

# Simulating ice nucleation, one molecule at a time, with the ‘DFT microscope’<sup>†</sup>

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Few physical processes are as ubiquitous as the nucleation of water into ice. However, ice nucleation and, in particular, heterogeneously catalyzed nucleation remains poorly understood at the atomic level. Here, we report an initial series of density functional theory (DFT) calculations aimed at putting our understanding of ice nucleation and water clustering at metallic surfaces on a firmer footing. Taking a prototype hydrophobic metal surface, Cu(111), for which scanning tunneling microscopy measurements of water clustering have recently been performed, possible structures of adsorbed clusters comprised of 2–6 H<sub>2</sub>O molecules have been computed. How the water clusters in this size regime differ from those in the gas phase is discussed, as is the nature of their interaction with the substrate.

## 1. Introduction

H<sub>2</sub>O–metal interactions are important in a wide variety of phenomena in materials science, catalysis, corrosion, electrochemistry, and so on. H<sub>2</sub>O–metal interfaces also provide fertile ground for understanding basic physical processes such as ice nucleation and water clustering. In this respect a wide variety of surface science style studies have been performed, focussing on understanding the structures and properties of thin ice films and water overlayers that form on well-defined single-crystal metal surfaces under ultra-high vacuum (UHV) conditions. By now such overlayer systems have been interrogated with almost every available experimental surface science probe as well as a variety of theoretical approaches.<sup>1–3</sup>

Many of the recent studies in this area have focussed on determining the nature and structures of the first wetting layer of H<sub>2</sub>O–ice that may form. Due to the competing influences of H<sub>2</sub>O–metal bonding and H<sub>2</sub>O–H<sub>2</sub>O epitaxial mismatch between the overlayer and the substrate a wide variety of extended overlayer structures have been proposed, such as 2D ice-like overlayers<sup>4–9</sup> quasi-2D overlayers,<sup>10</sup> 1D chains,<sup>11</sup> and mixed H<sub>2</sub>O–OH overlayers.<sup>12–19</sup> Several of these overlayer systems have been examined with a range of complementary experimental and theoretical techniques such as low-energy electron diffraction (LEED), vibrational spectroscopies, photoemission, and density functional theory (DFT) leading to a clear atomic-scale characterisation of their structures.

Much less is known, however, about the structures of small H<sub>2</sub>O clusters that form prior to the creation of the extended overlayers; dimers, trimers, tetramers, *etc.* Although on a few metal surfaces some of the clusters have been reported in infrared

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<sup>†</sup> The HTML version of this article has been enhanced with colour images.

reflection absorption (IRAS) spectroscopy<sup>20–22</sup> and scanning tunnelling microscopy (STM)<sup>3,23–25</sup> studies their internal structure or registry with the substrate remains, in every case, unclear. Moreover, it is not known how the structures and relative energies of the adsorbed clusters differ from the equivalent clusters in the gas phase. It is in this regard that first principles electronic structure theories can make valuable contributions. And, indeed, adsorbed H<sub>2</sub>O monomers and small H<sub>2</sub>O clusters have recently been computed with DFT on a number of close-packed metal surfaces providing predictions as to what structures may form as well as insight and understanding as to why particular structures are favoured over others.<sup>26–34</sup>

The study reported here is in a similar spirit to the previous DFT studies cited above. However, here we examine, for the first time, adsorbed clusters right up to the H<sub>2</sub>O hexamer; dimers, trimers, tetramers, pentamers, and hexamers have all been computed. In addition we examine how the structures and stability of these small H<sub>2</sub>O clusters differ from those in the gas phase, thus shedding light on the ‘catalytic’ role of the Cu(111) substrate in H<sub>2</sub>O cluster formation. We have chosen Cu(111) for this work mainly because recent low temperature STM experiments of H<sub>2</sub>O and D<sub>2</sub>O clustering have been reported on this surface.<sup>35</sup> In addition, Cu(111) is of interest because it is a substrate upon which H<sub>2</sub>O does not normally dissociate and is an hexagonal surface which can, in principle, support an adsorbed H<sub>2</sub>O–ice bilayer with a lattice mismatch of <2%.<sup>1,36</sup>

The plan for the remainder of this paper is the following. Details of our first principles total energy calculations are outlined below. Following this structures and energetics for the adsorbed H<sub>2</sub>O clusters are presented (section 3). In section 4 we briefly discuss our results, paying particular attention to the electronic structures of adsorbed H<sub>2</sub>O dimers and hexamers. In section 5 we close by drawing some conclusions.

## 2. Approach and computational details

The majority of the calculations reported here have been performed within the DFT framework as implemented in the CASTEP code.<sup>37</sup> The electron–ion interactions were treated with Vanderbilt ultrasoft pseudopotentials,<sup>38</sup> which were expanded within a plane-wave basis set up to a cut-off energy of 400 eV. Electron exchange and correlation effects were described by the Perdew Burke Ernzerhof (PBE)<sup>39</sup> generalized gradient approximation (GGA).

The Cu(111) surface was modelled by a periodic array of Cu slabs, separated by a vacuum region in excess of 12 Å. The majority of the adsorption calculations were performed in  $p(4 \times 4)$  or  $p(5 \times 5)$  unit cells. Such large cells were required in order to minimize the interaction between water clusters in adjacent unit cells. Because of the relatively large unit cells employed and the desire to explore a wide variety of structures for each cluster, thin 3 layer Cu slabs were used throughout. The significance of this apparent compromise in accuracy was, however, carefully checked with test calculations for adsorbed water clusters on slabs of up to 9 layers thickness. The main results of these tests are shown in Table 1, where it can be seen that the absolute adsorption energies obtained on the thicker slabs deviated by <10 meV per H<sub>2</sub>O and bond distances deviated by <0.1 Å. Monkhorst–Pack  $k$ -point meshes with the equivalent of at least  $8 \times 8 \times 1$  sampling within the surface Brillouin zone of a  $p(1 \times 1)$  unit cell were used throughout.<sup>40</sup>

In all optimizations the bottom two Cu layers were fixed at their *ab initio* bulk truncated positions (3.647 Å (expt 3.615 Å<sup>41</sup>)) and the remaining atoms were allowed to fully relax. For each cluster a large number of trial structures were optimized; as many as 30 trial structures for the pentamers and hexamers. In addition, the occasional simulated annealing *ab initio* molecular dynamics simulation was performed. However, we caution that configurational space becomes so large for systems with >2–3 adsorbed and interacting H<sub>2</sub>O molecules that we can in no way guarantee that the structures identified are the global minimum energy

**Table 1** Selected results of the layer and *k*-point sampling convergence tests for H<sub>2</sub>O monomer and H<sub>2</sub>O cluster (dimer and hexamer) adsorption on Cu(111)

Adsorbate	Layers	<i>k</i> mesh <sup>a</sup>	<i>E</i> <sub>ads</sub> (meV/H <sub>2</sub> O)	Cu–O <sup>b</sup> (Å)	O–O <sup>b</sup> (Å)
Monomer [ <i>p</i> (2 × 2) cell]	3	8 × 8 × 1	151	2.345	—
	3	12 × 12 × 1	146	2.370	—
	3	24 × 24 × 1	145	2.357	—
	9	8 × 8 × 1	157	2.347	—
Dimer [ <i>p</i> (3 × 3) cell]	3	12 × 12 × 1	321	2.202/3.032	2.740
	3	18 × 18 × 1	327	2.199/3.026	2.740
	9	12 × 12 × 1	332	2.152/2.934	2.716
Hexamer [ <i>p</i> (4 × 4) cell]	3	8 × 8 × 1	440	2.772	2.697
	3	16 × 16 × 1	435	2.771	2.697
	9	8 × 8 × 1	444	2.802	2.696

<sup>a</sup> *p*(1 × 1) equivalent sampling. <sup>b</sup> Average values are given for the hexamer.

structures. At best the structures identified serve merely as plausible candidates for the lowest energy adsorption structures of H<sub>2</sub>O clusters that may form on Cu(111).

Adsorption energies (*E*<sub>ads</sub>) per H<sub>2</sub>O molecule are calculated from,

$$E_{\text{ads}} = nE_{\text{H}_2\text{O}} + E_{\text{Cu}} - E_{n\text{H}_2\text{O}/\text{Cu}}, \quad (1)$$

where *E*<sub>H<sub>2</sub>O</sub>, *E*<sub>Cu</sub> and *E*<sub>*n*H<sub>2</sub>O/Cu</sub> are the total energies of an *isolated* H<sub>2</sub>O molecule, the clean Cu(111) surface, and the *n*H<sub>2</sub>O/Cu(111) adsorption system, respectively. In this definition positive adsorption energies correspond to an exothermic adsorption process. The reference energy of the isolated gas phase H<sub>2</sub>O molecule is calculated by placing it in a 20 Å<sup>3</sup> cell. Calculations of gas phase H<sub>2</sub>O clusters have also been performed within the same 20 Å<sup>3</sup> cell, for which their gas phase binding energy (*E*<sub>bind</sub>) is defined as,

$$E_{\text{bind}} = nE_{\text{H}_2\text{O}} - E_{n\text{H}_2\text{O}}, \quad (2)$$

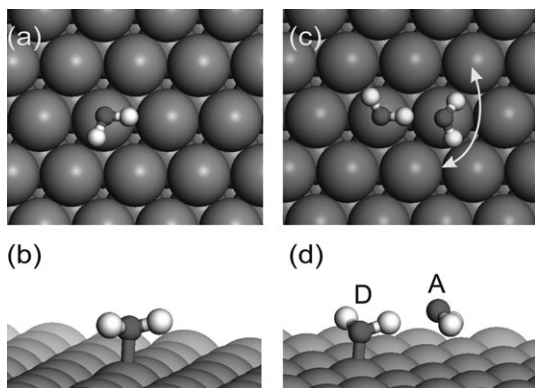
where *E*<sub>*n*H<sub>2</sub>O</sub> is the total energy of the *n*H<sub>2</sub>O gas phase cluster.

### 3. Results

We now consider the structures and energies of the low energy water clusters predicted by DFT, which represents the main body of results of this study.

#### 3.1 H<sub>2</sub>O monomer adsorption

The most stable structure for the H<sub>2</sub>O monomer on Cu(111) is displayed in Fig. 1(a) and (b). From Fig. 1(a) it can be seen that H<sub>2</sub>O adsorbs preferentially at an atop site and from the side view in Fig. 1(b) it can be seen that the molecular plane lies almost parallel to the surface. This structure has been reported before as the most stable one according to DFT for water adsorbed on Cu(111) and several other close-packed transition metal surfaces.<sup>26</sup> We show it again here simply because it is important to know how a single water adsorbs on Cu(111) in order to understand the structures of the adsorbed clusters that we come to next. The Cu–O bond length is 2.35 Å and the adsorption energy is 0.15 eV per H<sub>2</sub>O. The internal structure of the H<sub>2</sub>O molecule deforms little upon adsorption: the HOH angle is 1° less than its computed gas phase value of 104.6° and the OH bond lengths are essentially unchanged from their computed gas phase value of 0.98 Å. Indeed also in the H<sub>2</sub>O clusters we do not observe any significant changes of the internal structure of the H<sub>2</sub>O molecules and thus will not discuss this issue further.



**Fig. 1** Top and side views of the lowest energy adsorbed H<sub>2</sub>O monomer and H<sub>2</sub>O dimer structures identified. In (d) the H<sub>2</sub>O molecule which donates (accepts) the H bond is labelled D (A), and in (c) the arrow is to illustrate that rotation of the acceptor H<sub>2</sub>O in a plane about the surface normal is facile.

### 3.2 H<sub>2</sub>O dimer adsorption

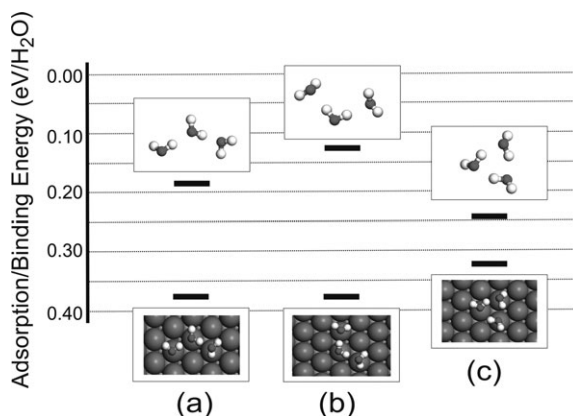
The most stable adsorbed H<sub>2</sub>O dimer structure identified is displayed in Fig. 1(c) and (d). The adsorption energy of this dimer (relative to two isolated H<sub>2</sub>O molecules as defined in eqn (1)) is 0.32 eV per H<sub>2</sub>O. In this structure both H<sub>2</sub>O molecules adsorb above atop sites with the H<sub>2</sub>O molecule that donates the H bond (H bond donor, D) noticeably closer to the surface than the H<sub>2</sub>O molecule that accepts the H bond (H bond acceptor, A). Specifically the shortest Cu–O bond lengths for the donating and accepting H<sub>2</sub>O molecules are 2.20 and 3.00 Å, respectively. The O–O distance in this configuration is 2.74 Å. As was found previously on Pd(111)<sup>28</sup> we see here on Cu(111) that there is essentially free rotation of the high-lying acceptor H<sub>2</sub>O about a plane normal to the surface, *i.e.*, the H bond acceptor is not constrained to remain above the precise atop site. For example, rotating the dimer so that the acceptor is located over a bridge site (with the donor still at the atop site) costs a negligible 2 meV.

The lowest energy dimer structure reported here is similar to the structures previously reported from DFT for dimers on Pt(111)<sup>29</sup> and Pd(111).<sup>28</sup> It was also reported in the previous studies that the H<sub>2</sub>O donor interacts more strongly with the substrate than the H<sub>2</sub>O acceptor. We provide a general explanation for these observations below.

### 3.3 H<sub>2</sub>O trimer adsorption

Two low energy trimer structures of essentially identical adsorption energy have been identified. These are labelled (a) and (b) in Fig. 2, and are displayed along with a third adsorbed trimer to be discussed in a moment. Also shown in Fig. 2 are the relative energies and structures of all three of these trimers in the gas phase. The two low energy adsorption structures are similar to each other in as much as they are bent structures with only two H bonds connecting the three H<sub>2</sub>O molecules. They differ, however, in that structure (b) has one H<sub>2</sub>O which donates two H bonds whereas structure (a) does not. The adsorption energy for both trimers is 0.37 eV per H<sub>2</sub>O.

It is interesting to see that the two bent adsorbed trimers identified here are not the lowest energy isomers for H<sub>2</sub>O trimers in the gas phase. Instead this is a cyclic structure with three H bonds between the three H<sub>2</sub>O molecules; each H<sub>2</sub>O donates and accepts a single H bond, as can be seen from the upper part of Fig. 2(c).



**Fig. 2** Relative energies and structures of three gas phase and adsorbed  $\text{H}_2\text{O}$  trimers. Adsorption energies and binding energies are relative to isolated gas phase  $\text{H}_2\text{O}$  molecules as defined in eqn (1) and (2), respectively.

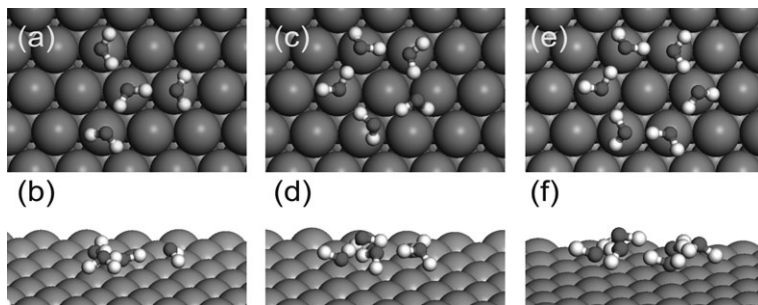
However, from the lower part of Fig. 2(c), it can be seen that when adsorbed the cyclic structure is  $\sim 0.05$  eV per  $\text{H}_2\text{O}$  less stable than structures (a) and (b). Thus it is clear from structures (a), (b), and (c) that the surface has a significant effect on the relative energies of these isomers, favouring those with only two H bonds. Essentially then the current calculations indicate that one H bond in the trimer breaks upon adsorption.

### 3.4 $\text{H}_2\text{O}$ tetramer adsorption

The lowest energy structure identified for the  $\text{H}_2\text{O}$  tetramer is displayed in Fig. 3(a) and (b). This structure resembles one of the low energy trimers (trimer b) but with a fourth  $\text{H}_2\text{O}$  added as a H bond donor to the central  $\text{H}_2\text{O}$ . The binding energy of this cluster is 0.41 eV per  $\text{H}_2\text{O}$ . Again the adsorbed structure differs significantly from the lowest energy gas phase isomer which is, like the trimer, a cyclic structure and is comprised of four H bonds. The O–O distances in the adsorbed structure range from 2.66 to 2.75 Å and the Cu–O distances from 2.20 to 3.10 Å.

### 3.5 $\text{H}_2\text{O}$ pentamer adsorption

The most stable  $\text{H}_2\text{O}$  pentamer identified is displayed in Fig. 3(c) and (d). In this structure each  $\text{H}_2\text{O}$  acts as a single H bond donor and a single H bond acceptor,



**Fig. 3** Top and side views of the lowest energy structures identified for an adsorbed  $\text{H}_2\text{O}$  tetramer ((a)–(b)), pentamer ((c)–(d)), and hexamer ((e)–(f)) on Cu(111).

rather similar to the low energy structure of the gas phase pentamer. Three of the H<sub>2</sub>O molecules are located over atop sites, whereas the two others are closest to threefold sites. There is a considerable buckling in the heights of the H<sub>2</sub>O molecules above the surface; a 0.8 Å difference between the lowest and highest H<sub>2</sub>O molecules. The O–O distances in the adsorbed structure range from 2.60 to 2.80 Å and its adsorption energy is 0.44 eV per H<sub>2</sub>O.

### 3.6 H<sub>2</sub>O hexamer adsorption

The most stable hexamer identified is the one shown in Fig. 3(e) and (f). It is a cyclic hexamer with a binding energy of 0.44 eV per H<sub>2</sub>O. The symmetry and registry of this cyclic hexamer with the substrate appears to be consistent with recent STM experiments in which it was observed.<sup>35</sup> From the top view of the hexamer in Fig. 3(e) it is clear that all six H<sub>2</sub>O molecules are located approximately above substrate atop sites and act as single H bond donors and single H bond acceptors. From the side view in Fig. 3(f) it can further be seen that this structure is significantly buckled with the H<sub>2</sub>O molecules residing at two distinct heights above the surface: the vertical displacement between adjacent H<sub>2</sub>O molecules is ~0.76 Å. Further, and unlike in the gas phase, the six nearest neighbour O–O distances are not equal in the adsorbed hexamer. Instead they alternate between two characteristic values: 2.76 and 2.63 Å. This symmetry-breaking dimerization is reminiscent of the alternating single and double C–C bonds in the Kekulé model of benzene.

Previous DFT reports of an isolated cyclic hexamer on Ru(0001)<sup>30</sup> and a cyclic hexamer as part of a quasi-2D water overlayer on Pd(111)<sup>10</sup> did not predict the buckled structure identified here. Instead a planar cyclic hexamer with all molecules at the same height was found. Here, on Cu(111), our PBE calculations indicate that the planar hexamer is ~0.12 eV per H<sub>2</sub>O less stable than the buckled one. Since it is not inconceivable that this difference is a result of our chosen computational set-up or exchange–correlation functional, we performed a series of tests in order to assess the reliability of this result. Specifically we compared the energy difference between the low energy buckled hexamer identified here and a hypothetical planar cyclic hexamer on: (i) a Cu(111) slab with the RPBE<sup>42</sup> functional; (ii) a close-packed Cu<sub>10</sub> cluster with the PBE functional, the hybrid DFT PBE0<sup>43</sup> functional, and with Møller–Plesset perturbation theory to second order (MP2).<sup>44</sup> The results of these test calculations are listed in Table 2, with the conclusion of all of them being essentially the same: there is a considerable energetic preference (>0.1 eV per H<sub>2</sub>O) for buckling on this surface.

**Table 2** Selected results of the test calculations of the energy difference,  $\Delta E$  (meV per H<sub>2</sub>O), between the buckled and planar cyclic H<sub>2</sub>O hexamers on Cu(111). A positive  $\Delta E$  indicates that the buckled hexamer is more stable than the planar one, which is always the case

Approach	$\Delta E$ (meV/H <sub>2</sub> O)
Cu(111) PBE	122 <sup>a</sup>
Cu(111) RPBE	178 <sup>a</sup>
Cu <sub>10</sub> cluster PBE	170 <sup>b</sup> , 175 <sup>c</sup>
Cu <sub>10</sub> cluster PBE0	170 <sup>b</sup> , 173 <sup>c</sup>
Cu <sub>10</sub> cluster MP2	194 <sup>b</sup> , 186 <sup>d</sup>

<sup>a</sup> Pseudopotential plus plane-wave approach with CASTEP as described in Section II. <sup>b</sup> All-electron Gaussian03 calculation with a 6-311 + G(2df,pd) basis set. <sup>c</sup> All-electron Gaussian03 calculation with a 6-311 + +G(3df,3pd) basis set. <sup>d</sup> All-electron Gaussian03 calculation with a 6-311 + +G(2df,pd) basis set.

## 4. Discussion

Let's now briefly investigate some details of the results presented above. First we consider the relative stability of the clusters identified and then several aspects of their electronic structures.

### 4.1 Relative energies of adsorbed and gas phase clusters

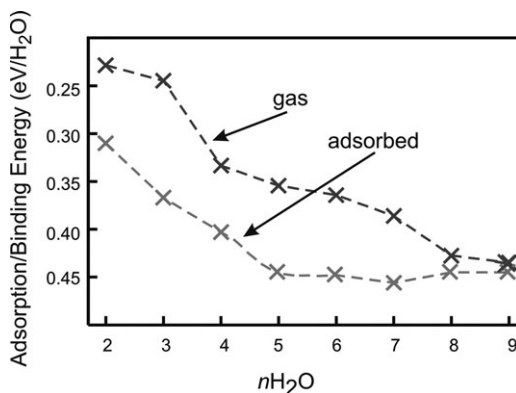
To begin, we compare the stability of the H<sub>2</sub>O clusters when adsorbed to when they are in their equilibrium gas phase configurations. We show this in Fig. 4, where the adsorption (binding) energies of adsorbed (gas phase) H<sub>2</sub>O clusters ranging from 2–9 H<sub>2</sub>O molecules are plotted. The structures of the larger 7–9 molecule gas phase clusters are based on the Hartree–Fock structures reported by Maheshwary *et al.*<sup>45</sup> Here we have simply re-optimized these gas phase structures within the current DFT-PBE set-up. The structures of the 7–9 molecule adsorbed clusters are those recently identified in a combined STM and DFT study of H<sub>2</sub>O on Cu(111).<sup>35</sup>

From Fig. 4 it can be seen that in the entire regime examined the adsorbed clusters are more stable than the gas phase ones. It is clear, however, that as the clusters grow in size the energy difference between the adsorbed and gas phase clusters decreases. The increased stability of the adsorbed clusters is obviously because of their binding with the substrate. However, it is interesting to note that the adsorbed clusters remain more stable than their gas phase counterparts even for those clusters which have fewer H bonds when adsorbed. For example the H<sub>2</sub>O trimer and tetramer have one less H bond when adsorbed as compared to in the gas phase. And for the larger clusters with 7–9 H<sub>2</sub>O molecules several more H bonds are broken.

Also clear from Fig. 4 is that the adsorption energy of the adsorbed clusters gradually decreases until around the pentamer and then seems to level off for the larger clusters. The adsorption energies for the clusters with 5, 6, 7, 8, and 9 molecules are 0.44, 0.44, 0.45, and 0.44 eV per H<sub>2</sub>O, respectively. The limiting value of the adsorption energy is at  $\sim 0.44$  eV per H<sub>2</sub>O similar to the adsorption energy reported for a hypothetical 2D ice-like bilayer on Cu(111).<sup>36</sup>

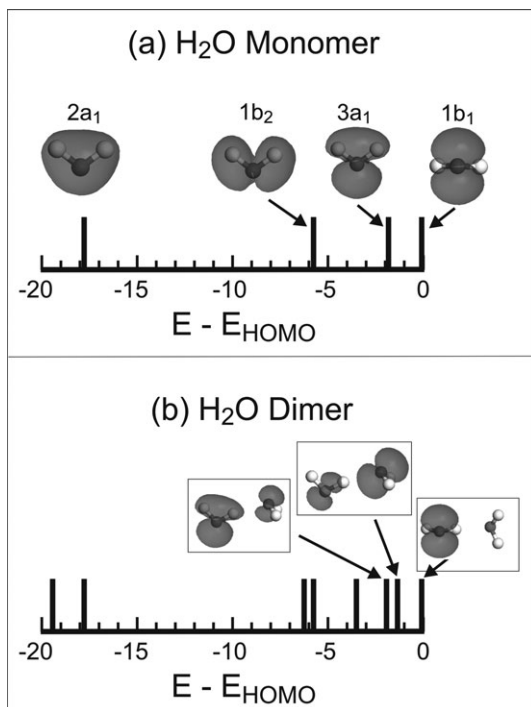
### 4.2 Electronic structures

Next we briefly consider the nature of the binding between some of the clusters and the Cu(111) substrate. In particular we focus on trying to understand the buckled structure of the H<sub>2</sub>O dimer and H<sub>2</sub>O hexamer.



**Fig. 4** Plot of the adsorption energies and binding energies for adsorbed  $n\text{H}_2\text{O}$  ( $n = 2-9$ ) clusters on Cu(111) and for gas phase  $n\text{H}_2\text{O}$  ( $n = 2-9$ ) clusters. The structures of the 7–9 H<sub>2</sub>O molecule gas phase and adsorbed clusters are taken from ref. 45 and ref. 35, respectively. The dashed lines are merely guides to the eye.





**Fig. 5** DFT computed energy level diagrams and selected Kohn–Sham orbitals for the highest occupied orbitals of an isolated (gas phase) H<sub>2</sub>O monomer (a) and an isolated (gas phase) H<sub>2</sub>O dimer (b). The energy of the highest occupied molecular orbital ( $E_{\text{HOMO}}$ ) is set to zero eV in each system.

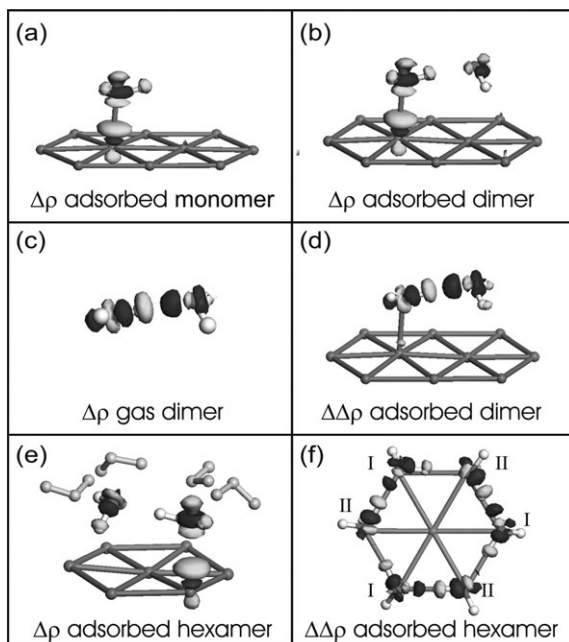
A consideration of how the H<sub>2</sub>O monomer interacts with the Cu(111) substrate provides a basis for understanding the clusters and so we recall the four highest energy occupied molecular orbitals of an isolated gas phase H<sub>2</sub>O (Fig. 5). In order of increasing energy these are labelled, according to  $C_{2v}$  symmetry, 2a<sub>1</sub>, 1b<sub>2</sub>, 3a<sub>1</sub> and 1b<sub>1</sub>. The highest occupied molecular orbital (HOMO) of H<sub>2</sub>O is the 1b<sub>1</sub> orbital. Previous studies have shown that the interaction of the H<sub>2</sub>O monomer with close-packed transition metal surfaces is mediated mainly through the 1b<sub>1</sub> orbital.<sup>17,33</sup> Indeed this is what we find here again for Cu(111). We demonstrate this in Fig. 6(a) with the electron density difference plot for a H<sub>2</sub>O monomer on Cu(111). The electron density difference ( $\Delta\rho$ ) is defined here as

$$\Delta\rho = \rho_{n\text{H}_2\text{O}/\text{Cu}} + \rho_{\text{Cu}} - \rho_{\text{H}_2\text{O}}, \quad (3)$$

where  $\rho_{n\text{H}_2\text{O}/\text{Cu}}$ ,  $\rho_{\text{Cu}}$ , and  $\rho_{\text{H}_2\text{O}}$  are the electron densities of the particular  $n\text{H}_2\text{O}/\text{Cu}(111)$  adsorption system under consideration, the isolated Cu(111) surface, and the isolated H<sub>2</sub>O molecule(s) each in the exact structure they adopt in the adsorption system. Electron density difference plots such as this capture the rearrangement of the electron density upon making the adsorption bond and in this case demonstrate the key role played by the 1b<sub>1</sub> orbital.

Moving to the H<sub>2</sub>O dimer we show in Fig. 6(b) a similar electron density difference plot. From this it is clear that the H bond donor interacts more strongly with the substrate than the acceptor does, which is what we would expect based on the structure alone. Further, it can be seen that the donor of the dimer interacts in a similar manner as the H<sub>2</sub>O monomer does, *i.e.*, through the H<sub>2</sub>O 1b<sub>1</sub> orbital. Since the nature of the H bond in the adsorbed and gas phase dimers is similar (*cf.* Fig. 6(c)





**Fig. 6** Isosurfaces of constant electron density difference ( $\Delta\rho$ ) and electron density “rearrangement” ( $\Delta\Delta\rho$ ) as defined in eqn (3) and (4), respectively.  $\Delta\rho$  is displayed for  $\text{H}_2\text{O}$  monomer adsorption (a),  $\text{H}_2\text{O}$  dimer adsorption (b), a gas phase  $\text{H}_2\text{O}$  dimer (c), and  $\text{H}_2\text{O}$  hexamer adsorption (e).  $\Delta\Delta\rho$  is displayed for the adsorbed  $\text{H}_2\text{O}$  dimer (d) and the adsorbed  $\text{H}_2\text{O}$  hexamer (f). Dark isosurfaces correspond to regions of electron accumulation and light isosurfaces to regions of electron depletion. In (a), (b), (c), and (e) the units are  $2 \times 10^{-2} \text{ e } \text{\AA}^{-3}$ , and in (d) and (f) the units are  $5 \times 10^{-2} \text{ e } \text{\AA}^{-3}$ . For clarity in (e)  $\Delta\rho$  is only displayed around the two front-most  $\text{H}_2\text{O}$  molecules and Cu atoms.

and (d)) it remains reasonable to seek insight into the nature of the adsorption bond by considering the electronic structure of the adsorbate in the gas phase, as we did for the  $\text{H}_2\text{O}$  monomer. Thus in Fig. 5(b) we display the energy level diagram for the high energy occupied orbitals of the gas phase  $\text{H}_2\text{O}$  dimer. Fig. 5(b) provides an immediate explanation for why the donor interacts more strongly with the substrate than the acceptor does and why this interaction is, like the monomer, mediated through the  $1b_1$  orbital. Specifically, it can be seen that this is because the HOMO of the gas phase dimer is a  $1b_1$ -like orbital located on the H bond donor, and that this  $1b_1$ -like orbital remains a non-bonding orbital, not being involved in the H bond. On the other hand the  $1b_1$ -like orbital on the acceptor is not free being shifted to a lower energy through the formation of the H bond. Thus the  $1b_1$ -like orbital of the H bond acceptor of the dimer is, in a chemical sense, “saturated” through its participation in the H bond and less inclined to bond with the substrate than the H bond donor.

A similar reasoning explains the symmetry broken buckled structure of the adsorbed hexamer. Indeed the structure of the hexamer is best understood by considering it as being comprised of three weakly interacting dimers. Within the (equilibrium) buckled adsorption structure the two types of water molecules interact differently with the substrate, as revealed by the electron density difference plot in Fig. 6(e). Again the low-lying  $\text{H}_2\text{O}$  molecules in the adsorbed hexamer interact with the surface through their  $1b_1$  molecular orbitals whereas the high-lying  $\text{H}_2\text{O}$  molecules do not. Since, as we have seen above, the  $1b_1$  orbital of  $\text{H}_2\text{O}$  is also implicated when  $\text{H}_2\text{O}$  acts as a H bond acceptor, we can anticipate that the low-lying  $\text{H}_2\text{O}$  molecules are rendered poor H bond acceptors through their bonding with the substrate. Indeed this is precisely what we see in the structure of the adsorbed

hexamer with the longer (2.76 Å) H bonds being formed when the low-lying H<sub>2</sub>O molecules act mainly as H bond acceptors, whereas the shorter (2.63 Å) H bonds form when the high-lying H<sub>2</sub>O molecules act mainly as H bond acceptors. The two types of H bond in the adsorbed hexamer is clear not only from the atomic structure, but also in the electronic structure. To illustrate this we examine the electron density “rearrangement” ( $\Delta\Delta\rho$ ) within the adsorbed hexamer. This is defined here as

$$\Delta\Delta\rho = \rho_{6\text{H}_2\text{O}/\text{Cu}} + \rho_{\text{Cu}} - \rho_{3\text{H}_2\text{O}-\text{I}/\text{Cu}} - \rho_{3\text{H}_2\text{O}-\text{II}/\text{Cu}}, \quad (4)$$

where  $\rho_{6\text{H}_2\text{O}/\text{Cu}}$  and  $\rho_{\text{Cu}}$  are the electron densities of the hexamer/Cu(111) adsorption system and the clean Cu(111) slab, respectively.  $\rho_{3\text{H}_2\text{O}-\text{I}/\text{Cu}}$  and  $\rho_{3\text{H}_2\text{O}-\text{II}/\text{Cu}}$  are the electron densities of two subsets of the 6 adsorbed H<sub>2</sub>O molecules, as labelled in Fig. 6(f). The two subsets of H<sub>2</sub>O molecules are selected so that the quantity  $\Delta\Delta\rho$  essentially reveals the H<sub>2</sub>O–H<sub>2</sub>O interaction in the adsorbed hexamer. Clearly from Fig. 6(f) it can be seen that the stronger H bonds form when the high-lying waters act mainly as the acceptors of the H bond, whereas the weaker H bonds form when the low-lying waters act mainly as acceptors. Essentially what the buckled structure of the hexamer tells us is that there is a competition between the ability of a H<sub>2</sub>O molecule to form a ‘strong’ bond with the surface and its ability to act as a ‘strong’ H bond acceptor.

## 5. Conclusions

In conclusion the initial results of a DFT study of H<sub>2</sub>O clustering on Cu(111) have been reported. Clusters with 2–6 H<sub>2</sub>O molecules have been examined and for each cluster low energy adsorption structures reported. In addition, several novel concepts have been illustrated such as the fact that high energy gas phase isomers with fewer H bonds can be stabilized upon adsorption and that the nature of the competition between water–water bonding and water–metal bonding is more subtle than previously realised with a clear distinction having been identified between H<sub>2</sub>O molecules that act either as H bond donors or as H bond acceptors.

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