# Exercise 4 - Backpropagation and unsupervised Learning

Winter term 2019/2020 name1, name2, name3



#### **Important**

Please solve the assignments in groups of 3 to 4 students. The solutions are going to be presented and discussed after the submission deadline. Sample solutions will not be uploaded. However, you are free to share correct solutions with your colleagues **after they have been graded**. Please submit your solutions via Moodle **and** in printed form. Only one member of the group has to submit the solutions. Therefore, make sure to specify the names of all group members. Please do not submit hand-written solutions, rather use proper type-setting software like LATEX or other comparable programs.

Your homework will be corrected and given back to you. Correct solutions are rewarded with a bonus for the exam (max. 10 percent, if all solutions submitted are correct). Please note: You have to pass the exam without the bonus points! (i.e. it is not possible to turn 5.0 into 4.0) The solutions have to be your own work. If you plagiarize, you will lose all bonus points!

#### Further remarks:

- Code assignments have to be done in Python
- The following packages are allowed: numpy, pandas (please ask, if you want to use a specific package not mentioned here)
- Do not use already implemented models (e.g. from scikit-learn)



### 1 Backpropagation

### a) Backpropagation by Hand (5 points)

You are given the neural network depicted below. Compute one forward-pass and one backward-pass based on the labeled training example  $\langle \boldsymbol{x} = [0.05, 0.10], \boldsymbol{y} = [0, 1] \rangle$ . Employ the squared error loss function:

$$\mathcal{J}(\mathbf{\Theta}) = (y_{pred} - y)^2$$

$$\mathcal{J}'(\mathbf{\Theta}) = 2 \cdot (y_{pred} - y)$$

The weight matrices and bias weights are initialized as follows (where for instance weight  $\Theta_{12}^{(1)}$  connects the input  $x_2$  with the first neuron in the hidden layer):

$$\Theta^{(1)} = \begin{pmatrix} 0.15 & 0.20 \\ 0.25 & 0.30 \end{pmatrix} \qquad \qquad \Theta^{(2)} = \begin{pmatrix} 0.40 & 0.45 \\ 0.50 & 0.55 \end{pmatrix} 
\mathbf{b}^{(1)} = \begin{pmatrix} 0.35 & 0.35 \end{pmatrix} \qquad \qquad \mathbf{b}^{(2)} = \begin{pmatrix} 0.60 & 0.60 \end{pmatrix}$$

Use the ReLU and sigmoid activation functions in the hidden layer and output layer, respectively. Write down all necessary computations. What are the gradients for the weights  $\Theta_{12}^{(1)}$ ,  $\Theta_{21}^{(2)}$ ?

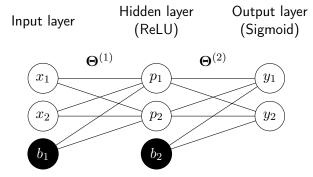


Figure 1: MLP architecture

Solution:



## 2 Unsupervised Learning

a) k-Means clustering (4 points)

Implement k-Means clustering for image compression. Compress the exemplary image file which can be found under the path  $\lceil \frac{data}{dhbw} \rceil$ . You can find an explanation of how image compression with k-Means works on this web page. 1

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b) PCA (1 point)

Explain how to choose the number of principal components for dimensionality reduction. Why does this work?

Solution:

 $<sup>^{1}</sup> https://medium.com/@agarwalvibhor84/image-compression-using-k-means-clustering-8c0ec055103f$ 



c) Bonus Question: Spectral clustering (1 point)

How can you automatically choose the number of clusters for spectral clustering?

Solution: