```
1 import numpy as np
2 import time
3 np.random.seed(1234)
5 \text{ n, d} = 100000, 100
6 X = np.random.normal(size=(n,d))
7 beta_0 = np.random.normal(size=d)
9 def get_prob(X, beta):
10
       return 1.0 / (1.0 + np.exp(- np.matmul(X, beta)))
11
12 def gen label(X, beta):
13
       return np.random.binomial(1, get_prob(X, beta))
14
15 Y_gt = gen_label(X, beta_0)
17 def get_gradient(X, Y_gt, Y_pred, batch_size):
18
       grad_beta = np.dot(np.transpose(X), Y_gt - Y_pred)
19
       return grad_beta / batch_size
20
21 def get likelihood(X, Y gt, prob):
22
       res = 1.0
       for i in range(X.shape[0]):
23
24
           if Y_gt[i] == 1.0:
25
               res *= prob[i]
26
           else:
               res *= 1.0 - prob[i]
27
28
       return res
29
30 def lr_scheduler(lr_init, step, decay):
31
       warm_up_step = 100.0
32
       lr decay = 1e-6
33
       if step <= warm_up_step:</pre>
34
           return lr_init * step / warm_up_step
35
       if not decay:
36
           return lr init
37
       return np.power(1 - lr_decay, step - 100) * lr_init
38
39 def get_batch(X, Y_gt, start_ele, batch_size):
40
       if start ele + batch size >= n:
41
           X_batch = np.concatenate((X[start_ele: ], X[ :start_ele + batch_size - n]))
42
           Y_gt_batch = np.concatenate((Y_gt[start_ele: ], Y_gt[ :start_ele + batch_size - n]))
43
       else:
           X_batch = X[start_ele: (start_ele + batch_size)]
44
45
           Y_gt_batch = Y_gt[start_ele: (start_ele + batch_size)]
       return X_batch, Y_gt_batch
46
47
48 \# batch size = n
49 def gd(X, Y_gt, lr_init, d, beta_est):
50
       start = time.time()
51
       loss = []
52
       beta = np.zeros(shape=d)
53
       step = 1
       while True:
54
55
           Y_pred = get_prob(X, beta)
56
           grad_beta = get_gradient(X, Y_gt, Y_pred, X.shape[0])
57
           lr = lr_scheduler(lr_init, step, 1)
           beta += lr * grad_beta
58
59
           step += 1
60
           loss_this = np.sum(np.absolute(beta_est - beta))
61
           loss.append(loss_this)
62
           if loss_this < 1e-3 or step > 1e4:
               print("vanilla GD ended with L_1 diff as: ", np.sum(np.absolute(beta_est - beta)))
63
               print("Total time:", time.time() - start, "total steps:", step)
64
65
               break;
       return loss
66
67
68 def nag(X, Y_gt, lr_init, d, beta_est):
69
       start = time.time()
70
       loss = []
71
       beta = np.zeros(shape=d)
72
       step = 1
```

```
73
       beta_tmp = beta
74
      while True:
75
           y_beta = beta + ((step - 2.0) / (step + 1.0)) * (beta - beta_tmp)
76
           Y_pred = get_prob(X, y_beta)
77
           grad_beta = get_gradient(X, Y_gt, Y_pred, X.shape[0])
78
           lr = lr_scheduler(lr_init, step, 1)
           beta_tmp = beta
79
           beta = y_beta + lr * grad_beta
20
81
           step += 1
82
           loss_this = np.sum(np.absolute(beta_est - beta))
83
           loss.append(loss_this)
           if loss_this < 1e-3 or step > 1e4:
84
85
               print("NAG ended with L_1 diff as: ", np.sum(np.absolute(beta_est - beta)))
               print("Total time:", time.time() - start, "total steps:", step)
87
               break;
88
       return loss, beta
89
90 def adagrad(X, Y_gt, lr_init, d, eps, batch_size, beta_est):
91
       start = time.time()
92
       loss = []
93
       beta = np.zeros(shape=d)
94
       step = 1
95
       g_beta = np.zeros(shape=d)
96
       while True:
           start_ele = ((step - 1) * batch_size) % n
97
98
           X_batch, Y_gt_batch = get_batch(X, Y_gt, start_ele, batch_size)
99
           Y_pred = get_prob(X_batch, beta)
            grad_beta = get_gradient(X_batch, Y_gt_batch, Y_pred, batch_size)
100
101
            g_beta += np.square(grad_beta)
            lr = lr scheduler(lr init, step, 0)
102
103
            beta += lr * np.multiply((1.0 / np.sqrt(g_beta + eps)), grad_beta)
104
            step += 1
105
            loss.append(np.sum(np.absolute(beta est - beta)))
106
            if step > 1e5:
                print("AdaGrad ended with L_1 diff as: ", np.sum(np.absolute(beta_est - beta)))
107
                print("Total time:", time.time() - start)
108
109
                break;
110
        return loss
111
112 def rmsprop(X, Y_gt, lr_init, d, eps, batch_size,beta_est):
113
        start = time.time()
114
        loss = []
115
        beta = np.zeros(shape=d)
        step = 1
116
117
        g_beta = np.zeros(shape=d)
118
        while True:
            start_ele = ((step - 1) * batch_size) % n
119
120
            X_batch, Y_gt_batch = get_batch(X, Y_gt, start_ele, batch_size)
121
            Y_pred = get_prob(X_batch, beta)
            grad_beta = get_gradient(X_batch, Y_gt_batch, Y_pred, batch_size)
122
            g_beta = 0.9 * g_beta + 0.1 * np.square(grad_beta)
123
            lr = lr_scheduler(lr_init, step, 0)
124
            beta += lr * np.multiply((1.0 / np.sqrt(g_beta + eps)), grad_beta)
125
126
            step += 1
127
            loss.append(np.sum(np.absolute(beta_est - beta)))
128
            if step > 1e5:
129
                print("RMSprop ended with L_1 diff as: ", np.sum(np.absolute(beta_est - beta)))
130
                print("Total time:", time.time() - start)
131
                break:
        return loss
132
133
134 def sgd(X, Y_gt, lr_init, d, batch_size, beta_est):
        start = time.time()
135
136
        loss = []
137
        beta = np.zeros(shape=d)
138
        step = 1
139
        while True:
            start_ele = ((step - 1) * batch_size) % n
140
141
            X_batch, Y_gt_batch = get_batch(X, Y_gt, start_ele, batch_size)
142
            Y_pred = get_prob(X_batch, beta)
            grad_beta = get_gradient(X_batch, Y_gt_batch, Y_pred, batch_size)
143
            lr = lr_scheduler(lr_init, step, 1)
144
145
            beta += lr * grad_beta
146
            step += 1
```

```
147
            loss.append(np.sum(np.absolute(beta_est - beta)))
148
            if step > 1e5:
                print("SGD ended with L_1 diff as: ", np.sum(np.absolute(beta_est - beta)))
149
                print("Total time:", time.time() - start)
150
151
                break;
152
        return loss
153
154 def adam(X, Y_gt, lr_init, d, b_1, b_2, eps, batch_size, beta_est):
        start = time.time()
155
156
        loss = []
157
        beta = np.zeros(shape=d)
        step = 1
158
159
        m_beta = np.zeros(shape=d)
        v_beta = np.zeros(shape=d)
160
161
        while True:
            start_ele = ((step - 1) * batch_size) % n
162
            X_batch, Y_gt_batch = get_batch(X, Y_gt, start_ele, batch_size)
163
164
            Y_pred = get_prob(X_batch, beta)
            grad_beta = get_gradient(X_batch, Y_gt_batch, Y_pred, batch_size)
165
            lr = lr_scheduler(lr_init, step, 0)
166
            m_{beta} = b_1 * m_{beta} + (1 - b_1) * grad_beta
167
            v_beta = b_2 * v_beta + (1 - b_2) * np.square(grad_beta)
168
            beta += lr * (m_beta / (1.0 - np.power(b_1, step)))
169
170
                    / np.sqrt(eps + v_beta / (1.0 - np.power(b_2, step)))
171
            step += 1
            loss.append(np.sum(np.absolute(beta_est - beta)))
172
173
            if step > 1e5:
                print("Adam ended with L_1 diff as: ", np.sum(np.absolute(beta_est - beta)))
174
                print("Total time:", time.time() - start)
175
176
177
        return loss
178
```