

BC2410 Assignment 3

Sem 1, Group 3

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Q1

- a) 100 ✓
- b) A C ✓
- c) B: 30 ✓
D: 100 ✓
- d) B D ✓
- e) C ✓
- f) A ✓
- g) min $-5A + 5B + 10C + 100D$
s.t. $-A + B = 2$
 $-3A + B + 4C + D = 5$
 $B + 2C = 2$
 $2A + B + C = 5$
 $C \geq 0 \quad D \geq 0 \quad A \leq 0 \quad B \leq 0$ (verified)

| Q2 | A | B | constraint |
|--------|---------|----------|------------|
| labour | $1/5 h$ | $3/10 h$ | ≤ 90 |
| test | $1/7 h$ | $3/7 h$ | ≤ 90 |
| raw | \$3 | \$1 | |
| market | \$7 | \$9 | |
| demand | 200 | 100 | |

a) let x_1 be the number of the first product produced
let x_2 be the number of the second product produced

$$\max \quad 4x_1 + 8x_2$$

st.

$$\frac{1}{5}x_1 + \frac{3}{10}x_2 \leq 90$$

$$\frac{1}{7}x_1 + \frac{3}{7}x_2 \leq 90$$

$$x_1 \geq 200$$

$$x_2 \geq 100$$

b) dual

$$\min \quad 90p_1 + 90p_2 + 200p_3 + 100p_4$$

$$\frac{1}{5}p_1 + \frac{1}{7}p_2 + p_3 \geq 4$$

$$\frac{3}{10}p_1 + \frac{3}{7}p_2 + p_4 \geq 8$$

$$p_1, p_2 \geq 0, \quad p_3, p_4 \leq 0$$

Q3

let $x_i = \begin{cases} 1, & \text{if show } i \text{ is shown} \\ 0, & \text{if show } i \text{ is not shown} \end{cases} \quad \forall i = 1, 2, \dots, 9$

let c_i be advertising revenue for show i (in millions)

let $y = \begin{cases} 1, & \text{more than 3 shows contain violence} \\ 0, & \text{3 or less shows contain violence} \end{cases}$

$$\max \sum_{i=1}^9 c_i x_i - 4y$$

$$\text{st } x_3 + x_6 + x_7 + x_9 \geq x_2 + x_3 + x_4 + x_6$$

$$x_7 \leq x_4 + x_3$$

$$x_7 + x_9 \leq 1$$

$$x_2 + x_3 + x_4 + x_7 \geq 5 - 2 - (x_1 + x_5 + x_6)$$

$$y \geq x_2 + x_3 + x_4 + x_6 - 3$$

$$\sum_{i=1}^9 x_i = 5$$

what if $x_1 = x_5 = x_6 = 0$

then $x_2 + x_3 + x_4 + x_7 \geq 3$

$$2(x_2 + x_3 + x_4 + x_7) \geq x_1 + x_5 + x_6 - 1$$

should work

$x_i \in \{0, 1\}$ for $i = 1, \dots, 9$ $y \in \{0, 1\}$

Workings for constraint 3d (NOT IN FINAL SOLUTION)

| | | | drama | comedy |
|-------------------|-------------------------------|--|-------|----------|
| $x_1 + x_5 + x_8$ | $x_1 + x_2 + x_3 + x_4 + x_7$ | $x_2 + x_3 + x_4 + x_7 \geq 5 - 2 - (x_1 + x_5 + x_6)$ | | |
| 0 | 3 or 4 | | | |
| 1 | 2 or 3 or 4 | | " | ≥ 3 |
| * 2 | 1 or 2 or 3 | | " | ≥ 2 |
| * 3 | 0 or 1 or 2 | | " | ≥ 1 |
| | | | " | ≥ 0 |

5 on the RHS of the equation comes from the total 5 shows that can be shown

2 on the RHS of the equation comes from the 2 shows that are neither drama nor comedy

Q4

$$\begin{aligned} \text{a) max } & \cancel{x_{12} + x_{15} + x_{13} + x_{26} + x_{27} +} \\ & \cancel{x_{23} + x_{34} + x_{47} + x_{49} + x_{57} +} \\ & x_{56} + x_{69} + x_{79} \end{aligned}$$

st.

$$x_{12} + x_{15} + x_{13} = x_{69} + x_{79} + x_{49}$$

← this three is the flow

$$x_{12} - x_{26} - x_{27} - x_{23} = 0$$

$$x_{13} + x_{23} - x_{34} = 0$$

$$x_{34} - x_{47} - x_{49} = 0$$

$$x_{15} - x_{56} - x_{57} = 0$$

$$x_{26} + x_{56} - x_{69} = 0$$

$$x_{27} + x_{57} + x_{47} - x_{79} = 0$$

$$0 \leq x_{12} \leq 9$$

$$0 \leq x_{15} \leq 20$$

$$0 \leq x_{13} \leq 5$$

$$0 \leq x_{23} \leq 18$$

$$0 \leq x_{26} \leq 20$$

$$0 \leq x_{27} \leq 15$$

$$0 \leq x_{34} \leq 15$$

$$0 \leq x_{47} \leq 5$$

$$0 \leq x_{49} \leq 16$$

$$0 \leq x_{57} \leq 5$$

$$0 \leq x_{56} \leq 14$$

$$0 \leq x_{69} \leq 6$$

$$0 \leq x_{79} \leq 8$$

b)

$$\min \quad 7x_{12} + 8x_{15} + 7x_{13} + 10x_{26} + 8x_{27} +$$

$$5x_{23} + 12x_{34} + 4x_{47} + 7x_{49} + 12x_{57} +$$

$$11x_{56} + 13x_{69} + 2x_{79}$$

st. $1 = x_{12} + x_{15} + x_{13}$

$$x_{12} - x_{26} - x_{27} - x_{23} = 0$$

$$x_{13} + x_{23} - x_{34} = 0$$

$$x_{34} - x_{47} - x_{49} = 0$$

$$x_{15} - x_{56} - x_{57} = 0$$

$$x_{26} + x_{56} - x_{69} = 0$$

$$x_{27} + x_{57} + x_{47} - x_{79} = 0$$

$$x_{69} + x_{79} + x_{49} = 1$$

$$x_{ij} > 0, \forall (i, j) \in A$$

A is not
defined

$$c) \quad \min \quad 7x_{12} + 8x_{15} + 7x_{13} + 10x_{26} + 8x_{27} + \\ 5x_{23} + 12x_{34} + 4x_{47} + 7x_{49} + 12x_{57} + \\ 11x_{56} + 13x_{69} + 2x_{79}$$

$$st. \quad 30 = x_{12} + x_{15} + x_{13}$$

$$x_{12} - x_{26} - x_{27} - x_{23} = 0$$

$$x_{13} + x_{23} - x_{34} = 0$$

$$x_{34} - x_{47} - x_{49} = 0$$

$$x_{15} - x_{56} - x_{57} = 10$$

$$x_{26} + x_{56} - x_{69} = 0$$

$$x_{27} + x_{57} + x_{47} - x_{79} = 15$$

$$x_{69} + x_{79} + x_{49} = 5$$

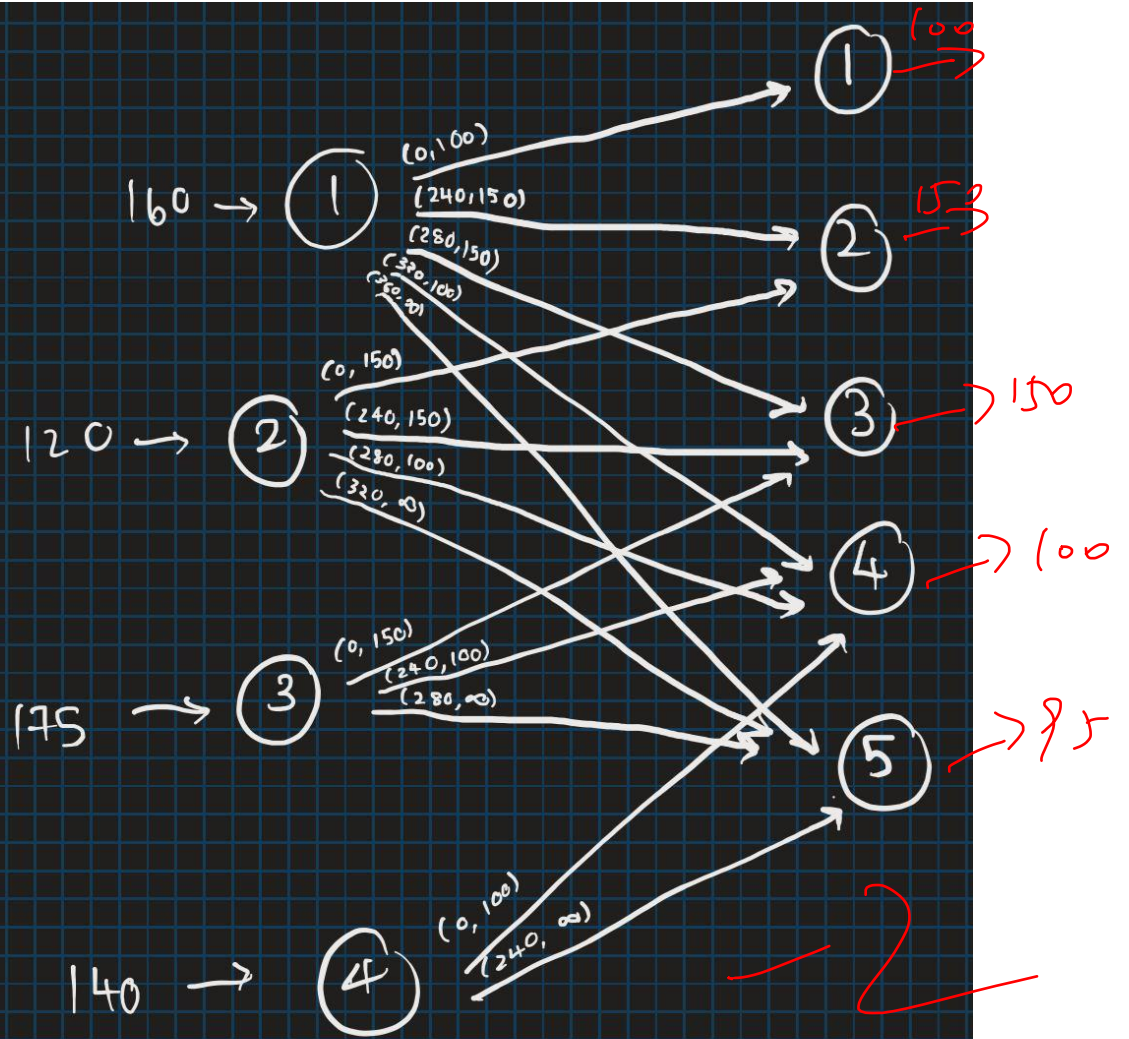
where are the capacity constraints?

$$x_{ij} \geq 0, \quad \forall (i, j) \in A$$

not defined.

Q5

a)



b)

$$\min \quad 240x_{12} + 280x_{13} + 310x_{14} + 360x_{15} + \\ 240x_{23} + 280x_{24} + 320x_{25} + \\ 240x_{34} + 280x_{35} + 240x_{45}$$

st.

$$160 = x_{11} + x_{12} + x_{13} + x_{14} + x_{15}$$

$$120 = x_{22} + x_{23} + x_{24} + x_{25}$$

$$175 = x_{33} + x_{34} + x_{35}$$

$$140 = x_{44} + x_{45}$$

$$x_{11} \leq 100$$

$$x_{12} + x_{22} \leq 150$$

$$x_{13} + x_{23} + x_{33} \leq 150$$

$$x_{14} + x_{24} + x_{34} + x_{44} \leq 100$$

$$x_{ij} \geq 0, \quad \forall (i,j) \in A$$

2

$$x_{15} + x_{25} + x_{35} + x_{45} + x_{55} = 95$$

not defined