Relation between Gross Domestic Product (GDP) per capita and life satisfaction of different countries

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1 Introduction

Happiness is probably the most important thing that many people aim to achieve in life but what are the factors that contribute to it is not immediately known. In fact, happiness very likely depends on several factors that contribute to it and some of these factors are more important than the others. Obviously happiness is very subjective and there are many ways to quantify it and one of the most important quantifiers of happiness is the perceived life satisfaction of a group of people. In this article I want to study what is the relation between the Gross Domestic Product (GPD) and the life satisfaction of a given country.

2 Data file loading and overview

To study the relation between GPD and life satisfaction, first is needed to have the tabular data of the GPD and life satisfaction of different countries and second it is necessary to prepare the data for the analysis. The tabular data of the GPD and life satisfaction can be easily found on internet respectively in the (IMF website, GPD per capita in US dollars) and (OECD website, Better Life Index). Both these tabular data files are provided with the Python code for analysis. Before starting the analysis, it is very important to have a look at the data present in the files in the tabular form by using for example Google Sheets. In Fig. 1, a section of the Better Life Index aggregate data on Google Sheet is shown. The file contains different information regarding Better Life Index but I am mostly interested in some of these data. I am interest in the column A that gives the country name, column D that gives the indicator of better life which in our case is (Life satisfaction), column G that gives inequality measurement and column O that gives the numeric value of each better life index present in column D.

In Fig. 2, a section of the Better Life Index is shown where in the column D we have the desired category of index, namely that of Life satisfaction index. The first data appears in the row nr. 1815 with Australia being the first country. If we roll down little with the file, we can see that there are data of the Life satisfaction for men, women and total (women+men). Here I work only with the total data which have a corresponding average score (columns I and J). These data extend from row nr. 1815 to 1853 and will be the data that I will use in what follows. The Life satisfaction data are displayed in the score scale from 0 to 10 where the value of 10 means extremely satisfied while the score value of 0 means extremely unsatisfied.

1	 fx 	LOCATION															
	A	В	С	D	E	F	G	Н	1	J	К	L	M	N	0	P	
1	LOCATION	Country	INDICATOR	Indicator	MEASURE	Measure	INEQUALITY	Inequality	Unit Code	Unit	PowerCode Cod	PowerCode	Reference Period	Reference Period	Value	Flag Codes	Flags
2	AUS	Australia	JE_LMIS	Labour market	n L	Value	TOT	Total	PC	Percentage	0	Units			5.4		
3	AUT	Austria	JE_LMIS	Labour market	n L	Value	TOT	Total	PC	Percentage	0	Units			3.5		
4	BEL		JE_LMIS	Labour market i	n L	Value	TOT	Total	PC	Percentage		Units			3.7		
5	CAN	Canada	JE_LMIS	Labour market i	n L	Value	TOT	Total	PC	Percentage	0	Units				6	
3	CZE	Czech Republic	JE_LMIS	Labour market i	n L	Value	TOT	Total	PC	Percentage	0	Units			3.1		
7	DNK	Denmark	JE_LMIS	Labour market i	n L	Value	TOT	Total	PC	Percentage	0	Units			4.2		
В	FIN	Finland	JE_LMIS	Labour market	n L	Value	TOT	Total	PC	Percentage	0	Units			3.9		
9	FRA	France	JE_LMIS	Labour market i	n L	Value	TOT	Total	PC	Percentage	0	Units			7.6		
0	DEU	Germany	JE_LMIS	Labour market i	n L	Value	TOT	Total	PC	Percentage	0	Units			2.7		
11	GRC	Greece	JE_LMIS	Labour market i	n L	Value	TOT	Total	PC	Percentage	0	Units			29.8		
12	HUN	Hungary	JE_LMIS	Labour market i	n L	Value	TOT	Total	PC	Percentage	0	Units			4.7		
13	ISL	Iceland	JE_LMIS	Labour market i	n L	Value	TOT	Total	PC	Percentage	0	Units			0.7		
14	IRL	Ireland	JE_LMIS	Labour market i	n L	Value	тот	Total	PC	Percentage	0	Units			7.8		
15	ITA	Italy	JE_LMIS	Labour market i	n L	Value	TOT	Total	PC	Percentage	0	Units			12.3		
16	JPN	Japan	JE_LMIS	Labour market i	n L	Value	TOT	Total	PC	Percentage	0	Units			1.4		
17	KOR	Korea	JE_LMIS	Labour market i	n L	Value	TOT	Total	PC	Percentage	0	Units			2.6		
8	LUX	Luxembourg	JE_LMIS	Labour market i	n L	Value	TOT	Total	PC	Percentage	0	Units			1.7		
19	MEX	Mexico	JE_LMIS	Labour market i	n L	Value	TOT	Total	PC	Percentage	0	Units			5.5		
20	NLD	Netherlands	JE_LMIS	Labour market i	n L	Value	TOT	Total	PC	Percentage	0	Units			4.8		
21	NZL	New Zealand	JE_LMIS	Labour market i	n L	Value	TOT	Total	PC	Percentage	0	Units			4.7		
22	POL	Poland	JE_LMIS	Labour market i	n L	Value	TOT	Total	PC	Percentage	0	Units			5.7		
23	PRT	Portugal	JE_LMIS	Labour market i	n L	Value	TOT	Total	PC	Percentage	0	Units			1	0	
24	SVK	Slovak Republic	JE_LMIS	Labour market	n L	Value	TOT	Total	PC	Percentage	0	Units			9.9		
25	ESP	Spain	JE LMIS	Labour market i	n L	Value	TOT	Total	PC	Percentage	0	Units			23.1		
6	SWE	Sweden	JE LMIS	Labour market i	n L	Value	TOT	Total	PC	Percentage	0	Units			3.2		
7	TUR	Turkey	JE_LMIS	Labour market i	n L	Value	TOT	Total	PC	Percentage	0	Units			12.5		
8	GBR	United Kingdom	JE_LMIS	Labour market i	n L	Value	TOT	Total	PC	Percentage	0	Units			4.5		
9	USA	-	JE LMIS	Labour market i	n L	Value	тот	Total	PC	Percentage	0	Units			7.7		
30	CHL		JE LMIS	Labour market i	n L	Value	тот	Total	PC	Percentage	0	Units			8.7		
31	EST	Estonia	JE LMIS	Labour market i		Value	TOT	Total	PC	Percentage		Units			3.8		

Figure 1: Appearance of the first 31 rows of OECD Better Life Index aggregate data on Google Sheets. Here I am interested in the column A data (Country), column D data (Indicator), column G data (INEQUALITY) and column O data (Value).

- ,	LOCATION															
A	В	С	D	Е	F	G	Н	I	J	K	L	M	N	0	Р	
12 LVA	Latvia	HS_SFRH	Self-reported hea	εL	Value	LW	Low	PC	Percentage	0	Units			28		
13 SVN	Slovenia	HS_SFRH	Self-reported hea	εL	Value	LW	Low	PC	Percentage	0	Units			53		
OECD	OECD - Total	HS_SFRH	Self-reported hea	٤L	Value	LW	Low	PC	Percentage	0	Units			61		
AUS	Australia	SW_LIFS	Life satisfaction	L	Value	TOT	Total	AVSCORE	Average score	0	Units			7.3		
16 AUT	Austria	SW_LIFS	Life satisfaction	L	Value	TOT	Total	AVSCORE	Average score	0	Units			7.1		
BIT BEL	Belgium	SW_LIFS	Life satisfaction	L	Value	TOT	Total	AVSCORE	Average score	0	Units			6.9		
18 CAN	Canada	SW_LIFS	Life satisfaction	L	Value	TOT	Total	AVSCORE	Average score	0	Units			7.4		
19 CZE	Czech Republic	SW_LIFS	Life satisfaction	L	Value	TOT	Total	AVSCORE	Average score	0	Units			6.7		
20 DNK	Denmark	SW_LIFS	Life satisfaction	L	Value	тот	Total	AVSCORE	Average score	0	Units			7.6		
321 FIN	Finland	SW_LIFS	Life satisfaction	L	Value	TOT	Total	AVSCORE	Average score	0	Units			7.6		
322 FRA	France	SW_LIFS	Life satisfaction	L	Value	TOT	Total	AVSCORE	Average score	0	Units			6.5		
323 DEU	Germany	SW_LIFS	Life satisfaction	L	Value	TOT	Total	AVSCORE	Average score	0	Units			7		
324 GRC	Greece	SW_LIFS	Life satisfaction	L	Value	TOT	Total	AVSCORE	Average score	0	Units			5.4		
HUN	Hungary	SW_LIFS	Life satisfaction	L	Value	TOT	Total	AVSCORE	Average score	0	Units			5.6		
326 ISL	Iceland	SW_LIFS	Life satisfaction	L	Value	TOT	Total	AVSCORE	Average score	0	Units			7.5		
327 IRL	Ireland	SW_LIFS	Life satisfaction	L	Value	TOT	Total	AVSCORE	Average score	0	Units			7		
328 ITA	Italy	SW_LIFS	Life satisfaction	L	Value	TOT	Total	AVSCORE	Average score	0	Units			6		
329 JPN	Japan	SW_LIFS	Life satisfaction	L	Value	TOT	Total	AVSCORE	Average score	0	Units			5.9		
330 KOR	Korea	SW_LIFS	Life satisfaction	L	Value	TOT	Total	AVSCORE	Average score	0	Units			5.9		
31 LUX	Luxembourg	SW_LIFS	Life satisfaction	L	Value	TOT	Total	AVSCORE	Average score	0	Units			6.9		
32 MEX	Mexico	SW_LIFS	Life satisfaction	L	Value	TOT	Total	AVSCORE	Average score	0	Units			6.5		
333 NLD	Netherlands	SW_LIFS	Life satisfaction	L	Value	TOT	Total	AVSCORE	Average score	0	Units			7.4		
NZL	New Zealand	SW_LIFS	Life satisfaction	L	Value	TOT	Total	AVSCORE	Average score	0	Units			7.3		
NOR	Norway	SW_LIFS	Life satisfaction	L	Value	TOT	Total	AVSCORE	Average score	0	Units			7.6		
POL	Poland	SW_LIFS	Life satisfaction	L	Value	TOT	Total	AVSCORE	Average score	0	Units			6.1		
PRT PRT	Portugal	SW_LIFS	Life satisfaction	L	Value	TOT	Total	AVSCORE	Average score	0	Units			5.4		
SVK	Slovak Republic	SW_LIFS	Life satisfaction	L	Value	TOT	Total	AVSCORE	Average score	0	Units			6.2		
SSP ESP	Spain	SW_LIFS	Life satisfaction	L	Value	TOT	Total	AVSCORE	Average score	0	Units			6.3		
SWE	Sweden	SW_LIFS	Life satisfaction	L	Value	тот	Total	AVSCORE	Average score	0	Units			7.3		
CHE	Switzerland	SW_LIFS	Life satisfaction	L	Value	тот	Total	AVSCORE	Average score	0	Units			7.5		
342 TUR	Turkey	SW_LIFS	Life satisfaction	L	Value	тот	Total	AVSCORE	Average score	0	Units			5.5		
GBR	United Kingdom	SW_LIFS	Life satisfaction	L	Value	тот	Total	AVSCORE	Average score	0	Units			6.8		
344 USA	United States	SW LIFS	Life satisfaction	L	Value	TOT	Total	AVSCORE	Average score	0	Units			6.9		

Figure 2: Google sheet section containing the (Life satisfaction) indicator in column D of the Better Life Index aggregate data file.

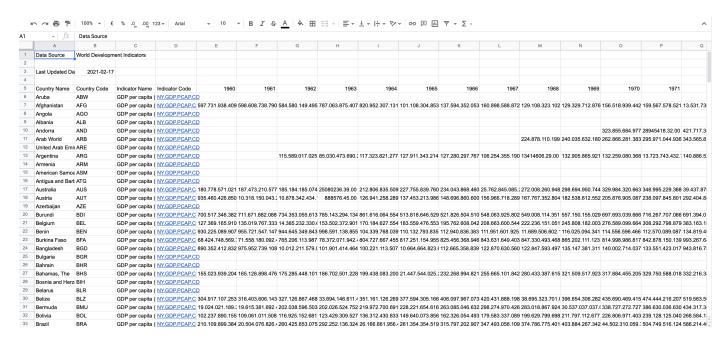


Figure 3: Google sheet section containing the GDP per capita in (US dollars) for different countries and years.

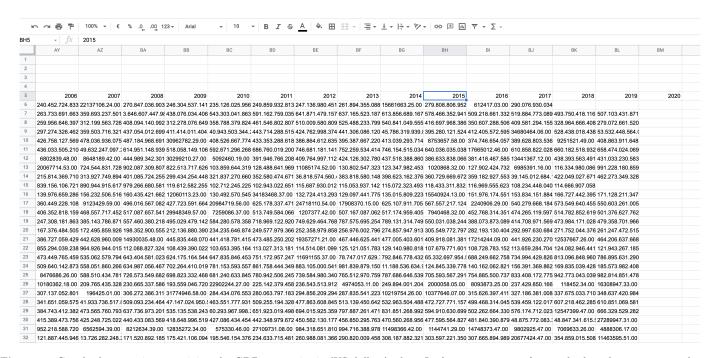


Figure 4: Google sheet section containing the GDP per capita in (US dollars) where I select as a matter of example the column corresponding to the year 2015 for my analysis.

In Fig. 3 a section of the data file containing the information of the GPD per capita is (US dollars) for different countries and years in Google sheets is shown. We can see that the data appear quite messy and they overlap with each other. The data sheet contains different data and I will be interested only in some of them. The heading of the GPD per capita file starts at the row nr. 1 in Fig. 3 "Data Source" and "World Development Indicators" appear. In what follows, I will be interested in the data with heading in row nr. 5 which among them are the "Country Name", "Indicator Name" and years (in numerical values). In Fig. 4 a section of the GPD per capita file corresponding to the years from 2006 to 2019 is shown for different countries. As a matter of example, in my analysis I choose¹ the year 2015 which is the selected column in blue in Fig. 4.

3 Data wrangling

In sec. 2, I showed some sections of the Better Life Index and GPD per capita files as they appear when visualized with Google Sheets. In this section, I show how to clean and prepare the data for the analysis by using Python 3. It is important to set since know the goal of my analysis and the way to reach that goal. The goal of my analysis is that to collect and tabulate the data of the life satisfaction index and GDP per capita for each country name and find the relationship (if there is one) between the data.

I start first by importing the libraries and/or modules that I use in my python analysis by using the "Jupyter Notebook":

- import numpy as np
- import pandas as pd
- *import* scipy *as* sp
- \bullet import sklearn.neighbors

Here I have imported the NumPy, Matplotlib, Pandas, Scipy and Sklearn modules/libraries and have used the standard abbreviations to call them. As I discussed in sec. 2 both data files contain many data categories that are not needed for this analysis and I select only those data that are necessary to reach my goal. I start first by loading the files in Jupyter Notebook by using Pandas library

- $\bullet \ \mathrm{GDP} = \mathrm{pd.read_csv}(\mathrm{``gdp\ per\ capita.csv''},\ \mathrm{delimiter} = \mathrm{``,''},\ \mathrm{header} = 2)$
- LS=pd.read_csv("better life index.csv")

The next step is that of data wrangling by using the Pandas library. In the GDP per capita file I set the "Country name" as the index in the Pandas dataframe and the value column being the "GDP per capita 2015 (USD)". Here I use Pandas to rename some columns and set as dataframe index the column that I am interested in of the original tabular data. Details of these operation are presented in the accompanying Jupyter Notebook file. I use similar data wrangling for the Better Life Index file where

¹One is free to choose another year for the analysis if wishes so.

I rename some columns and set the country column as index of the Pandas dataframe and column value being the "Life Satisfaction Value". In Fig. 5 sections of the Pandas dataframes are shown. On the left a section of the "GDP per capita 2015 (USD)" dataframe is shown and on the right only the first ten entries of the "Life Satisfaction Value" dataframe is shown. After data wrangling the "GDP per capita 2015 (USD)" dataframe has 264 country entry values of the GPD per capita as can be seen from the left dataframe in Fig. 5 while the "Life Satisfaction Value" dataframe has in total 40 country value entries of the life satisfaction values.

	GPD per capita 2015 (USD)
Country Name	
Aruba	27980.880695
Afghanistan	578.466353
Angola	4166.979684
Albania	3952.801215
Andorra	35762.523074
Kosovo	3603.025501
Yemen, Rep.	1602.037841
South Africa	5734.633629
Zambia	1337.795586
Zimbabwe	1445.071062
264 rows × 1 c	columns

Figure 5: Pandas sections containing the "GDP per capita 2015 (USD)" and "Life Satisfaction Value" for different countries is shown.

The next step of the analysis is to make a final Pandas joint dataframe where are selected only those countries that have available values of both "GDP per capita 2015 (USD)" and "Life Satisfaction Value". This can be done by using the Pandas join function as shown in details in the accompanying Jupyter Notebook file. At the end we obtain the final Pandas joint data frame as shown in Fig. 6 where only a section of the whole dataframe is shown. The whole joint Pandas dataframe has 38 country entries for the "GDP per capita 2015 (USD)" and "Life Satisfaction Value" values where the country names do not necessarily appear in alphabetic order.

4 Data analysis and statistical/machine learning methods

After collecting the data in one dataframe as shown in Fig. 6, the first step to proceed with the analysis is to make a scatter plot and see if there is relation between the data. A scatter plot of the data present in the dataframe of Fig. 6 is shown in Fig. 7 where the feature data (X), namely "GDP per capita 2015 (USD)" is plotted versus the output data (Y = f(X)), namely "Life Satisfaction value".

4.1 Simple linear regression method (supervised learning)

By looking at the scatter plot in Fig. 7 it seems that the data might follow a linear relationship between them. Indeed, by using the correlation function of the Pandas dataframe, "pd.corr(...)", a Pearson corre-

	Life Satisfaction Value	GPD per capita 2015 (USD)
Country Name		
Australia	7.3	56755.721712
Austria	7.1	44178.047378
Belgium	6.9	40991.808138
Canada	7.4	43585.511982
Czech Republic	6.7	17829.69832
Denmark	7.6	53254.856370
Finland	7.6	42784.69836
France	6.5	36638.184929
Germany	7.0	41086.72967
Greece	5.4	18167.77372
Hungary	5.6	12706.89121
Iceland	7.5	52564.429179
Ireland	7.0	61995.42280
Italy	6.0	30230.22630
Japan	5.9	34524.46986
Luxembourg	6.9	101376.49657
Mexico	6.5	9616.64500
Netherlands	7.4	45175.231893
New Zealand	7.3	38615.99518
Norway	7.6	74355.515858

Figure 6: Pandas section of the joint "GDP per capita 2015 (USD)" and "Life Satisfaction Value" dataframes for different countries is shown.

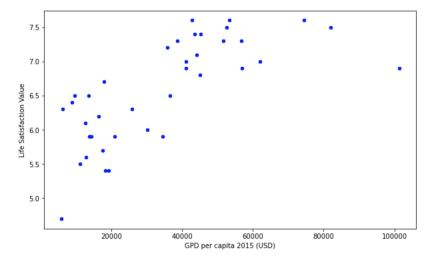


Figure 7: Scatter plot of the "Life Satisfaction Value" vs. "GDP per capita 2015 (USD)" for 38 different countries of the dataframe in Fig. 6 is shown.

lation coefficient of the value $r \simeq 0.72$ is found. Clearly such a value of r indicates that the data might be modelled by a linear relationship of the type $Y = \beta_0 + \beta_1 X$ where β_0 is the intercept value and β_1 is the slope value of the linear equation.

In order to find a possible linear relationship, I make use of the "stats" module of the "SciPy" library² and use the linear regression built in method:

- result = sp.stats.linregress(X, Y)
- print(result)LinregressResult(slope=2.399629982572962e-05, intercept=5.741754353755319, rvalue=0.7202871953226535, pvalue=3.426556470065171e-07, stderr=3.851624914535906e-06, intercept_stderr=0.15853194959552191)

The linear regression method used gives the values of the intercept $\hat{\beta}_0 \simeq 5.74$ and slope $\hat{\beta}_1 \simeq 2.39 \times 10^{-5}$ with their respective standard errors $s_{\hat{\beta}_0} \simeq 0.15$ and $s_{\hat{\beta}_1} \simeq 3.35 \times 10^{-6}$. The equation for the linear relationship between the data is thus given by the equation line

$$Y(X) \simeq 5.74 + 2.39 \times 10^{-5} X.$$
 (1)

In addition to the equation line (1) it is also very useful to have the confidence intervals (CIs) for the regression coefficients $\beta_{0,1}$ which are give by

$$\beta_{0,1} \in [\hat{\beta}_{0,1} - s_{\hat{\beta}_{0,1}} t_{1-\alpha/2,n-2}, \hat{\beta}_{0,1} + s_{\hat{\beta}_{0,1}} t_{1-\alpha/2,n-2}],$$

where $t_{1-\alpha/2,n-2}$ is the $1-\alpha/2$ pecentile (or t-score) of the random T variable that enters the Student-T distribution function with n-2 degrees of freedom and α is the level of significance. If we ask a test statistic for the T variable at the level of significance of $\alpha = 0.05$ or confidence level (CL) of 95%, we get for n-2=36 a t-score of $t_{0.975} \simeq 2.028$. Thus at the 95% CL, we get the following CIs for the intercept β_0 and slope β_1 of the OLS linear regression method

$$\beta_0 \in [5.43, 6.04], \qquad \beta_1 \in [1.71 \times 10^{-5}, 3.06 \times 10^{-5}].$$

Other two important parameters derived from the linear regression method are the Pearson correlation coefficient, $r \simeq 0.72$, that fits the data relatively well and the P-value of the parameter β_1 under the null Hypothesis, $H_0: \beta_1 = 0$. The null Hypothesis is accepted if $P(\beta_1) \geq 1 - \alpha$ otherwise it is rejected. Since, $P(\beta_1) \simeq 3.42 \times 10^{-7} \ll 1 - \alpha = 0.95$, we thus reject the null hypothesis and consequently there is a relation between the data, a fact that is also confirmed from the value of $r \simeq 0.72$. In Fig. 8 the OLS fit line equation (1) and the original data of Fig. 7 are shown.

With the help of the linear relationship in (1) we can make predictions and inference. For example, in the year 2015 it is not known the life satisfaction value of Albania where the country had a GDP per capita of 3952.8 (USD), see the left dataframe in Fig. 5. By using equation (1) and the GDP per capita of Albania, $X_{\text{Albania}} = 3952.8$ (USD), one can easily find the life satisfaction of Albanians, $Y_{\text{Albania}} \simeq 5.83$. On the other hand, we can use equation (1) for inference purposes. For example, it is not known the GDP per capita in 2015 of the countries of Korea and Russia but are known the values of the life satisfaction. Korea in 2015 had a life satisfaction value of $Y_{\text{Russia}} = 5.8$. By using equation (1), one can find $X_{\text{Korea}} \simeq 6694.5$ (USD) and $X_{\text{Russia}} \simeq 2510.4$ (USD).

²In alternative to the "stats" module one can also use the "sklearn.linear_model" module of the Scikit-learn library.

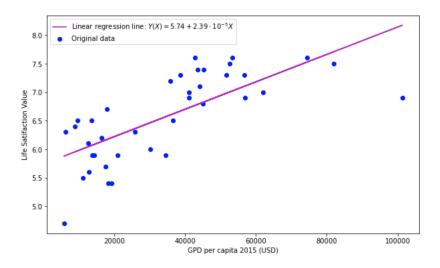


Figure 8: Scatter plot of the "Life Satisfaction Value" vs. "GDP per capita 2015 (USD)" for 38 different countries of the dataframe in Fig. 6 is shown.

4.2 KNN regression method (supervised learning)

In alternative to the simple linear regression method, one can also use the K-nearest neighbour (KNN) regression method. From the dataset of Fig. 6, we can see that many countries have close values of the "Life Satisfaction Value". For example, Australia, Canada, Denmark, Finland, Iceland, Netherland, New Zeland, Norway have respectively life satisfaction values of (7.3, 7.4, 7.6, 7.6, 7.5, 7.4, 7.3, 7.6) and the average value of life satisfaction of these countries is 7.4. The KNN regression method can be implemented in python as follows where the default value of regression neighbors is K = 5.

- $\bullet \ \ model = sklearn.neighbors.KNeighborsRegressor()$
- model.fit(X, y)
- $X_{\text{new}} = [[(\text{input new predictor numerical value})]]$
- $print(model.predict(X_{new}))$

Now I can make predictions for new life satisfaction values given new GDP per capita values. For example in our training method, the countries of Albania, United Arab Emirates (UAE) and Armenia were not included in our analysis. These countries had respectively a GDP per capita in the year 2015 (see the whole dataframe on the left in Fig. 5) in USD: $X_{\rm Albania} \simeq 3952.8$ (USD), $X_{\rm UAE} \simeq 38663.38$ (USD) and $X_{\rm Armenia} \simeq 3607.29$ (USD). The KNN regression model predicts the following life satisfaction values: $Y_{\rm Albania} = 5.88$, $Y_{\rm UAE} = 6.98$ and $Y_{\rm Armenia} = 5.88$.

5 Conclusions

In this article I studied the relationship between the GDP per capita of a given country and the perceived life satisfaction of that country. After analysing the data by using two different regression methods, one is able to predict and make inferences for new data not present in the training set. The simple linear regression method, gives a value of the linear correlation coefficient of $r \simeq 0.72$ and a generalized correlation coefficient of $R^2 = r^2 \simeq 0.51$, where R^2 is the generalized correlation coefficient. On the other hand, the KNN regression method gives a generalized correlation coefficient of $R^2 \simeq 0.69$. A comparison of R^2 between the two models, would suggest that the KNN regression model by having a higher value of R^2 would give better fit and predictions for the analyzed data.