



Efficient Deobfuscation of Linear Mixed Boolean-Arithmetic Expressions

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- Denuvo provides anti-piracy solutions for video games
- Interested in effective and efficient code obfuscation techniques
- We want small and fast MBAs that cannot be easily broken
 - ▶ Are *linear* MBAs worth using?

- Mixed Boolean-arithmetic expressions (MBAs) are a common ingredient for obfuscation
 - ▶ Hide secret information or code via introduction of exaggerated complexity
- E.g., $x + y$ can be written as

$$2((x \& y) | (\sim x \& \sim y)) - 2(\sim x \& y) + 3((\sim x \& y) | (x \& \sim y)) - 2 \cdot \sim y$$

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- Hard to simplify due to the incompatibility of arithmetic and bitwise operations
- There is a variety of techniques for simplification
 - ▶ pattern matching, neural networks, bit-blasting, stochastic program synthesis ...
- Most existing tools fail on simplifying or even verifying those expressions
- In 2021, *MBA-Blast* and *MBA-Solver* simplify *linear* MBAs within fractions of a second
 - ▶ ... but there are some caveats to be resolved in order to make Liu et al.'s approach powerful in practice

Mixed Boolean-arithmetic expressions

- An MBA mixes bitwise (\equiv logical) and arithmetic operations
- Introduced by Zhou et al. in 2006.
- Hard to simplify:
 - ▶ Arithmetic or logical simplification rules are not compatible
 - ▶ Established tools either concentrate on arithmetic or logical expressions
 - ▶ Most MBA simplifiers are not (yet) powerful enough

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 - ▶ Established tools either concentrate on arithmetic or logical expressions
 - ▶ Most MBA simplifiers are not (yet) powerful enough
- We concentrate on *linear* MBAs: functions $e : (B^n)^t \rightarrow B^n$ of the form

$$e(x_1, \dots, x_t) = \sum_{i \in I} a_i e_i(x_1, \dots, x_t),$$

where $B = \{0, 1\}$, $n, t \in \mathbb{N}$, $I \subset \mathbb{N}$ is an index set, $a_i \in B^n$ are constants and e_i are bitwise expressions of x_1, \dots, x_t for $i \in I$.

Mixed Boolean-arithmetic expressions

- Examples:
 - ▶ $x + (x \& y) - 2 \cdot (x | y) + 42$ is a *linear* MBA
 - ▶ $y \cdot (x \wedge y) - (x \& y)^2 - 1$ is a *polynomial* MBA
 - ▶ $3 \cdot x^y + x + 17$ is *not polynomial*
 - ▶ $5 + (x | 3) - (5 \& y)$ is *not polynomial*
- Methods for generation:
 - ▶ (Iterative) application of known rewriting rules (see, e.g., *LOKI*)
 - ▶ Solution of random linear equation systems (Zhou et al. 2007)
 - ▶ ...
- Zhou et al.: Linear MBAs are equivalent on B^n for any $n \in \mathbb{N}$ if they are equivalent on $B = \{0, 1\}$.
 - ▶ Bitwise expressions can be considered logical expressions.
 - ▶ MBAs with t variables identified by only 2^t (rather than 2^{nt}) values!

The myth of Zhou et al.'s reversed direction

- In more detail, Zhou et al. prove that an MBA $e \equiv 0$ if and only if the vector $Y_a = (a_1, \dots, a_s)^T$ of its coefficients solves a linear equation system $AY = o$, where A is a *truth value matrix* of e 's bitwise expressions.

The myth of Zhou et al.'s reversed direction

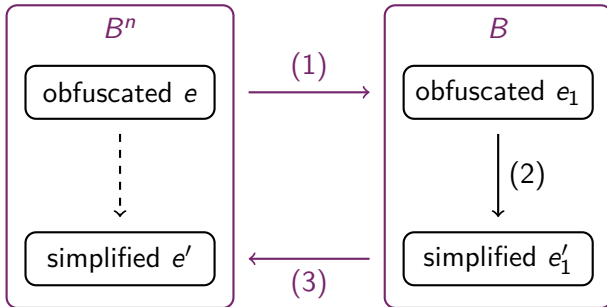
- In more detail, Zhou et al. prove that an MBA $e \equiv 0$ if and only if the vector $Y_a = (a_1, \dots, a_s)^T$ of its coefficients solves a linear equation system $AY = 0$, where A is a *truth value matrix* of e 's bitwise expressions.
- But unfortunately, he formulates the theorem wrongly.

*$A = (v_{i,j})_{2^t \times s}$, be the $\{0,1\}$ -matrix of truth tables over $Z/(2^n)$. Then $e = 0$ if and only if the linear system $AY = 0$ **has a solution** over ring $Z/(2^n)$, where $Y_{s \times 1} = (y_0, \dots, y_{s-1})^T$ is a vector of s variables over $Z/(2^n)$.*

- This might have delayed powerful algebraic simplification tools for years!
- Liu et al. claim to be the first to prove the reverse direction in their MBA-Blast paper in 2021.

MBA-Blast & MBA-Solver

- Very similar simplifiers written in Python.
- Both transform a linear MBA from B^n to B and simplify it there.



- Each bitwise expression (and hence each MBA) with t variables can be written as a linear combination of 2^t base expressions.
 - ▶ E.g., for $t = 2$, $\{1, x, y, x \& y\}$
 - ▶ ... or $\{\sim(x | y), \sim(x | \sim y), x \& \sim y, x \& y\}$
- Simple potential solutions can be found via a lookup table.
 - ▶ E.g., $x + y - (x \& y) \rightarrow x | y$

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- Simple potential solutions can be found via a lookup table.
 - ▶ E.g., $x + y - (x \& y) \rightarrow x | y$
- Main differences:
 - ▶ MBA-Solver transforms whole MBAs while MBA-Blast transforms bitwise expressions and combines the results.
 - ▶ MBA-Solver uses a more complex basis in order to solve equation systems without usage of NumPy.
 - ▶ MBA-Solver is significantly faster.
 - ▶ MBA-Solver misses simple solutions.

SiMBA (*Simple MBA Simplifier*)

- We adapt the approach and resolve the existing tools' main sufferings.
- We follow the following principles:
 - ▶ We use generic code that works for *arbitrary* variable count.
 - ▶ We want to be independent of lookup tables (4 variables: $2^{2^4} = 65\,536$ entries).
 - ▶ We do not use any library such as SymPy or NumPy for simplification or equation system solving.
 - ▶ We find simplest solutions whenever the **simplified** expression has few enough variables.
 - ▶ We validate input expressions.
 - ▶ Our algorithm is invariant to an expression's concrete representation.

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 - ▶ We prove and use a generalization of Zhou et al.'s theorem.
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- We use a **generic** basis for every $t \in \mathbb{N}$:

$$\{1\} \cup \bigcup_{i=1}^t \{x_i\} \cup \bigcup_{\substack{i_1, i_2=1 \\ i_1 < i_2}}^t \{x_{i_1} \& x_{i_2}\} \cup \bigcup_{\substack{i_1, i_2, i_3=1 \\ i_1 < i_2 < i_3}}^t \{x_{i_1} \& x_{i_2} \& x_{i_3}\} \cup \dots \cup \{x_1 \& \dots \& x_t\}$$

- ▶ This gives us a nice truth table s.t. in each iteration of Gaussian elimination there is a row with only one 1.
- ▶ We can generically determine the row in which a specific conjunction is eliminated.

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- ▶ This gives us a nice truth table s.t. in each iteration of Gaussian elimination there is a row with only one 1.
 - ▶ We can generically determine the row in which a specific conjunction is eliminated.
- We find the **simplest** solution (in place of the resulting linear combination of conjunctions) for every input that does not depend on more than 3 variables.

Verification and comparison

- Experiments:
 - ▶ Verification via simplification of MBAs from Matteo Favaro's *NeuReduce* Github repository
 - ▶ Comparison via simplification of MBAs from *MBA-Solver*'s Github repository
 - ▶ Comparison via simplification of self-generated MBAs
 - ▶ Simplification of MBAs encoded via affine functions
- See the MBA-Blast and MBA-Solver papers for a comparison with *Arybo*, *SSPAM* and *Syntia*.

- Verification of SiMBA on the dataset of linear MBAs provided by Matteo Favaro's Github repository:

	Total	Solved	Runtime
2 variables	4 000	4 000	0.00024 s
3 variables	4 560	4 560	0.00069 s
4 variables	441	441	0.00084 s
5 variables	999	999	0.00147 s

Comparison

- Comparison on the dataset of linear MBAs provided by MBA-Solver's Github repository:

	2 variables (551 expr.)	3 variables (350 expr.)	4 variables (107 expr.)
MBA-Blast	0.02501 s	0.06726 s	—
MBA-Solver	0.00047 s	0.00121 s	0.14362 s
MBA-Flatten*	0.01872 s	0.08455 s	0.85104 s
SiMBA	0.00024 s	0.00116 s	0.00257 s

* published in September 2022 by Liu et al.

Comparison

- Comparison on 1 000 self-generated expressions for 5 target functions:

▶ $e_1(x, y) = x + y$

▶ $e_2 = 49\,374$

▶ $e_3(x) = 3\,735\,936\,685\,x + 49\,374$

▶ $e_4(x, y) = 3\,735\,936\,685\,(x \wedge y) + 49\,374$

▶ $e_5(x) = 3\,735\,936\,685 \cdot \sim x$

MBA-Solver

	2 variables	3 variables	4 variables
e_1	0.00074 s	0.00091 s	0.12761 s
e_2	0.00052 s	0.00092 s	0.12352 s
e_3	0.00026 s	0.00150 s	0.12802 s
e_4	0.00041 s	0.00160 s	0.12683 s
e_5	0.00072 s	0.00134 s	0.12871 s

SiMBA

	2 variables	3 variables	4 variables
e_1	0.00019 s	0.00117 s	0.00550 s
e_2	0.00010 s	0.00045 s	0.00528 s
e_3	0.00020 s	0.00109 s	0.00544 s
e_4	0.00024 s	0.00100 s	0.00564 s
e_5	0.00022 s	0.00108 s	0.00543 s

Encoded expressions

- Runtime of SiMBA on 1 000 MBAs with output encoding generated for five expressions:
 - ▶ $e'_i = ae_i + b$ for random $a, b \in B^{64}$
 - ▶ Not supported by MBA-Solver and MBA-Blast

	2 variables	3 variables	4 variables
e'_1	0.00020 s	0.00118 s	0.00484 s
e'_2	0.00010 s	0.00029 s	0.00481 s
e'_3	0.00021 s	0.00125 s	0.00460 s
e'_4	0.00020 s	0.00098 s	0.00516 s
e'_5	0.00015 s	0.00110 s	0.00547 s

Outlook: Nonlinear MBAs

- Possible extension to polynomial and nonpolynomial MBAs via identifying all linear subexpressions of a nonlinear MBA and additional tricks
- Comparison on the datasets of linear, polynomial and nonpolynomial MBAs provided by MBA-Solver's Github repository:

Category	Total	MBA-Solver [*]		MBA-Flatten [*]		SiMBA	
		Solved	Runtime	Solved	Runtime	Solved	Runtime
Linear	1 008	1 008	0.01546 s	1 008	0.12374 s	1 008	0.00250 s
Polynom.	1 008	1 008	0.02271 s	737	0.18124 s	1 008	0.00326 s
Nonpolyn.	899	109	0.07965 s	88	0.22775 s	899	0.00957 s

^{*} MBA-Solver and MBA-Flatten, as available to us, require additional knowledge about the input.

- Zhou et al.'s transformation $B^n \leftrightarrow B$ is a powerful basis for deobfuscation
- Linear MBAs can be broken easily and fast
 - ▶ **Hypothesis:** This is also true for all nonlinear MBAs that can be reduced to linear ones.
 - ▶ However, increasing the number of variables makes it exponentially harder.
- *SiMBA*'s source code is available here: github.com/DenuvoSoftwareSolutions/SiMBA

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THANK YOU!



FAVARO, Matteo:

NeuReduce.

<https://github.com/fvrmatteo/NeuReduce>



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MBA-Solver Code and Dataset.

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