

Assignment I

CH603

Molecular Geometry and Rotational Constant Analysis

1. Read the molecular cartesian coordinates and atomic numbers from the given file.

Hint 1: Opening and closing the file

Hint 2: Reading the number of atoms

Hint 3: Storing the z-values and the coordinates

2. Calculate all possible interatomic distances, R_{ij} .

$$R_{ij} = \sqrt{(X_i - X_j)^2 + (Y_i - Y_j)^2 + (Z_i - Z_j)^2}$$

Hint 1: Memory allocation

Hint 2: Loop structure

Hint 3: Printing the results

3. Calculate all possible bond angles. For example, the angle, ϕ_{ijk} , between atoms i-j-k, where j is the central atom is given by:

$$\cos \phi_{ijk} = e_{ji} \cdot e_{jk}$$

where the e_{ij} are unit vectors between the atoms, e.g.,

$$e_{ij}^x = -\frac{(X_i - X_j)}{R_{ij}} \quad e_{ij}^y = -\frac{(Y_i - Y_j)}{R_{ij}} \quad e_{ij}^z = -\frac{(Z_i - Z_j)}{R_{ij}}$$

Hint 1: Memory allocation

Hint 2: Avoiding a divide-by-zero

Hint 3: Memory allocation for the bond angles

Hint 4: Printing only unique non-zero angle

4. Calculate all possible out-of-plane angles. For example, the angle θ_{ijkl} for atom i out of the plane containing atoms j-k-l (with k as the central atom) is given by:

$$\sin \theta_{ijkl} = \frac{(\tilde{e}_{kj} \times \tilde{e}_{kl}) \cdot \tilde{e}_{ki}}{\sin \phi_{jkl}}$$

Hint 1: Decide do we need to store it.

Hint 2: Calculation of Cross products

Hint 3: Take care of the numerical precision to make sure that sin functions can only have values from -1.0 to +1.0

Hint 4. need to exclude ijk combinations involving coincidences among the indices as well as distant atom pairs:

5. Calculate all possible torsional angles. For example, the torsional angle τ_{ijkl} for the atom connectivity i-j-k-l is given by:

$$\cos \tau_{ijkl} = \frac{(\tilde{e}_{ij} \times \tilde{e}_{jk}) \cdot (\tilde{e}_{jk} \times \tilde{e}_{kl})}{\sin \phi_{ijk} \sin \phi_{jkl}}$$

Can you also determine the sign of the torsional angle?

Hint 1: Decide do we need to store it.

Hint 2: Take care of the numerical precision to make sure that sin functions can only have values from -1.0 to +1.0

Hint 3. Print only the unique dihedral angles and limit the printing only to atom pairs that are close together.

6. Find the center of mass of the molecule

$$X_{c.m.} = \frac{\sum_i m_i X_i}{\sum_i m_i} \quad Y_{c.m.} = \frac{\sum_i m_i Y_i}{\sum_i m_i} \quad Z_{c.m.} = \frac{\sum_i m_i Z_i}{\sum_i m_i}$$

where m_i is the mass of atom i and the summation runs over all atoms in the molecule

Hint 1: An excellent source for atomic masses and other physical constants is the [National Institute of Standard and Technology \(NIST\) website](https://www.nist.gov/patent/publications).

Hint 2: Use the masses of the most abundant isotope of each element

7. Calculate elements of the moment of inertia tensor.

$$I_{\alpha\alpha} = \sum_i m_i (\beta_i^2 + \gamma_i^2)$$

$$I_{\alpha\beta} = \sum_i m_i \alpha_i \beta_i$$

where α , β , and γ correspond to choices of x, y, and z (e.g., I_{xy} is one choice of $I_{\alpha\beta}$).

8. Diagonalize the inertia tensor to obtain the principal moments of inertia.

$$I_a \leq I_b \leq I_c$$

Hint 1: Use numpy for diagonalization

9. Determine the molecular type:

- diatomic
- linear polyatomic
- asymmetric top
- symmetric top (prolate or oblate)
- spherical top

10. Determine the moments of inertia in $\text{amu}\cdot\text{\AA}^2$ and $\text{g}\cdot\text{cm}^2$ and determine the rotational constants in cm^{-1} and MHz.

$$A \geq B \geq C$$
$$A = \frac{h}{8\pi^2 I_a} \quad B = \frac{h}{8\pi^2 I_b} \quad C = \frac{h}{8\pi^2 I_c}$$

test input and sample output can be found in the input and output directory. For more information see E.B. Wilson, J.C. Decius, and P.C. Cross, 'Molecular Vibrations', McGraw-Hill, 1955.

(Adapted from <https://crawford.chem.vt.edu>)