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Simplex method calculator

Algorithm and examples

Method

1. Simplex method (BigM method)

Solve the Linear programming problem using Simplex method calculator

Type your linear programming problem

MIN $Z = 20x_1 + 15x_2$

subject to

$.3x_1 + .4x_2 \geq 2000$

$.4x_1 + .2x_2 \geq 1500$

$.2x_1 + .3x_2 \geq 500$

$x_1 \leq 9000$

OR

Total Variables : 2

Total Constraints : 5

Generate

Min $Z = 20$

$x_1 + 15$

x_2

Subject to constraints

$.3$

$x_1 + .4$

$x_2 \geq$

2000

$.4$

$x_1 + .2$

$x_2 \geq$

1500

$.2$

$x_1 + .3$

$x_2 \geq$

500

1

$x_1 + 0$

$x_2 \leq$

9000

0

$x_1 + 1$

$x_2 \leq$

6000

and $x_1, x_2 \geq 0$ and unrestricted in sign

☐ x_1 , ☐ x_2

Mode : Decimal

☐ Solve after converting Min function to Max function

Calculate : $Z_j - C_j$

☐ Alternate Solution (if exists) ☒ Artificial Column Remove

Find

Random

New

Solution Help

Solution will be displayed step by step (In 6 parts)

Solution

Find solution using Simplex method (BigM method)

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https://cbom.atozmath.com/CBOM/Simplex.aspx?q=sm&q1=2%605%60MIN%60Z%60x1%2cx2%6020%2c15%60.3%2c.4%3b.4%2c.2%3b.2%2c.3%... 1/6

$$x_2 \leq 6000$$
$$\text{and } x_1, x_2 \geq 0$$

Solution:
Problem is

$$\text{Min } Z = 20x_1 + 15x_2$$

subject to

$$0.3 x_1 + 0.4 x_2 \geq 2000$$

$$0.4 x_1 + 0.2 x_2 \geq 1500$$

$$0.2 x_1 + 0.3 x_2 \geq 500$$

$$x_1 \leq 9000$$

$$x_2 \leq 6000$$

and $x_1, x_2 \geq 0$;

The problem is converted to canonical form by adding slack, surplus and artificial variables as appropriate

1. As the constraint-1 is of type ' \geq ' we should subtract surplus variable S_1 and add artificial variable A_1
2. As the constraint-2 is of type ' \geq ' we should subtract surplus variable S_2 and add artificial variable A_2
3. As the constraint-3 is of type ' \geq ' we should subtract surplus variable S_3 and add artificial variable A_3
4. As the constraint-4 is of type ' \leq ' we should add slack variable S_4
5. As the constraint-5 is of type ' \leq ' we should add slack variable S_5

After introducing slack,surplus,artificial variables

$$\text{Min } Z = 20x_1 + 15x_2 + 0S_1 + 0S_2 + 0S_3 + 0S_4 + 0S_5 + MA_1 + MA_2 + MA_3$$

subject to

$$0.3 x_1 + 0.4 x_2 - S_1 + A_1 = 2000$$

$$0.4x_1 + 0.2x_2 - S_2 + A_2 = 1500$$

$$0.2x_1 + 0.3x_2 - S_3 + A_3 = 500$$

$$x_1 + S_4 = 9000$$

$$x_2 + S_5 = 6000$$

and $x_1, x_2, S_1, S_2, S_3, S_4, S_5, A_1, A_2, A_3 \geq 0$

Iteration-1		C_j	20	15	0	0	0	0	0	M	M	M	
B	C_B	X_B	x_1	x_2	S_1	S_2	S_3	S_4	S_5	A_1	A_2	A_3	MinRatio $\frac{X_B}{x_2}$
A_1	M	2000	0.3	0.4	-1	0	0	0	0	1	0	0	$\frac{2000}{0.4} = 5000$
A_2	M	1500	0.4	0.2	0	-1	0	0	0	0	1	0	$\frac{1500}{0.2} = 7500$
A_3	M	500	0.2	(0.3)	0	0	-1	0	0	0	0	1	$\frac{500}{0.3} = 1666.6667 \rightarrow$
S_4	0	9000	1	0	0	0	0	1	0	0	0	0	---
S_5	0	6000	0	1	0	0	0	0	1	0	0	0	$\frac{6000}{1} = 6000$
$Z = 4000M$		Z_j	$0.9M$	$0.9M$	$-M$	$-M$	$-M$	0	0	M	M	M	
		$Z_j - C_j$	$0.9M - 20$	$0.9M - 15 \uparrow$									

Positive maximum $Z_j - C_j$ is $0.9M - 15$ and its column inc

Minimum ratio is 1666.6667 and its row index is 3. So, **tr**

∴ The pivot element is 0.3.

Entering = x_2 , Departing = A_3 , Key Element = 0.3

$$\perp R(\text{new}) = R(\text{old}) \div 0.3$$



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$$+ R_2(\text{new}) = R_2(\text{old}) - 0.2R_3(\text{new})$$

$$+ R_4(\text{new}) = R_4(\text{old})$$

$$+ R_5(\text{new}) = R_5(\text{old}) - R_3(\text{new})$$

Iteration-2		C_j	20	15	0	0	0	0	0	M	M	
B	C_B	X_B	x_1	x_2	S_1	S_2	S_3	S_4	S_5	A_1	A_2	MinRatio $\frac{X_B}{S_3}$
A_1	M	1333.3333	0.0333	0	-1	0	(1.3333)	0	0	1	0	$\frac{1333.3333}{1.3333} = 1000 \rightarrow$
A_2	M	1166.6667	0.2667	0	0	-1	0.6667	0	0	0	1	$\frac{1166.6667}{0.6667} = 1750$
x_2	15	1666.6667	0.6667	1	0	0	-3.3333	0	0	0	0	---
S_4	0	9000	1	0	0	0	0	1	0	0	0	---
S_5	0	4333.3333	-0.6667	0	0	0	3.3333	0	1	0	0	$\frac{4333.3333}{3.3333} = 1300$
$Z = 2500M + 25000$		Z_j	$0.3M + 10$	15	$-M$	$-M$	$2M - 50$	0	0	M	M	
		$Z_j - C_j$	$0.3M - 10$	0	$-M$	$-M$	$2M - 50 \uparrow$	0	0	0	0	

Positive maximum $Z_j - C_j$ is $2M - 50$ and its column index is 5. So, the entering variable is S_3 .

Minimum ratio is 1000 and its row index is 1. So, the leaving basis variable is A_1 .

\therefore The pivot element is 1.3333.

Entering = S_3 , Departing = A_1 , Key Element = 1.3333

$$+ R_1(\text{new}) = R_1(\text{old}) \div 1.3333$$

$$+ R_2(\text{new}) = R_2(\text{old}) - 0.6667R_1(\text{new})$$

$$+ R_3(\text{new}) = R_3(\text{old}) + 3.3333R_1(\text{new})$$

$$+ R_4(\text{new}) = R_4(\text{old})$$

$$+ R_5(\text{new}) = R_5(\text{old}) - 3.3333R_1(\text{new})$$

Iteration-3		C_j	20	1
B	C_B	X_B	x_1	x
S_3	0	1000	0.025	(
A_2	M	500	0.25	(
x_2	15	5000	0.75	1



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$Z = 500M + 75000$		Z_j	$0.25M + 11.25$	15	$0.5M - 37.5$	$-M$	0	0	0	M	
		$Z_j - C_j$	$0.25M - 8.75$	0	$0.5M - 37.5 \uparrow$	$-M$	0	0	0	0	

Positive maximum $Z_j - C_j$ is $0.5M - 37.5$ and its column index is 3. So, the entering variable is S_1 .

Minimum ratio is 400 and its row index is 5. So, the leaving basis variable is S_5 .

\therefore The pivot element is 2.5.

Entering = S_1 , Departing = S_5 , Key Element = 2.5

$$+ R_5(\text{new}) = R_5(\text{old}) \div 2.5$$

$$+ R_1(\text{new}) = R_1(\text{old}) + 0.75R_5(\text{new})$$

$$+ R_2(\text{new}) = R_2(\text{old}) - 0.5R_5(\text{new})$$

$$+ R_3(\text{new}) = R_3(\text{old}) + 2.5R_5(\text{new})$$

$$+ R_4(\text{new}) = R_4(\text{old})$$

Iteration-4		C_j	20	15	0	0	0	0	0	M	
B	C_B	X_B	x_1	x_2	S_1	S_2	S_3	S_4	S_5	A_2	MinRatio $\frac{X_B}{x_1}$
S_3	0	1300	-0.2	0	0	0	1	0	0.3	0	---
A_2	M	300	(0.4)	0	0	-1	0	0	-0.2	1	$\frac{300}{0.4} = 750 \rightarrow$
x_2	15	6000	0	1	0	0	0	0	1	0	---
S_4	0	9000	1	0	0	0	0	1	0	0	$\frac{9000}{1} = 9000$
S_1	0	400	-0.3	0	1	0	0	0	0.4	0	---
$Z = 300M + 90000$		Z_j	$0.4M$	15	0	$-M$	0	0	$-0.2M + 15$	M	
		$Z_j - C_j$	$0.4M - 20 \uparrow$	0	0	$-M$	0	0	$-0.2M + 15$	0	

Positive maximum $Z_j - C_j$ is $0.4M - 20$ and its column index is 1. So, the entering variable is x_1 .

Minimum ratio is 750 and its row index is 2. So, the leaving basis variable is A_2 .

\therefore The pivot element is 0.4.

Entering = x_1 , Departing = A_2 , Key Element = 0.4

$$+ R_2(\text{new}) = R_2(\text{old}) \div 0.4$$

$$+ R_1(\text{new}) = R_1(\text{old}) + 0.2R_2(\text{new})$$

$$+ R_3(\text{new}) = R_3(\text{old})$$

$$+ R_4(\text{new}) = R_4(\text{old}) - R_2(\text{new})$$



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Iteration-5		C_j	20	15	0	0	0	0	0	
B	C_B	X_B	x_1	x_2	S_1	S_2	S_3	S_4	S_5	MinRatio $\frac{X_B}{S_5}$
S_3	0	1450	0	0	0	-0.5	1	0	0.2	$\frac{1450}{0.2} = 7250$
x_1	20	750	1	0	0	-2.5	0	0	-0.5	---
x_2	15	6000	0	1	0	0	0	0	1	$\frac{6000}{1} = 6000$
S_4	0	8250	0	0	0	2.5	0	1	0.5	$\frac{8250}{0.5} = 16500$
S_1	0	625	0	0	1	-0.75	0	0	(0.25)	$\frac{625}{0.25} = 2500 \rightarrow$
$Z = 105000$		Z_j	20	15	0	-50	0	0	5	
		$Z_j - C_j$	0	0	0	-50	0	0	5 ↑	

Positive maximum $Z_j - C_j$ is 5 and its column index is 7. So, the entering variable is S_5 .

Minimum ratio is 2500 and its row index is 5. So, the leaving basis variable is S_1 .

∴ The pivot element is 0.25.

Entering = S_5 , Departing = S_1 , Key Element = 0.25

$$+ R_5(\text{new}) = R_5(\text{old}) \div 0.25$$

$$+ R_1(\text{new}) = R_1(\text{old}) - 0.2R_5(\text{new})$$

$$+ R_2(\text{new}) = R_2(\text{old}) + 0.5R_5(\text{new})$$

$$+ R_3(\text{new}) = R_3(\text{old}) - R_5(\text{new})$$

$$+ R_4(\text{new}) = R_4(\text{old}) - 0.5R_5(\text{new})$$

Iteration-6		C_j	20	15	0	0	0	0	0	
B	C_B	X_B	x_1	x_2	S_1	S_2	S_3	S_4	S_5	MinRatio
S_3	0	950	0	0	-0.8	0.1	1	0	0	
x_1	20	2000	1	0	2	-4	0	0	0	
x_2	15	3500	0	1	-4	3	0	0	0	
S_4	0	7000	0	0						
S_5	0	2500	0	0						
$Z = 92500$		Z_j	20	15						
		$Z_j - C_j$	0	0						

Since all $Z_j - C_j \leq 0$

Hence, optimal solution is arrived with value of variable
 $x_1 = 2000, x_2 = 3500$

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