RR intervals phase space reconstruction and recurrence plot

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1 R-R intervals time series

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Functions used in previous notebooks will be used. To exemplify, we will use the meditation recordings as well as one recording in rest and after performing exercise.

The objective of this notebook is to visualize the techniques used in previous notebooks (phase space recontruction and recurrence plot), but only using the R/R intervals time series. Consider that there must be an adequate R peak detection in the recording.

2 Setting up the notebook

We begin by setting up the Jupyter notebook and importing the Python modules needed for plotting figures, create animations, etc. We include commands to view plots in the Jupyter notebook, and to create figures with good resolution and large labels. These commands can be customized to produce figures with other specifications.

```
[1]: # Imports python libraries
     import numpy as np
     import random as rd
     import wave
     import sys
     import os
     import matplotlib.pyplot as plt
     from matplotlib.pyplot import figure
     import matplotlib as mpl
     from mpl_toolkits.axes_grid1.inset_locator import inset_axes
     sys.path.insert(1, r'./../functions') # add to pythonpath
     # commands to create high-resolution figures with large labels
     %config InlineBackend.figure_formats = {'png', 'retina'}
     plt.rcParams['figure.dpi'] = 50
     plt.rcParams['axes.labelsize'] = 16 # fontsize for figure labels
     plt.rcParams['axes.titlesize'] = 18 # fontsize for figure titles
```

```
plt.rcParams['font.size'] = 14 # fontsize for figure numbers
plt.rcParams['lines.linewidth'] = 1.4 # line width for plotting
```

2.1 Extracting data

ECG recordings were obtained using the Backyard Brains Heart and Brain Spiker Box. The recordings are saved as audio files in .wav format. The first thing we have to do is open the .wav files and extract the data. We can extract the number of recording channels, sampling rate, etc.

```
[2]: #Function that extracts the number of recording channels, sampling rate, time__
     \rightarrow and signal
     #variable is the path and filename of the .wav file
     def ecg(variable):
         record = wave.open(variable, 'r') # load the data
         # Get the number of channels, sample rate, etc.
         numChannels = record.getnchannels() #number of channels
         numFrames = record.getnframes() #number of frames
         sampleRate = record.getframerate() #sampling rate
         sampleWidth = record.getsampwidth()
         # Get wave data
         dstr = record.readframes(numFrames * numChannels)
         waveData = np.frombuffer(dstr, np.int16)
         # Get time window
         timeECG = np.linspace(0, len(waveData)/sampleRate, num=len(waveData))
         return timeECG, waveData
```

3 R peaks

Function for detecting R peaks. We will be able to calculate the heart frequency and R-R intervals.

The following function creates an array of values which surpass a certain threshold. Afterwards, it determines the maximum value of this array and adds it in the R-vector. And this is repeated until the end of the time series.

```
[3]: def detecta_maximos_locales(timeECG, waveData, threshold_ratio=0.7):

# If not all the R peaks are detected, lower the threshold_ratio

# If components that are not R peaks (like T waves) are detected, higher_

→ the threshold_ratio

if len(timeECG) != len(waveData): #Raises an error if the two arrays have_

→ different lengths

raise Exception("The two arrays have different lengths.")
```

```
interval = max(waveData) - min(waveData)
   threshold = threshold_ratio*interval + min(waveData)
   maxima = []
   maxima_indices = []
   mxs_indices = []
   banner = False
   for i in range(0, len(waveData)):
       if waveData[i] >= threshold:#If a threshold value is surpassed,
           # the indices and values are saved
           banner = True
           maxima_indices.append(i)
           maxima.append(waveData[i])
       elif banner == True and waveData[i] < threshold: \#If\ the\ threshold_{\sqcup}
\rightarrow value is crossed
           # the index of the maximum value in the original array is saved
           index_local_max = maxima.index(max(maxima))
           mxs_indices.append(maxima_indices[index_local_max])
           maxima = []
           maxima indices = []
           banner = False
   return mxs_indices
```

```
[4]: # If the input of this function is time, the intervals will be given in those
→ same units

# Obtaining the indexes at which the R peaks occur.

def R_intervals(time_indices):

length = len(time_indices)
intervals = np.zeros(length-1)

for i in range(0, length-1):
    intervals[i] = time_indices[i+1]-time_indices[i]

return intervals
```

4 Comencing the analysis

For analyzing several recordings at the same time, we must obtain the names of every file. One option is to extract the file names one by one, but another option is just to give a folder's name and extract the recordings from there.

```
[6]: corresponding_folder.append("S1_rest")
    corresponding_folder.append("S1_exercise")
    corresponding_folder.append("S2_rest")
    corresponding_folder.append("S2_exercise")
    corresponding_folder.append("S3_rest")
    corresponding_folder.append("S3_exercise")

recordings_path.append("ECG_samples/S1_rest.wav")
    recordings_path.append("ECG_samples/S1_exercise.wav")

recordings_path.append("ECG_samples/S2_rest.wav")
    recordings_path.append("ECG_samples/S2_rest.wav")

recordings_path.append("ECG_samples/S3_rest.wav")

recordings_path.append("ECG_samples/S3_rest.wav")

recordings_path.append("ECG_samples/S3_rest.wav")

recordings_path.append("ECG_samples/S3_exercise.wav")
```

```
[6]: ['ECG_samples/meditation_data/respiraciones_profundas_55_abdomen/BYB_Recording_2 018-06-07_18.40.01.wav',
    'ECG_samples/meditation_data/respiraciones_profundas_55_abdomen/BYB_Recording_2 018-06-07_18.43.56.wav',
    'ECG_samples/meditation_data/respiraciones_profundas_55_abdomen/BYB_Recording_2 018-06-07_18.38.19.wav',
    'ECG_samples/meditation_data/control/BYB_Recording_2018-06-07_18.07.34.wav',
    'ECG_samples/meditation_data/control/BYB_Recording_2018-06-07_18.09.49.wav',
```

```
'ECG samples/meditation data/control/BYB Recording 2018-06-07 18.05.04.wav',
 'ECG samples/meditation_data/respiraciones_profundas_55_pecho/BYB_Recording_201
8-06-07_18.20.29.wav',
 'ECG samples/meditation_data/respiraciones_profundas_55_pecho/BYB_Recording_201
8-06-07_18.22.37.wav',
 'ECG_samples/meditation_data/respiraciones_profundas_55_pecho/BYB_Recording_201
8-06-07 18.17.12.wav',
 'ECG_samples/meditation_data/sostener_respiracion_abdomen/BYB_Recording_2018-06
-07 18.31.55.wav',
 'ECG_samples/meditation_data/sostener_respiracion_abdomen/BYB_Recording_2018-06
-07 18.34.18.wav',
 'ECG_samples/meditation_data/sostener_respiracion_abdomen/BYB_Recording_2018-06
-07 18.35.39.wav',
 'ECG samples/meditation_data/sostener_respiracion_pecho/BYB_Recording_2018-06-0
7 18.26.47.wav',
 'ECG_samples/meditation_data/sostener_respiracion_pecho/BYB_Recording_2018-06-0
7_18.28.02.wav',
 'ECG samples/meditation_data/sostener_respiracion_pecho/BYB_Recording_2018-06-0
7_18.29.22.wav',
 'ECG samples/meditation_data/respiracion_ola/BYB_Recording_2018-06-07_18.47.21.
 'ECG_samples/meditation_data/respiracion_ola/BYB_Recording_2018-06-07_18.54.36.
 'ECG samples/meditation data/respiracion ola/BYB Recording 2018-06-07 18.53.00.
wav',
 'ECG_samples/S1_rest.wav',
 'ECG_samples/S1_exercise.wav',
 'ECG_samples/S2_rest.wav',
 'ECG_samples/S2_exercise.wav',
 'ECG_samples/S3_rest.wav',
 'ECG_samples/S3_exercise.wav']
```

Now we introduce the object used in previous notebooks. This will make it easier handling several recordings at once.

```
[7]: # Object
class Sujeto:
    def __init__(self, timeECG, waveData):
        self.timeECG = timeECG
        self.waveData = waveData

        self.mxs_indices = detecta_maximos_locales(timeECG, waveData)
        self.RR = R_intervals(timeECG[self.mxs_indices])
        self.timeRpeaks = timeECG[self.mxs_indices]
```

```
[8]: recordings = []
```

```
for i in range(0, len(recordings_path)):
    timeECG, waveData = ecg(recordings_path[i])
    recordings.append(Sujeto(timeECG, waveData))
    print("Finished recording ", i+1)
```

```
Finished recording 1
Finished recording
Finished recording 3
Finished recording
Finished recording 5
Finished recording 6
Finished recording 7
Finished recording 8
Finished recording 9
Finished recording 10
Finished recording 11
Finished recording 12
Finished recording 13
Finished recording 14
Finished recording 15
Finished recording 16
Finished recording
                  17
Finished recording
Finished recording
                  19
Finished recording 20
Finished recording 21
Finished recording 22
Finished recording 23
Finished recording 24
```

5 Phase space reconstruction

In the previous technique we only compared the R intervals with the next interval. What would happen if we compare not the R interval, but the whole recording with a certain time delay we choose. Instead of comparing one data point with its next in time, we choose an arbitrary time delay? In other words, we are going to generalize what we applied in the previous technique with the whole ECG data series and with an arbitrary time delay.

```
[9]: #Generating a function that will reconstruct the phase space for a certain time

delay

# data_series is the voltage of our signal

# period is the time delay

# identifier is a string that will help us identify that particular graph

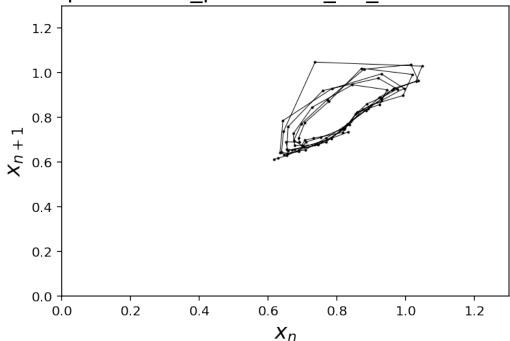
def graph_phase_space(waveData, period = 210, identifier = "xx"):

time = period*0.1 #time is in miliseconds

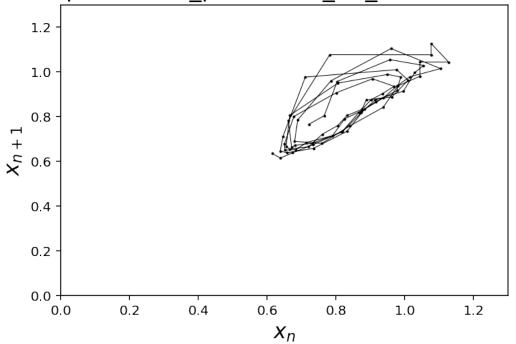
n = np.size(waveData) #size of the voltage vector
```

```
[10]: for i in range(len(recordings)):
    graph_phase_space(recordings[i].RR, 1, corresponding_folder[i])
```

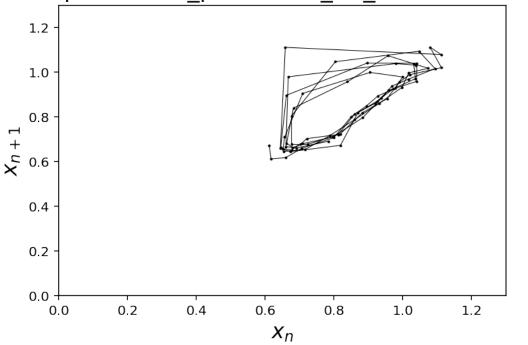
respiraciones_profundas_55_abdomen R-R

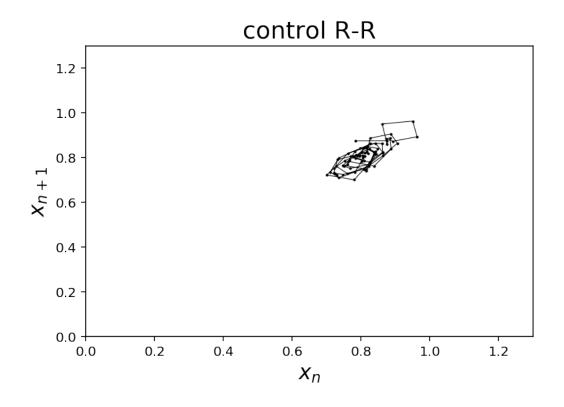


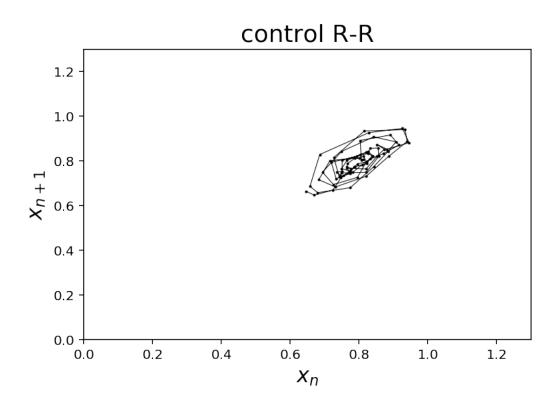
respiraciones_profundas_55_abdomen R-R

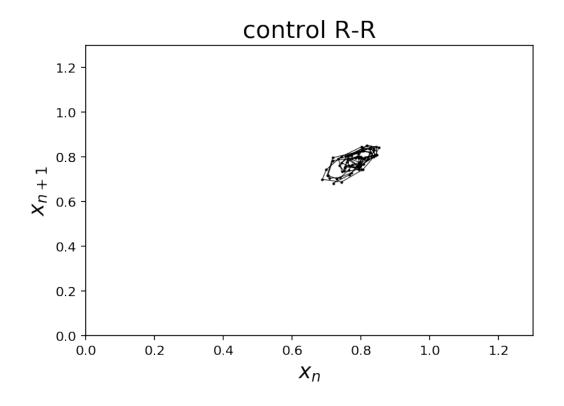


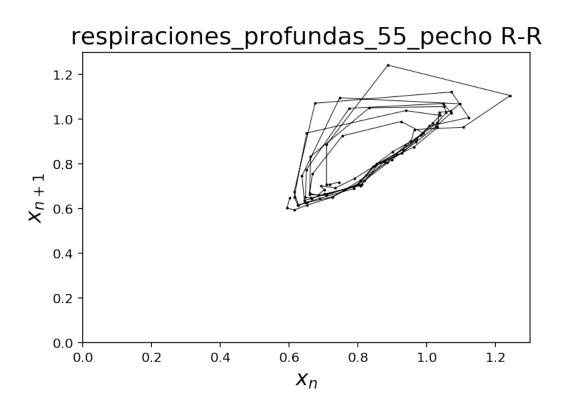
respiraciones_profundas_55_abdomen R-R

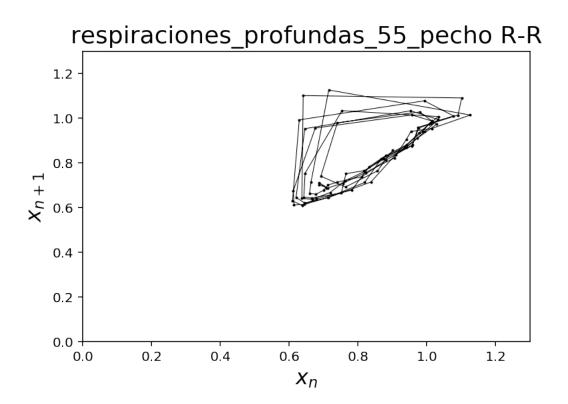


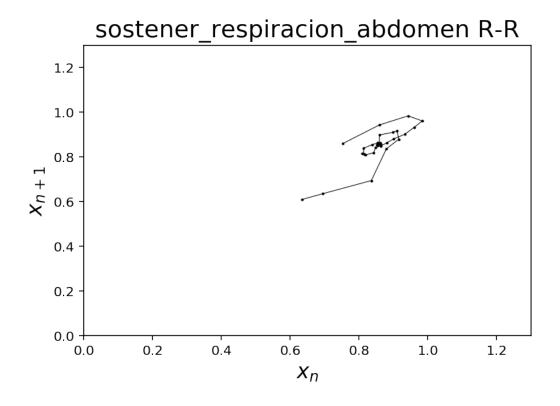


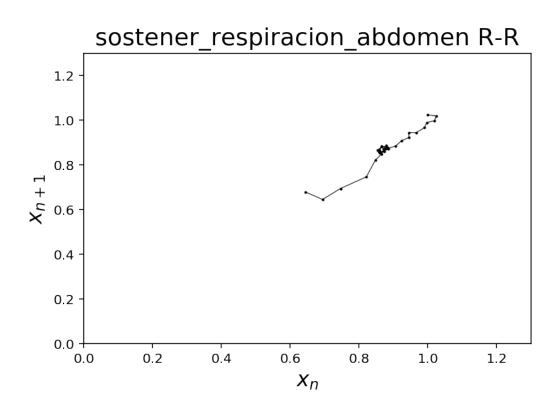


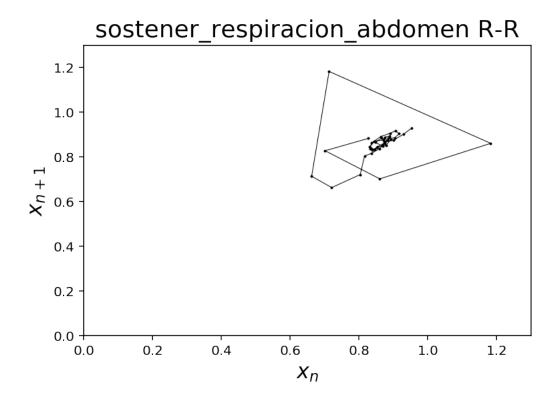


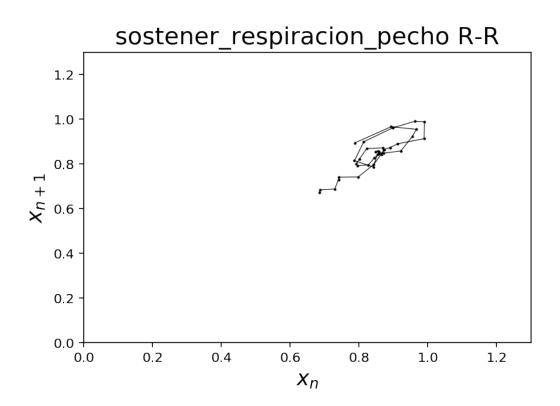


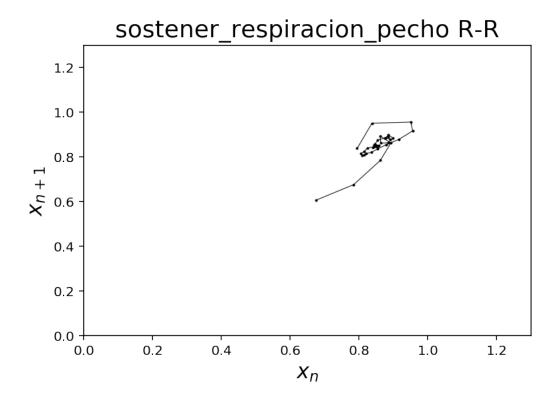


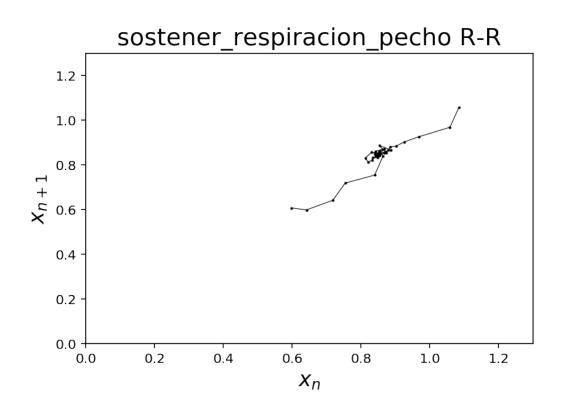


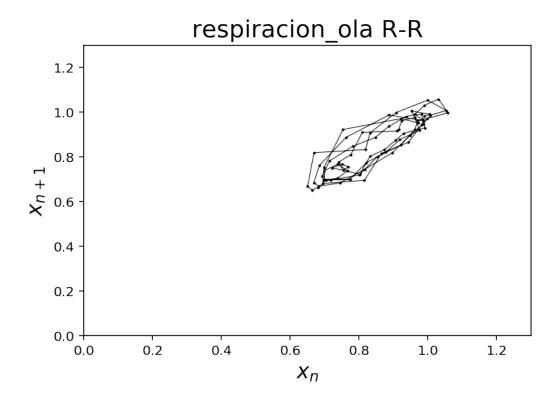


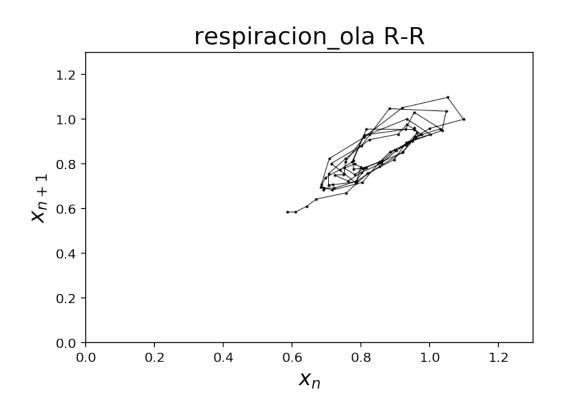


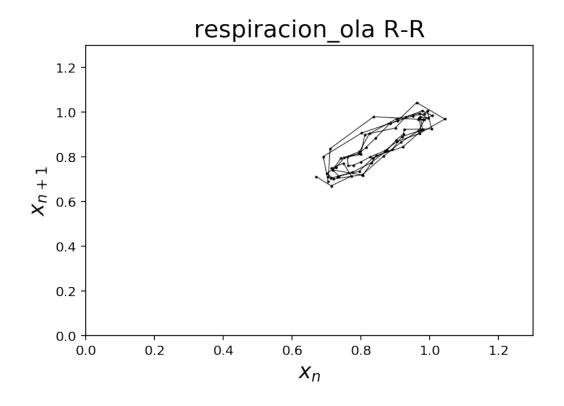


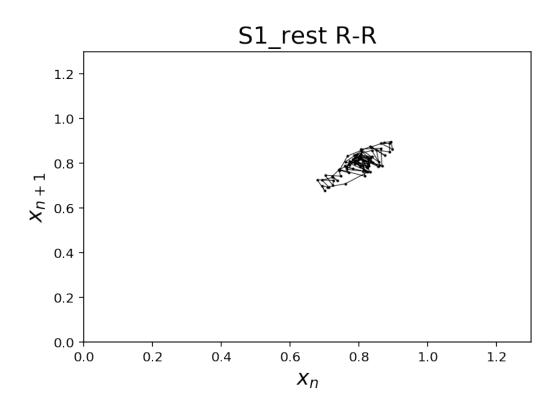


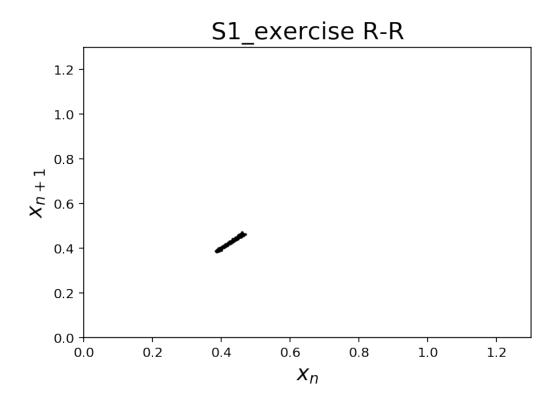


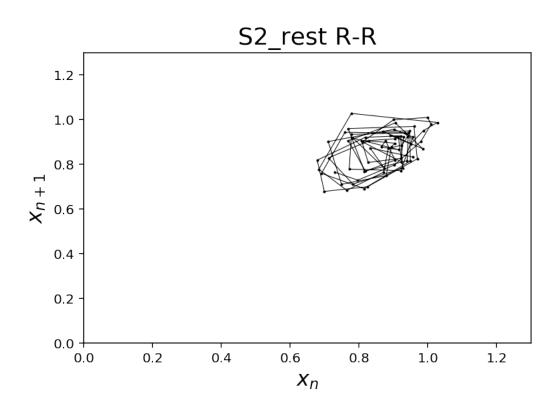


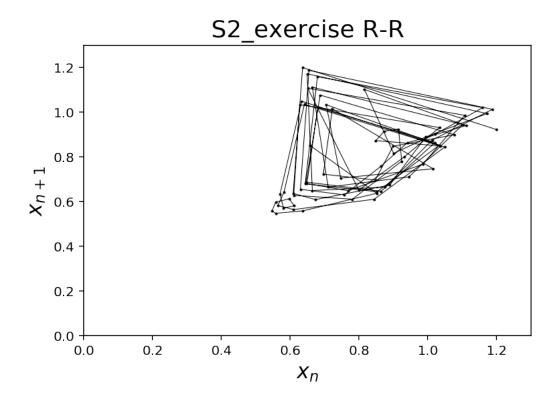


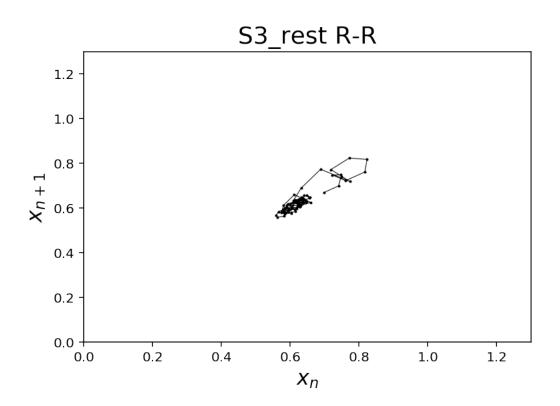


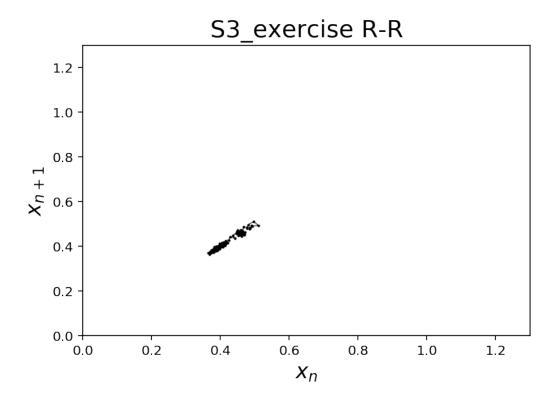












Notice how the trajectory in phase space becomes smaller when the subject is holdings his breath.

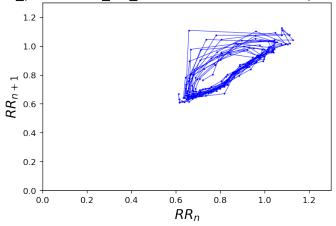
With this time series, we will use Takens theorem to see what we can recontruct. The time delay we will use is 1 R-R interval.

Recording superposition when the person holds his/her breath. The same colors as in the Poincaré plot are used to make it easier observe a pattern.

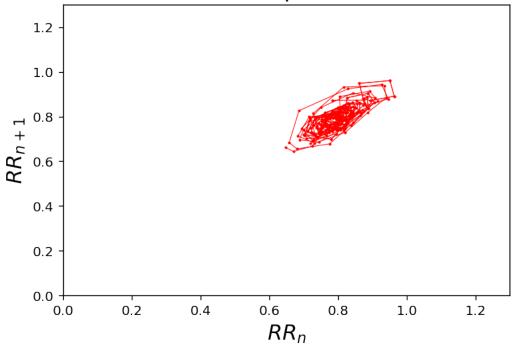
```
plt.ylim(0, 1.3)
        plt.xlabel(r"$RR_n$")
        plt.ylabel(r"$RR_{n+1}$")
        plt.savefig('RR_intervals/phase_space_'+str(corresponding_folder[i])+'.
 →jpg')#Saves images in folder
        plt.show()
        plt. plot(recordings[i].RR[0: n-time_delay], recordings[i].
 →RR[time_delay: n],
              marker = "o", markersize = 1, linewidth = 0.5, c=_{\square}
 →colors[color_index])
    plt. plot(recordings[i].RR[0: n-time_delay], recordings[i].RR[time_delay:__
 \hookrightarrown],
              marker = "o", markersize = 1, linewidth = 0.5, c=__

¬colors[color_index])
plt.title(str(corresponding_folder[i-1]) + " R-R")
plt.xlim(0, 1.3)
plt.ylim(0, 1.3)
plt.xlabel(r"$RR_n$")
plt.ylabel(r"$RR_{n+1}$")
plt.savefig('RR_intervals/phase_space_'+str(corresponding_folder[i])+'.
→ jpg')#Saves images in folder
plt.show()
```

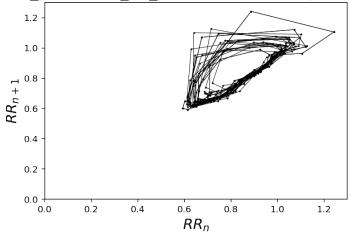
respiraciones profundas 55 abdomen R-R Phase space reconstruction



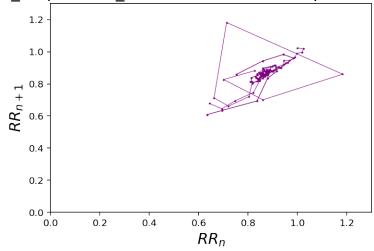
control R-R Phase space reconstruction



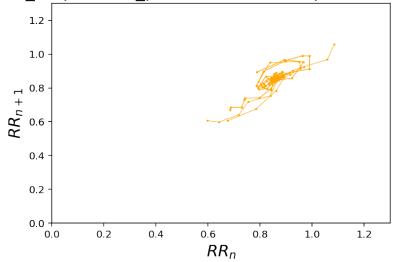
respiraciones_profundas_55_pecho R-R Phase space reconstruction



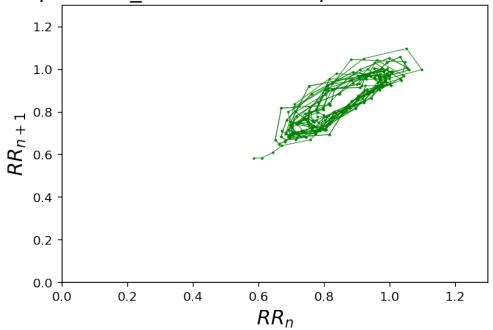
sostener_respiracion_abdomen R-R Phase space reconstruction

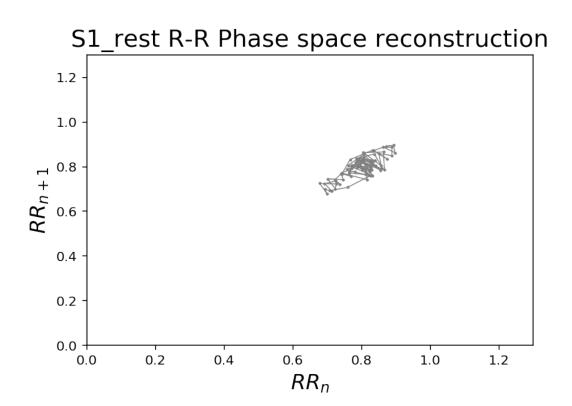


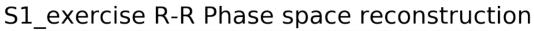
sostener_respiracion_pecho R-R Phase space reconstruction

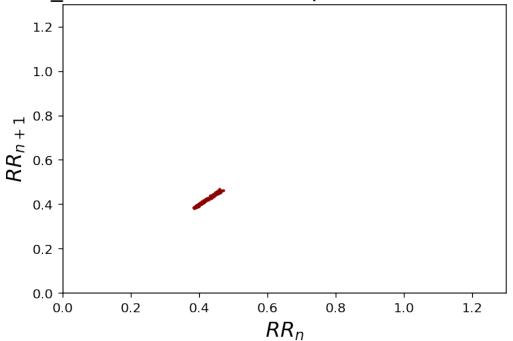


respiracion_ola R-R Phase space reconstruction

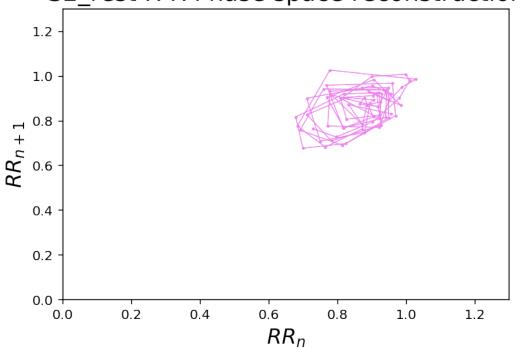




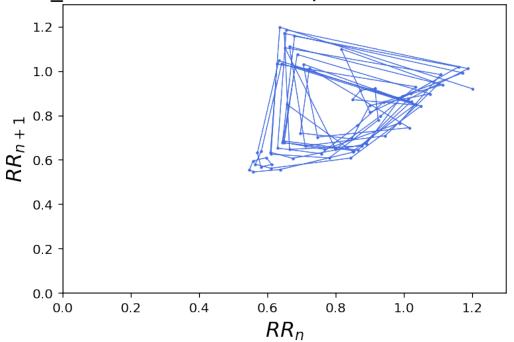




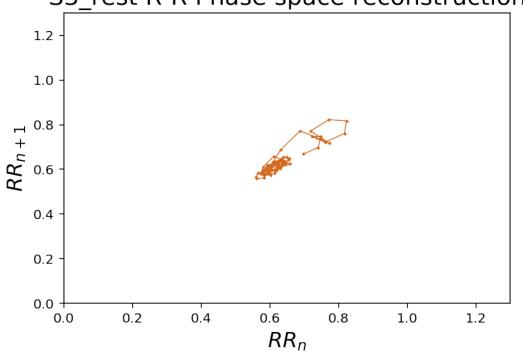
S2_rest R-R Phase space reconstruction

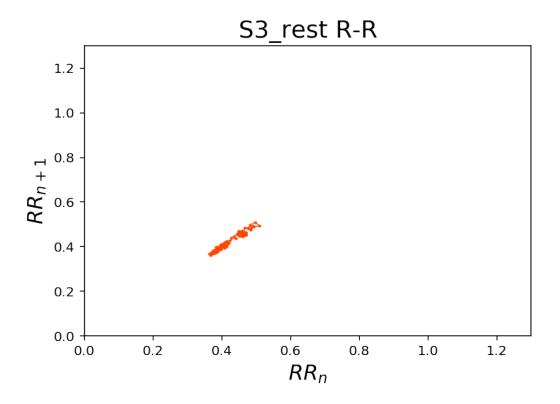


S2_exercise R-R Phase space reconstruction



S3_rest R-R Phase space reconstruction



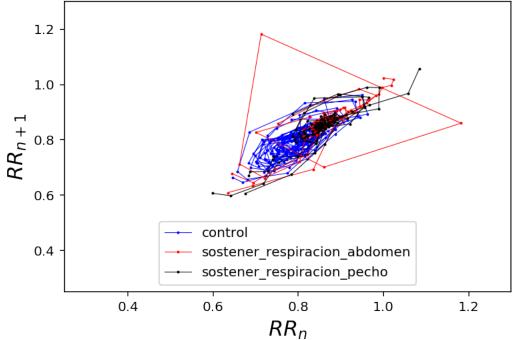


```
[13]: # Comparison between control, holding breath in chest and holding breath in
      \rightarrow abdomen
      colors = ['blue', 'red', 'black', 'purple', "orange", "green"]
      color_index = 0
      banner = False
      time_delay = 1
      for i in range(len(recordings)):
          if corresponding_folder[i] == "control" or "sostener" in_
      →corresponding_folder[i]: #First event
              n = np.size(recordings[i].RR) #size of the voltage vector
              if banner == False: #First event
                  plt. plot(recordings[i].RR[0: n-time_delay], recordings[i].
       \rightarrowRR[time_delay: n],
                            marker = "o", markersize = 1, linewidth = 0.5, c=__
       label = corresponding_folder[i])
              else: #Other events, does not plot label
```

```
plt. plot(recordings[i].RR[0: n-time_delay], recordings[i].
 \rightarrowRR[time_delay: n],
                      marker = "o", markersize = 1, linewidth = 0.5, c=__
 →colors[color_index])
        banner = True
    if len(recordings)-1 != i:
        if banner == True and corresponding_folder[i] !=__

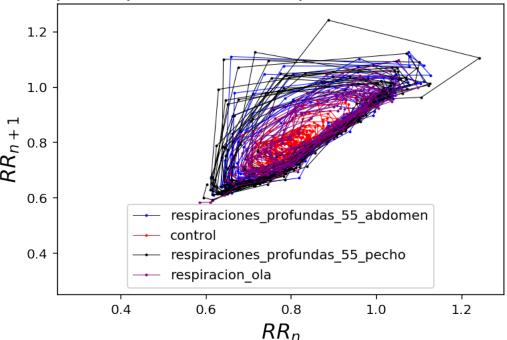
→corresponding_folder[i+1]:
            color_index = color_index+1
            banner = False
plt.title("Superimposed Phase space reconstruction")
plt.xlim(0.25, 1.3)
plt.ylim(0.25, 1.3)
plt.xlabel(r"$RR_n$")
plt.ylabel(r"$RR_{n+1}$")
plt.legend(loc='lower center')
plt.savefig('RR_intervals/phase_space_superimposed_sostener.jpg') #Saves images_
\rightarrow in folder
plt.show()
```

Superimposed Phase space reconstruction



```
[14]: # Comparar: control, respiraciones profundas 55 pecho, respiraciones profundas
       \hookrightarrow 55 abdomen, respiraciones en ola.
      colors = ['blue', 'red', 'black', 'purple', "orange", "green"]
      color index = 0
      banner = False
      time delay = 1
      for i in range(len(recordings)):
          if corresponding_folder[i] == "control" or "55" in corresponding_folder[i] or__
       →"ola" in corresponding_folder[i]: #First event
              n = np.size(recordings[i].RR) #size of the voltage vector
              if banner == False: #First event
                  plt. plot(recordings[i].RR[0: n-time_delay], recordings[i].
       →RR[time_delay: n],
                            marker = "o", markersize = 1, linewidth = 0.5, c=__
       label = corresponding_folder[i])
              else: #Other events, does not plot label
                  plt. plot(recordings[i].RR[0: n-time_delay], recordings[i].
       \rightarrowRR[time_delay: n],
                            marker = "o", markersize = 1, linewidth = 0.5, c=__
       banner = True
          if len(recordings)-1 != i:
              if banner == True and corresponding folder[i] !=___
       →corresponding_folder[i+1]:
                  color index = color index+1
                  banner = False
      plt.title("Superimposed Phase space reconstruction")
      plt.xlabel(r"$RR n$")
      y = r' RR_{n+1} 
      plt.ylabel(y)
      plt.xlim(0.25, 1.3)
      plt.ylim(0.25, 1.3)
      plt.legend(loc='lower center')
     plt.savefig('RR_intervals/phase_space_superimposed_respirar.jpg') #Saves images_
      \rightarrow in folder
      plt.show()
```





```
[]:
```

5.0.1 Exercise: Are the results obtained in a Poincaré plot and in a recurrence plot contradictory? While we are observing a loss in the first plot's variability with exercise, we are seeing the opposite in a recurrence plot. Why?

6 Recurrence plots

This is a technique which compares every single data point to every other. Because of this reason, it is a very expensive algorithm computationaly. To reduce this computational time, we must create a surrogate data set. Be sure to create a surrogate data set that includes at least two QRS complexes.

In the following cell, change the start and end values to obtain two QRS complexes.

```
[15]: # Heat map Recurrence plot
def recurrence_plot(surrogate, data_point_delay = 25):
    n = len(surrogate)
    euclid = np.zeros((n,n), dtype = 'float')
```

```
normal_euclid = np.zeros((n,n), dtype = 'float')
    #Cycle for obtaining the euclid distance between any two points
    for i in range(0, n-data_point_delay):
        for j in range(data_point_delay, n):
            euclid[i][j] = np.sqrt(np.abs(surrogate[i]**2 - surrogate[j]**2))__
 →#euclidian norm
    normal_aux = np.max(euclid)
    # Cycle for normalizing the distance
    for i in range(0, n-data_point_delay):
        for j in range(data_point_delay, n):
            normal_euclid[i][j] = np.abs(euclid[i][j]/normal_aux-1)
            \#Normalizing the values, and the farthest points have the lowest \sqcup
\rightarrowvalue (0).
            #while the nearest points have a value near 1
    return normal_euclid
def graph recurrence(surrogate data, index surrogate, normal euclid, label):
    #Initializing the graphic space
    fig = plt.figure(figsize=(6,8))
    gs = mpl.gridspec.GridSpec(2, 2, height_ratios=[1, 1], width_ratios=[2, 1])
    ax1 = fig.add_subplot(gs[1, 0])
    ax2 = fig.add subplot(gs[0, 0], sharex=ax1)
    plt.tick_params(which='both', top=False, right=False)
    ax2.set_autoscalex_on(False)
    # Tachogram
    ax1.set_title("Tachogram")
    ax1.set_ylabel('R-R interval')
    ax1.set xlabel('Time index')
    ax1.set_xlim(0, len(surrogate_data))
    ax1.set_ylim(0.3, 1.3)
    ax1.plot(index_surrogate, surrogate_data, marker="o", c="k")__
 →#index_surrogate or time_surrogate (ms)
    # Recurrence plot
    ax2.set_title("Recurrence plot")
    ax2.set_ylabel('Time index')
    ax2.set_xlabel('Time index')
    plot = ax2.imshow(normal_euclid, origin='lower', aspect="auto", cmap="jet")
    axins = inset_axes(ax2,
                   width="5%", # width = 10% of parent_bbox width
                   height="100%", # height : 50%
```

An important detail to mention is that every recurrence plot is being normalized by its own metric. The biggest distance is being taken to normalize each individual recurrence plot. That means that colors in different plots are not necessarily equivalent. For example, what is red in one plot could be a lighter shade of orange in another.

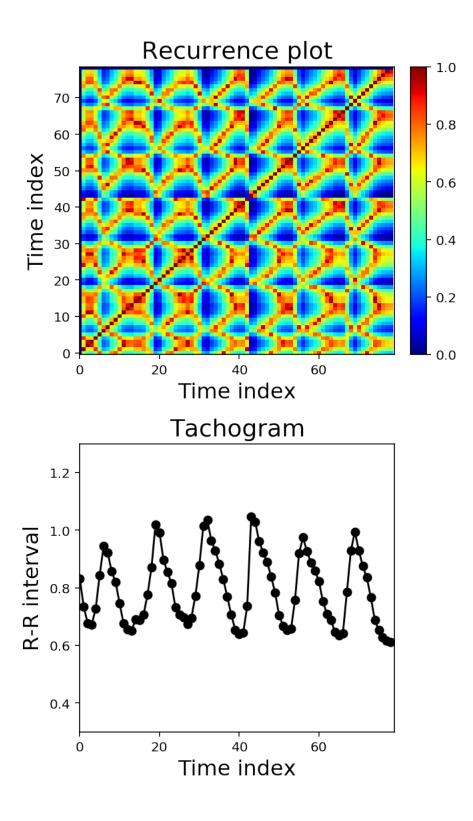
```
[16]: normal_euclid = []

for i in range(len(recordings)):
    normal_euclid.append(recurrence_plot(recordings[i].RR, 1))
    print("Finished recording "+str(i+1))
```

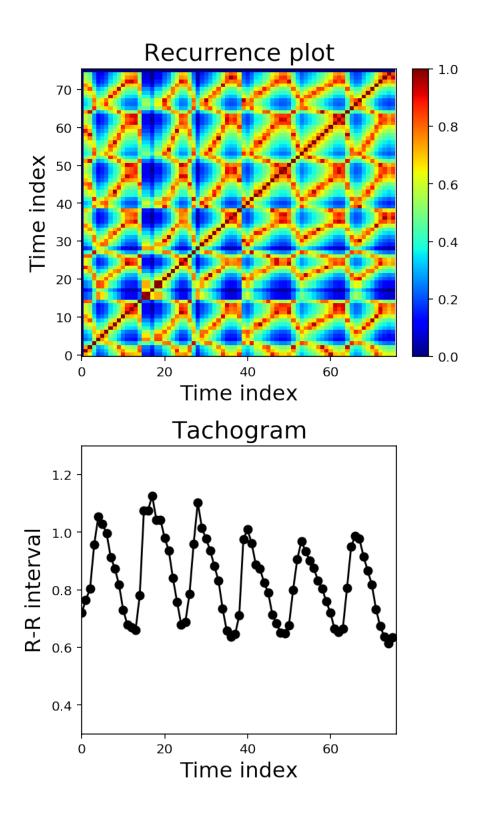
```
Finished recording 1
Finished recording 2
Finished recording 3
Finished recording 4
Finished recording 5
Finished recording 6
Finished recording 7
Finished recording 8
Finished recording 9
Finished recording 10
Finished recording 11
Finished recording 12
Finished recording 13
Finished recording 14
Finished recording 15
Finished recording 16
Finished recording 17
Finished recording 18
Finished recording 19
Finished recording 20
Finished recording 21
Finished recording 22
Finished recording 23
```

Finished recording 24

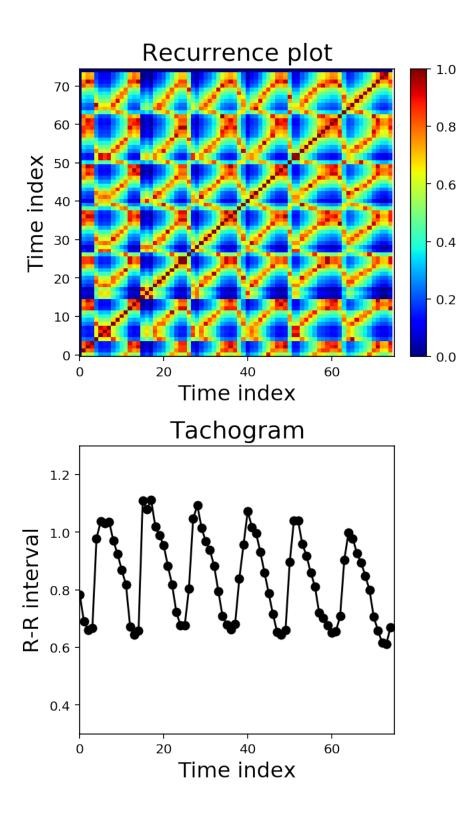
Recording respiraciones_profundas_55_abdomen



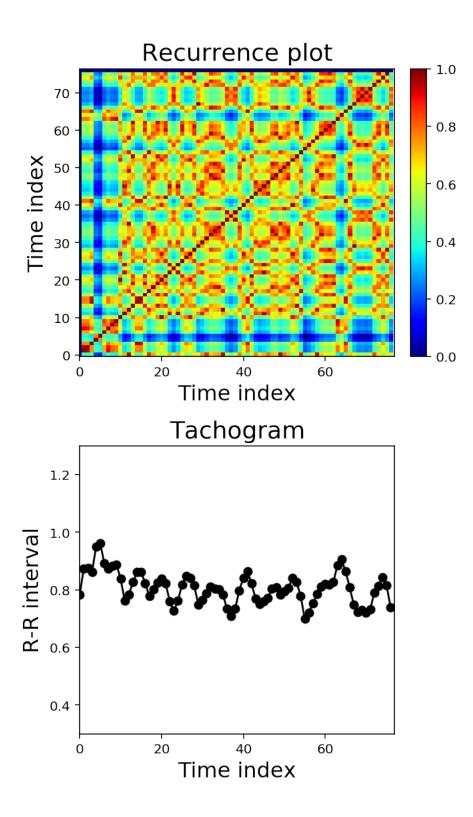
Recording respiraciones_profundas_55_abdomen



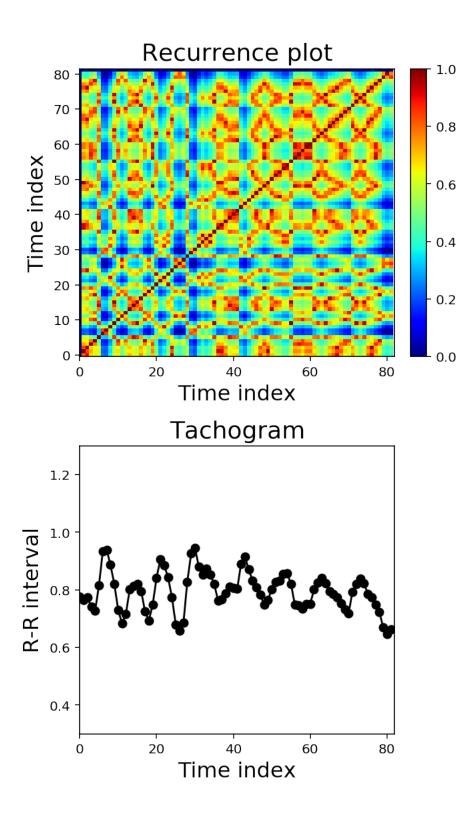
Recording respiraciones_profundas_55_abdomen



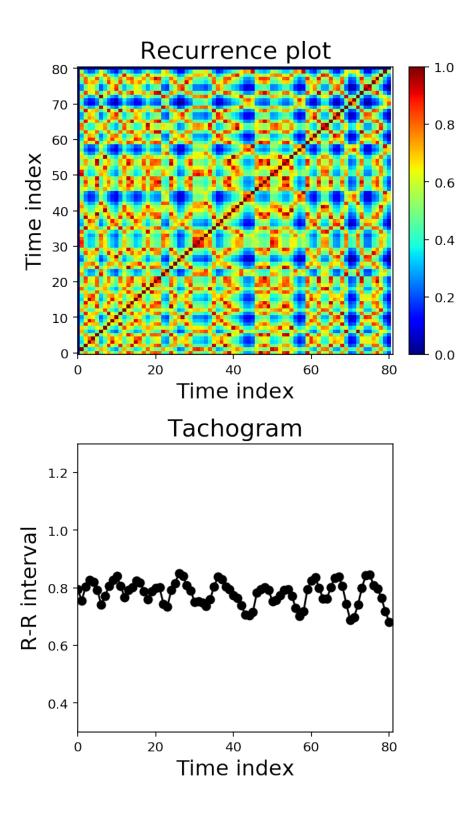
Recording control



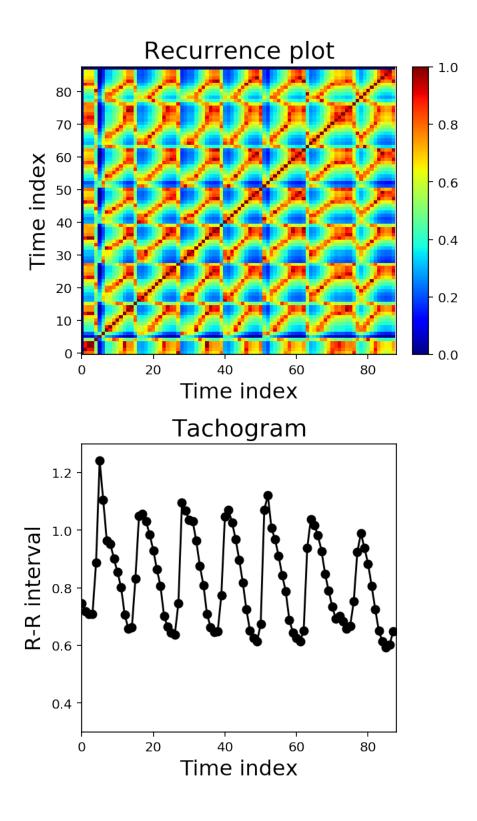
Recording control



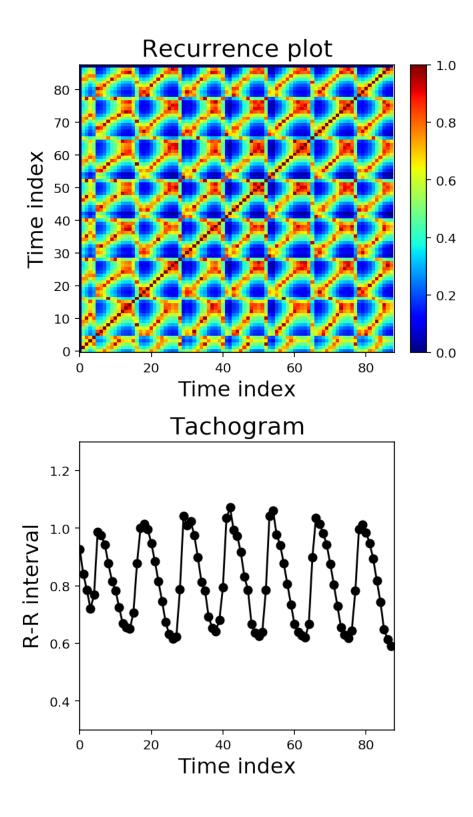
Recording control



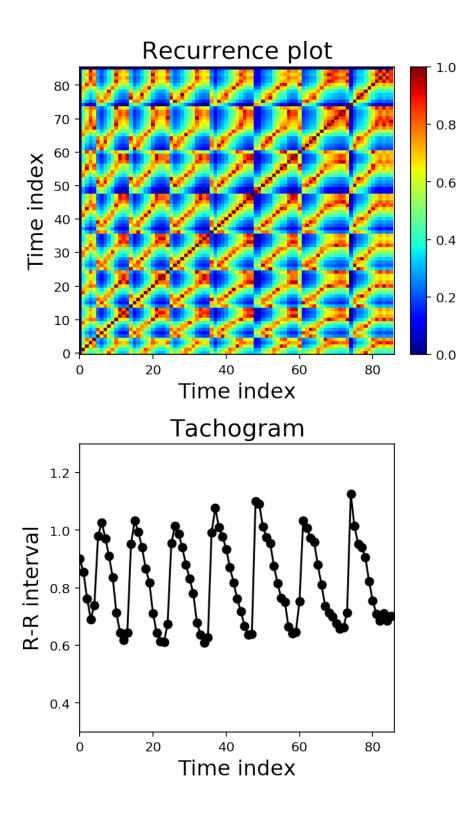
Recording respiraciones_profundas_55_pecho



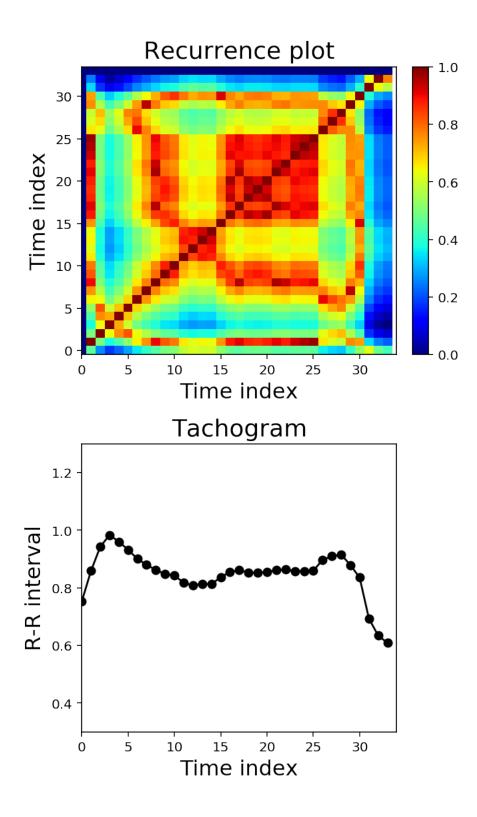
Recording respiraciones_profundas_55_pecho



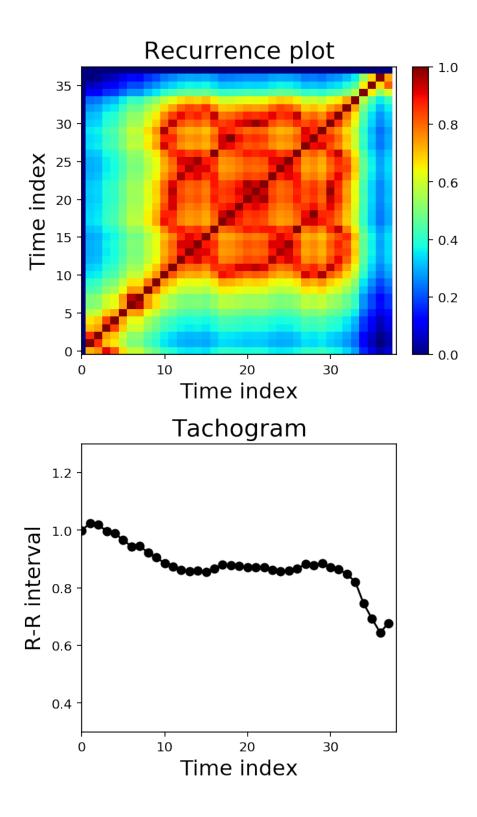
Recording respiraciones_profundas_55_pecho



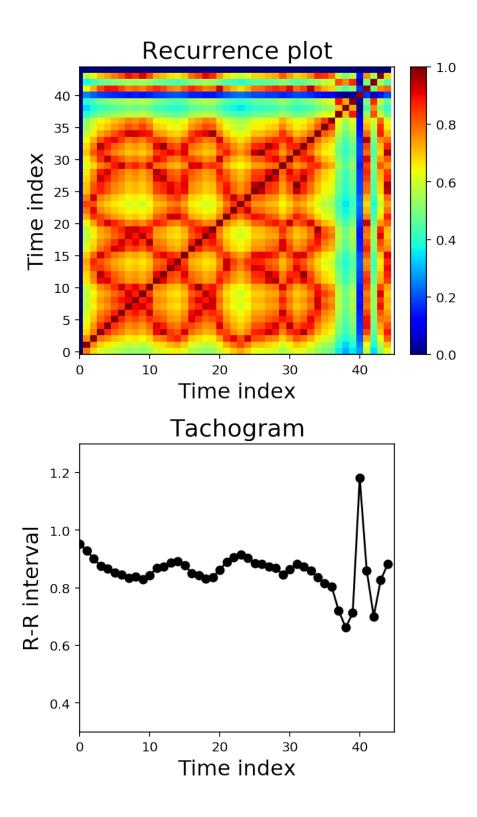
Recording sostener_respiracion_abdomen



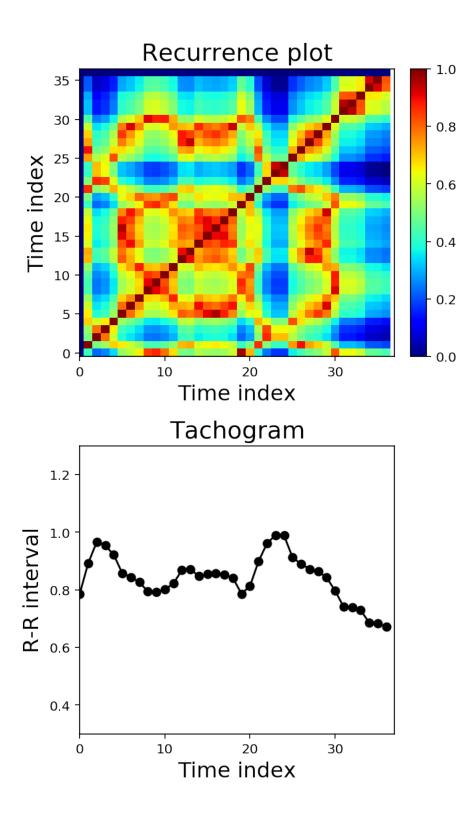
Recording sostener_respiracion_abdomen



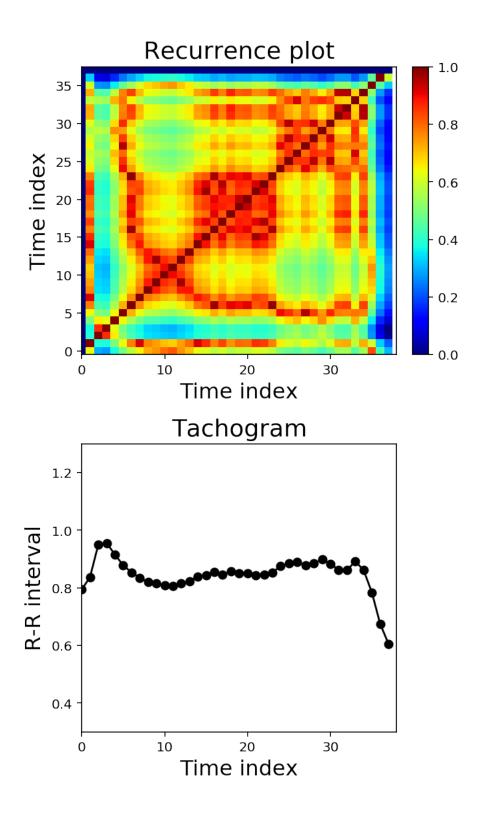
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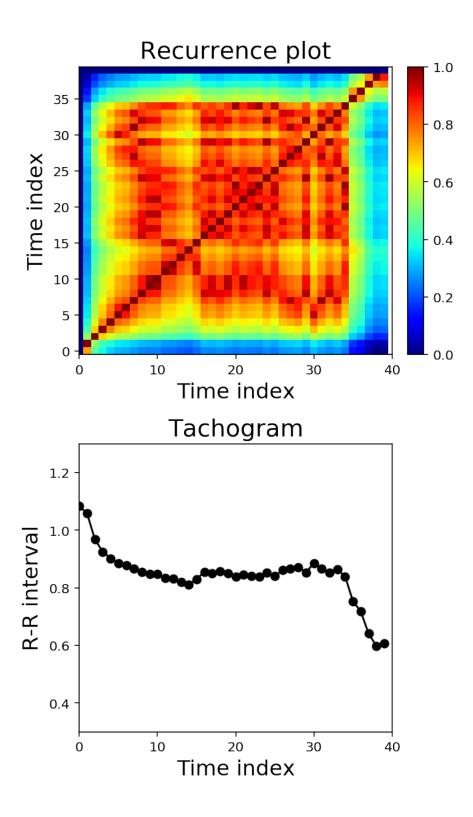
Recording sostener_respiracion_pecho



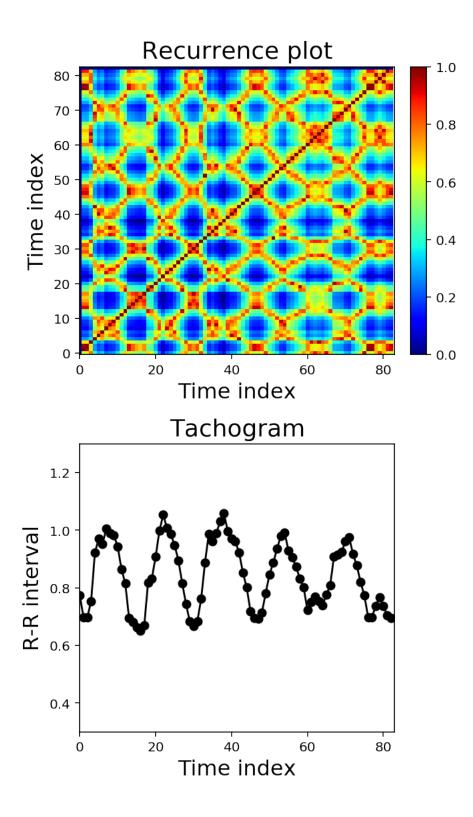
Recording sostener_respiracion_pecho



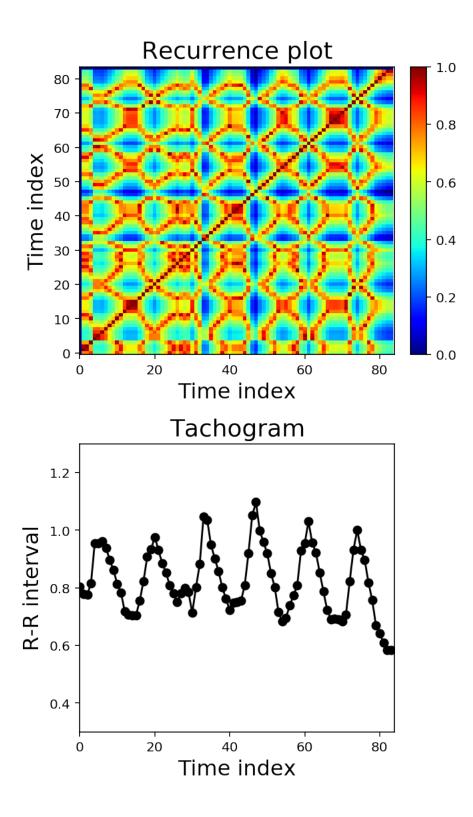
Recording sostener_respiracion_pecho



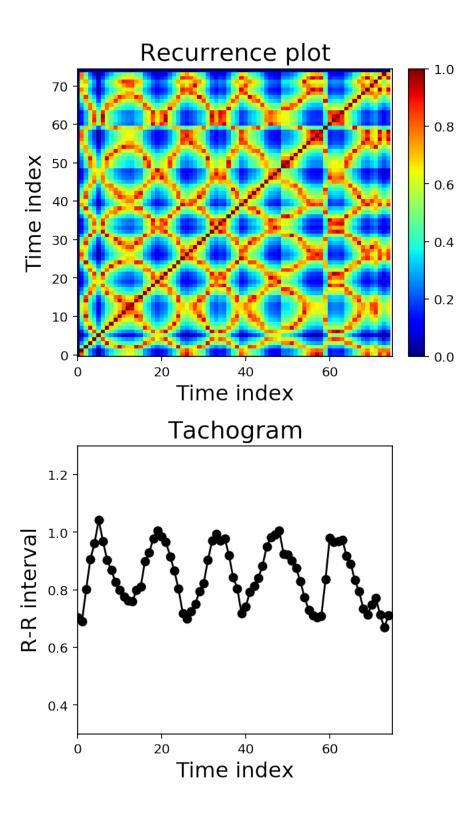
Recording respiracion_ola



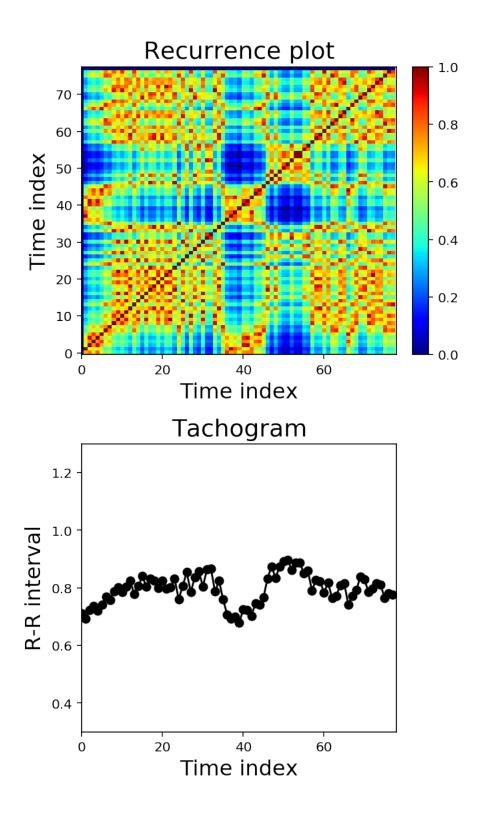
Recording respiracion_ola



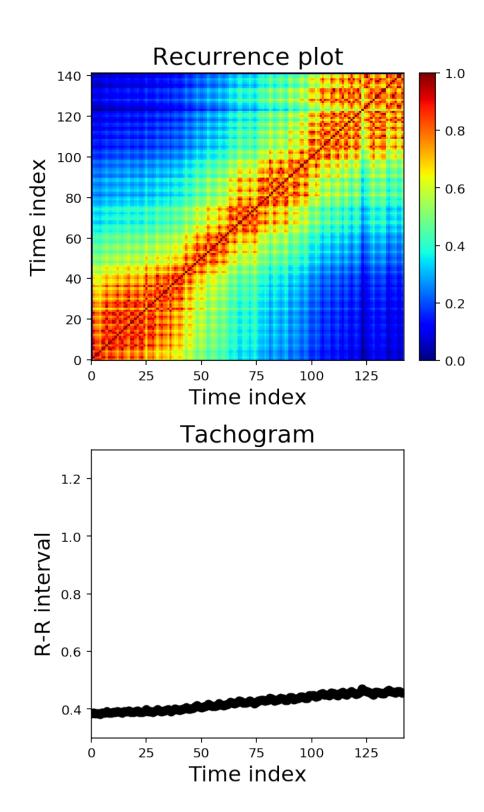
Recording respiracion_ola



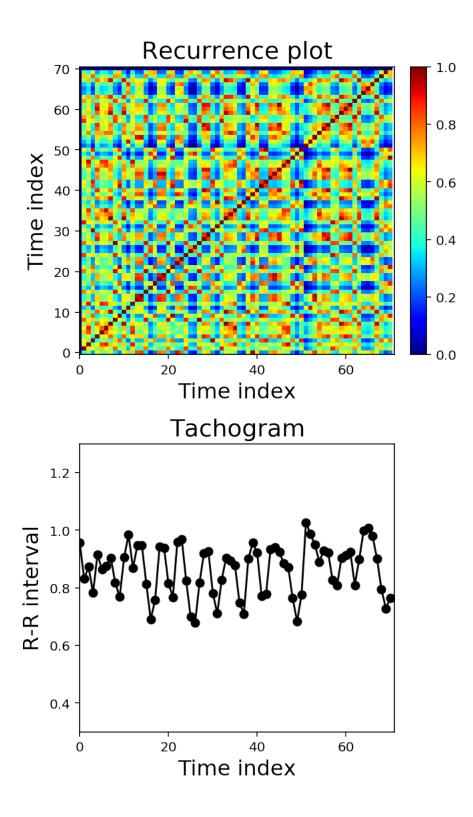
Recording S1_rest



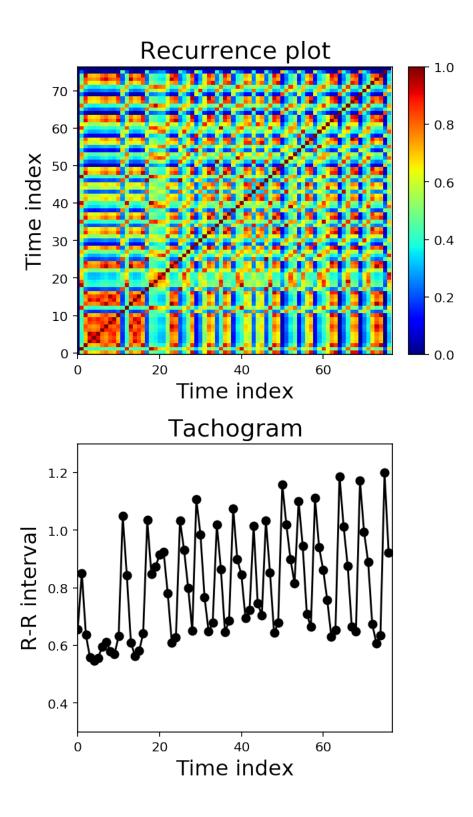
Recording S1_exercise



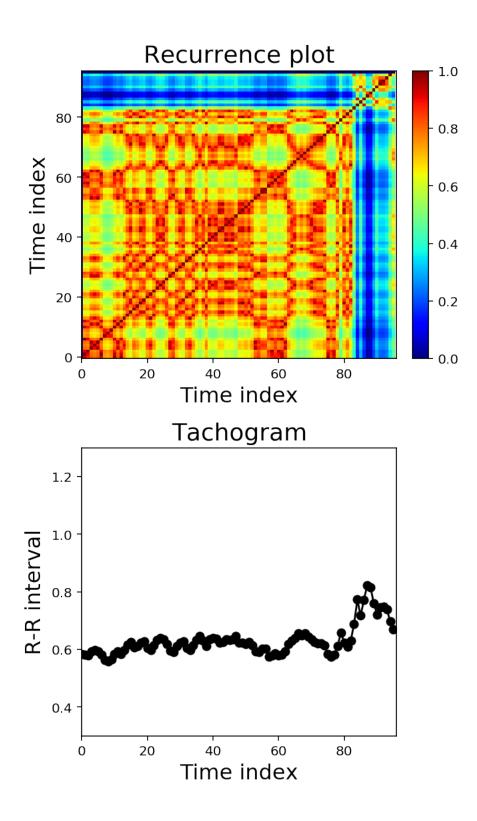
Recording S2_rest



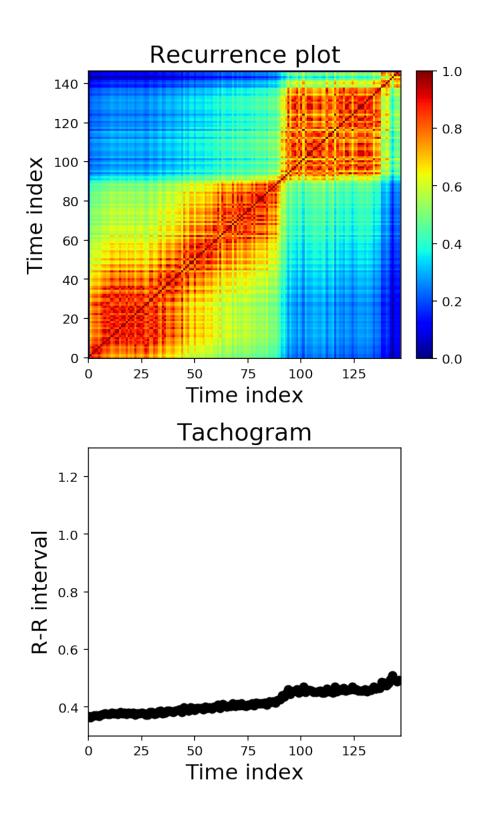
Recording S2_exercise



Recording S3_rest



Recording S3_exercise



7 Final remarks

As you have seen in this notebook, the R-R interval time series does provide valuable information for the analysis, even though there is lost information.