2n Espà Ascinssov

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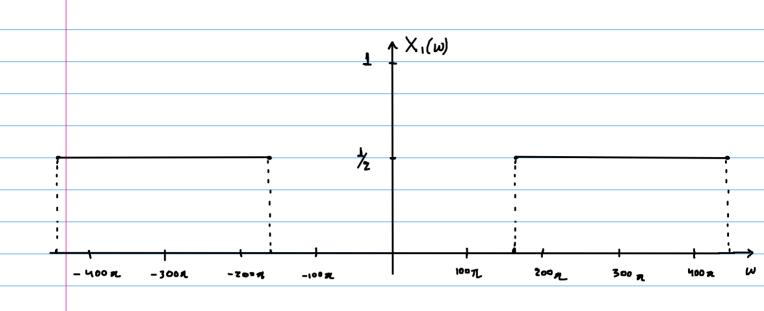
 $\alpha = AM \mod 10 + 1 = 6 + 1 = 7$

2.1)
$$\times_1(t) = \sin(20ant)\cos(360a.t) = \sin(140nt)\cos(300nt)$$

$$x_1(t) = 2 \sin(140\pi t) \cos(300\pi t) \cdot \frac{1}{2\pi t}$$

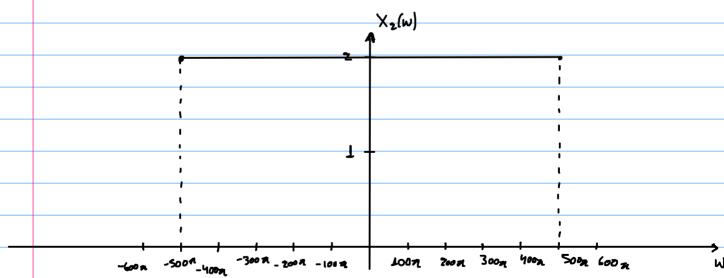
$$X_{i}(\omega) = F[x_{i}(t)] = \frac{1}{2}F[\frac{\sin 440at}{nt}] - \frac{1}{2}F[\frac{\sin 60at}{nt}]$$

$$X_{1}(\omega) = \begin{cases} \frac{1}{2}, & \omega \in (-9, -990\pi) \cup (-160\pi, 160\pi) \cup (990\pi, +\infty) \\ \frac{1}{2}, & \omega \in (-990\pi, -160\pi) \cup (160\pi, 990\pi) \end{cases}$$



$$X_2(\omega) = F[x_2(t)] = 2F[\frac{\sin(500\pi t)}{\pi t}] =$$

$$= \begin{cases} 0, & w \in (-\infty, -500\pi)_{U}(500\pi, +\infty) \\ = \\ 2, & -500\pi < w < 500\pi \end{cases}$$



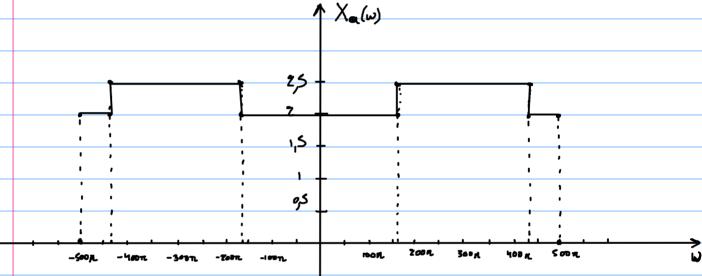
$$(x, (t) + x_2(t))$$

$$X_{01}(w) = F[x, (t) + x_2(t)] = F[x_1(t)] + F[x_2(t)] =$$

$$= X_1(w) + X_2(w) =$$

$$(x_1(w) + x_2(w)) = (x_1(w) + x_2(w))$$

$$\begin{cases}
0, & W \in (-\infty, -500n) \cup (500n, +\infty) \\
2, & W \in (-500n, +40n) \cup (-160n, 160n) \cup (440n, 500n) \\
\frac{5}{2}, & W \in (-440n, -160n) \cup (160n, 440n)
\end{cases}$$



$$W = 1000n \Rightarrow w_s > 2w \Rightarrow \frac{\pi}{T_s} > w \Rightarrow T_s < \frac{\pi}{w} = \frac{\pi}{1000n} = 10^3 s$$

$$b \times_{6}(t) = \times_{1}^{3}(t) = \times_{1}(t) \cdot \times_{1}^{2}(t)$$

$$X_{i}^{2}(t) \Rightarrow F[x_{i}^{2}(t)] = X_{i}(w) * X_{i}(w)$$

$$X_{\varrho}(\omega) = X_{\iota}(\omega) * F[X_{\iota}^{2}(t)],$$

$$W = W_{x_1} + W_{x_1} = 880n + 1760n = 2640n$$

$$\chi$$
 $\times_{b}(t) = \times_{1}(t) \star \times_{2}(t)$

$$X_{1}(w) = X_{1}(w) \cdot X_{2}(w)$$

$$w = \min \{w_1, w_2\} = \{880\pi, 1000\pi\} = 880\pi$$

$$\omega_s > 2\omega \Rightarrow 2\pi > 2-880 \mu \Rightarrow T_s < 880_s$$

$$S) \times r(t) = \gamma_1(t) \cdot \left[\times_2(t) \right]^2 + \left[\times_1(t) \right]^2 * \gamma_2(t)$$

$$X_{s(\omega)} = F[\gamma_{s(t)} \cdot [x_{z(t)}]^{2}] + F[x_{s(t)}]^{2} * \gamma_{z(t)}$$

0.0	
2.2)	

2.3)
$$w_s = (2 + 7 mod 3) w_n = (2 + 1) w_n = 3 w_n$$

a) $y_d[n] = \frac{x[n-1] - 2x[n] + x[n+1]}{4} = \frac{1}{4} x[n-1] - \frac{1}{2} x[n] + \frac{1}{4} x[n+1]$

$$\chi_{1}[\circ] = \frac{1}{4}e^{-j^{\circ}} \times_{1}[\circ] - \frac{1}{2} \times_{1}[\circ] + \frac{1}{4}e^{j^{\circ}} \times_{1}[\circ] \Rightarrow$$

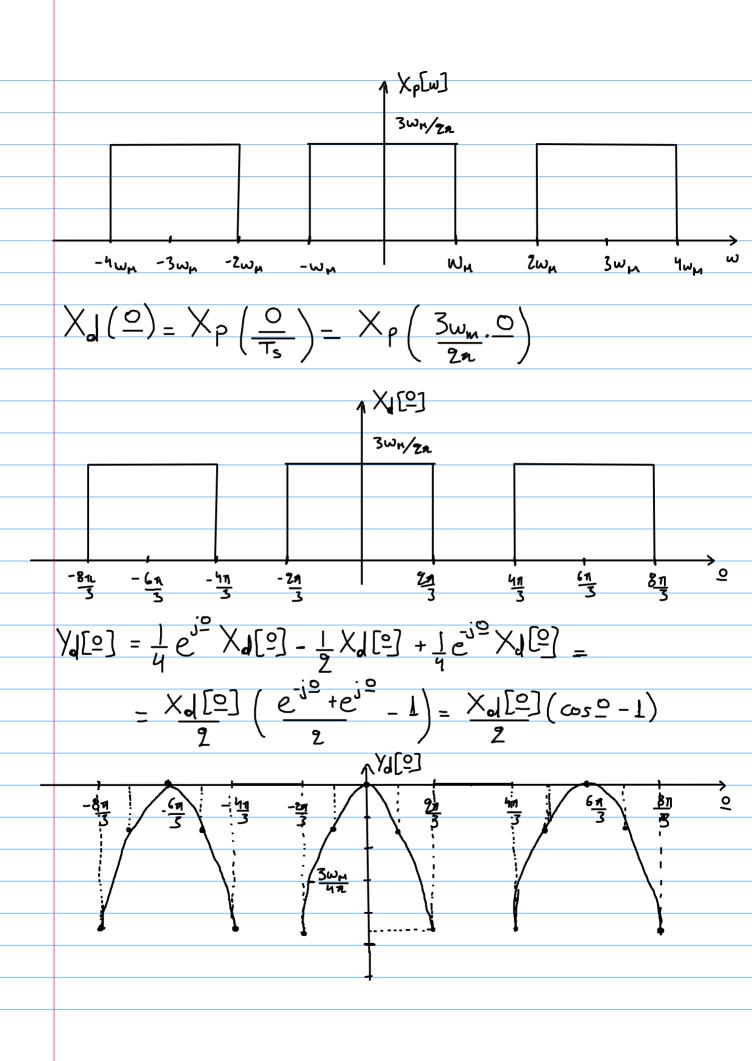
$$\frac{\chi_{1}[0]}{\times d[0]} = \frac{1}{2} \left(\frac{e^{-j0} + e^{j0}}{2} - 1 \right) = \frac{1}{2} \left(\cos 0 - 1 \right)$$

$$H_d[\underline{0}] = \frac{1}{2} \left(\cos \underline{0} - 1 \right)$$

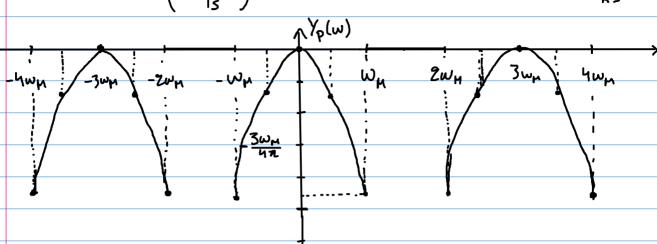
$$h_{d}[n] = F^{-1}[H_{d}[^{\circ}]] = \frac{1}{4}F^{-1}[e^{-j^{\circ}} + e^{j^{\circ}}] - \frac{1}{2}F^{-1}[1] = \frac{1}{4}S[n-1] + \frac{1}{4}S[n+1] - \frac{1}{2}S[n] = \frac{1}{4}S[n-1] - \frac{2}{2}S[n] + \frac{1}{4}S[n+1]$$

b)
$$\chi(t) = \frac{\sin(\omega_{m}t)}{\pi t}$$
, $w_{s} = \frac{2a}{T_{s}} \rightarrow T_{s} = \frac{2a}{\omega_{s}} = \frac{2a}{3\omega_{m}}$

$$\times \rho[w] = \times_{c}(w) * F\left[\sum_{n} \int (t-nT_{s})\right] = \times_{c} * \left[\frac{1}{T_{s}} \sum_{m=-\infty}^{+\infty} (w-mu_{s})\right] = \frac{1}{T_{s}} \sum_{m=-\infty}^{+\infty} \times_{c} (w-mu_{s}) = \frac{1}{2\pi} \sum_{m=-\infty}^{+\infty} \times_{c} (w-mu_{s})$$



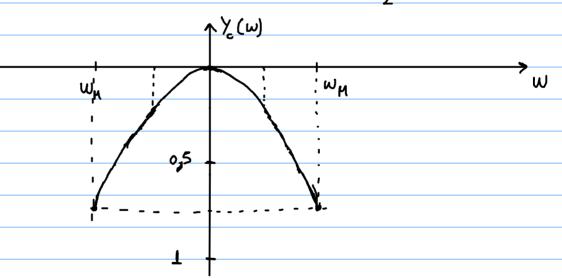
$$Y_{d}[Q] = Y_{p}(\frac{Q}{T_{s}}) \Rightarrow Y_{p}(\omega) = Y_{d}[\omega T_{s}] = Y_{d}[\omega \frac{2n}{3\omega_{n}}]$$



$$H_{r}(\omega) = \begin{cases} T & |\omega| < \frac{\omega_{s}}{2} = \frac{3\omega_{h}}{2} \\ O & |\omega| > \frac{\omega_{s}}{2} = \frac{3\omega_{h}}{2} \end{cases}$$

$$\begin{cases} O & |\omega| > \frac{\omega_{s}}{2} = \frac{3\omega_{h}}{2} \\ \frac{2\pi}{3\omega_{h}} \cdot \sqrt{\rho(\omega)} & |\omega| < \frac{3\omega_{h}}{2} \end{cases}$$

$$\begin{cases} \gamma_{c}(\omega) = \sqrt{\rho(\omega)} \cdot \| r(\omega) = \begin{cases} O & |\omega| > \frac{3\omega_{h}}{2} \end{cases}$$



$$\begin{aligned} & \text{Eno}_{l} | \text{Evous} & \text{H}_{c}(\omega) = \begin{cases} \frac{1}{2} \left(\cos(\frac{2\pi}{3} \cdot \frac{\omega}{\omega_{h}}) - \frac{1}{2} \right), & |\omega| \leq \frac{\pi}{15} = \frac{\pi}{2\pi} = \frac{3\omega_{h}}{2} \\ & \text{O}, & |\omega| > \frac{3\omega_{h}}{2} \end{cases} \\ & \text{O}, & |\omega| > \frac{3\omega_{h}}{2} \end{cases} \end{aligned}$$

$$\begin{aligned} & \text{If } | \text{O} | \text{O} | \text{If } | \text{O} | \text{$$

$$= \frac{336 z \left(1-z^{2}\right)}{(z+z)^{2}(7z-1)^{2}} , |z| > \frac{1}{7}, |z| > \frac{1}{7} \Rightarrow |z| < 7$$

$$|z| = \frac{1}{7} |z| |z| < 7$$

$$|z| = \frac{1}{7} |z| |z| |z| + \frac{1}{7} |z| |z| |z| = \frac{1}{7} |z| |z| |z| + \frac{1}{7} |z| +$$

$$= \frac{\sqrt{2}}{2} \left[-\frac{7}{2} \frac{1}{d_{z}} \left(\frac{\sqrt{3}}{2} \cdot \frac{7z}{4\sqrt{3}z^{2} - 7z + 1} \right) - \frac{2}{2} \frac{1}{d_{z}} \left(\frac{1}{2} \cdot \frac{7z(14z - 1)}{4\sqrt{3}z^{2} - 7z + 1} \right) \right] =$$

$$= -\frac{7\sqrt{2}}{4} \left[\sqrt{3} \cdot \frac{4\sqrt{3}z^{2} - 7z + 1}{(4\sqrt{3}z^{2} - 7z + 1)^{2}} + \frac{2}{(4\sqrt{3}z^{2} - 7z + 1)^{2}} + \frac{2}{(4\sqrt{3}z^{2} - 7z + 1)^{2}} \right] =$$

$$= -\frac{7\sqrt{2}}{4} \cdot 2 \left[\sqrt{3} \cdot \frac{-4\sqrt{3}z^{2} + 1}{(4\sqrt{3}z^{2} - 7z + 1)^{2}} + \frac{2+\frac{7}{2}z^{2} + 4\sqrt{2}z^{2} + 4\sqrt{2}z^{2} + 4\sqrt{2}z^{2} + 2\sqrt{2}z^{2} + 2\sqrt{2}z^{2$$

$$X_{4}[n] = 7^{n} u[-n-1] + \left(\frac{1}{2}\right)^{n} \frac{\cos(n\pi) + 1}{2} u[n] + \left(\frac{1}{3}\right)^{n} \left[\frac{\cos(n\pi) + 1}{2} - \cos(n\pi)\right] u[n] = \frac{7^{n} u[-n-1] + \left(\frac{1}{2}\right)^{n} \cdot \frac{\cos(n\pi) + 1}{2} u[n] + \left(\frac{1}{3}\right)^{n} \cdot \frac{1 - \cos(n\pi)}{2} u[n] = \frac{7^{n} u[-n-1] + \left(\frac{1}{2}\right)^{n} \cdot \frac{\cos(n\pi) + 1}{2} u[n] + \left(\frac{1}{3}\right)^{n} \cdot \frac{1 - \cos(n\pi)}{2} u[n] = \frac{7^{n} u[-n-1] + \left(\frac{1}{2}\right)^{n} \cdot \frac{\cos(n\pi) + 1}{2} u[n] + \left(\frac{1}{3}\right)^{n} \cdot \frac{1 - \cos(n\pi)}{2} u[n] = \frac{7^{n} u[-n-1] + \left(\frac{1}{2}\right)^{n} \cdot \frac{\cos(n\pi) + 1}{2} u[n] + \left(\frac{1}{3}\right)^{n} \cdot \frac{1 - \cos(n\pi)}{2} u[n] = \frac{7^{n} u[-n-1] + \left(\frac{1}{2}\right)^{n} \cdot \frac{\cos(n\pi) + 1}{2} u[n] + \left(\frac{1}{3}\right)^{n} \cdot \frac{1 - \cos(n\pi)}{2} u[n] = \frac{7^{n} u[-n-1] + \left(\frac{1}{2}\right)^{n} \cdot \frac{\cos(n\pi) + 1}{2} u[n] + \left(\frac{1}{3}\right)^{n} \cdot \frac{1 - \cos(n\pi)}{2} u[n] = \frac{7^{n} u[-n-1] + \left(\frac{1}{2}\right)^{n} \cdot \frac{\cos(n\pi) + 1}{2} u[n] + \left(\frac{1}{3}\right)^{n} \cdot \frac{1 - \cos(n\pi)}{2} u[n] = \frac{7^{n} u[-n-1] + \left(\frac{1}{2}\right)^{n} \cdot \frac{\cos(n\pi) + 1}{2} u[n] + \left(\frac{1}{3}\right)^{n} \cdot \frac{1 - \cos(n\pi)}{2} u[n] = \frac{1}{2} u[n] + \frac{$$

$$= -\left(-\frac{7}{4}u[-N-1]\right) + \left(\frac{1}{2}\right)^{N} \cos(n\pi) + u[n] + \left(\frac{1}{3}\right)^{N} \cdot \frac{1-\cos(n\pi)}{2}u[n] =$$

$$= -\left(-\frac{7}{4}u[-N-1]\right) + \frac{1}{2} \cdot \left(\frac{1}{2}\right)^{N} \cos(n\pi)u[n] + \frac{1}{2}\left(\frac{1}{2}\right)^{N} u[n] +$$

$$+ \frac{1}{2}\left(\frac{1}{3}\right)^{N} u[n] - \frac{1}{2}\left(\frac{1}{3}\right)^{N} \cos(n\pi)u[n]$$

$$\times \frac{1}{4}\left(\frac{1}{2}\right)^{N} u[n] - \frac{1}{2}\left(\frac{1}{3}\right)^{N} \cos(n\pi)u[n]$$

$$+ \frac{1}{2}\left(\frac{1}{3}\right)^{N} u[n] - \frac{1}{2}\left(\frac{1}{3}\right)^{N} \cos(n\pi)u[n] =$$

$$= -\frac{1}{1-7\epsilon^{-1}} + \frac{1}{2} \cdot \frac{1-\frac{1}{2}\cos\pi \cdot z^{-1}}{1-2\cdot\frac{1}{2}\cos\pi \cdot z^{-1} + \frac{1}{4}z^{-2}} + \frac{1}{2} \cdot \frac{1}{1-\frac{1}{2}z^{-1}} + \frac{1}{2} \cdot \frac{1}{1-\frac{1}{3}z^{-1}} -$$

$$= -\frac{1}{1-\frac{1}{3}\cos\pi z^{-1}} + \frac{1}{2} \cdot \frac{1-\frac{1}{2}\cos\pi \cdot z^{-1}}{1-2\cdot\frac{1}{2}\cos\pi \cdot z^{-1} + \frac{1}{2}\cdot \frac{1}{1-\frac{1}{2}z^{-1}} + \frac{1}{2} \cdot \frac{1}{1-\frac{1}{3}z^{-1}} -$$

$$= -\frac{1}{2} \cdot \frac{1-\frac{1}{3}\cos\pi z^{-1}}{1-2\cdot\frac{1}{3}\cos\pi z^{-1} + \frac{1}{2}\cdot \frac{2\pi^{-1}}{1-\frac{1}{2}z^{-1}} + \frac{1}{2} \cdot \frac{1}{1-\frac{1}{2}z^{-1}} + \frac{1}{2} \cdot \frac{1}{1-\frac{1}{2}z^{-1}} + \frac{1}{2} \cdot \frac{1}{1-\frac{1}{2}z^{-1}} + \frac{1}{2} \cdot \frac{2\pi^{-1}}{1-\frac{1}{2}z^{-1}} + \frac{1}{2} \cdot \frac{2\pi^{-1}}{1-\frac{1}{2}z^{-1}} + \frac{1}{2} \cdot \frac{2\pi^{-1}}{3\pi^{-1}} + \frac{1}{2} \cdot \frac{2\pi^{-1}}{3\pi^{-1}} + \frac{1}{2} \cdot \frac{3\pi^{-1}}{3\pi^{-1}} - \frac{1}{2} \cdot \frac{3\pi^{-1}}{3\pi^{-1}} + \frac{1}{2}$$

$$(2.5)$$
 a) $(2) = \frac{2-3}{2^2-9z+9}$, (1) aluazi

$$\frac{Q}{4} = \frac{\pi}{4}, r = \sqrt{2} \times [n] = (\sqrt{2})^{n} \cos(\frac{\pi}{4}n)u[n]$$

$$\frac{X(z) = \frac{1 - \sqrt{2} \cdot \sqrt{2} \cdot z^{-1}}{1 - 2 \cdot \sqrt{2} \cdot \sqrt{2} \cdot z^{-1} + (2)^{2} \cdot z^{-2}} = \frac{\frac{z - 1}{2}}{z^{2} - 2z + 2} = \frac{z^{2} - z}{z^{2} - 2z + 2} = \frac{z^{2} - z}{z^{2} - 2z + 2}$$

$$\frac{2^{2}-2z+2+z-2}{2^{2}-2z+2} = 1 + \frac{z-2}{z^{2}-2z+2}$$

$$\frac{\chi_{(z)} = \frac{\sqrt{z} \cdot \sqrt{z} z^{-1}}{1 - 2 \cdot 6 \cdot \sqrt{z} z^{-1} + 2z^{-2}} = \frac{z^{-1}}{z^{2} - 2z + 2} = \frac{z}{z^{2} - 2z + 2}$$

$$\frac{2-3}{z^2-2z+2} = \alpha \left(\frac{1+z-2}{z^2-2z+2}\right) + 6. \frac{z}{z^2-2z+2} + \gamma \Rightarrow$$

$$\alpha+\gamma=0 \Rightarrow , 2\gamma=-3 \Rightarrow , 6-\alpha-2\gamma=1 \Rightarrow$$

 $\alpha=-\gamma=\frac{3}{2} \qquad \beta=-\frac{3}{2} \qquad 6=2\gamma+\alpha+1=-3+\frac{3}{2}+1=-\frac{1}{2}$

Nogw spartikimzas:

$$A_{\rho\alpha} \times_{[n]} = \frac{3}{2} (\sqrt{2})^{n} \cos(\frac{\pi}{4}n) u[n] - \frac{1}{2} (\sqrt{2})^{n} \sin(\frac{\pi}{4}n) u[n] - \frac{3}{2} \delta[n]$$

$$A_{2}(z) = \frac{z + 2z^{-1}}{z^{2} + 4} , |z| > 2$$

$$X_{2}(z) = \frac{z^{-1} + 2z^{-3}}{1 + 4z^{-2}} = \frac{z^{-1}}{1 + 4z^{-2}} + \frac{2z^{-3}}{1 + 4z^{-2}} =$$

$$= \frac{1}{2} \cdot \frac{2z^{-1}}{1 + 4z^{-2}} + \frac{2z^{-1}}{1 + 4z^{-2}} \cdot z^{-2} , |z| = \frac{1}{2} \cdot \frac{2}{1 + 4z^{-2}} + \frac{2z^{-1}}{1 + 4z^{-2}} \cdot z^{-2} , |z| = \frac{1}{2} \cdot \frac{2}{1 + 4z^{-2}} + \frac{2}{1 + 4z^{-2}} \cdot z^{-2} \cdot z^{-2}$$

$$\times_{2}[u] = \frac{1}{2} \cdot \frac{2}{1 + 2z^{-1}} + \frac{2}{1 + 4z^{-2}} \cdot z^{-2} \cdot z^{-2$$

$$= 2^{n-1} \sin\left(\frac{\pi}{2}n\right) \left[u[n] - u[n-2]\right] =$$

$$= 2^{n-1} \sin\left(\frac{\pi}{2}u\right) \cdot \frac{2u[n] - u[n-2]}{2} =$$

$$= 2^{n-2} \sin\left(\frac{\pi}{2}u\right) \cdot \frac{2u[n] - u[n-2]}{2} =$$

$$= 2^{n-2} \sin\left(\frac{\pi}{2}u\right) \cdot \frac{2u[n] - u[n-2]}{2} =$$

$$\chi$$
) $\chi_3(z) = \frac{7z^2 + 4z}{z^3 + z^2 - 4z - 4}$, $|z| < 1$

$$\chi_{3(z)} = \frac{7z^2 + 4z}{z^2(z+1) - 4(z+1)} = \frac{7z^2 + 4z}{(z+1)(z-2)(z+2)}$$

$$\frac{7z^{2}+4z}{(z+1)(z+2)(z-2)} = \frac{A}{z+1} + \frac{B}{z+2} + \frac{\Gamma}{z-2} \Rightarrow$$

$$72^{2}+42 = A(2^{2}-4) + B(2+1)(2-2) + \Gamma(2+1)(2+2) \Rightarrow$$

$$72^{2}+42 = A2^{2}-4A+32^{2}-B2-2B+\Gamma2^{2}+3\Gamma2+2\Gamma \Rightarrow$$

$$72^{2}+42 = (A+B+\Gamma)2^{2}+(3\Gamma-B)2+2\Gamma-4A-2B$$

$$A+B+\Gamma=7 \Rightarrow A+2-3A+2-A=7 \Rightarrow A=-1$$

 $3\Gamma-B=Y=>B=3\Gamma-Y \Rightarrow B=6A+3B-Y=>2B=Y-6A\Rightarrow$
 $2\Gamma-YA-2B=O\Rightarrow \Gamma=2A+B=2A+2-3A=2-A$ $B=2-3A$

$$X_3(z) = -\frac{1}{z+1} + 5 \cdot \frac{1}{z+2} + 3 \cdot \frac{1}{z-2} =$$

$$S = 5$$

$$\Gamma = 3$$

$$=-\frac{z^{-1}}{1+z^{-1}} + 5 \cdot \frac{z^{-1}}{1+2z^{-1}} + 3 \cdot \frac{z^{-1}}{1-2z^{-1}} =$$

$$= -\left(\frac{1-\frac{1}{1+z^{-1}}}{1+z^{-1}}\right) + \frac{5}{2} \left(\frac{1-\frac{1}{1+2z^{-1}}}{1+2z^{-1}}\right) + \frac{3}{2} \left(-\frac{1+\frac{1}{1-2z^{-1}}}{1-2z^{-1}}\right) =$$

$$= -\frac{1}{2} + \frac{5}{2} - \frac{3}{2} + \frac{1}{1+z^{-1}} - \frac{5}{2} \cdot \frac{1}{1+2z^{-1}} + \frac{3}{2} \cdot \frac{1}{1-2z^{-1}} =$$

$$\frac{5)}{(2+1)(2^{2}-2z-3)} \times \frac{z^{3}(5z+1)}{(2+1)(2^{2}-2z-3)} + \frac{1 < |z| < 3}{(2+1)(2^{2}-2z-3)}$$

$$\frac{\chi_{4(z)}}{z^{3}-z^{2}-5z-3}+3Lz^{2}+4\frac{5}{2}+8}{z^{3}-z^{2}-5z-3}+3Lz^{2}+4\frac{5}{2}+8} = 5z+6+\frac{3Lz^{2}+45z+8}{(z+1)^{2}(z-3)}$$

$$\frac{31z^{2}+45z+18}{(z+1)^{2}(z-3)} = \frac{A}{z+1} + \frac{B}{(z+1)^{2}} + \frac{\Gamma}{z-3} \Rightarrow$$

$$B+17=-3B+13 \Rightarrow 4B=-4 \Rightarrow B=-1$$

$$A=-\frac{1+17}{4}=\frac{16}{4}=\frac{4}{1}$$

$$\Gamma=31-4=27$$

$$X_{4}(z) = 5z + 6 + \frac{4}{z+1} - \frac{1}{(z+1)^{2}} + \frac{27}{z-3} =$$

$$\frac{-5z^{-(-1)}+6+\frac{4}{2-(-1)}+\frac{-1}{(z-(-1))^2}+27.\frac{z^{-1}}{1-3z^{-1}}$$

$$\frac{-5z^{-(-1)}}{+6+\frac{4}{z-(-1)}} + \frac{-1}{(z-(-1))^2} + \frac{9\cdot(-1+\frac{1}{1-3z^{-1}})}{1-3z^{-1}} =$$

$$= 5z^{-(-1)} - 3 + \frac{4}{2-(-1)} + \frac{-1}{(z-(-1))^2} + 9 \cdot \frac{1}{1-3z^4}$$

$$x_{4}[n] = 5\delta[n+1] - 3\delta[n] + 4(-1)^{n-1}u[n-1] + (n-1)(-1)^{n-1}u[n-1] - -9.3^{n}u[-n-1] =$$

$$= 55[n+1] - 35[n] + (n+3)(-1)^{n-1} u[n-L] - 3^{n+2} u[-n-1]$$

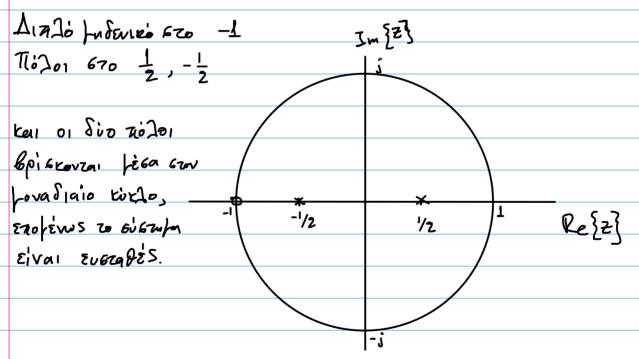
2.6) a)
$$y[n] - \frac{1}{4}y[n-2] = x[n] + 2x[n-1] + x[n-2] \Rightarrow$$

$$y(z) - \frac{1}{4}z^{-2}y(z) = x(z) + 2z^{-1}x(z) + z^{-2}x(z) \Rightarrow$$

$$y(z) \cdot \frac{4-z^{-2}}{4} - x(z)(1+2z^{-1}+z^{-2}) \Rightarrow$$

$$\frac{y(z)}{x(z)} = \frac{4+8z^{-1}+4z^{-2}}{4-z^{-2}} \Rightarrow \frac{||f(z)|| + 4+8z^{-1}+4z^{-2}}{4-z^{-2}}$$

$$\frac{||H(z)|| - ||H(z)||^2 + 8z + 4|| - ||H(z+1)||^2}{||H(z)|| - ||H(z+1)||^2}$$



Για να βρούζε την H(2) θα πάροζε το DFT της εξίδωσης διαφορών:

$$|H[9]| = 4.$$
 $|e^{j^{2}} + 1|^{2}$ $= 4. \frac{|e^{j^{2}} + 1|^{2}}{|ze^{j^{2}} - 1| \cdot |2e^{j^{2}} + 1|} = 4. \frac{(\cos^{2} + 1)^{2} + \sin^{2} \frac{1}{2}}{\sqrt{[z\cos^{2} - 1]^{2} + |z\sin^{2} \frac{1}{2}|}}$

$$= \frac{9(\cos^2 + 1)}{\sqrt{25 - 16\cos^2 2}} = \frac{16\cos^2(\frac{0}{2})}{\sqrt{25 - 16\cos^2 2}}$$

$$|H(9)| = 0 \quad \text{fix } \frac{Q}{2} = (2k+1)\pi \Rightarrow Q = (2k+1)\pi$$

$$|H(9)| = 0 \quad \text{fix } \frac{Q}{2} = (2k+1)\pi \Rightarrow Q = 2k\pi$$

$$E_{\chi \circ \psi z}$$
 $|H(e)| = 16 = 16$

Mz zu boulzia zou Matlab Boiseoufe zur nepiodo 6,27

$$\chi = \frac{4(z+1)^2}{(2z-1)(2z+1)} = \frac{4(z^2+2z+1)}{4z^2-1} = \frac{4z^2+8z+4}{4z^2-1}$$

$$H(z) = \frac{8z+5+4z^2-1}{4z^2-1} - \frac{1}{4} + \frac{8z+5}{(2z+1)(2z+1)}$$

$$\frac{8z+5}{(7z-1)(2z+1)} - \frac{A}{2z-1} + \frac{B}{2z+1} \Rightarrow 8z+5 = 2Az+A + 2Bz-B \Rightarrow$$

$$A+B=4$$
 $(+) \Rightarrow 2A=9 \Rightarrow A=\frac{9}{2}$, $B=-\frac{1}{2}$ $A-B=5$

$$H(z) = \frac{1}{2} + \frac{9}{2} \cdot \frac{1}{2z-1} = \frac{1}{2} \cdot \frac{1}{2z+1} = \frac{1}{4} \cdot \frac{1}{z-\frac{1}{2}} \cdot \frac{1}{4} \cdot \frac{1}{z+\frac{1}{2}}$$

$$h(n) = \delta(n) + \frac{9}{4} \left(\frac{1}{2}\right)^{n-1} u(n-1) - \frac{1}{4} \left(-\frac{1}{2}\right)^{n-1} u(n-1) = \frac{1}{2} \cdot \frac{1}{2} \cdot$$

$$5) \times [n] = (-\frac{1}{2})^n u[n] , y[-1] = \frac{1}{2} , y[-2] = 1$$

$$y_{zs}[n] = x[n]*h[n] \longrightarrow y_{zs}(z) = x(z)·H(z)$$

$$X(z) = Z^{-1} \left[\left(-\frac{1}{2} \right)^{4} u[u] \right] = \frac{1}{1 + \frac{1}{2z}} = \frac{2z}{2z+1}$$

$$\frac{1}{2}(z) = \frac{2z}{2z+1} \cdot \frac{4z^2+8z+4}{4z^2-1} = \frac{8z^3+16z^2+8z}{8z^3+4z^2-2z-1}$$

$$\frac{82^{3} + 162^{2} + 82 + 0}{-82^{3} + 102^{2} + 12^{2} + 12^{2} + 1}$$

$$\frac{122^{2} + 102 + 1}{122^{2} + 102^{2} + 1}$$

$$\frac{\sqrt{(z)} = 1 + \frac{|2z^2 + |0z + 1|}{(2z + 1)^2}}{(2z + 1)(2z + 1)^2}$$

$$\frac{|2z^{2}+|0z+1|}{(2z-1)^{2}-2z+1} = \frac{A}{2z-1} + \frac{B}{2z+1} + \frac{\Gamma}{(2z+1)^{2}} \Rightarrow$$

$$A - B - \Gamma = 1 \Rightarrow 3 - B - B - B + 1 = 1 \Rightarrow 4B = 3 \Rightarrow B = \frac{3}{4}$$

$$A = \frac{9}{4}, \quad \Gamma = \frac{1}{2}$$

$$Y_{1}(2) = 1 + \frac{9}{4}, \quad 1 = 1$$

$$\frac{1}{23} (2) = 1 + \frac{9}{4} \cdot \frac{1}{9_{2-1}} + \frac{3}{4} \cdot \frac{1}{2z+1} + \frac{1}{2} \cdot \frac{1}{(2z+1)^{2}} = \frac{1 + \frac{9}{8} \cdot \frac{1}{z-\frac{1}{2}} + \frac{3}{8} \cdot \frac{1}{z+\frac{1}{2}} + \frac{1}{4} \cdot \frac{1/9}{(z+\frac{1}{2})^{2}}$$

$$y_{25}[N] = 2^{-1} \left[\frac{1}{25}(2) \right] = 2^{-1} \left[\frac{1}{2} \right] + \frac{3}{8} 2^{-1} \left[\frac{1}{2 - 1/2} \right] + \frac{3}{8} 2^{-1} \left[\frac{1}{2 + 1/2} \right] - \frac{1}{4} 2^{-1} \left[\frac{-1/2}{(2 + 1/2)^2} \right] = \frac{1}{8} 2^{-1} \left[\frac{1}{2 - 1/2} \right] = \frac{1}{8} 2^{-1} \left[\frac{1}{2 + 1/2} \right] = \frac{1}{8} 2^{-1}$$

$$= S[n] + \frac{9}{8} \cdot \left(\frac{1}{2}\right)^{n-1} u[n-1] + \frac{3}{8} \cdot \left(-\frac{1}{2}\right) u[n-1] - \frac{1}{4}(n-1)\left(-\frac{1}{2}\right) u[n-1] =$$

$$= S[n] + \left(\frac{1}{2}\right)^{n} u[n-1] \left(\frac{9}{4} - \frac{3}{4}(-1)^{n} + \frac{h-1}{2}(-1)^{n}\right) =$$

$$= 5[n] + (\frac{1}{2})^{n+2} u[n-1] (9 - (2n-5)(-1)^{n})$$

la zur azorpien fudmiens Ereodou:

$$\frac{1}{2} \left(\frac{1}{2} \right) - \frac{1}{4} \left(\frac{2^{-2}}{2} \frac{1}{2} \left(\frac{1}{2} \right) + \frac{1}{2} \frac{1}{4} \left(\frac{1}{2} \right) + \frac{1}{4} \left(\frac{1}{2} \right) = 0 \Rightarrow$$

$$\frac{1}{2i}(2) - \frac{1}{4z^2} \frac{1}{2i} - \frac{1}{4} \left(\frac{1}{2z} + L \right) = 0 \Rightarrow$$

$$\frac{\gamma_{zi}(z)\left(\frac{\gamma_{z^2}-1}{\gamma_{z^2}}\right)}{\frac{\gamma_{z^2}}{\gamma_{z^2}}} = \frac{1}{\gamma_z} \cdot \frac{2z+1}{2z} \Rightarrow \frac{\gamma_{zi}(z)-\frac{1}{2}}{\frac{2}{2z-1}} \cdot \frac{z}{\gamma_{z-1}} = \frac{1}{\gamma_z} \cdot \frac{2z}{\gamma_{z-1}} = \frac{1}{\gamma_z} \cdot \frac{2z}{\gamma_z} = \frac{1}{\gamma_z} = \frac{1}{\gamma_z} \cdot \frac{2z}{\gamma_z} = \frac{1}{\gamma_z} \cdot \frac{2z}{\gamma_z} = \frac{1}{\gamma_z} \cdot \frac$$

$$= \frac{1}{4} \left(\frac{1}{1} + \frac{1}{2z-1} \right) = \frac{1}{4} \left(\frac{1+1}{2} \cdot \frac{1}{z-\frac{1}{2}} \right)$$

$$3zi[n] = 2 \left[\frac{1}{2}i(z) \right] = \frac{1}{4} \left[S[n] + \frac{1}{2} \cdot \left(\frac{1}{2}\right)^{n-1} u[n-1] \right] =$$

$$= \frac{1}{4} S[n] + \frac{1}{4} \left(\frac{1}{2}\right)^{n} u[n-1]$$

$$- \int [n] + \left(\frac{1}{2}\right)^{n+2} u[n-1] \left(9 - \left(2n-5\right)(-1)^{n}\right) + \frac{1}{4} \int [n] + \left(\frac{1}{2}\right)^{n} u[n-1] = \frac{5}{4} \int [n] + \left(\frac{1}{2}\right)^{n+2} u[n-1] \left(9+1-(2n-5)(-1)\right) = \frac{5}{4} \int [n] + \left(\frac{1}{2}\right)^{n+2} u[n-1] \left(9+1-(2n-5)(-1)\right) = \frac{5}{4} \int [n] + \frac{1}{4} \int [n] u[n-1] \left(9+1-(2n-5)(-1)\right) = \frac{5}{4} \int [n] u[n-1] \left(9+1-(2n-5)(-1)$$

$$=\frac{5}{4}S[n]+\left(\frac{1}{2}\right)^{n+2}u[n-1]\left(10-(2n-5)(-1)^{n}\right)$$

2.7)
$$\times [n] = S[n] + 2S[n-9]$$

$$= \sum_{n=0}^{5} \frac{j2n \cdot kn}{6} = \sum_{n=0}^{4} e^{-j\frac{2n}{6}kn} \left(S[n] + 2S[n-2] \right) = \sum_{n=0}^{4} e^{-j\frac{2n}{6}kn} \left(S[n] + 2S[n-2] \right)$$

$$=1+0+2e^{-\frac{14n}{6}k}+0+0+0=1+2e^{-\frac{12n}{3}k}$$

6)
$$Z[k] = e^{j\frac{2n}{6}} \cdot X[k] = e^{j\frac{2n}{6}} \left[1 + 2e^{-j\frac{4n}{6}k}\right] =$$

$$= e^{j\frac{2nk}{6}} + 2e^{j\frac{2nk}{6}}$$

$$\frac{N-1}{2[n]} = \frac{1}{N} = \frac{2[k]e^{j\frac{2nk}{N}}n}{|x|^{\frac{2nk}{N}}} = \frac{1}{6} = \frac{1}{6}$$

$$= \frac{1}{6} \sum_{k=0}^{5} \left[e^{j\frac{\pi k}{3}} + 2e^{-j\frac{\pi k}{3}} \right] e^{j\frac{\pi k}{3}} =$$

$$= \frac{1}{6} \left[3 + \left(e^{j\frac{\pi}{3}} + 2e^{-j\frac{\pi}{3}} \right) e^{j\frac{\pi k}{3}} + \left(e^{j\frac{2\pi}{3}} + 2e^{-j\frac{2\pi}{3}} \right) e^{j\frac{2\pi}{3}} +$$

$$+ \left(e^{j\frac{\pi}{3}} + 2e^{-j\frac{\pi}{3}} \right) e^{j\frac{\pi k}{3}} + \left(e^{j\frac{2\pi}{3}} + 2e^{-j\frac{2\pi}{3}} \right) e^{j\frac{2\pi}{3}} +$$

$$= \frac{1}{6} \left[3 + \left(\frac{1}{2} + j\frac{\sqrt{3}}{2} + \frac{2}{2} - 2 \right) \frac{\sqrt{3}}{2} \right) e^{j\frac{2\pi}{3}} + \left(-\frac{1}{2} + j\frac{\sqrt{3}}{2} - \frac{2}{2} - \frac{1}{2} - \frac{1}{2}$$

$$|h[n] = u[n-1] - u[n-6]$$

$$|h[n] = u[n-1] - u[n-6]$$

$$|h[n] = \delta[n-1] + \delta[n-2] + \delta[n-3] + \delta[n-4] + \delta[n-5]$$

$$|h[k] = \sum_{n=0}^{N-1} h[n] e^{-\frac{2i\pi}{N}kn} = \sum_{n=0}^{-\frac{i\pi}{N}kn} |h[n-2] + \delta[n-3] + \delta[n-4] + \delta[n-5] e^{-\frac{i\pi}{N}kn} = \sum_{n=0}^{-\frac{i\pi}{N}kn} |h[n] = \sum_{n=0}^{-\frac{i\pi}{N}$$

$$\begin{cases}
[2] = \frac{1}{6} \left[3 \cdot 4 + j 2 \cdot 3 \cdot (e^{j\frac{2\pi}{3}} - e^{j\frac{2\pi}{3}}) \right] = 2 + j \cdot \frac{13}{3} \left(-\frac{1}{2} \cdot j \cdot \frac{13}{2} + \frac{1}{2} \cdot \frac{13}{2} \right) = 2 + j \cdot \frac{13}{3} \left(-\frac{1}{2} \cdot j \cdot \frac{13}{2} + \frac{1}{2} \cdot \frac{13}{2} \right) = 2 + j \cdot \frac{13}{3} \left(-\frac{1}{2} \cdot j \cdot \frac{13}{2} + \frac{1}{2} \cdot \frac{13}{2} \right) = 2 + j \cdot \frac{13}{3} \left(-\frac{1}{2} \cdot j \cdot \frac{13}{2} + \frac{1}{2} \cdot \frac{13}{2} \right) = 2 + j \cdot \frac{13}{3} \left(-\frac{1}{2} \cdot j \cdot \frac{13}{2} + \frac{1}{2} \cdot j \cdot \frac{13}{2} \right) = 2 + j \cdot \frac{13}{3} \left(-\frac{1}{2} \cdot j \cdot \frac{13}{2} + \frac{1}{2} \cdot j \cdot \frac{13}{2} \right) = 2 + j \cdot \frac{13}{3} \left(-\frac{1}{2} \cdot j \cdot \frac{13}{2} + \frac{1}{2} \cdot j \cdot \frac{13}{2} \right) = 2 + j \cdot \frac{13}{3} \left(-\frac{1}{2} \cdot j \cdot \frac{13}{2} + \frac{1}{2} \cdot j \cdot \frac{13}{2} \right) = 2 + j \cdot \frac{13}{3} \left(-\frac{1}{2} \cdot j \cdot \frac{13}{2} + \frac{1}{2} \cdot j \cdot \frac{13}{2} \right) = 2 + j \cdot \frac{13}{3} \left(-\frac{1}{2} \cdot j \cdot \frac{13}{2} + \frac{1}{2} \cdot j \cdot \frac{13}{2} \right) = 2 + j \cdot \frac{13}{3} \left(-\frac{1}{2} \cdot j \cdot \frac{13}{2} + \frac{1}{2} \cdot j \cdot \frac{13}{2} \right) = 2 + j \cdot \frac{13}{3} \left(-\frac{1}{2} \cdot j \cdot \frac{13}{2} + \frac{1}{2} \cdot j \cdot \frac{13}{2} \right) = 2 + j \cdot \frac{13}{3} \left(-\frac{1}{2} \cdot j \cdot \frac{13}{2} + \frac{1}{2} \cdot j \cdot \frac{13}{2} \right) = 2 + j \cdot \frac{13}{3} \left(-\frac{1}{2} \cdot j \cdot \frac{13}{2} + \frac{1}{2} \cdot j \cdot \frac{13}{2} \right) = 2 + j \cdot \frac{13}{3} \left(-\frac{1}{2} \cdot j \cdot \frac{13}{2} + \frac{1}{2} \cdot j \cdot \frac{13}{2} \right) = 2 + j \cdot \frac{13}{3} \left(-\frac{1}{2} \cdot j \cdot \frac{13}{2} + \frac{1}{2} \cdot j \cdot \frac{13}{2} \right) = 2 + j \cdot \frac{13}{3} \left(-\frac{1}{2} \cdot j \cdot \frac{13}{2} + \frac{13}{2} \right) = 2 + j \cdot \frac{13}{3} \left(-\frac{1}{2} \cdot j \cdot \frac{13}{2} + \frac{13}{2} \right) = 2 + j \cdot \frac{13}{3} \left(-\frac{1}{2} \cdot j \cdot \frac{13}{2} + \frac{13}{2} \right) = 2 + j \cdot \frac{13}{3} \left(-\frac{1}{2} \cdot j \cdot \frac{13}{2} + \frac{13}{2} \right) = 2 + j \cdot \frac{13}{3} \left(-\frac{1}{2} \cdot j \cdot \frac{13}{2} + \frac{13}{2} \right) = 2 + j \cdot \frac{13}{3} \left(-\frac{1}{2} \cdot j \cdot \frac{13}{2} + \frac{13}{2} \right) = 2 + j \cdot \frac{13}{3} \left(-\frac{1}{2} \cdot j \cdot \frac{13}{2} + \frac{13}{2} \right) = 2 + j \cdot \frac{13}{3} \left(-\frac{1}{2} \cdot j \cdot \frac{13}{2} + \frac{13}{2} \right) = 2 + j \cdot \frac{13}{3} \left(-\frac{1}{2} \cdot j \cdot \frac{13}{2} + \frac{13}{2} \right) = 2 + j \cdot \frac{13}{3} \left(-\frac{1}{2} \cdot j \cdot \frac{13}{2} + \frac{13}{2} \right) = 2 + j \cdot \frac{13}{3} \left(-\frac{1}{2} \cdot j \cdot \frac{13}{2} + \frac{13}{2} \right) = 2 + j \cdot \frac{13}{3} \left(-\frac{1}{2} \cdot j \cdot \frac{13}{2} + \frac{13}{2} \right) = 2 + j \cdot \frac{13}{3} \left(-\frac{1}{2} \cdot j \cdot \frac{13}{2} \right) = 2 + j \cdot \frac{13}{3} \left(-\frac{1}{2} \cdot j$$

$$g[0] = \frac{1}{2} \times [m]h[-m] = 0$$

$$g[1] = \frac{1}{2} \times [m]h[-m] = \times [o] = 1$$

$$g[2] = \frac{3}{2} \times [m]h[2-m] = \times [o] + \times [o] = 1 + 0 = 1$$

$$9[3] - \frac{7}{2} \times [m] \cdot [3-m] = \times [0] + \times [1] + \times [2] = 1 + 0 + 2 = 3$$

$$g[4] = \frac{1}{2} \times [m] \left[\frac{1}{4} - m \right] = \times [0] + \times [1] + \times [2] + \times [3] = 1 + 0 + 2 + 0 = 3$$

$$g[5] = \frac{1}{2} \times [m] \left[\frac{1}{5} - m \right] = \times [0] + \times [1] + \times [2] + \times [3] + \times [4] = 3$$

$$g[7] = \int_{m=0}^{7} x[m]h[7-m] = x[2] + x[3] + x[4] + x[5] + x[6] = 2$$

