```
In [1]: import statistics
   import pprint
   import pandas as pd
   import numpy as np
   from random import uniform
   from tslearn.utils import to_time_series_dataset
   from tslearn.metrics import dtw#, gak
   import plotly.express as px
   import scipy.stats as st
   import matplotlib.pyplot as plt
   from scipy.optimize import curve_fit
   import seaborn as sns; sns.set()
   #ToDo: Threading
```

```
In [2]: def get best distribution(data):
            dist names = ["gamma", "gumbel 1", "cauchy", "dgamma", "beta", "bet
        aprime", "exponweib", "rayleigh", "fisk",
                          "gausshyper", "invweibull", "pareto", "alpha", "expo
        n", "hypsecant", "mielke", "loggamma",
                           "rdist", "rice"] ## Agregar más a voluntad
            dist results = []
            params = {}
            for dist name in dist names:
                dist = getattr(st, dist name)
                param = dist.fit(data)
                params[dist name] = param
                # Applying the Kolmogorov-Smirnov test
                D, p = st.kstest(data, dist name, args=param)
                print("p value for "+dist name+" = "+str(p))
                dist results.append((dist name, p))
            # select the best fitted distribution
            best dist, best p = (max(dist results, key=lambda item: item[1]))
            # store the name of the best fit and its p value
            print("Best fitting distribution: "+str(best dist))
            print("Best p value: "+ str(best p))
            parms = params[best dist]
            #print("Parameters for the best fit: "+ str(parms))
            map parms = {}
            dist = getattr(st, best dist)
                counter wrong chars = 0
                                                                              #T0
        solve a bug
                for position, shape parameter in enumerate(dist.shapes):
                     #print(position, shape parameter)
                    if shape parameter not in [' ', ',']:
                        map parms[shape parameter] = parms[position-counter wro
        ng chars]
                    else:
                        counter wrong chars += 1
            except:
                pass
            finally:
                map parms["loc"] = parms[-2]
                map parms["scale"] = parms[-1]
            print("Parameters for the best fit: "+ str(map parms))
            return best dist, best p, parms, map parms
```

```
In [3]: def get optimal curves (df curves, example curves, ts example curves, di
        ct probability distrs, prob distrs,
                        min count generated curves, a, b, E min, min f load, roo
        f dtw distance, min corr):
            I = 5000
                                              #5000
            acum generated curves = 0
            while acum generated curves < min count generated curves:
                 for i in range (1, I+1):
                     C i = [None] * 24
                     h max = int(round(uniform(19, 21), 0))
                     C_i[h_max] = 1
                     for h, none in enumerate(C i):
                         if h != h max:
                             function = dict probability distrs[prob distrs
        [h][0]]
                             parms = prob distrs[h][1]
                             was random number found = False
                             while was random number found is False:
                                 E = function.rvs(**parms, size=1)[0]
                                 if (E>=E \min \text{ and } E<1):
                                     was random number found = True
                             C i[h] = E
                     E acum = sum(C i)
                     if (E acum>=a and E acum<=b):</pre>
                         \#print(C_i, type(C_i))
                         f load = statistics.mean(C i) / max(C i)
                         if f load >= min f load:
                             ts C i = to time series dataset(C i)[0]
                             dtw distances = []
                             for k, curve in enumerate(ts example curves):
                                 dtw_distance = dtw(ts C i, curve)
                                 dtw distances.append(dtw distance)
                             average dtw = statistics.mean(dtw distances)
                             if average dtw < roof dtw distance:</pre>
                                 corrs = []
                                 for example curve in example curves:
                                      corr = np.corrcoef(C i, example curve)
                                      corrs.append(corr[0][1])
                                 average corr = statistics.mean(corrs)
                                 if average corr>=min corr:
                                     print(i, f load, E acum, average dtw, avera
        ge corr)
                                     df curves = df curves.append(
                                              { '0': C i[0], '1': C i[1], '2': C
        i[2],
                                               '3': C i[3], '4': C i[4], '5': C i
        [5],
                                               '6': C i[6], '7': C i[7], '8': C i
        [8],
                                               '9': C i[9], '10': C i[10], '11':
```

```
C i[11],
                                      '12': C i[12], '13': C i[13], '14
': C i[14],
                                      '15': C i[15], '16': C i[16], '17
': C_i[17],
                                      '18': C_i[18], '19': C_i[19], '20
': C_i[20],
                                      '21': C_i[21], '22': C_i[22], '23
': C i[23],
                                      'FC': f_load, 'Sum': E_acum,
                                      'DTW_avg_distance': average_dtw, '
Avg correlation': average_corr },
                                 ignore_index=True
                            acum generated curves += 1
                            if acum generated curves>=min count generat
ed curves:
                                return (df curves)
```

```
In [4]: df_example_curves = pd.read_excel (r'Curvas.xlsx')
    df_example_curves.drop(
        df_example_curves.columns[
            df_example_curves.columns.str.contains('unnamed', case = False,
        na=False)
        ],
        axis = 1,
        inplace = True
)

a = df_example_curves['Sum'].min()
b = df_example_curves['Sum'].max()

df_example_curves = df_example_curves.drop(['FC', 'Sum', 'Comentario'],
        axis=1)

print("a: ", a, " b: ", b)
print(df_example_curves)
```

a: 15.161736140999999 b: 19.249227906976746							
0	1	2	3	4	5		
6 \							
0 0.465685 26	0.397058	0.367646	0.372548	0.382352	0.421568	0.5686	
1 0.637209 81	0.506977	0.469767	0.469767	0.488372	0.548837	0.7255	
2 0.637209 81	0.506977	0.469767	0.469767	0.488372	0.548837	0.7055	
3 0.617209 81	0.486977	0.449767	0.449767	0.468372	0.528837	0.6855	
4 0.589328 43	0.474497	0.439237	0.440463	0.456867	0.512020	0.6713	
5 0.539052 96	0.436891	0.403702	0.403582	0.420730	0.470823	0.6210	
7	8	9	• • •	14	15	16	
17 \							
0 0.622548	0.784315	0.779408	0.64	7058 0.50	4901 0.49	5097	
0.460784	0.00000	0 001005	0.01	0.605 0.06	-116 0 00	2000	
1 0.800000	0.990698	0.981395	0.81	8605 0.86	5116 0.89	3023	
0.734884	0.001000	0 001005	0.01	0605 0 06	F116 0 00	2002	
2 0.800000	0.901320	0.891395	0.81	8605 0.86	5116 0.89	3023	
0.767884 3 0.800000	0.901320	0.891395	0 01	8605 0.86	5116 0.87	3023	
0.747884	0.901320	0.891393	0.81	.8603 0.86	3110 0.87	3023	
4 0.755637	0.894413	0.885899	0 77	5718 0.77	5062 0.78	8542	
0.677859	0.094413	0.000099	0.77	3/10 0.//	3002 0.70	0342	
5 0.702376	0.844583	0.829497	0.72	8547 0.71	8564 0.73	1319	
0.641747	0.011303	0.023137	0.72	0.71	0001 0.70	1010	
0.011/1/							
18	19	20	21	22	23		
0 0.593136	0.931371	1.000000	0.936270	0.838232	0.622548		
1 0.758140	0.995349	1.000000	0.999256	0.989507	0.809302		
2 0.758140	0.965742	0.994320	1.000000	0.932314	0.809302		
3 0.758140	0.925742	1.000000	0.956440	0.932314	0.759302		
4 0.716889	0.954551	0.999999	1.000000	0.923092	0.750114		
5 0.694820	1.000000	0.975000	0.978047	0.900141	0.709570		

[6 rows x 24 columns]

```
In [5]: prob_distrs = []
    plots = []
    for (columnName, columnData) in df_example_curves.iteritems():
        ## Maximizar el p-value ##
        print('Column Name : ', columnName)
        #print('Column Contents : ', columnData.values, type(columnData.values), columnData.values.shape)
        best_dist, best_p, parms, map_parms = get_best_distribution(columnData.values)
        prob_distrs.append([best_dist, map_parms])
        #if columnName == 12:
        # ax = sns.distplot(columnData.values, kde=False)
        #ax = sns.distplot(columnData.values, kde=False)
    print("prob_distrs: ")
    pprint.pprint(prob_distrs)
```

```
Column Name: 0
p value for gamma = 0.9153858662603467
p value for gumbel 1 = 0.9611650805916115
p value for cauchy = 0.5828338337557992
p value for dgamma = 0.7103295891934879
p value for beta = 0.4258226481275949
p value for betaprime = 0.9240764030877295
C:\ProgramData\Anaconda3\lib\site-packages\scipy\stats\_continuous_di
stns.py:708: RuntimeWarning: divide by zero encountered in true divid
  a/(b-1.0),
C:\ProgramData\Anaconda3\lib\site-packages\scipy\stats\ continuous di
stns.py:712: RuntimeWarning: divide by zero encountered in true divid
  a*(a+1.0)/((b-2.0)*(b-1.0)),
C:\ProgramData\Anaconda3\lib\site-packages\scipy\stats\ distn infrast
ructure.py:1063: RuntimeWarning: invalid value encountered in subtrac
 mu2 = mu2p - mu * mu
C:\ProgramData\Anaconda3\lib\site-packages\scipy\stats\ distn infrast
ructure.py:2407: RuntimeWarning: invalid value encountered in double
scalars
  Lhat = muhat - Shat*mu
p value for exponweib = 0.09960496852055273
p value for rayleigh = 0.6757859930739376
p value for fisk = 0.9528344588739082
C:\ProgramData\Anaconda3\lib\site-packages\scipy\stats\ continuous di
stns.py:3373: RuntimeWarning: divide by zero encountered in power
 return 1.0/Cinv * x**(a-1.0) * (1.0-x)**(b-1.0) / (1.0+z*x)**c
p value for gausshyper = 0.30576640871424515
p value for invweibull = 0.8417519047290813
p value for pareto = 0.5336665364053506
p value for alpha = 0.9067330652747674
p value for expon = 0.4587312555913199
p value for hypsecant = 0.9223079906180552
p value for mielke = 0.47566663473773685
p value for loggamma = 0.0037722908093278493
C:\ProgramData\Anaconda3\lib\site-packages\scipy\stats\ distn infrast
ructure.py:1702: RuntimeWarning: divide by zero encountered in log
  return log(self. pdf(x, *args))
```

```
p value for rdist = 0.0
p value for rice = 0.9112020080835465
Best fitting distribution: gumbel 1
Best p value: 0.9611650805916115
Parameters for the best fit: {'loc': 0.6085684047258331, 'scale': 0.0
42804155481658675}
Columm Name: 1
p value for gamma = 0.8889958053792573
p value for gumbel 1 = 0.9646057727711407
p value for cauchy = 0.8261402488613532
p value for dgamma = 0.9029286229445405
p value for beta = 0.42576280633747704
p value for betaprime = 0.8990403693904233
p value for exponweib = 0.14434269055250448
p value for rayleigh = 0.6539560891521108
p value for fisk = 0.9763835373511555
p value for gausshyper = 0.4257544581462159
p value for invweibull = 0.8033963410294281
p value for pareto = 0.43577568017068163
p value for alpha = 0.8662969549571008
p value for expon = 0.438748236767811
p value for hypsecant = 0.9617653431217729
p value for mielke = 0.9338345346805417
p value for loggamma = 0.0037722908093278493
p value for rdist = 0.0
p value for rice = 0.8828955905498191
Best fitting distribution: fisk
Best p value: 0.9763835373511555
Parameters for the best fit: {'c': 110700791.6736241, 'loc': -267925
2.0299123884, 'scale': 2679252.5025851782}
Columm Name: 2
p value for gamma = 0.8880133797117553
p value for gumbel 1 = 0.9603542298049117
p value for cauchy = 0.8503807156937999
p value for dgamma = 0.925443406240686
p value for beta = 0.4257580548841562
p value for betaprime = 0.9055074478771753
p value for exponweib = 0.018042221288103823
p value for rayleigh = 0.6534853437425535
p value for fisk = 0.9853322716409895
p value for gausshyper = 0.32739697804479817
p value for invweibull = 0.6862142836462212
p value for pareto = 0.5191456709040805
p value for alpha = 0.877983073622411
p value for expon = 0.43608645826686726
p value for hypsecant = 0.9685694883456961
p value for mielke = 0.458096562321279
p value for loggamma = 0.0037722908093278493
p value for rdist = 0.0
p value for rice = 0.8789205538846989
Best fitting distribution: fisk
Best p value: 0.9853322716409895
Parameters for the best fit: {'c': 489772.7331588231, 'loc': -10700.8
54448774731, 'scale': 10701.291971158724}
Columm Name : 3
p value for gamma = 0.8646588801686683
```

```
p value for gumbel l = 0.9594013468474849
p value for cauchy = 0.8572999478325235
p value for dgamma = 0.9334887453165497
p value for beta = 0.4257627549572284
p value for betaprime = 0.9051923058931672
p value for exponweib = 0.021779940761754053
p value for rayleigh = 0.6402162044840866
p value for fisk = 0.9780979288657342
p value for gausshyper = 0.3470643413439783
p value for invweibull = 0.7158332576038476
p value for pareto = 0.3931039060807708
p value for alpha = 0.8661149486735855
p value for expon = 0.4246686745275836
p value for hypsecant = 0.9698762755260467
p value for mielke = 0.935808156047545
p value for loggamma = 0.0037722908093278493
p value for rdist = 0.0
p value for rice = 0.8605570869653416
Best fitting distribution: fisk
Best p value: 0.9780979288657342
Parameters for the best fit: {'c': 116592818.89739853, 'loc': -246097
1.9200478606, 'scale': 2460972.3582348386}
Columm Name: 4
p value for gamma = 0.8965748044479315
p value for gumbel 1 = 0.9626779479601569
p value for cauchy = 0.8394204068060477
p value for dgamma = 0.915231968556558
p value for beta = 0.4257613743918177
p value for betaprime = 0.8066199059659821
p value for exponweib = 0.11344321021270526
p value for rayleigh = 0.6543915959226873
p value for fisk = 0.986143784521361
p value for gausshyper = 0.3906556726115891
p value for invweibull = 0.8035296188722569
p value for pareto = 0.4312838610891643
p value for alpha = 0.8755954409799727
p value for expon = 0.43891407443899394
p value for hypsecant = 0.9653808682887519
p value for mielke = 0.517711153776423
p value for loggamma = 0.0037722908093278493
p value for rdist = 0.0
p value for rice = 0.8832069624216988
Best fitting distribution: fisk
Best p value: 0.986143784521361
Parameters for the best fit: {'c': 89049207.38371027, 'loc': -198658
3.0182634608, 'scale': 1986583.4736009042}
Columm Name: 5
p value for gamma = 0.8897459584800032
p value for gumbel 1 = 0.970927442906684
p value for cauchy = 0.7117286422697515
p value for dgamma = 0.8579798425377843
p value for beta = 0.4257809008556552
p value for betaprime = 0.9230155289172822
p value for exponweib = 0.0019271563280967017
p value for rayleigh = 0.6630777639028033
p value for fisk = 0.9758261422843311
```

```
p value for gausshyper = 0.42575445814207347
p value for invweibull = 0.8038553334747851
p value for pareto = 0.4695851665864335
p value for alpha = 0.8960460193519899
p value for expon = 0.4463011938337734
p value for hypsecant = 0.9486089600196449
p value for mielke = 0.48699425897357856
p value for loggamma = 0.0037722908093278493
p value for rdist = 0.0
p value for rice = 0.8940037370173213
Best fitting distribution: fisk
Best p value: 0.9758261422843311
Parameters for the best fit: {'c': 129895838.77416685, 'loc': -348898
6.76553393, 'scale': 3488987.276380528}
Column Name: 6
p value for gamma = 0.8980711629535092
p value for gumbel 1 = 0.9981493181130431
p value for cauchy = 0.9695410392634496
p value for dgamma = 0.9687455462436659
p value for beta = 0.996255197908629
p value for betaprime = 0.8546792905999896
p value for exponweib = 0.08578575673502599
p value for rayleigh = 0.6593123351515688
p value for fisk = 0.9831150580280652
p value for gausshyper = 0.8185259288766672
p value for invweibull = 0.8004204115288965
p value for pareto = 0.5103204911545219
p value for alpha = 0.8692031022654653
p value for expon = 0.4378665272165728
p value for hypsecant = 0.991131412052655
p value for mielke = 0.9998358673660042
p value for loggamma = 4.2866941015089106e-05
p value for rdist = 0.0
C:\ProgramData\Anaconda3\lib\site-packages\scipy\stats\ continuous di
stns.py:1608: RuntimeWarning: invalid value encountered in add
  negxc + sc.xlogy(c - 1.0, x))
```

```
p value for exponweib = 0.03883655304054355
p value for rayleigh = 0.6362219194693021
p value for fisk = 0.81077888034992
p value for gausshyper = 0.06558641975271512
p value for invweibull = 0.8432989693608792
p value for pareto = 0.4909984342470688
p value for alpha = 0.6187465093875405
p value for expon = 0.46038765914758417
p value for hypsecant = 0.8010978605201914
p value for mielke = 0.08650095941200725
p value for loggamma = 0.06558641975308642
p value for rdist = 0.0
p value for rice = 0.6150327026762274
Best fitting distribution: invweibull
Best p value: 0.8432989693608792
Parameters for the best fit: {'c': 89762340.98886724, 'loc': -641827
1.597604012, 'scale': 6418272.308923408}
Columm Name: 8
p value for gamma = 0.8909274136772382
p value for gumbel_1 = 0.5668489340967714
p value for cauchy = 0.8089051243416464
p value for dgamma = 0.4257526467691534
p value for beta = 0.2072037795466098
p value for betaprime = 0.902588161776341
p value for exponweib = 0.30383723296705595
p value for rayleigh = 0.7341108707671156
p value for fisk = 0.9071054886509802
p value for gausshyper = 0.7417524962010064
p value for invweibull = 0.8143495044364858
p value for pareto = 0.44999428134931413
p value for alpha = 0.8976045948696798
p value for expon = 0.44702201335536357
p value for hypsecant = 0.9049309439911588
p value for mielke = 0.03779365280092401
p value for loggamma = 0.8813912827002307
p value for rdist = 0.0
p value for rice = 0.8950602943009982
Best fitting distribution: fisk
Best p value: 0.9071054886509802
Parameters for the best fit: {'c': 24349073.45796358, 'loc': -868246.
0790497053, 'scale': 868246.9655063269}
Columm Name: 9
p value for gamma = 0.8951485153215494
p value for gumbel 1 = 0.5616206928215003
p value for cauchy = 0.7059692741400958
p value for dgamma = 0.4257544567064905
p value for beta = 0.27331963201966203
p value for betaprime = 0.8789583370699603
p value for exponweib = 0.22512866129595388
p value for rayleigh = 0.713728862407169
p value for fisk = 0.8925500777526092
C:\ProgramData\Anaconda3\lib\site-packages\scipy\stats\ continuous di
stns.py:547: RuntimeWarning: invalid value encountered in sqrt
  sk = 2*(b-a)*np.sqrt(a + b + 1) / (a + b + 2) / np.sqrt(a*b)
```

```
p value for beta = 0.42575445968738856
p value for betaprime = 0.9340419420995283
p value for exponweib = 0.1912368964165128
p value for rayleigh = 0.686326276822022
p value for fisk = 0.9864105748028513
p value for gausshyper = 0.42575445815486407
p value for invweibull = 0.8237504309089143
p value for pareto = 0.4552939665002624
p value for alpha = 0.9020986421326999
p value for expon = 0.4531596049126275
p value for hypsecant = 0.994839115540973
p value for mielke = 0.6286174246263803
p value for loggamma = 0.0037722908093278493
p value for rdist = 0.0
p value for rice = 0.9050530696799255
Best fitting distribution: hypsecant
Best p value: 0.994839115540973
Parameters for the best fit: {'loc': 0.8937249916078858, 'scale': 0.0
49857587343792586}
Columm Name: 11
p value for gamma = 0.6303708391173221
p value for gumbel 1 = 0.47652857952026006
p value for cauchy = 0.06644746581252656
p value for dgamma = 0.44063818285977574
p value for beta = 0.06563832891444513
p value for betaprime = 0.626898464523127
p value for exponweib = 0.09450109823857221
p value for rayleigh = 0.6459534776456458
p value for fisk = 0.8289207231424871
p value for gausshyper = 0.06558641975240037
p value for invweibull = 0.7216347757775902
p value for pareto = 0.47739242750312594
p value for alpha = 0.6400028113061278
p value for expon = 0.4583372179696159
p value for hypsecant = 0.8010501963083594
p value for mielke = 0.09747005894242201
p value for loggamma = 0.06558641975308642
p value for rdist = 0.0
p value for rice = 0.6230603972351948
Best fitting distribution: fisk
Best p value: 0.8289207231424871
Parameters for the best fit: {'c': 25622.28074224032, 'loc': -1046.21
63111149446, 'scale': 1047.100475108277}
Columm Name: 12
p value for gamma = 0.9000339397648278
p value for gumbel 1 = 0.986932609089354
p value for cauchy = 0.8957499243633867
p value for dgamma = 0.9195317886793581
p value for beta = 0.8940135607369734
p value for betaprime = 0.9287012530031191
p value for exponweib = 0.04355403087344065
p value for rayleigh = 0.6879614830362372
p value for fisk = 0.9857300781258278
p value for gausshyper = 0.5054685602639493
p value for invweibull = 0.8389559984013213
p value for pareto = 0.441526390547176
```

```
p value for alpha = 0.8957920729322958
p value for expon = 0.45404035313855945
p value for hypsecant = 0.9906679185278626
p value for mielke = 0.027657469673356166
p value for loggamma = 0.9773037695743986
p value for rdist = 0.0
p value for rice = 0.9063696546221549
Best fitting distribution: hypsecant
Best p value: 0.9906679185278626
Parameters for the best fit: {'loc': 0.9085276840337329, 'scale': 0.0
4491738502602223}
Columm Name: 13
p value for gamma = 0.67254065485954
p value for gumbel 1 = 0.4784651973451519
p value for cauchy = 0.0666273244413018
p value for dgamma = 0.44015264573054164
p value for beta = 0.06563459245560707
p value for betaprime = 0.6125997822792638
p value for exponweib = 0.2123716410391767
p value for rayleigh = 0.6456940664506213
p value for fisk = 0.8146419010081765
p value for gausshyper = 0.06558641975290405
p value for invweibull = 0.731514735668143
p value for pareto = 0.4332775007958757
p value for alpha = 0.6213550165874666
p value for expon = 0.4638525796760709
p value for hypsecant = 0.8005592515132045
p value for mielke = 0.1482351006331736
p value for loggamma = 0.06558641975308642
p value for rdist = 0.0
p value for rice = 0.6223209184066696
Best fitting distribution: fisk
Best p value: 0.8146419010081765
Parameters for the best fit: {'c': 85052737.61507161, 'loc': -343575
0.954842735, 'scale': 3435751.8014597762}
Columm Name: 14
p value for gamma = 0.6206817462694757
p value for gumbel 1 = 0.47880227739560177
p value for cauchy = 0.0672871386969308
p value for dgamma = 0.4403974802933155
p value for beta = 0.06563889648993398
p value for betaprime = 0.6858479000485802
p value for exponweib = 0.0160556769080774
p value for rayleigh = 0.6471355258324951
p value for fisk = 0.8155182840071702
p value for gausshyper = 0.06558641975238105
p value for invweibull = 0.8250735954059218
p value for pareto = 0.44703962550681037
p value for alpha = 0.6169213128999123
p value for expon = 0.4611413063265274
p value for hypsecant = 0.800325282066208
p value for mielke = 0.06751804375302277
p value for loggamma = 0.06558641975308642
p value for rdist = 0.0
p value for rice = 0.6226851101537889
Best fitting distribution: invweibull
```

```
Best p value: 0.8250735954059218
Parameters for the best fit: {'c': 13054.131467397729, 'loc': -897.43
35864004695, 'scale': 898.1653702212532}
Column Name: 15
p value for gamma = 0.3762901077683317
p value for gumbel 1 = 0.4835523102628958
p value for cauchy = 0.06643961993005029
p value for dgamma = 0.47166772459391676
p value for beta = 0.0657906271561995
p value for betaprime = 0.6799738276128438
p value for exponweib = 0.05624535993535162
p value for rayleigh = 0.5881505067483151
p value for fisk = 0.8437465799007223
p value for gausshyper = 0.06558641975067768
p value for invweibull = 0.7096558751003664
p value for pareto = 0.2593679484386502
p value for alpha = 0.680366148734665
p value for expon = 0.24238426958265474
p value for hypsecant = 0.7375412878028462
p value for mielke = 0.15430418101226823
p value for loggamma = 0.06558641975308642
p value for rdist = 0.0
p value for rice = 0.0
Best fitting distribution: fisk
Best p value: 0.8437465799007223
Parameters for the best fit: {'c': 115488161.99855241, 'loc': -812132
9.627112514, 'scale': 8121330.414561536}
Columm Name: 16
p value for gamma = 0.2919129621354061
p value for gumbel 1 = 0.7242884012085219
p value for cauchy = 0.36107777114150025
p value for dgamma = 0.5825763310552533
p value for beta = 0.4262741701229195
p value for betaprime = 0.8486320957033308
p value for exponweib = 0.2102342061577885
p value for rayleigh = 0.5492950827260542
p value for fisk = 0.9045892179461279
p value for gausshyper = 0.14429030542277665
p value for invweibull = 0.6331440522769305
p value for pareto = 0.2609791485979628
p value for alpha = 0.8399127050950357
p value for expon = 0.22856676012098903
p value for hypsecant = 0.8551896110840269
p value for mielke = 0.6843350154384503
p value for loggamma = 0.0037722908093278493
p value for rdist = 0.0
p value for rice = 0.0
Best fitting distribution: fisk
Best p value: 0.9045892179461279
Parameters for the best fit: {'c': 67096.92213942789, 'loc': -5107.48
7236737725, 'scale': 5108.28892342235}
Columm Name: 17
p value for gamma = 0.019772857946657573
p value for gumbel 1 = 0.9004192015853957
p value for cauchy = 0.7279729407390465
p value for dgamma = 0.8874087117014774
```

```
p value for beta = 0.6756769142638492
p value for betaprime = 0.9150416640420204
p value for exponweib = 0.06691649705021503
p value for rayleigh = 0.47726793222145436
p value for fisk = 0.974231510527606
p value for gausshyper = 0.13159242251700254
p value for invweibull = 0.6541472070216855
p value for pareto = 0.20352211747404736
p value for alpha = 0.9077311275010344
p value for expon = 0.2029074493410869
p value for hypsecant = 0.9609063276729631
p value for mielke = 0.9848303581998389
p value for loggamma = 4.2866941015089106e-05
p value for rdist = 0.0
p value for rice = 0.0
Best fitting distribution: mielke
Best p value: 0.9848303581998389
Parameters for the best fit: {'k': 73326215.23085016, 's': 171141943
9.8636742, 'loc': -7400304.56267521, 'scale': 7400305.33546778}
Columm Name: 18
p value for gamma = 0.08240545537395466
p value for gumbel 1 = 0.48706557118831884
p value for cauchy = 0.06696354454564168
p value for dgamma = 0.47851016292457665
p value for beta = 0.06581480326322475
p value for betaprime = 0.7028046121273227
p value for exponweib = 0.017275901989393102
p value for rayleigh = 0.5056750049202393
p value for fisk = 0.8338576230706877
p value for gausshyper = 0.06558641974695038
p value for invweibull = 0.573645939526151
p value for pareto = 0.23770983603904716
p value for alpha = 0.6936920266648501
p value for expon = 0.21326094427435005
p value for hypsecant = 0.7307888334887699
p value for mielke = 0.41078769849771235
p value for loggamma = 0.06558641975308642
p value for rdist = 0.0
p value for rice = 0.0
Best fitting distribution: fisk
Best p value: 0.8338576230706877
Parameters for the best fit: {'c': 294993556.1385083, 'loc': -905152
8.952159427, 'scale': 9051529.67594156}
Columm Name: 19
p value for gamma = 0.9516363575303212
p value for gumbel 1 = 0.953853831982619
p value for cauchy = 0.9888000151876468
p value for dgamma = 0.9376793491764674
p value for beta = 0.9770414499693317
p value for betaprime = 0.958820968010875
p value for exponweib = 0.057868731964175586
p value for rayleigh = 0.940404850100629
p value for fisk = 0.28887485288320547
p value for gausshyper = 0.0392041605139932
p value for invweibull = 0.9718769002363463
p value for pareto = 0.9466782426944375
```

```
p value for alpha = 0.9521724839190224
p value for expon = 0.9470509015881015
p value for hypsecant = 0.9623269532515218
p value for mielke = 0.9663380662901748
p value for loggamma = 0.9531845732660127
p value for rdist = 0.9952823413036828
p value for rice = 0.9388879901589855
Best fitting distribution: rdist
Best p value: 0.9952823413036828
Parameters for the best fit: {'c': 1.0609993438745944, 'loc': 0.96465
94345073922, 'scale': 0.03891703450739226}
Columm Name: 20
p value for gamma = 0.008100258685190079
p value for gumbel 1 = 0.18311500709503842
p value for cauchy = 0.0677097913134959
p value for dgamma = 0.06558645565109904
p value for beta = 0.31653555007241735
p value for betaprime = 0.287260453320707
p value for exponweib = 0.013147581956943096
p value for rayleigh = 0.22954751123061612
p value for fisk = 0.4050575975137472
p value for gausshyper = 0.003778954425048489
p value for invweibull = 0.36996067841006147
p value for pareto = 0.11970590838192162
p value for alpha = 0.26116644583157766
p value for expon = 0.11810363540671524
p value for hypsecant = 0.32089554628644035
p value for mielke = 0.13929221701829408
p value for loggamma = 0.0037913779475018975
p value for rdist = 0.0
p value for rice = 0.0
Best fitting distribution: fisk
Best p value: 0.4050575975137472
Parameters for the best fit: {'c': 341675704.2338467, 'loc': -150853
4.8998198714, 'scale': 1508535.8968744436}
Columm Name: 21
p value for gamma = 0.5500989648653845
p value for gumbel 1 = 0.4836560296376879
p value for cauchy = 0.14448092094878107
p value for dgamma = 0.48684156078535634
p value for beta = 0.4259367161814764
p value for betaprime = 0.5395174190829946
p value for exponweib = 0.02373109072598405
p value for rayleigh = 0.5700710901669934
p value for fisk = 0.6964541271509157
p value for gausshyper = 0.09657091802714728
p value for invweibull = 0.6998147866412076
p value for pareto = 0.5756244624394926
p value for alpha = 0.5464521333791471
p value for expon = 0.5816161203604638
p value for hypsecant = 0.8419260444022465
p value for mielke = 0.12758783491252562
p value for loggamma = 0.0037722908093278493
p value for rdist = 0.0
p value for rice = 0.5586562416572148
Best fitting distribution: hypsecant
```

```
Best p value: 0.8419260444022465
Parameters for the best fit: {'loc': 0.9832313307890309, 'scale': 0.0
18033385915142468}
Columm Name : 22
p value for gamma = 0.9495739946393842
p value for gumbel 1 = 0.655404848825679
p value for cauchy = 0.917781871334807
p value for dgamma = 0.4258475165907629
p value for beta = 0.19517346652265957
p value for betaprime = 0.9376465814834966
p value for exponweib = 0.0476178667203046
p value for rayleigh = 0.8208938196368079
p value for fisk = 0.9160532591991455
p value for gausshyper = 0.8851016266536179
p value for invweibull = 0.8715110297563478
p value for pareto = 0.2981828931909373
p value for alpha = 0.9475405143362311
p value for expon = 0.3123403992562756
p value for hypsecant = 0.9171445549717535
p value for mielke = 0.26191951270452685
p value for loggamma = 0.8692540949219563
p value for rdist = 0.0
p value for rice = 0.9497100431378136
Best fitting distribution: rice
Best p value: 0.9497100431378136
Parameters for the best fit: {'b': 1.943763232844457, 'loc': 0.809480
4453402771, 'scale': 0.04938076437684877}
Columm Name: 23
p value for gamma = 0.9424008887894284
p value for gumbel 1 = 0.9387185867241562
p value for cauchy = 0.9770143223733181
p value for dgamma = 0.9961169634109586
p value for beta = 0.42575446119808
p value for betaprime = 0.9459986495638795
p value for exponweib = 0.0311407553304246
p value for rayleigh = 0.724291674513198
p value for fisk = 0.9959848159529379
p value for gausshyper = 0.42575445815478546
p value for invweibull = 0.8724804774158588
p value for pareto = 0.3929785009162604
p value for alpha = 0.9386427609716709
p value for expon = 0.37884648563088963
p value for hypsecant = 0.9941053555538182
p value for mielke = 0.8145674189358512
p value for loggamma = 0.0037722908093278493
p value for rdist = 0.0
p value for rice = 0.9400473552026078
Best fitting distribution: dgamma
Best p value: 0.9961169634109586
Parameters for the best fit: {'a': 0.9150410513721037, 'loc': 0.75930
23255813959, 'scale': 0.05044580639008252}
[['gumbel 1', {'loc': 0.6085684047258331, 'scale': 0.0428041554816586
75}],
 ['fisk',
  {'c': 110700791.6736241,
```

```
'loc': -2679252.0299123884,
   'scale': 2679252.5025851782}],
 ['fisk',
  {'c': 489772.7331588231,
   'loc': -10700.854448774731,
   'scale': 10701.291971158724}],
 ['fisk',
  {'c': 116592818.89739853,
   'loc': -2460971.9200478606,
   'scale': 2460972.3582348386}],
 ['fisk',
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   'loc': -1986583.0182634608,
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   'loc': -3488986.76553393,
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 ['mielke',
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   'loc': -3921399.169850569,
   's': 728375815.5223036,
   'scale': 3921399.896689184}],
 ['invweibull',
  {'c': 89762340.98886724,
   'loc': -6418271.597604012,
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 ['fisk',
  {'c': 24349073.45796358,
   'loc': -868246.0790497053,
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 ['hypsecant', {'loc': 0.8778802262868111, 'scale': 0.041483206783774
65}],
 ['hypsecant', {'loc': 0.8937249916078858, 'scale': 0.049857587343792
586}],
 ['fisk',
  {'c': 25622.28074224032,
   'loc': -1046.2163111149446,
   'scale': 1047.100475108277}],
 ['hypsecant', {'loc': 0.9085276840337329, 'scale': 0.044917385026022
23}],
 ['fisk',
  {'c': 85052737.61507161,
   'loc': -3435750.954842735,
   'scale': 3435751.8014597762}],
 ['invweibull',
  {'c': 13054.131467397729,
   'loc': -897.4335864004695,
   'scale': 898.1653702212532}],
 ['fisk',
  {'c': 115488161.99855241,
   'loc': -8121329.627112514,
   'scale': 8121330.414561536}],
 ['fisk',
  {'c': 67096.92213942789,
   'loc': -5107.487236737725,
```

```
'scale': 5108.28892342235}],
         ['mielke',
          {'k': 73326215.23085016,
           'loc': -7400304.56267521,
           's': 1711419439.8636742,
           'scale': 7400305.33546778}],
         ['fisk',
          {'c': 294993556.1385083,
           'loc': -9051528.952159427,
           'scale': 9051529.67594156}],
         ['rdist',
          {'c': 1.0609993438745944,
           'loc': 0.9646594345073922,
           'scale': 0.03891703450739226}],
         ['fisk',
          {'c': 341675704.2338467,
           'loc': -1508534.8998198714,
           'scale': 1508535.8968744436}],
         ['hypsecant', {'loc': 0.9832313307890309, 'scale': 0.018033385915142
        468}],
         ['rice',
          {'b': 1.943763232844457,
           'loc': 0.8094804453402771,
           'scale': 0.04938076437684877}],
In [6]: dict probability distrs = { "gamma": st.gamma, "gumbel l": st.gumbel l,
        "cauchy": st.cauchy, "dgamma": st.dgamma,
                                    "beta": st.beta, "betaprime": st.betaprime,
        "exponweib": st.exponweib, "rayleigh": st.rayleigh,
                                    "fisk": st.fisk, "gausshyper": st.gausshype
        r, "invweibull": st.invweibull, "pareto": st.pareto,
                                    "alpha": st.alpha, "expon": st.expon, "hypse
        cant": st.hypsecant, "mielke": st.mielke,
                                   "loggamma": st.loggamma, "rdist": st.rdist,
        "rice": st.rice }
In [7]: example curves = df example curves.values.tolist()
        ts example curves = to time series dataset(example curves)
        #pprint.pprint(ts example curves)
```

[0 rows x 28 columns]

- 171 0.7647251331973163 18.35340319673559 0.24503839754008055 0.961931 004890237
- $3323 \quad 0.7643839578333489 \quad 18.34521498800037 \quad 0.24547113782050675 \quad 0.95460 \\ 63977452295$
- 3563 0.7688067637255614 18.451362329413477 0.24813106456230546 0.9656 95644938727
- 4503 0.765315690300572 18.367576567213728 0.24941423267433088 0.95759 25135551389
- 4656 0.765117687890543 18.362824509373034 0.2465874505082063 0.950532 602590968
- 303 0.7638784961744066 18.33308390818576 0.23952572194898983 0.959238 945217764
- 1338 0.7636822787411582 18.328374689787797 0.24931849291311164 0.9608 439128899408
- 2178 0.7644288616935668 18.346292680645604 0.24485351528679425 0.9586 88497511137
- 930 0.7625874552448444 18.302098925876262 0.2495956201062087 0.952529 7815128697
- 1528 0.7665429814088554 18.397031553812532 0.24951533093937722 0.9594 38828470824
- 1975 0.7627562723310513 18.30615053594523 0.246796913882674 0.9597233 601560198
- 2287 0.7635390850453465 18.324938041088316 0.24536118350853603 0.9683 438606387573
- 3971 0.7641261700839537 18.339028082014885 0.23196229888748496 0.9662 829522957982
- 562 0.7679573461710194 18.430976308104466 0.24090494728437123 0.95596 13347979116
- 4225 0.7645447944666002 18.349075067198406 0.24741318068746676 0.9530 021427690418
- 2596 0.766774974340985 18.40259938418364 0.23757411804463513 0.959454 3074079265
- 4091 0.7687534210134895 18.450082104323748 0.24806832111244398 0.9574 828187183869
- 1743 0.7646185735020942 18.350845764050263 0.2492214675928359 0.95629 40913260015
- 671 0.7629166230037233 18.30999895208936 0.2456570931394796 0.9611989 573514303
- 1232 0.7627742357374949 18.306581657699876 0.24759312590266563 0.9612 802669225594
- 3992 0.7645138801278767 18.34833312306904 0.23946324325089557 0.96677 06943315902
- 683 0.7724547856448182 18.538914855475635 0.24375775634485272 0.96252 65340767684
- 2204 0.7630014296179811 18.312034310831546 0.2498586534397405 0.97160 69227668427
- 3421 0.7626335124546738 18.303204298912167 0.24985713485508393 0.9640 309536101712
- 4669 0.7657127801281483 18.377106723075556 0.2358868906109151 0.97005 43312036126

In [10]: print(df_curves)

	0	1	2	3	4	5	
0	0.610331	0.434236	0.449072	0.401362	0.469460	0.527173	0.721
520 1	0.584646	0.446702	0.425810	0.459555	0.451049	0.591894	0.708
186	0.601119	0.486388	0.416625	0.486396	0.474938	0.542921	0.613
405 3 438	0.631015	0.481942	0.445273	0.430063	0.459355	0.515438	0.690
4	0.597480	0.468423	0.495378	0.478195	0.481154	0.464275	0.686
589 5	0.569603	0.464617	0.444821	0.425164	0.471543	0.528657	0.700
729 6 045	0.582364	0.488758	0.444639	0.411429	0.432149	0.587136	0.750
7 855	0.617605	0.498322	0.432600	0.459844	0.511347	0.508999	0.726
8 504	0.565926	0.485179	0.439380	0.405086	0.515203	0.525995	0.716
9 293	0.551098	0.507204	0.489339	0.437384	0.461882	0.560855	0.686
10 671	0.575701	0.505688	0.479513	0.435272	0.493991	0.500583	0.668
11 188	0.601050	0.461377	0.428182	0.426886	0.446890	0.503203	0.701
12 435	0.567889	0.475363	0.469553	0.459329	0.464381	0.507080	0.706
13 048	0.606832	0.558500	0.446838	0.425723	0.452666	0.489967	0.677
14 581	0.608089	0.456735	0.426914	0.469663	0.463503	0.484841	0.681
15 828	0.593597	0.512707	0.452895	0.431816	0.472401	0.549037	0.692
16 774	0.579149	0.479544	0.462354	0.448638	0.529496	0.525509	0.710
17 509	0.621202	0.517476	0.395390	0.483414	0.523765	0.511839	0.704
18 869	0.576396	0.454978	0.464117	0.483288	0.501596	0.562533	0.667
19 126	0.550749	0.442094	0.408348	0.464953	0.438253	0.587730	0.719
20 041	0.583954	0.487172	0.466046	0.449141	0.512082	0.586618	0.700
21 889	0.582889	0.519084	0.445525	0.446502	0.472892	0.480493	0.693
22 204	0.595415	0.468229	0.486110	0.407924	0.476947	0.528138	0.736
23 191	0.573570	0.499195	0.437844	0.448753	0.476909	0.569435	0.716
24 049	0.590578	0.495606	0.457482	0.511778	0.466572	0.523478	0.719
515	7	8	9		18	19	20
21 0	0.805128		0.854495	0.73	0580 0.92		
	-						

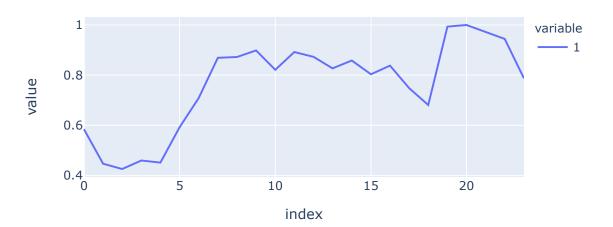
1.000000						
1 0.868968 0.973175	0.872311	0.898259	• • •	0.680803	0.993300	1.000000
2 0.787211 0.979745	0.957635	0.878689		0.735049	1.000000	0.993491
3 0.696887	0.843409	0.861639		0.771561	0.940681	1.000000
0.973746 4 0.812116	0.775915	0.888854		0.679053	0.961869	1.000000
0.952062 5 0.712695	0.808513	0.869409		0.755403	0.962396	1.000000
0.990879 6 0.810974	0.934806	0.891414		0.719578	0.974938	1.000000
0.993948 7 0.852907	0.904960	0.872153		0.786658	1.000000	0.998248
0.994051 8 0.807198	0.865226	0.855095		0.642927	0.966234	0.998750
1.000000 9 0.818304	0.890324	0.872878		0.719487	1.000000	0.991797
0.994524 10 0.865534	0.897513	0.931538		0.753769	0.981755	1.000000
0.955048 11 0.828686	0.926019	0.892286		0.713970	1.000000	0.995353
0.971315 12 0.810038	0.852903	0.908589		0.703210	1.000000	0.995361
0.976136 13 0.784099	0.937545	0.824590		0.690498	0.997580	0.994436
1.000000 14 0.757003	0.903793	0.885075		0.711228	0.932500	0.993643
1.000000						
15 0.798460 0.992387	0.865597	0.932701	•••	0.786419	1.000000	0.985692
16 0.800766 1.000000	0.870810	0.885892	• • •	0.749812	0.964640	0.990651
17 0.847926 0.972218	0.925868	0.932277	• • •	0.708537	0.976736	1.000000
18 0.726720 1.000000	0.951390	0.863404	• • •	0.722370	0.963382	0.995184
19 0.781916 0.956537	0.848816	0.857951	• • •	0.729142	0.989391	1.000000
20 0.795496	0.909213	0.879520		0.698039	0.954411	0.998974
21 0.806863 0.948558	0.911280	0.902454		0.782325	0.976283	1.000000
22 0.752517	0.907268	0.865346		0.719541	0.991781	1.000000
0.949757 23 0.682673	0.890427	0.878648		0.769428	1.000000	0.991502
0.986843 24 0.783704 1.000000	0.925827	0.887782	•••	0.677566	0.958990	0.990497
22	23	FC		Sum DTW	_avg_dista	nce Avg_co
	0.760741	0.764725	18.3	53403	0.245	038
0.961931 1 0.944064 0.954606	0.787006	0.764384	18.3	45215	0.245	471

2 0.957858 0.965696	0.770301	0.768807	18.451362	0.248131
3 0.894379	0.815266	0.765316	18.367577	0.249414
0.957593 4 0.944624	0.781170	0.765118	18.362825	0.246587
0.950533 5 0.955520	0.744181	0.763878	18.333084	0.239526
0.959239	0 550000	0 860600	10 00000	0 040010
6 0.909428 0.960844	0.758223	0.763682	18.328375	0.249318
7 0.955644	0.772123	0.764429	18.346293	0.244854
0.958688				
8 0.932136	0.795833	0.762587	18.302099	0.249596
0.952530				
9 0.972552	0.746250	0.766543	18.397032	0.249515
0.959439 10 0.993480	0.732835	0.762756	18.306151	0.246797
0.959723	0.732033	0.702730	10.500151	0.240737
11 0.904928	0.775960	0.763539	18.324938	0.245361
0.968344				
12 0.941367	0.775846	0.764126	18.339028	0.231962
0.966283				
13 0.925390	0.759007	0.767957	18.430976	0.240905
0.955961	0 757157	0 764545	10 240075	0 047410
14 0.896448 0.953002	0.757157	0.764545	18.349075	0.247413
15 0.936814	0.777048	0.766775	18.402599	0.237574
0.959454	0.777010	0.700773	10.102099	0.237371
16 0.946515	0.743536	0.768753	18.450082	0.248068
0.957483				
17 0.946179	0.744502	0.764619	18.350846	0.249221
0.956294	0 500040	0 000010	10.00000	0 045655
18 0.932184 0.961199	0.769242	0.762917	18.309999	0.245657
19 0.937225	0 769230	0 762774	18 306582	0.247593
0.961280	0.703230	0.702774	10.300302	0.247333
20 0.987470	0.758447	0.764514	18.348333	0.239463
0.966771				
21 0.921090	0.773489	0.772455	18.538915	0.243758
0.962527				
22 0.923676	0.782096	0.763001	18.312034	0.249859
0.971607 23 0.903781	0.750081	0.762634	18.303204	0.249857
0.964031	0./50001	0.702034	10.303204	0.24900/
	0.770900	0.765713	18.377107	0.235887
0.970054		-		

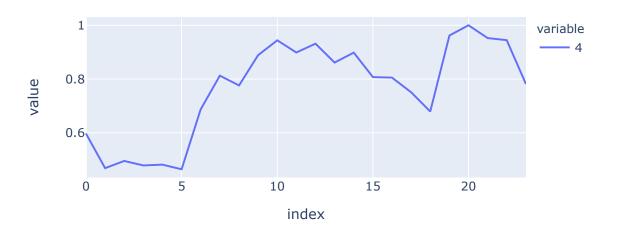
[25 rows x 28 columns]

```
In [11]: for index, row in df_curves.loc[:, "0":"23"].iterrows():
    fig = px.line(row, width=600, height=300)
    fig.show()
```



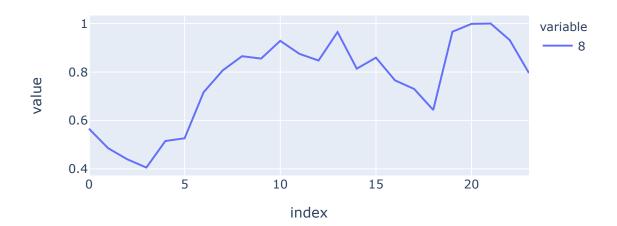




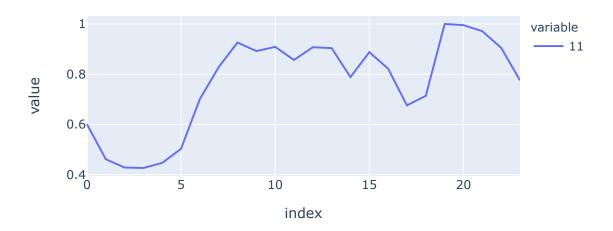




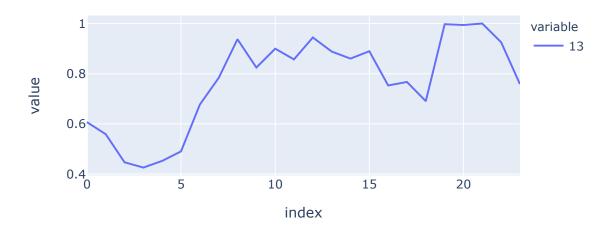


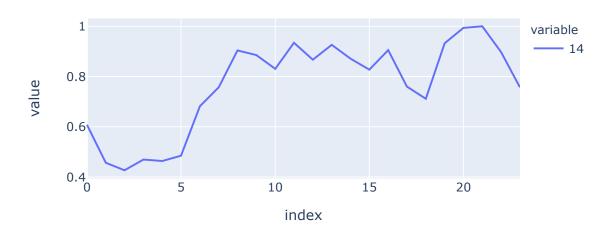






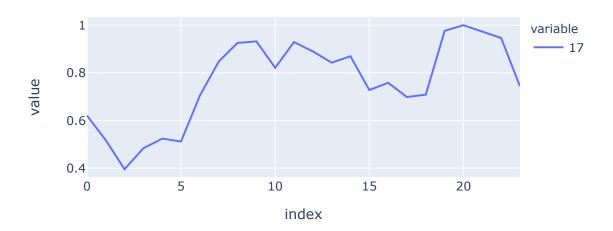
1 variable



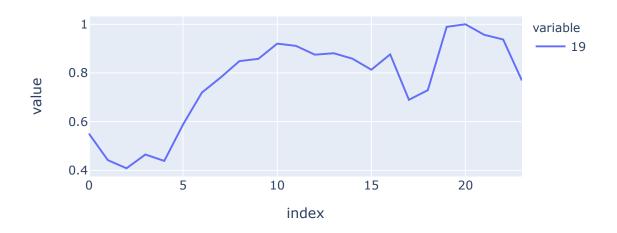


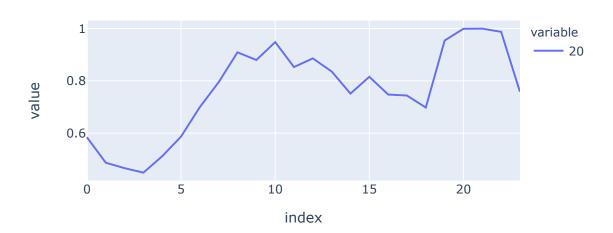


















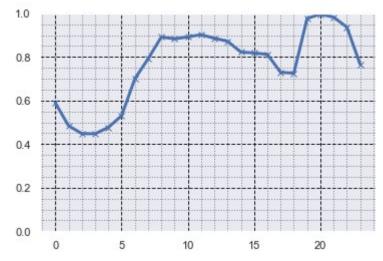


```
In [12]: average optimal curve = df curves.loc[:, "0":"23"].mean(axis=0)
         print(average_optimal_curve, type(average_optimal_curve))
         print("Load Factor: ", )
         0
               0.588730
               0.483821
         1
         2
               0.448402
               0.447502
               0.476817
         5
               0.530553
         6
               0.699839
         7
               0.791792
               0.891977
         9
               0.882838
         10
               0.892188
         11
               0.902291
         12
               0.885800
         13
               0.872095
         14
               0.822360
         15
               0.818517
         16
               0.811809
         17
               0.729538
         18
               0.725478
         19
               0.976659
         20
               0.996382
         21
               0.982437
         22
               0.936843
         23
               0.766819
         dtype: float64 <class 'pandas.core.series.Series'>
         Load Factor:
```

```
In [47]: average_optimal_curve.plot(linewidth=3.0, marker='x', ms=6.5)
    plt.axis((None, None, 0, 1))
    plt.grid(b=True, which='major', color='k', linestyle='--')
    plt.minorticks_on()
    plt.grid(b=True, which='minor', color='grey', linestyle=':')
    plt.show()

final_load_factor = average_optimal_curve.mean() / average_optimal_curv
    e.max()
    print("final_load_factor: ", final_load_factor)

final_energy_sum = average_optimal_curve.sum()
    print("final_energy_sum: ", final_energy_sum)
```



final_load_factor: 0.7678401436126037
final_energy_sum: 18.36148530228425

```
In [ ]:
```