

The chemical history of molecules in circumstellar disks

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ABSTRACT

Context. Many chemical changes occur during the collapse of a molecular cloud to form a low-mass star and the surrounding disk. One-dimensional models have been used so far to analyse these chemical processes, but they cannot properly describe the incorporation of material into disks.

Aims. The goal of this work is to understand how material changes chemically as it is transported from the cloud to the star and the disk. Of special interest is the chemical history of the material in the disk at the end of the collapse.

Methods. A two-dimensional, semi-analytical model is presented that, for the first time, follows the chemical evolution from the pre-stellar core to the protostar and circumstellar disk. The model computes infall trajectories from any point in the cloud and tracks the radial and vertical motion of material in the viscously evolving disk. It includes a full time-dependent radiative transfer treatment of the dust temperature, which controls much of the chemistry. A small parameter grid is explored to understand the effects of the sound speed and the mass and rotation of the cloud. The freeze-out and evaporation of carbon monoxide (CO) and water (H₂O), as well as the potential for forming complex organic molecules in ices, are considered as important first steps towards illustrating the full chemistry.

Results. Both species freeze out towards the centre before the collapse begins. Pure CO ice evaporates during the infall phase and re-adsorbs in those parts of the disk that cool below the CO desorption temperature of ~18 K. Water remains solid almost everywhere during the infall and disk formation phases and evaporates within ~10 AU of the star. Mixed CO-H₂O ices are important in keeping some solid CO above 18 K and in explaining the presence of CO in comets. Material that ends up in the planet- and comet-forming zones of the disk (~5–30 AU from the star) is predicted to spend enough time in a warm zone (several 10⁴ yr at a dust temperature of 20–40 K) during the collapse to form first-generation complex organic species on the grains. The dynamical timescales in the hot inner envelope (hot core or hot corino) are too short for abundant formation of second-generation molecules by high-temperature gas-phase chemistry.

Key words. astrochemistry – stars: formation – stars: circumstellar matter – stars: planetary systems: protoplanetary disks – molecular processes

1. Introduction

The formation of low-mass stars and their planetary systems is a complex event, spanning several orders of magnitude in temporal and spatial scales, and involving a wide variety of physical and chemical processes. Thanks to observations (see reviews by [di Francesco et al. 2007](#); and [White et al. 2007](#)), theory (see review by [Shu et al. 1987](#)) and computer simulations (see reviews by [Klein et al. 2007](#); and [Dullemond et al. 2007](#)), the general picture of low-mass star formation is now understood. An instability in a cold molecular cloud leads to gravitational collapse. Rotation and magnetic fields cause a flattened density structure early on, which evolves into a circumstellar disk at later times. The protostar continues to accrete matter from the disk and the remnant envelope, while also expelling matter in a bipolar pattern. Grain growth in the disk eventually leads to the formation of planets, and as the remaining dust and gas disappear, a mature solar system emerges. While there has been ample discussion in the literature on the origin and evolution of grains in disks (see reviews by [Natta et al. 2007](#); and [Dominik et al. 2007](#)), little attention has so far been paid to the chemical history of the more volatile material in a two- or three-dimensional setting.

Chemical models are required to understand the observations and develop the simulations (see reviews by [Ceccarelli et al. 2007](#); [Bergin et al. 2007](#); and [Bergin & Tafalla 2007](#)). The chemistry in pre-stellar cores is relatively easy to model, because the dynamics and the temperature structure are simpler before the protostar is formed than afterwards. A key result from the pre-stellar core models is the depletion of many carbon-bearing species towards the centre of the core ([Bergin & Langer 1997](#); [Lee et al. 2004](#)).

[Ceccarelli et al. \(1996\)](#) modelled the chemistry in the collapse phase, and others have done so more recently ([Rodgers & Charnley 2003](#); [Doty et al. 2004](#); [Lee et al. 2004](#); [Garrod & Herbst 2006](#); [Aikawa et al. 2008](#); [Garrod et al. 2008](#)). All of these models are one-dimensional, and thus necessarily ignore the circumstellar disk. As the protostar turns on and heats up the surrounding material, all models agree that frozen-out species return to the gas phase if the dust temperature surpasses their evaporation temperature. The higher temperatures can further drive a hot-core-like chemistry, and complex molecules may be formed if the infall timescales are long enough.

If the model is expanded into a second dimension and the disk is included, the system gains a large reservoir where

infalling material from the cloud can be stored for a long time before accreting onto the star. This can lead to further chemical enrichment, especially in the warmer parts of the disk (Aikawa et al. 1997; Aikawa & Herbst 1999; Willacy & Langer 2000; van Zadelhoff et al. 2003; Rodgers & Charnley 2003; Aikawa et al. 2008). The interior of the disk is shielded from direct irradiation by the star, so it is colder than the disk's surface and the remnant cloud. Hence, molecules that evaporated as they fell in towards the star may freeze out again when they enter the disk. This was first shown quantitatively by Brinch et al. (2008, hereafter BWH08) using a two-dimensional hydrodynamical simulation.

In addition to observations of nearby star-forming regions, the comets in our own solar system provide a unique probe into the chemistry that takes place during star and planet formation. The bulk composition of the cometary nuclei is believed to be mostly pristine, closely reflecting the composition of the pre-solar nebula (Bockelée-Morvan et al. 2004). However, large abundance variations have been observed between individual comets and these remain poorly understood (Kobayashi et al. 2007). Two-dimensional chemical models may shed light on the cometary chemical diversity.

Two molecules of great astrophysical interest are carbon monoxide (CO) and water (H₂O). They are the main reservoirs of carbon and oxygen and control much of the chemistry. CO is an important precursor for more complex molecules; for example, solid CO can be hydrogenated to formaldehyde (H₂CO) and methanol (CH₃OH) at low temperatures (Watanabe & Kouchi 2002; Fuchs et al. *subm.*). In turn, these two molecules form the basis of even larger organic species like methyl formate (HCOOCH₃; Garrod & Herbst 2006; Garrod et al. 2008). The key role of H₂O in the formation of life on Earth and potentially elsewhere is evident. If the entire formation process of low-mass stars and their planets is to be understood, a thorough understanding of these two molecules is essential.

This paper is the first in a series aiming to model the chemical evolution from the pre-stellar core to the disk phase in two dimensions, using a simplified, semi-analytical approach for the dynamics of the collapsing envelope and the disk, but including detailed radiative transfer for the temperature structure. The model follows individual parcels of material as they fall in from the cloud into the disk. The gaseous and solid abundances of CO and H₂O are calculated for each infalling parcel to obtain global gas-ice profiles. The semi-analytical nature of the model allows for an easy exploration of physical parameters like the cloud's mass and rotation rate, or the effective sound speed. Tracing the temperature history of the infalling material provides a first clue into the formation of more complex species. The model also provides some insight into the origin of the chemical diversity in comets.

Section 2 contains a full description of the model. Results are presented in Sect. 3 and discussed in a broader astrophysical context in Sect. 4. Conclusions are drawn in Sect. 5.

2. Model

The physical part of our two-dimensional axisymmetric model describes the collapse of an initially spherical, isothermal, slowly rotating cloud to form a star and circumstellar disk. The collapse dynamics are taken from Shu (1977, hereafter S77), including the effects of rotation as described by Cassen & Moosman (1981, hereafter CM81) and Terebey et al. (1984, hereafter TSC84). Infalling material hits the equatorial plane inside the centrifugal radius to form a disk, whose further

evolution is constrained by conservation of angular momentum (Lynden-Bell & Pringle 1974). Some properties of the star and the disk are adapted from Adams & Shu (1986) and Young & Evans (2005, hereafter YE05). Magnetic fields are not included in our model. They are unlikely to affect the chemistry directly and their main physical effect (causing a flattened density distribution; Galli & Shu 1993) is already accounted for by the rotation of the cloud.

Our model is an extension of the one used by Dullemond et al. (2006) to study the crystallinity of dust in circumstellar disks. That model was purely one-dimensional; our model treats the disk more realistically as a two-dimensional structure.

2.1. Envelope

The cloud (or envelope) is taken to be a uniformly rotating singular isothermal sphere at the onset of collapse. It has a solid-body rotation rate Ω_0 and an r^{-2} density profile (S77):

$$\rho_0(r) = \frac{c_s^2}{2\pi G r^2}, \quad (1)$$

where G is the gravitational constant and c_s the effective sound speed. Throughout this work, r is used for the spherical radius and R for the cylindrical radius. Setting the outer radius at r_{env} , the total mass of the cloud is

$$M_0 = \frac{2c_s^2 r_{\text{env}}}{G}. \quad (2)$$

After the collapse is triggered at the centre, an expansion wave (or collapse front) travels outwards at the sound speed (S77; TSC84). Material inside the expansion wave falls in towards the centre to form a protostar. The infalling material is deflected towards the gravitational midplane by the cloud's rotation. It first hits the midplane inside the centrifugal radius (where gravity balances angular momentum; CM81), resulting in the formation of a circumstellar disk (Sect. 2.2).

The dynamics of a collapsing singular isothermal sphere were computed by S77 in terms of the non-dimensional variable $x = r/c_s t$, with t the time after the onset of collapse. In this self-similar description, the head of the expansion wave is always at $x = 1$. The density and radial velocity are given by the non-dimensional variables \mathcal{A} and v , respectively. (S77 uses α for the density, but our model already uses that symbol for the viscosity in Sect. 2.2.) These variables are dimensionalised through

$$\rho(r, t) = \frac{\mathcal{A}(x)}{4\pi G t^2}, \quad (3)$$

$$u_r(r, t) = c_s v(x). \quad (4)$$

Values for \mathcal{A} and v are tabulated in S77.

CM81 and TSC84 analysed the effects of slow uniform rotation on the S77 collapse solution, with the former focussing on the flow onto the protostar and the disk and the latter on what happens further out in the envelope. In the axisymmetric TSC84 description, the density and infall velocities depend on the time, t , the radius, r , and the polar angle, θ :

$$\rho(r, \theta, t) = \frac{\mathcal{A}(x, \theta, \tau)}{4\pi G t^2}, \quad (5)$$

$$u_r(r, \theta, t) = c_s v(x, \theta, \tau), \quad (6)$$

where $\tau = \Omega_0 t$ is the non-dimensional time. The polar velocity is given by

$$u_\theta(r, \theta, t) = c_s w(x, \theta, \tau). \quad (7)$$

The differential equations from TSC84 were solved numerically to obtain solutions for \mathcal{A} , v and w .

The TSC84 solution breaks down around $x = \tau^2$, so the CM81 solution is used inside of this point. A streamline through a point (r, θ) effectively originated at an angle θ_0 in this description:

$$\frac{\cos \theta_0 - \cos \theta}{\sin^2 \theta_0 \cos \theta} - \frac{R_c}{r} = 0, \quad (8)$$

where R_c is the centrifugal radius,

$$R_c(t) = \frac{1}{16} c_s m_0^3 t^3 \Omega_0^2, \quad (9)$$

with m_0 a numerical factor equal to 0.975. The CM81 radial and polar velocity are

$$u_r(r, \theta, t) = -\sqrt{\frac{GM}{r}} \sqrt{1 + \frac{\cos \theta}{\cos \theta_0}}, \quad (10)$$

$$u_\theta(r, \theta, t) = \sqrt{\frac{GM}{r}} \sqrt{1 + \frac{\cos \theta}{\cos \theta_0}} \frac{\cos \theta_0 - \cos \theta}{\sin \theta}, \quad (11)$$

and the CM81 density is

$$\rho(r, \theta, t) = -\frac{\dot{M}}{4\pi r^2 u_r} \left[1 + 2 \frac{R_c}{r} P_2(\cos \theta_0) \right]^{-1}, \quad (12)$$

where P_2 is the second-order Legendre polynomial and $\dot{M} = m_0 c_s^3 / G$ is the total accretion rate from the envelope onto the star and disk (S77; TSC84). The primary accretion phase ends when the outer shell of the envelope reaches the star and disk. This point in time ($t_{\text{acc}} = M_0 / \dot{M}$) is essentially the beginning of the T Tauri or Herbig Ae/Be phase, but it does not yet correspond to a typical T Tauri or Herbig Ae/Be object (see Sect. 3.2).

The TSC84 and CM81 solutions do not reproduce the cavities created by the star's bipolar outflow, so they have to be put in separately. Outflows have been observed in two shapes: conical and curved (Padgett et al. 1999). Both can be characterised by the outflow opening angle, γ , which grows with the age of the object. Arce & Sargent (2006) found a linear relationship in log-log space between the age of a sample of 17 young stellar objects and their outflow opening angles. Some explanations exist for the outflow widening in general, but it is not yet understood how $\gamma(t)$ depends on parameters like the initial cloud mass and the sound speed. It is likely that the angle depends on the relative age of the object rather than on the absolute age.

The purpose of our model is not to include a detailed description of the outflow cavity. Instead, the outflow is primarily included because of its effect on the temperature profiles (Whitney et al. 2003). Its opening angle is based on the fit by Arce & Sargent (2006) to their Fig. 5, but it is taken to depend on t/t_{acc} rather than t alone. The outflow is also kept smaller, which brings it closer to the Whitney et al. angles. Its shape is taken to be conical. With the resulting formula,

$$\log \frac{\gamma(t)}{\text{deg}} = 1.5 + 0.26 \log \frac{t}{t_{\text{acc}}}, \quad (13)$$

the opening angle is always 32° at $t = t_{\text{acc}}$. The numbers in Eq. (13) are poorly constrained; however, the details of the outflow (both size and shape) do not affect the temperature profiles strongly, so this introduces no major errors in the chemistry results. The outflow cones are filled with a constant mass of $0.002 M_0$ at a uniform density, which decreases to 10^3 – 10^4 cm^{-3} at t_{acc} depending on the model parameters. The outflow effectively removes about 1% of the initial envelope mass.

2.2. Disk

The rotation of the envelope causes the infalling material to be deflected towards the midplane, where it forms a circumstellar disk. The disk initially forms inside the centrifugal radius (CM81), but conservation of angular momentum quickly causes the disk to spread beyond this point. The evolution of the disk is governed by viscosity, for which our model uses the common α prescription (Shakura & Sunyaev 1973). This gives the viscosity coefficient ν as

$$\nu(R, t) = \alpha c_{s,d} H. \quad (14)$$

The sound speed in the disk, $c_{s,d} = \sqrt{k T_m / \mu m_p}$ (with k the Boltzmann constant, m_p the proton mass and μ the mean molecular mass of 2.3 nuclei per hydrogen molecule), is different from the sound speed in the envelope, c_s , because the midplane temperature of the disk, T_m , varies as described in Hueso & Guillot (2005). The other variable from Eq. (14) is the scale height:

$$H(R, t) = \frac{c_{s,d}}{\Omega_k}, \quad (15)$$

where Ω_k is the Keplerian rotation rate:

$$\Omega_k(R, t) = \sqrt{\frac{GM_*}{R^3}}, \quad (16)$$

with M_* the stellar mass (Eq. (29)). The viscosity parameter α is kept constant at 10^{-2} (Dullemond et al. 2007; Andrews & Williams 2007b).

Solving the problem of advection and diffusion yields the radial velocities inside the disk (Dullemond et al. 2006; Lynden-Bell & Pringle 1974):

$$u_R(R, t) = -\frac{3}{\Sigma \sqrt{R}} \frac{\partial}{\partial R} (\Sigma \nu \sqrt{R}). \quad (17)$$

The surface density evolves as

$$\frac{\partial \Sigma(R, t)}{\partial t} = -\frac{1}{R} \frac{\partial}{\partial R} (\Sigma R u_R) + S, \quad (18)$$

where the source function S accounts for the infall of material from the envelope:

$$S(R, t) = 2N\rho u_z, \quad (19)$$

with u_z the vertical component of the envelope velocity field (Eqs. (6), (7), (10) and (11)). The factor 2 accounts for the envelope accreting onto both sides of the disk and the normalization factor N ensures that the overall accretion rate onto the star and the disk is always equal to \dot{M} . Both ρ and u_z in Eq. (19) are to be computed at the disk-envelope boundary, which will be defined at the end of this section.

As noted by Hueso & Guillot (2005), the infalling envelope material enters the disk with a subkeplerian rotation rate, so, by conservation of angular momentum, it would tend to move a bit further inwards. Not taking this into account would artificially generate angular momentum, causing the disk to take longer to accrete onto the star. As a consequence the disk will, at any given point in time, have too high a mass and too large a radius. Hueso & Guillot solved this problem by modifying Eq. (19) to place the material directly at the correct radius. However, this causes an undesirable discontinuity in the infall trajectories. Instead, our model adds a small extra component to Eq. (17) for $t < t_{\text{acc}}$:

$$u_R(R, t) = -\frac{3}{\Sigma \sqrt{R}} \frac{\partial}{\partial R} (\Sigma \nu \sqrt{R}) - \eta_r \sqrt{\frac{GM}{R}}. \quad (20)$$

The functional form of the extra term derives from the CM81 solution. A constant value of 0.002 for η_r is found to reproduce very well the results of [Hueso & Guillot](#). It also provides a good match with the disk masses from [Yorke & Bodenheimer \(1999\)](#), [YE05](#) and [BWH08](#), whose models cover a wide range of initial conditions.

The disk's inner radius is determined by the evaporation of dust by the star (e.g. [YE05](#)):

$$R_i(t) = \sqrt{\frac{L_*}{4\pi\sigma T_{\text{evap}}^4}}, \quad (21)$$

where σ is the Stefan-Boltzmann constant. The dust evaporation temperature, T_{evap} , is set to 2000 K. Taking an alternative value of 1500 K has no effect on our results. The stellar luminosity, L_* , is discussed in Sect. 2.3. Inward transport of material at R_i leads to accretion from the disk onto the star:

$$\dot{M}_{d \rightarrow *} = -2\pi R_i u_R \Sigma, \quad (22)$$

with the radial velocity, u_R , and the surface density, Σ , taken at R_i . The disk gains mass from the envelope at a rate $\dot{M}_{e \rightarrow d}$, so the disk mass evolves as

$$M_d(t) = \int_0^t (\dot{M}_{e \rightarrow d} - \dot{M}_{d \rightarrow *}) dt'. \quad (23)$$

Our model uses a Gaussian profile for the vertical structure of the disk ([Shakura & Sunyaev 1973](#)):

$$\rho(R, z, t) = \rho_c \exp\left(-\frac{z^2}{2H^2}\right), \quad (24)$$

with z the height above the midplane. The scale height comes from Eq. (15) and the midplane density is

$$\rho_c(R, t) = \frac{\Sigma}{H\sqrt{2\pi}}. \quad (25)$$

Along with the radial motion (Eq. (20), taken to be independent of z), material also moves vertically in the disk, as it must maintain the Gaussian profile at all times. To see this, consider a parcel of material that enters the disk at time t at coordinates R and z into a column with scale height H and surface density Σ . The column of material below the parcel is

$$\int_0^z \rho(R, \zeta, t) d\zeta = \frac{1}{2} \Sigma \text{erf}\left(\frac{z}{H\sqrt{2}}\right), \quad (26)$$

where erf is the error function. At a later time t' , the entire column has moved to R' and has a scale height H' and a surface density Σ' . The same amount of material must still be below the parcel:

$$\frac{1}{2} \Sigma' \text{erf}\left(\frac{z'}{H'\sqrt{2}}\right) = \frac{1}{2} \Sigma \text{erf}\left(\frac{z}{H\sqrt{2}}\right). \quad (27)$$

Rearranging gives the new height of the parcel, z' :

$$z'(R', t') = H' \sqrt{2} \text{erf}^{-1}\left[\frac{\Sigma}{\Sigma'} \text{erf}\left(\frac{z}{H\sqrt{2}}\right)\right], \quad (28)$$

where erf^{-1} is the inverse of the error function. In the absence of mixing, our description leads to purely laminar flow.

The location of the disk-envelope boundary (needed, for instance, in Eq. (19)) is determined in two steps. First, the surface is identified where the density due to the disk (Eq. (24)) equals

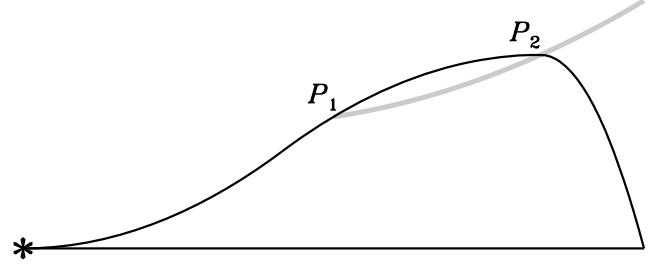


Fig. 1. Schematic view of the disk-envelope boundary in the (R, z) plane. The black line indicates the surface where the density due to the disk equals that due to the envelope. The grey line is the infall trajectory that would lead to point P_1 . However, it already intersects the disk at point P_2 , so no accretion is possible at P_1 . The disk-envelope boundary is therefore raised at P_1 until it can be reached freely by an infall trajectory.

that due to the envelope (Eqs. (5) and (12)). In order for accretion to take place at a given point P_1 on the surface, it must be intersected by an infall trajectory. Due to the geometry of the surface, such a trajectory might also intersect the disk at a larger radius P_2 (Fig. 1). Material flowing in along that trajectory will accrete at P_2 instead of P_1 . Hence, the second step in determining the disk-envelope boundary consists of raising the surface at “obstructed points” like P_1 to an altitude where accretion can take place. The source function is then computed at that altitude. Physically, this can be understood as follows: the region directly above the obstructed points becomes less dense than what it would be in the absence of a disk, because the disk also prevents material from reaching there. The lower density above the disk reduces the downward pressure, so the disk puffs up and the disk-envelope boundary moves to a higher altitude.

The infall trajectories in the vicinity of the disk are very shallow, so the bulk of the material accretes at the outer edge. Because the disk quickly spreads beyond the centrifugal radius, much of the accretion occurs far from the star. In contrast, accretion in one-dimensional collapse models occurs at or inside of R_c . Our results are consistent with the hydrodynamical work of [BWH08](#), where most of the infalling material also hits the outer edge of a rather large disk. The large accretion radii lead to weaker accretion shocks than commonly assumed (Sect. 2.5).

2.3. Star

The star gains material from the envelope and from the disk, so its mass evolves as

$$M_*(t) = \int_0^t (\dot{M}_{e \rightarrow *} + \dot{M}_{d \rightarrow *}) dt'. \quad (29)$$

The protostar does not come into existence immediately at the onset of collapse; it is preceded by the first hydrostatic core (FHC; [Masunaga et al. 1998](#); [Boss & Yorke 1995](#)). Our model follows [YE05](#) and takes a lifetime of 2×10^4 yr and a size of 5 AU for the FHC, independent of other parameters. After this stage, a rapid transition occurs from the large FHC to a protostar of a few R_\odot :

$$R_* = (5 \text{ AU}) \left(1 - \sqrt{\frac{t - 20\,000 \text{ yr}}{100 \text{ yr}}}\right) + R_*^{\text{PS}} \quad (30)$$

$20\,000 < t \text{ (yr)} < 20\,100$,

where R_*^{PS} (ranging from 2 to 5 R_\odot) is the protostellar radius from [Palla & Stahler \(1991\)](#). For $t > 2.01 \times 10^4$ yr, R_* equals R_*^{PS} .

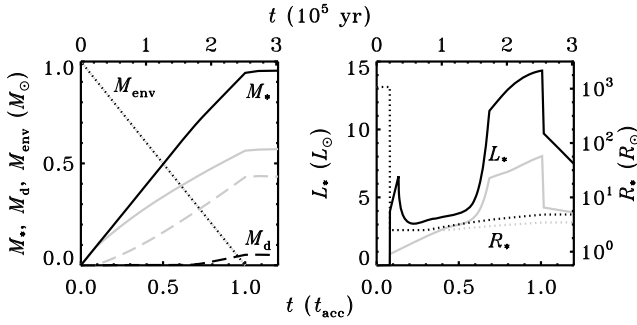


Fig. 2. Evolution of the mass of the envelope, star and disk (left panel) and the luminosity (solid lines) and radius (dotted lines) of the star (right panel) for our standard model (black lines) and our reference model (grey lines).

Our results are not sensitive to the exact values used for the size and lifetime of the FHC or the duration of the FHC-protostar transition.

The star's luminosity, L_* , consists of two terms: the accretion luminosity, $L_{*,\text{acc}}$, dominant at early times, and the luminosity due to gravitational contraction and deuterium burning, L_{phot} . The accretion luminosity comes from Adams & Shu (1986):

$$L_{*,\text{acc}}(t) = L_0 \left\{ \frac{1}{6u_*} [6u_* - 2 + (2 - 5u_*) \sqrt{1 - u_*}] + \frac{\eta_*}{2} [1 - (1 - \eta_d) \mathcal{M}_d] [1 - (1 - \eta_d) \sqrt{1 - u_*}] \right\}, \quad (31)$$

where $L_0 = GMM/R_*$ (with M the total accreted mass, i.e., $M = M_* + M_d$), $u_* = R_*/R_c$, and

$$\mathcal{M}_d = \frac{1}{3} u_*^{1/3} \int_{u_*}^1 \frac{\sqrt{1 - u}}{u^{4/3}} du. \quad (32)$$

Analytical solutions exist for the asymptotic cases of $u_* \approx 0$ and $u_* \approx 1$. For intermediate values, the integral must be solved numerically. The efficiency parameters η_* and η_d in Eq. (31) have values of 0.5 and 0.75 for a $1 M_\odot$ envelope (YE05). The photospheric luminosity is adopted from D'Antona & Mazzitelli (1994), using YE05's method of fitting and interpolating, including a time difference of $0.38 t_{\text{acc}}$ (equal to the free-fall time) between the onset of $L_{*,\text{acc}}$ and $L_{*,\text{phot}}$ (Myers et al. 1998). The sum of these two terms gives the total stellar luminosity:

$$L_*(t) = L_{*,\text{acc}} + L_{*,\text{phot}}. \quad (33)$$

Figure 2 shows the evolution of the stellar mass, luminosity and radius for our standard case of $M_0 = 1.0 M_\odot$, $c_s = 0.26 \text{ km s}^{-1}$ and $\Omega_0 = 10^{-14} \text{ s}^{-1}$, and our reference case of $M_0 = 1.0 M_\odot$, $c_s = 0.26 \text{ km s}^{-1}$ and $\Omega_0 = 10^{-13} \text{ s}^{-1}$ (Sect. 2.6). The transition from the FHC to the protostar at $t = 2 \times 10^4 \text{ yr}$ is clearly visible in the R_* and L_* profiles. At $t = t_{\text{acc}}$, there is no more accretion from the envelope onto the star, so the luminosity decreases sharply.

The masses of the disk and the envelope are also shown in Fig. 2. Our disk mass of $0.43 M_\odot$ at $t = t_{\text{acc}}$ in the reference case is in excellent agreement with the value of $0.4 M_\odot$ found by BWH08 for the same parameters.

2.4. Temperature

The envelope starts out as an isothermal sphere at 10 K and it is heated up from the inside after the onset of collapse. Using the star as the only photon source, the dust temperature in the

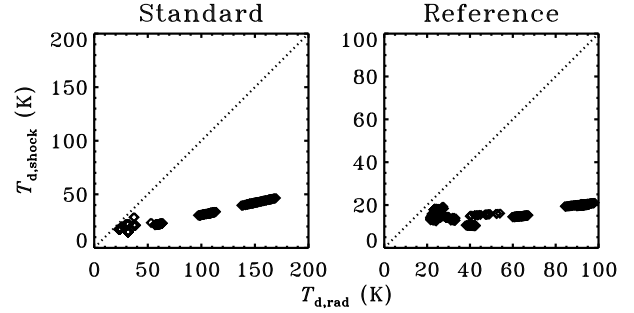


Fig. 3. Dust temperature due to the accretion shock (vertical axis) and stellar radiation (horizontal axis) at the point of entry into the disk for $0.1\text{-}\mu\text{m}$ grains in a sample of several hundred parcels in our standard (left) and reference (right) models. These parcels occupy positions from $R = 1$ to 300 AU in the disk at t_{acc} . Note the different scales between the two panels.

disk and envelope is computed with the axisymmetric three-dimensional radiative transfer code RADMC (Dullemond & Dominik 2004). Because of the high densities throughout most of the system, the gas and dust are expected to be well coupled, and the gas temperature is set equal to the dust temperature. Cosmic-ray heating of the gas is included implicitly by setting a lower limit of 8 K in the dust radiative transfer results. As mentioned in Sect. 2.1, the presence of the outflow cones has some effect on the temperature profiles (Whitney et al. 2003). This will be discussed further in Sect. 3.2.

2.5. Accretion shock

The infall of high-velocity envelope material into the low-velocity disk causes a J-type shock. The temperature right behind the shock front can be much higher than what it would be due to the stellar photons. Neufeld & Hollenbach (1994) calculated in detail the relationship between the pre-shock velocities and densities (u_s and n_s) and the maximum grain temperature reached after the shock ($T_{\text{d,s}}$). A simple formula, valid for $u_s < 70 \text{ km s}^{-1}$, can be extracted from their Fig. 13:

$$T_{\text{d,s}} \approx (104 \text{ K}) \left(\frac{n_s}{10^6 \text{ cm}^{-3}} \right)^{0.21} \left(\frac{u_s}{30 \text{ km s}^{-1}} \right)^p \left(\frac{a_{\text{gr}}}{0.1 \mu\text{m}} \right)^{-0.20}, \quad (34)$$

with a_{gr} the grain radius. The exponent p is 0.62 for $u_s < 30 \text{ km s}^{-1}$ and 1.0 otherwise.

The pre-shock velocities and densities are highest at early times, when accretion occurs close to the star and all ices would evaporate anyway. Important for our purposes is the question whether the dust temperature due to the shock exceeds that due to stellar heating. If all grains have a radius of $0.1 \mu\text{m}$, as assumed in our model, this is not the case for any of the material in the disk at t_{acc} for either our standard or our reference model (Fig. 3; cf. Simonelli et al. 1997).

In reality, the dust spans a range of sizes, extending down to a radius of about $0.005 \mu\text{m}$. Small grains are heated more easily; $0.005\text{-}\mu\text{m}$ dust reaches a shock temperature almost twice as high as does $0.1\text{-}\mu\text{m}$ dust (Eq. (34)). This is enough for the shock temperature to exceed the radiative heating temperature in part of the sample in Fig. 3. However, this has no effect on the CO and H_2O gas-ice ratios. In those parcels where shock heating becomes important for small grains, the temperature from radiative heating lies already above the CO evaporation temperature of about 18 K and the shock temperature remains below 60 K,

Table 1. Summary of the parameter grid used in our model^a.

Case ^b	Ω_0 (s ⁻¹)	c_s (km s ⁻¹)	M_0 (M_\odot)	t_{acc} (10 ⁵ yr)	τ_{ads} (10 ⁵ yr)	M_d (M_\odot)
1	10 ⁻¹⁴	0.19	1.0	6.3	14.4	0.22
2	10 ⁻¹⁴	0.19	0.5	3.2	3.6	0.08
3 (std)	10 ⁻¹⁴	0.26	1.0	2.5	2.3	0.05
4	10 ⁻¹⁴	0.26	0.5	1.3	0.6	0.001
5	10 ⁻¹³	0.19	1.0	6.3	14.4	0.59
6	10 ⁻¹³	0.19	0.5	3.2	3.6	0.25
7 (ref)	10 ⁻¹³	0.26	1.0	2.5	2.3	0.43
8	10 ⁻¹³	0.26	0.5	1.3	0.6	0.16

^a Ω_0 : solid-body rotation rate; c_s : effective sound speed; M_0 : initial envelope mass; t_{acc} : accretion time; τ_{ads} : adsorption timescale for H₂O at the edge of the initial cloud; M_d : disk mass at t_{acc} .

^b Case 3 is our standard parameter set and Case 7 is our reference set.

which is not enough for H₂O to evaporate. Hence, shock heating is not included in our model.

H₂O may also be removed from the grain surfaces in the accretion shock through sputtering (Tielens et al. 1994; Jones et al. 1994). The material that makes up the disk at the end of the collapse in our standard model experiences a shock of at most 8 km s⁻¹. At that velocity, He⁺, the most important ion for sputtering, carries an energy of 1.3 eV. However, a minimum of 2.2 eV is required to remove H₂O (Bohdansky et al. 1980), so sputtering is unimportant for our purposes.

Some of the material in our model is heated to more than 100 K during the collapse (Fig. 12) or experiences a shock strong enough to induce sputtering. This material normally ends up in the star before the end of the collapse, but mixing may keep some of it in the disk. The possible consequences are discussed briefly in Sect. 4.4.

2.6. Model parameters

The standard set of parameters for our model corresponds to Case J from Yorke & Bodenheimer (1999), except that the solid-body rotation rate is reduced from 10⁻¹³ to 10⁻¹⁴ s⁻¹ to produce a more realistic disk mass of 0.05 M_\odot , consistent with observations (e.g. Andrews & Williams 2007a,b). The envelope has an initial mass of 1.0 M_\odot and a radius of 6700 AU, and the effective sound speed is 0.26 km s⁻¹.

The original Case J (with $\Omega_0 = 10^{-13}$ s⁻¹), which was also used in BWH08, is used here as a reference model to enable a direct quantitative comparison of the results with an independent method. This case results in a much higher disk mass of 0.43 M_\odot . Although such high disk masses are not excluded by observations and theoretical arguments (Hartmann et al. 2006), they are considered less representative of typical young stellar objects than the disks of lower mass.

The parameters M_0 , c_s and Ω_0 are changed in one direction each to create a 2³ parameter grid. The two values for Ω_0 , 10⁻¹⁴ and 10⁻¹³ s⁻¹, cover the range of rotation rates observed by Goodman et al. (1993). The other variations are chosen for their opposite effect: a lower sound speed gives a more massive disk, and a lower initial mass gives a less massive disk. The full model is run for each set of parameters to analyse how the chemistry can vary between different objects. The parameter grid is summarised in Table 1. Our standard set is Case 3 and our reference set is Case 7.

Table 1 also lists the accretion time and the adsorption timescale for H₂O at the edge of the initial envelope. For

comparison, Evans et al. (2009) found a median timescale for the embedded phase (Class 0 and I) of 5.4×10^5 yr from observations. It should be noted that the end point of our model (t_{acc}) is not yet representative of a typical T Tauri disk (see Sect. 3.2). Nevertheless, it allows an exploration of how the chemistry responds to plausible changes in the environment.

2.7. Adsorption and desorption

The adsorption and desorption of CO and H₂O are solved in a Lagrangian frame. When the time-dependent density, velocity and temperature profiles have been calculated, the envelope is populated by a number of parcels of material (typically 12 000) at $t = 0$. They fall in towards the star or disk according to the velocity profiles. The density and temperature along each parcel's infall trajectory are used as input to solve the adsorption-desorption balance. Both species start fully in the gas phase. The envelope is kept static for 3×10^5 yr before the onset of collapse to simulate the pre-stellar core phase. This is the same value as used by Rodgers & Charnley (2003) and BWH08, and it is consistent with recent observations by Enoch et al. (2008). The amount of gaseous material left over near the end of the pre-collapse phase is also consistent with observations, which show that the onset of H₂O ice formation is around an A_V of 3 (Whittet et al. 2001). In six of our eight parameter sets, the adsorption timescales of H₂O at the edge of the cloud are shorter than the combined collapse and pre-collapse time (Table 1), so all H₂O is expected to freeze out before entering the disk. Because of the larger cloud size, the adsorption timescales are much longer in Cases 1 and 5, and some H₂O may still be in the gas phase when it reaches the disk.

No chemical reactions are included other than adsorption and thermal desorption, so the total abundance of CO and H₂O in each parcel remains constant. The adsorption rate in cm⁻³ s⁻¹ is taken from Charnley et al. (2001):

$$R_{\text{ads}}(X) = (4.55 \times 10^{-18} \text{ cm}^3 \text{ K}^{-1/2} \text{ s}^{-1}) n_{\text{H}} n_{\text{g}}(X) \sqrt{\frac{T_{\text{g}}}{M(X)}}, \quad (35)$$

where n_{H} is the total hydrogen density, T_{g} the gas temperature, $n_{\text{g}}(X)$ the gas-phase abundance of species X and $M(X)$ its molecular weight. The numerical factor assumes unit sticking efficiency, a grain radius of 0.1 μm and a grain abundance n_{gr} of 10⁻¹² with respect to H₂.

The thermal desorption of CO and H₂O is a zeroth-order process:

$$R_{\text{des}}(X) = (1.26 \times 10^{-21} \text{ cm}^2) n_{\text{H}} f(X) \nu(X) \exp\left[-\frac{E_{\text{b}}(X)}{kT_{\text{d}}}\right], \quad (36)$$

where T_{d} is the dust temperature and

$$f(X) = \min\left[1, \frac{n_{\text{s}}(X)}{N_{\text{b}} n_{\text{gr}}}\right], \quad (37)$$

with $n_{\text{s}}(X)$ the solid abundance of species X and $N_{\text{b}} = 10^6$ the typical number of binding sites per grain. The numerical factor in Eq. (36) assumes the same grain properties as in Eq. (35). The pre-exponential factor, $\nu(X)$, and the binding energy, $E_{\text{b}}(X)/k$, are set to $7 \times 10^{26} \text{ cm}^{-2} \text{ s}^{-1}$ and 855 K for CO and to $1 \times 10^{30} \text{ cm}^{-2} \text{ s}^{-1}$ and 5773 K for H₂O (Bisschop et al. 2006; Fraser et al. 2001).

Using a single $E_{\text{b}}(\text{CO})$ value means that all CO evaporates at the same temperature. This would be appropriate for a pure

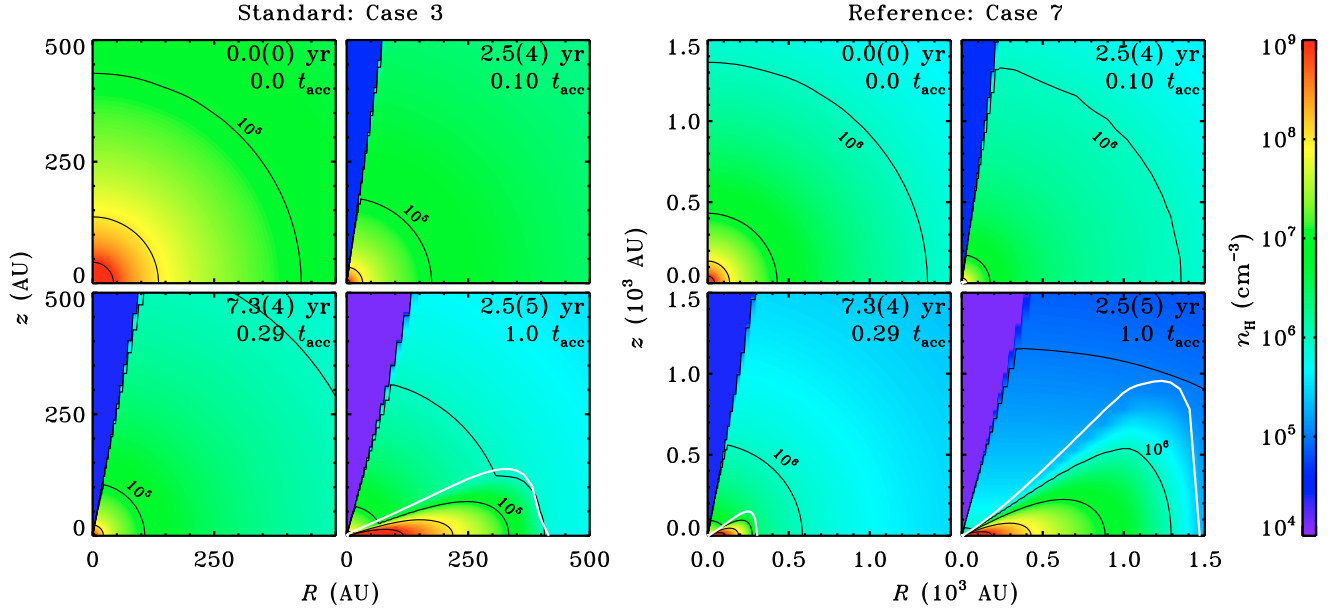


Fig. 4. Total density at four time steps for our standard model (Case 3; *left*) and our reference model (Case 7; *right*). The time is given in years as well as in units of the accretion time, with $a(b)$ meaning $a \times 10^b$. The density contours increase by factors of ten going inwards; the 10^5-cm^{-3} contours are labelled in the standard panels and the 10^6-cm^{-3} contours in the reference panels. The white curves indicate the surface of the disk as defined in Sect. 2.2 (only visible in three panels). Note the different scale between the two sets of panels.

Table 2. Binding energies and desorbing fractions for the four-flavour CO evaporation model^a.

Flavour	$E_b(\text{CO})/k \text{ (K)}^b$	Fraction ^c
1	855	0.350
2	960	0.455
3	3260	0.130
4	5773	0.065

^a Based on Viti et al. (2004).

^b The rates for Flavours 1–3 are computed from Eq. (36) with $X = \text{CO}$. The rate for Flavour 4 is equal to the H_2O desorption rate.

^c These numbers indicate fractions of adsorbing CO: 35% of all adsorbing CO becomes Flavour 1, and so on.

CO ice, but not for a mixed CO- H_2O ice as is likely to form in reality. During the warm-up phase, part of the CO is trapped inside the H_2O ice until the temperature becomes high enough for the H_2O to evaporate. Recent laboratory experiments suggest that CO desorbs from a CO- H_2O ice in four steps (Collings et al. 2004). This can be simulated with four “flavours” of CO ice, each with a different $E_b(\text{CO})$ value (Viti et al. 2004). For each flavour, the desorption is assumed to be zeroth order. The four-flavour model is summarised in Table 2.

3. Results

Results are presented in this section for our standard and reference models (Cases 3 and 7) as described in Sect. 2.6. These cases will be compared to the other parameter sets in Sect. 4.1. Appendix A describes a formula to estimate the disk formation efficiency, defined as M_d/M_0 at the end of the collapse phase, based on a fit to our model results.

3.1. Density profiles and infall trajectories

In our standard model (Case 3), the envelope collapses in 2.5×10^5 yr to give a star of $0.94 M_\odot$ and a disk of $0.05 M_\odot$. The remaining $0.01 M_\odot$ has disappeared through the bipolar outflow. The centrifugal radius in our standard model at t_{acc} is 4.9 AU, but the disk has spread to 400 AU at that time due to angular momentum redistribution. The densities in the disk are high: more than 10^9 cm^{-3} at the midplane inside of 120 AU (Fig. 4, left) and more than 10^{14} cm^{-3} near 0.3 AU. The corresponding surface densities of the disk are 2.0 g cm^{-2} at 120 AU and 660 g cm^{-2} at 0.3 AU.

Due to the higher rotation rate, our reference model (Case 7) gets a much higher disk mass: $0.43 M_\odot$. This value is consistent with the mass of $0.4 M_\odot$ reported by BWH08. Overall, the reference densities from our semi-analytical model (Fig. 4, right) compare well with those from their more realistic hydrodynamical simulations; the differences are generally less than a factor of two.

In both cases, the disk first emerges at 2×10^4 yr, when the FHC contracts to become the protostar, but it is not until a few 10^4 yr later that the disk becomes visible on the scale of Fig. 4. The regions of high density ($n_{\text{H}} > 10^5\text{--}10^6 \text{ cm}^{-3}$) are still contracting at that time, but the growing disks eventually cause them to expand again.

Material falls in along nearly radial streamlines far out in the envelope and deflects towards the midplane closer in. When a parcel enters the disk, it follows the radial motion caused by the viscous evolution and accretion of more material from the envelope. At any time, conservation of angular momentum causes part of the disk to move inwards and part of it to move outwards. An individual parcel entering the disk may move out for some time before going further in. This leads the parcel through several density and temperature regimes, which may affect the gas-ice ratios or the chemistry in general. The back-and-forth motion occurs especially at early times, when the entire system changes more rapidly than at later times. The parcel

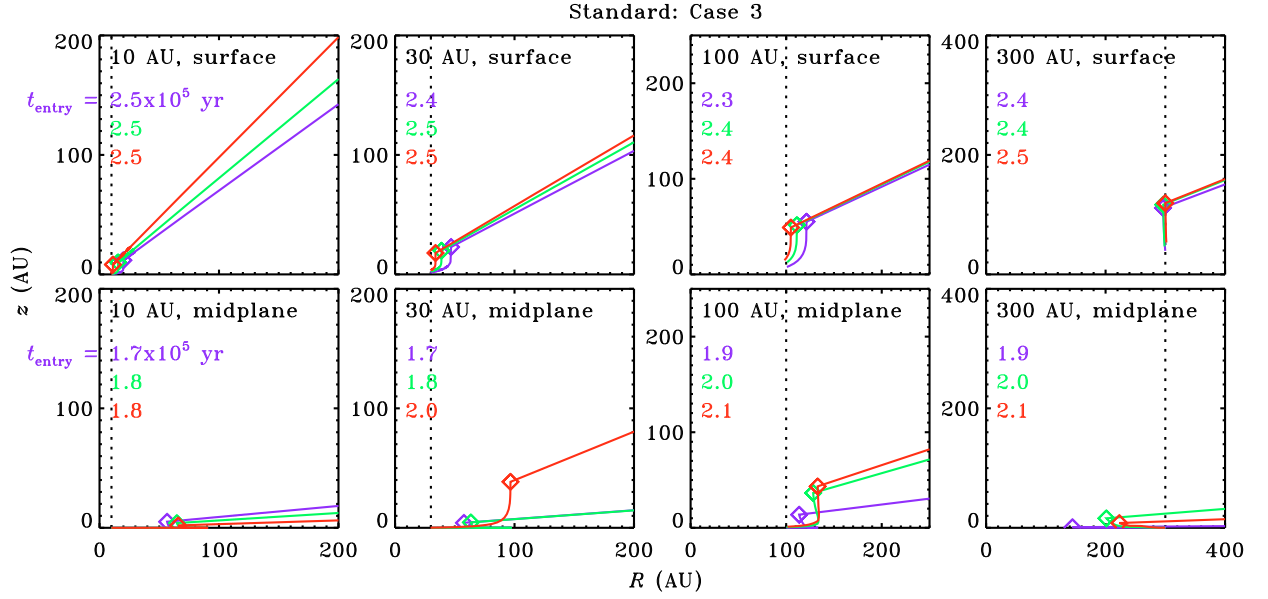


Fig. 5. Infall trajectories for parcels in our standard model (Case 3) ending up near the surface (*top panels*) or at the midplane (*bottom panels*) at radial positions of 10, 30, 100 and 300 AU (dotted lines) at $t = t_{\text{acc}}$. Each panel contains trajectories for three parcels, which are illustrative for material ending up at the given location. Trajectories are only drawn up to $t = t_{\text{acc}}$. Diamonds indicate where each parcel enters the disk; the time of entry is given in units of 10^5 yr. Note the different scales between some panels.

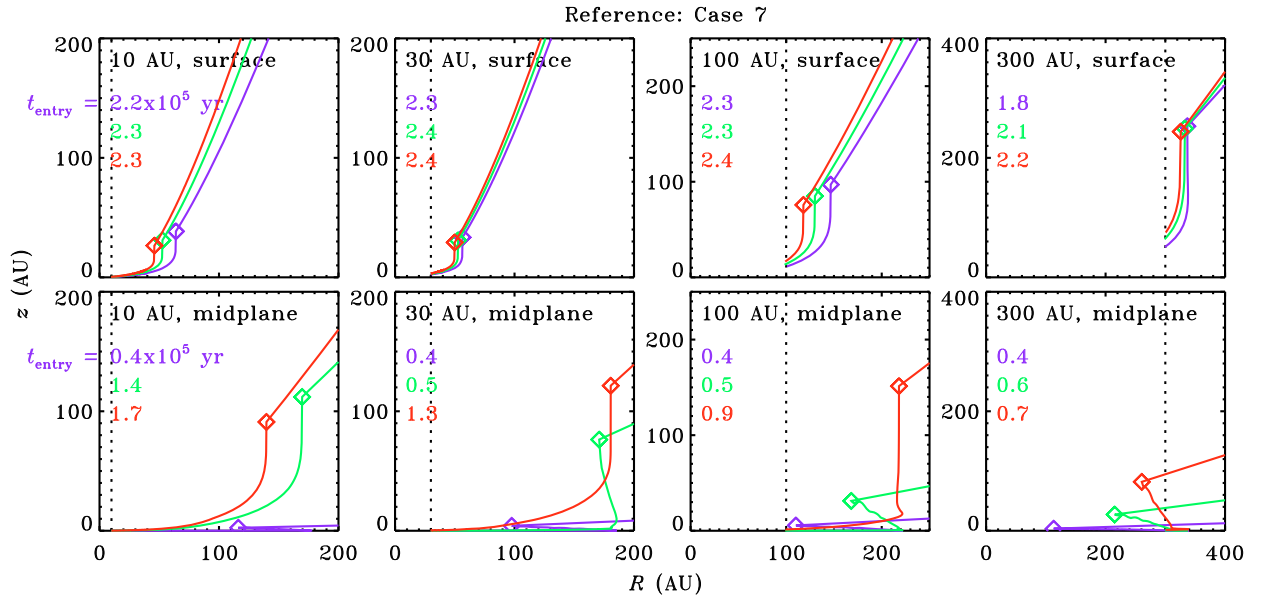


Fig. 6. Same as Fig. 5, but for our reference model (Case 7).

motions are visualised in Figs. 5 and 6, where infall trajectories are drawn for 24 parcels ending up at one of eight positions at t_{acc} : at the midplane or near the surface at radial distances of 10, 30, 100 and 300 AU. Only parcels entering the disk before $t \approx 2 \times 10^5$ yr in our standard model or $t \approx 1 \times 10^5$ yr in our reference model undergo the back-and-forth motion. The parcels ending up near the midplane all entered the disk earlier than the ones ending up at the surface.

Accretion from the envelope onto the disk occurs in an inside-out fashion. Because of the geometry of the disk (Fig. 1), most of the material enters near the outer edge and prevents the older material from moving further out. Our flow inside the disk is purely laminar, so some material near the midplane does move outwards underneath the newer material at higher altitudes.

Because of the low rotation rate in our standard model, the disk does not really begin to build up until 1.5×10^5 yr ($0.6 t_{\text{acc}}$) after the onset of collapse. In addition, most of the early material to reach the disk proceeds onto the star before the end of the accretion phase, so the disk at t_{acc} consists only of material from the edge of the original cloud (Fig. 7, left two panels).

The disk in our reference model, however, begins to form right after the FHC-protostar transition at 2×10^4 yr. As in the standard model, a layered structure is visible in the disk, but it is more pronounced here. At the end of the collapse, the midplane consists mostly of material that was originally close to the centre of the envelope (Fig. 7, right two panels). The surface and outer parts of the disk are made up primarily of material from the outer parts of the envelope. This was also reported by BWH08.

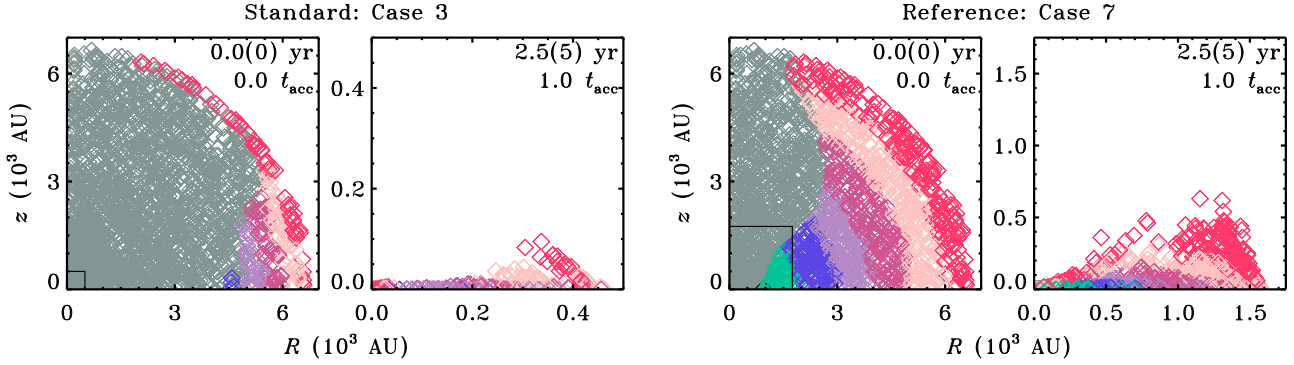


Fig. 7. Position of parcels of material in our standard model (Case 3; *left*) and our reference model (Case 7; *right*) at the onset of collapse ($t = 0$) and at the end of the collapse phase ($t = t_{acc}$). The parcels are colour-coded according to their initial position. The grey parcels from $t = 0$ are in the star or have disappeared through the outflow at $t = t_{acc}$. Note the different spatial scale between the two panels of each set; the small box in the *left* panel indicates the scale of the *right* panel.

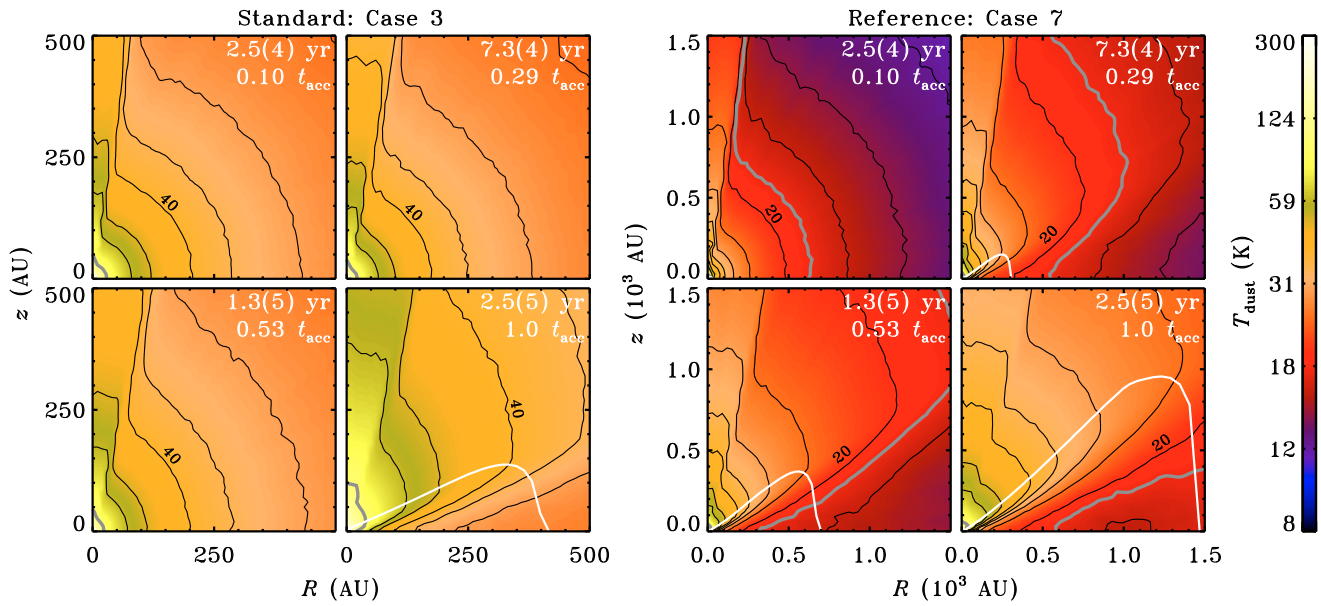


Fig. 8. Dust temperature, as in Fig. 4. Contours are drawn at 100, 60, 50, 40, 35, 30, 25, 20, 18, 16, 14 and 12 K. The 40- and 20-K contours are labelled in the standard and reference panels, respectively. The 18- and 100-K contours are drawn as thick grey lines. The white curves indicate the surface of the disk as defined in Sect. 2.2 (only visible in four panels).

3.2. Temperature profiles

When the star turns on at 2×10^4 yr, the envelope quickly heats up and reaches more than 100 K inside of 10 AU. As the disk grows, its interior is shielded from direct irradiation and the mid-plane cools down again. At the same time, the remnant envelope material above the disk becomes less dense and warmer. As in Whitney et al. (2003), the outflow has some effect on the temperature profile. Photons emitted into the outflow can scatter and illuminate the disk from the top, causing a higher disk temperature beyond $R \approx 200$ AU than if there were no outflow cone. At smaller radii, the disk temperature is lower than in a no-outflow model. Without the outflow, the radiation would be trapped in the inner envelope and inner disk, increasing the temperature at small radii.

At $t = t_{acc}$ in our standard model, the 100- and 18-K isotherms (where H_2O and pure CO evaporate) intersect the mid-plane at 20 and 2000 AU (Fig. 8, left). The disk in our reference model is denser and therefore colder: it reaches 100 and 18 K at 5 and 580 AU on the midplane (Fig. 8, right). Our radiative transfer method is a more rigorous way to obtain the dust

temperature than the diffusion approximation used by BWH08, so our temperature profiles are more realistic than theirs.

Compared to typical T Tauri disk models (e.g. D’Alessio et al. 1998, 1999, 2001), our standard disk at t_{acc} is warmer. It is 81 K at 30 AU on the midplane, while the closest model from the D’Alessio catalogue is 28 K at that point. If our model is allowed to run beyond t_{acc} , part of the disk accretes further onto the star. At $t = 4 t_{acc}$ (10^6 yr), the disk mass goes down to $0.03 M_\odot$. The luminosity of the star decreases during this period (D’Antona & Mazzitelli 1994), so the disk cools down: the midplane temperature at 30 AU is now 42 K. Meanwhile, the dust is likely to grow to larger sizes, which would further decrease the temperatures (D’Alessio et al. 2001). Hence, it is important to realise that the normal end point of our models does not represent a “mature” T Tauri star and disk as typically discussed in the literature.

3.3. Gas and ice abundances

Our two species, CO and H_2O , begin entirely in the gas phase. They freeze out during the static pre-stellar core phase from the

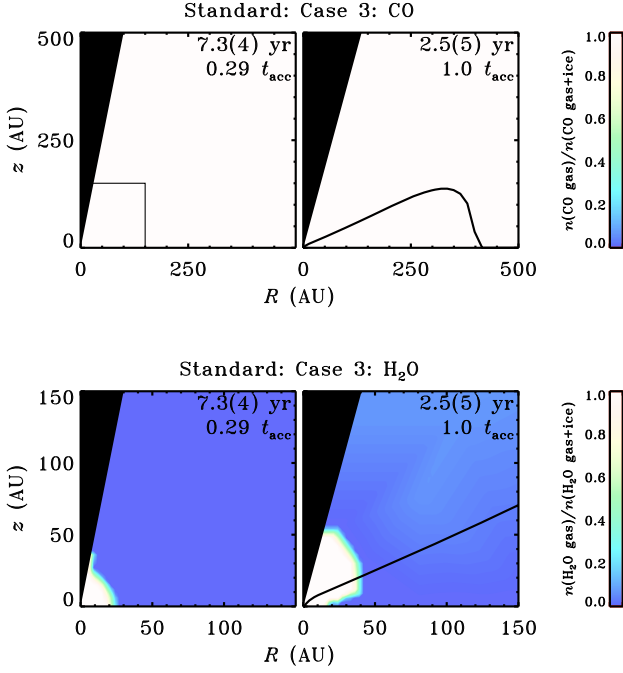


Fig. 9. Gaseous CO as a fraction of the total CO abundance (*top*) and idem for H₂O (*bottom*) at two time steps for our standard model (Case 3). The black curves indicate the surface of the disk (only visible in two panels). The black area near the pole is the outflow, where no abundances are computed. Note the different spatial scale between the two panels of each set; the small box in the left CO panel indicates the scale of the H₂O panels.

centre outwards due to the density dependence of Eq. (35). After the pre-collapse phase of 3×10^5 yr, only a few tenths of per cent of each species is still in the gas phase at 3000 AU. About 30% remains in the gas phase at the edge of the envelope.

Up to the point where the disk becomes important and the system loses its spherical symmetry, our model gives the same results as the one-dimensional collapse models: the temperature quickly rises to a few tens of K in the collapsing region, driving some CO (evaporating around 18 K in the one-flavour model) into the gas phase, but keeping H₂O (evaporating around 100 K) on the grains.

As the disk grows in mass, it provides an increasingly large body of material that is shielded from the star’s radiation, and that is thus much colder than the surrounding envelope. However, the disk in our standard model never gets below 18 K before the end of the collapse (Sect. 3.2), so CO remains in the gas phase (Fig. 9, top). Note that trapping of CO in the H₂O ice is not taken into account here; this possibility will be discussed in Sect. 4.3.

The disk in our reference model is more massive and therefore colder. After about 5×10^4 yr, the outer part drops below 18 K. CO arriving in this region re-adsorbs onto the grains (Fig. 10, top). Another 2×10^5 yr later, at $t = t_{\text{acc}}$, 19% of all CO in the disk is in solid form. Moving out from the star, the first CO ice is found at the midplane at 400 AU. The solid fraction gradually increases to unity at 600 AU. At $R = 1000$ AU, nearly all CO is solid up to an altitude of 170 AU. The solid and gaseous CO regions meet close to the 18-K surface. The densities throughout most of the disk are high enough that once a parcel of material goes below the CO desorption temperature, all CO rapidly disappears from the gas. The exception to this rule occurs at the outer edge, near 1500 AU, where the adsorption and

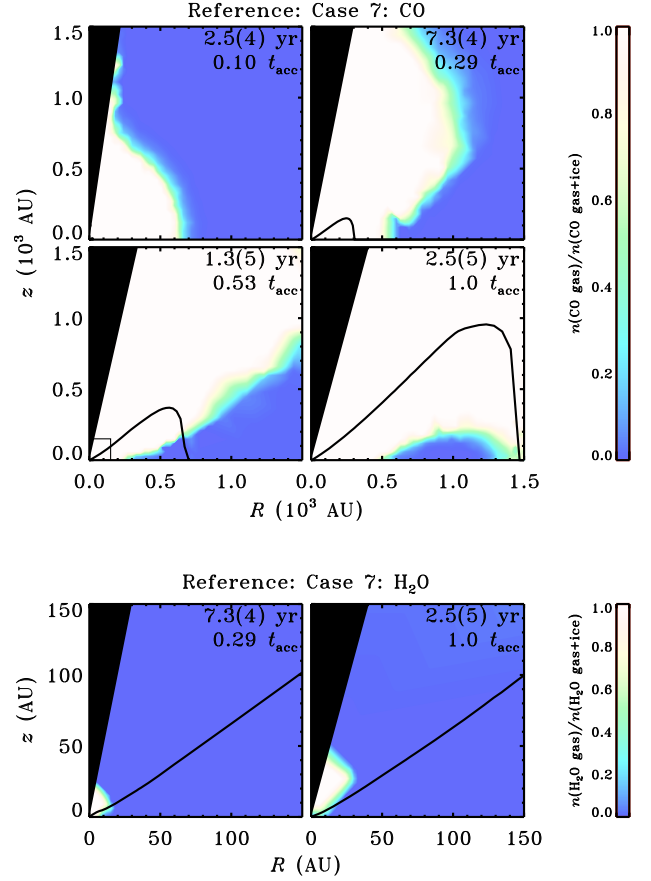


Fig. 10. Same as Fig. 9, but for our reference model (Case 7). The CO gas fraction is plotted on a larger scale and at two additional time steps.

desorption timescales are longer than the dynamical timescales of the infalling material. Small differences between the trajectories of individual parcels then cause some irregularities in the gas-ice profile.

The region containing gaseous H₂O is small at all times during the collapse. At $t = t_{\text{acc}}$, the snow line (the transition of H₂O from gas to ice) lies at 15 AU at the midplane in our standard model (Fig. 9, bottom). The surface of the disk holds gaseous H₂O out to $R = 41$ AU, and overall 13% of all H₂O in the disk is in the gas phase. This number is much lower in the colder disk of our reference model: only 0.4%. The snow line now lies at 7 AU and gaseous H₂O can be found out to 17 AU in the disk’s surface layers (Fig. 10, bottom).

Using the adsorption-desorption history of all the individual infalling parcels, the original envelope can be divided into several chemical zones. This is trivial for our standard model. All CO in the disk is in the gas phase and it has the same qualitative history: it freezes out before the onset of collapse and quickly evaporates as it falls in. H₂O also freezes out initially and only returns to the gas phase if it reaches the inner disk.

Our reference model has the same general H₂O adsorption-desorption history, but it shows more variation for CO, as illustrated in Fig. 11. For the red parcels in that figure, more than half of the CO always remains on the grains after the initial freeze-out phase. On the other hand, more than half of the CO comes off the grains during the collapse for the green parcels, but it freezes out again inside the disk. The pink parcels, ending up in the inner disk or in the upper layers, remain warm enough to keep CO off the grains once it first evaporates. The blue parcels

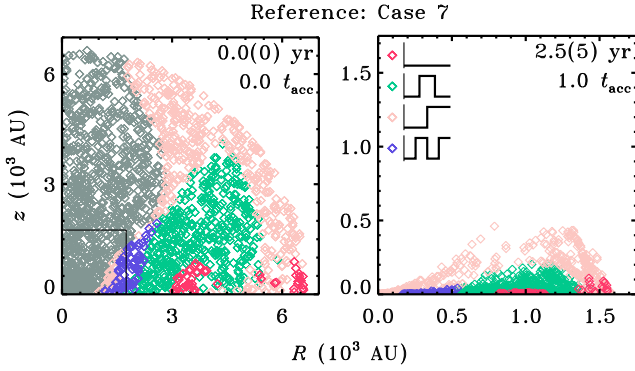


Fig. 11. Same as Fig. 7, but only for our reference model (Case 7) and with a different colour scheme to denote the CO adsorption-desorption behaviour. In all parcels, CO adsorbs during the pre-collapse phase. Red parcels: CO remains adsorbed; green parcels: CO desorbs and re-adsorbs; pink parcels: CO desorbs and remains desorbed; blue parcels: CO desorbs, re-adsorbs and desorbs once more. The fraction of gaseous CO in each type of parcel as a function of time is indicated schematically in the inset in the right panel. The grey parcels from $t = 0$ are in the star or have disappeared through the outflow at $t = t_{\text{acc}}$. In our standard model (Case 3), all CO in the disk at t_{acc} is in the gas phase and it all has the same qualitative adsorption-desorption history, equivalent to the pink parcels.

follow a more erratic temperature profile, with CO evaporating, re-adsorbing and evaporating a second time. This is related to the back-and-forth motion of some material in the disk (Fig. 6).

3.4. Temperature histories

The proximity of the CO and H₂O gas-ice boundaries to the 18- and 100-K surfaces indicates that the temperature is primarily responsible for the adsorption and desorption. At $n_{\text{H}} = 10^6 \text{ cm}^{-3}$, adsorption and desorption of CO are equally fast at $T_{\text{d}} = 18 \text{ K}$ (a timescale of $9 \times 10^3 \text{ yr}$). For a density a thousand times higher or lower, the dust temperature only has to increase or decrease by 2–3 K to maintain $k_{\text{ads}} = k_{\text{des}}$.

The exponential temperature dependence in the desorption rate (Eq. (36)) also holds for other species than CO and H₂O, as well as for the rates of some chemical reactions. Hence, it is useful to compute the temperature history for infalling parcels that occupy a certain position at t_{acc} . Figures 12 and 13 show these histories for material ending up at the midplane or near the surface of the disk at radial distances of 10, 30, 100 and 300 AU. Parcels ending up inside of 10 AU have a very similar temperature history as those ending up at 10 AU, except that the final temperature of the former is higher.

Each panel in Figs. 12 and 13 contains the history of several dozen parcels ending up close to the desired position. The qualitative features are the same for all parcels. The temperature is low while a parcel remains far out in the envelope. As it falls in with an ever higher velocity, there is a temperature spike as it traverses the inner envelope, followed by a quick drop once it enters the disk. Inward radial motion then leads to a second temperature rise; because of the proximity to the star, this one is higher than the first increase. For most parcels in Figs. 12 and 13, the second temperature peak does not occur until long after t_{acc} . In all cases, the shock encountered upon entering the disk is weak enough that it does not heat the dust to above the temperature caused by the stellar photons (Fig. 3).

Based on the temperature histories, the gas-ice transition at the midplane would lie inside of 10 AU for H₂O and beyond 300 AU for CO in both our models. This is indeed where they were found to be in Sect. 3.3. The transition for a species with an intermediate binding energy, such as H₂CO, is then expected to be between 10 and 100 AU, if its abundance can be assumed constant throughout the collapse.

The dynamical timescales for the infalling material before it enters the disk are between 10^4 and 10^5 yr . The timescales decrease as it approaches the disk, due to the rapidly increasing velocities. Once inside the disk, the material slows down again and the dynamical timescales return to 10^4 – 10^5 yr . The adsorption timescales for CO and H₂O are initially a few 10^5 yr , so they exceed the dynamical timescale before entering the disk. Depletion occurs nonetheless because of the pre-collapse phase with a duration of $3 \times 10^5 \text{ yr}$. The higher densities in the disk cause the adsorption timescales to drop to 100 yr or less. If the temperature approaches (or crosses) the desorption temperature for CO or H₂O, the corresponding desorption timescale becomes even shorter than the adsorption timescale. Overall, the timescales for these specific chemical processes (adsorption and desorption) in the disk are shorter by a factor of 1000 or more than the dynamical timescales.

At some final positions, there is a wide spread in the time that the parcels spend at a given temperature. This is especially true for parcels ending up near the midplane inside of 100 AU in our reference model. All of the midplane parcels ending up near 10 AU exceed 18 K during the collapse; the first one does so at $3.5 \times 10^4 \text{ yr}$ after the onset of collapse, the last one at $1.6 \times 10^5 \text{ yr}$. Hence, some parcels at this final position spend more than twice as long above 18 K than others. This does not appear to be relevant for the gas-ice ratio, but it is important for the formation of more complex species (Garrod & Herbst 2006). This will be discussed in more detail in Sect. 4.2.

4. Discussion

4.1. Model parameters

When the initial conditions of our model are modified (Sect. 2.6), the qualitative chemistry results do not change. In Cases 3, 4 and 8, the entire disk at t_{acc} is warmer than 18 K, and it contains no solid CO. In the other cases, the disk provides a reservoir of relatively cold material where CO, which evaporates early on in the collapse, can return to the grains. H₂O can only desorb in the inner few AU of the disk and remnant envelope.

Figures 14 and 15 show the density and dust temperature at t_{acc} for each parameter set; our standard and reference models are the top and bottom panel in the second column (Case 3 and 7). Several trends are visible:

- with a lower sound speed (Cases 1, 2, 5 and 6), the overall accretion rate (\dot{M}) is smaller so the accretion time increases ($t_{\text{acc}} \propto c_s^{-3}$). The disk can now grow larger and more massive. In our standard model, the disk is $0.05 M_{\odot}$ at t_{acc} and extends to about 400 AU radially. Decreasing the sound speed to 0.19 km s^{-1} (Case 1) results in a disk of $0.22 M_{\odot}$ and nearly 2000 AU. The lower accretion rate also reduces the stellar luminosity. These effects combine to make the disk colder in the low- c_s cases;
- with a lower rotation rate (Cases 1–4), the infall occurs in a more spherically symmetric fashion. Less material is captured in the disk, which remains smaller and less massive. From our reference to our standard model, the disk

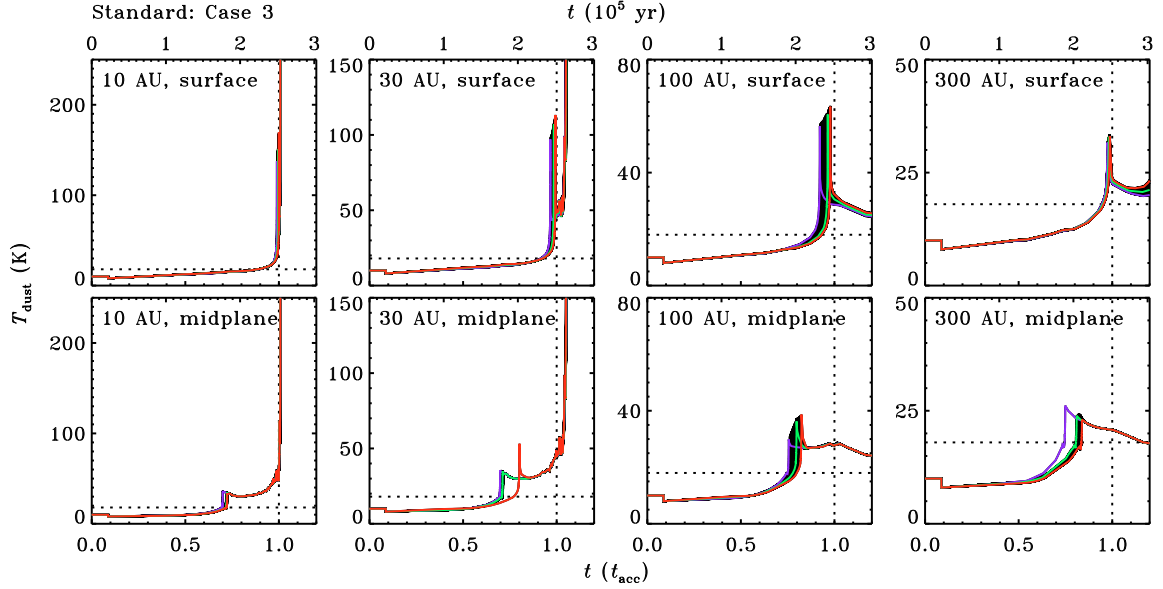


Fig. 12. Temperature history for parcels in our standard model (Case 3) ending up near the surface (*top panels*) or at the midplane (*bottom panels*) at radial positions of 10, 30, 100 and 300 AU at $t = t_{\text{acc}}$. Each panel contains between 22 and 90 curves; the coloured curves correspond to the parcels from Fig. 5. The dotted lines are drawn at $T_d = 18$ K and $t = t_{\text{acc}}$. Note the different vertical scales between some panels.

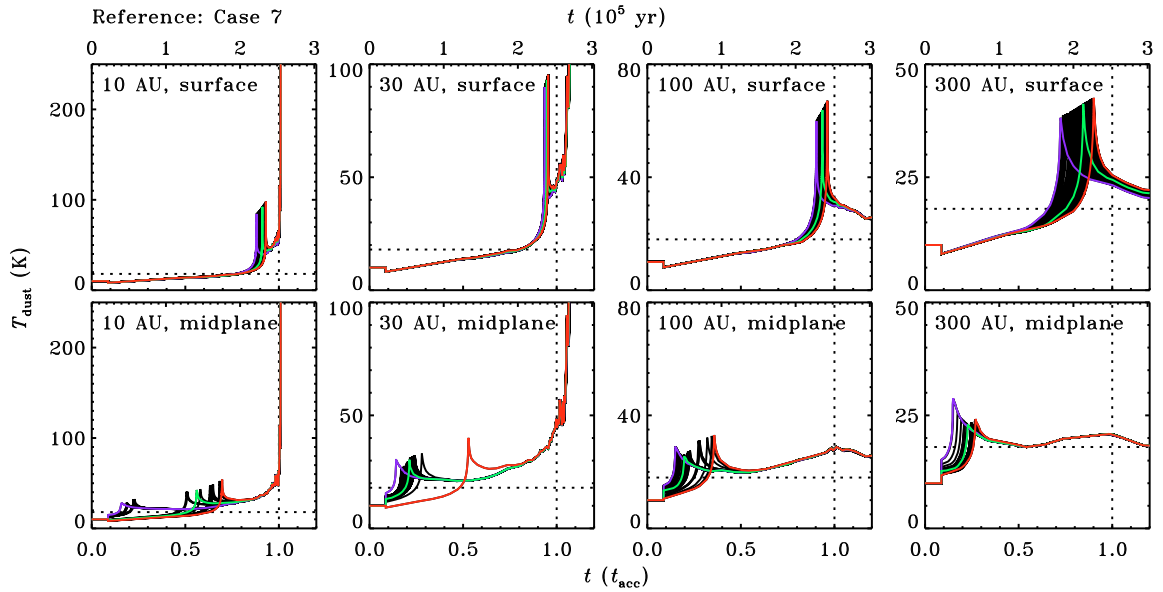


Fig. 13. Same as Fig. 12, but for our reference model (Case 7). The coloured curves correspond to the parcels from Fig. 6.

mass goes from 0.43 to $0.05 M_{\odot}$ and the radius from 1400 to 400 AU. The stronger accretion onto the star causes a higher luminosity. Altogether, this makes for a small, relatively warm disk in the low- Ω_0 cases;

- with a lower initial mass (Cases 2, 4, 6 and 8), there is less material to end up on the disk. The density profile is independent of the mass in a Shu-type collapse (Eq. (1)), so the initial mass is lowered by taking a smaller envelope radius. The material from the outer parts of the envelope is the last to accrete and is more likely, therefore, to end up in the disk. If the initial mass is halved relative to our standard model (as in Case 4), the resulting disk is only $0.001 M_{\odot}$ and 1 AU. Our reference disk goes from $0.43 M_{\odot}$ and 1400 AU to $0.16 M_{\odot}$ and 600 AU (Cases 7 and 8). The luminosity at t_{acc} is lower in the high- M_0 cases and the cold part of the disk ($T_d < 18$ K) has a somewhat larger relative size.

Dullemond et al. (2006) noted that accretion occurs closer to the star for a slowly rotating cloud than for a fast rotating cloud, resulting in a larger fraction of crystalline dust in the former case. The same effect is seen here, but overall the accretion takes place further from the star than in Dullemond et al. (2006). This is due to our taking into account the vertical structure of the disk. Our gaseous fractions in the low- Ω_0 disks are higher than in the high- Ω_0 disks (consistent with a higher crystalline fraction), but not because material enters the disk closer to the star. Rather, as mentioned above, the larger gas content comes from the higher temperatures throughout the disk.

Combining the density and the temperature, the fractions of cold ($T_d < 18$ K), warm ($T_d > 18$ K) and hot ($T_d > 100$ K) material in the disk can be computed. The warm and hot fractions are listed in Table 3 along with the fractions of gaseous CO and H₂O in the disk at t_{acc} . Across the parameter grid, 23–100% of

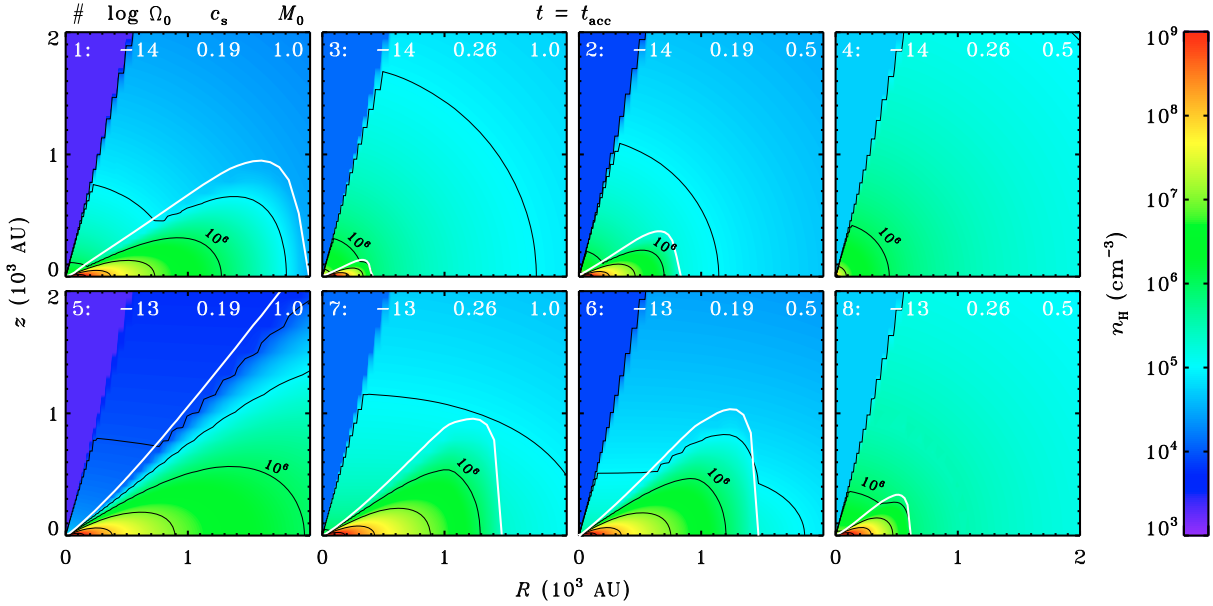


Fig. 14. Total density at $t = t_{\text{acc}}$ for each parameter set in our grid. The numbers at the top of each panel are the parameter set number, the rotation rate ($\log \Omega_0$ in s^{-1}), the sound speed (km s^{-1}) and the initial mass (M_\odot). The density contours increase by factors of ten going inwards; the 10^6-cm^{-3} contour is labelled in each panel. The white curves indicate the surfaces of the disks; the disk for Case 4 is too small to be visible.

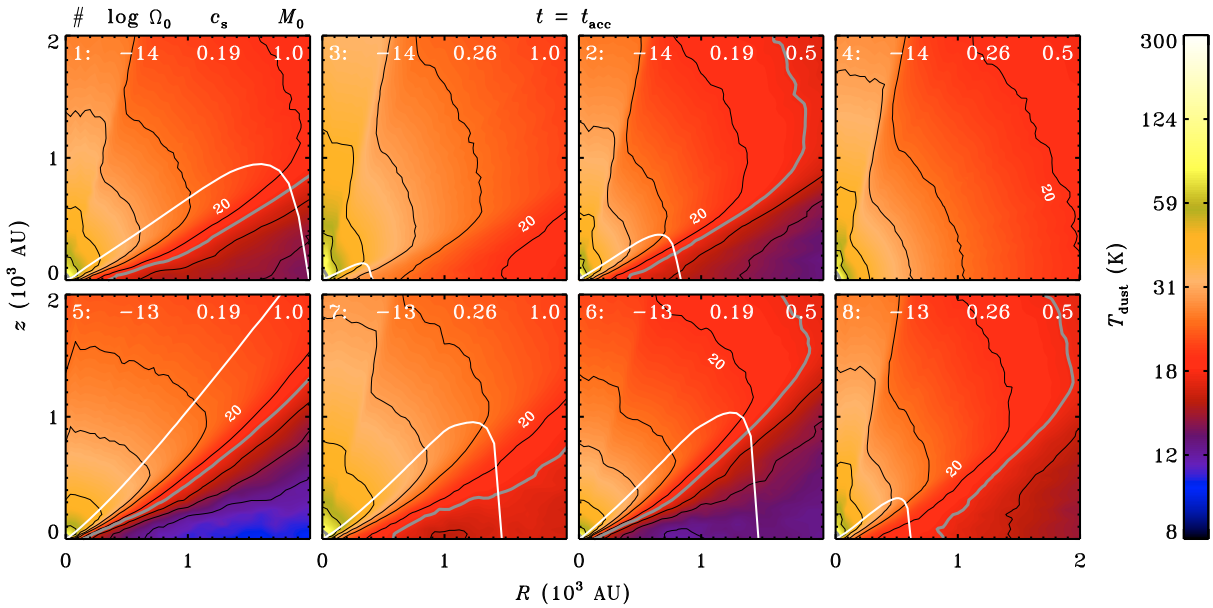


Fig. 15. Dust temperature, as in Fig. 14. The temperature contours are drawn at 100, 60, 40, 30, 25, 20, 18, 16, 14 and 12 K from the centre outwards; the 20-K contour is labelled in each panel.

the CO is in the gas, along with 0.3–100% of the H_2O . This includes Case 4, which only has a disk of $0.0014 M_\odot$. If that one is omitted, at most 13% of the H_2O in the disk at t_{acc} is in the gas. The gaseous H_2O fractions for Cases 1, 2, 6, 7 and 8 (at most a few per cent) are quite uncertain, because the model does not have sufficient resolution in the inner disk to resolve these small amounts. These fractions may be lower by up to a factor of 10 or higher by up to a factor of 3.

There is good agreement between the fractions of warm material and gaseous CO. In Case 5, about a third of the CO gas at t_{acc} is gas left over from the initial conditions, due to the long adsorption timescale for the outer part of the cloud. This is also the case for the majority of the gaseous H_2O in Cases 1, 5 and 6. For the other parameter sets, f_{hot} and $f_{\text{gas}}(\text{H}_2\text{O})$ are the same

within the error margins. Overall, the results from the parameter grid show once again that the adsorption-desorption balance is primarily determined by the temperature, and that the adsorption-desorption timescales are usually shorter than the dynamical timescales.

By comparing the fraction of gaseous material at the end of the collapse to the fraction of material above the desorption temperature, the history of the material is disregarded. For example, some of the cold material was heated above 18 K during the collapse, and CO desorbed before re-adsorbing inside the disk. This may affect the CO abundance if the model is expanded to include a full chemical network. In that case, the results from Table 3 only remain valid if the CO abundance is mostly constant throughout the collapse. The same caveat holds for H_2O .

Table 3. Summary of properties at $t = t_{\text{acc}}$ for our parameter grid^a.

Case	M_d/M^b	f_{warm}^c	f_{hot}^c	$f_{\text{gas}}(\text{CO})^d$	$f_{\text{gas}}(\text{H}_2\text{O})^d$
1	0.22	0.69	0.004	0.62	0.028
2	0.15	0.94	0.035	0.93	0.020
3 (std)	0.05	1.00	0.17	1.00	0.13
4	0.003	1.00	1.00	1.00	1.00
5	0.59	0.15	0.0001	0.23	0.11
6	0.50	0.34	0.0004	0.27	0.02
7 (ref)	0.43	0.83	0.003	0.81	0.004
8	0.33	1.00	0.028	1.00	0.003

^a These results are for the one-flavour CO desorption model.^b The fraction of the disk mass with respect to the total accreted mass ($M = M_* + M_d$).^c The fractions of warm ($T_d > 18$ K) and hot ($T_d > 100$ K) material with respect to the entire disk. The warm fraction also includes material above 100 K.^d The fractions of gaseous CO and H₂O with respect to the total amounts of CO and H₂O in the disk.

4.2. Complex organic molecules

A full chemical network is required to analyse the gas and ice abundances of more complex species. While this will be a topic for a future paper, the current CO and H₂O results, combined with recent other work, can already provide some insight.

In general, the formation of organic species can be divided into two categories: first-generation species that are formed on and reside in the grain surfaces, and second-generation species that are formed in the warm gas phase when the first-generation species have evaporated. Small first-generation species (like CH₃OH) are efficiently formed during the pre-collapse phase (Garrod & Herbst 2006). Their gas-ice ratios should be similar to that of H₂O, due to the similar binding energies.

Larger first-generation species such as methyl formate (HCOOCH₃) can be formed on the grains if material spends at least several 10⁴ yr at 20–40 K. The radicals involved in the surface formation of HCOOCH₃ (HCO and CH₃O) are not mobile enough at lower temperatures and are not formed efficiently enough at higher temperatures. A low surface abundance of CO (at temperatures above 18 K) does not hinder the formation of HCOOCH₃: HCO and CH₃O are formed from reactions of OH and H with H₂CO, which is already formed at an earlier stage and which does not evaporate until ~40 K (Garrod & Herbst 2006). Cosmic-ray-induced photons are available to form OH from H₂O even in the densest parts of the disk and envelope (Shen et al. 2004).

As shown in Sect. 3.4, many of the parcels ending up near the midplane inside of ~300 AU in our standard model spend sufficient time in the required temperature regime to allow for efficient formation of HCOOCH₃ and other complex organics. Once formed, these species are likely to assume the same gas-ice ratios as H₂O and the smaller organics. They evaporate in the inner 10–20 AU, so in the absence of mixing, complex organics would only be observable in the gas phase close to the star. The Atacama Large Millimeter/submillimeter Array (ALMA), currently under construction, will be able to test this hypothesis.

The gas-phase route towards complex organics involves the hot inner envelope ($T_d > 100$ K), also called the hot core or hot corino in the case of low-mass protostars (Ceccarelli 2004; Bottinelli et al. 2004, 2007). Most of the ice evaporates here and a rich chemistry can take place if material spends at least several 10³ yr in the hot core (Charnley et al. 1992). However, the material in the hot inner envelope in our model is essentially in

freefall towards the star or the inner disk, and its transit time of a few 100 yr is too short for complex organics to be formed abundantly (see also Schöier et al. 2002). Additionally, the total mass in this region is very low: about a per cent of the disk mass. In order to explain the observations of second-generation complex molecules, there has to be some mechanism to keep the material in the hot core for a longer time. Alternatively, it has recently been suggested that molecules typically associated with hot cores may in fact form on the grain surfaces as well (Garrod et al. 2008).

4.3. Mixed CO-H₂O ices

In the results presented in Sect. 3, all CO was taken to desorb at a single temperature. In a more realistic approach, some of it would be trapped in the H₂O ice and desorb at higher temperatures. This was simulated with four “flavours” of CO ice, as summarised in Table 2. With our four-flavour model, the global gas-ice profiles are mostly unchanged. All CO is frozen out in the sub-18 K regions and it fully desorbs when the temperature goes above 100 K. Some 10 to 20% remains in the solid phase in areas of intermediate temperature. In our standard model, the four-flavour variety has 15% of all CO in the disk at t_{acc} on the grains, compared to 0% in the one-flavour variety. In our reference model, the solid fraction increases from 19 to 33%.

The grain-surface formation of H₂CO, CH₃OH, HCOOCH₃ and other organics should not be very sensitive to these variations. H₂CO and CH₃OH are already formed abundantly before the onset of collapse, when the one- and four-flavour models predict equal amounts of solid CO. H₂CO is then available to form HCOOCH₃ (via the intermediates HCO and CH₃O) during the collapse. The higher abundance of solid CO at 20–40 K in the four-flavour model could slow down the formation of HCOOCH₃ somewhat, because CO destroys the OH needed to form HCO (Garrod & Herbst 2006). H₂CO evaporates around 40 K, so HCOOCH₃ cannot be formed efficiently anymore above that temperature. On the other hand, if a multiple-flavour approach is also employed for H₂CO, some of it remains solid above 40 K, and HCOOCH₃ can continue to be produced. Overall, then, the multiple-flavour desorption model is not expected to cause large variations in the abundances of these organic species compared to the one-flavour model.

4.4. Implications for comets

Comets in our solar system are known to be abundant in CO and they are believed to have formed between 5 and 30 AU in the circumsolar disk (Bockelée-Morvan et al. 2004; Kobayashi et al. 2007). However, the dust temperature in this region at the end of the collapse is much higher than 18 K for all of our parameter sets. This raises the question of how solid CO can be present in the comet-forming zone.

One possible answer lies in the fact that even at $t = t_{\text{acc}}$, our objects are still very young. As noted in Sect. 3.2, the disks will cool down as they continue to evolve towards “mature” T Tauri systems. Given the right set of initial conditions, this may bring the temperature below 18 K inside of 30 AU. However, there are many T Tauri disk models in the literature where the temperature at those radii remains well above the CO evaporation temperature (e.g. D’Alessio et al. 1998, 2001). Specifically, models of the minimum-mass solar nebula (MMSN) predict a dust temperature of ~40 K at 30 AU (Lecar et al. 2006).

A more plausible solution is to turn to mixed ices. At the temperatures computed for the comet-forming zone of the MMSN, 10–20% of all CO may be trapped in the H₂O ice. Assuming typical CO–H₂O abundance ratios, this is entirely consistent with observed cometary abundances (Bockelée-Morvan et al. 2004).

Large abundance variations are possible for more complex species, due to the different densities and temperatures at various points in the comet-forming zone in our model, as well as the different density and temperature histories for material ending up at those points. This seems to be at least part of the explanation for the chemical diversity observed in comets. Our current model will be extended in a forthcoming paper to include a full gas-phase chemical network to analyse these variations and compare them against cometary abundances.

The desorption and re-adsorption of H₂O in the disk-envelope boundary shock has been suggested as a method to trap noble gases in the ice and include them in comets (Owen et al. 1992; Owen & Bar-Nun 1993). As shown in Sects. 2.5 and 3.4, a number of parcels in our standard model are heated to more than 100 K just prior to entering the disk. However, these parcels end up in the disk’s surface. Material that ends up at the midplane, in the comet-forming zone, never gets heated above 50 K. Vertical mixing, which is ignored in our model, may be able to bring the noble-gas-containing grains down into the comet-forming zone.

Another option is episodic accretion, resulting in temporary heating of the disk (Sect. 4.5). In the subsequent cooling phase, noble gases may be trapped as the ices reform. The alternative of trapping the noble gases already in the pre-collapse phase is unlikely. This requires all the H₂O to start in the gas phase and then freeze out rapidly. However, in reality (contrary to what is assumed in our model) it is probably formed on the grain surfaces by hydrogenation of atomic oxygen, which would not allow for trapping of noble gases.

4.5. Limitations of the model

The physical part of our model is known to be incomplete and this may affect the chemical results. For example, our model does not include radial and vertical mixing. Semenov et al. (2006) and Aikawa (2007) recently showed that mixing can enhance the gas-phase CO abundance in the sub-18 K regions of the disk. Similarly, there could be more H₂O gas if mixing is included. This would increase the fractions of CO and H₂O gas listed in Table 3. The gas-phase abundances can also be enhanced by allowing for photodesorption of the ices in addition to the thermal desorption considered here (Shen et al. 2004; Öberg et al. 2007, 2009). Mixing and photodesorption can each increase the total amount of gaseous material by up to a factor of 2. The higher gas-phase fractions are mostly found in the regions where the temperature is a few degrees below the desorption temperature of CO or H₂O.

Accretion from the envelope onto the star and disk occurs in our model at a constant rate \dot{M} until all of the envelope mass is gone. However, the lack of widespread red-shifted absorption seen in interferometric observations suggests that the infall may stop already at an earlier time (Jørgensen et al. 2007). This would reduce the disk mass at t_{acc} . The size of the disk is determined by the viscous evolution, which would probably not change much. Hence, if accretion stops or slows down before t_{acc} , the disk would be less dense and therefore warmer. It would also reduce the fraction of disk material where CO never desorbed, because most of that material comes from the outer edge of the original cloud (Fig. 11). Both effects would increase the gas-ice ratios of CO and H₂O.

Our results are also modified by the likely occurrence of episodic accretion (Kenyon & Hartmann 1995; Evans et al. 2009). In this scenario, material accretes from the disk onto the star in short bursts, separated by intervals where the disk-to-star accretion rate is a few orders of magnitude lower. The accretion bursts cause luminosity flares, briefly heating up the disk before returning to an equilibrium temperature that is lower than in our models. This may produce a disk with a fairly large ice content for most of the time, which evaporates and re-adsorbs after each accretion episode. The consequences for complex organics and the inclusion of various species in comets are unclear.

5. Conclusions

This paper presents the first results from a two-dimensional, semi-analytical model that simulates the collapse of a molecular cloud to form a low-mass protostar and its surrounding disk. The model follows individual parcels of material from the cloud into the star or disk and also tracks their motion inside the disk. It computes the density and temperature at each point along these trajectories. The density and temperature profiles are used as input for a chemical code to calculate the gas and ice abundances for carbon monoxide (CO) and water (H₂O) in each parcel, which are then transformed into global gas-ice profiles. Material ending up at different points in the disk spends a different amount of time at certain temperatures. These temperature histories provide a first look at the chemistry of more complex species. The main results from this paper are as follows:

- Both CO and H₂O freeze out towards the centre of the cloud before the onset of collapse. As soon as the protostar turns on, a fraction of the CO rapidly evaporates, while H₂O remains on the grains. CO returns to the solid phase when it cools below 18 K inside the disk. Depending on the initial conditions, this may be in a small or a large fraction of the disk (Sect. 3.3).
- All parcels that end up in the disk have the same qualitative temperature history (Fig. 12). There is one temperature peak just before entering the disk, when material traverses the inner envelope, and a second one (higher than the first) when inward radial motion brings the parcel closer to the star. In some cases, this results in multiple desorption and adsorption events during the parcel’s infall history (Sect. 3.4).
- Material that originates near the midplane of the initial envelope remains at lower temperatures than material originating from closer to the poles. As a result, the chemical content of the material from near the midplane is less strongly modified during the collapse than the content of material from other regions (Fig. 11). The outer part of the disk contains the chemically most pristine material, where at most only a small fraction of the CO ever desorbed (Sect. 3.3).
- A higher sound speed results in a smaller and warmer disk, with larger fractions of gaseous CO and H₂O at the end of the envelope accretion. A lower rotation rate has the same effect. A higher initial mass results in a larger and colder disk, and smaller gaseous CO and H₂O fractions (Sect. 4.1).
- The infalling material generally spends enough time in a warm zone that first-generation complex organic species can be formed abundantly on the grains (Fig. 12). Large differences can occur in the density and temperature histories for material ending up at various points in the disk. These differences allow for spatial abundance variations in the complex organics across the entire disk. This appears to be at least

part of the explanation for the cometary chemical diversity (Sects. 4.2 and 4.4).

- Complex second-generation species are not formed abundantly in the warm inner envelope (the hot core or hot corino) in our model, due to the combined effects of the dynamical timescales and low mass fraction in that region (Sect. 4.2).
- The temperature in the disk's comet-forming zone (5–30 AU from the star) lies well above the CO desorption temperature, even if effects of grain growth and continued disk evolution are taken into account. Observed cometary CO abundances can be explained by mixed ices: at temperatures of several tens of K, as predicted for the comet-forming zone, CO can be trapped in the H₂O ice at a relative abundance of a few per cent (Sect. 4.4).

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Appendix A: Disk formation efficiency

The results from our parameter grid can be used to derive the disk formation efficiency, η_{df} , as a function of the sound speed, c_s , the solid-body rotation rate, Ω_0 , and the initial cloud mass, M_0 . This efficiency can be defined as the fraction of M_0 that is in the disk at the end of the collapse phase ($t = t_{acc}$) or as the mass ratio between the disk and the star at that time. The former is used in this Appendix.

In order to cover a wider range of initial conditions, the physical part of our model was run on a 9^3 grid. The sound speed was varied from 0.15 to 0.35 km s⁻¹, the rotation rate from 10^{-14.5} to 10^{-12.5} s⁻¹ and the initial cloud mass from 0.1 to 2.1 M_\odot . The resulting η_{df} at $t = t_{acc}$ were fitted to

$$\eta_{df} = \frac{M_d}{M_0} = g_1 + g_2 \left[\frac{\log(\Omega_0/s^{-1})}{-13} \right] \quad (A.1)$$

with

$$g_1 = k_1 + k_2 \left[\frac{\log(\Omega_0/s^{-1})}{-13} \right]^{q_1} + k_3 \left[\frac{c_s}{0.2 \text{ km s}^{-1}} \right]^{q_2} + k_4 \left[\frac{M_0}{M_\odot} \right]^{q_3}, \quad (A.2)$$

$$g_2 = k_5 + k_6 \left[\frac{\log(\Omega_0/s^{-1})}{-13} \right] + k_7 \left[\frac{c_s}{0.2 \text{ km s}^{-1}} \right] + k_8 \left[\frac{M_0}{M_\odot} \right]. \quad (A.3)$$

Equation (A.1) can give values lower than 0 or larger than 1. In those cases, it should be interpreted as being 0 or 1.

The best-fit values for the coefficients k_i and the exponents q_i are listed in Table A.1. The absolute and relative difference between the best fit and the model data have a root mean square (rms) of 0.04 and 5%. The largest absolute and relative difference are 0.20 and 27%. The fit is worst for a high cloud mass, a low sound speed and an intermediate rotation rate, as well as for a low cloud mass, an intermediate to high sound speed and a high rotation rate.

Figure A.1 shows the disk formation efficiency as a function of the rotation rate, including the fit from Eq. (A.1). The efficiency is roughly a quadratic function in $\log \Omega_0$, but due to the narrow dynamic range of this variable, the fit appears as straight lines. Furthermore, the efficiency is roughly a linear function in c_s and a square root function in M_0 .

Table A.1. Coefficients and exponents for the best fit for the disk formation efficiency.

Coefficient	Value	Coefficient	Value	Exponent	Value
k_1	2.08	k_5	-0.106	q_1	0.236
k_2	0.020	k_6	-1.539	q_2	0.255
k_3	0.035	k_7	-0.470	q_3	0.537
k_4	0.914	k_8	-0.344		

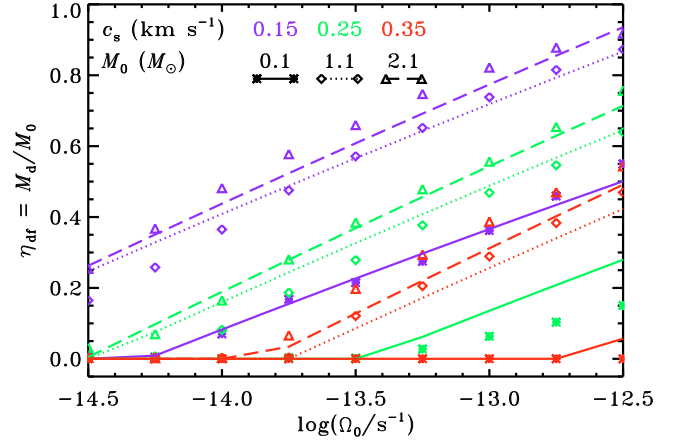


Fig. A.1. Disk formation efficiency as a function of the solid-body rotation rate. The model values are plotted as symbols and the fit from Eq. (A.1) as lines. The different values of the sound speed are indicated by colours and the different values of the initial cloud mass are indicated by symbols and line types, with the solid lines corresponding to the asterisks, the dotted lines to the diamonds and the dashed lines to the triangles.

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