

1 (a) and 1 (b)

1 a x_1 = units of hard bags of seed
 x_2 = units of serrated bags of seed

- Linear

$$\begin{aligned} \text{Max } & 275.75x_1 + 120.50x_2 \\ \text{s.t. } & 100.05x_1 + 60.75x_2 \leq 810.50 \\ & 5.50x_1 + 10.25x_2 \leq 655.80 \\ & 75.30x_1 + 24.84x_2 \leq 520.75 \\ & x_1, x_2 \geq 0 \end{aligned}$$

★ Standard Form

$$\begin{aligned} \text{Max } & 275.75x_1 + 120.50x_2 \\ \text{s.t. } & 100.05x_1 + 60.75x_2 + s_1 = 810.50 \\ & 5.50x_1 + 10.25x_2 + s_2 = 655.80 \\ & 75.30x_1 + 24.84x_2 + s_3 = 520.75 \\ & x_1, x_2, s_1, s_2, s_3 \geq 0 \end{aligned}$$

1 b Using my graph from assignment two, there are 3 extreme points within the feasible region. (intersection of lines of constraints)
 Basic: $s_1 = 810.50, s_2 = 655.80, s_3 = 520.75$
 Feasible: 3

1 (c)

Assignment 3, Problem 1(c) | Daniel Carpenter

Objective Function 275.75 120.50

Setup Basic Vars

is Basic

| | | |
|----|----------|------|
| s1 | (34,099) | TRUE |
| s2 | (2,096) | TRUE |
| s3 | (23,236) | TRUE |

Calculations

| Basis | z | x1 | x2 | s1 | s2 | s3 | Solution | Ratio |
|-------|------|---------|---------|------|------|------|----------|--------|
| s1 | 0 | 100.05 | 60.75 | 1.00 | 0 | 0 | 810.50 | 8.10 |
| s2 | 0 | 5.50 | 10.25 | 0 | 1.00 | 0 | 655.80 | 119.24 |
| s3 | 0 | 75.30 | 24.84 | 0 | 0 | 1.00 | 520.75 | 6.92 |
| z | 1.00 | -275.75 | -120.50 | 0 | 0 | 0 | 0 | |

Iteration 2: s3 leaves basis, x1 enters basis

| Basis | z | x1 | x2 | s1 | s2 | s3 | Solution | Calculation | Ratio |
|-------|------|------|--------|------|------|-------|----------|--------------------------|-------|
| s1 | 0 | 0 | 27.75 | 1.00 | 0 | -1.33 | 118.59 | $= -\$D16 * I\$26 + I16$ | 4.27 |
| s2 | 0 | 0 | 8.44 | 0 | 1.00 | -0.07 | 617.76 | $= -\$D17 * I\$26 + I17$ | 73.23 |
| x1 | 0 | 1.00 | 0.33 | 0 | 0 | 0.01 | 6.92 | $= I18 / \$D18$ | 20.96 |
| z | 1.00 | 0 | -29.54 | 0 | 0 | 3.66 | 1,907.00 | $= -\$D19 * I\$26 + I19$ | |

Iteration 2: s1 leaves basis, x2 enters basis

| Basis | z | x1 | x2 | s1 | s2 | s3 | Solution | Calculation |
|-------|------|------|------|-------|------|-------|----------|-------------------------|
| x2 | 0 | 0 | 1.00 | 0.04 | 0 | -0.05 | 4.27 | $= I24 / \$E24$ |
| s2 | 0 | 0 | 0 | -0.30 | 1.00 | 0.33 | 581.71 | $= I25 - \$E25 * I\31 |
| x1 | 0 | 1.00 | 0 | -0.01 | 0 | 0.03 | 5.51 | $= I26 - \$E26 * I\31 |
| z | 1.00 | 0 | 0 | 1.06 | 0 | 2.25 | 2,033.23 | $= I27 - \$E27 * I\31 |

Final Note

Since all variables contained in z's equation are negative (except z itself), we have arrived at the optimal solution.

Solution 2,033.23399 $= I34$

2 (a)

[illegible]

2(b)

2(c)

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Assignment 3, Problem 2(c) | Daniel Carpenter

ITER 1: Setup

| Basis | z | x1 | x2 | S1 | S2 | S3 | S4 | S5 | R1 | R2 | R3 | Solution | Ratio |
|-------|---|-------|-------|--------|--------|--------|-------|-------|-------|-------|-------|----------|----------|
| R1 | 0 | 0.300 | 0.400 | -1.000 | 0 | 0 | 0 | 0 | 1.000 | 0 | 0 | 2,000.00 | 5,000.00 |
| R2 | 0 | 0.400 | 0.200 | 0 | -1.000 | 0 | 0 | 0 | 0 | 1.000 | 0 | 1,500.00 | 7,500.00 |
| R3 | 0 | 0.200 | 0.300 | 0 | 0 | -1.000 | 0 | 0 | 0 | 0 | 1.000 | 500.00 | 1,666.67 |
| S4 | 0 | 1.000 | 0 | 0 | 0 | 0 | 1.000 | 0 | 0 | 0 | 0 | 9,000.00 | |
| S5 | 0 | 0 | 1.000 | 0 | 0 | 0 | 0 | 1.000 | 0 | 0 | 0 | 6,000.00 | 6,000.00 |
| Z | 1 | 0.900 | 0.900 | -1.000 | -1.000 | -1.000 | 0 | 0 | 1.000 | 1.000 | 1.000 | 0 | |

ITER 2: R3 leaves basis, x2 enters

| Basis | z | x1 | x2 | S1 | S2 | S3 | S4 | S5 | R1 | R2 | R3 | Solution | Calculation | Ratio |
|-------|---|--------|-------|--------|--------|--------|-------|-------|-------|-------|----|-----------|----------------------|----------|
| R1 | 0 | 0.033 | 0 | -1.000 | 0 | 1.333 | 0 | 0 | 1.000 | 0 | | 1,333.33 | =N6 - \$E6 * N\$18 | 1,000.00 |
| R2 | 0 | 0.267 | 0 | 0 | -1.000 | 0.667 | 0 | 0 | 0 | 1.000 | | 1,166.67 | =N7 - \$E7 * N\$18 | 1,750.00 |
| x2 | 0 | 0.667 | 1.000 | 0 | 0 | -3.333 | 0 | 0 | 0 | 0 | | 1,666.67 | =N8 / \$E8 | |
| S4 | | 1.000 | 0 | 0 | 0 | 0 | 1.000 | 0 | 0 | 0 | | 9,000.00 | =N9 - \$E9 * N\$18 | |
| S5 | 0 | -0.667 | 0 | 0 | 0 | 3.333 | 0 | 1.000 | 0 | 0 | | 4,333.33 | =N10 - \$E10 * N\$18 | 1,300.00 |
| Z | 0 | 0.300 | 0 | -1.000 | -1.000 | 2.000 | 0 | 0 | 1.000 | 1.000 | | -1,500.00 | | |

ITER 3: R5 leaves basis, s1 enters

| Basis | z | x1 | x2 | S1 | S2 | S3 | S4 | S5 | R1 | R2 | R3 | Solution | Calculation | Ratio |
|-------|---|--------|-------|--------|--------|-------|-------|-------|----|-------|----|-----------|----------------------|----------|
| S3 | 0 | 0.025 | 0 | -0.750 | 0 | 1.000 | 0 | 0 | | 0 | | 1,000.00 | =N16 / \$H16 | |
| R2 | 0 | 0.250 | 0 | 0.500 | -1.000 | 0 | 0 | 0 | | 1.000 | | 500.00 | =N17 - \$H17 * N\$25 | 1,000.00 |
| x2 | 0 | 0.750 | 1.000 | -2.500 | 0 | 0 | 0 | 0 | | 0 | | 5,000.00 | =N18 - \$H18 * N\$25 | |
| S4 | 0 | 1.000 | 0 | 0 | 0 | 0 | 1.000 | 0 | | 0 | | 9,000.00 | =N19 - \$H19 * N\$25 | |
| S5 | 0 | -0.750 | 0 | 2.500 | 0 | 0 | 0 | 1.000 | | 0 | | 1,000.00 | =N20 - \$H20 * N\$25 | 400.00 |
| Z | 0 | 0.250 | 0 | 0.500 | -1.000 | 0 | 0 | 0 | | 1.000 | | -3,500.00 | | |

ITER 4: R2 leaves basis, x1 enters

| Basis | z | x1 | x2 | S1 | S2 | S3 | S4 | S5 | R1 | R2 | R3 | Solution | Calculation | Ratio |
|-------|---|--------|-------|-------|--------|-------|-------|--------|----|-------|----|-----------|----------------------|----------|
| S3 | 0 | -0.200 | 0 | 0 | 0 | 1.000 | 0 | 0.300 | | 0 | | 1,300.00 | =N25 - \$F25 * N\$38 | |
| x1 | 0 | 0.400 | 0 | 0 | -1.000 | 0 | 0 | -0.200 | | 1.000 | | 300.00 | =N26 - \$F26 * N\$38 | 750.00 |
| x2 | 0 | 0 | 1.000 | 0 | 0 | 0 | 0 | 1.000 | | 0 | | 6,000.00 | =N27 - \$F27 * N\$38 | |
| S4 | 0 | 1.000 | 0 | 0 | 0 | 0 | 1.000 | 0 | | 0 | | 9,000.00 | =N28 - \$F28 * N\$38 | 9,000.00 |
| S5 | 0 | -0.300 | 0 | 1.000 | 0 | 0 | 0 | 0.400 | | 0 | | 400.00 | =N29 / \$F\$29 | |
| Z | 0 | 0.400 | 0 | 0 | -1.000 | 0 | 0 | -0.200 | | 1.000 | | -3,700.00 | | |

ITER 5: S1 leaves basis, s5 enters

| Basis | z | x1 | x2 | S1 | S2 | S3 | S4 | S5 | R1 | R2 | R3 | Solution | Calculation | Ratio |
|-------|---|-------|-------|-------|--------|-------|-------|--------|----|----|----|-----------|----------------------|-----------|
| S3 | 0 | 0 | 0 | 0 | -0.500 | 1.000 | 0 | 0.200 | | | | 1,450.00 | =N34 - \$D34 * N\$44 | 7,250.00 |
| x1 | 0 | 1.000 | 0 | 0 | -2.500 | 0 | 0 | -0.500 | | | | 750.00 | =N35 / \$D35 | |
| x2 | 0 | 0 | 1.000 | 0 | 0 | 0 | 0 | 1.000 | | | | 6,000.00 | =N36 - \$D36 * N\$44 | 6,000.00 |
| S4 | 0 | 0 | 0 | 0 | 2.500 | 0 | 1.000 | 0.500 | | | | 8,250.00 | =N37 - \$D37 * N\$44 | 16,500.00 |
| s1 | 0 | 0 | 0 | 1.000 | -0.750 | 0 | 0 | 0.250 | | | | 625.00 | =N38 - \$D38 * N\$44 | 2,500.00 |
| Z | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | | | | -4,000.00 | =N39 - \$D39 * N\$44 | |

Final Note

Initial basic solution achieved.

| | A | B | C | D | E | F | G | H | I | J | K | L | M | N | O | P | Q | R | | | | | | | | | | | | | | | |
|----|---|--|---|--------|--------|---------|---------|-------|-------|--------|----|----|----|------------|----------------------|---|-----------|---|--|--|--|--|--|--|--|--|--|--|--|--|--|--|--|
| 1 | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | |
| 2 | | Assignment 3, Problem 2(d) Daniel Carpenter | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | |
| 3 | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | |
| 4 | | --> Iter 5 from Problem 2(b) <-- | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | |
| 5 | | Basis | z | x1 | x2 | S1 | S2 | S3 | S4 | S5 | R1 | R2 | R3 | Solution | Calculation | | Ratio | | | | | | | | | | | | | | | | |
| 6 | | S3 | 0 | 0 | 0 | 0 | -0.500 | 1.000 | 0 | 0.200 | | | | 1,450.00 | =2(b)/!N43 | | 7,250.00 | | | | | | | | | | | | | | | | |
| 7 | | x1 | 0 | 1.000 | 0 | 0 | -2.500 | 0 | 0 | -0.500 | | | | 750.00 | =2(b)/!N44 | | | | | | | | | | | | | | | | | | |
| 8 | | x2 | 0 | 0 | 1.000 | 0 | 0 | 0 | 0 | 1.000 | | | | 6,000.00 | =2(b)/!N45 | | 6,000.00 | | | | | | | | | | | | | | | | |
| 9 | | S4 | 0 | 0 | 0 | 0 | 2.500 | 0 | 1.000 | 0.500 | | | | 8,250.00 | =2(b)/!N46 | | 16,500.00 | | | | | | | | | | | | | | | | |
| 10 | | s1 | 0 | 0 | 0 | 1.000 | -0.750 | 0 | 0 | 0.250 | | | | 625.00 | =2(b)/!N47 | | 2,500.00 | | | | | | | | | | | | | | | | |
| 11 | | Z | 1 | 20.000 | 15.000 | 0 | -50.000 | 0 | 0 | 5.000 | | | | 105,000.00 | =2(b)/!N48 | | | | | | | | | | | | | | | | | | |
| 12 | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | |
| 13 | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | |
| 14 | | ITER 6: S1 leaves, s5 enters | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | |
| 15 | | Basis | z | x1 | x2 | S1 | S2 | S3 | S4 | S5 | R1 | R2 | R3 | Solution | Calculation | | | | | | | | | | | | | | | | | | |
| 16 | | S3 | 0 | 0 | 0 | -0.800 | 0.100 | 1.000 | 0 | 0 | | | | 950.00 | =N6 - \$I6 * N\$20 | | | | | | | | | | | | | | | | | | |
| 17 | | x1 | 0 | 1.000 | 0 | 2.000 | -4.000 | 0 | 0 | 0 | | | | 2,000.00 | =N7 - \$I7 * N\$20 | | | | | | | | | | | | | | | | | | |
| 18 | | x2 | 0 | 0 | 1.000 | -4.000 | 3.000 | 0 | 0 | 0 | | | | 3,500.00 | =N8 - \$I8 * N\$20 | | | | | | | | | | | | | | | | | | |
| 19 | | S4 | 0 | 0 | 0 | -2.000 | 4.000 | 0 | 1.000 | 0 | | | | 7,000.00 | =N9 - \$I9 * N\$20 | | | | | | | | | | | | | | | | | | |
| 20 | | s5 | 0 | 0 | 0 | 4.000 | -3.000 | 0 | 0 | 1.000 | | | | 2,500.00 | =N10 / \$I10 | | | | | | | | | | | | | | | | | | |
| 21 | | Z | 1 | 20.000 | 15.000 | -20.000 | -35.000 | 0 | 0 | 0 | | | | 92,500.00 | =N11 - \$I11 * N\$20 | | | | | | | | | | | | | | | | | | |
| 22 | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | |
| 23 | | Final Note | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | |
| 24 | | Since all variables contained in z's equation are negative (except z itself), we have arrived at the optimal solution. | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | |
| 25 | | Minimized Cost (\$): | | 92,500 | | =N21 | | | | | | | | | | | | | | | | | | | | | | | | | | | |
| 26 | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | |
| 27 | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | |
| 28 | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | |