" are available in years 2003, 2004, 2005, 2006, 2007
years tag=2001=1999:2003 tag=2005=2003:2007
```

14.2. More examples of shorthand syntax and use of reserved and key characters

Categories

CASAL2 allows for many user-defined categories so shorthand syntax has been added to aid in the definition of complex configuration labelling and partition structures. For example, when defining categories a comma "," can be used to shorten lists of categories.

This syntax is the long way:

```
@categories
format sex.stage
names male.immature male.mature female.immature female.mature
```

For the exact same partition structure specified in a shorter way:

```
@categories
format sex.stage
names male,female.immature,mature
```

CASAL2 requires categories in processes and observations so that the correct model dynamics can be applied to the correct elements of the partition.

An example of a process where categories are required as an input command is for ageing

```
# 1. The standard way
@ageing my_ageing
categories male.immature male.mature female.immature female.mature

# 2. The first shorthand way
@ageing my_ageing
categories male,female.immature,mature

# 3. Wild Card (all categories)
```

```
@ageing my_ageing
categories *

# 4. The second shorthand way
@ageing my_ageing
categories sex=male sex=female
```

To combine/aggregate categories together, use the "+" special character. For example, this feature can be used to specify that the total biomass of the population is made up of both males and females.

For example,

```
@observation CPUE
type biomass
catchability Fishq
time_step one
categories male+female
selectivities FishSel
likelihood lognormal
years 1992:2001
time_step_proportion 1.0
obs 1.50 1.10 0.93 1.33 1.53 0.90 0.68 0.75 0.57 1.23
error_value 0.35
```

This combination/aggregation functionality can be used to compare an observation to the total combined population:

```
@observation CPUE
type biomass
catchability Fishq
time_step one
categories *+
selectivities FishSel
likelihood lognormal
years 1992:2001
time_step_proportion 1.0
obs 1.50 1.10 0.93 1.33 1.53 0.90 0.68 0.75 0.57 1.23
error_value 0.35
```

If male and female are the only categories in a population, then this is the same syntax as the command block above it.

Shorthand syntax can be useful when applying processes to a select group of categories from the partition.

For example, to apply a spawning migration to the mature categories in the partition and the partition was defined:

```
@categories
format area.maturity.tag
names north.immature.notag,2011 north.mature.notag,2011 south.immature.notag,2011
south.mature.notag,2011
```

Then, to migrate a portion of the mature population from the southern area to the northern area:

```
@process spawn_migration
type transition_category
from format=south.mature.*
to format=north.mature.*
proportions 1.0
selectivities One
```

Parameters

CASAL2 also allows parameters that are of type vector or map to be referenced and estimated fully or partially. An example of a parameter that is type vector is `ycs_values` in a recruitment process.

For example, a recruitment block:

```
@process WestRecruitment
type recruitment_beverton_holt
r0 400000
years
ycs_values 1 1 1 1 1 1 1
ycs_years 1975:1983
# An alternative method to specify a sequence of values
# use an asterix to represent a vector of repeating integers
ycs_values 1*8
steepness 0.9
age 1
```

To estimate the last four years of the parameter `process[WestRecruitment].ycs_values` only can be specified as

```
@estimate
parameter process[WestRecruitment].ycs_values{1980:1983}
type uniform
lower_bound 0.1 0.1 0.1 0.1
upper_bound 10 10 10 10
```

Note that the first element of a vector is indexed by 1. This syntax can be applied to parameters that are of type map as well. For information on what type a parameter is see the syntax section.

An example of a parameter that is of type map is `@time_varying[label].type=constant`.

For a `@time_varying` block

```
@time_varying q_step1
type constant
parameter catchability[Fishq].q
years 1992 1993 1994 1995
value 0.2 0.2 0.2 0.2
```

For example, to estimate only one element of the map (say 1992), and force all other years to be the same as the one estimate, can be done in the `@estimate` block using `same`:

```
@estimate
parameter time_varying[q_step1].value{1992}
same time_varying[q_step1].value{1993:1995}
type uniform
lower_bound 0.1 0.1 0.1 0.1
upper_bound 10 10 10 10
```

In-line declaration

In-line declarations can help shorten models by passing @ blocks.

For example,

```
@observation chatCPUE
type biomass
catchability [q=6.52606e-005]
time_step one
categories male+female
selectivities chatFselMale chatFselFemale
likelihood lognormal
years 1992:2001
time_step_proportion 1.0
obs 1.50 1.10 0.93 1.33 1.53 0.90 0.68 0.75 0.57 1.23
error_value 0.35

@estimate
parameter catchability[chatTANbiomass.one].q
type uniform_log
lower_bound 1e-2
upper_bound 1
```

In the above code catchability is defined and estimated without explicitly creating a @catchability block.

When an in-line declaration is made, the new object will be created with the name of the creator's label.index, where index is the word "one" through "nine" if it is 1 through 9, and the number if it is 10+.

For example,

```
@mortality halfm
selectivities [type=constant; c=1]

would create
@selectivity halfm.one
```

If there are 10 categories, each with its own selectivity, the 10th selectivity is labelled

```
@selectivity halfm.10
```

14.3. Processes

Processes are special in how they can be defined. Throughout this document specifying a process has been

```
@process Recruitment
type recruitment_beverton_holt
```

However, for convenience and clarity, this block can also be specified as

```
@recruitment Recruitment
type beverton_holt
```

The difference is that the keyword `process` can be replaced with the first word of the process type. In the example above this is the `recruitment` process. This option can be used to create more succinct model configurations.

More examples:

```
@mortality Fishing_and_M
type instantaneous
```

```
@transition Migration
type category
```

14.4. An example of a simple model

This example describes a single species and area model, with recruitment, maturation, natural and fishing mortality, and an annual age increment. The population structure has ages 1 – 30⁺ with a single category.

The default CASAL2 configuration filename is `config.csl2`. In this example, `config.csl2` specifies the files to include to run the CASAL2 model from the current directory using the `!include` command.

```
!include "population.csl2"
!include "reports.csl2"
!include "observation.csl2"
!include "estimation.csl2"
```

It is recommended to separate the sections of a CASAL2 model for enhancing readability and error checking, and including the files in a version control system.

The file `population.csl2` contains the population information. The model years are from 1975 through 2012, with 3 time steps. The model is initialised over a 120 year period prior to 1975 and applies the following processes

- A Beverton-Holt recruitment process, recruiting a constant number of individuals to the first age class (i.e., $age = 1$).
- A constant mortality process representing natural mortality(M). This process is repeated in all 3 time steps, so that a proportion of M is applied in each time step.
- An ageing process, where all individuals are aged by one year, and with a plus group accumulator age class at $age = 30$.

Following initialisation, the model runs from the years 1975 to 2012 iterating through 3 time steps.

The first time step applies processes of recruitment, and $\frac{1}{2}M_1 + F + \frac{1}{2}M_1$ processes, where M_1 is the proportion of M applied in the first time step. The exploitation process (fishing) is applied in the years 1975 - 2012. Catches are defined in the catches table and attributes for each fishery, such as selectivity and time step they are implemented, are in the fisheries table in the `@process` block.

The second time step applies an age increment and the remaining natural mortality.

The third time step applies TODO.

The first 28 lines of the main section of the `population.csl2`:

```

#THE MODEL constraints
@model
start_year 1975
final_year 2012
min_age 1
max_age 30
age_plus true
base_weight_units tonnes
initialisation_phases Equilibrium_state
time_steps Sep_Feb Mar_May Jun_Aug ##
length_bins 10 20 30 40 50 60 70 80 90 100 110 120 130 140 150 160 170 180 190 200 210 220 230
            240 250

#CATEGORIES
@categories
format stock ## Single sex and area population
names HAK4
age_lengths age_size

@initialisation_phase Equilibrium_state
type derived

## Define the processes in the Annual Cycle
## This is a list of labels that correspond to a process
@time_step Sep_Feb
processes Recruitment Instantaneous_Mortality

@time_step Mar_May
processes Instantaneous_Mortality

```

To run the model to verify that the model runs without any syntax errors, use the command `casal2 -r`. Since CASAL2 reads in the default filename `config.csl2`, this filename can be overridden. For example, if the model is in file `Mymodel.txt`, then this filename would be specified using the `-c` option, `casal2 -r -c Mymodel.txt`.

To estimate the parameters defined in the file `estimation.csl2` (the catchability constant q , recruitment R_0 , and the selectivity parameters a_{50} and a_{t095}), use `casal2 -e`. The output has been redirected to file `estimate.log` using the command `casal2 -e > estimate.log`. Reports for the user-defined reports `reports.csl2` from the final iteration of the estimation are output to the file `estimate.log`, and successful convergence is printed to the screen

```

Total elapsed time: 1 second
Completed

```

The main output from the estimation run is summarised in the file `estimate.log`, and the final MPD parameter values can also be redirected as a separate report, in this case named `paramaters.out`, using the command `casal2 -e -o paramaters.out > estimate.log`.

A profile on the R_0 parameter can be run, using `casal2 -p > profile.log`. See the examples folder for the example of the output.

15. Post-processing output using R

R (<https://www.r-project.org/>) is the main application used to process and visualise output from a CASAL2 model. **R** is free and can be downloaded from <https://cran.r-project.org/>. Once you have installed **R** you can install the `casal2` **R** package from the file (`casal2_1.0.tar.gz`) which is part of the CASAL2 download.

The CASAL2 **R** package has functionality to parse CASAL2 output into a list. It also has diagnostic, plotting, and summarising functions.

There are three types of output that CASAL2 can produce, depending on the type of analysis run. These outputs are: Standard, MCMC, and Derived Quantity.

The Standard outputs are the reports that are produced in most CASAL2 run modes, with the exception of `-s` and `-m`. The Standard output can be split into two additional categories, a single parameter run (`casal2 -r`) or a multi-parameter run (`casal2 -r -i many_pars.out`), or running in projection mode (`-f 1`). The Standard outputs can be read into **R** using the `extract.mpd()` function.

The second type of output is generated when doing an MCMC analysis (`casal2 -m`), which can generate two files, `mcmc_objective.out` and `mcmc_samples.out`. The MCMC outputs can be used to summarise convergence properties or chain behaviour, and can also be used to view marginal posteriors and quantify parameter uncertainty.

The third output type is the Derived Quantity outputs, also referred to as tabular output. The Derived Quantity output can be generated after an MCMC analysis is done, to produce the marginal posteriors for derived quantities. A commonly reported derived quantity in fisheries stock assessment modelling is the time series of spawning stock biomass. To get the posterior distributions for these derived quantities use the `--tabular` flag (e.g., `casal2 -r -i mcmc_samples.out --tabular > Tabular_report.out`). This output can then be read into **R** using the `extract.tabular()` function.

CASAL2's reported output is written so that each `@report` will start with a `'*`' and end with `'*end'`. This format can be used as the basis to construct functions that read CASAL2 output to identify and read individual reports for post-processing.

The CASAL2 **R** `extract()` functions differ by how the expected output is structured and they each create a different `casal2` object. The `summary()` and `plot()` functions will generate different plots for the different `casal2` objects. Objects produced by the `extract()` function can be queried with `class(object)`.

The list of `casal2` **R** functions include:

- `extract.mpd()`, which parses the CASAL2 default output into a list
- `extract.mcmc()`, which parses the CASAL2 MCMC output into a list
- `extract.tabular()`, which parses the CASAL2 tabular output into a list
- `extract.parameters()`, which parses the CASAL2 parameter files into a list
- `generate.starting.pars()`, which reads in a file that contains the `@estimate` blocks and generates 'N' starting values to test convergence (???)
- `burn.in.tabular()`, which omits the first 'N' rows from a `casal2TAB` object
- `plot.derived_quantities()`, which plots the derived quantities
- `plot.selectivities()`, which plots the selectivities

- `plot.ycs()`, which plots the true YCS strengths
- `plot.pressure()`, which plots the fishing pressures
- `summary()`, which summarises a model run
- `extract.csl2.file()`, which reads a CASAL2 `.csl2` (configuration) file into a list
- `write.csl2.file()`, which writes a CASAL2 `.csl2` (configuration) file from (???)
- `ReadSimulatedData()`, which parses CASAL2 output from a `casal2 -s` run
- `Method.TA1.8()`, which returns a weighting factor for age or length composition data. See [Francis \(2011\)](#) for more detail.
- `apply.dataweighting.to.csl2()`, which parses a CASAL2 `.csl2` (configuration) file that contains `@observation` blocks, applies a weighting factor to an age or length composition data set, and generates a new `.csl2` file with modified effective sample size values

The required and optional arguments for these functions can be queried after loading the CASAL2 **R** library with `library(casal2)` and using the standard **R** help syntax `?` (e.g., `?param.profile()`). Many of the help files have example code and data to demonstrate function syntax.

Standard diagnostic functions and plots for model output

TODO (functionality description)

```
plot.derived_quantity()
```

When comparing model output either: different parameters for the same model structure are being compared (Situation 1), or outputs from multiple model structures are being compared (Situation 2). These functions can be useful for both comparison types.

- `plot.selectivities()`
- `plot.pressure()`
- `plot.fit()`
- `plot.ycs()`

Data weighting

An important component of fisheries stock assessment modelling is addressing data conflicts through the use of data weighting. There are a range of methods that can be used ([Francis \(2011\)](#)). The CASAL2 **R** function is `Method.TA1.8()`. An additional function `apply.dataweighting.to.csl2()` automatically applies a weighting factor to a specific age or length composition data in an `@observation` block, and generates a new `.csl2` file with modified effective sample size values.

```
library(casal2)

## read in the reported output from a "casal2 -e" run
## ensure there is a @report block for the observation of interest.
mpd <- extract.mpd(file = "estimate.log")

## calculate weighting factor from Francis method
WeightingFactor <- Method.TA1.8(model = mpd, observation_labels = "chatTANage")

## Apply the weighting factor to the block in the Observation.csl2 file
```

```
## this call generates a new file (Observation.csl2.0) with the re-weighted effective sample
  sizes
apply.dataweighting.to.csl2(weighting_factor = WeightingFactor,
                             Observation_csl2_file = "Observations.csl2",
                             Observation_label = "chatTANage",
                             Observation_out_filename = "Observation.csl2.0")
```

Automating the data weighting process:

```
library(casal2)

mpd <- extract.mpd(file = "estimate.log")

ModelFactor <- Method.TA1.8(mpd, observation_labels = c("ObserverProportionsAtAge"))

## make a back-up copy of the file Observation.csl2 before running this section

while(abs(ModelFactor - 1) > 0.01) {
  shell("betadiff & casal2 -e > estimate.log 2> log.out")

  new_mpd <- extract.mpd(file = "estimate.log")

  ModelFactor <- Method.TA1.8(new_mpd, observation_labels = c("ObserverProportionsAtAge"))

  apply.dataweighting.to.csl2(weighting_factor = ModelFactor,
                               Observation_csl2_file = "Observation.csl2",
                               Observation_out_filename = "Observation.csl2",
                               Observation_label = c("ObserverProportionsAtAge"))

  print(ModelFactor)
}
```

Troubleshooting the **casal2** R package

If you get this error when using one of the `extract()` functions

```
Read 1 item
Warning messages:
1: In scan(filename, what = "", sep = "\n", fileEncoding = fileEncoding) :
  embedded nul(s) found in input
2: In extract.mpd(file = "results.txt", fileEncoding = "") :
  File is empty, no reports found
```

You may be able to resolve this issue by using an alternative UTF format by specifying this format with the `fileEncoding` parameter

```
MyOutput <- extract.mpd(file = "Estimate.log", path = getwd(), fileEncoding = "UTF-16LE")
```

16. Troubleshooting

This section is to aid users in debugging models. If you cannot resolve an issue using these guidelines then please contact the development team. To report an issue please follow the format described in Section 16.2.1.

Most user errors should be well documented and CASAL2 should produce informative error messages. There are runtime options that users can enable to attempt to resolve or at least isolate an error or bug, including different levels of logging.

16.1. Logging

CASAL2's internal logging system can be invoked at the command line with argument `-loglevel` followed by one of these options: `trace`, `finest`, `fine`, `medium`.

An example of logging with trace level output:

- On Windows: `casal2 -r -loglevel trace > output.log 2> log.out`
- On Linux: `casal2 -r -loglevel trace > output.log 2&> log.out`

This argument will output CASAL2's reports to the file "output.log", and the "2>" or "2&>" syntax will print the error logged information to the file "log.out". You should be able to see where CASAL2 is exiting by going to the end of the "log.out" file.

The optimal level of logging will depend on what run mode you are using and the granularity of information that you would like to see. There is an ordering in the options, with `medium` being the most coarse, and `trace` being the finest level, with `fine` and `finest` in between. We suggest that if you are running CASAL2 in an iterative state such as for estimation (`casal2 -e`) or MCMC you use `medium` level. This is because the logging can print a lot of information for a single model run, so an estimation which could comprise thousands of model runs can produce very large text files with the finer logging option specified. For a single iteration run such as `casal2 -r` each of the logging options can be useful during different phases of model development.

You can see how CASAL2 creates these reports by looking in the ".cpp" files in the Observation or Processes source code subdirectories and see code such as in `Model/Model.cpp`,

```
LOG_FINE() « "Model: State change to Execute";
```

16.2. Reporting errors

If you find a bug or error in CASAL2, please submit an issue in the GitHub repository at <https://github.com/NIWAFisheriesModelling/CASAL2/issues>.

Please follow the guidelines below so that the bug or error can be reproduced. It is helpful to be as detailed and specific as possible when describing the observed behavior as well as the expected behaviour.

16.2.1. Guidelines for reporting an error with CASAL2

1. Ensure you are using the most recent version of CASAL2, as the bug or error you are having may have already been resolved.

2. Provide the version of CASAL2 you are using, e.g., "CASAL2 v2020-07-07 (rev. b86d98a)". The version is output by CASAL2 with the command `casal2 -v`.
3. Provide the operating system you are using, e.g., "IBM-PC Intel CPU with Microsoft Windows 10 Enterprise".
4. Provide a brief description of the problem, e.g., "a segmentation fault was produced".
5. If the problem is reproducible, please describe in detail the steps required to cause it, and include the CASAL2 configuration files, other input files, and any output files generated. Specify the *exact* command line arguments that were used, e.g., "Using the command `casal2 -e -q` produced a segmentation fault. The input configuration files are attached."
6. If the problem is not reproducible (it happened only once, or occasionally for no apparent reason), please describe in detail the circumstances in which it occurred and the behaviour observed, e.g., "CASAL2 crashed, but I have not been able to reproduce the issue. It seemed to be related to a local network crash but I cannot be sure."
7. If the problem produced any error messages, please give the *exact* text displayed, e.g., "segmentation fault (core dumped)".
8. Attach all relevant input and output files so that the problem can be reproduced; these files can be compressed into a single file e.g., a zip file, and uploaded to GitHub.

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21. Quick reference

@additional_prior label Define an object of type *additional_prior*

parameter The name of the parameter to generate additional prior on

label The label for the additional prior

type The type of additional prior

@additional__prior[label].type=beta

mu Beta distribution mean ,mu, parameter

sigma Beta distribution variance ,sigma, parameter

a Beta distribution lower bound of the range ,A, parameter

b Beta distribution upper bound of the range ,B, parameter

@additional__prior[label].type=element_difference

second_parameter The name of the second parameter for comparing

multiplier Multiply the penalty by this factor

@additional__prior[label].type=log_normal

mu The lognormal prior mean ,mu, parameter

cv The lognormal variance ,cv, parameter

@additional__prior[label].type=uniform_log

@additional__prior[label].type=vector_average

method Which calculation method to use: k, l, or m

k The k value to use in the calculation

multiplier The multiplier for the penalty amount

@additional__prior[label].type=vector_smoothing

log_scale Should the sums of squares be calculated on the log scale?

multiplier Multiply the penalty by this factor

lower_bound The first element to apply the penalty to in the vector

upper_bound The last element to apply the penalty to in the vector

r Penalty applied to rth differences

@ageing_error label Define an object of type *ageing_error*

label The label of the ageing error

type The type of ageing error

@ageing__error[label].type=data

@ageing__error[label].type=none

@ageing__error[label].type=normal

cv CV of the misclassification matrix

k k defines the minimum age of individuals which can be misclassified, i.e., individuals of age less than k have no ageing error

@ageing__error[label].type=off_by_one

p1 The proportion misclassified as one year younger, e.g., the proportion of age 3 individuals that were misclassified as age 2

p2 The proportion misclassified as one year older, e.g., the proportion of age 3 individuals that were misclassified as age 4

k The minimum age of animals which can be misclassified, i.e., animals of age less than k are assumed to be correctly classified

@age_length label Define an object of type *age_length*

label The label of the age length relationship

type The type of age length relationship

time_step_proportions The fraction of the year applied in each time step that is added to the age for the purposes of evaluating the length, i.e., a value of 0.5 for a time step will evaluate the length of individuals at age+0.5 in that time step

distribution The assumed distribution for the growth curve

cv_first The CV for the first age class

cv_last The CV for last age class

casal_switch If true, use the ,less accurate, equation for the cumulative normal function as was used in the legacy version of CASAL.

by_length Specifies if the linear interpolation of CVs is a linear function of mean length at age. Default is by age only

@age__length[label].type=data

external_gaps The method to use for external data gaps

internal_gaps The method to use for internal data gaps

length_weight The label from an associated length-weight block

time_step_measurements_were_made The time step label for which size-at-age data are provided

@age__length[label].type=none**@age__length[label].type=schnute**

y1 The y_1 parameter

y2 The y_2 parameter

tau1 The τ_1 parameter

tau2 The τ_2 parameter

a The a parameter

b The b parameter

length_weight The label of the associated length-weight relationship

@age__length[label].type=von_bertalanffy

linf The $L_{infinity}$ parameter

k The k parameter

t0 The t_0 parameter

length_weight The label of the associated length-weight relationship

@catchability label Define an object of type *catchability*

label Label of the catchability
type The type of catchability

@catchability[label].type=free

q The value of the catchability

@catchability[label].type=nuisance

lower_bound The upper bound for nuisance catchability

upper_bound The lower bound for nuisance catchability

q

@categories label Define an object of type *categories*

format The format that the category names use

names The names of the categories to be used in the model

years The years that individual categories will be active for. This overrides the model values

age_lengths R, The labels of age_length objects that are assigned to categories,

length_weight R, The labels of the length_weight objects that are assigned to categories,

age_weight R, The labels of the age_weight objects that are assigned to categories,

@derived_quantity label Define an object of type *derived_quantity*

label The label of the derived quantity

type The type of derived quantity

time_step The time step in which to calculate the derived quantity after

categories The list of categories to use when calculating the derived quantity

selectivities A list of one selectivity

time_step_proportion The proportion through the mortality block of the time step when calculated

time_step_proportion_method The method for interpolating for the proportion through the mortality block

values

@derived_quantity[label].type=abundance

@derived_quantity[label].type=biomass

@estimate label Define an object of type *estimate*

label The label of the estimate

type The prior type for the estimate

parameter The name of the parameter to estimate in the model

lower_bound The lower bound for the parameter

upper_bound The upper bound for the parameter

same List of parameters that are constrained to have the same value as this parameter

estimation_phase The first estimation phase to allow this to be estimated

mcmc Indicates if this parameter is estimated at the point estimate but fixed during MCMC estimation run

transformation Type of simple transformation to apply to estimate

transform_with_jacobian Apply jacobian during transformation

prior_applies_to_transform Does the prior apply to the transformed parameter? a legacy switch, see Manual for more information

@estimate[label].type=beta

mu Beta prior mean ,mu, parameter
sigma Beta prior variance ,sigma, parameter
a Beta prior lower bound of the range ,A, parameter
b Beta prior upper bound of the range ,B, parameter

@estimate[label].type=lognormal

mu The lognormal prior mean ,mu, parameter
cv The lognormal variance ,cv, parameter

@estimate[label].type=normal

mu The normal prior mean ,mu, parameter
cv The normal variance ,standard deviation, parameter

@estimate[label].type=normal_by_stdev

mu The normal prior mean ,mu, parameter
sigma The normal variance ,sigma, parameter
lognormal_transfomration Add a Jacobian if the derived outcome of the estimate is assumed to be lognormal, e.g., used for recruitment deviations in the recruitment process. See the User Manual for more information

@estimate[label].type=normal_log

mu The normal-log prior mean ,mu, parameter
sigma The normal-log prior variance ,standard deviation, parameter

@estimate[label].type=uniform**@estimate[label].type=uniform_log**

@estimate_transformation label Define an object of type *estimate_transformation*

label Label for the transformation block
type The type of transformation
transform_with_jacobian Apply Jacobian during transformation

@estimate__transformation[label].type=average_difference

theta2 The label of the @estimate block relating to the θ_2 parameter in the transformation. See the User Manual for more information
theta1 The label of @estimate block relating to the θ_1 parameter in the transformation. See the User Manual for more information

@estimate__transformation[label].type=inverse

estimate_label The label of estimate block to apply transformation. Defined as θ_1 in the documentation

@estimate__transformation[label].type=log

`estimate_label` Label of estimate block to apply transformation. Defined as θ_1 in the documentation

`@estimate__transformation[label].type=log_sum`

`theta2` The label of the @estimate block relating to the θ_2 parameter in the transformation. See the User Manual for more information

`theta1` The label of @estimate block relating to the θ_1 parameter in the transformation. See the User Manual for more information

`@estimate__transformation[label].type=orthogonal`

`theta2` The label of the @estimate block relating to the θ_2 parameter in the transformation. See the User Manual for more information

`theta1` The label of @estimate block relating to the θ_1 parameter in the transformation. See the User Manual for more information

`@estimate__transformation[label].type=simplex`

`lower_bound` The empirical lower bound for the simplex transformed. This should be -Inf but some of the minimisers do not allow that

`upper_bound` The empirical upper bound for the simplex transformed. This should be Inf but some of the minimisers do not allow that

`@estimate__transformation[label].type=square_root`

`estimate_label` The label of the estimate block to apply transformation. Defined as θ_1 in the documentation

`@estimate__transformation[label].type=sum_to_one`

`estimate_labels` The label for the estimates for the sum to one transformation

`upper_bound` The empirical upper bounds for the transformed parameters. There should be one less bound than parameters

`lower_bound` The empirical lower bound for the transformed parameters. There should be one less bound than parameters

`@initialisation_phase label` Define an object of type *initialisation_phase*

`label` The label of the initialisation phase

`type` The type of initialisation

`@initialisation__phase[label].type=cinitial`

`categories` The list of categories for the Cinitial initialisation

`@initialisation__phase[label].type=derived`

`insert_processes` Additional processes not defined in the annual cycle that are to be inserted into this initialisation phase

`exclude_processes` Processes in the annual cycle to be excluded from this initialisation phase

`casal_initialisation_switch` Run an extra annual cycle to evaluate equilibrium SSBs. Warning - if true, this may not correctly evaluate the equilibrium state. Set to true if replicating a

CASAL model

@initialisation__phase[label].type=iterative

years The number of iterations ,years, over which to execute this initialisation phase
insert_processes The processes in the annual cycle to be included in this initialisation phase
exclude_processes The processes in the annual cycle to be excluded from this initialisation phase
convergence_years The iteration ,year, when the test for convergence ,lambda, is evaluated
lambda The maximum value of the absolute sum of differences ,lambda, between the partition at year-1 and year that indicates successful convergence

@initialisation__phase[label].type=state_category_by_age

categories The list of categories for the category state initialisation
min_age The minimum age of values supplied in the definition of the category state
max_age The maximum age of values supplied in the definition of the category state
@length_weight label Define an object of type *length_weight*
label The label of the length-weight relationship
type The type of the length-weight relationship

@length_weight[label].type=basic

a The a parameter , $W = aL^b$,
b The b parameter , $W = aL^b$,
units The units of measure ,tonnes, kgs, grams,

@length_weight[label].type=none

@likelihood label Define an object of type *likelihood*

@likelihood[label].type=binomial

@likelihood[label].type=binomial_approx

@likelihood[label].type=dirichlet

@likelihood[label].type=log_normal

@likelihood[label].type=log_normal_with_q

@likelihood[label].type=multinomial

@likelihood[label].type=normal

@likelihood[label].type=pseudo

@mcmc label Define an object of type *mcmc*

label The label of the MCMC

type The type of MCMC

length The number of iterations in for the MCMC chain

active Indicates if this is the active MCMC algorithm

step_size Initial stepsize ,as a multiplier of the approximate covariance matrix,

@mcmc[label].type=independence_metropolis

start The covariance multiplier for the starting point of the MCMC
keep The spacing between recorded values in the MCMC
max_correlation The maximum absolute correlation in the covariance matrix of the proposal distribution
covariance_adjustment_method The method for adjusting small variances in the covariance proposal matrix
correlation_adjustment_diff The minimum non-zero variance times the range of the bounds in the covariance matrix of the proposal distribution
proposal_distribution The shape of the proposal distribution ,either the t or the normal distribution,
df The degrees of freedom of the multivariate t proposal distribution
adapt_stepsize_at The iteration numbers in which to check and resize the MCMC stepsize
adapt_covariance_matrix_at The iteration numbers in which to check and resize the MCMC stepsize
adapt_stepsize_method The method to use to adapt the step size
@minimiser label Define an object of type *minimiser*
label The minimiser label
type The type of minimiser to use
active Indicates if this minimiser is active
covariance Indicates if a covariance matrix should be generated

@minimiser[label].type=adolc

iterations The maximum number of iterations
evaluations The maximum number of evaluations
tolerance The tolerance of the gradient for convergence
step_size The minimum step size before minimisation fails

@minimiser[label].type=betadiff

iterations The maximum number of iterations
evaluations The maximum number of evaluations
tolerance The tolerance of the gradient for convergence

@minimiser[label].type=cppad

retape Retape?
print_level The level of debug to stdout
sb String buffer output?
pidi Print iteration diagnostic information?
max_iter The maximum number of iterations
tol The tolerance for convergence
acceptable_tol The acceptable tolerance
acceptable_obj_change_tol
derivative_test How to test for derivatives
point_perturbation_radius The point perturbation radius

@minimiser[label].type=de_solver

population_size The number of candidate solutions to have in the population

`crossover_probability` The minimiser's crossover probability
`difference_scale` The scale to apply to new solutions when comparing candidates
`max_generations` The maximum number of iterations to run
`tolerance` The total variance between the population and best candidate before acceptance
`method` The type of candidate generation method to use

@minimiser[label].type=d_lib

`minimisation_type` The type of minimisation to use
`search_strategy` The type of search strategy to use
`tolerance` The tolerance of the gradient for convergence
`lbfgs_max_size` The maximum size for the LBFGS search strategy
`bobyqa_interpolation_points` BOBYQA interpolation points
`bobyqa_initial_trust_radius` BOBYQA initial trust radius
`bobyqa_stopping_trust_radius` BOBYQA stopping trust radius
`bobyqa_max_evaluations` BOBYQA max objective evaluations
`verbose` Print debug of objective function calls?

@minimiser[label].type=numerical_differences

`iterations` The maximum number of iterations
`evaluations` The maximum number of evaluations
`tolerance` The tolerance of the gradient for convergence
`step_size` The minimum step size before minimisation fails

@model label Define an object of type *model*

`start_year` The first year of the model, immediately following initialisation
`final_year` The final year of the model, excluding years in the projection period
`min_age` The minimum age of individuals in the population
`max_age` The maximum age of individuals in the population
`age_plus` The oldest age or extra length midpoint ,plus group size, as a plus group
`initialisation_phases` The labels of the phases of the initialisation
`time_steps` The labels of the time steps, in the order that they are applied, to form the annual cycle
`projection_final_year` The final year of the model in projection mode
`type` The type of model ,the partition structure,: age, length, or hybrid
`length_bins` The minimum length in each length bin
`length_plus` Is there a length plus group or not?
`length_plus_group` The mean length of length plus group
`base_weight_units` The units for the base weight. This will be the default unit of any weight
input parameters

@observation label Define an object of type *observation*

`label` The label of the observation
`type` The type of observation
`likelihood` The type of likelihood to use
`categories` The category labels to use
`delta` The robustification value ,delta, for the likelihood
`simulation_likelihood` The simulation likelihood to use
`likelihood_multiplier` The likelihood score multiplier
`error_value_multiplier` The error value multiplier for likelihood

@observation[label].type=abundance

time_step The label of the time step that the observation occurs in
catchability The label of the catchability coefficient ,q,
selectivities The labels of the selectivities
process_error The process error
years The years for which there are observations
obs The observed values
error_value The error values of the observed values ,note that the units depend on the likelihood,

@observation[label].type=biomass

time_step The label of the time step that the observation occurs in
catchability The label of the catchability coefficient ,q,
selectivities The labels of the selectivities
process_error The process error
years The years of the observed values
obs The observed values
error_value The error values of the observed values ,note that the units depend on the likelihood,
age_weight_labels R,The labels for the @age_weight block which corresponds to each category, to use the weight calculation method for biomass calculations,

@observation[label].type=process_removals_by_age

min_age The minimum age
max_age The maximum age
plus_group Is the maximum age the age plus group
time_step The label of time-step that the observation occurs in
tolerance The tolerance
years The years for which there are observations
process_errors The label of process error to use
ageing_error The label of the ageing error to use
method_of_removal The label of the observed method of removals
mortality_instantaneous_process The label of the mortality instantaneous process for the observation

@observation[label].type=process_removals_by_age_retained

min_age The minimum age
max_age The maximum age
plus_group Is the maximum age the age plus group?
time_step The label of the time step that the observation occurs in
tolerance The tolerance
years The years for which there are observations
process_errors The label of the process error to use
ageing_error The label of the ageing error to use
method_of_removal The label of observed method of removals
mortality_instantaneous_process The label of the mortality instantaneous process for the

observation

@observation[label].type=process_removals_by_age_retained_total

min_age The minimum age
max_age The maximum age
plus_group Is the maximum age the age plus group?
time_step The label of the time step that the observation occurs in
tolerance The tolerance
years The years for which there are observations
process_errors The label of the process error to use
ageing_error The label of the ageing error to use
method_of_removal The label of observed method of removals
mortality_instantaneous_process The label of the mortality instantaneous process for the observation

@observation[label].type=process_removals_by_length

time_step The time step to execute in
tolerance The tolerance for rescaling proportions
years The years for which there are observations
process_errors The process error
method_of_removal The label of observed method of removals
length_bins The length bins
length_plus Is the last length bin a plus group? ,defaults to @model value,
mortality_instantaneous_process The label of the mortality instantaneous process for the observation

@observation[label].type=process_removals_by_length_retained

time_step The time step to execute in
tolerance The tolerance for rescaling proportions
years The years for which there are observations
process_errors The process error
method_of_removal The label of observed method of removals
length_bins The length bins
length_plus Is the last length bin a plus group? ,defaults to @model value,
mortality_instantaneous_process The label of the mortality instantaneous process for the observation

@observation[label].type=process_removals_by_length_retained_total

time_step The time step to execute in
tolerance The tolerance for rescaling proportions
years The years for which there are observations
process_errors The process error
method_of_removal The label of observed method of removals
length_bins The length bins
length_plus Is the last length bin a plus group? ,defaults to @model value,
mortality_instantaneous_process The label of the mortality instantaneous process for the observation

@observation[label].type=proportions_at_age

min_age The minimum age
max_age The maximum age
plus_group Is the maximum age the age plus group?
time_step The label of the time step that the observation occurs in
tolerance The tolerance on the constraint that for each year the sum of proportions in each age must equal 1, e.g., if tolerance = 0.1 then 1 - Sum,Proportions, can be as great as 0.1
years The years of the observed values
selectivities The labels of the selectivities
process_errors The process error
ageing_error The label of ageing error to use

@observation[label].type=proportions_at_length

time_step The label of the time step that the observation occurs in
tolerance The tolerance for rescaling proportions
years The years for which there are observations
selectivities The labels of the selectivities
process_errors The process error
length_bins The length bins

@observation[label].type=proportions_by_category

min_age The minimum age
max_age The maximum age
time_step The label of the time step that the observation occurs in
plus_group Use the age plus group?
years The years for which there are observations
selectivities The labels of the selectivities
categories2 The target categories
selectivities2 The target selectivities

@observation[label].type=proportions_mature_by_age

min_age The minimum age
max_age The maximum age
time_step The label of time-step that the observation occurs in
plus_group Use the age plus group?
years The years for which there are observations
ageing_error The label of ageing error to use
total_categories All category labels that were vulnerable to sampling at the time of this observation ,not including the categories already given,
time_step_proportion The proportion through the mortality block of the time step when the observation is evaluated

@observation[label].type=proportions_migrating

min_age The minimum age

max_age The maximum age
time_step The label of the time step that the observation occurs in
plus_group Is the maximum age the age plus group?
years The years for which there are observations
process_errors The process error
ageing_error The label of the ageing error to use
process The process label

@observation[label].type=tag_recapture_by_age

min_age The minimum age
max_age The maximum age
plus_group Is the maximum age the age plus group?
years The years for which there are observations
categories2 The available categories in the partition
selectivities The labels of the selectivities
time_step The label of the time step that the observation occurs in
selectivities2 The categories of tagged individuals for the observation
detection The probability of detecting a recaptured individual
time_step_proportion The proportion through the mortality block of the time step when the observation is evaluated

@observation[label].type=tag_recapture_by_length

years The years for which there are observations
time_step The time step to execute in
length_bins The length bins
selectivities The labels of the selectivities used for untagged categories
tagged_selectivities The labels of the tag category selectivities
detection The probability of detecting a recaptured individual
dispersion The overdispersion parameter ϕ ,
time_step_proportion The proportion through the mortality block of the time step when the observation is evaluated

@penalty label Define an object of type *penalty*

label The label of the penalty
type The type of penalty

@penalty[label].type=process

multiplier The penalty multiplier
log_scale Indicates if the sums of squares is calculated on the log scale

@process label Define an object of type *process*

label The label of the process
type The type of process

@process[label].type=ageing

categories The labels of the categories

@process[label].type=growth_basic

categories The labels of the categories
number_of_growth_episodes The number of growth episodes per year
growth_time_steps The time step in which each growth episode occurs
cv The CV for the growth model
sigma_min The lower bound on sigma for the growth model

@process[label].type=maturation

from The list of categories to mature from
to The list of categories to mature to
selectivities The list of selectivities to use for maturation
years The years to be associated with the maturity rates
rates The rates to mature for each year

@process[label].type=mortality_constant_rate

categories The list of categories labels
m The mortality rates
time_step_ratio The time step ratios for the mortality rates

@process[label].type=mortality_event

categories The categories
years The years in which to apply the mortality process
catches The number of removals ,catches, to apply for each year
u_max The maximum exploitation rate , U_{max} ,
selectivities The list of selectivities
penalty The label of the penalty to apply if the total number of removals cannot be taken

@process[label].type=mortality_event_biomass

categories The category labels
selectivities The labels of the selectivities for each of the categories
years The years in which to apply the mortality process
catches The biomass of removals ,catches, to apply for each year
u_max The maximum exploitation rate , U_{max} ,
penalty The label of the penalty to apply if the total biomass of removals cannot be taken

@process[label].type=mortality_holling_rate

prey_categories The prey categories labels
predator_categories The predator categories labels
is_abundance Is vulnerable amount of prey and predator an abundance [true] or biomass [false]
a Parameter a
b Parameter b
x This parameter controls the functional form: Holling function type 2 , $x=2$, or 3 , $x=3$, or

generalised ,Michaelis Menten, $x=1$,
u_max The maximum exploitation rate , U_{max} ,
prey_selectivities The selectivities for prey categories
predator_selectivities The selectivities for predator categories
penalty The label of penalty
years The years in which to apply the mortality process

@process[label].type=mortality_initialisation_event

categories The categories
catch The number of removals ,catches, to apply for each year
u_max The maximum exploitation rate , U_{max} ,
selectivities The list of selectivities
penalty The label of the penalty to apply if the total number of removals cannot be taken

@process[label].type=mortality_initialisation_event_biomass

categories The categories
catch The number of removals ,catches, to apply for each year
u_max The maximum exploitation rate , U_{max} ,
selectivities The list of selectivities
penalty The label of the penalty to apply if the total number of removals cannot be taken

@process[label].type=mortality_instantaneous

categories The categories for instantaneous mortality
m The natural mortality rates for each category
time_step_ratio The time step ratios for natural mortality
selectivities The selectivities to apply on the categories for natural mortality

@process[label].type=mortality_instantaneous_retained

categories The categories for instantaneous mortality
m The natural mortality rates for each category
time_step_ratio The time step ratios for natural mortality
selectivities The selectivities to apply on the categories for natural mortality

@process[label].type=mortality_pre_suitability

prey_categories The prey categories labels
predator_categories The predator categories labels
consumption_rate The predator consumption rate
electivities The prey electivities
u_max U_{max}
prey_selectivities The selectivities for prey categories
predator_selectivities The selectivities for predator categories
penalty The label of the penalty
years The year that process occurs

@process[label].type=recruitment_beverton_holt

categories The category labels
r0 **R0**
b0 **B0**
proportions The proportion for each category
age The age at recruitment
ssb_offset The spawning biomass year offset
steepness Steepness ,h,
ssb The SSB label ,derived quantity,
b0_initialisation_phase The initialisation phase label that B0 is from
yces_values The YCS values
yces_years The recruitment years. A vector of years that relates to the year of the spawning event that created this cohort
standardise_yces_years The years that are included for year class standardisation

@process[label].type=recruitment_beverton_holt_with_deviations

categories The category labels
r0 **R0**
b0 **B0**
proportions The proportion for each category
age The age at recruitment
ssb_offset The spawning biomass year offset
steepness Steepness ,h,
ssb The SSB Label ,derived quantity,
sigma_r sigma R
b_max The maximum bias adjustment
last_year_with_no_bias The last year with no bias adjustment
first_year_with_bias The first year with full bias adjustment
last_year_with_bias The last year with full bias adjustment
first_recent_year_with_no_bias The first recent year with no bias adjustment
b0_initialisation_phase The initialisation phase label that B0 is from
deviation_values The recruitment deviation values
deviation_years The recruitment years. A vector of years that relates to the year of the spawning event that created this cohort

@process[label].type=recruitment_constant

categories The categories
proportions The proportions
length_bins The length bins that recruits are uniformly distributed over at the time of recruitment
r0 **R0**

@process[label].type=survival_constant_rate

categories The list of categories
s The survival rates
time_step_ratio The time step ratios for S
selectivities The selectivity label

@process[label].type=tag_by_age

from The categories to transition from
to The categories to transition to
min_age The minimum age to transition
max_age The maximum age to transition
penalty The penalty label
u_max U Max
years The years to execute the transition in
initial_mortality The initial mortality value
initial_mortality_selectivity The initial mortality selectivity label
loss_rate The loss rate
loss_rate_selectivities The loss rate selectivity label
selectivities The selectivity labels
n N

@process[label].type=tag_by_length

from The categories to transition from
to The categories to transition to
penalty The penalty label
u_max U Max
initial_mortality
initial_mortality_selectivity
selectivities
n

@process[label].type=tag_loss

categories The list of categories
tag_loss_rate The tag loss rates
time_step_ratio The time step ratios for tag loss
tag_loss_type The type of tag loss
selectivities The selectivities
year The year the first tagging release process was executed

@process[label].type=transition_category

from The from category
to The to category
proportions The proportions
selectivities The selectivity names

@process[label].type=transition_category_by_age

from The categories to transition from

to The categories to transition to
 min_age The minimum age to transition
 max_age The maximum age to transition
 penalty The penalty label
 u_max U max
 years The years to execute the transition in
@profile *label* Define an object of type *profile*
 label The label of the profile
 steps The number of steps between the lower and upper bound
 lower_bound The lower bounds
 upper_bound The upper bounds
 parameter The system parameter to profile
 same A parameter that is constrained to have the same value as the parameter being profiled
@project *label* Define an object of type *project*
 label Label
 type Type
 years Years to recalculate the values
 parameter Parameter to project
 multiplier Multiplier that is applied to the projected value

@project [label] .type=constant

values The values to assign to the addressable

@project [label] .type=empirical_sampling

start_year The start year of sampling
 final_year The final year of sampling

@project [label] .type=log_normal

mean The mean of the lognormal process
 sigma The standard deviation ,sigma, of the lognormal process

@project [label] .type=log_normal_empirical

mean The mean of gaussian process
 start_year The start year of sampling
 final_year The final year of sampling

@project [label] .type=user_defined

equation The equation to do a test run of
@report *label* Define an object of type *report*
 label The label for the report
 type The type of report
 file_name The filename for this report to be in a separate file
 write_mode The write mode

@report[label].type=addressable

parameter The parameter to print
years The years to print the addressable for
time_step The time Step label

@report[label].type=age_length

time_step The time step label
years The years for the report
age_length The age-length label
category The category label

@report[label].type=ageing_error_matrix

ageing_error The ageing error label

@report[label].type=catchability**@report[label].type=category_info****@report[label].type=category_list****@report[label].type=correlation_matrix****@report[label].type=covariance_matrix****@report[label].type=derived_quantity****@report[label].type=equation_test**

equation The equation to do a test run of

@report[label].type=estimate_summary**@report[label].type=estimate_value****@report[label].type=estimation_result****@report[label].type=hessian_matrix****@report[label].type=initialisation_partition****@report[label].type=initialisation_partition_mean_weight****@report[label].type=mcmc_covariance****@report[label].type=mcmc_objective****@report[label].type=mcmc_sample****@report[label].type=m_p_d****@report[label].type=objective_function****@report[label].type=observation**

observation The observation label
normalised_residuals Print Normalised Residuals?
pearsons_residuals Print Pearsons Residuals?

@report[label].type=output_parameters

@report[label].type=partition

time_step The time step label

years The years for the report

@report[label].type=partition_biomass

time_step The time step label

years The years for the report

@report[label].type=partition_mean_length

time_step The time step label

years The years for the report

@report[label].type=partition_mean_weight

time_step The time step label

years The years for the report

@report[label].type=partition_year_cross_age_matrix

@report[label].type=process

process The process label that is reported

@report[label].type=project

project The project label that is reported

@report[label].type=random_number_seed

@report[label].type=selectivity

selectivity The selectivity name

@report[label].type=simulated_observation

observation The observation label

@report[label].type=standard_header

@report[label].type=time_varying

@selectivity label Define an object of type *selectivity*

label The label for this selectivity

type The type of selectivity

length_based Is the selectivity length based?

intervals The number of quantiles to evaluate a length-based selectivity over the age-length distribution

partition_type The type of partition that this selectivity will support. Defaults to the same as

the model
values
length_values

@selectivity[label].type=all_values

v The v parameter

@selectivity[label].type=all_values_bounded

l The low value ,L,
h The high value ,H,
v The v parameter

@selectivity[label].type=constant

c The constant value

@selectivity[label].type=double_exponential

x0 The X0 parameter
x1 The X1 parameter
x2 The X2 parameter
y0 The Y0 parameter
y1 The Y1 parameter
y2 The Y2 parameter
alpha alpha

@selectivity[label].type=double_normal

mu The mean ,mu,
sigma_l The sigma L parameter
sigma_r The sigma R parameter
alpha alpha

@selectivity[label].type=increasing

l The low value ,L,
h The high value ,H,
v The v parameter
alpha alpha

@selectivity[label].type=inverse_logistic

a50 a50
ato95 ato95
alpha alpha

@selectivity[label].type=knife_edge

e The edge value
alpha alpha

@selectivity[label].type=logistic

a50 a50
ato95 ato95
alpha alpha

@selectivity[label].type=logistic_producing

l The low value ,L,
h The high value ,H,
a50 a50
ato95 ato95
alpha alpha
@simulate label Define an object of type *simulate*

label Label
type Type
years Years to recalculate the values
parameter Parameter to simulate

@simulate[label].type=constant

value The value to assign to the addressable
@time_step label Define an object of type *time_step*

label The label of the timestep
processes The labels of the processes for this time step in the order that they occur
@time_varying label Define an object of type *time_varying*

label The time-varying label
type The time-varying type
years The years in which to vary the values
parameter The name of the parameter to time vary

@time__varying[label].type=annual_shift

values The values
a Parameter A
b Parmeter B
c Parameter C
scaling_years The scaling years

@time__varying[label].type=constant

values The value to assign to addressable

@time__varying[label].type=exogenous

a The shift parameter
exogeneous_variable The values of exogeneous variable for each year

@time__varying[label].type=linear

slope The slope of the linear trend ,additive unit per year,
intercept The intercept of the linear trend value for the first year

@time__varying[label].type=random_draw

mean The mean ,mu,
sigma The standard deviation ,sigma,
distribution The distribution

@time__varying[label].type=random_walk

mean The mean ,mu,
sigma The standard deviation ,sigma,
upper_bound The upper bound for the random walk
lower_bound The lower bound for the random walk
rho The autocorrelation parameter ,rho,
distribution The distribution

Appendices

A. Investigating two options for YCS prior distribution formulations

There are two common ways of parameterising the lognormal prior distribution of year class strength (YCS) when fitting models.

Let YCS_y represent the YCS for year y . The two parameterisations used are:

1. $YCS_y \sim LN(\mu, \sigma_R^2)$, with μ chosen so that $E(YCS_y) = 1$.
2. $YCS_y = e^{\varepsilon_y - \frac{1}{2}\sigma_R^2}$, where $\varepsilon_y \sim N(0, \sigma_R^2)$.

To check whether the two representations are equivalent, we will determine, in each case the density function of YCS_y on the log-scale.

Note that, in general, if $Y \sim LN(\mu, \sigma_R^2)$ (i.e., random variable Y has a lognormal distribution with parameters μ and σ_R^2), then the expectation, $E(Y)$, and variance, $Var(Y)$, of Y are given by

$$E(Y) = e^{\mu + \frac{1}{2}\sigma_R^2},$$

and

$$Var(Y) = \left[e^{\sigma_R^2} - 1 \right] e^{2\mu + \sigma_R^2}.$$

The lognormal distribution can be expressed on the log scale:

$$\log Y \sim \text{Normal}(\mu, \sigma_R^2).$$

Option 1: $YCS_y \sim LN(\mu, \sigma_R^2)$, with $E(YCS_y) = 1$

Setting $E(YCS_y) = 1$ implies

$$\begin{aligned} e^{\mu + \frac{1}{2}\sigma_R^2} &= 1 \\ \Rightarrow \mu + \frac{1}{2}\sigma_R^2 &= \log 1 \\ \Rightarrow \mu &= -\frac{1}{2}\sigma_R^2 \end{aligned} \tag{A.1}$$

and

$$\begin{aligned} Var(YCS_y) &= \left[e^{\sigma_R^2} - 1 \right] e^{2\mu + \sigma_R^2} \\ &= \left[e^{\sigma_R^2} - 1 \right] e^{2(-\frac{1}{2}\sigma_R^2) + \sigma_R^2} \\ &= \left[e^{\sigma_R^2} - 1 \right] e^0 \\ &= e^{\sigma_R^2} - 1. \end{aligned} \tag{A.2}$$

So, on the log scale:

$$\log YCS_y \sim N\left(-\frac{1}{2}\sigma_R^2, \sigma_R^2\right).$$

Option 2: $YCS_y = e^{\varepsilon_y - \frac{1}{2}\sigma_R^2}$, where $\varepsilon_y \sim N(0, \sigma_R^2)$

In this case, $YCS_y = e^{\varepsilon_y - \frac{1}{2}\sigma_R^2}$ implies

$$\log YCS_y = \varepsilon_y - \frac{1}{2}\sigma_R^2$$

and

$$E(\log YCS_y) = E\left(\varepsilon_y - \frac{1}{2}\sigma_R^2\right) = -\frac{1}{2}\sigma_R^2,$$

since $E(\varepsilon_y) = 0$.

Also:

$$\begin{aligned} \text{Var}(\log(YCS_y)) &= \text{Var}\left(\varepsilon_y - \frac{1}{2}\sigma_R^2\right) \\ &= \text{Var}(\varepsilon_y) \\ &= \sigma_R^2 \end{aligned} \tag{A.3}$$

Therefore

$$\log YCS_y \sim N\left(-\frac{1}{2}\sigma_R^2, \sigma_R^2\right).$$

Therefore, the two parameterisations result in exactly the same distribution for YCS_y values and should give the same results **if expressed correctly** in MCMC algorithms.

To illustrate that these two distributions are exactly the same, we first use simulations to show that we get the same YCS_y values when generating sequences from these two formulations. One is generated directly from the lognormal distribution, while the other is obtained by transforming a normal random variable.

Investigating prior specification

Given the two different representations, the question is, how should their prior distribution contributions to the negative log posterior be specified?

Prior based on Option 1

For Option 1, this is straight-forward. The YCS s are generated from a lognormal distribution, so the contribution to the log posterior is based on the lognormal density function. That is, if we let $Y = YCS_y$, then the density function of Y is given by

$$f(y) = \frac{1}{y\sigma_R\sqrt{2\pi}} e^{-\frac{1}{2\sigma_R^2}(\log y - \mu)^2}.$$

Since $\mu = -\frac{1}{2}\sigma_R^2$ as shown in Equation A.1, we have

$$-\log f(y) = \log y + \log \sigma_R + \frac{1}{2} \log 2\pi + \frac{1}{2\sigma_R^2} \left(\log y - \left(-\frac{1}{2}\sigma_R^2\right) \right)^2. \quad (\text{A.4})$$

Prior based on Option 2

For Option 2, we will look at two ways used to specify the prior and say which one is correct.

Prior 2 - Normal distribution for ϵ_y

In this approach, we have

$$YCS_y = e^{\epsilon_y - \frac{1}{2}\sigma_R^2}, \text{ where } \epsilon_y \sim N(0, \sigma_R^2).$$

What is sometimes done is to then express the contribution to the negative log posterior using $-\log f(\epsilon_y)$, where

$$f(\epsilon_y) = \frac{1}{\sigma_R\sqrt{2\pi}} e^{-\frac{1}{2\sigma_R^2}\epsilon_y^2},$$

and therefore

$$-\log f(\epsilon_y) = \log \sigma_R + \frac{1}{2} \log 2\pi + \frac{1}{2\sigma_R^2}\epsilon_y^2. \quad (\text{A.5})$$

However, this contribution is based on the density function for ϵ_y and not for Y . Such an approach is incorrect. The two contributions are different as seen in Equations A.4 and A.5, and as shown below.

So what does this mean in practice?

The overall model is based on YCS_y , rather than ϵ_y . Using a negative log posterior based on $f(\epsilon_y)$ gives incorrect weights to the YCS_y values in the model, meaning that in MCMC steps, acceptance probabilities will be incorrect. When using the specification based on ϵ_y , the correct approach is to use variable transformation methods to obtain probability densities for the YCS_y values. These density values based on $f(Y)$ are the ones to use in the negative log posterior.

Prior 3 - Variable transformation to obtain $f(Y)$ based on $f(\epsilon_y)$

Given $Y = e^{\epsilon_y - \frac{1}{2}\sigma_R^2}$, where $\epsilon_y \sim N(0, \sigma_R^2)$, we need to find $g(y)$, the distribution of the transformed variable YCS_y .

Variable transformation theory tells us that:

$$g(y) = f(s(y)) \left| \frac{ds(y)}{dy} \right|,$$

where $s(y) = \epsilon_y(y)$ is the result of the conversion from Y to ϵ_y , and $\left| \frac{ds(y)}{dy} \right|$ is the Jacobian of the transformation.

We find $s(y)$ by expressing ϵ_y as a function of y :

$$\begin{aligned} y &= e^{\epsilon_y - \frac{1}{2}\sigma_R^2} \\ \Rightarrow \log y &= \epsilon_y - \frac{1}{2}\sigma_R^2 \\ \Rightarrow \epsilon_y &= \log y + \frac{1}{2}\sigma_R^2. \end{aligned} \tag{A.6}$$

Therefore

$$\frac{ds(y)}{dy} = \frac{d\epsilon_y(y)}{dy} = \frac{d}{dy} \left(\log y + \frac{1}{2}\sigma_R^2 \right) = \frac{1}{y}.$$

Then

$$\begin{aligned} g(y) &= \frac{1}{\sigma_R \sqrt{2\pi}} e^{-\frac{1}{2\sigma_R^2} [\log y + \frac{1}{2}\sigma_R^2]^2} \cdot \left| \frac{1}{y} \right| \\ &= \frac{1}{y\sigma_R \sqrt{2\pi}} \exp \left\{ -\frac{[\log y - (-\frac{1}{2}\sigma_R^2)]^2}{2\sigma_R^2} \right\}. \end{aligned} \tag{A.7}$$

This is the density function of a lognormal distribution with parameters $\mu = -\frac{1}{2}\sigma_R^2$ and σ_R^2 , that is,

$$Y \sim LN \left(-\frac{1}{2}\sigma_R^2, \sigma_R^2 \right)$$

and from equation A.7 we see that

$$-\log g(y) = \log y + \log \sigma_R + \frac{1}{2} \log 2\pi + \frac{1}{2\sigma_R^2} \left(\log y - \left(-\frac{1}{2}\sigma_R^2 \right) \right)^2. \tag{A.8}$$

which is exactly the same expression as that for $-\log f(y)$ in equation A.4.

Therefore if used correctly, Option 2 parameterisation results in the same contribution, $-\log g(y)$, to the negative log posterior as Option 1, $-\log f(y)$.

Note that $-\log f(y) = -\log f(\epsilon_y)$ only for $Y = 1$.

We will carry out a brief simulation exercise to illustrate the point. We will use the density functions derived above, rather than existing R functions and calculate $-\log f(y) = -\log g(y)$ and $-\log f(\epsilon_y)$ for a sequence of YCS_y values.

The simulation results indicate that $-\log f(y) = -\log g(y) = -\log f(\epsilon_y)$ only for $Y = 1$. For other values of Y , the size of the difference between $-\log f(y)$ and $-\log f(\epsilon_y)$ is given by $|\log y|$ and does not depend on σ_R^2 . Therefore, the differences increase in size as the YCS value diverges further from 1.

What is the implication of this?

Incorrect use of the prior based on ϵ_y (i.e., using $-\log f(\epsilon_y)$ in place of $-\log g(y)$) results in prior contributions to the negative log-posterior that are lower or higher by $\log YCS_y$ than what they should be.