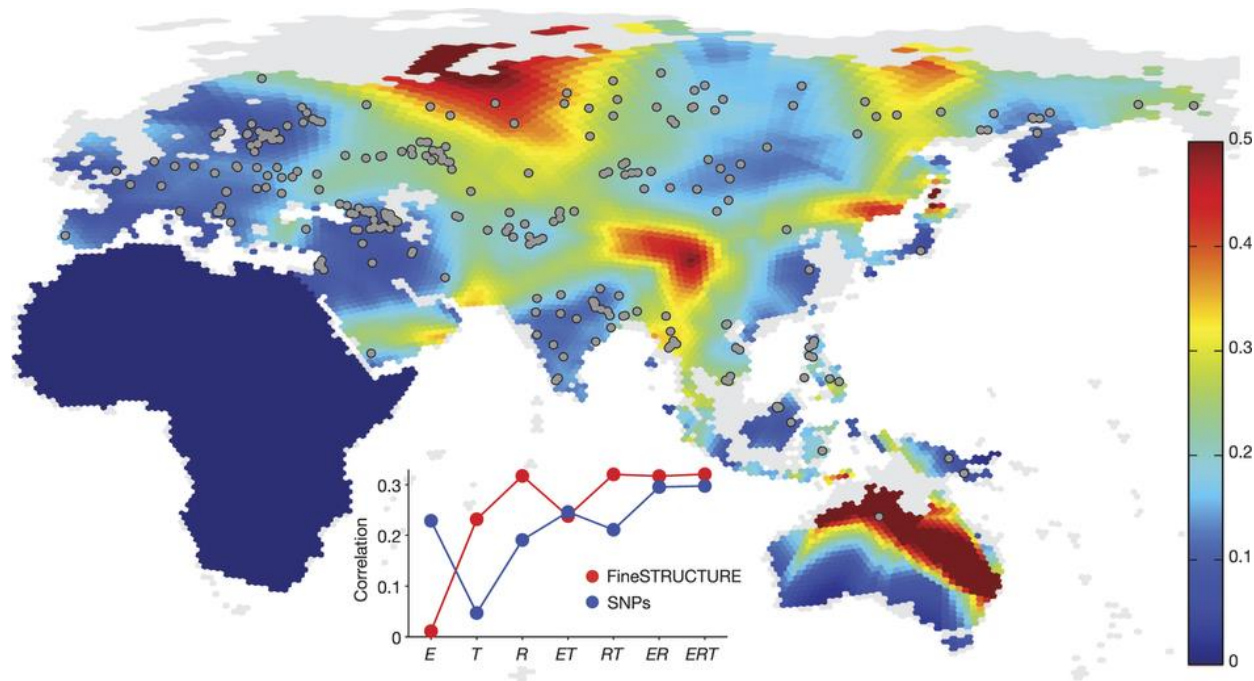


# Quantifying relationships among populations: Many populations



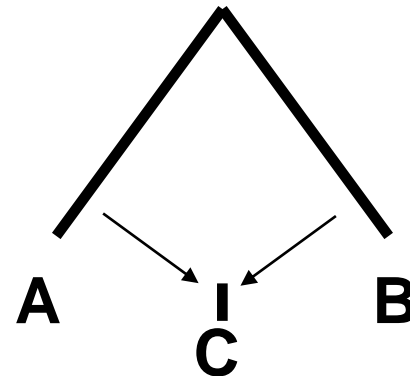
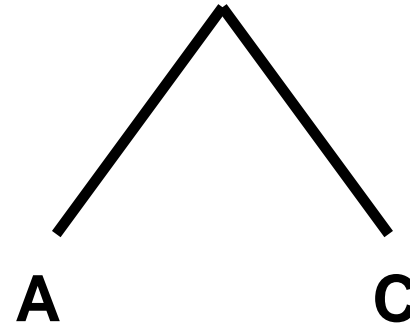
Andrea Manica



UNIVERSITY OF  
CAMBRIDGE

# Outline

- Generalising  $f_4$
- Quantifying distances between populations
- Building trees
- Admixture Graphs
- Some spatial statistics



## qpWave: generalising $f_4$

0

1

2

L: pop\_a, pop\_b, pop\_c

0

1

2

R: pop\_d, pop\_e, pop\_f

$$X(l_i, r_i) = f_4(l_0, l_i; r_0, r_i)$$

rank + 1  $\leq$

n waves

$$f_4(a, b; d, e)$$

$$f_4(a, b; d, f)$$

$$f_4(a, b; d, e)$$

$$f_4(a, b; d, e)$$

## qpAdm: estimating proportions from multiple sources

T: pop\_t

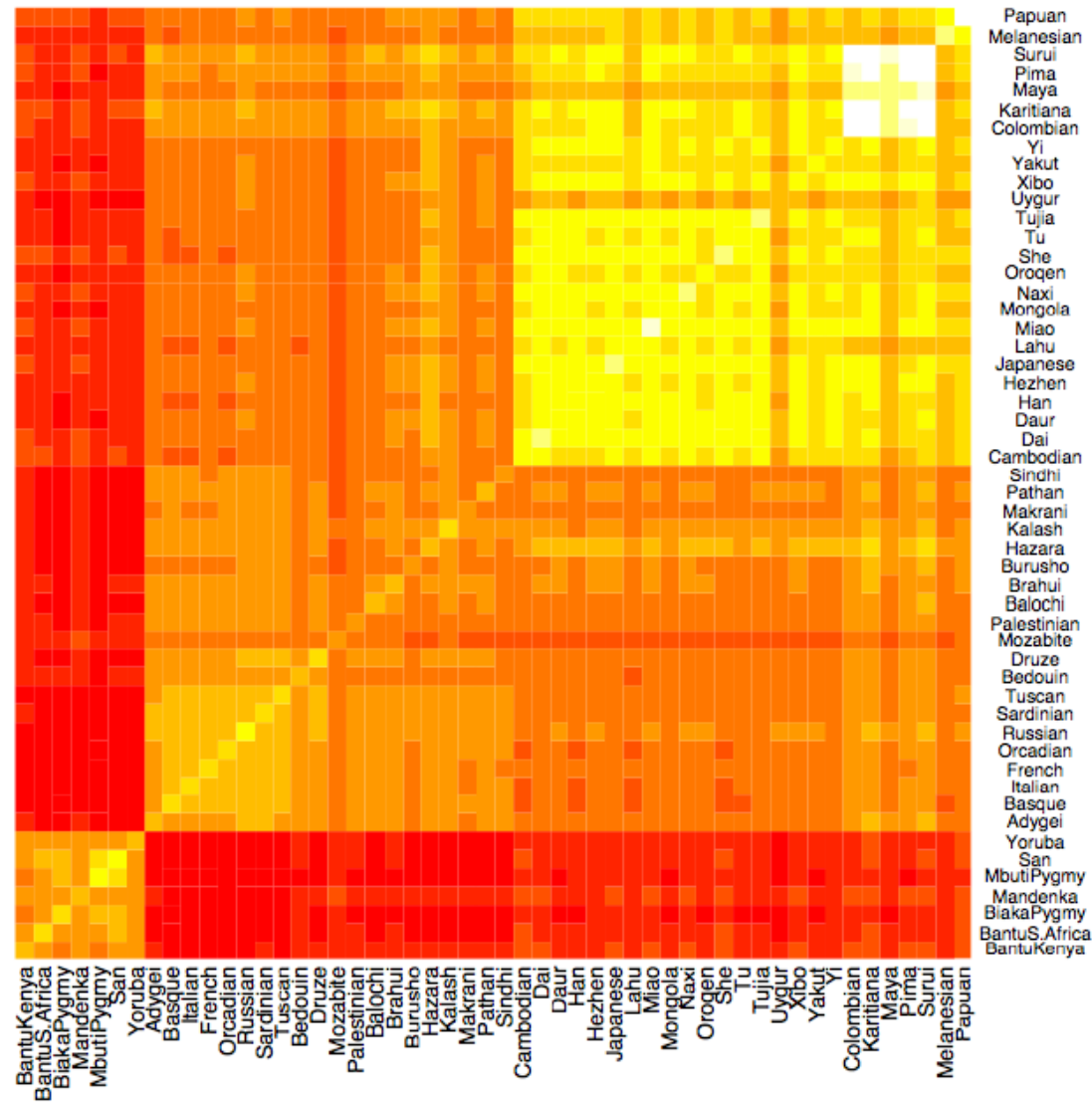
S: pop\_a, pop\_b, pop\_c

R: pop\_d, pop\_e, pop\_f

$$T = \sum_{i=1}^n w_i s_i$$

$$\begin{aligned} \sum_i w_i f_4(T, s_i, r_1, r_2) &= f_4(T, T, r_1, r_2) \\ &= 0 \end{aligned}$$

# Quantifying distances among populations



## Quantifying distances among populations

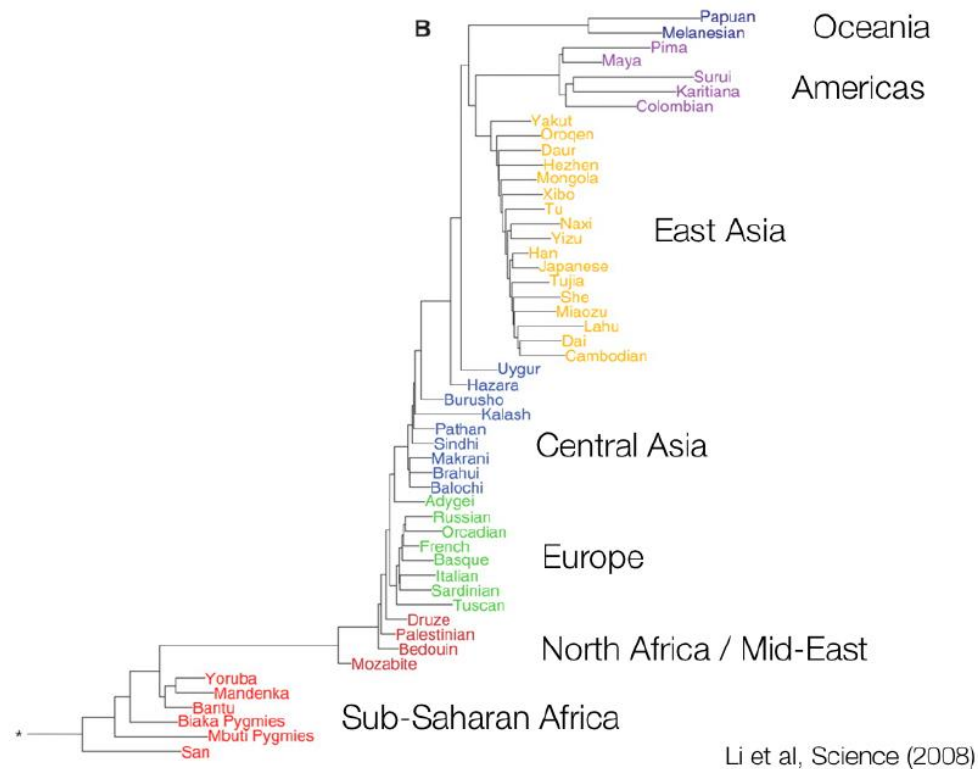
$$f_2(A,B) = E[(p_A - p_B)^2]$$

$$\hat{F}_2(P_1, P_2) = \pi_{12} - \frac{\pi_{11} + \pi_{22}}{2}.$$

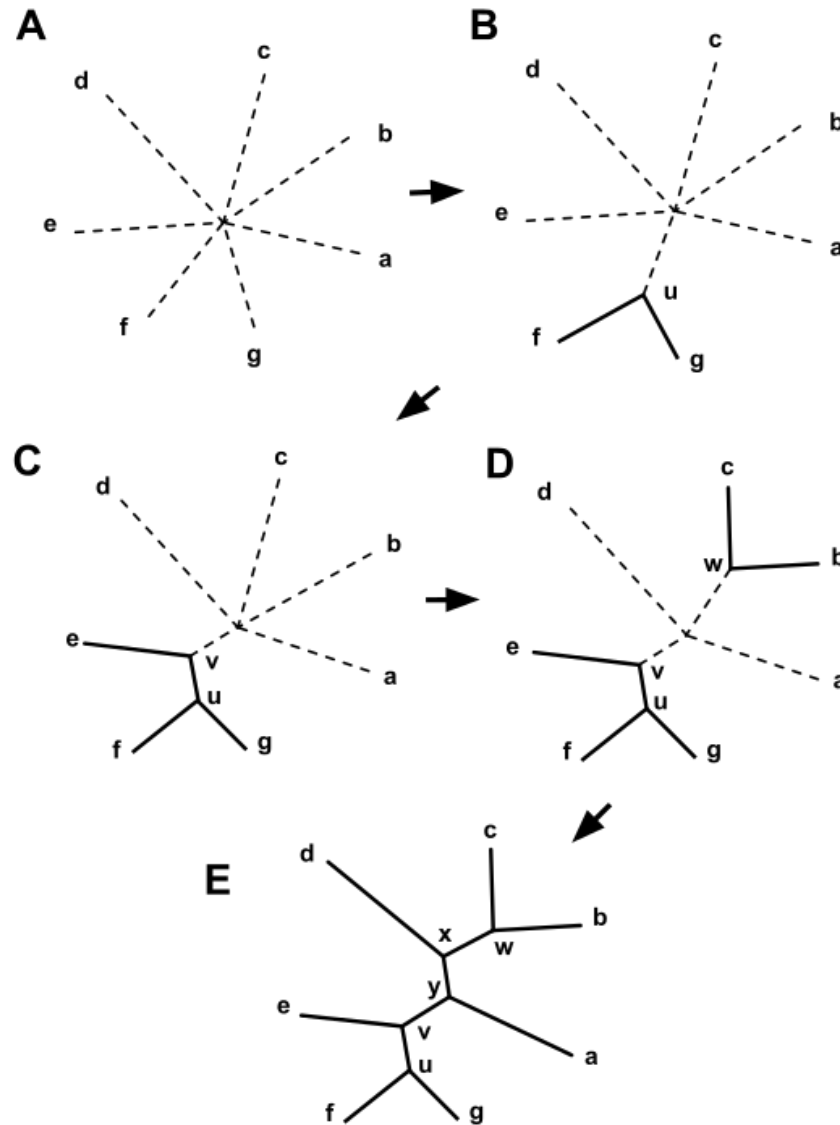
$$F_2(P_1, P_2) = \frac{1}{2} F_{ST} \mathbb{E} H_{\text{exp}}.$$

$$F_2(P_1, P_2) = 2\mathbb{E} T_{12} - \mathbb{E} T_{11} - \mathbb{E} T_{22}$$

# Quantifying distances among populations

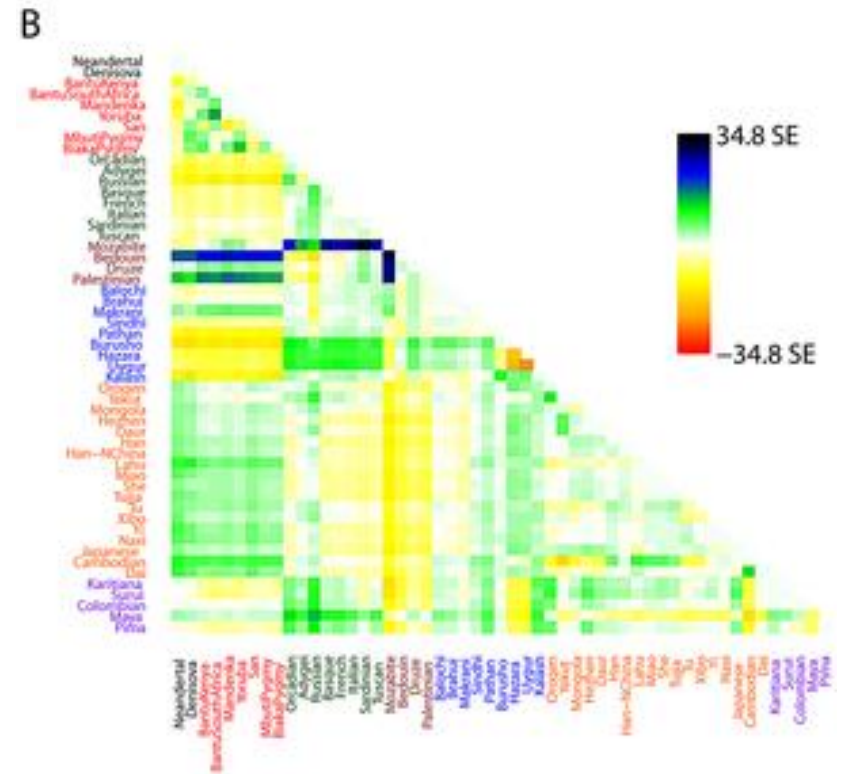
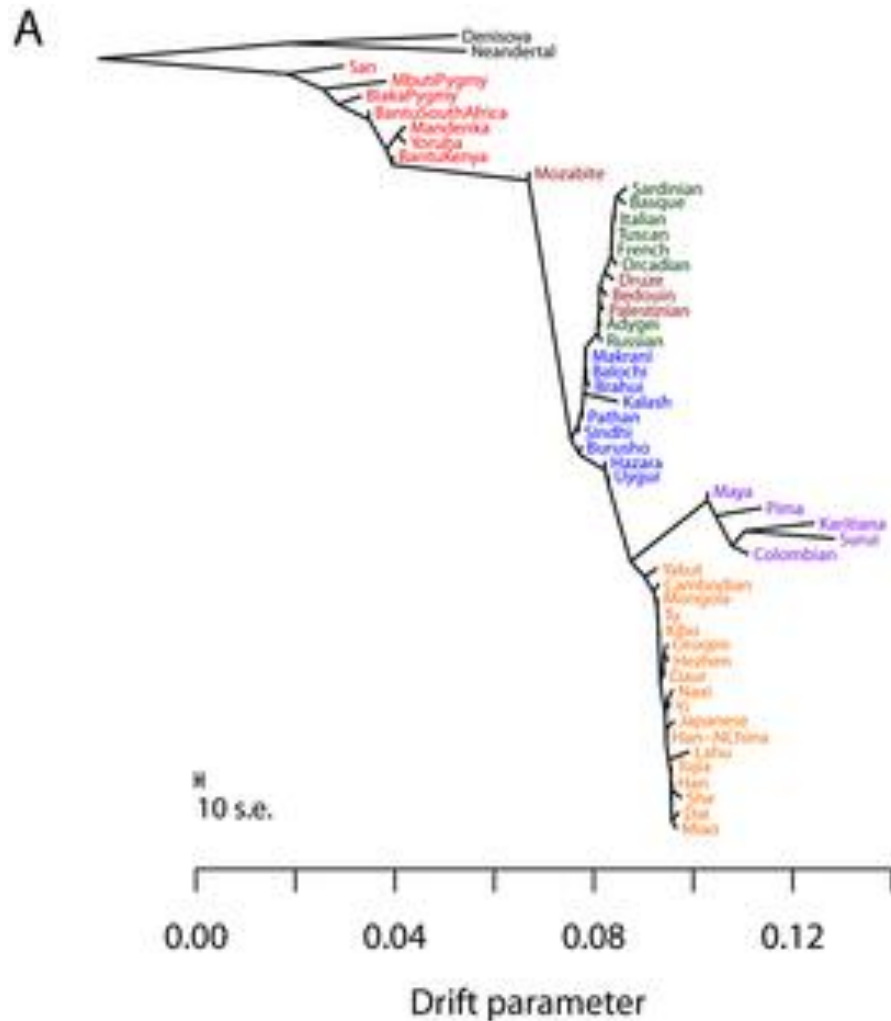


# Neighbour Joining trees

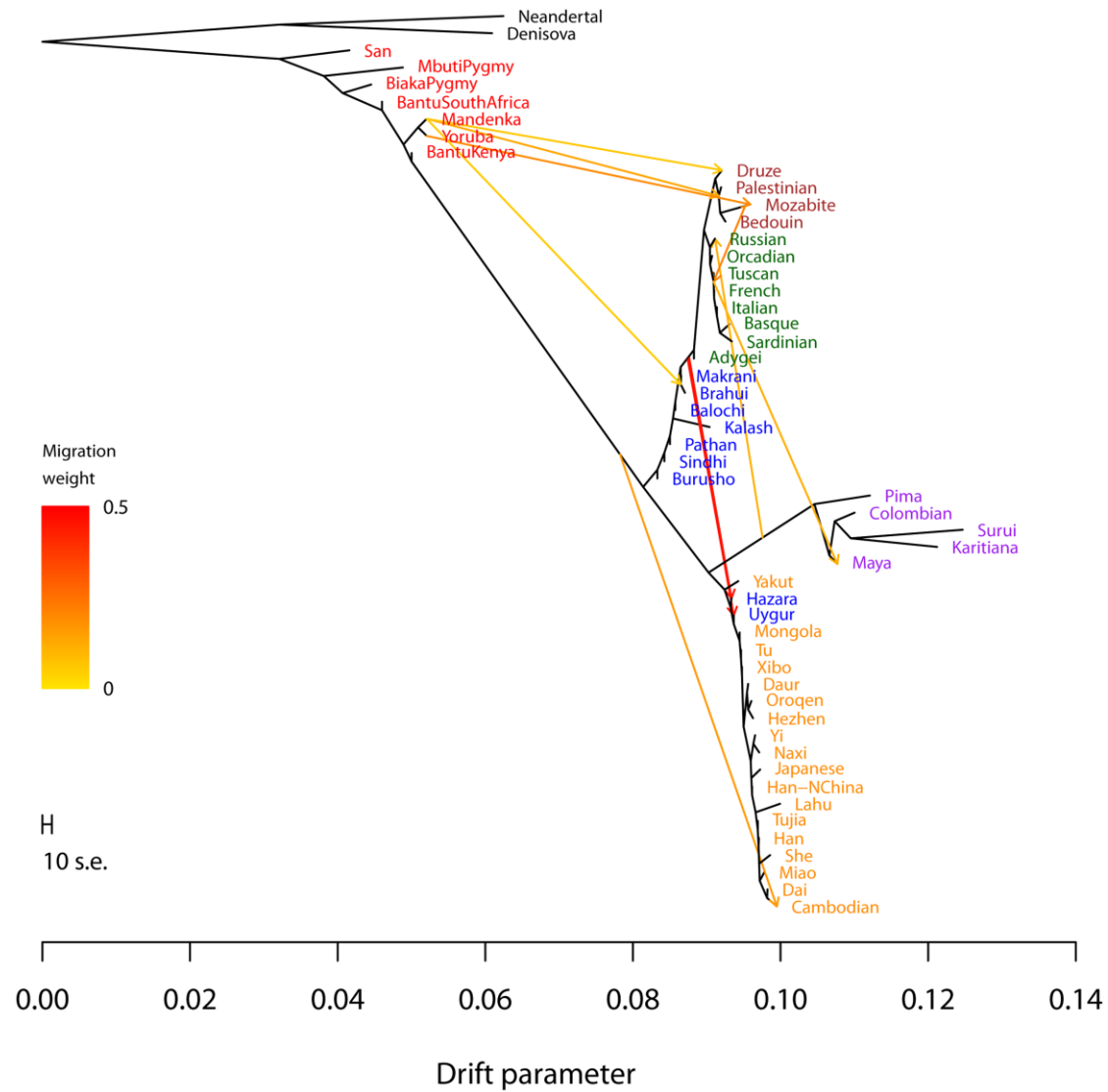




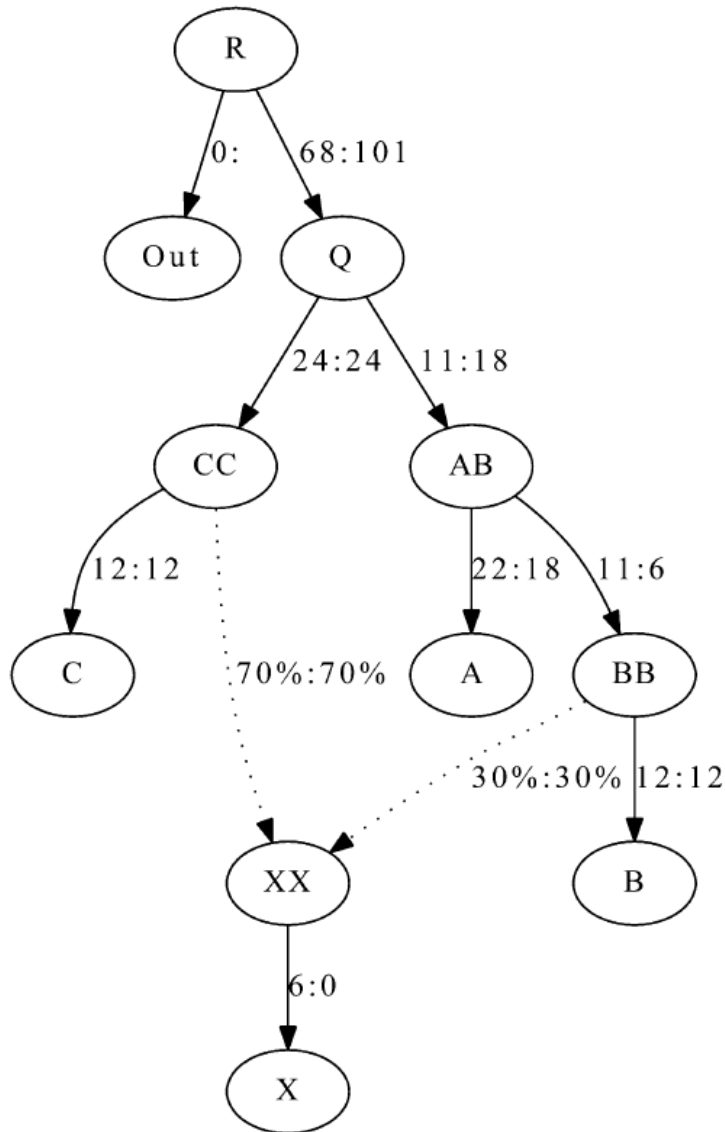
# Breaking the tree



# Treemix



# qpGraph



Fitted on  $f_2$  or  $f_3$

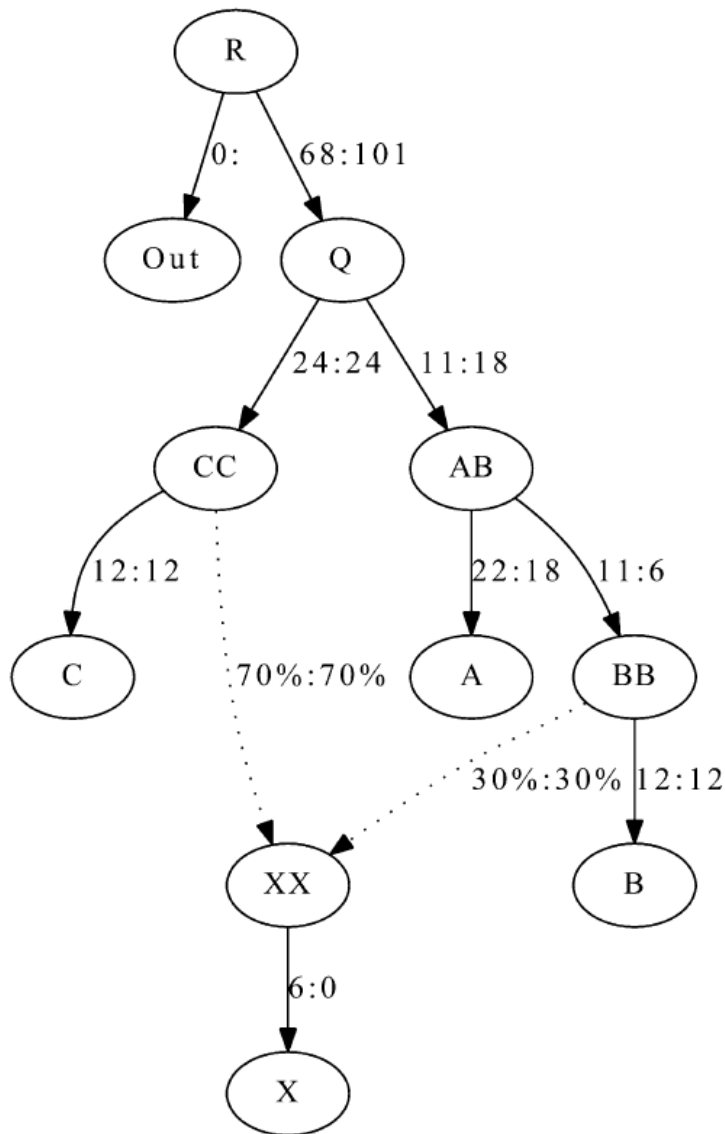
First fit unadmixed skeleton

Then test admixture  
scenarios

Check for mismatches in  
predicted vs observed  $f_3$   
and  $f_4$

Not exhaustive, multiple  
graphs might fit data  
equally

# qpGraph – changing philosophies

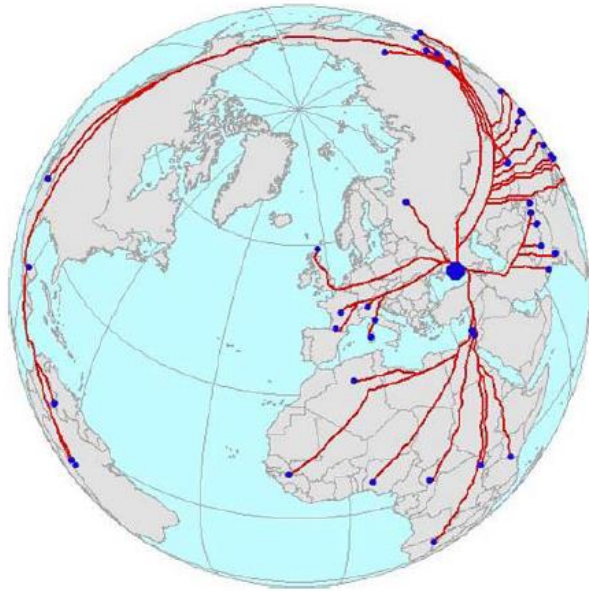


Even for simple scenarios, there are many graph that fit the data

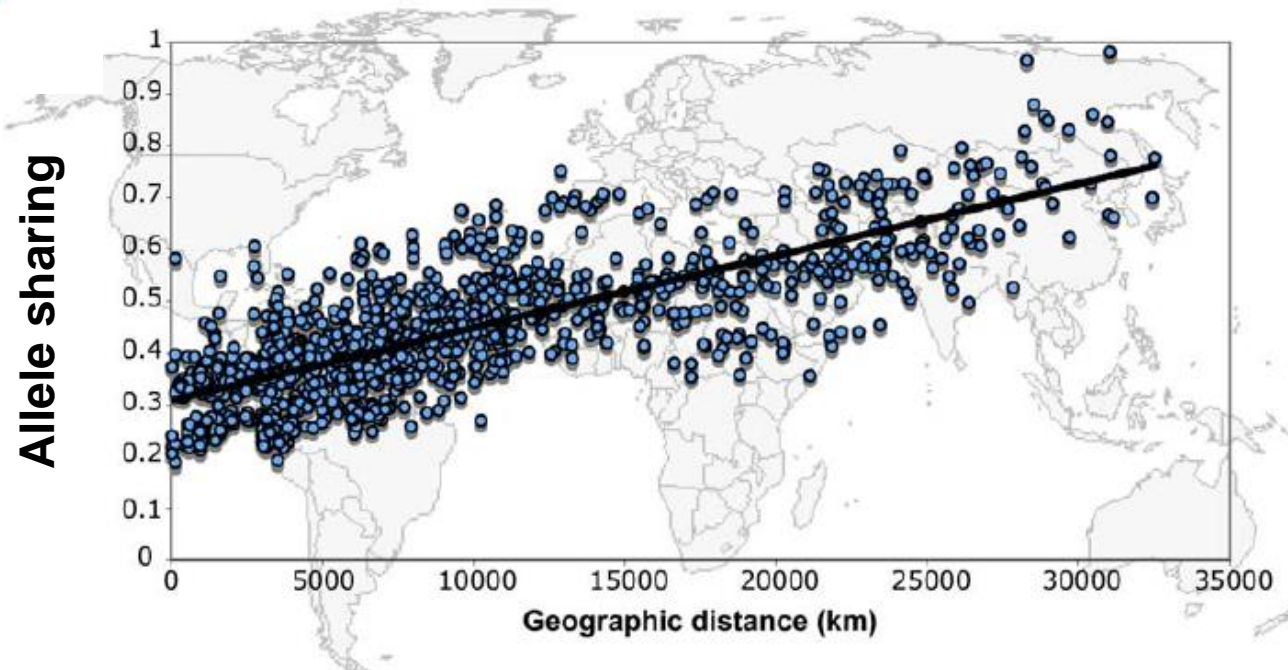
Manual searches are not enough

Extensive searches are needed, and evidence from admixture graphs needs to be complemented with other approaches

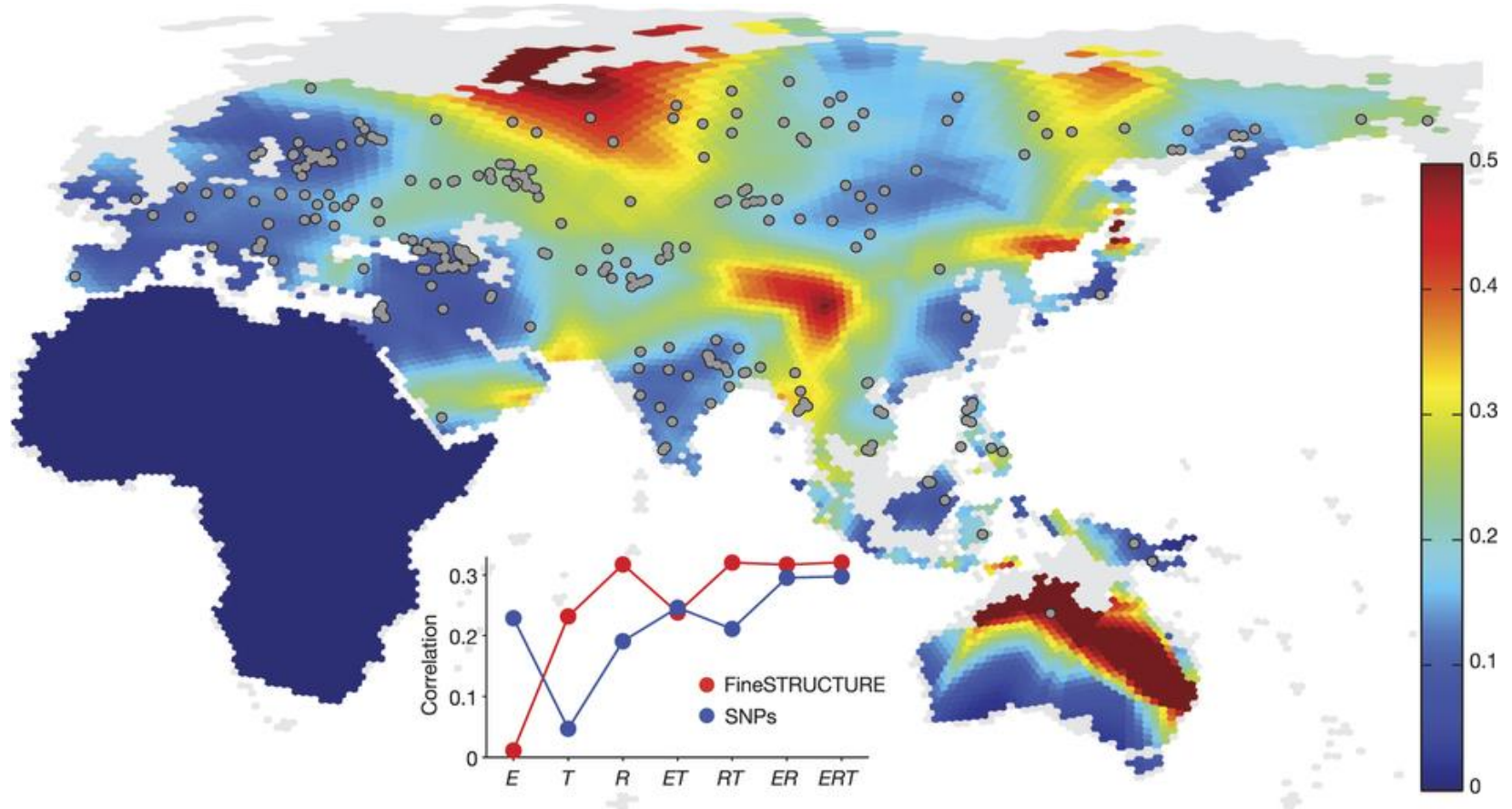
# Using space to model many populations



Isolation by distance can explain a lot of differences

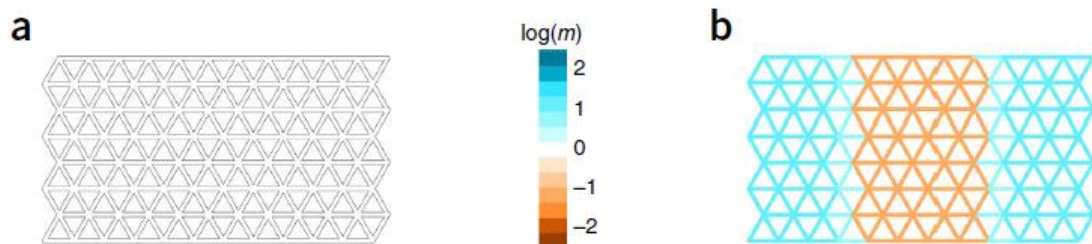


# Barriers for human movement

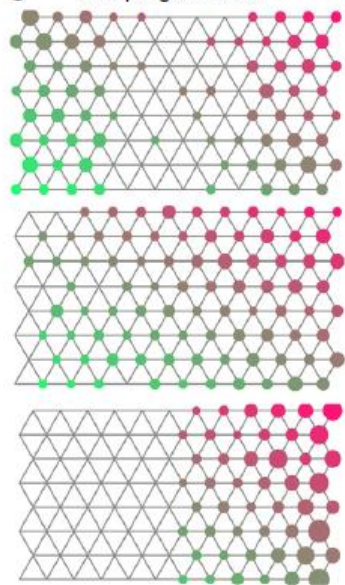




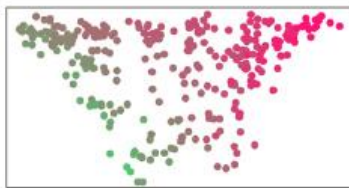
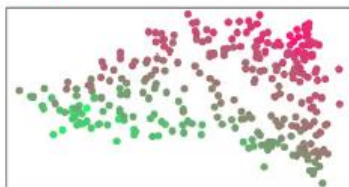
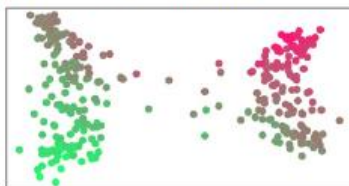
# EMMS



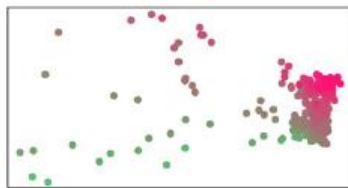
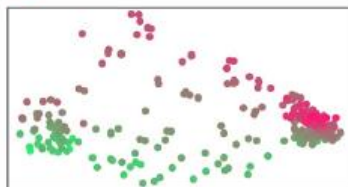
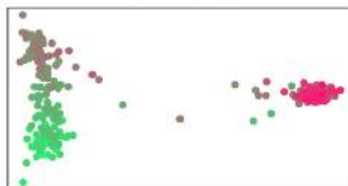
**c** Sampling schemes



**d** PCA: uniform



PCA: barrier



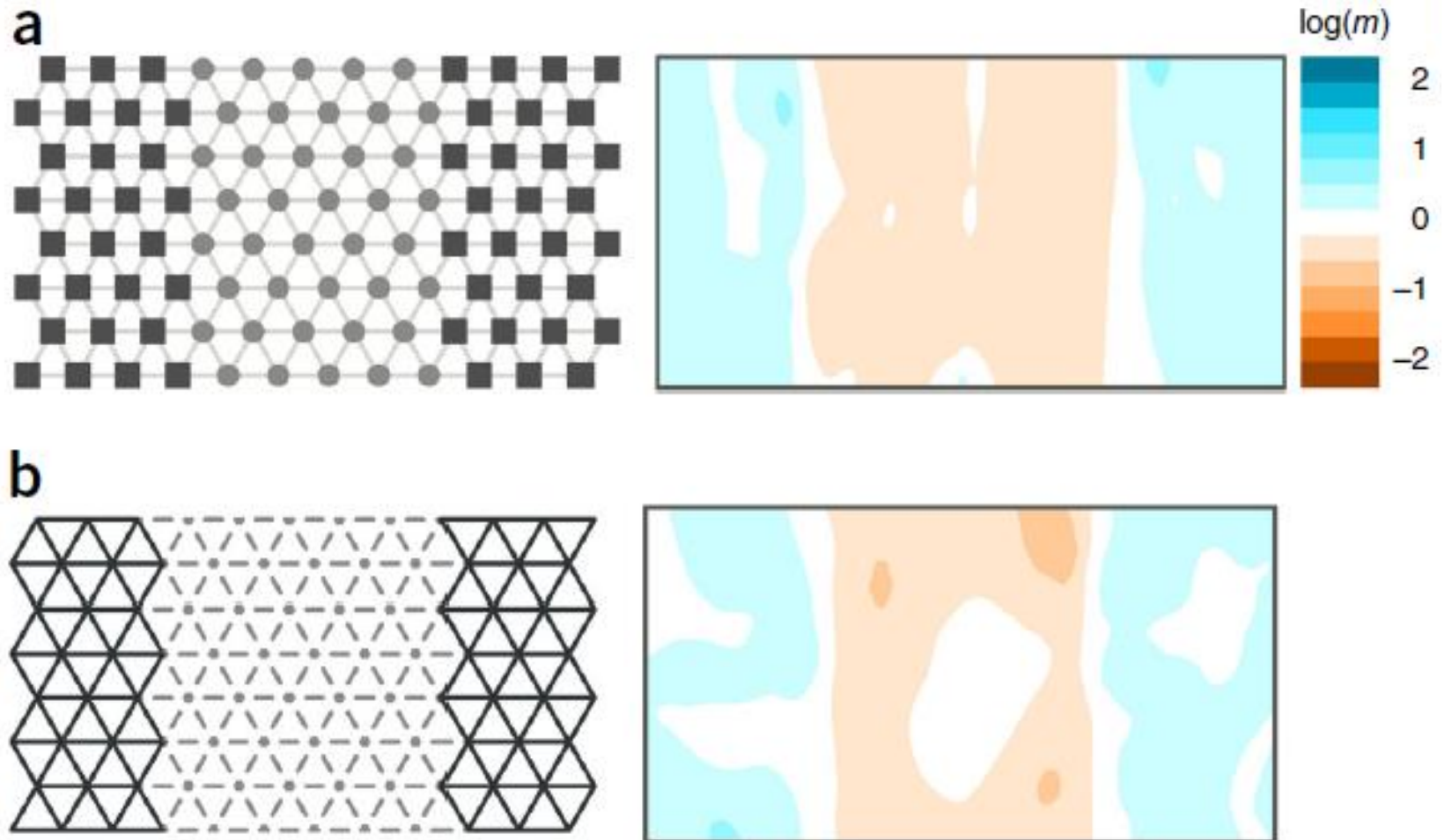
**e** EEMS: uniform



EEMS: barrier



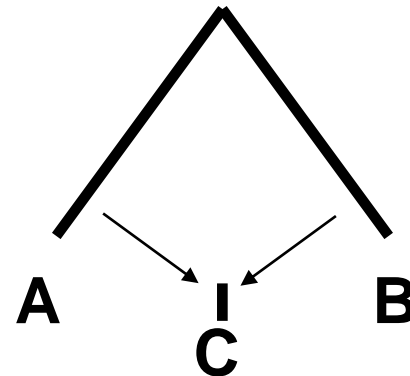
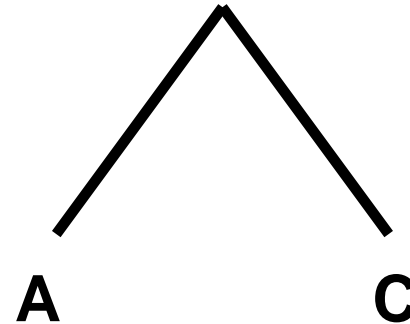
# EMMS – migration vs population size





# Outline

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# Practical

- Use Admixtools to fit admixture graph
- Human dataset with modern and ancient