$$F_{ij} = \sum_{\mu\nu} C_\mu^j C_\nu^i \left\langle \phi_\mu \right| \hat{F} \left| \phi_\nu \right\rangle = \sum_{\mu\nu} C_\mu^j C_\nu^i F_{\mu\nu}$$