

Recursion (class 2)

11-03-2023

Date.....

Que climbing stairs.

You are climbing a staircase. It takes n steps to reach the top. Each time you can either climb 1 or 2 steps.

In how many ways can you climb to the top.

for example:-

Input, $n = 2$

Output, 2

Explanation, There are two ways to climb to the top.

2 ways to climb to stair 2 { way 1, 0 to 1 + 1 to 2
1 step + 1 step,
i.e., 2 steps.
way 2, 2 steps.

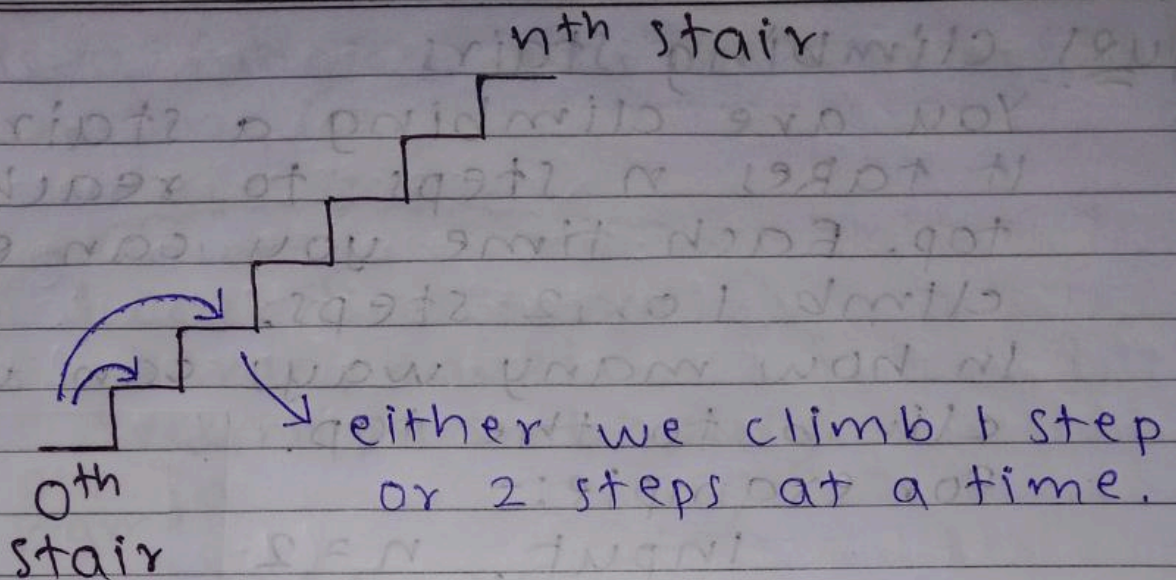
for example:-

Input, $n = 3$

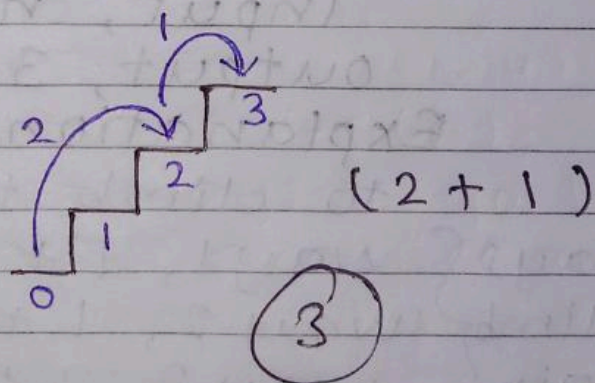
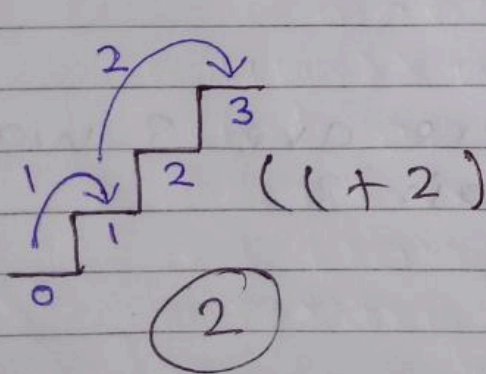
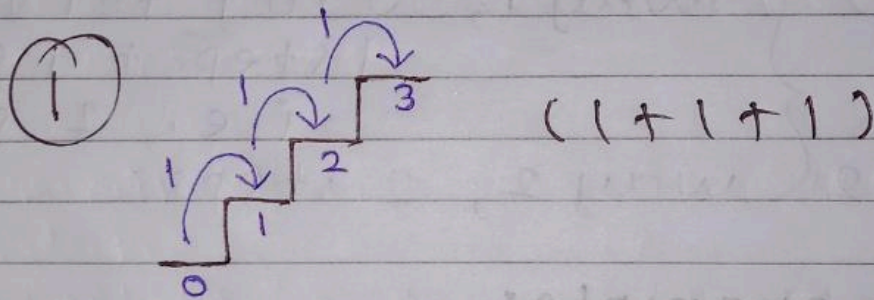
output, 3

Explanation, There are 3 way to climb to stair 3.

3 ways to climb to stair 3 { way 1, 1 + 1 + 1
way 2, 1 + 2
way 3, 2 + 1



To climb at stair 3, the no. of ways are :-



In this problem, rather than we think that how to go from 0th stair to nth stair, we directly think that how we get on nth stair.

n^{th} stair pe pahuchne ke 2 ways hai, either we came from $n-1^{\text{th}}$ stair by taking 1 step or we came from $n-2^{\text{th}}$ stair by taking 2 steps. There is no other way to reach at n^{th} stair.

$$\left[\text{climb}(n) = \text{climb}(n-1) + \text{climb}(n-2) \right]$$

↙ recursive relation for this question.

This recursive relation is same as of the Fibonacci series recursive relation.

Here, we just solved for only 1 case, i.e., for last n^{th} stair & rest for all stairs recursion automatically solve the problem.

code:-

```

#include <iostream>
using namespace std;
int climbstairs(int n) {
    if (n == 0) {
        return 1;
    }
    if (n == 1) {
        return 1;
    }
    int ans = climbstairs(n-1) +
               climbstairs(n-2);
    return ans;
}

int main() {
    int n;
    cout << "enter which stair you
    want to go: ";
    cin >> n;
    int ans = climbstairs(n);
    cout << "No. of ways to go to
    stair " << n << " are: " << ans;
    return 0;
}

```

} 1 way to go on 0th stair from 0th stair (jump)
 } 1 way to go on 1st stair from 0th stair.

Ques Traverse on array using recursion.

```
#include <iostream>
using namespace std;
// recursive approach
void printArray (int arr[], int n,
                int i)
{
    // base case
    if (i >= n) {
        return;
    }
    cout << arr[i] << " ";
    printArray (arr, n, i+1);
}

int main()
{
    int arr[] = {10, 20, 30, 40, 50, 60};
    int n = 6;
    int i = 0;
    printArray (arr, n, i);
    return 0;
}
```


Que: find maximum number in an array using recursion.

```
#include<iostream>
using namespace std;
void findMax(int arr[], int n,
             int &maxi, int i)
{
    //base case
    if (i >= n) {
        return;
    }
    if (arr[i] > maxi) {
        maxi = arr[i];
    }
    findMax(arr, n, maxi, i+1);
}

int main()
{
    int arr[] = {10, 20, 70, 68, 80, 49, 15};
    int n = 7;
    int i = 0;
    int maxi = INT_MIN;
    findMax(arr, n, maxi, i);
    cout << "Max no. is " << maxi;
    return 0;
}
```

↓
passed as
reference for
change in the
original value.

Ques: Find minimum number in an array using recursion.

```
#include <iostream>
using namespace std;
void findMin(int arr[], int n,
             int &mini, int i)
{
```

```
    // base case
```

```
    if (i >= n) {
```

```
        return;
```

```
    }
```

```
    if (arr[i] < mini) {
```

```
        mini = arr[i];
```

```
    }
```

```
    findMin(arr, n, mini, i++);
```

```
}
```

```
int main ()
```

```
{
```

```
    int arr[] = {10, 20, 70, 3, 2, 80};
```

```
    int n = 6;
```

```
    int i = 0;
```

```
    int mini = INT_MAX;
```

```
    findMin(arr, n, mini, i);
```

```
    cout << "Min no. is " << mini;
```

```
    return 0;
```

```
}
```


Ques Traverse string using Recursion.

```
#include <iostream>
using namespace std;
void findChar (string str, int n,
               char c, int i, int &charIndex)
{
    // base case
    if (i >= n) {
        return;
    }
    if (str[i] == c) {
        charIndex = i;
    }
    findChar (str, n, c, i+1, charIndex);
}

int main ()
{
    string str = "baabubhaiya";
    int n = str.length();
    int i = 0;
    char c = 'y';
    int charIndex;
    findChar (str, n, c, i, charIndex);
    cout << "Index where the char-
    -acter " << c << " is found is : " <<
        charIndex << endl;
    return 0;
}
```


→ Print every index where the characters found.

```
if (str[i] == c) {  
    cout << "Found at" << i;  
}
```


Ques Given a number 'n', print all digits of a number using recursion.

```
#include <iostream>
using namespace std;
void printDigits (int n)
{
    // base case
    if (n == 0) {
        return;
    }
    int newValue = n / 10;
    printDigits(newValue);
    int digit = n % 10;
    cout << digit;
    cout << endl;
}
int main()
{
    int n = 647;
    printDigits(n);
    return 0;
}
```

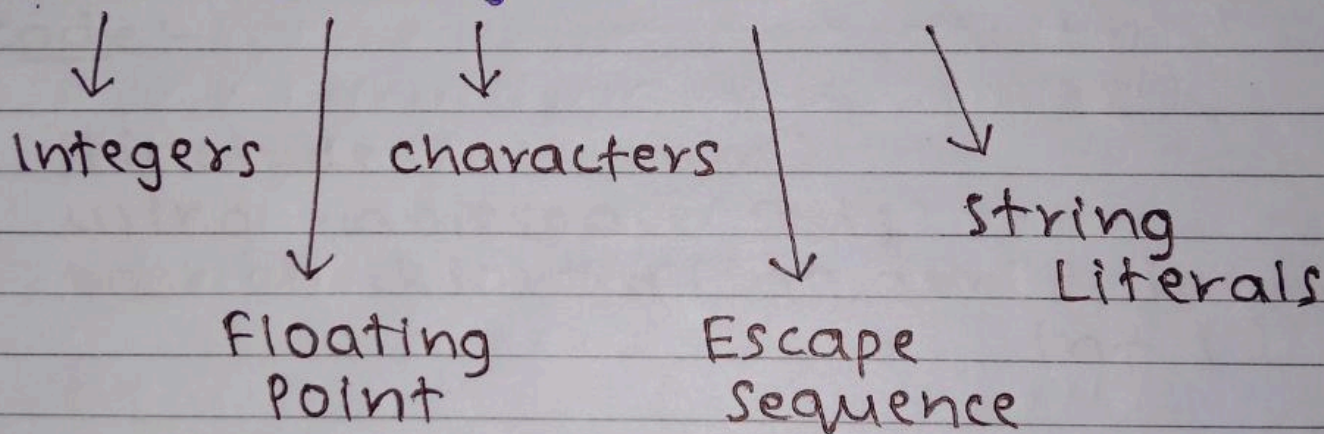

In previous question, if given value of n is 0647. Then the digits printing are 4 2 3.

↓ why?

Because, the first digit cannot be zero.

Integer literals begins with the digit 0 are interpreted as an octal integer literal rather than as a decimal integer literal.

There are many literals in C++ :-



- ① Integer Literal = An integer is a numeric literal (associate with numbers) without any fractional or exponential part. There are 3 types of integer literals in C++ :-
- i) decimal (base 10)
 - ii) octal (base 8)
 - iii) hexadecimal (base 16)

For example:-

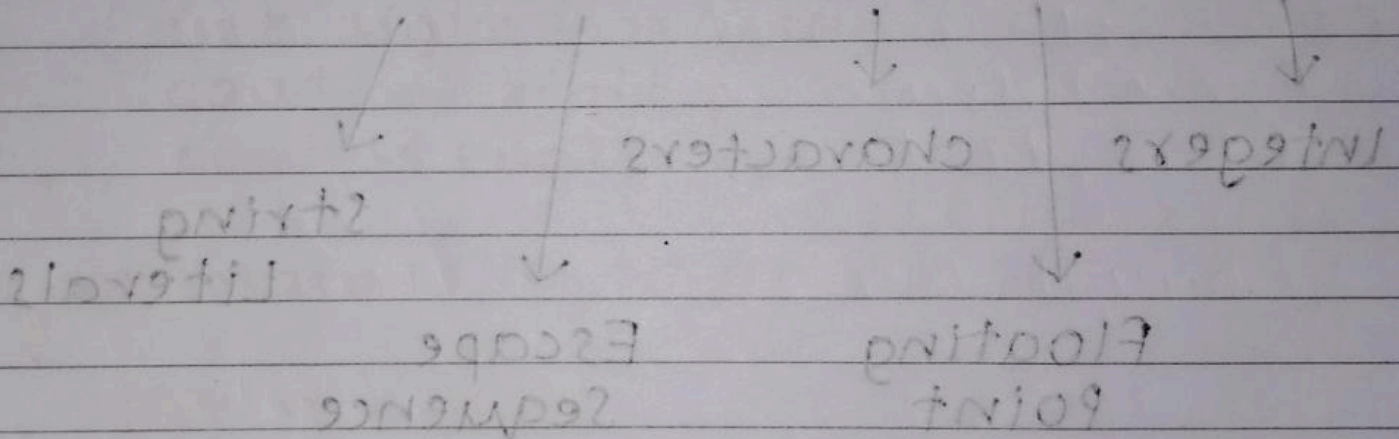
decimal: 0, -9, 22, etc.

octal: 021, 077, 033, etc.

hexadecimal: 0x7f, 0x2a, etc.

In C++, octal starts with 0.

Hexadecimal starts with 0x.



①

(i) decimal (base 10)

(ii) octal (base 8)

(iii) hexadecimal (base 16)