

AI Planning for Autonomy

1. Plan & Goal Recognition

Speak Up Room: "COMP90054-2017-PGR", PIN: 39044

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Outline of the Lecture

- 1 Perceiving and Interpreting the Behavior of Others
- 2 Plan and Goal Recognition in AI
- 3 Plan and Goal Recognition and Classical Planning

The Heider-Simmel Experiment

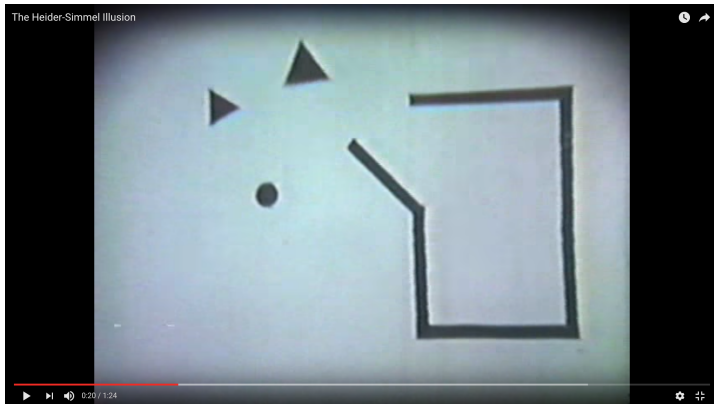


Figure: *An Experimental Study of Apparent Behavior.* F. Heider, M. Simmel.
The American Journal of Psychology, Vol. 57, No. 2, April 1944

[Link to video \(YouTube\)](#)

Parsing the Big Triangle



Figure: The BIG triangle T .

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Question!

What kind of person is the Big Triangle?

- | | |
|-------------------------------|------------------------|
| (A): Aggressive, mean, angry. | (B): Strong, powerful. |
| (C): Dumb, stupid. | (D): Ugly, sly. |

- (A): 97% of Heider & Simmel 1944 **experimental subjects** thought so.
- (B): 14% thought the Big triangle was a **bully**.
- (C): 8% didn't think T was very *bright*.
- (D): And a 2% were perhaps letting their **imagination go wild** a bit too much.

what about the Smaller one...



Figure: The small triangle t .

Question!

What kind of person is the Small Triangle?

(A): Fearless, defiant, cocky.

(B): Passive-aggressive.

(C): Clever, weak.

(D): Protective, loyal, devoted.

→ (A): 47% of the subjects chose words in this category.

→ (B): 11% found that t was a **bit unpleasant**.

→ (C): 53% had a lot of imagination.

→ (D): And 14% chose this one.

and about the circle...



Figure: The circle c .

Question!

What kind of person is the Circle?

(A): Frightened, fearful, helpless.

(B): Fidgety, playful, nervous.

(C): Clever, smart.

(D): Courageous.

→ (A): 75% of the subjects certainly *didn't think much* of c .

→ (B): And 61% found c a *bit of a handful*.

→ (C): 14% saw a *lot of nuance* in a black dot.

→ (D): And 11% found c to be *brave* (when T isn't around).

Significance of Heider & Simmel Results

Leaving *aside* possible issues with *priming* the experimental subjects...

It does clearly follow from the results that

- ① humans *tend* to **ascribe intentions** to pretty much *anything* that *changes* over time,
- ② this rests on *deeply rooted* **assumptions**.

Heider & Simmel results are the *first* **quantitative** characterization of:

Folk Psychology

Human capacity to **explain** and **predict** *behavior* and *mental state* of others

... we're *usually* *very good* at it, but we **fail often**!

A Theory of Common Sense

Proposed by **philosopher Daniel Dennett** on *The Intentional Stance* (1988)

- ① **Decide** to consider the object being observed as *rational*.
- ② Work out its **beliefs** and **goals** based on its *place* and *purpose* in the world.
- ③ Use **practical reasoning** to assess what the agent *ought to do* to pursue its **goals**.

The above provides a *systematic, reason-giving explanation* for actions, based on **deeply** embedded **beliefs** about the agent.

So Deep we are Barely Aware of Them

Typical Assumptions

- a) Agent's **actions** are *entirely* **rational**
 - cares about **some measure** of **value**, but may be **bad** at appraising it
- b) Actions are **reasonable** or follow some **law**
 - e.g. effects follow from **known** laws of physics, or economic **theories**
 - all models are **wrong**
- c) Beliefs and Goals held **for the duration** of the performance
 - may **change** their mind, we may be observing **reflex** action
- d) **Future** actions can be **systematically predicted** from beliefs and goals *ascribed*
 - we may be **missing possible** and **relevant goals**,
 - we may **lack enough time** to test **plausible explanations** exhaustively.

Several of them **false most of the time**, yet *rarely* **all** of them are.

Plan and Goal Recognition in Artificial Intelligence

Key Idea: use *generative* models of behavior to *predict* actions.

Plan Recognition (PR) is *Planning in reverse*.

- *Planning* – we seek *plans* π to *achieve* goals G .
- *PR*: find goals G *accounting for* partially *observed* plan π .

Multi-Agent setting

Two possible *roles* for each agent:

- **Actor** – *performs* actions to change the state of the world.
- **Observer** – *perceives* actions and updates its beliefs on the **Actor** intentions.

and three possible *stances* for the **Actor**:

- *Adversarial* – obfuscates deliberately its goals.
- *Cooperative* – tries to tell the **Observer** what she is up to.
- *Indifferent* – does not care about the **Observer**.

Open Challenge → Stances could be *changing over time*

The Elements of PR

Actions describe *what* the **Actor** does

- Walking from X to Y , opening a door, using a credit card...

Goals describe *what* the **Actor** wants

- To have breakfast, Plant a bomb, Troll the Interwebs...

Plans describe *how* goals can be *achieved*

- **Ordered** sequences of actions
- These can be **ranked** according to **cost** or **efficiency**

Sensor Model describes *what* does the **Observer** *perceives*

- Does it always see **every** action done by the **Actor**?
- Are actions observed **directly**? Or only their **effects** are?
- Does it know exactly **where** in the world the **Actor** is?

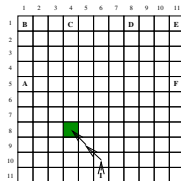
Example: Agent on a Grid World

	1	2	3	4	5	6	7	8	9	10	11
1	B			C				D			E
2											
3											
4											
5	A										F
6											
7											
8											
9											
10											
11						I					

- **starts** in "I", may head to "A", "B", ..., "F".
- **moves along compass directions** *North*, etc. with cost 1 and *North West*, etc. with cost $\sqrt{2}$.

Example

Actor now at (4,8) after going *N* once, and twice *NW*.



Question!

Assuming the Actor prefers **CHEAPEST** plans which goals are most likely?

(A): *A* & *B*.

(B): *C*.

(C): *D*

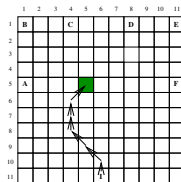
(D): *E* & *F*

→ (A) & (B): Cheapest plans for *A*, *B*, *C* **exist** with those **actions embedded**.

→ (C) & (D): Cheapest plans for *D*, *E* & *F* **do not have** those actions.

Example

Actor now at (5,5) after going *N* twice and once *NE*.



Question!

For which goal(s) observed actions are in a **CHEAPEST** plan?

(A): *A & B.*

(B): *C.*

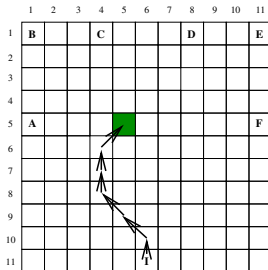
(C): *D, E & F*

(D): *None*

→(D) : Observed actions **are not** in any of the cheapest plans for **any** of the goals.

So Folk Psychology is Useless?

Perhaps, but as a **framework** is **useful** we can **extend** it.



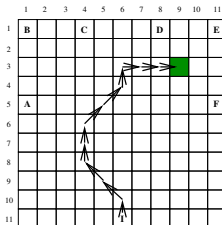
Idea to handle Non-Optimal Behaviour

Compare **best** plans that **comply** with observed actions, with best plans that **do not**.

→ Then it follows *B* and *C* **more likely** than *A* or **the rest**.

Example

Actor at (9, 3), has gone *NE*, *N* and three times *E*.



Question!

Now, which are the most likely goals?

(A): *A* & *B*.

(B): *C* & *D*.

(C): *E*

(D): *F*

→(C) : For *E* this difference is *minimal*.

Plan Recognition over Plan Libraries

Definition

PR problem defined as tuple $T = \langle \mathcal{G}, \mathcal{L}, A, O \rangle$ where

- \mathcal{G} is the set of **possible goals** G ,
- $\mathcal{L} = \bigcup \mathcal{L}(G)$ set of **possible plans** π for G , $G \subseteq \mathcal{G}$,
- O is **observation sequence** $(a_1, \dots, a_i, \dots, a_n)$, $a_i \in A$

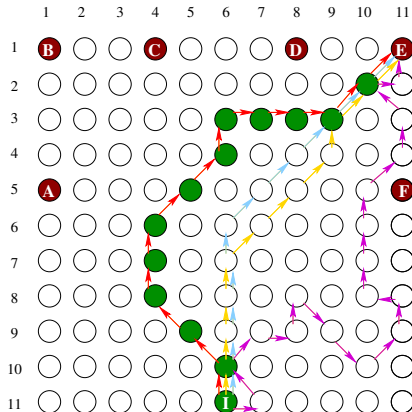
Key Property

An action sequence π **satisfies** O if O **embedded** in π .

Solution

A possible goal $G \in \mathcal{G}$ is **plausible** if \exists plan π in $\mathcal{L}(G)$ that **satisfies** O .

Plan Recognition over Plan Libraries: Limitations



4 plans:

- two optimal
- two valid

What plans get into \mathcal{L} ?

Why?

$|\mathcal{L}|$ **exponential** on size of grid to be **complete**.

Key Facts of the Model-Based Approach

- ① \mathcal{L} given **implicitly**, requires to **solve** $|\mathcal{G}|$ planning tasks
- ② Plans “**extracted**” with **off-the-shelf** planning algorithms.
- ③ **Plausibility** of goals \mathcal{G} given as a **probability distribution**

Plan Recognition As Planning (Ramirez & Geffner, 2009-10)

Define possible agent behavior **implicitly**, according to **general principles**:

- A STRIPS **planning domain** $P[\cdot]$,
- **Cost function** over **actions and/or states**,
- **Hypothetic** set of goals \mathcal{G} ,
- **General Knowledge** given as **prior probability** distribution over \mathcal{G} .

Assume the **Actor** **prefers lower cost** plans

- **Rationality Assumption** in *The Intentional Stance* (Dennett, 1987).

and is **indifferent** towards the **Observer**

Use **generic planners** to **compute** $P(G|O)$.

STRIPS: A Factored Representation of Planning Models

A STRIPS planning **domain** is the tuple $P[\cdot] = \langle F, I, A \rangle$ where

- F is the set of **fluents**.
- $I \subseteq F$ is **initial** situation.
- A set of STRIPS **actions**, $Pre(a), Add(a), Del(a) \subset F$.

A planning **problem** $P[G]$ is domain P and goal $G \subseteq F$.

Solution of $P[G]$ is a **valid** sequence of actions, or **plan**

$$\pi = (a_1, \dots, a_n)$$

Defining Plans as Constrained Action Sequences

Hard Constraints: Valid plans for $P[G]$, is sequence $\pi = (a_1, \dots, a_n)$ s.t.

- 1 $Pre(a_1) \subseteq I$,
- 2 $Pre(a_i) \subseteq I[a_1, \dots, a_{i-1}]$ for $i > 1$,
- 3 $G \subseteq I[a_1, \dots, a_n]$.

Soft Constraints: The cost of a plan π is

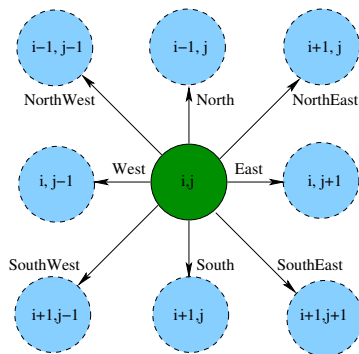
$$c(\pi) = \sum_{a \in \pi} c(a)$$

Valid plans are optimal when they have minimum cost.

The cost of $P[G]$, $c^*(P[G])$, is the cost of an optimal plan.

Example: STRIPS Model

Fluent set $F = \{p_{i,j} | 1 \leq i, j \leq 11\}$, state space $S = 2^F$ (**power set**)



Actions A are:

- $N_{i,j}$: $Pre = \{p_{i,j}\}$, $Add = \{p_{i-1,j}\}$, $Del = \{p_{i,j}\}$, $c(N_{i,j}) = 1$
- $E_{i,j}$: $Pre = \{p_{i,j}\}$, $Add = \{p_{i,j+1}\}$, $Del = \{p_{i,j}\}$, $c(E_{i,j}) = 1$
- $NW_{i,j}$: $Pre = \{p_{i,j}\}$, $Add = \{p_{i-1,j-1}\}$, $Del = \{p_{i,j}\}$, $c(NW_{i,j}) = \sqrt{2}$

Example: STRIPS Model (2)

Initial state:

$$I = \{p_{11,6}\}$$

Five goals:

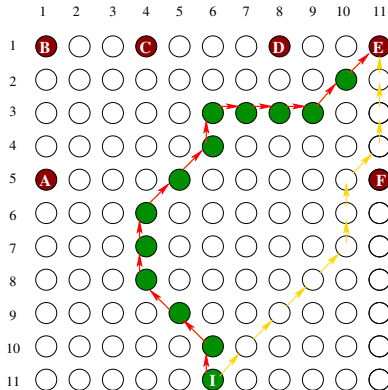
$$G_A = \{p_{5,1}\}$$

$$G_B = \{p_{1,1}\}$$

...

$$G_E = \{p_{1,11}\}$$

$$G_F = \{p_{5,11}\}$$



Execution:

$$s_0 = \{p_{11,6}\}$$

$$s_1 = \{p_{10,6}\}$$

$$s_2 = \{p_{9,5}\}$$

...

$$s_7 = \{p_{4,6}\}$$

...

$$s_{13} = \{p_{1,11}\}$$

- **Valid** plan for $P[G_E]$: $\pi = (N_{11,6}, NW_{10,6}, \dots, NE_{3,9}, NE_{2,10})$
- **Optimal** plan: $\pi = (NE_{11,6}, NE_{10,7}, \dots, NE_{3,11}, NE_{2,11})$

Demo: A Slightly More Interesting STRIPS Model



Fluents: *facts about the world*

- Locations of people
- State of appliances
- Locations of objects

Actions: *stuff people may do*

- Move across the place
- Interaction with objects & appliances

Goals: *why people do stuff*

- Cook some foodstuff
- Watch a movie
- Listen to a record
- Go to sleep
- Get ready to leave for work

Unitary action costs (to keep it simple)

[GITHUB Repo](#)

Roadmap

- 1 Make off-the-shelf planners to compute plans constrained w.r.t. O ,
- 2 Derive $P(G|O)$ from best plans that comply with or work around O .

Computing Plans that Satisfy O

Problem

To find **efficiently** what plans **satisfy** O with an **unmodified** planner.

Idea #1: Plan Constraints

Constrain plans to **embed** (or **avoid so**) O **requiring extra dummy** goals through **changing preconditions and effects**

Idea #2: Implicit Sorting of Plans

For each $G \in \mathcal{G}$, formulate **two** planning tasks, **splitting** set of valid plans

- ① π plan for $P[G]$ that **satisfies** O **iff** π plan for $P'[G + O]$
- ② π plan for $P[G]$ that **doesn't satisfy** O **iff** π plan for $P'[G + \overline{O}]$

PR as planning: Inferring the Goal Probabilities

Goal

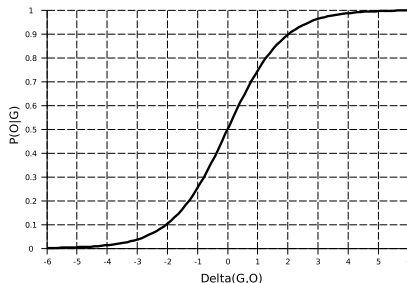
Obtain **probability distribution** $P(G|O)$, $G \in \mathcal{G}$.

Outline of Approach

From **Bayes' Rule** $P(G|O) = \alpha P(O|G) Prob(G)$, where

- α norm. constant
- $Prob(G)$ given in problem specification
- $P(O|G)$ function of extra cost needed to not comply with O

$$P(O|G) = \text{function}(c^*(P'[G + \overline{O}])) - c^*(P'[G + O]) \quad (1)$$

$P(O|G)$ and $P(\overline{O}|G)$ 

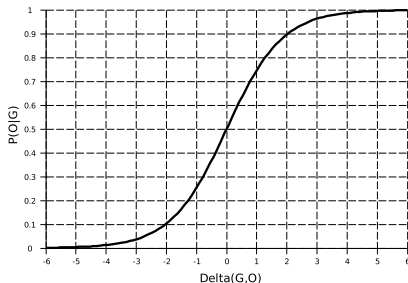
Ramirez & Geffner Observer Model (AAAI, 2010)

$$P(O|G) = \text{sigmoid}(\beta \Delta(G, O))$$

where

$$\Delta(G, O) = c^*(P'[G + \overline{O}]) - c^*(P'[G + O])$$

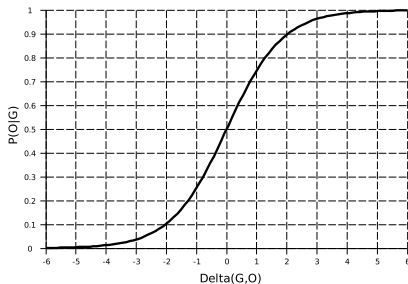
Goals as Predictors for O (informally)



Properties

- 1 G predicts O **badly** when it would be **more efficient** to deviate from O .
- 2 G predicts O **perfectly** when G **unfeasible** if **not doing** O .

Goals as Predictors for O (formally)



Properties

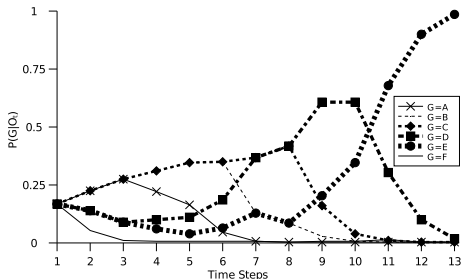
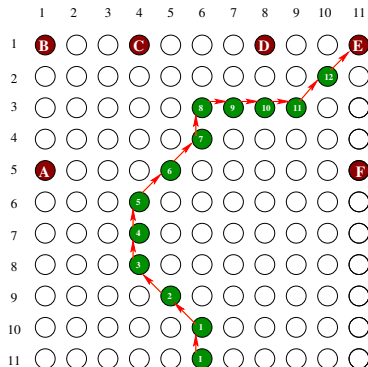
- ① G predicts O **badly** when $P(O|G) < P(\overline{O}|G)$ since

$$c^*(P'[G + \overline{O}]) < c^*(P[G + O])$$

- ② G predicts O **perfectly** when $P(O|G) = 1$ since

$$c^*(P'[G + \overline{O}]) = \infty$$

Example



- After $N_{11,6}$, $NW_{10,6}$, $NW_{9,5}$, most likely: A, B and C.
- After $N_{8,4}$, $N_{7,4}$, $NE_{6,4}$, most likely: B and C.
- After $NE_{5,5}$, ..., $E_{3,8}$, most likely: E.

Prob. PR as Planning: Summary

A **plan recognition problem** is a tuple $T = (P, \mathcal{G}, O, Prob)$ where

- P is a **planning domain** $P = (F, I, A)$
- \mathcal{G} is a set of **possible goals** $G, G \subseteq F$
- O is the **observation sequence** $(a_1, \dots, a_n), a_i \in O$
- $Prob$ is **prior distribution** over \mathcal{G}

Posterior distribution $P(G|O)$ obtained from

- **Bayes Rule** $P(G|O) = \alpha P(O|G) Prob(G)$ and
- **Likelihood** $P(O|G) = sigmoid\{\beta [c^*(P'[G + \overline{O}]) - c^*(P'[G + O])]\}$
 $c^*(P'[G + O])$ and $c^*(P'[G + \overline{O}])$ **computed**
 - **exactly** with an **optimal** planner
 - **approximately** with a **sub-optimal** planner

In either case, $2 \cdot |\mathcal{G}|$ planner calls are needed for $P(G|O)$

Further Reading or Watching

- Article** *An Experimental Study of Apparent Behavior*. F. Heider, M. Simmel. The American Journal of Psychology, 57(2), 1944
- A Probabilistic Plan Recognition Algorithm based on Plan Tree Grammars* C. Geib, R. Goldman, Artificial Intelligence 173(11), 2009
- Probabilistic Plan Recognition using off-the-shelf Classical Planners*. M. Ramirez and H. Geffner. Proceedings AAAI, 2010.
- Landmark-Based Heuristics for Goal Recognition*. R. Pereira, N. Oren and F. Meneguzzi. Proceedings AAAI, 2017.
- Heuristic Online Goal Recognition in Continuous Domains*, M. Vered and G. Kaminka. Proceedings IJCAI, 2017.
- Book** *Chapter 4, Section 4.3 A Concise Introduction to Models and Methods for Automated Planning*. B. Bonet & H. Geffner, Morgan Claypool, 2013.
- Video** *Lecture Engineering & Reverse-engineering Human Common Sense*, J. Tenenbaum, Allen Institute for AI, 2015.