Rate Equations

The following kinetic expressions were used:

$$v_{\text{GLT}} = \frac{V_m \left(\text{GLCo} - \frac{\text{GLCi}}{K_{\text{eq}}} \right)}{K_m \left(\frac{\text{GLCi}}{K_m} + \frac{\text{GLCo}}{K_m} + \frac{\text{GLCi} \text{GLCo} K_i}{K_m^2} + 1 \right)}$$
(1)

$$v_{\text{HXK}} = \frac{V_m \left(\text{ATP GLCi} - \frac{\text{ADP G6P}}{K_{\text{eq}}} \right)}{K_{m,\text{glc}} K_{m,\text{atp}} \left(\frac{\text{ADP}}{K_{m,\text{adp}}} + \frac{\text{ATP}}{K_{m,\text{atp}}} + 1 \right) \left(\frac{\text{G6P}}{K_{m,\text{g6p}}} + \frac{\text{GLCi}}{K_{m,\text{glc}}} + \frac{\text{T6P}}{K_{i,\text{t6p}}} + 1 \right)}$$
(2)

$$v_{\text{PGM1}} = \frac{V_m \left(\text{G1P} - \frac{\text{G6P}}{K_{\text{eq}}}\right)}{K_{m,\text{G1P}} \left(\frac{\text{G1P}}{K_{m,\text{G1P}}} + \frac{\text{G6P}}{K_{m,\text{G6P}}} + 1\right)}$$
(3)

$$V_m$$
 F6P G6P UDPGLC

$$v_{\text{TPS1}} = \frac{V_m \,\text{F6P G6P UDPGLC}}{K_{m,\text{G6P}} \,K_{m,\text{UDPGLC}} \left(\frac{\text{G6P}}{K_{m,\text{G6P}}} + 1\right) \left(\frac{\text{PI}}{K_{i,\text{PI}}} + 1\right) \left(\frac{\text{UDPGLC}}{K_{m,\text{UDPGLC}}} + 1\right) \left(\text{F6P} + K_{m,\text{F6P}}\right)}$$
(4)

$$v_{\text{TPS2}} = \frac{V_m \text{ PI T6P}}{\text{PI } (K_{m,\text{T6P}} + \text{T6P}) + K_{i,\text{PI}} K_{m,\text{T6P}}}$$
 (5)

$$v_{\text{NTH1}} = \frac{V_m \text{ TRE}}{K_{m,\text{TRE}} \left(\frac{\text{TRE}}{K_{m,\text{TRE}}} + 1\right)}$$
 (6)

$$v_{\text{PGI}} = \frac{V_m \left(\text{G6P} - \frac{\text{F6P}}{K_{\text{eq}}}\right)}{K_{m,\text{g6p}} \left(\frac{\text{F6P}}{K_{m,\text{f6p}}} + \frac{\text{G6P}}{K_{m,\text{g6p}}} + 1\right)}$$
(7)

$$v_{\rm PFK} = \frac{V_m \, R \, g_R \, {\rm lam}_1 \, {\rm lam}_2}{R^2 + L \, T^2} \tag{8}$$

$$lam_1 = \frac{F6P}{K_{R,F6P}} \tag{9}$$

$$lam_2 = \frac{ATP}{K_{R,ATP}} \tag{10}$$

$$R = \lim_{1 \to \infty} 1 + g_R \lim_{1 \to \infty} 1 + 1 \tag{11}$$

$$T = c_{\text{ATP}} \, \text{lam}_2 + 1 \tag{12}$$

$$L = \frac{L_0 \left(\frac{\text{AMP } c_{i,\text{AMP}}}{K_{\text{AMP}}} + 1\right)^2 \left(\frac{\text{ATP } c_{i,\text{ATP}}}{K_{\text{ATP}}} + 1\right)^2 \left(\frac{\text{F26bP } c_{i,\text{F26bP}}}{K_{\text{F26bP}}} + \frac{\text{FBP } c_{i,\text{FBP}}}{K_{\text{FBP}}} + 1\right)}{\left(\frac{\text{AMP }}{K_{\text{AMP}}} + 1\right)^2 \left(\frac{\text{ATP }}{K_{\text{ATP}}} + 1\right)^2 \left(\frac{\text{F26bP }}{K_{\text{F26bP}}} + \frac{\text{FBP }}{K_{\text{FBP}}} + 1\right)}$$
(13)

$$v_{\text{ALD}} = \frac{V_m \left(\text{FBP} - \frac{\text{DHAP GAP}}{K_{\text{eq}}} \right)}{K_{m,\text{FBP}} \left(\frac{\text{FBP}}{K_{m,\text{FBP}}} + \left(\frac{\text{DHAP}}{K_{m,\text{dhap}}} + 1 \right) \left(\frac{\text{GAP}}{K_{m,\text{gap}}} + 1 \right) \right)}$$
(14)

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$$v_{\text{TPI}} = \frac{V_m \left(\text{DHAP} - \frac{\text{GAP}}{K_{\text{eq}}} \right)}{K_{m,\text{dhap}} \left(\frac{\text{DHAP}}{K_{m,\text{dhap}}} + \frac{\text{GAP}}{K_{m,\text{gap}}} + 1 \right)}$$
(15)

$$v_{\text{GPD}} = \frac{V_m \left(\text{DHAP NADH} - \frac{\text{G3P NAD}}{K_{\text{eq}}} \right)}{K_{m,\text{NADH}} K_{m,\text{DHAP}} \left(\frac{\text{NAD}}{K_{m,\text{NAD}}} + \frac{\text{NADH}}{K_{m,\text{NADH}}} + 1 \right) \left(\frac{\text{DHAP}}{K_{m,\text{DHAP}}} + \frac{\text{G3P}}{K_{m,\text{G3P}}} + 1 \right) \left(\frac{\text{ADP}}{K_{i,\text{ADP}}} + \frac{A^{i}}{K_{i,\text{CMAD}}} \right)}{(16)}$$

$$v_{\text{HOR2}} = \frac{V_m \,\text{G3P}}{K_{m,\text{G3P}} \left(\frac{\text{G3P}}{K_{m,\text{G3P}}} + 1\right) \left(\frac{\text{PI}}{K_{i,\text{PI}}} + 1\right)} \tag{17}$$

$$V_{\text{GLYCt}} = K_{\text{GLYCt}} \text{ (GLYC - GLYCe)}$$
 (18)

$$v_{\text{GAPDH}} = \frac{V_m \left(\text{GAP NAD PI} - \frac{\text{BPG NADH}}{K_{\text{eq}}} \right)}{K_{m,\pi} K_{m,\text{nad}} K_{m,\text{gap}} \left(\left(\frac{\text{BPG}}{K_{m,\text{bpg}}} + 1 \right) \left(\frac{\text{NADH}}{K_{m,\text{nadh}}} + 1 \right) + \left(\frac{\text{GAP}}{K_{m,\text{gap}}} + 1 \right) \left(\frac{\text{NAD}}{K_{m,\text{nad}}} + 1 \right) \left(\frac{1}{K_{m,\text{nadh}}} + 1 \right)} \right)$$
(19)

$$v_{\text{PGK}} = \frac{V_m \text{ (ADP BPG } K_{\text{eq}} - \text{ATP P3G)}}{K_{m,\text{P3G}} K_{m,\text{ATP}} \left(\frac{\text{BPG}}{K_{m,\text{BPG}}} + \frac{\text{P3G}}{K_{m,\text{P3G}}} + 1\right) \left(\frac{\text{ADP}}{K_{m,\text{ADP}}} + \frac{\text{ATP}}{K_{m,\text{ATP}}} + 1\right)}$$
(20)

$$v_{\text{PGM}} = \frac{V_m \left(\text{P3G} - \frac{\text{P2G}}{K_{\text{eq}}} \right)}{K_{m,\text{P3G}} \left(\frac{\text{P2G}}{K_{m,\text{P2G}}} + \frac{\text{P3G}}{K_{m,\text{P3G}}} + 1 \right)}$$
(21)

$$v_{\text{ENO}} = \frac{V_m \left(\text{P2G} - \frac{\text{PEP}}{K_{\text{eq}}} \right)}{K_{m,\text{P2G}} \left(\frac{\text{P2G}}{K_{m,\text{P2G}}} + \frac{\text{PEP}}{K_{m,\text{PEP}}} + 1 \right)}$$
 (22)

$$v_{\text{PYK}} = \frac{V_m \text{ ADP PEP} \left(\frac{\text{PEP}}{K_{m,\text{pep}}} + 1\right)^{\text{hill}}}{K_{m,\text{adp}} K_{m,\text{pep}} \left(\left(\frac{\text{PEP}}{K_{m,\text{pep}}} + 1\right)^{\text{hill}} + L\left(\frac{\frac{\text{ATP}}{K_{i,\text{ATP}}} + 1}{\frac{\text{FBP}}{K_{a,\text{FBP}}} + 1}\right)^{\text{hill}}\right) \left(\frac{\text{ADP}}{K_{m,\text{adp}}} + 1\right) \left(\frac{\text{PEP}}{K_{m,\text{pep}}} + 1\right)}$$
(23)

$$v_{\text{PDC}} = \frac{V_m \left(\frac{\text{PYR}}{K_{m,\text{PYR}}}\right)^{\text{hill}}}{\left(\frac{\text{PYR}}{K_{m,\text{PYR}}}\right)^{\text{hill}} + 1}$$
(24)

$$v_{\text{ADH}} = -\frac{1}{K_{i,\text{NAD}} K_{m,\text{ETOH}} \left(\frac{\text{NAD}}{K_{i,\text{NAD}}} + \frac{\text{NADH}}{K_{i,\text{NADH}}} + \frac{\text{ACE} K_{m,\text{NADH}}}{K_{i,\text{NADH}} K_{m,\text{ACE}}} + \frac{\text{ACE} \text{NADH}}{K_{i,\text{NADH}} K_{m,\text{ACE}}} + \frac{\text{ETOH} K_{m}}{K_{i,\text{NAD}} K_{m}} \right)}$$
(25)

$$V_{\text{ETOHt}} = K_{\text{ETOHt}} \text{ (ETOH - ETOHe)}$$
 (26)

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$$V_{\text{mito}} = \frac{V_m \text{ ADP PI}}{(\text{ADP} + K_{m,\text{ADP}}) (K_{m,\text{PI}} + \text{PI})}$$
(27)

$$V_{\text{ATPase}} = \frac{\text{ATP } K}{\text{ADP}} \tag{28}$$

$$V_{\rm ADK} = K \left(\text{ADP}^2 - \frac{\text{AMP ATP}}{K_{\rm eq}} \right) \tag{29}$$

$$V_{\text{vacPi}} = -K \text{ (PI - PIvac)}$$
 (30)

$$V_{\text{mitoNADH}} = \frac{V_m \,\text{NADH}}{K_m + \text{NADH}}$$
(31)

$$V_{\text{sinkG6P}} = \frac{V_m \,\text{G6P}}{\text{G6P} + K_m} \tag{32}$$

$$V_{\text{sinkF6P}} = \frac{V_m \,\text{F6P}}{\text{F6P} + K_m} \tag{33}$$

$$V_{\text{sinkGAP}} = \frac{V_m \, \text{GAP}}{\text{GAP} + K_m} \tag{34}$$

$$V_{\text{sinkP3G}} = \frac{V_m \,\text{P3G}}{K_m + \text{P3G}} \tag{35}$$

$$V_{\text{sinkPEP}} = \frac{V_m \, \text{PEP}}{K_m + \text{PEP}} \tag{36}$$

$$V_{\rm sinkPYR} = \frac{V_m \, PYR}{K_m + PYR} \tag{37}$$

$$V_{\text{sinkACE}} = \frac{V_m \text{ ACE}}{\text{ACE} + K_m}$$
(38)

Reactions added in this model:

$$v_{\text{ATH}} = \frac{\text{ATH } K_{\text{cat}} \text{ TRE}}{K_{M,\text{TRE}} \left(\frac{\text{TRE}}{K_{M,\text{TRE}}} + 1\right)}$$
(39)

$$v_{\text{AGT1}} = \frac{\text{AGT}_{1} K_{\text{cat}} \left(\text{TRE}_{\text{cyt}} - \frac{\text{TRE}_{\text{ec}}}{K_{\text{eq}}} \right)}{K_{M,\text{TRE}} \left(\frac{\text{TRE}_{\text{ec}}}{K_{M,\text{TRE}}} + \frac{\text{TRE}_{\text{cyt}}}{K_{M,\text{TRE}}} + \frac{\text{UDP}_{\text{GLC}}}{K_{i,\text{UDPglc}}} + 1 \right)}$$
(40)

$$v_{\text{vacuoleT}} = \frac{V_{\text{max}} \left(\text{TRE}_{\text{cyt}} - \frac{\text{TRE}_{\text{vac}}}{K_{\text{eq}}} \right)}{K_{M,\text{TRE}} \left(\frac{\text{TRE}_{\text{vac}}}{K_{M,\text{TRE}}} + \frac{\text{TRE}_{\text{cyt}}}{K_{M,\text{TRE}}} + 1 \right)}$$
(41)

Glycogen synthesis and degradation were directly interpolated from the data, with the addition of a saturation component, to avoid that it become a constraint in the system, especially when fluxes were overall small.

$$v_{\text{glyc,synthesis}} = \frac{v_{\text{glyc,synthesis,interpolated UDP}_{GLC}}{\text{UDP}_{GLC} + 1E^{-4}}$$
(42)

$$v_{\text{glyc,degradation}} = \frac{v_{\text{glyc,degradation,interpolated Glycogen}}}{\text{Glycogen} + 1\text{E}^{-4}}$$
 (43)

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