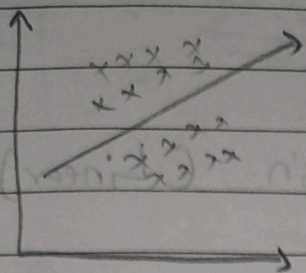


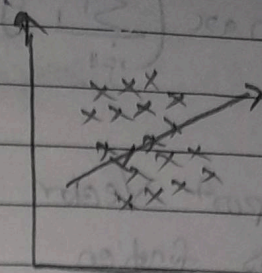
* Support Vector Machine

WORLD STAR™

Date: _____
Page: _____



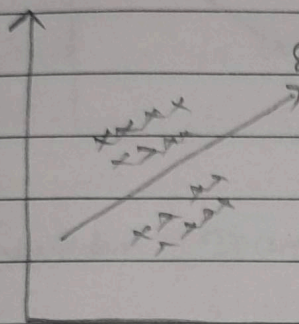
Linear
Separable



Non-Linear
Separable

SVM → Kernel trick

(We can solve this problem using)



Equation for this line

$$\Rightarrow y = mx + c$$

(or)

$$y = w_0x + c$$

$$\Rightarrow y = m_1x_1 + m_2x_2 + m_3x_3$$

Way of representation of above Eq

$$mx \rightarrow \begin{bmatrix} \quad \end{bmatrix} \begin{bmatrix} \quad \end{bmatrix}$$

matrix

(norms) \Rightarrow (distance between)
Point and Plane

norms for distance
between point and
plane

#

$$\text{Norms} = \frac{mx + c}{\|m\|}$$

distance $\rightarrow \|m\|$

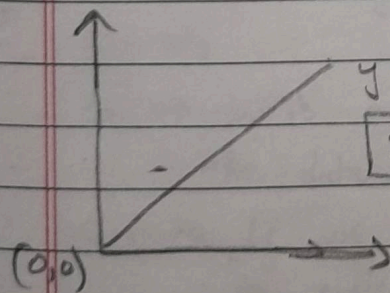
magnitude

distance point and
plane

(vector) value + direction

$$(or) \Rightarrow \text{Norms} = \frac{w^T x + c}{\|w\|}$$

$$\frac{1}{0} = \text{not}$$



$$y = mx + c \quad (c=0)$$

$$y = mx$$

$$\text{norms} = \frac{w^T x}{\|w\|}$$

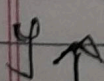
$\|w\| \leftarrow$ unit vector

value = 1

$$\text{Norms} = w^T x \Rightarrow mx$$

#

Binary class



true above the line $\Rightarrow +ve$

false below the line $\Rightarrow -ve$

$$\max \left(\sum_{i=1}^n y_i \times w^T x_i \right) \leftarrow \text{(loss or cost func)}$$

data point

* (1) Support Vector \rightarrow max margin (Linear)

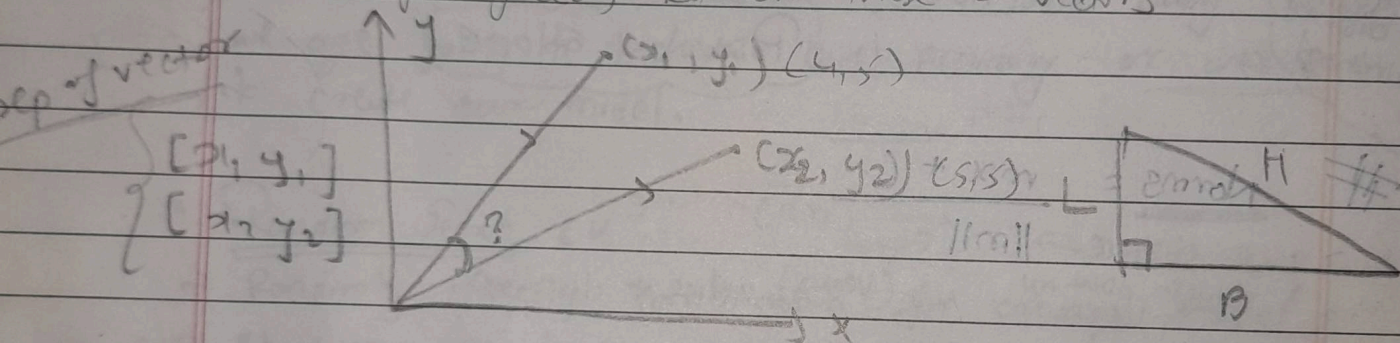
(2) Loss function

* Non-Linear Separable Data (MLSD)

- (1) Polynomial } Kernel trick
(2) RBF

SVM notebook \Rightarrow ML Dep Vector

* # calculating angle (θ) between these 2 vectors



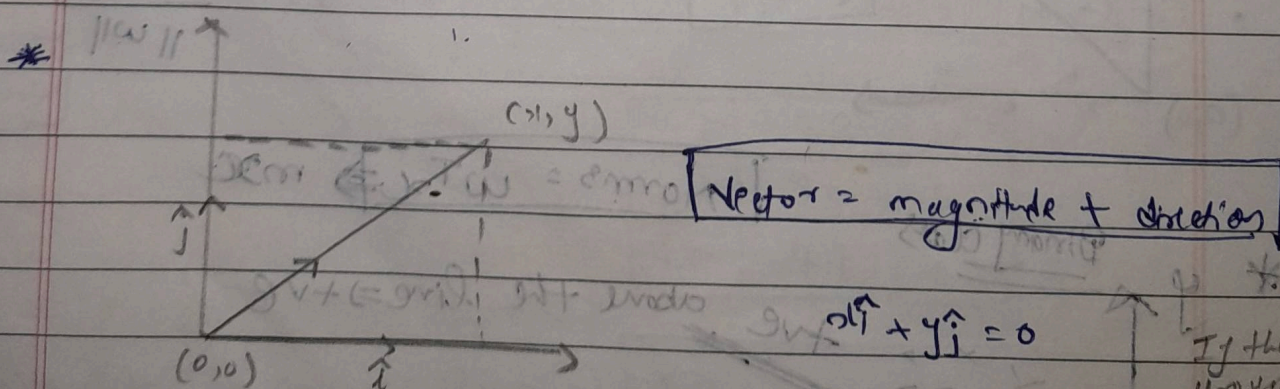
$$\tan \theta = \frac{L}{B}$$

$$y + x^T w = \text{error} \leftarrow (w)$$

$\|w\|$

$$\theta = \tan^{-1} \frac{L}{B}$$

$y - Tw = \text{error}$

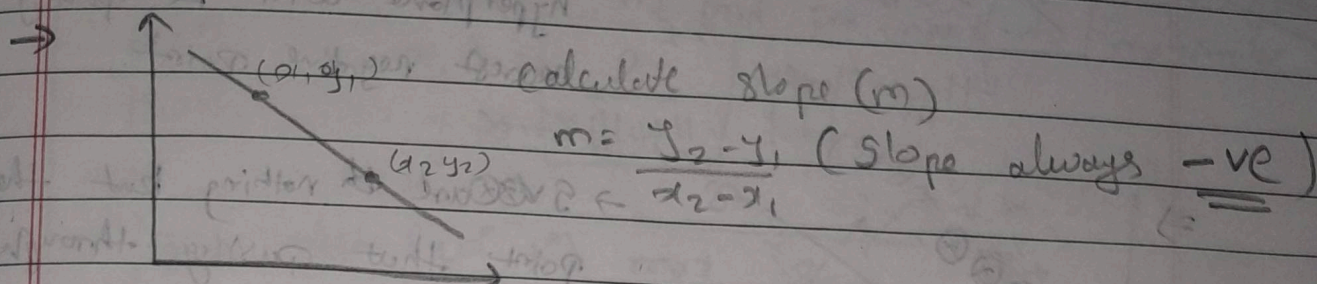
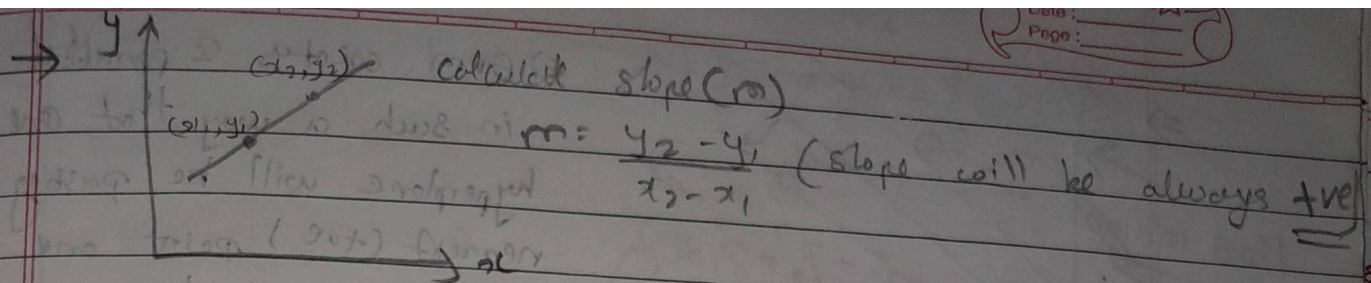


If the line going through origin will be

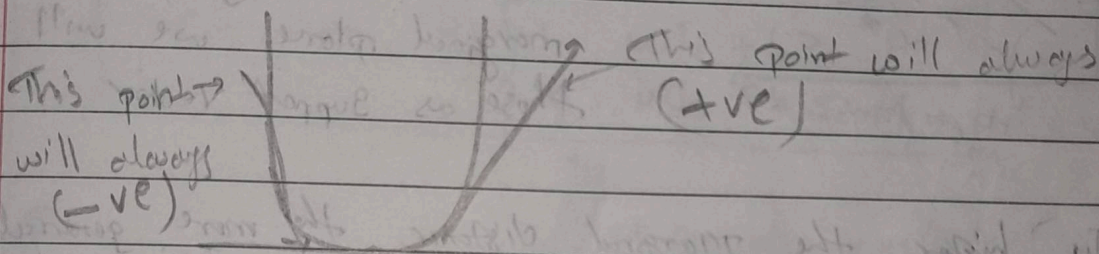
General Equation of line $\Rightarrow ax + by + c = 0$

Equation for vector

$$ax + by = 0$$



Gradient Descent curve \Rightarrow



• Kernel trick

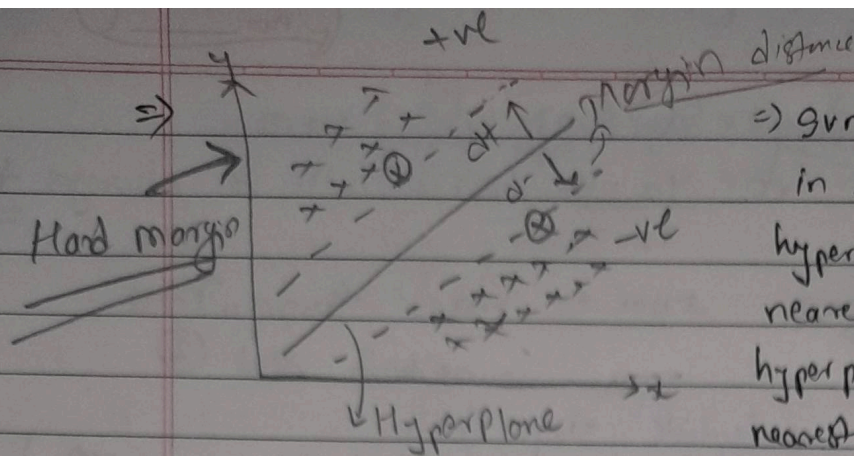
\hookrightarrow we will convert low dimensions into higher dimensions this polynomial and RBF

Interview Question \Rightarrow What is Difference between SVC and SVM?

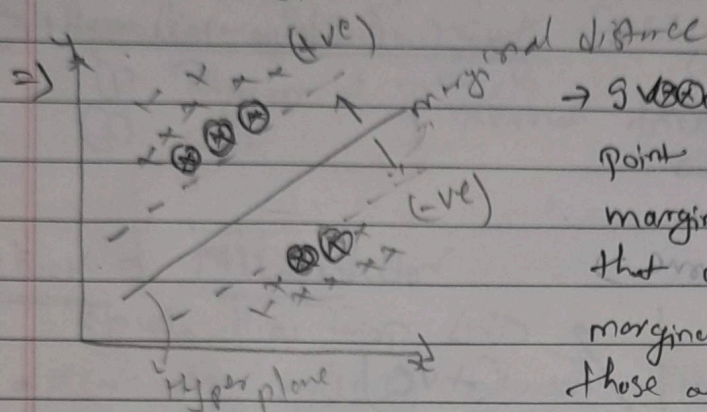
Ans \Rightarrow

SVC \rightarrow It is a linear classifier which is able to separate the data that is called support vector classifier

SVM \rightarrow If we are going to transform our data then it is called SVM. There are three ways transforming the data = Polynomial, RBF

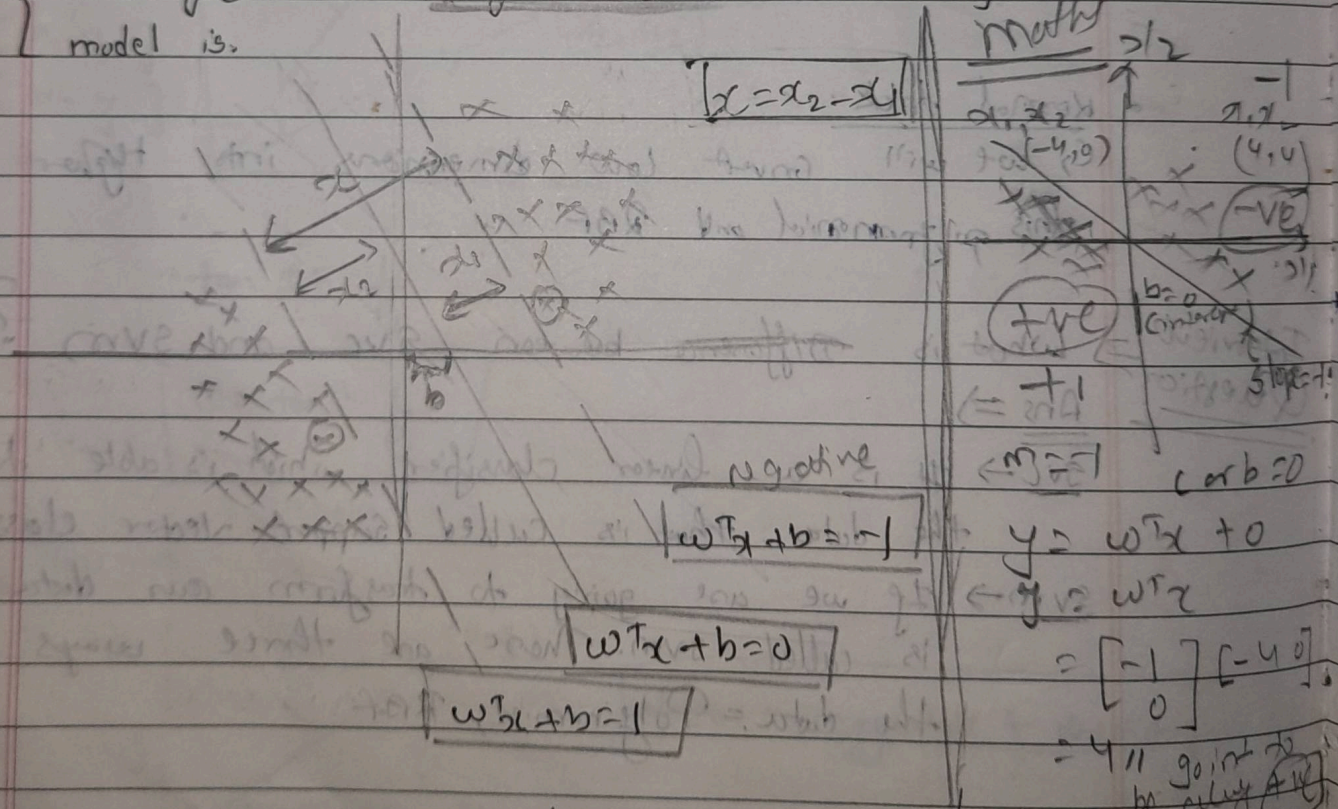


⇒ SVM creates 2 parallel hyperplanes in such a way that one of the hyperplane will be passing to the nearest (+ve) point and the other hyperplane will be passing to the nearest negative point.



→ SVM are the nothing but they are the points that passing through the marginal plane, Any no. of points that are passing through this particular marginal plane we will consider those as Support Vector

Note:- { The higher the marginal distance the more generalized our model is.



→ In order to compute the distance between two marginal distance.

$$y = w^T x + b$$

$$= \begin{bmatrix} -1 \\ 1 \\ 0 \end{bmatrix} \begin{bmatrix} -4 \\ 0 \end{bmatrix}$$

$$= -4 // \text{ point to be class +ve}$$

$$y = w^T x + b$$

$$= \begin{bmatrix} -1 \\ 1 \\ 0 \end{bmatrix} \begin{bmatrix} 4 \\ 0 \end{bmatrix}$$

$$= 4 //$$

Linear Algor $w^T x_1 + b = -1$
 $w^T x_2 + b = 1$

$w^T (x_2 - x_1) = 2$

This is my optimization function and we need to maximize this

$\frac{w^T (x_2 - x_1)}{\|w\|} = \frac{2}{\|w\|}$ ↑↑↑
 $\|w\| \leftarrow$ norm of w

update
 such that (w^*, b^*) max $\frac{2}{\|w\|}$
 such that
 Condition $y_i \begin{cases} +1 & w^T x_i + b \geq 1 \\ -1 & w^T x_i + b \leq -1 \end{cases}$

$y_i * w^T x_i + b_i \geq 1$

we can also represent like this also

$\Rightarrow (w^*, b^*) = \min \frac{\|w\|}{2} + C_i \sum_{i=1}^n \xi_i$

This we also call it Regularization

Include 2 terminology to optimize my model better

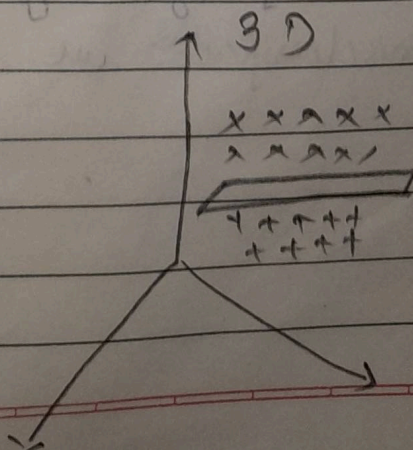
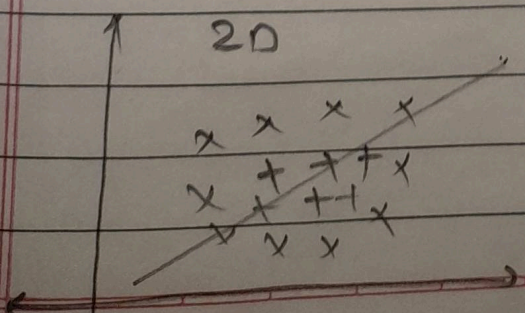
How many errors my model can consider? (misclassification data)

Value of the error (whatever distance i am getting with this approx I am just going to do summation)

* SVM Kernels \Leftrightarrow # convert into 2 Dim into 3 Dim

- ① Polynomial Kernel
- ② RBF Kernel
- ③ Sigmoid Kernel

Soft margin



Transformation can be done using {mathematical ~~equation~~ formula}

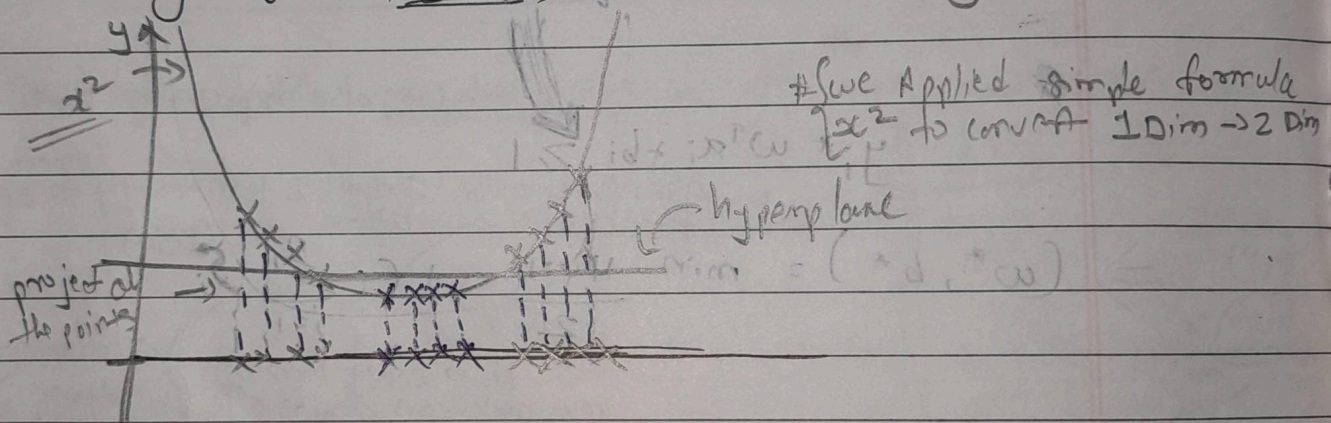
→ 1 dimension

f_1

~~xxxxx~~
Note:- If want to classify these two points, i can create one
hyperplane over here, but the "error will be v.v. high"
in order to classify this particular thing

Convert:- 1d \rightarrow 2d Then probably i will be able to probably
draw a hyperplane and try to split this particular data

Considering Equation, $y = f(x)$ this function is nothing but x^2



Types of Margin

↳ ① Soft Margin

↳ ② Hard Margin

Soft → In Soft Margin there will be some percentage of error.
Suppose my soft margin has an error of C ; C=3
(3 misclassification we can consider)

Polynomial Kernel

Independent x_1, x_2 Dependent y

we can write as

$$y = f(x_1, x_2)$$

$$f(x_1, x_2) = (x_1^T \cdot x_2 + 1)$$

dot product
transpose operation

vector operation

← dimensionality
identity matrix

$$= \begin{bmatrix} x_1 \\ x_2 \end{bmatrix} \cdot \begin{bmatrix} x_1 & x_2 \end{bmatrix}$$

$$= \begin{bmatrix} x_1^2 & x_1 x_2 \\ x_1 x_2 & x_2^2 \end{bmatrix}$$

from here we will take unique elements

This two Dim (x_1, x_2) now
becoming 5 dimensions

$$\begin{bmatrix} x_1 & x_2 & x_1^2 & x_2^2 & x_1 x_2 \end{bmatrix}$$

This are my all the features now, which i will probably using In order to convert, this into a Higher Dim and create a plane line

