HOW TO USE:

// This is Python code. Color is from my IDE theme.

This is R code, with no styling. Sometimes, this is just pure English.

```
/*
This is SAS Code
*/
```

Read CSV

```
import numpy as np

data = pd.read_csv("/Users/gan/Desktop/Mods/ST2137/data/midterm_marks")

bats = pd.read_csv("/Users/gan/Desktop/Mods/ST2137/data/bats.csv", skiprows=[1,2]) # Skip

first 2 rows, keeping header

bats = pd.read_fwf("/Users/gan/Desktop/Mods/ST2137/data/ex_1_fixed.txt", widths=[2, 1, 3, 3, 1],

header=None) # Fixed width

data.columns = ["1st", "2nd"] # Must input all col names, no need assign back

data = df.rename(columns={'2nd' : "New name"}) # Rename specific column by comma

separated, must assign back

crab = pd.read_csv("/Users/gan/Desktop/Mods/ST2137/data/crab.txt", header=0,

delim_whitespace=True) # Treat any number of white space as 1
```

data = read.csv("/Users/gan/Desktop/Mods/ST2137/data/midterm_marks")

Read Excel

```
pinot = pd.read_excel("/Users/gan/Desktop/Mods/ST2137/Midterm/pinot_noir.xls")

# The rest like rename, and accessing, all same as above, read csv

install.packages("readxl")

library(readxl)

pinot = read_excel("/Users/gan/Desktop/zquiz1/pinot_noir.xls")

Just import normally
```

After importing csv, access the column called 'X'

```
df['x'] # df = pd.read_csv("), or use df.x

c2 = df[['height', 'weight', "gender"]] # Read multiple col, note the inner bracket

print(df.iloc[:, 0:2]) # Read first 2 col of df

data['x'][, 1] // data = read.csv("")

OR
data$x
```

Create Dataframe

```
data = {"1stCol": [1,2,3,4], '2ndCol':[5,6,7,8]}

df = pd.DataFrame(data, columns=['1stCol', '2ndCol'])

print(list(df)) # Get title, ['1stCol', '2ndCol']

matr = matrix( c(1:9), 3, 3)

df = data.frame(matr)

or df = data.frame(colname = matr)

names(df) = c("Col1", "Col2", "Col3")
```

;

Transformation of data

To transform

```
> tablets
                                                   4.07
   lab1 lab2 lab3 lab4 lab5 lab6 lab7
1 4.13 3.86 4.00 3.88 4.02 4.02 4.00
2 4.07 3.85 4.02 3.88 3.95 3.86 4.02
3 4.04 4.08 4.01 3.91 4.02 3.96 4.03
4 4.07 4.11 4.01 3.95 3.89 3.97 4.04
                                                   4.10
5 4.05 4.08 4.04 3.92 3.91 4.00 4.10
6 4.04 4.01 3.99 3.97 4.01 3.82 3.81
7 4.02 4.02 4.03 3.92 3.89 3.98 3.91
                                                   3.85
8 4.06 4.04 3.97 3.90 3.89 3.99 3.96
                                                   4.11
9 4.10 3.97 3.98 3.97 3.99 4.02 4.05
10 4.04 3.95 3.98 3.90 4.00 3.93 4.06
                                         into 16
                                                   4.01
```

amount = c(tablets\$lab1, tablets\$lab2, tablets\$lab3, tablets\$lab4, tablets\$lab5, tablets\$lab6, tablets\$lab7)

lab = c(rep(1, length(tablets\$lab1)), rep(2, length(tablets\$lab2)), rep(3, length(tablets\$lab3)), rep(4, length(tablets\$lab4)), rep(5, length(tablets\$lab5)), rep(6, length(tablets\$lab6)), rep(7, length(tablets\$lab7)))

newtablets = data.frame(amount = amount, lab = lab)

```
tablets = pd.read_csv("/Users/gan/Desktop/Mods/ST2137/data/tablets1.txt")
tablets.columns = ["lab1", "lab2", "lab3", "lab4", "lab5", "lab6", "lab7"]
amount = np.array([tablets.lab1, tablets.lab2, tablets.lab3, tablets.lab4, tablets.lab5, tablets.lab6,
tablets.lab7]).flatten()
x = [1, 2, 3, 4, 5, 6, 7]
lab = np.repeat(x, [len(tablets.lab1), len(tablets.lab2), len(tablets.lab3), len(tablets.lab4),
len(tablets.lab5), len(tablets.lab6), len(tablets.lab7)])
df = pd.DataFrame({"Amount": amount, "Lab": lab})
proc sql;
create table mysql table like tablets;
insert into mysql table
select * from tablets;
create table mysql_table2(
        amount numeric,
        lab numeric
);
```

```
insert into mysql_table2(amount, lab)
select Lab1, 1 from mysql_table
union all
select Lab2, 2 from mysql_table
union all
select Lab3, 3 from mysql_table
union all
select Lab4, 4 from mysql_table
union all
select Lab5, 5 from mysql_table
union all
select Lab6, 6 from mysql_table
union all
select Lab6, 7 from mysql_table
inion all
select Lab7, 7 from mysql_table
;
```

Add, replace, delete Dataframe

```
df.iloc[0:5, ] # First 5 rows

newCol = [9, 10, 11, 12]

df['NewColName'] = newCol # Add new col

df['ExistingName'] = newCol # Replace existing col with new values

del df['ExistingName'] # Delete existing column

df.loc[4] = [-1, -1, -1] # Replace row if index exist, else create the new index and insert the row

df.loc[len(df)] = [-2, -2, -2] # Append new row to the end

df = df.drop(df.index[2]) # Remove Row 3, must assign back
```

Merge

```
data = pd.read_csv()

newData = pd.read_csv()

data = pd.concat([data, newData], axis=1) # Add the 2 dataframe together by putting newData to new column, doesnt natural join

newData2 = pd.merge(df1, df2, on=['id', 'test']) # df1 JOIN df2 ON df1.id = df2.id AND df1.test = df2.test
```

Set value based on another value

```
@@@@ Method 1

df = pd.read_csv("/Users/gan/Desktop/Mods/ST2137/data/test.csv")

df['Grade'] = 'F' # Initialise all value, optional

df.loc[df.test > 50, "Grade"] = "D" # If df['test'] value > 50, set df['Grade']. Grade can be existing
```

```
df.loc[df.test > 60, "Grade"] = "C" # Set in descending order
@@@@ Method 2
grade2 = list()
for i in range(len(df)):
  if df['test'][i] >= 80:
     grade2.append("A")
  elif df['test'][i] >= 70:
     grade2.append("B")
     grade2.append("F")
df['Grade2'] = grade2
df['NewCol'] = c(10, 11, 12)
which(names(df) == 'Col3') # Return the index 3
df = df[, -2] \# Remove the 2<sup>nd</sup> col
df = df[, which(names(df) == 'Col3') * -1] # Remove the col called 'col3'
df = df[-2, ] # Remove the 2<sup>nd</sup> row
nrow(df) # Return number of rows of df
The rest all same as matrix
data mydata4;
        merge mydata mydata2;
        by id; /* Must be sorted */
run;
Create Matrix
matrix = np.array([[1,2,3,4,5],[6,7,8,9,10]])
matr = matrix(c(1,2,3,4,5,6,7,8,9,10), 2, 5)
     5
Accessing 2<sup>nd</sup> col:
matrix[:, 1] # [2 5 8]
matr[, 2]
Accessing 2<sup>nd</sup> and 3<sup>rd</sup> row:
matrix[1:3,]
```

```
matr[2:3, ]
```

Accessing (5, 8), i.e. 2nd and 3rd row of the 2nd col

```
matrix[1:3, 1] # [5 8]
```

matr[2:3, 2]

Add new rows to matrix (append to end):

```
matrix = np.vstack((matrix, [10, 11, 12])) # Does not affect original matrix
```

```
matr = rbind(matr, c(10, 11, 12)) # non-mutating
```

or matr = c(matr[1:1], c(10, 11, 12), matr[2:length(matr)])

```
/* Add mydata2 below mydata and save in mydata3. Can be use even if different number col
*/
DATA mydata3;
```

SET mydata mydata2;

RUN;

Add new rows to matrix after 1st row:

```
matrix = np.insert(matrix, 1, newMatrix, axis=0) # newMatrix can be multirow, or 1 row [10, 11,
```

matr = rbind(matr[1:1,], c(10, 11, 12), matr[2:nrow(matr),]) # non-mutating

Add new col to matrix (append to end):

```
matrix = np.column_stack((matrix, [10, 11, 12])) # Non-mutating
```

```
matr = cbind(matr, c(10, 11, 12)) # non-mutating
```

```
data mydata6;
       set work.mydata5;
       myNewCol = 3; /* If myNewCol is not defined then add new col. */
       if weight = "." then final grade="";
       else if weight > 65 then final grade="C";
       else final_grade="D";
run;
```

Add new col to matrix after 1st col:

```
matrix = np.insert(matrix, 1, [10, 11, 12], axis=1)
```

matr = cbind(matr[, 1:1], c(10, 11, 12), matr[, 2:ncol(matr)]) # non-mutating

Delete the 3rd col:

```
matrix = np.delete(matrix, 2, axis=1) # Non-mutating
```

matr[, -3] # non-mutating

Delete the 3rd row:

```
matrix = np.delete(matrix, 2, axis=0) # Non-mutating
```

matr[-3,] # non-mutating

```
Filter
bats = pd.read_csv("/Users/gan/Desktop/Mods/ST2137/data/bats.csv")
print(bats) # All the dataframe
print(bats[bats['type'] == 1]) # Dataframe where type == 1
print(bats['energy'][bats['type'] == 1]) # The energy content where type == 1
k = student[(student.workhour > 0) & (student.workhour < 20)]
k = [1, 2, 3, 4]
print(list(filter(lambda x: x > 2, k))) # Method 1 => [3, 4]
k = np.array(k)
print(np.where(k > 2)[0]) # Method 2 => [2 3] impt for [0] to get array() element out
bats = read.csv("") # Have column energy, mass, type
attach(bats) # Now we can access energy, mass, type directly
energy # [43, 44, 23, ...., 1.02]
type # [1 1 1 1 2 2 1 1 .... 3]
energy[which(type == 1)] # [43, 44] Give those energy whose type is 1
    ■ Alternatively, don't attach:
    bats['energy'][which(bats['type'][, 1] == 2), 1] # Find type 2
EASY WAY:
# Give those energy whose type is 1:
bats$energy[bats$type == 1]
# Select all the df rows and all col where type == 1
bats[bats$type == 1,]
DATA mydata;
       SET height weight;
       WHERE gender="M" AND weight > 60;
        KEEP id; /* Col name */
       /* DROP id; */
RUN;
Number of rows:
print(matrix.shape[0]) # 3, also applies to df from Panda, numpy array
```

nrow(matr)

```
To limit number of rows when saving:

DATA ..

SET ..

IF _n_ > 5 THEN /* Only save 5 rows. _n_ refers to each of the row name. */

STOP;

RUN;
```

Number of col:

```
print(matrix.shape[1]) # 3, Also applies to df from Panda, numpy array
```

ncol(matr)

Mean

```
np.mean(data) # 18.25
```

mean(data)

```
proc means data=work.pinot mean var std Q1 Median Q3 min max;
var Quality;
run;
```

Median

```
np.median(data) # 18.25
```

median(data)

```
proc means data=work.pinot mean var std Q1 Median Q3 min max;
var Quality;
run;
```

Mode

```
import scipy.stats as sc
print(sc.mode([1,2,3,3])) # ModeResult(mode=array([3]), count=array([2]))

getmode <- function(v) {
    uniqv <- unique(v)
    uniqv[which.max(tabulate(match(v, uniqv)))]
}

proc means data=work.pinot mean var std Q1 Median Q3 min max mode;
    var Quality;
run;</pre>
```

Trimmed Mean

Sort data, then take out x% top and x% bottom, then calculate remaining mean.

```
import scipy.stats as sc
print(sc.trim_mean(bats.energy, 0.2)) # 20% trimmed mean
```

mean(bats\$energy, trim=0.2) # 20% trimmed

```
proc univariate data=pinot trimmed=0.4;
var Quality;
ods select TrimmedMeans;
run;
```

Winsorized Mean

Sort data, take out x% top and x% bottom and replace them with the min value of the remaining data and the max value of the remaining data.

```
import scipy.stats as sc
```

print(np.mean(sc.mstats.winsorize(bats.energy, [0.2, 0.2]))) # 20% Winsorized mean

library(psych)

winsor.mean(bats\$energy, 0.2)

```
proc univariate data=pinot winsorized=0.2;
var Quality;
ods select WinsorizedMeans;
run;
```

MAD Median Absolution Deviation

```
# Either will do
```

mad = sc.median_abs_deviation(heats.heat, scale=1)

mad2 = np.median(np.absolute(heats.heat - np.median(heats.heat)))

mad(heats\$heat, scale=1)

Percentile

np.percentile([1,2,3,4,5], 25) # 2.0

quantile(c(1,2,3,4,5), 0.25)

```
proc univariate data=pinot noprint;
var Quality;
output out=data1 pctlpre=P_ pctlpts= 30, 50, 75 to 100 by 5;
run;
proc print data=data1;
run;
```

Matrix Transponse

matrix.T # Shape (5, 2)

t(matr) // dim(matr) is 2 5

Matrix Inverse

```
## True if matr is invertible, false otherwise
print(matr.shape[0] == matr.shape[1] and np.linalg.matrix_rank(matr) == matr.shape[0])
## Inverse of matr
inverse = np.linalg.inv(matr)
print(inverse)
solve(matrixsq)
```

Variance

Range of values

```
c(1:9) # 1 2 3 4 5 6 7 8 9
seq(from=1, to=10, by=2) # 1 3 5 7
np.arange(1, 10) # 1 2 3 4 5 6 7 8 9
np.arange(3, 7, 2) # 3 5
```

Replicate

```
rep(c(1, 2, 3), c(4, 5, 6)) # 1 1 1 1 1 2 2 2 2 2 3 3 3 3 3 3
```

```
x = [1, 2, 3]
y = np.repeat(x, [4, 5, 6])
print(y) # [1 1 1 1 2 2 2 2 2 3 3 3 3 3 3]
```

or

```
lab = [[1]*len(tablets.lab1), [2]*len(tablets.lab2), [3]*len(tablets.lab3), [4]*len(tablets.lab4), [5]*len(tablets.lab5), [6]*len(tablets.lab6), [7]*len(tablets.lab7)]
lab_flatten = sum(lab, [])
```

Tilde / Tilda ~

Tilde operator is used to define the relationship between dependent variable and independent variables in a statistical model formula. The variable on the left-hand side of **tilde** operator is the dependent variable and the variable(s) on the right-hand side of **tilde** operator is/are called the independent variable(s).

Sort

np.sort(ran)

```
sort(ran)
```

```
proc sort data=mydata;
by id;
/* by descending id; */
run;
```

Reverse

arr[::-1] # View of original

arr[length(arr):1] # non-mutating
OR
rev(arr) # non-mutating

Copy

arr2 = np.copy(arr)

matr2 = matr # matr2 and matr are 2 separate copies with same values

Unique

```
arr = np.array([1,1,1,2,3])

print(np.unique(arr)) # [1 2 3]

unique(c(1,1,1,2,3))
```

Skew

from scipy.stats import skew

skew(marks)

install.packages("moments")
library(moments)
skewness(marks) # -0.4140474
OR use psych

Kurtosis

from scipy.stats import kurtosis

kurtosis(marks) # -0.6752517

install.packages("psych")
library(psych)
describe(marks)\$kurtosis

ggplot

```
# Plot a bar chart
ggplot(iris, aes(x = Sepal.Length)) + geom_bar()
# Add label
ggplot(iris, aes(x = Sepal.Length)) + geom_bar() + labs(title = 'Hey', x = 'Length', y = 'Money')
```

```
# Add fill
ggplot(iris, aes(x = Sepal.Length, fill = Species)) + geom bar()
# Plot 3 graphs by Species (since theres 3 species)
ggplot(iris, aes(x = Sepal.Length)) + geom_bar() + facet_wrap(~ Species)
# Box plot by Species
ggplot(iris, aes(x = Species, y = Sepal.Length)) + geom boxplot()
# scatter plot separated by 2 types
ggplot(testscore) + geom point(aes(x = A, y = B, color = "Male"), data=subset(testscore,
testscore$gender == "M"), shape=19) + geom point(aes(x = A, y = B, color="Female"),
data=subset(testscore, testscore$gender == "F"), shape=24) + scale color manual(name =
"Gender", values = c("red", "blue")) + guides(color = guide legend(override.aes =
list(shape=c(24, 19))))
# Convert a continuous variable into categorical:
Bats$species = as.factor(Bats$species)
newtablets['lab'] = newtablets['lab'].astype(object)
Histogram
import matplotlib.pyplot as plt
plt.hist(marks)
plt.title("Histogram Title")
plt.xlabel("Bottom axis")
plt.ylabel("Side axis")
plt.show()
hist(marks)
hist(marks, freq=F) # Shows the pdf
plot(ecdf(marks)) # CDF
# To add a PDF of normal not using ggplot:
hist(marks, freq=F)
curve(dnorm(x, mean(marks), sd(marks)), 3, 10, add=T) # Here x is nothing, just x. 3 10
means from x value of 3 to 10
proc univariate data=work.pinot;
       var Aroma; /* Can choose more than 1 var */
       /* Choose one of the following */
       histogram; /* Pure histogram of Aroma */
       histogram / normal; /* Add a normal dist with mu=mean(Quality) sigma=sd(Quality)
*/
       histogram / normal(color=red mu=13 sigma=2.1);
```

Using ggplot:

run;

```
data = c()
data_F = data.frame(data)
ggplot(data_F) + geom_histogram(aes(x = VARNAME, y = ..density..), binwidth = 30)
## To add PDF of Normal
x_range = seq(min(data) - 30, max(data) + 30, length.out = length(data))
y_values = dnorm(x_range, mean(data), sd(data))
ggplot()... + geom_line(aes(x = xrange, y = y_values))
```

Boxplot

```
import matplotlib.pyplot as plt
plt.boxplot(marks)
plt.title('Histogram')
plt.xlabel('Marks')
plt.ylabel('Values')
plt.show()
```

or use panda

```
bats = pd.read_csv("/Users/gan/Desktop/Mods/ST2137/data/bats.csv")
bats.boxplot(column='energy', by='type')
plt.show()
```

Multiple boxplot:

```
fig = plt.figure()

ax1 = fig.add_subplot(121)

bats.boxplot(column="energy", ax=ax1, grid=False)

ax1.title.set_text("Boxplot of all bats")

ax1.set_xlabel("All bats")

ax1.set_ylabel("Energy")

ax2 = fig.add_subplot(122)

bats.boxplot(column="energy", by="type", ax=ax2, grid=False)

ax2.title.set_text("Boxplot separated by Bats type")

ax2.set_xlabel("Bats type")

ax2.set_ylabel("Energy")

fig.suptitle("Overall Title")

plt.show()
```

boxplot(marks, xlab = "mark")

```
##
ggplot(iris) + geom_boxplot(aes(x = Species, y = Sepal.Length))
```

```
proc sgplot data=pinot noautolegend;
  vbox Quality / category=Region; /* Boxplot separated by region */
run;
```

Multiple box plot separate by a type

```
bats = read.csv("") # Bats have the column energy, type, mass
boxplot(bats['energy'][,1] ~bats['type'][, 1]) # Group by type, show the value for energy
## or ggplot:
ggplot(bats, aes(x = type, y = energy)) + geom_boxplot()
```

QQ Plots

Scatter Plot

```
import matplotlib.pyplot as plt
midterm = pd.read_csv("/Users/gan/Desktop/Mods/ST2137/data/midterm_marks")
midterm = midterm['x']
final = pd.read_csv("/Users/gan/Desktop/Mods/ST2137/data/final_marks")
final = final['x']
plt.scatter(midterm, final)
plt.xlabel('Height')
plt.ylabel('Weight')
plt.title('Weight vs Height')
plt.show()
plot(midterm, final)
OR
ggplot(..) + geom_point(aes(x = midterm, y = final))
# Scatter plot with line of best fit:
```

```
ggplot(data=ex10) + geom_point(aes(x=weight, y=height)) + geom_smooth(aes(x=weight, y=height), method='lm', formula= y^{x})
```

```
proc sgscatter data=ex10;
plot height * weight; /* Y*X */
run;
```

Scatter plot separated by category:

```
/* Scatter plot separated by gender */
proc sgscatter data=ex10;
/* Y*X */
plot height * weight / datalabel=gender group=gender;
run;

/* More colourful version */
ods graphics on / attrpriority=none;
proc sgplot data=crab;
title 'Scatter plot of Width and Weight classified by Spine condition ';
styleattrs datasymbols=(circlefilled squarefilled starfilled);
scatter x=width y=weight / group=spine markerattrs=(size=10px);
run;
ods graphics / reset;
```

Scatter plot with line of best fit:

```
proc sgplot data=ex10 noautolegend; reg x=weight y=height; run;
```

Superimpose Plot

```
x = np.arange(1, 31) # 1 to 30
y1 = x * 1
y2 = x * 2
y3 = x * 3
# Plot 3 lines in the same graph
plt.plot(x, y1, color="red") # Plot vales of x from 1-30, and value of y as x
plt.plot(x, y2, color="blue") # Plot vales of x from 1-30, and value of y as x*2
plt.plot(x, y3, color="green") # Plot vales of x from 1-30, and value of y as x*3
plt.show()
```

Plot histogram and PDF

```
plt.hist(df['test'], bins=5, density=True)

x = np.arange(0, 110)

y = sc.norm.pdf(x, loc=np.mean(df['test']), scale=np.sqrt(np.var(df['test'])))

plt.plot(x, y)

plt.show()
```

Plot 2 scatter plot separated by type onto same graph, with legend

```
plt.scatter(gasoline['x10'][gasoline['x11'] == 1], gasoline['y'][gasoline['x11'] == 1], color="red",
marker="x", label="Manual")

plt.scatter(gasoline['x10'][gasoline['x11'] == 0], gasoline['y'][gasoline['x11'] == 0], color="blue",
marker="o", label="Auto")

plt.legend(loc="upper right")

plt.show()

In R:

eq = function(x) x

curve(eq, 1, 10) # Draw a straight line, from 1 to 10. Can't use anonymous function.

curve(eq, 1, 10, add=T) # Draw a straight line on existing graph

# Using ggplot:

x_range = seq(1, 10, length.out=length(data$data)

y_range = x_range * 2

ggplot() ... + geom_line(aes(x = x_range, y = y_range)) # Draw (x, x*2) line
```

Settings for multiple Plots

```
bats = pd.read_csv("/Users/gan/Desktop/Mods/ST2137/data/bats.csv")

### Use the method ax1 below, if you want to have xlabel, ylabel, and title

plt.subplot(1, 3, 1)

plt.hist(bats['energy'][bats['type'] == 1], density=True, label="Type 1") # Show Energy probability

for Type 1

plt.subplot(1, 3, 2)

plt.hist(bats['energy'][bats['type'] == 2], density=True, label="Type 2")

plt.subplot(1, 3, 3)

plt.hist(bats['energy'][bats['type'] == 3], density=True, label="Type 3")

plt.show()
```

Subplot with add subplot, and label

```
fig = plt.figure()

ax1 = fig.add_subplot(121)

ax1.title.set_text("Male")

ax1.set_xlabel("X label")

ax1.set_ylabel("Y label")

ax1.scatter(testscore.A[testscore.gender == "M"], testscore.B[testscore.gender == "M"],

marker="x", color="red", label="Male")

ax2 = fig.add_subplot(122)
```

```
ax2.title.set_text("Female")
ax2.set_xlabel("X label")
ax2.set_ylabel("Y label")
ax2.scatter(testscore.A[testscore.gender == "F"], testscore.B[testscore.gender == "F"],
marker="o", color="blue", label="Female")
plt.show()
par(mfrow=c(2, 2)) # 2 by 2 graph
# To use ggplot on multiple side by side:
install.packages("gridExtra")
library(gridExtra)
plot1 = ggplot(..) + ...
plot2 = ggplot(..) + ...
grid.arrange(plot1, plot2, ncol=2) # Put 2 gg plot side by side
Frequency Table (of 1 categorical variable)
A table that shows the total count, e.g.
Table---
Female: 99
Male: 79
Also plot a frequency table. This is slightly different from histogram in the sense histogram
may group values together, but frequency table does not group together values.
bats = pd.read_csv("/Users/gan/Desktop/Mods/ST2137/data/bats.csv")
```

```
bats = pd.read_csv("/Users/gan/Desktop/Mods/ST2137/data/bats.csv")

tab = pd.crosstab(index=bats.type, columns="Counts")

print("Frequency table of Bats Type")

print(tab) # Tabular form

plt.bar(tab.index, np.array(tab).flatten())

plt.title("Frequency table of Bats Type")

plt.xlabel("Bats Type")

plt.ylabel("Count")

plt.show()

freq_table = table(bats$type)

barplot(freq_table)

OR

gendergp <- ifelse(gender=="F","Female","Male")

# for every observation in gender, if F then label as Female, else label as Male
```

Correlation Coefficient

np.corrcoef(midterm, final)[0, 1] # 0.7778, Must put [0,1] becos output is a 2x2 matrix

k = np.corrcoef(np.array([ex10.height, ex10.weight, ex10.age])) # > 2 variables

```
# Plot line of best fit
```

```
x = bats.energy[bats.type == 2]
y = bats.mass[bats.type == 2]
plt.plot(np.unique(x), np.poly1d(np.polyfit(x, y, 1))(np.unique(x)), color='blue')
C1 = c(1,2,3,4,5)
C2 = c(6,20,8,9,10)
cor(C1, C2) # -0.08689
cor(cbind(ex10$height, ex10$weight, ex10$age)) # If we want > 2 variables
proc corr data=ex10 nosimple;
title "Correlation Coefficient";
var height weight age;
run;
```

Function declaration

```
def myfunc(x, y):
    return x * y

myfunc = function(x, y) {
        return(x * y)
}
```

For loop

```
k = [1,2,3,4,5]
for (index, data) in enumerate(k):
    print(str(index) + ": " + str(data))
for(i in 1:10) {
        data = i
        index = which(data == i) # only if data is unique
}
```

If-else

```
if ave_mark >= 90 and HW = "A" then final_grade = "A";
else if ave_mark >= 85 then final_grade = "B";
else final_grade = "C";
```

Normal Distribution fn

```
import scipy.stats as sc
sc.norm.ppf(0.5) # Equivalent to qnorm(0.5)
```

qnorm(0.5) # 0. Returns the output where P(X < output) = Input. i.e. input is the area, output is the point.

qnorm(x, mean, sd), e.g. qnorm(0.5, 25, 20). No mean and sd, assume to be standard norm.

import scipy.stats as sc

sc.norm.cdf(0.2) # Equivalent to pnorm(0.2)

pnorm(q, mean, sd), e.g. pnorm(0) returns 0.5. I.e. P(X < input) = output (area).

sc.norm.pdf(x, loc=np.mean(df['test']), scale=np.sqrt(np.var(df['test'])))

Equivalent to dnorm

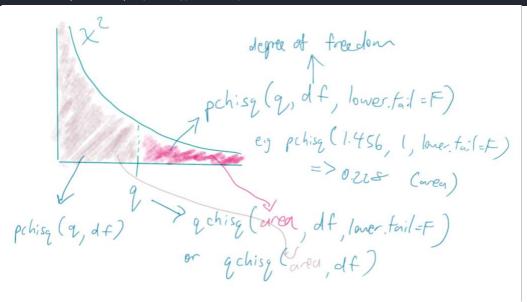
dnorm gives the y-value at the input x-value. E.g. dnorm(0) = 0.3984, i.e. the y-value at the point x = 0.

Chi-square

import scipy.stats as sc

sc.chi2.ppf(0.7724, 1) # qchisq(0.7724, 1)

sc.chi2.cdf(1.456, 1) # pchisq(1.456, 1)



par(mfrow=c(2, 2)) # 2 by 2 graph plot(xxx) # Will be at 1,1 plot(xxx) # Will be at 1,2

Student t

import scipy stats as sc

sc.t.ppf(0.3, 2) # qt(0.3, 2)

sc.t.cdf(0.3, 2) # pt(0.3, 2)

?dt, pt, qt, rt

Same definition as normal dist above.

F distribution

sc.f.cdf(F0, 1, len(x) - 2) # pf(x, df1, df2)

?df, pf, qf, rf

Ask user input

```
while True:
  try:
    userInput = input("Enter input")
    userInput = float(userInput)
    break
  except ValueError:
     pass
print(userInput)
 total cost = NA
 while (length(total cost) == 0 || is.na(total cost) || total cost <= 0) {
  print("Please enter the cost of your dream home in positive numbers: ")
  total_cost = scan("", what="", nmax=1)
  total_cost = suppressWarnings(as.numeric(total_cost))
 print(total_cost)
}
Export
```

```
df.to_csv("/Users/gan/Desktop/Mods/ST2137/data/MINE.csv")
df.to_csv("/Users/gan/Desktop/Mods/ST2137/data/MINE.txt", sep="\t')
write.csv(df, "path")
write.table(df, "path", sep='t')

/* Or just open snippets -> Generate csv file */
proc export data=work.pinot
    outfile="/folders/myshortcuts/Working_Folder/testout2.csv"
    dbms=csv replace;
run;
```

SAS output value to another table

ods output WinsorizedMeans=winMeans;

Useful Packages

```
install.packages("psych")
library(psych)
describe(df or arr or matr) # Get list of useful things
```

Print

```
proc print data = subset heat;
```

Response vs Explanatory

Response is y-axis. Explanatory is x-axis. Explanatory cause response to change. Regressor is X, i.e. regressor is explanatory to the target variable (response) Y.

Hypothesis Testing

Rules:

- 1. State assumptions
- 2. State hypothesis H0 H1
- 3. Measure test statistic
- 4. Calculate p-value. Reject H0 if p-value is small.
- 5. Conclude

Chi-square Test (Expected count > 5, 2 categorical variables)

- 1. Assumption: The expected count in all cells are > 5 (<5 use fisher exact test). Applicable to r x c table, not necessarily must be 2x2. Note, does not care about order, hence ordinal variable ordering is ignored. We find the frequency count of the categorical variable, and put them into the table.
- 2. Hypothesis. H0: The two variables are independent vs. H1: The two variables are dependent.
- 3. Calculate test statistics.

$$\mathsf{Expected} \ \mathsf{count} = \frac{\mathsf{Row} \ \mathsf{total} \times \mathsf{Column} \ \mathsf{total}}{\mathsf{Total} \ \mathsf{sample} \ \mathsf{size}}$$

The formula χ^2 test statistic (with continuity correction) is:

$$\chi^2 = \sum \frac{(|\text{observed count} - \text{expected count}| - 0.5)^2}{\text{expected count}}.$$

Note that there are variations on this formula in other books/documents.

degree of freedom: (r-1)(c-1)

,		Chest Pain		No Chest Pain		Total
Mal	e	40.2	46	479.8	474	520
Fem	ale	3 42.8	37	510.2	516	553
Tota	al	83		990		1073
All the expected o	ounts	are larger	tha	n 5.		2





• Conclusion: Data do not provide enough evidence against H_0 ; At $\alpha = 0.05$,

import scipy.stats as sc

data = np.array([[46, 474], [37, 516]]) # Original data, not expected count

```
test_statistic, p_value, dof, expected_count = sc.chi2_contingency(data, correction=True) # Also
applicable to table larger than 2x2
print("Test Statistic:", test_statistic)
print("P-value:", p_value)
print("Degree of freedom:", dof)
print("Expected Count:", expected_count) # Make sure all values are > 5
print("All values of expected count are > 5:", np.all(expected_count > 5))
```

To get p-value and test-statistic:

chestpain = matrix(c(46, 37, 474, 516), 2, 2) # Can also be larger than 2x2 table chisq.test(chestpain) #chestpain is the original 2x2 matrix, not expected count matrix ## To find residual:

chisq.test(politician)\$stdres # See page 43 of Topic6 to find out meaning of residual. ## To find expected count of each cell:

chisq.test(politician)\$expected

- 4. See p-value
- 5. Conclude. If p-value < alpha (0.05), reject H0. Else, do not reject H0.

```
/* Reformat data in this way */
data cp3;
input gender $ chest_pain $ Count;
datalines;
M yes 46
M no 474
F yes 37
F no 516
;

/* Look for chisq or continuity adjusted chisq row */
proc freq data=cp3 order=data;
    weight count;
    tables gender*chest_pain / chisq;
run;
```

Fisher Exact Test (Expected count < 5, categorical variables)

- 1. Assumption. No need expected count in cell to be > 5. ONLY for 2x2 table.
- 2. Same hypothesis as chi-square test above. H0: The two variables are independent vs. H1: The two variables are dependent.
- 3. Calculate p-value.

```
import scipy.stats as sc
# Data:
# 4 184
```

```
#2 260
claritin = np.array([[4, 184], [2, 260]]) # Original data, not expected count
result = sc.fisher_exact(claritin, alternative="two-sided")
p_value = result[1]
print("P-value:", p_value)
# Data:
# 4 184
# 2 260
claritin = matrix(c(4, 2, 184, 260), 2, 2) # Data is original, not the expected count data
fisher.test(claritin) # Get p-value
```

```
/* Reformat data in this way */
data cp3;
input gender $ chest_pain $ Count;
datalines;
M yes 46
M no 474
F yes 37
F no 516
;

/* Look for fisher's exact test p_value*/
proc freq data=cp3 order=data;
    weight count;
    tables gender*chest_pain / chisq;
run;
```

Linear by Linear Association Test (2 ordinal categorical variables)

- 1. Assumption. We use this for 2 ordinal variables (where order matters). No need sort, but make sure corresponding row scores are correct.
- 2. Hypothesis H0: Two variables are independent vs H1: Two variables are dependent. Can also consider H1: Association between two variables is positive/negative.

```
def linear_by_linear_test(data, row_scores, col_scores, alternative="two.sided"):
    data = np.array(data)
    col_scores = np.array(col_scores)
    row_scores = np.array(row_scores)
    nrow = data.shape[0]
    ncol = data.shape[1]
    rsum = np.sum(data, axis=1) # row sums
    csum = np.sum(data, axis=0) # column sum
```

```
n = np.sum(data) # total cell counts
  rowp = rsum / n # margin prob for rows
  colp = csum / n # margin prob for columns
  ubar = np.sum(row_scores * rowp) # weighted average scores for rows
  vbar = np.sum(col_scores * colp) # weighted average scores for columns
  numerator = 0
  for v in range(ncol):
     for u in range(nrow):
       numerator = numerator + (row_scores[u] - ubar) * (col_scores[v] - vbar) * (data[u, v] / n)
  V1 = np.sum((row_scores - ubar)**2 * rsum / n) # weighted variance for rows' scores
  V2 = np.sum((col_scores - vbar)**2 * csum / n) # weighted variance for columns' scores
  r = numerator / np.sqrt(V1 * V2) # weighted correlation
  M = np.sqrt(n - 1) * r # Normalized test statistic
  M2 = M^{**}2
  if alternative == "two.sided":
     p_value = 1 - sc.chi2.cdf(M2, 1)
  elif alternative == "less":
     p_value = sc.norm.cdf(np.abs(M))
  else:
     p_value = 1 - sc.norm.cdf(np.abs(M))
  return M2, p_value
data = np.array([[17066, 48], [14464, 38], [788, 5], [126, 1], [37, 1]])
print(data)
print("LINEAR:")
print(linear_by_linear_test(data, [0, 0.5, 1.5, 4, 7], [0, 1]))
## Using package COIN:
Input =(
"MI
         Absent Present
Alcohol
```

```
Zero
         17066
                    48
                      38
Below.1
          14464
1-2
          788
                   5
3-5
          126
                   1
          37
>6
                  1
")
set = as.table(read.ftable(textConnection(Input)))
set
library(coin)
test = lbl test(set,scores = list(MI = c(0,1), Alcohol = c(0,0.5,1.5,4,7)))
```

One sample t-test (Parametric, Quantitative)

- 1. Assumption: Sample taken randomly. Sample follows or approx. Normal dist, or sample size > 30.
- 2. Hypothesis: Population mean $\mu = 3.3$ vs $\mu != 3.3$
 - 3. Test statistic:

$$T = \frac{\bar{X} - \mu_0}{\text{s.e}(\bar{X})} = \frac{3.208 - 3.3}{\sqrt{0.2564/47}} = -1.2456, \quad \text{=-1.246786}$$

where μ_0 is the value of parameter μ under H_0 .

Under H0, test statistic T follows t-dist with t(n-1) degree of freedom

```
from scipy import stats

test_statistic, p_value = sc.stats.ttest_1samp(baby.weight, popmean=3.3) # 2-sided p-value

df = len(baby.weight) - 1 # Degree of freedom

one_sided_left_p_value = sc.t.cdf(test_statistic, df)

one_sided_right_p_value = 1 - sc.t.cdf(test_statistic, df)

print("Test statistic: ", test_statistic)

print("2-sided test P-value:", p_value)

print("1-sided-left test P-value:", one_sided_left_p_value)

print("1-sided-right test P-value:", one_sided_right_p_value)

conf_interval_95 = sc.t.interval(0.95, df=df, loc=np.mean(baby.weight),

scale=sc.sem(baby.weight))

print("95% confidence intervale:", conf_interval_95)

# Draw it out

# x = np.linspace(test_statistic - 5, test_statistic + 5)
```

```
x = np.linspace(test_statistic - 5, test_statistic + 5, 100)
y = sc.t.pdf(x, df)
plt.plot(x, y)
plt.fill_between(x, y, where=(x < -1 * np.abs(test_statistic)), color="orange")
plt.fill_between(x, y, where=(x > np.abs(test_statistic)), color="orange")
plt.title("2 sided t-Test with " + str(df) + " degrees of freedom" + "\nTest-statstic: " +
str(test_statistic) + "\np-value: " + str(p_value))
plt.xlabel("x-values")
plt.ylabel("Density")
plt.show()
t.test(pinot$Quality, mu=13) # 2-Sided
t.test(pinot$Quality, mu=13, alternative="less") # Left-sided
t.test(pinot$Quality, mu=13, alternative="greater") # Right-sided
t.test(pinot$Quality, mu=12, conf.level=0.9) # Same p-value, just show different conf.level
Calculate manually:
test statistic = (mean(pinot$Quality) - 13) / (sqrt(var(pinot$Quality) / length(pinot$Quality)))
p-value = pt(test statistic, length(pinot$Quality) - 1) # Left-sided
proc univariate data=work.pinot mu0=13;
       var Quality;
       /* Then read the table Test for location -> Student's t. Note it is default 2-sided */
run;
# To get 1-sided left or right:
proc univariate data=work.pinot mu0=13;
       var Quality;
       ods output TestsForLocation=TestsForLocation;
       /* Then read the table Test for location -> Student's t. Note it is default 2-sided */
run;
```

```
data result;
set TestsForLocation(obs=1);
one_sided_left_pvalue=cdf('T', Stat, 37); /* DF is n-1 */
one_sided_right_pvalue=1-cdf('T', Stat, 37); /* DF is n-1 */
put one_sided_left_pvalue=one_sided_right_pvalue=;
run;

/* Run this independently to get the p-value */
proc print data=result;
    var one_sided_left_pvalue;
    var one_sided_right_pvalue;
run;
```

- 4. See p-value as above.
- 5. Reject H0 if p-value is small.

One Sample Sign Test (Non-parametric, quantitative)

- 1. No need assume sample from normal. No need to have large sample size.
- 2. Hypothesis: H_0 : Population Median = 3.3 vs H_1 : Population Median < 3.3
 - \bullet A sample of size n is randomly collected from population: $x_1,x_2,...,x_n$ that is skewed. We want to test

```
H_0 : population median = m_0 vs H_1 : population median \neq m_0
```

- We'll assign the sign (+ or -) to each data point: if $x_i > m_0$ then x_i has + sign; if $x_i < m_0$ then x_i has sign; if $x_i = m_0$ then no sign is given and the sample size will be reduced. If datapoint == m0 then exclude it
- \bullet The total number of positive sign is counted, V+; and the total number of negative sign is V-.
- We then take the test statistic $V = \min(V+, V-)$.
- This test statistic follow Binomial distribution $Bin(n^*,0.5).$ $n^*=n$ number of data points that are equal to $m_0.$
- p-value is then calculated (2 tails probability for the 2 sided test).
- 3. Compute test statistics

H0 = Median is 3.3 vs H1: Median < 3.3

```
import scipy.stats as sc
success_weight = baby.weight[baby.weight < 3.3]
failure_weight = baby.weight[baby.weight > 3.3]
p_value = sc.binom_test(x=[len(success_weight), len(failure_weight)], p=0.5, alternative="less") #
alternative="less" "greater" "two-sided"
print(p_value)
success.weight = baby$weight[baby$weight < 3.3]</pre>
```

success.weight = baby\$weight[baby\$weight < 3.3]
failure.weight = baby\$weight[baby\$weight > 3.3]
binom.test(x = c(length(success.weight), length(failure.weight)), alternative="less")

proc univariate data=work.pinot mu0=13;
var Quality;
/* Then read the table Test for location -> Sign. Note it is default 2-sided. If it is 1.0 then too bad =(*/ run;

- 4. Calculate p-value as above.
- 5. Conclude.

Wilcoxon Signed Rank Test One Sample (Non-parametric, quantitative)

- 1. No need assume sample from normal. No need have large sample.
- 2. Hypothesis: H_0 : Population Median = 3.3 vs H_1 : Population Median < 3.3
- 3. Compute test statistic
 - Hypotheses:

 H_0 : population median $= m_0$ vs H_1 : population median $\neq m_0$

- The difference of data point and m_0 is calculated $x_i m_0$ and give the sign accordingly, they are $d_i(+)$ or $d_i(-)$.
- V+ is the sum of all the positive differences. V- is the sum of all the negative difference.
- $\begin{array}{l} \bullet \text{ The idea behind the test is that if } V+\approx V-\underset{\text{x1, x2, ..., x10}}{\text{therf-lighted easigned -9 becos x1-m0}} \underset{\text{cassigned -9 becos x1-m0}}{\text{e--9}} \\ & \xrightarrow{\text{therf-lighted behind}} H_0. \end{array}$

x8 assigned 0, ignored

- If V+ is much greater (lesser) than V-, then we will be evidence that the median is greater (lesser) than the hypothesised, value of them to find the rank.
- This test is stronger than the sign test.

 Test statistic is V+

Thin, we take absolute value of them to find the rank. Rank is smallest to largest. So e.g. 49=1 is rank 1, x10=2 is rank 2, ... x2=i81 = rank 8, x1=i91 = rank 9. Assuming no tie in ranking. Then, we assign sign back to them again, so x10=rank +2, x9= rank+1, x1=rank -9. Then, V+ is sum of all positive rank to be the test statistic.

```
import scipy.stats as sc
m0 = 3.3
# 2-sided:
test_stastic, p_value = sc.wilcoxon(x=baby.weight-m0, y=None, zero_method='wilcox',
correction=False)
# Left-tail:
# test_stastic, p_value = sc.wilcoxon(x=baby.weight-m0, y=None, zero_method='wilcox',
correction=False, alternative="less")
# Right-tail"
# test_stastic, p_value = sc.wilcoxon(x=baby.weight-m0, y=None, zero_method='wilcox',
correction=False, alternative="greater")
```

print(test_stastic)
print(p_value)

weight.non.0 = baby\$weight[baby\$weight != 0]
wilcox.test(weight.non.0, mu=3.3, alternative="less")

proc univariate data=work.pinot mu0=13; /* Change the param */
var Quality;

/* Then read the table Test for location -> Signed Rank. Note it is default 2-sided. If it is 1.0 then too bad =(* /

run;

Two Sample t-test (Parametric, independent)

- Assuming two <u>independent random</u> samples. Two <u>sample variances</u> are the <u>same</u>(else use equal_variance = False). Population distribution of each group is approx. normal or n is large.
- 2. Hypothesis H0: u1 = u2, or u1 u2 = 0. Where u1 and u2 is the population mean of group 1 and group 2. H1: u1 != u2, or u1 u2 != (<, >) 0.
- 3. Check if variances are equal first, then compute test statistic.
 - Let us represent the sample from group 1 as $X_1, X_2, \ldots, X_{n_1}$ and the sample from group 2 as $Y_1, Y_2, \ldots, Y_{n_2}$.
 - We shall denote the sample mean from group 1 as \bar{X} and the sample mean from group 2 as \bar{Y} . Note that n_1 and n_2 need not be equal.
 - The point estimate of the difference between the population means is

$$\bar{X} - \bar{Y}$$

- Let us denote the sample variance from group 1 as s_1^2 and the sample variance from group 2 as s_2^2 .
- Recall that this test, we have assumed that the population variances of the two groups are equal. If we denote this common value by σ^2 , then we can use the data from both samples to estimate it. We shall call this the pooled estimate of the common variance:

$$s_p^2 = \frac{(n_1 - 1)s_1^2 + (n_2 - 1)s_2^2}{n_1 + n_2 - 2}$$

- The test statistic is the distance between the point estimate and the null
 hypothesis value of the difference between population means, which is 0.
- This distance is measured in terms of standard error:

$$T = \frac{(\bar{X} - \bar{Y}) - 0}{\frac{se}{se}}$$

where the standard error is computed as

e assumes the 2 samples have similar variance for this test
$$se=s_p\sqrt{rac{1}{n_1}+rac{1}{n_2}}$$

- If H₀ is true, then T follows a t-distribution with n₁ + n₂ 2 degrees of freedom.
- 4. Compute test statistic. If H0 is true, $T^{t}(n1 + n2 2)$

```
import scipy.stats as sc
protein = pd.read_csv("/Users/gan/Desktop/Mods/ST2137/data/protein_and_weight_gain.csv")
x = protein.weight_gain[protein.level == "high"]
y = protein.weight_gain[protein.level == "low"]
barlett_statistic, barlett_pvalue = sc.bartlett(x, y) # P-value high indicates equal variance. Then we
print(barlett_statistic)
print(barlett_pvalue)
test_statistic, p_value = sc.ttest_ind(x, y, axis=0, equal_var=True)
df = len(x) + len(y) - 2 # Degree of freedom
one sided left p value = sc.t.cdf(test statistic, df)
one_sided_right_p_value = 1 - sc.t.cdf(test_statistic, df)
print("Test statistic: ", test_statistic)
print("2-sided test P-value:", p_value)
print("1-sided-left test P-value:", one_sided_left_p_value)
print("1-sided-right test P-value:", one_sided_right_p_value)
import statistics as st
df = len(x) + len(y) - 2
xbar_minus_ybar = np.mean(x) - np.mean(y)
alpha = 0.05 # 95% confidence interval
half alpha = alpha / 2
sp2 = ((len(x) - 1) * st.variance(x) + (len(y) - 1) * st.variance(y)) / (len(x) + len(y) - 2)
se = np.sqrt(sp2) * np.sqrt((1/len(x)) + (1/len(y)))
q = (sc.t.ppf(1-half_alpha, df=df)) * se
conf_interval = [xbar_minus_ybar - q, xbar_minus_ybar + q]
print("95% confidence interval:", conf_interval)
```

```
## First, check the 2 variances. Must be similar for this test.
protein = read.csv("/Users/gan/Desktop/Mods/ST2137/data/protein and weight gain.csv")
x = protein$weight gain[protein$level == "high"]
y = protein$weight gain[protein$level == "low"]
var.test(x, y) # p-value should be large
## Then compute test statistic and p-value
t.test(x, y, mu=0, var.equal=T) # indicate 2 variances same, then use pooled variance
## Compute manually:
sp2 = ((length(x) - 1)*var(x) + (length(y) - 1)*var(y)) / (length(x) + length(y) - 2)
se = sqrt(sp2)*sqrt((1/length(x)) + (1/length(y)))
test statistic = ((mean(x) - mean(y)) - 0) / se
p_value = pt(test_statistic, df=(length(x) + length(y) - 2), lower.tail=F) * 2 # two-sided
/* Import data first */
PROC TTEST data=work.protein;
       var weight gain;
       class level;
       /* Then read off pooled p-value if variance are similar. Folded F p-value is to check 2
variances similarity. p-value should be high for similar */
run;
# To get 1 sided:
/* Import data first */
PROC TTEST data=protein alpha=0.1;
       var weight_gain;
       class level;
       ods output TTests=TTests;
       /* Then read off pooled p-value if variance are similar. Folded F p-value is to check 2
variances similarity. p-value should be high for similar */
run;
data result;
       set TTests;
       one_sided_left_pvalue=cdf('T', tValue, DF);
       one sided right pvalue=1-cdf('T', tValue, DF);
       put one sided left pvalue=one sided right pvalue=;
run;
/* Run this independently to get the p-value */
proc print data=result;
       var one sided left pvalue;
       var one sided right pvalue;
run;
```

5. Conclude. If confidence interval contain 0, do not reject. Otherwise, reject H0. Also means p-value is small, reject.

Two Sample Mann-Whitney U-Test (Non-parametric)

- 1. Assumption. Two <u>independent</u> samples. Samples no need to be normally distributed. Sample sizes can be small. Sample can even have data that are categorical, or ranked.
- Mann-Whitney test is also can be called as Wilcoxon Rank Sum test.
- Let $X_1, ..., X_n$ be IID with cdf F, and $Y_1, ..., Y_m$ IID with cdf G.
- We consider the null hypothesis $H_0: F = G$.
- ullet We are interested in whether X values are on the whole larger than the Y values or vice-versa.

H0: The 2 populations (not mean) are equal, i.e. distributions of both populations are equal. H1: The 2 populations are not equal.

2. Compute test statistic.

```
import scipy.stats as sc

test_statistic, p_value = sc.mannwhitneyu(x, y, use_continuity=True, alternative="two-sided")
print(test_statistic)
print(p_value)
```

with_breakfast = c(87, 96, 92, 84) # Exam score students who ate breakfast no_breakfast = c(93, 83, 79, 73) # Exam score students who dont eat breakfast wilcox.test(with breakfast, no breakfast)

```
proc npar1way data=work.protein wilcoxon;
var weight_gain;
class level;
run;
```

Two Dependent Samples (Paired t-Test, Parametric)

- 1. Assumption. 2 <u>dependent</u> variables. MuX muY follow approx. normal dist, or large size.
- 2. Hypothesis. H0: $\mu_X \mu_y = 0$ vs. H1: $\mu_X \mu_y ! = 0$. muX and muY are the population mean.

```
before = [25, 25, 27, 44, 30, 67, 53, 53, 52, 60, 28] # ate breakfast
after = [27, 29, 37, 56, 46, 82, 57, 80, 61, 59, 43] # no breakfast
test_statistic, p_value = sc.ttest_rel(after, before, axis=0, nan_policy="propagate")
df = len(before) - 1 # Degree of freedom
one_sided_left_p_value = sc.t.cdf(test_statistic, df)
one_sided_right_p_value = 1 - sc.t.cdf(test_statistic, df)
print("Test statistic: ", test_statistic)
print("2-sided test P-value:", p_value)
print("1-sided-left test P-value:", one_sided_left_p_value)
print("1-sided-right test P-value:", one_sided_right_p_value)
import statistics as st
alpha = 0.05 # 95% confidence interval
xbar_minus_ybar = np.mean(after) - np.mean(before)
dbar = np.array([after]) - np.array([before])
half_alpha = alpha / 2
se = sc.sem(dbar.flatten()) # std error
q = (sc.t.ppf(1-half_alpha, df=df)) * se
conf_interval = [xbar_minus_ybar - q, xbar_minus_ybar + q]
print("95% confidence interval:", conf_interval)
before = c(25, 25,27, 44,30,67, 53, 53,52, 60, 28)
after = c(27, 29, 37, 56, 46, 82, 57, 80,61,59,43)
t.test(after, before, mu = 0, paired = TRUE, conf.level = 0.9)
data platelet;
        input before after;
        datalines;
25 27
25 29
27 37
```

44 56

```
30 46

67 82

53 57

53 80

52 61

60 59

28 43

;

/* 2-sided read off Pr > |t| */

proc ttest data=platelet alpha=0.05;

paired after*before;

run;
```

To get 1-sided:

```
/* 1-sided-left we store t value and run cdf */
proc ttest data=platelet;
       paired after*before;
       ods output TTests=TTests;
run;
data result;
       set TTESTS;
       one sided left pvalue=cdf('T', tValue, DF);
       one_sided_right_pvalue=1-cdf('T', tValue, DF);
       put one_sided_left_pvalue=one_sided_right_pvalue=;
run;
/* Run this independently to get the p-value */
proc print data=result;
       var one sided left pvalue;
       var one_sided_right_pvalue;
       var Probt; /*2-sided */
run;
```

Non-Parametric Paired Sample

1. Can be used for data small, non-normal data.

```
drugA = np.array([20, 40, 30, 45, 19, 27, 32, 26])
drugB = np.array([18, 36, 32, 46, 15, 22, 29, 25])
diff = drugA - drugB

# Signed Test
p_value = sc.binom_test([(diff < 0).sum(), (diff > 0).sum()], p=0.5)
print(p_value)
```

```
# Wilcoxon Signed Rank Test

test_statistic, p_value = sc.wilcoxon(x=diff, y=None, zero_method='wilcox', correction=True,
alternative='two-sided')

print("Test statistic:", test_statistic)

print("P-value:", p_value)

drugA = c(20, 40, 30, 45, 19, 27, 32, 26)

drugB = c(18, 36, 32, 46, 15, 22, 29, 25)

diff = drugA - drugB

ncount <-sum(sign(diff[diff>0]))# the number of positive signs
binom.test(ncount, length(diff),0.5) # Signed Test
wilcox.test(diff) # Wilcoxon Signed Rank Test
```

```
data drug;
input DrugA DrugB;
datalines;
20 18
40 36
30 32
45 46
19 15
27 22
32 29
26 25
data drug;
set drug;
diff = DrugA - DrugB;
run;
/* Look for signed rank pr */
proc univariate data=drug mu0=0;
var diff;
run;
```

Expectation of Sum of squares (SSD)

I = Number of treaments/groups

J = Number of measurements in each group

For groups with same size, i.e. same J:

$$SS_{TOT} = SS_W + SS_B = \sum_{i=1}^{I} \sum_{j=1}^{J} (Y_{ij} - Y_i)^2 + J \sum_{i=1}^{I} (Y_i - overallAve)^2$$

$$E(SS_W) = I(J-1)\sigma^2$$

$$E(SS_B) = J \sum_{i=1}^{I} \alpha_i^2 + (I-1)\sigma^2$$

$$E(Y_{ij}) = E(Y_i) = \mu + \alpha_i$$

Unbias estimate $s_p^2 = \frac{SS_W}{I(J-1)}$

 $SS_W = \sum_{i=1}^{I} (J-1)s_i^2$, where s_i^2 is the sample variance in the i-th group.

ANOVA

1. Assumption: Random samples. Equal variance (different group share the same variance, if unequal variance, use Kruskal straight). We check normality of response (check individually for each group) first before proceed (if sample large but not normal, also can). Then, after anova we check normality of errors. Independence of errors.

Use barlette or levene to test variance, QQPlot or shapiro to test normality.

2. H0: $\alpha_1 = \alpha_2 = \cdots = \alpha_I$

3. Test statistic
$$F = \frac{SS_B/(I-1)}{SS_W/[I(J-1)]} \sim F_{df_1,df_2}$$
, $df_1 = (I-1)$,
$$df_2 = I(J-1) \{ for \ different \ group \ size, df2 = n-I, where \ n \ is \ total \ samples \ in \ all \ groups \}$$

Under H0, F should be close to 1.

If H0 is false, number of F reflects variation between different groups and variations within groups, denominator reflects only variations within groups.

H0 is rejected for large values of F.

```
newtablets$lab = as.factor(newtablets$lab)
model1 = aov(amount~lab, data=newtablets) # amount and lab are cols in newtablets,
dep~ind
summary(model1)
anova_vector = unlist(summary(model1))
df1 = anova vector[1]
df2 = anova vector[2]
SS B = anova vector[3]
SS W = anova vector[4]
test_statistic = anova_vector[7]
p value = anova vector[9]
 > anova <- aov (amount ~lab, data = newdata)
 > summary(anova) ss_B
            Df Sum Sq Mean Sq F value Pr(>F)
            6 0.1247 0.020790 5.66 9.45e-05 ***
 lab
 Residuals 63 0.2314 0.003673
                   ່ ⇒ss_w
 Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
```

import statsmodels.api as sm

from statsmodels.formula.api import ols

```
newtablets.lab = newtablets.lab.astype(object) # declare lab as a factor
model = ols('amount~lab', data=newtablets).fit() # amount and lab are col names of newtablets
anova = sm.stats.anova_lm(model, typ=2)
print(anova)
p_value = anova.iloc[0, 3]
test_statistic = anova.iloc[0, 2]
SS_B = anova.iloc[0, 0]
SS_W = anova.iloc[1, 0]
df1 = anova.iloc[0, 1]
df2 = anova.iloc[1, 1]
print("P_value:", p_value)
print("Test-statistic F:", test_statistic)
print("Sum of square between (SSB):", SS_B)
print("Sum of square within (SSW):", SS W)
print("df 1:", df1)
print("df 2:", df2)
proc anova data=mysql table2;
class lab;
model amount = lab;
means;
```

ANOVA Assumption checking

Normality Test:

HO: Sample that is tested follows normal distribution.

```
shapiro.test(newtablets$amount) # Reject low p-value indicating not normal.
anova_result = aov(amount~lab, data=newtablets)
shapiro.test(anova_result$res) # Check residuals normality, i.e. normality of the error.
Should be large for ANOVA becos we assumed this to be normal when using ANOVA. If small, then might want consider using Kruskal-Wallis instead.
```

```
# Check variable amount normality
shapiro_test_statistic, shapiro_p_value = sc.shapiro(newtablets.amount)
print("Shapiro Test statistic:", shapiro_test_statistic)
print("Shapiro P_value", shapiro_p_value)

# Check residual error normality
```

```
newtablets.lab = newtablets.lab.astype(object)
model = ols('amount~lab', data=newtablets).fit() # amount and lab are col names of newtablets
shapiro_test_statistic, shapiro_p_value = sc.shapiro(model.resid)
print("Shapiro Test statistic:", shapiro_test_statistic)
print("Shapiro P_value", shapiro_p_value)
/* look at test for normality section */
proc univariate data=tablets normal;
var amount;
histogram amount / normal; /* Optional */
qqplot / normal (mu=est sigma=est); /* Optional */
run;
To test for residual:
proc glm data=tablets;
title2 'Proc glm analysis';
class lab;
model amount = lab;
/* Store fitted values and fitted residuals in dataset 'amountfit'*/
output out=amountfit p=yhat r=resid; /*p is fitted value, r is residual */
proc univariate data=amountfit normal;
var resid;
run;
Equal Variance Test:
bartlett.test(newtablets$amount, newtablets$lab) # Assume sample normal
OR
install.packages("car")
library(car)
leveneTest(newtablets$amount, newtablets$lab) # Suitable if sample distribution unknown)
# We want p-value to be high so as not to reject H0 = same variances
bar_test, p_value = sc.bartlett(newtablets.amount[newtablets.lab == 1],
newtablets.amount[newtablets.lab == 2],
           newtablets.amount[newtablets.lab == 3], newtablets.amount[newtablets.lab == 4],
           newtablets.amount[newtablets.lab == 5], newtablets.amount[newtablets.lab == 6],
           newtablets.amount[newtablets.lab == 7])
print("Barlette Test statistic:", bar_test)
print("Barlette Test p_value:", p_value)
```

```
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```

bar_test, p_value = sc.levene(newtablets.amount[newtablets.lab == 1],

```
/* Levene test for equal variances */
proc anova data=tablets;
class lab; /* independent var */
model amount = lab; /* amount is dependent */
means lab / hovtest=levene alpha=0.05;
run;
/* Barlette test for equal variances */
proc anova data=tablets;
class lab; /* independent var */
model amount = lab; /* amount is dependent */
means lab / hovtest=bartlett alpha=0.05;
run;
```

Both:

```
# Use this to draw plot
mcheck=function(obj){
res=obj$resid
fit=obj$fitted
par(mfrow=c(2,1))
plot(fit,res,xlab="Fitted values",ylab="Residuals")
abline(h=0,lty=2)
qqnorm(res,datax = TRUE, xlab="Z scores",ylab="Residuals")
qqline(res,datax = TRUE, lty=2)
par(mfrow=c(1,1))
}
```

Kruskal-Wallis Test (Non-parametric ANOVA)

1. Assumption. Can violate ANOVA. Observations can be categorical or non-normal. Can have different variances. No need assume any distribution form. Assumed independent observation.

kruskal.test(newtablets\$amount~newtablets\$lab)

```
kruskal_test_statistic, p_value = sc.kruskal(newtablets.amount[newtablets.lab == 1],
newtablets.amount[newtablets.lab == 2], newtablets.amount[newtablets.lab == 3],
newtablets.amount[newtablets.lab == 4])
```

```
print("Kruskal Test statistic:", kruskal_test_statistic)
print("P-value:", p_value)

proc npar1way data=mysql_table2 wilcoxon dscf;
class lab;
var amount;
run;
```

Multiple Comparison Tests: Bonferroni

If we test k null hypothesis and we want α family error rate, Each individual null hypothesis is tested at level $\frac{\alpha}{k}$ Give good results if k is not too large. Can use for both ANOVA and Kruskal.

R:

pairwise.t.test(newtablets\$amount, newtablets\$lab, p.adjust.method = "bonf") # Then, compare the p-value with family error rate.

```
import statsmodels.stats.multicomp as mc
comparison = mc.MultiComparison(newtablets.amount, newtablets.lab)

## IF All groups satisfy ANOVA, then use t-test for pairwise comparison
result, tb1, tb2 = comparison.allpairtest(sc.ttest_ind, method="bonf", alpha=0.05)

## IF group doesn't satisfy ANOVA (aka using Kruskal-W test), then use M.Whitney for pairwise comparison
result, tb1, tb2 = comparison.allpairtest(sc.mannwhitneyu, method="bonf", alpha=0.05)
print(result)

# The result:

# stat: Test-statistic

# pval: The p-value if conducting the 2-independent t-test with the 2 groups with equal variance

# pval_corr: The adjusted p-value we using to compare with our alpha=0.05

# reject: If False (pval_corr > alpha), the 2 groups have similar means.

/*
Doesn't give p-value. Rather, the *** represents those rejected, i.e. the groups are significantly different from each other.

*/
proc anova data=mysql_table2;
class lab;
model amount = lab;
means lab / BON CLDIFF alpha=0.05;
run;
```

Tukey Test (Only used for those applicable to ANOVA, i.e. not Kruskal)

Generally better than Bonferroni's correction. Let α be the family type 1 error rate for k tests.

R:

TukeyHSD(aov(amount~lab, data=newtablets), conf.level = 0.95) # Alpha=0.05 # Then, compare value of 'p adj' to alpha and reject those below alpha. E.g. if lab 4-1 p adj is small, meaning lab4 and lab1 are significantly different from each other.

```
import statsmodels.stats.multicomp as mc
comparison = mc.MultiComparison(newtablets.amount, newtablets.lab)
tukey = comparison.tukeyhsd(alpha=0.05)
print(tukey.summary())
# Its rejecting those whose Confidence Interval doesn't contain 0.

/*
Doesn't give p-value. Rather, the *** represents those rejected, i.e. the groups are significantly different from each other.
 */
proc anova data=mysql_table2;
class lab;
model amount = lab;
means lab / tukey CLDIFF alpha=0.05;
run;
```

Standard error

```
se = function(x) {
  return(sqrt(var(x) / length(x)))
}
```

Estimating Regressor

Simple model: $y = \beta_0 + \beta_1 x$

Y is response, x is Regressor aka explanatory.

Before fitting linear model, we check and make sure response is normal first.

- 1. Assumption: Relationship of X and Y are linear (check with scatter plot). Normality assumption for errors and constant variance. All errors are uncorrelated to each other. All regressors are uncorrelated.
- 2. H0: All coefficients (not counting intercept) in the model are 0H1: At least one coefficient is non-zero.Simple model: H0: B1 = 0, H1: B1 != 0

Using Built-in python:

Single:

```
import statsmodels.api as sm
weight = ex10.weight # response
n = len(weight)
inter = [1]*n
X = np.column_stack((inter, ex10.height))
model1 = sm.OLS(weight, X)
results1 = model1.fit()
print(results1.summary())

## Anova:
from statsmodels.formula.api import ols
import statsmodels.api as sm
mod = ols('weight ~ height', data=ex10).fit()
anova1 = sm.stats.anova_lm(mod , typ=2)
print(anova1)
```

Multiple:

```
import statsmodels.api as sm
weight = ex10.weight # response
n = len(weight)
inter = [1]*n

X = np.column_stack((inter, ex10.height, ex10.age))
model2 = sm.OLS(weight, X)
results2 = model2.fit()
print(results2.summary())

## Anova:
from statsmodels.formula.api import ols
import statsmodels.api as sm
mod2 = ols('weight ~ height + age', data=ex10).fit()
anova2 = sm.stats.anova_lm(mod2, typ=2)
print(anova2)
```

With indicators (Categorical):

```
ex10['gender'] = ex10['gender'].astype(object)
dummy = pd.get_dummies(ex10.gender).values # convert categorical into dummy
print(dummy)
print(dummy[:, 1]) # Choose this that sets M = 1 and F = 0
print(dummy[:, 0]) # Choose this that sets F = 1 and M = 0
import statsmodels.api as sm
weight = ex10.weight # response
n = len(weight)
inter = [1]*n
X = np.column_stack((inter, ex10.height, ex10.age, dummy[:, 1])) # X3 will be M=1 F=0
model3 = sm.OLS(weight, X)
results3 = model3.fit()
print(results3.summary())
# OR if we want to explicitly state which one is reference
import statsmodels.api as sm
crab['spine'] = crab['spine'].astype(object)
weight = crab.weight # response
n = len(weight)
s1 = np.zeros(n)
s1[(crab.spine == 1)] = 1
s2 = np.zeros(n)
s2[(crab.spine == 2)] = 1
print(s1)
inter = [1]*n
X = np.column_stack((inter, crab.width, s1, s2))
model3 = sm.OLS(weight, X)
results3 = model3.fit()
print(results3.summary())
```

With Interaction Term (e.g. height related with gender):

```
import statsmodels.api as sm

weight = ex10.weight # response
```

```
n = len(weight)
inter = [1]*n
ex10['gender'] = ex10['gender'].astype(object)
dummy = pd.get_dummies(ex10.gender).values # convert categorical into dummy
HG = ex10['height']*dummy[:, 1] # Height*Gender
X = np.column_stack((inter, ex10.height, ex10.age, dummy[:, 1], HG)) #X1: height, X2: age, X3:
model4 = sm.OLS(weight, X)
results4 = model4.fit()
print(results4.summary())
Fitted values:
print(results1.fittedvalues)
Raw Residuals:
print(results1.resid)
Standardized Residual:
analysis = results1.get_influence()
SR = analysis.resid_studentized_internal
print(SR)
Leverage:
analysis = results1.get_influence()
leverage = analysis.hat_matrix_diag
print(leverage)
Cook's distance:
analysis = results1.get_influence()
cooks_d, p = analysis.cooks_distance
print(cooks d)
Predict and confidence:
newpoint = [1,27,1,0] # intercept, x1 value, x2 value, x3 value
y = results3.predict(newpoint) # predict out of sample
print(y)
predictions = results3.get_prediction(newpoint)
print(predictions.summary_frame(alpha=0.05))
```

Scatter Plot of Standardized Residuals vs Fitted values:

```
fitted_values = results1.fittedvalues

analysis = results1.get_influence()

SR = analysis.resid_studentized_internal

plt.scatter(fitted_values, SR)

plt.xlabel("fitted weight")

plt.ylabel("Standardized Residuals")

plt.title("SR vs Fitted")

plt.hlines(0, xmin=min(fitted_values), xmax=max(fitted_values))

plt.show()
```

QQPlot of Standardized Residual

```
import pylab
import scipy.stats as scst

analysis = results3.get_influence()
SR = analysis.resid_studentized_internal
scst.probplot(SR, dist="norm", plot=pylab)
pylab.title("QQ Plot")
pylab.ylabel("Standardized Residuals")
pylab.show()
```

OLS Regression Results			
Dep. Variable:	weight	R-squared:	0.944
Model:	OLS	Adj. R-squared:	0.933
Method:	Least Squares	F-statistic:	84.45
Date:	Sat, 10 Oct 2020	Prob (F-statistic): 0.000256
Time:	00:03:13	Log-Likelihood:	-26.068
No. Observations:	7	AIC:	56.14
Df Residuals:	5	BIC:	56.03
Df Model:	1		
Covariance Type:	nonrobust		
coe	ef std err	t P> t	[0.025 0.975]
const -592.644	6 81.542	-7.268 0.001	-802.255 -383.034
x1 11.191		9.190 0.000	8.061 14.322
b1	SE(B1)=sgrt(MS_res / S	_xx)	0.001
Omnibus:	B1/ nan	SE(B1)~t(df=5) Durbin-Watson:	2.161
Prob(Omnibus):		()	0.741
,	nan		0.690
Skew:	-0.033		
Kurtosis:	1,407	Cond. No.	1.22e+03

The Anova table

```
from statsmodels.formula.api import ols

mod1 = ols('weight ~ height', data=data).fit()
anova1 = sm.stats.anova_lm(mod1, typ=2)
print(anova1)

Regression of sum of sq. i.e. get_SSr
sum_sq df F PR(>F)
height 11880.327238 1.0 84.450853 0.000256
Residual 703.387048 5.0 NaN NaN
Sum of squared residuals, i.e. get_SSres
```

Write manually:

```
ex10 = pd.read_csv("/Users/gan/Desktop/Mods/ST2137/data/ex10_1.txt", sep=" ")
x = ex10.height
y = ex10.weight
def get_b1(x, y):
  return (np.sum(y * x) - ((np.sum(y) * np.sum(x)) / len(x))) / (np.sum(x**2) - (np.sum(x)**2 / len(x)))
def get_b0(x, y):
  return np.mean(y) - get_b1(x, y) * np.mean(x)
def get_Sxx(x):
  return np.sum((x - np.mean(x)) ** 2)
def get_Sxy(x, y):
  return np.sum(y * (x - np.mean(x)))
def get_fitted_model_yhats(x, y):
  b0 = get_b0(x, y)
  yhat = b0 + b1*x
  return yhat
def get_individ_res(x, y):
  yhat = get_fitted_model_yhats(x, y)
```

```
return y - yhat
def get_SSres(x, y):
  yhat = get_fitted_model_yhats(x, y)
  return np.sum((y - yhat) ** 2)
def get_SSr(x, y):
  return get_b1(x, y) * get_Sxy(x, y)
def get_SStotal(x, y):
  return get_SSr(x, y) + get_SSres(x, y)
def get_MSres(x, y):
  return get_SSres(x, y) / (len(x) - 2) # n-2 becos simple model 2 coefficients. n - #regressors + 1 for multi.
def get_MSr(x, y):
  return get_SSr(x, y) / 1 # n-2 becos simple model 2 coefficients
def get_StdMSres(x, y):
  return np.sqrt(get_MSres(x, y))
def get_F_statistic(x, y):
  return (get_SSr(x, y) / 1) / (get_SSres(x, y) / (len(x) - 2))
def get_Ftest_p_value(x, y):
  return 1 - sc.f.cdf(F0, 1, len(x) - 2)
def get_T_statistic(x, y):
  return get_b1(x, y) / np.sqrt(get_MSres(x, y) / get_Sxx(x))
def get_Ttest_p_value(x, y):
  T0 = get_T_statistic(x, y)
  return sc.t.cdf(np.abs(T0)*-1, len(x) - 2) * 2
```

Using built in R:

Single Model:

model1 = Im(weight~height, data=ex10) #Y~X
summary(model1)
anova(model1)

Multiple Model:

model2 = Im(weight~height+age, data=ex10)
summary(model2)
anova(model2)

With indicators (let R choose):

```
ex10$gender = as.factor(ex10$gender)
model3 = Im(weight ~ height + age + gender, data=ex10)
summary(model3)
anova(model3)
```

With indicators (we choose):

```
#Model 2: We choose the indicator for spine where spine = 3 is the reference. s1 = c(rep(0,173)) #173 is nrow(crab) s2 = c(rep(0,173)) s1[which(spine==1)] = 1 s2[which(spine==2)] = 1 data$s1 = s1 data$s2 = s2 model2 = Im(weight ~ width + s1 + s2, data = data)
```

With interaction term:

```
ex10$gender = as.factor(ex10$gender)
model4 = Im(weight ~ height + age + gender + height*gender, data=ex10)
summary(model4)
anova(model4)
```

Fitted values:

model1\$fitted.values

Residuals & Standardize Residuals:

model1\$res # Raw residuals of model1 rstandard(model1) # Standardized residuals of model 1 cooks.distance(model1)

Leverage:

```
x2 = cbind(c(rep(1, len(x))), x) # x is the regressor hat = <math>x2 \%*\% solve(t(x2) \%*\% x2) \%*\% t(x2)
```

```
leverage = diag(hat)
```

Predict:

```
newpoint=data.frame(width = 27,s1 = 1, s2 = 0)
# the 95% CI for the mean weight is:
predict(model2, newpoint, interval = "confidence", level = 0.95)
```

Plot Standardise Residual vs Fitted weight:

```
plot(model1$fitted.values, rstandard(model1), main="SR vs Fitted", xlab="fitted weight", ylab="Standadized Residuals")
x_range = seq(min(model1$fitted.values) - 5, max(model1$fitted.values) + 5,
length.out=length(model1$fitted.values))
y_range = x_range * 0
lines(x_range, y_range)
```

Plot QQ Plot of Standardized Residuals:

```
SR = rstandard(model1)
qqnorm(SR,datax = TRUE, ylab = "Standardized Residuals", xlab = "Z scores", main = "QQ
Plot", pch = 20)
qqline(SR,datax = TRUE)
```

Residuals:

```
1 2 3 4 5 6 7
-13.361 8.977 2.595 14.256 -9.553 -9.788 6.873
```

```
Coefficients: Fitted model: Weight = -592.645 + 11.191 * height
```

Multiple R-squared: 0.9441, Adjusted R-squared: 0.9329 F-statistic: 84.45 on 1 and 5 DF, p-value: 0.000256

Signif. codes: 0 '*** 0.001 '** 0.01 '* 0.05 '.' 0.1 ' 1

```
Residuals:
           1
                        2
                                     3
                                                               5
                                                                                          7
    1.252
                 2.281
                              6.232
                                           5.877 -12.783 -8.513
                                                                                   5.654
                       To interpret coefficient 5.2309: At the same age and same gender, when the height increases
 Coefficients: by 1 unit, the mean weight (response) will increase by 5.2309 units
                      Estimate Std. Error t value Pr(>|t|)
 (Intercept) -254.1068
                                        277.3604 -0.916
                                                                         0.427
                                           4.6831
                                                          1.117
                                                                         0.345
height
                         5.2309
                         1.5870
                                           0.9204
                                                           1.724
                                                                         0.183
 age
 genderM
                        15.6511
                                          23.2239
                                                          0.674
                                                                         0.549
  Fitted model: Weight_hat = -254.1068 + 5.2309°H + 1.5870°Age + 15.6511°Indicator(Gender==M) weight of male and female given they
Indicator(Gender==M) = 1 if Male, 0 if Female (Chosen by R, as seen in genderM)

Residual standard error: 10.77 on 3 degrees of freedom
                                                            Adjusted R-squared:
Multiple R-squared: 0.9723,
F-statistic: 35.16 on 3 and 3 DF, p-value: 0.007742 > (3)
Calculate manually:
# For y=b0 + b1x model
# x is vectors of x, y is vectors of y
# x is regressor (explanatory)
get b1 = function(x, y) {
return((sum(y*x) - ((sum(y)*sum(x))/length(x))) / (sum(x^2) - (sum(x)^2 / length(x))))
get_b0 = function(x, y) {
return(mean(y) - get b1(x, y)*mean(x))
get Sxx = function(x) {
return(sum((x - mean(x))^2))
get Sxy = function(x, y) {
return(sum(y * (x - mean(x))))
# Param x,y are vectors of x-y values
# Returned a vector fitted values of yhats based on OLS
get fitted model yhats = function(x, y) {
b1 = get b1(x, y)
b0 = get_b0(x, y)
yhat = b0 + b1*x
return(yhat)
# Get the raw residuals after having the fitted model, i.e. (y-yhat)
# Accept param of raw x and y and calculate the fitted model.
get_individ_res = function(x, y) {
yhat = get_fitted_model_yhats(x, y)
return((y - yhat))
# Return the Sum of squared residuals after having the fitted model, i.e. sum( (y-yhat)^2)
```

Accept param of raw x and y and calculate the fitted model.

get_SSres = function(x, y) {

```
yhat = get_fitted_model_yhats(x, y)
return(sum((y - yhat)^2))
# Regression sum of squares, with df1 in simple model, df=k in multiple model with k coefficients(less intercept)
get_SSr = function(x, y) {
return(get_b1(x, y) * get_Sxy(x, y))
# Return the total sum of square errors. SS_T is fixed regardless of model.
get_SStotal = function(x, y) {
return(get_SSr(x, y) + get_SSres(x, y))
# Return the residual mean square of simple model, i.e. sigmahat^2
get_MSres = function(x, y) {
return(get SSres(x, y) / (length(x) - 2)) # n-2 becos simple model 2 coefficients. n - #regressor + 1 (intercept) for multi.
get_MSr = function(x, y) {
return(get_SSr(x, y)/1) # n-2 becos simple model 2 coefficients
# Return residual standard error or standard error of regression
get StdMSres = function(x, y) {
return(sqrt(get_MSres(x, y)))
}
# F-test test statistic ~ F(1, length(x) -2)
get_F_statistic = function(x, y) {
return((get_SSr(x, y)/1) / (get_SSres(x, y)/(length(x)-2)))
# If p-value small, reject H0 => implies x helps in explaning variability in y.
# If p-value small, fail to reject H0 \Rightarrow there is no linear relationship between y and x.
get_Ftest_p_value = function(x, y) {
F0 = get_F_statistic(x, y)
return(pf(F0, 1, length(x)-2, lower.tail=F))
get_T_statistic = function(x, y) {
return(get_b1(x, y) / sqrt(get_MSres(x, y)/get_Sxx(x)))
# 2-sided ttest p-value
get_Ttest_p_value = function(x, y) {
T0 = get_T_statistic(x, y)
return(pt(abs(T0), length(x)-2, lower.tail=F) * 2)
# Return the coefficient of determination, R^2
get_r2 = function(x, y) {
return(get_SSr(x, y) / get_SStotal(x, y))
```

Single:

```
proc reg data=ex10;
model weight = height; /* Y (response) = X (Explanatory/Regressor) */
output out=analysis P=yhat R=residual STUDENT=resid cookd=cooks H=leverage;
/* P=fitted, R=raw residuals, student is standadized residuals; */
```

```
run;
```

Multiple:

```
proc reg data=ex10;
model weight = height age/SS1;
run;
quit;
*/ SS1 is the SS_R (Type I SS) as in anova table in R */
```

With indicator (categorical variable):

```
data ex10_gen;
set ex10;
if gender = "M" then gen = 1;
if gender = "F" then gen = 0;
run;
/* when fitting categorical var into model, use this gen instead of raw gender */
proc reg data=ex10_gen;
model weight = height age gen/SS1;
run;
quit;
```

OR easier:

```
proc glm data=ex10;
  class gender;     /* generates dummy variables internally. Can add more */
  model weight = height age gender / solution;
run;
quit;
```

OR with graphs and no need auto set categorical

```
proc glmmod data=ex10 outdesign=GLMDesign outparm=GLMParm;
  class gender;
  model weight = height age gender;
run;

/* regression analysis by using dummy variables */
proc reg data=GLMDesign;
  DummyVars: model weight = COL2-COL5; /* dummy variables except intercept */
quit;
```

With interaction term (height related to gender):

```
data ex10;

set ex10;

if gender = "M" then gen = 1;

if gender = "F" then gen = 0;

height_gen = height*gen;

run;

proc reg data=ex10;

model weight = height age gen height_gen;
```

```
run;
quit;
```

Predicted and confidence:

```
/* Alr have columns s1 and s2 */
data crab:
set crab end=last;
output;
if last then do;
  VAR1 = .;
  color = .; *information for color is missed;
  spine = .; *spine variable is not needed for the prediction;
  width = 27; *width is given, here it = 27cm;
  satell =.;
  weight =.;
  s1 = 1; *spine = 1 means s1 = 1 and s2 = 0;
  s2 = 0;
  output;
end;
run;
*Using the model to predict the weight when width = 27 cm and spine = 1, output is saved in
table "predict";
proc reg data=crab alpha = 0.05;
 model weight = width s1 s2;
output out=predict(where=(weight=.)) p=predicted uclm=UCL Pred lclm=LCL Pred;
run;
quit;
* Use IcIm - ulcm: lower and upper bounds of the CI for the prediction of Mean weight;
*Check the dataset "Predict" under the My Libararies --> WORK folder in the LEFT side;
*Predicted weight and 95% CI is: 2.6520425038
                                                   (2.5658029279,
                                                                         2.7382820798);
```

Test Significance of Model (F-test)

- 1. Assumption: Relationship between X and Y is linear (check by using scatter plot of x and y). 2^{nd} assumption is normality assumption and constant variance assumption, for $\in_i \sim N(0, \sigma^2)$, where variance is constant and most of time unknown. 3^{rd} assumption is \in_i , \in_j uncorrelated for all i!= j. For model > 1 regressor, all regressors are uncorrelated.
- 2. Hypothesis:

H0: All coefficients in the model are 0. For simple model: H_0 : $\beta_1=0$, i.e. model is not significant

H1: At least one coefficient is non-zero. For simple model, $H_1: \beta_1 \neq 0$

3. Test statistic:

$$F = \frac{SS_R/k}{SS_{Res}/(n-k-1)} = \frac{MS_R}{MS_{Res}} \sim F_{k,n-k-1}$$

Note: Degree of freedom only for simple model df1=1, df2=n-2

k = number of regressor (exclude intercept) in the model. K=1 for simple.

- 4. P-value of F test stastitic is right area under F(k, n-k-1).
- 5. Reject H0 if p-value less than alpha. Fail to reject H0 implies there is no linear relationship between y and x. If reject H0, it implies x helps in variability in y, i.e. straight line model is adequate, or a better model could be obtained by adding higher order term(s) of x. In multi, rejection of H0 implies at least one regressor contributes significantly to the model.
- 6. To get calculation, refer to above Estimating Regressor

Test significance of regressor (T-test)

- 1. Assumption same as F-test above.
- 2. $H_0: \beta_1 = 0 \text{ vs } H_1: \beta_1 \neq 0$
- 3. Test statistic:

$$T = \frac{\beta_1 hat}{SE(\beta_1 hat)} = \frac{\beta_1 hat}{\sqrt{(M}S_{res}/S_{xx})} \sim t_{n-2} \text{ for simple model}$$

 $\mathsf{T} = \frac{B_i hat}{SE(B_i hat)} = \frac{B_i hat}{\sqrt{(MS_{res}*C_{ii})}} \sim t_{n-k-1} \text{ for multi, where } c_{ii} \text{ is the diagonal element of } (X'X)^{-1} \text{ corresponding to } B_i hat. \text{ This is a test of contribution of } x_i \text{ given the other regressors in the model}$

Note: $T^2 = F$

To get calculation, refer to above Estimating Regressor.

Coefficient of Determination R^2

$$R^2 = \frac{SS_R}{SS_T} = 1 - \frac{SS_{Res}}{SS_T}$$

 $0 \le R^2 \le 1$. The larger R^2 , the better fitted model is. Does not indicate appropriateness of linear model.

To get calculation, refer to above Estimating Regressor.

Adjust R^2:

$$R_{Adj}^2 = 1 - \frac{SS_{Res}/(n-p)}{SS_T/(n-1)}$$

p = # Regressors (not counting intercept) + 1. i.e. total number of coefficients including intercept.

Here R^2 adjusted will drop if add regressor that is not significant, whereas R^2 will always increase if adding more regressors.

Confidence Interval

Determine 95% confidence interval for B1 of variable width

confint(model2, "width", level=0.95)

```
model3 = sm.OLS(weight, X)

results3 = model3.fit()

print(results3.summary())

print(results3.conf_int(alpha=0.05)) # 95% Cl
```

```
/* Basically add alpha and clparam */
proc glm data=crab alpha=0.05; /* 95% */
class spine; /* generates dummy variables internally. Can add more */
model weight = width spine / solution clparm;
run;
quit;

/* If normal reg, add alpha and clb */
proc reg data=ex10_gen alpha=0.05;
model weight = height age gen/SS1 clb;
run;
quit;
```

Various variable

Variance, sigma^2 of the error term:

```
model3 = sm.OLS(weight, X)

results3 = model3.fit()

print(results3.summary())

est_variance = results3.scale # variance of the error term
```

est_variance = summary(model2)\$sigma ^ 2

```
* sigma = Root MSE = 0.26564; /* Read off Root MSE */

*the estimation of variance of error term is = 0.26564^2;
```