

$$H_0: \theta \in \Theta_0, H_1: \theta \notin \Theta_0$$

$$X_1, \dots, X_n \in \underline{F}(\theta)$$

$$f(X_1, \dots, X_n) = \hat{\theta}$$



$$\alpha = P(\text{принимать } H_1 | H_0)$$

$$\beta = P(\text{принимать } H_0 | H_1)$$

$$s(\theta) = \frac{\partial \log L(\theta)}{\partial \theta}$$

$$J = E \left(\frac{\partial \log L(\theta)}{\partial \theta} \right)^2$$

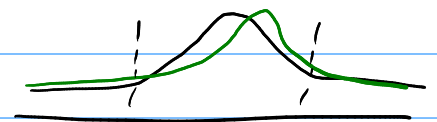
$$J = -E \frac{\partial^2 \log L(\theta)}{\partial \theta^2}$$

$$D(\hat{\theta}) \geq \frac{1}{J(\theta)}$$

$$t = \frac{(\bar{x} - \mu_0)}{(\sigma/\sqrt{n})} \sim t(n-1)$$

$$\frac{\bar{x} - \mu_0}{\sigma/\sqrt{n}} \sim t(n-1)$$

$$\bar{x} \sim N(\mu_0, \frac{\sigma^2}{n}) -$$



$$\frac{\sigma^2}{n} (n-1) \sim \chi^2(n-1) -$$

$$U = \sum_{i=1}^n \sum_{j=1}^m S(x_i, y_j)$$

$$\begin{matrix} x_1, \dots, x_n \\ y_1, \dots, y_m \end{matrix}$$

$$S(x, y) = \begin{cases} 1, & x > y \\ 0.5, & x = y \\ 0, & x < y \end{cases}$$

$$\sqrt{n} = \frac{(\sigma^{-1}\alpha + \sigma^{-1}(1-\beta))(\sigma_x + \sigma_y)}{n D E^2}$$

$$f(x) > a, \quad H_0: \theta > \theta_0, \quad H_1: \theta \leq \theta_0$$

$$P(f(x) > a \mid \theta > \theta_0) = \alpha$$

$$P(f(x) \leq a \mid \theta \leq \theta_0) = \beta$$

CLPED

$$E(\hat{\theta}) = \theta$$

$$\hat{\theta}_{CLP} = \hat{\theta} - \alpha \hat{\theta}_a, \quad E(\hat{\theta}_a) = 0$$

$$D(\hat{\theta}_{CLP}) = D(\hat{\theta}) + D(\hat{\theta}_a) - 2 \text{Cov}(\hat{\theta}, \hat{\theta}_a)$$

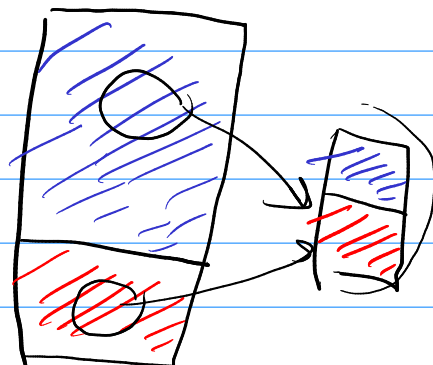
$$D(\hat{\theta}_{CLP}) = D(\hat{\theta}) + \alpha^2 D(\hat{\theta}_a) - 2\alpha \text{Cov}(\hat{\theta}, \hat{\theta}_a)$$

$$2\alpha D(\hat{\theta}_a) - 2\text{Cov}(\hat{\theta}, \hat{\theta}_a) = 0$$
















$$\alpha = \frac{\text{Cov}(\hat{\theta}, \hat{\theta}_a)}{D(\hat{\theta}_a)}$$

$$\hat{\theta}_{CLP} = \hat{\theta} - \frac{\text{Cov}(\hat{\theta}, \hat{\theta}_a)}{D(\hat{\theta}_a)} \cdot \hat{\theta}_a$$

0,2	0,8
180	170



$$\bar{y} = \frac{1}{n} \sum_{k=1}^K \sum_{j=1}^{n_k} y_{kj} ; \bar{y}_{str} = \sum_{k=1}^K \frac{w_k}{n} \bar{y}_k$$

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