

# Weibull transition probabilities

## 0.1 Weibull hazard

To add a state-residence dependency to the simulation-time-dependent Sick-Sicker model defined above, we assume the risk of progression from S1 to S2 increases as a function of the time  $\tau = 1, \dots, n_{\text{tunnels}}$  the cohort remains in the S1 state. This increase follows a Weibull hazard function,  $h(\tau)$ , defined as

$$h(\tau) = \gamma\lambda(\lambda\tau)^{\gamma-1},$$

with a corresponding cumulative hazard,  $H(\tau)$ ,

$$H(t) = (\lambda\tau)^\gamma,$$

where  $\lambda$  and  $\gamma$  are the scale and shape parameters of the Weibull function, respectively.

## 0.2 Weibull transition probability

To derive a transition probability,  $\text{tp}(\tau)$ , as a function of time from  $H(\tau)$ , we use the following equation[Diaby2014]

$$p_{[S1_\tau, S2, \tau]} = 1 - \exp(H(\tau - 1) - H(\tau)) \quad (1)$$

Substituting the Weibull cumulative hazard in Equation (1), the transition probability from S1 to S2 as a function of the time the cohort spends in S1,  $p_{[S1_\tau, S2, \tau]}$ , is

$$p_{[S1_\tau, S2, \tau]} = 1 - \exp((\lambda(\tau - 1))^\gamma - (\lambda\tau)^\gamma)$$