

# Help Mayor Editorial

There are  $O(R)$  lines that intersect with the circle and that can be represented as  $x = c$  (where  $c$  is an integer).

For each of them, we can apply Pythagorean theorem to find the range of  $y$  coordinates of the intersection of the line and the circle, so we can find the number of lattice points that is within the circle and on the line  $x = c$ .

However, the floating-point error is a big issue here.

For example, given  $(X, Y) = (-0.0001, 0)$ ,  $R = 100000$ , when calculating the upper bound of the intersection of line  $x = 0$  and the circle, we have to calculate  $(10^5)^2 - (10^{-4})^2$ , which requires far more precision than double type.

To resolve the issue, multiply  $X$ ,  $Y$ ,  $R$  by  $10^4$  to make them integers. Then, we can count the number of points where both  $x$  and  $y$  are multiples of  $10^4$ .

Just like before, there are  $O(R)$  lines that intersect with the circle and that can be represented as  $x = 10^4 c$  (where  $c$  is an integer), so it can be solved in the similar way. Since entire calculation are done with integer, we don't have to care about precision errors.

The complexity is  $O(R \log(R))$  in total, with assumption that calculating the square root requires an  $O(\log(R))$  time.

Since  $X$ ,  $Y$  and  $R$  cannot be inputted precisely in most cases, just multiplying them by  $10^4$  may not precisely results in integers. Therefore, use proper functions to round into integers, such as round function in C++. (In C++, a double value is rounded to int value in the direction of 00, so an attempt to convert to int after adding 0.5 fails if it is negative)