

Introduction to Optimization: Benchmarking

September 20, 2017
TC2 - Optimisation

Université Paris-Saclay, Orsay, France



Dimo Brockhoff
Inria Saclay – Ile-de-France

Course Overview

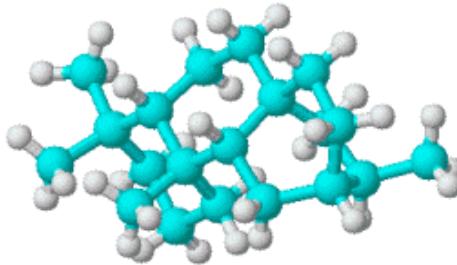
1	Mon, 18.9.2017 Tue, 19.9.2017	first lecture groups defined via wiki everybody went (actively!) through the Getting Started part of github.com/numbbo/coco
2	Wed, 20.9.2017	today's lecture: "Benchmarking", final adjustments of groups everybody can run and postprocess the example experiment (~1h for final questions/help during the lecture)
3	Fri, 22.9.2017	lecture "Introduction to Continuous Optimization"
4	Fri, 29.9.2017	lecture "Gradient-Based Algorithms"
5	Fri, 6.10.2017	lecture "Stochastic Algorithms and DFO"
6	Fri, 13.10.2017	lecture "Discrete Optimization I: graphs, greedy algos, dyn. progr." deadline for submitting data sets
	Wed, 18.10.2017	deadline for paper submission
7	Fri, 20.10.2017	final lecture "Discrete Optimization II: dyn. progr., B&B, heuristics"
	Thu, 26.10.2017 / Fri, 27.10.2017	oral presentations (individual time slots)
	after 30.10.2017	vacation aka learning for the exams
	Fri, 10.11.2017	written exam

All deadlines:
23:59pm Paris time

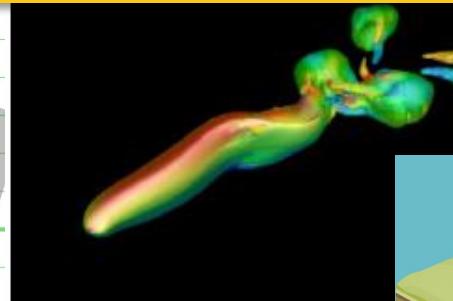
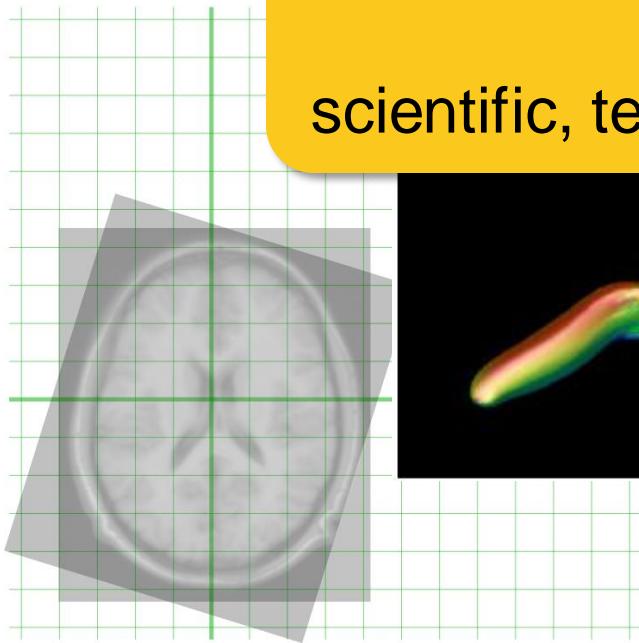
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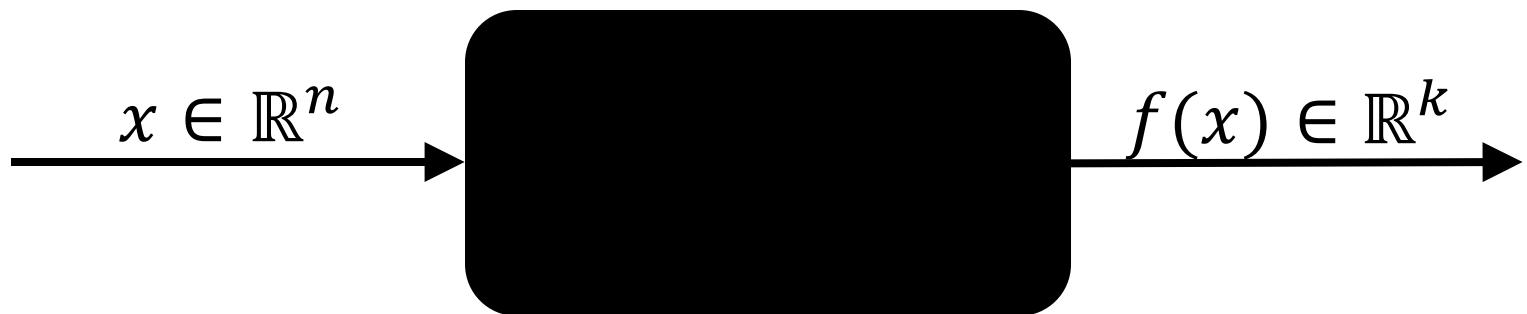


challenging optimization problems
appear in many
scientific, technological and industrial domains



Numerical Blackbox Optimization

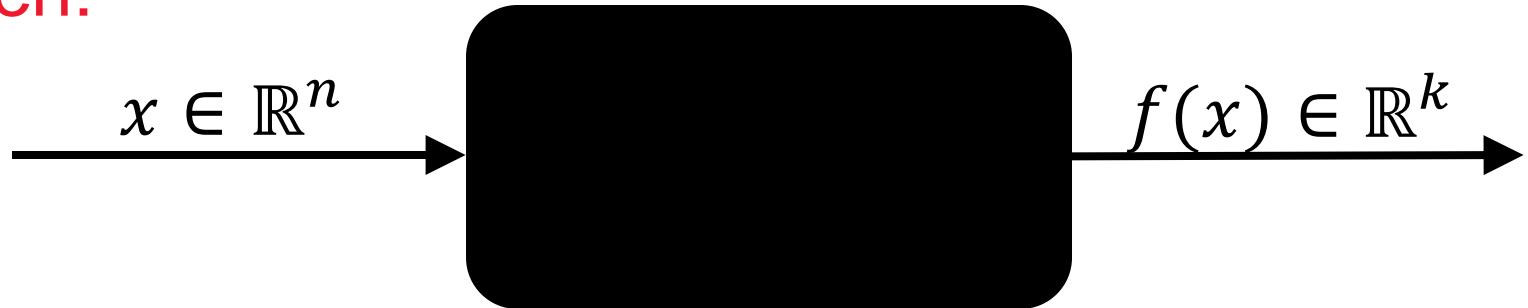
Optimize $f: \Omega \subset \mathbb{R}^n \mapsto \mathbb{R}^k$



derivatives not available or not useful

Practical Blackbox Optimization

Given:



Not clear:

which of the many algorithms should I use on my problem?

Numerical Blackbox Optimizers

Deterministic algorithms

Quasi-Newton with estimation of gradient (**BFGS**) [Broyden et al. 1970]

Simplex downhill [Nelder & Mead 1965]

Pattern search [Hooke and Jeeves 1961]

Trust-region methods (NEWUOA, BOBYQA) [Powell 2006, 2009]

Stochastic (randomized) search methods

Evolutionary Algorithms (continuous domain)

- Differential Evolution [Storn & Price 1997]
- Particle Swarm Optimization [Kennedy & Eberhart 1995]
- **Evolution Strategies, CMA-ES**

[Rechenberg 1965, Hansen & Ostermeier 2001]

- Estimation of Distribution Algorithms (EDAs)

[Larrañaga, Lozano, 2002]

- Cross Entropy Method (same as EDA) [Rubinstein, Kroese, 2004]
- **Genetic Algorithms** [Holland 1975, Goldberg 1989]

Simulated annealing [Kirkpatrick et al. 1983]

Simultaneous perturbation stochastic approx. (SPSA) [Spall 2000]

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choice typically not immediately clear although practitioners have knowledge about which difficulties their problem has (e.g. multi-modality, non-separability, ...)

- **Evolution Strategies, CMA-ES**

[Rechenberg 1965, Hansen & Ostermeier 2001]

- Estimation of Distribution Algorithms (EDAs)

[Larrañaga, Lozano, 2002]

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Need: Benchmarking

- understanding of algorithms
- algorithm selection
- putting algorithms to a standardized test
 - simplify judgement
 - simplify comparison
 - regression test under algorithm changes

Kind of everybody has to do it (and it is tedious):

- choosing (and implementing) problems, performance measures, visualization, stat. tests, ...
- running a set of algorithms

that's where COCO comes into play



Comparing Continuous Optimizers Platform
<https://github.com/numbbo/coco>

automatized benchmarking

benchmarking is non-trivial

[remember the tutorial of Antonio]

**hence, COCO implements a
reasonable, well-founded, and
well-documented
pre-chosen methodology**

How to benchmark algorithms with COCO?

<https://github.com/numbbo/coco>

Screenshot of a web browser showing the GitHub repository page for `numbbo/coco`. The URL in the address bar is <https://github.com/numbbo/coco>.

The repository name is `numbbo / coco`. It has 16,007 commits, 11 branches, 31 releases, and 15 contributors. A red box highlights the **Clone or download** button.

Recent commits listed:

- brockho committed on GitHub Merge pull request #1352 from numbbo/development ... Latest commit 4b1497a on 20 Apr
- code-experiments A little more verbose error message when suite regression test fails a month ago
- code-postprocessing Hashes are back on the plots. a month ago
- code-preprocessing Fixed preprocessing to work correctly with the extended biobjective s... 3 months ago
- howtos Update create-a-suite-howto.md 4 months ago
- .clang-format raising an error in bbbob2009_logger.c when best_value is NULL. Plus s... 2 years ago
- .hgignore raising an error in bbbob2009_logger.c when best_value is NULL. Plus s... 2 years ago
- AUTHORS small correction in AUTHORS a year ago
- LICENCE Update LICENCE 11 months ago

<https://github.com/numbbo/coco>

The screenshot shows a GitHub repository page for 'numbbo/coco'. The top navigation bar includes links for 'Most Visited', 'Getting Started', 'COCO-Algorithms', 'numbbo/numbbo', 'RandOpt', 'CMAP', 'Inria GitLab', and 'RER B from lab'. The repository header shows 'numbbo / coco' with 15 stars, 38 forks, and 24 open issues. Below the header, there are tabs for 'Code', 'Issues 133', 'Pull requests 1', 'Projects 9', 'Settings', and 'Insights'. A summary section displays 16,007 commits, 11 branches, 31 releases, and 15 contributors. A dropdown menu for 'Branch: master' shows 'New pull request'. On the right, a 'Clone with HTTPS' section provides the URL <https://github.com/numbbo/coco.git>, with options to 'Open in Desktop' or 'Download ZIP'. The 'Download ZIP' button is highlighted with a red box. The main content area lists recent commits:

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- AUTHORS**: small correction in AUTHORS
- LICENSE**: Update LICENSE
- README.md**: Added link to #1335 before closing.

A context menu is open over the last commit, showing options:

- Clone with HTTPS
- Use SSH
- Open in Desktop
- Download ZIP** (highlighted with a red box)
- 4 months ago

<https://github.com/numbbo/coco>

numbbo/coco: Numerical ... + GitHub, Inc. (US) https://github.com/numbbo/coco Search Most Visited Getting Started COCO-Algorithms numbbo/numbbo · Gi... RandOpt CMAP Inria GitLab RER B from lab Edit Add topics

Numerical Black-Box Optimization Benchmarking Framework <http://coco.gforge.inria.fr/>

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Branch: master New pull request Create new file Upload files Find file Clone or download

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README.md

Clone with HTTPS Use SSH
Use Git or checkout with SVN using the web URL.
<https://github.com/numbbo/coco.git>
Open in Desktop Download ZIP 4 months ago

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The screenshot shows a web browser window with the GitHub URL <https://github.com/numbbo/coco>. The page displays the repository's history and files. A context menu is open over the repository name, specifically highlighting the 'Download ZIP' option, which is circled in red.

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[Open in Desktop](#) [Download ZIP](#) 4 months ago

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numbbo/coco: Comparing Continuous Optimizers

<https://github.com/numbbo/coco>

numbbo/coco: Numerical ... [+](#)

[GitHub, Inc. \(US\)](#) | <https://github.com/numbbo/coco> [Search](#)

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This code reimplements the original Comparing Continuous Optimizer platform, now rewritten fully in `ANSI C` with other languages calling the `C` code. As the name suggests, the code provides a platform to benchmark and compare continuous optimizers, AKA non-linear solvers for numerical optimization. Languages currently available are

- `C/C++`
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Contributions to link further languages (including a better example in `C++`) are more than welcome.

For more information,

- read our [benchmarking guidelines introduction](#)
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- see the [bbob-biobj](#) and [bbob-biobj-ext](#) COCO multi-objective functions testbed documentation and the [specificities of the performance assessment for the bi-objective testbeds](#).
- consult the [BBOB workshops series](#),
- consider to [register here](#) for news,
- see the [previous COCO home page here](#) and
- see the [links below](#) to learn more about the ideas behind CoCo.

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Getting Started

0. Check out the [Requirements](#) above.
1. Download the COCO framework code from github,
 - either by clicking the [Download ZIP button](#) and unzip the `zip` file,
 - or by typing `git clone https://github.com/numbbo/coco.git`. This way allows to remain up-to-date easily (but needs `git` to be installed). After cloning, `git pull` keeps the code up-to-date with the latest release.

The record of official releases can be found [here](#). The latest release corresponds to the [master branch](#) as linked above.

2. In a system shell, `cd` into the `coco` or `coco-<version>` folder (framework root), where the file `do.py` can be found.
Type, i.e. execute, one of the following commands once

```
python do.py run-c  
python do.py run-java  
python do.py run-matlab  
python do.py run-octave  
python do.py run-python
```

depending on which language shall be used to run the experiments. `run-*` will build the respective code and run the example experiment once. The build result and the example experiment code can be found under `code-experiments/build/<language>` (`<language>=matlab` for Octave). `python do.py` lists all available commands.

3. On the computer where experiment data shall be post-processed, run

```
python do.py install-postprocessing
```

requirements & download

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installation II: postprocessing

to (user-locally) install the post-processing. From here on, `do.py` has done its job and is only needed again for updating the builds to a new release.

4. Copy the folder `code-experiments/build/YOUR-FAVORITE-LANGUAGE` and its content to another location. In Python it is sufficient to copy the file `example_experiment.py`. Run the example experiment (it already is compiled). As the details vary, see the respective read-me's and/or example experiment files:

- C [read me](#) and [example experiment](#)
- Java [read me](#) and [example experiment](#)
- Matlab/Octave [read me](#) and [example experiment](#)
- Python [read me](#) and [example experiment](#)

If the example experiment runs, connect your favorite algorithm to Coco: replace the call to the random search optimizer in the example experiment file by a call to your algorithm (see above). Update the output `result_folder`, the `algorithm_name` and `algorithm_info` of the observer options in the example experiment file.

Another entry point for your own experiments can be the `code-experiments/examples` folder.

5. Now you can run your favorite algorithm on the `bbob` suite (for single-objective algorithms) or on the `bbob-biobj` and `bbob-biobj-ext` suites (for multi-objective algorithms). Output is automatically generated in the specified data `result_folder`. By now, more suites might be available, see below.

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coupling algo + COCO

Simplified Example Experiment in Python

```
import cocoex
import scipy.optimize

### input
suite_name = "bbob"
output_folder = "scipy-optimize-fmin"
fmin = scipy.optimize.fmin

### prepare
suite = cocoex.Suite(suite_name, "", "")
observer = cocoex.Observer(suite_name,
                           "result_folder: " + output_folder)

### go
for problem in suite: # this loop will take several minutes
    problem.observe_with(observer) # generates the data for
                                    # cocopp post-processing
    fmin(problem, problem.initial_solution)
```

Note: the actual example_experiment.py contains more advanced things like restarts, batch experiments, other algorithms (e.g. CMA-ES), etc.

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6. Postprocess the data from the results folder by typing

```
python -m cocopp [-o OUTPUT_FOLDERNAME] YOURDATA
```

Any subfolder in the folder arguments will be searched for different folders collected under a single "root" `YOURDATAFOLDER` folder. We can also compare more than one algorithm by specifying several data result folders generated by different algorithms.

A folder, p file, useful the output

A summary template template

7. Once indep

running the experiment

tip:
start with small #funevals (until bugs fixed ☺)
then increase budget to get a feeling
how long a "long run" will take

8. The experiments can be parallelized with any re-distribution of single problem instances to batches (see `example_experiment.py` for an example). Each batch must write in a different target folder (this should happen automatically). Results of each batch must be kept under their separate folder as is. These folders then must be

<https://github.com/numbbo/coco>

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```
python -m cocopp [-o OUTPUT_FOLDERNAME] YOURDATAFOLDER [MORE_DATAFOLDERS]
```

Any subfolder in the folder arguments will be searched for logged data. That is, experiments from different batches can be in different folders collected under a single "root" `YOURDATAFOLDEF`, specifying several data result folders generated by different algos.

A folder, `ppdata` by default, will be generated, which contains a file, useful as main entry point to explore the result with a browser. The output folder name with the `-o OUTPUT_FOLDERNAME` option.

A summary pdf can be produced via LaTeX. The corresponding templates can be found in the `code-postprocessing/latex-templates`.

7. Once the postprocessing is done, the results can be visualized in a browser.

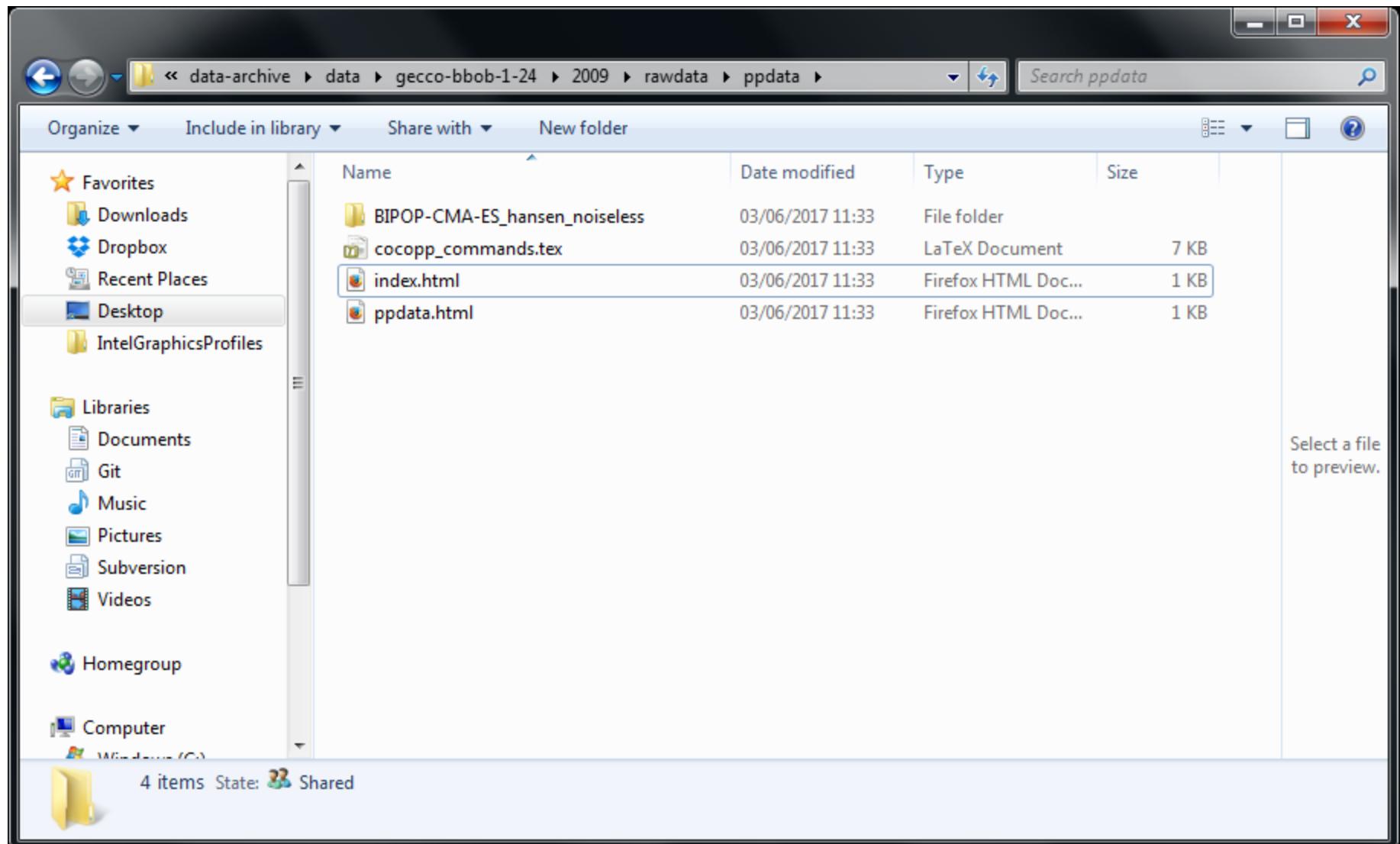
8. The postprocessing script is located in `code-experiments/postprocessing`.

`example_experiment.py` (for an example). Each batch must write in a different target folder (this should happen automatically). Results of each batch must be kept under their separate folder as is. These folders then must be

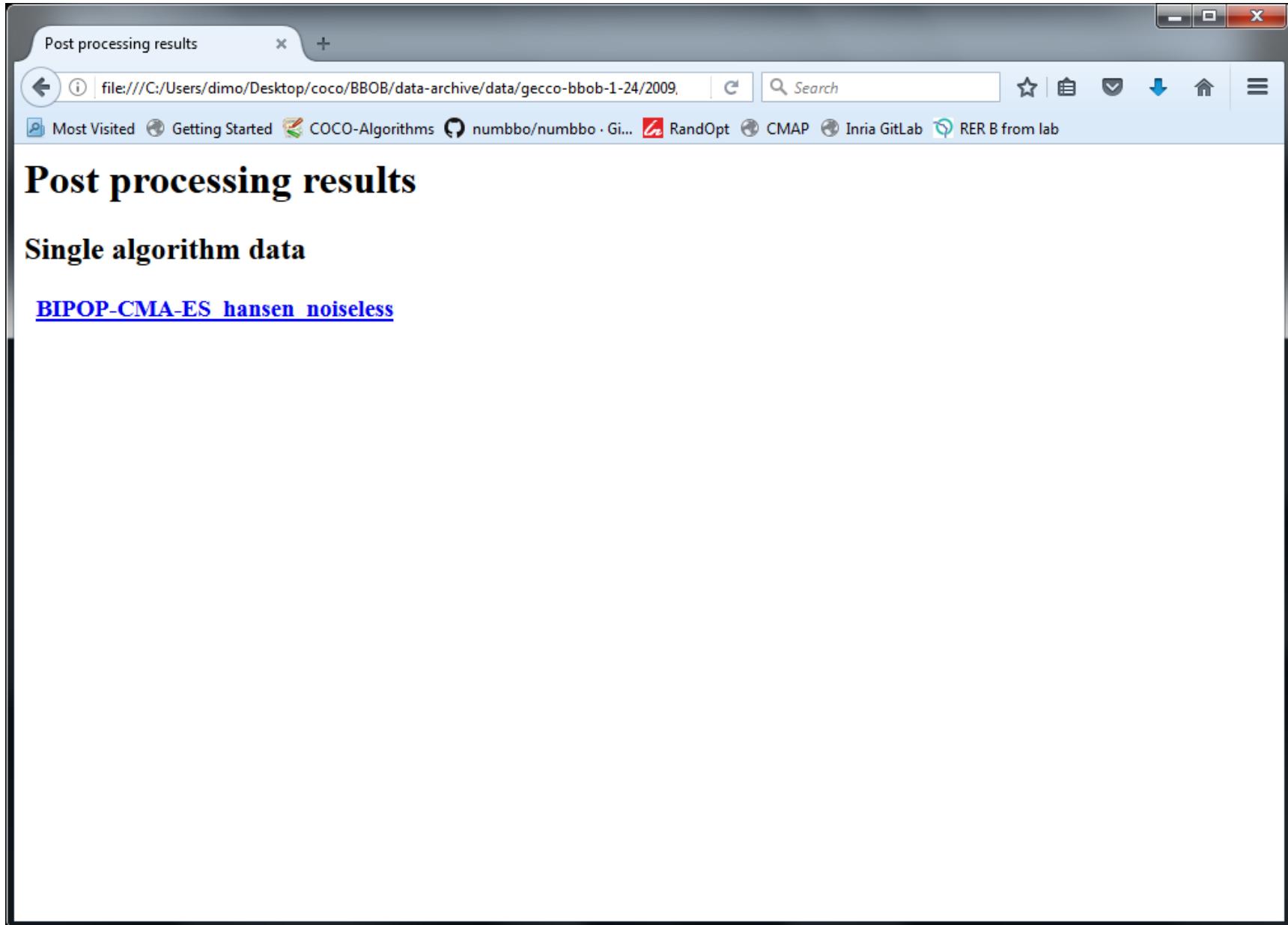
postprocessing

**tip to reduce time:
use parameter --omit-single
(will become the default in v2.2)**

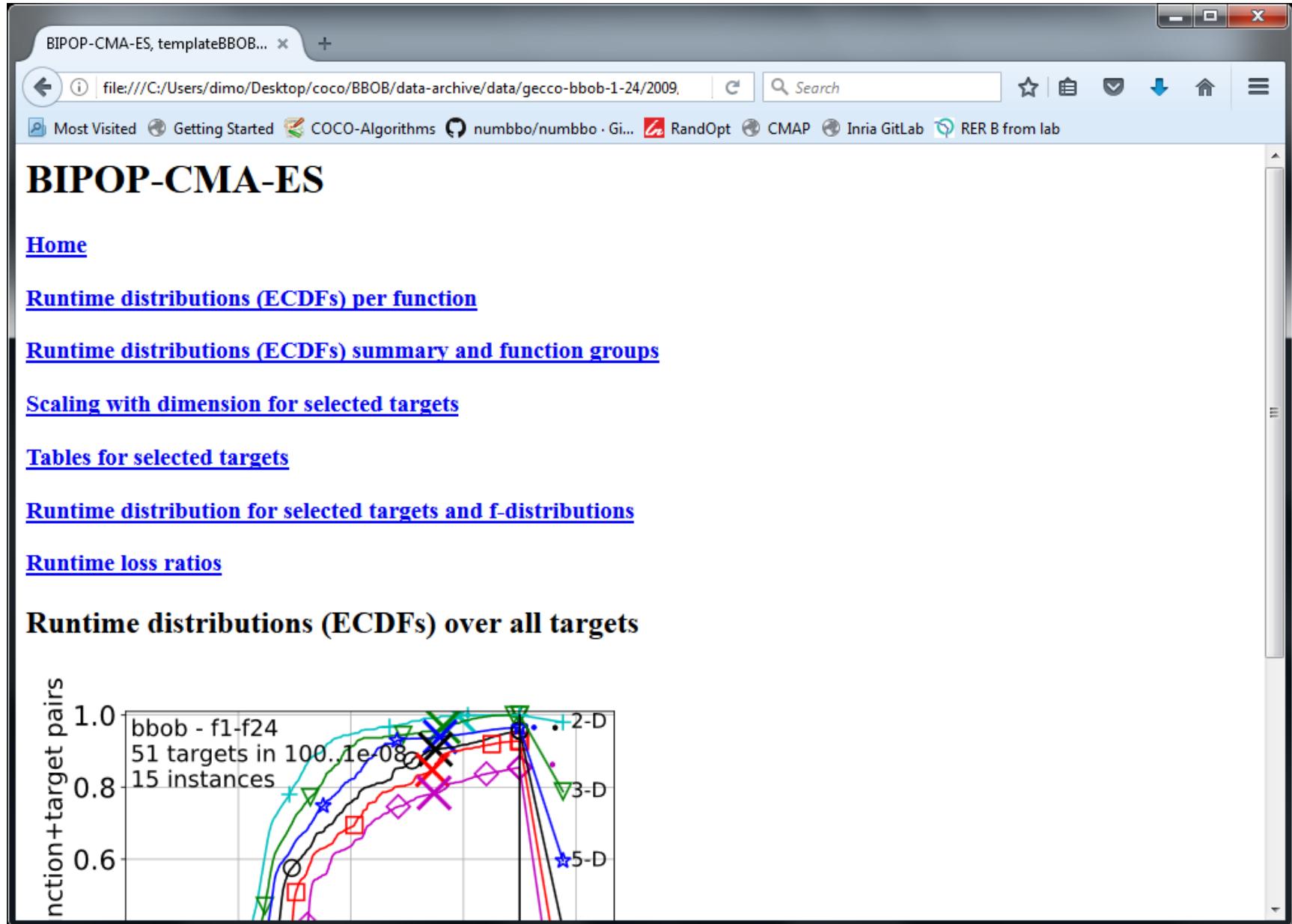
Result Folder



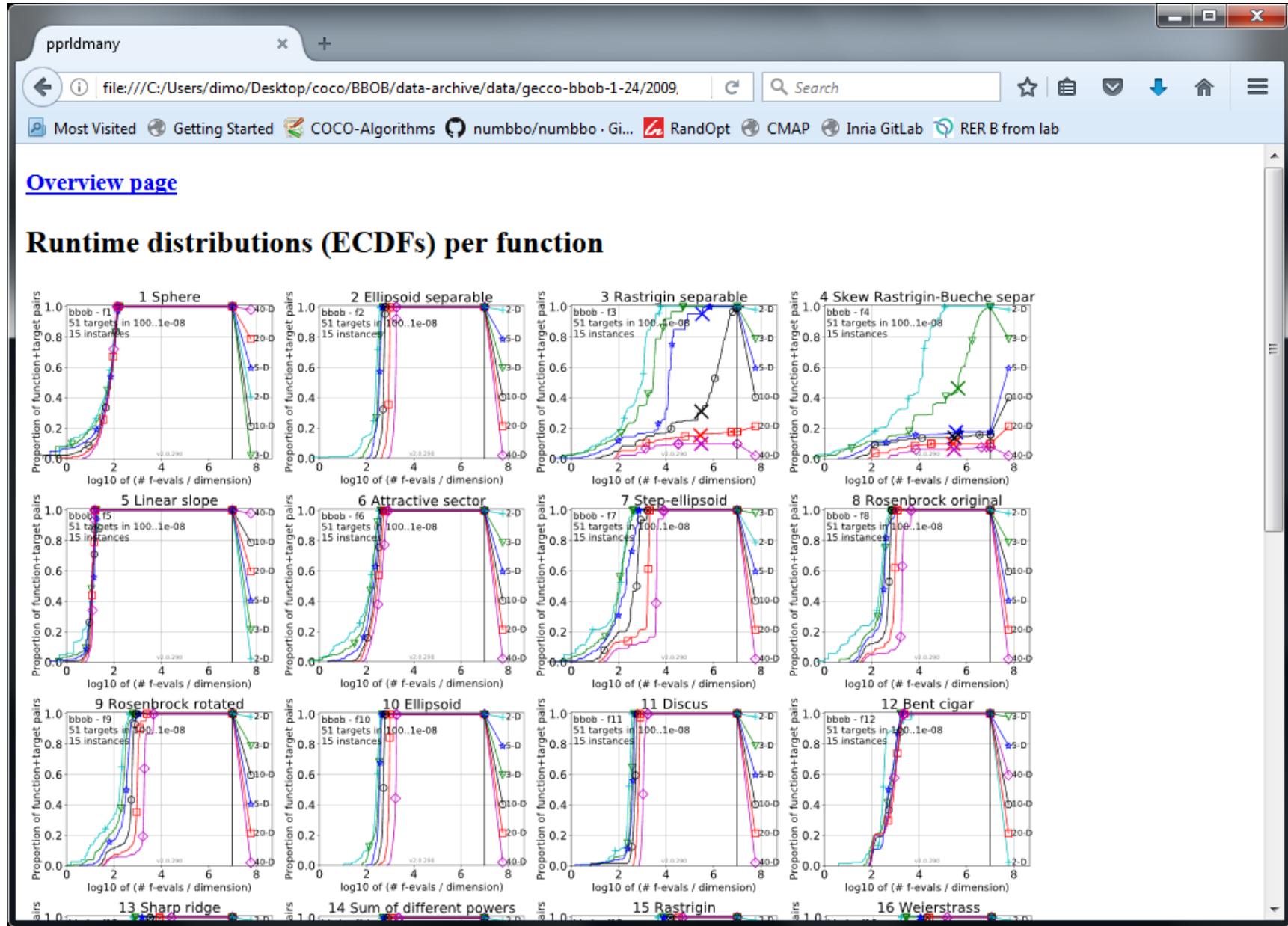
Automatically Generated Results



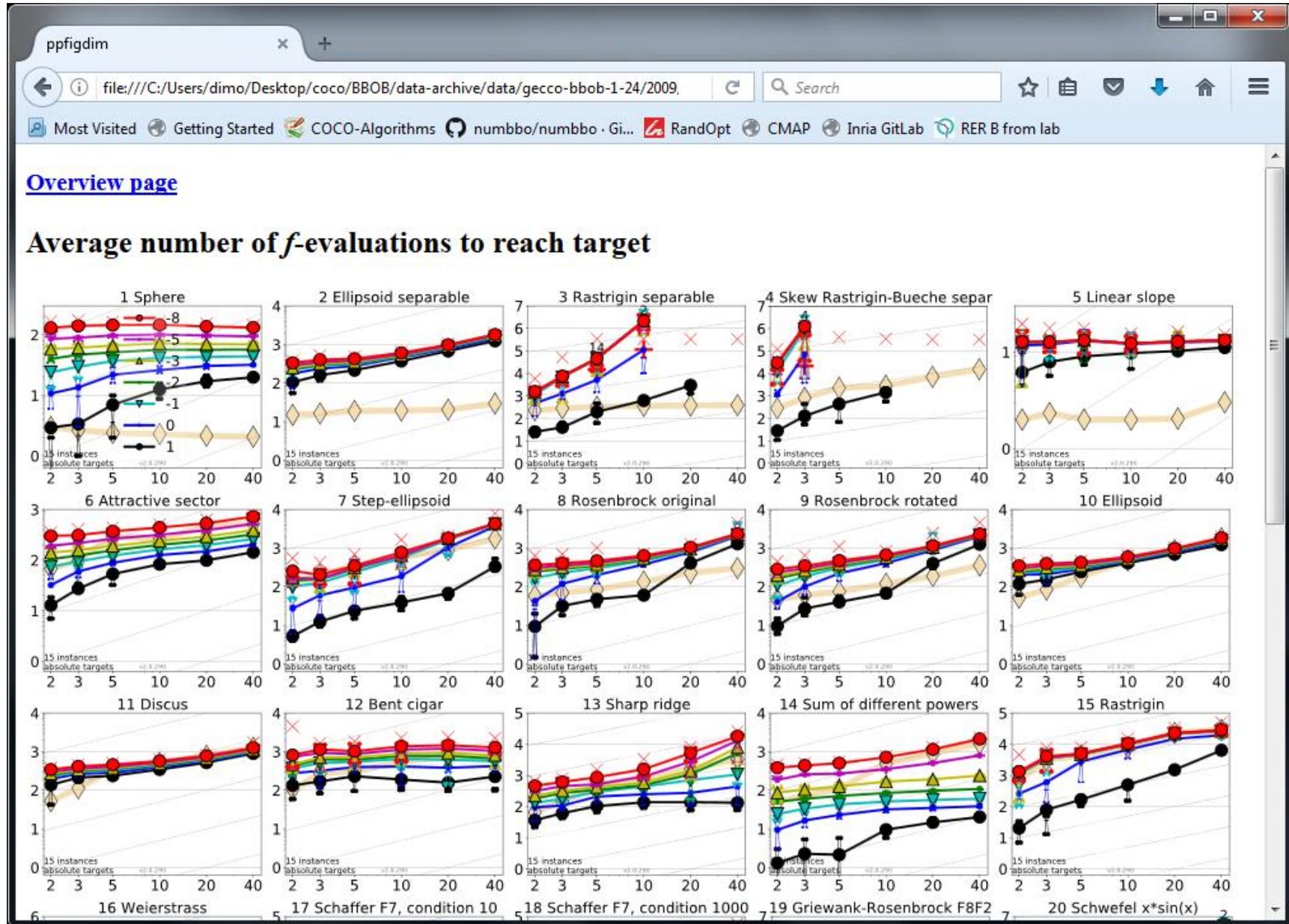
Automatically Generated Results



Automatically Generated Results



Automatically Generated Results



so far:

data for about 170 algorithm variants
(some of which on noisy or multiobjective test functions)
132 workshop papers
by 101 authors from 28 countries

Measuring Performance

On

- real world problems
 - expensive
 - comparison typically limited to certain domains
 - experts have limited interest to publish
- "artificial" benchmark functions
 - cheap
 - controlled
 - data acquisition is comparatively easy
 - problem of representativeness

Test Functions

- define the "scientific question"
the relevance can hardly be overestimated
- should represent "reality"
- are often too simple?
remind separability
- a number of testbeds are around
- account for invariance properties
prediction of performance is based on “similarity”,
ideally equivalence classes of functions

Available Test Suites in COCO

bbob	24 noiseless fcts	140+ algo data sets
bbob-noisy	30 noisy fcts	40+ algo data sets
bbob-biobj	55 bi-objective fcts	16 algo data sets

How Do We Measure Performance?

Meaningful quantitative measure

- quantitative on the ratio scale (highest possible)
"algo A is two *times* better than algo B" is a meaningful statement
- assume a wide range of values
- meaningful (interpretable) with regard to the real world
possible to transfer from benchmarking to real world

runtime or **first hitting time** is the prime candidate
(we don't have many choices anyway)

How Do We Measure Performance?

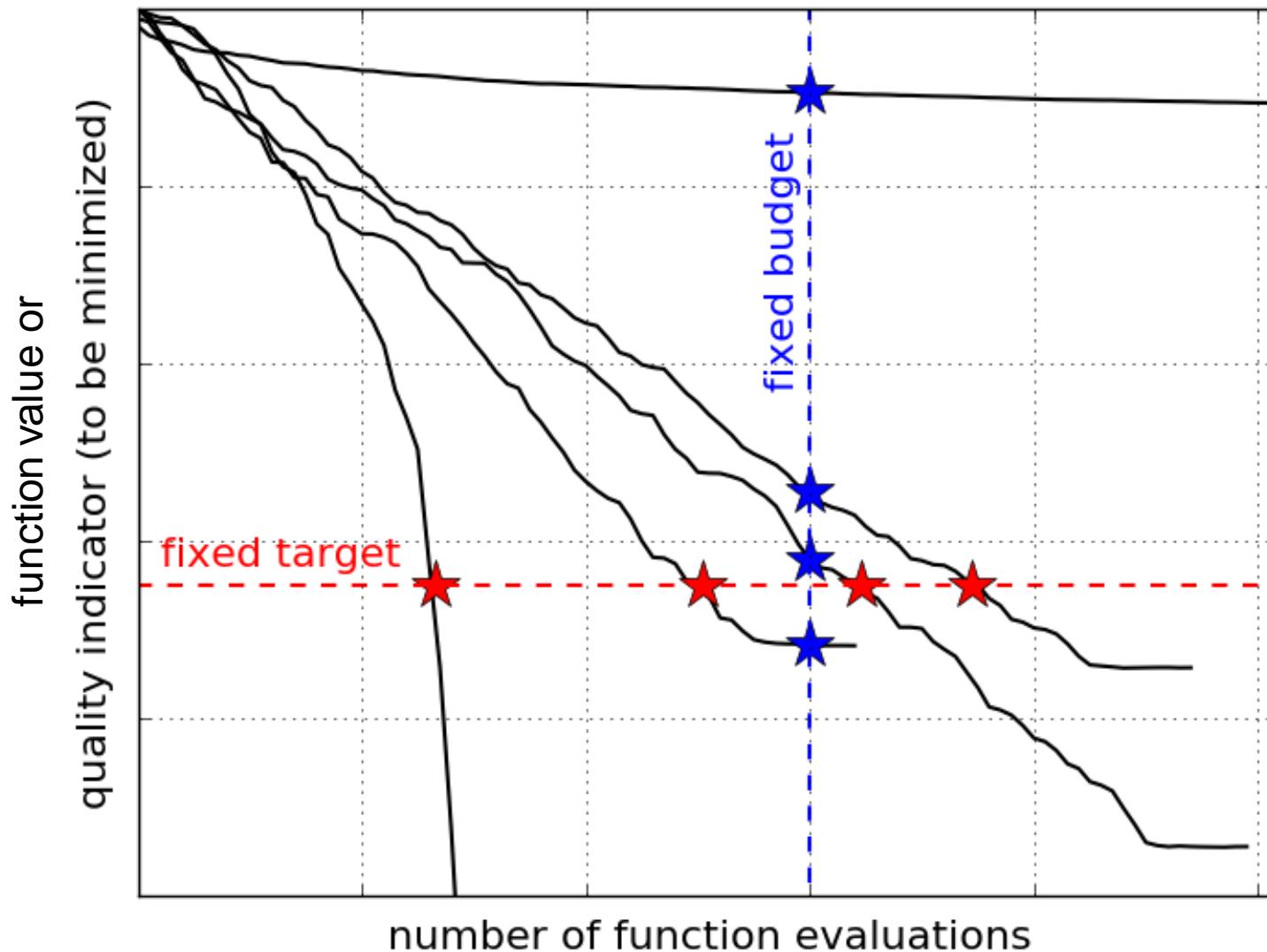
Two objectives:

- Find solution with small(est possible) function/indicator value
- With the least possible search costs (number of function evaluations)

For measuring performance: fix one and measure the other

Measuring Performance Empirically

convergence graphs is all we have to start with...

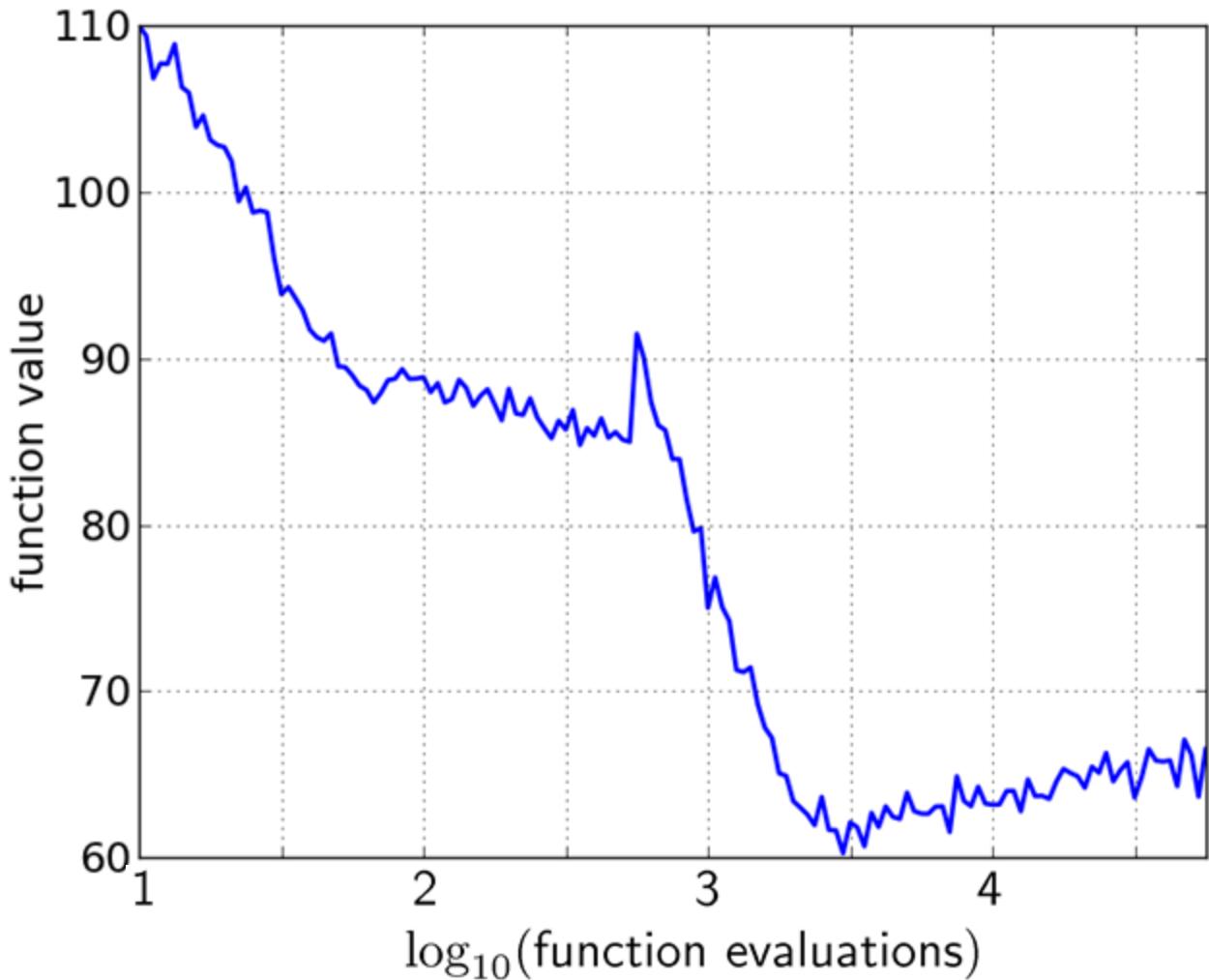


ECDF:

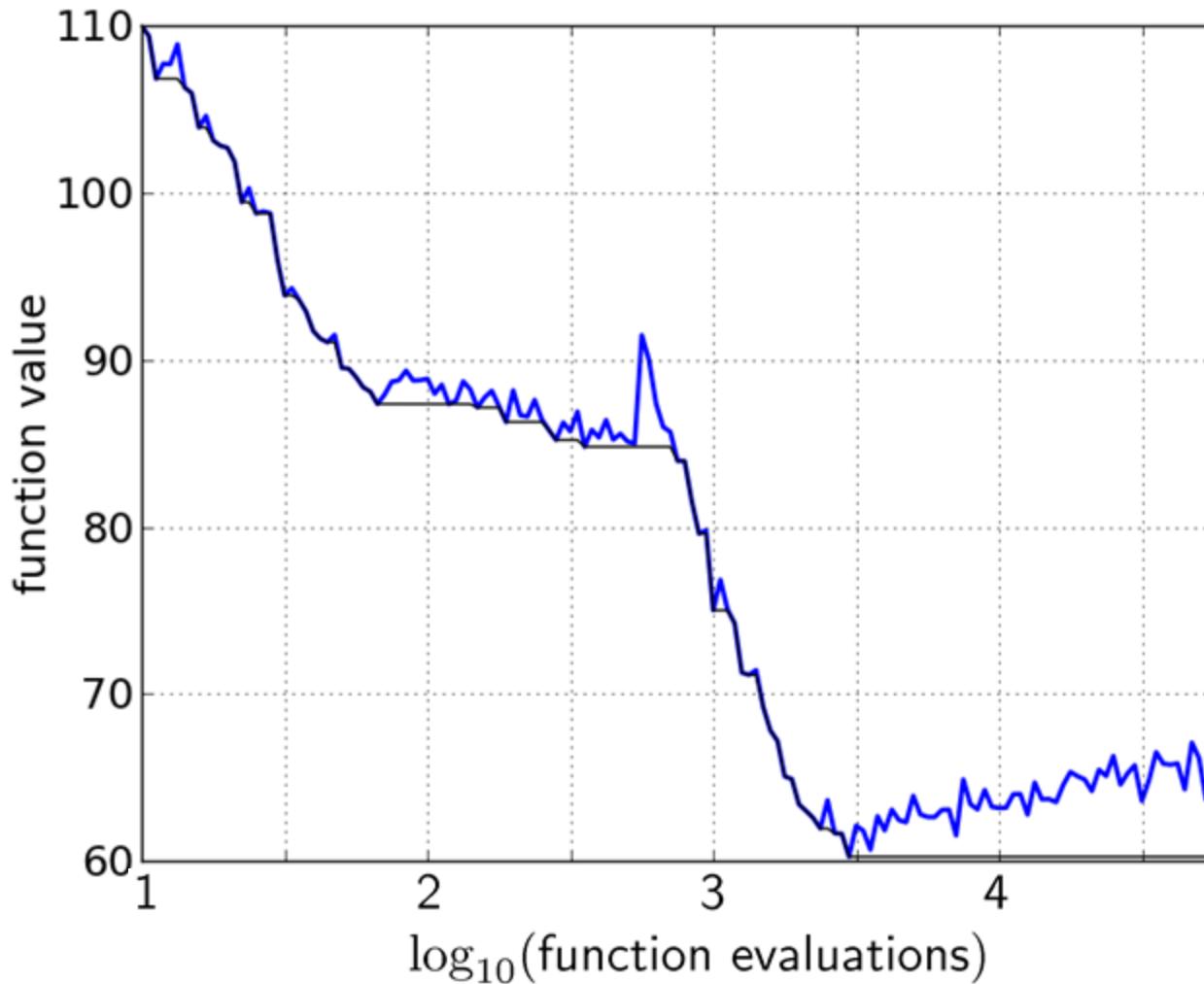
Empirical Cumulative Distribution Function of the
Runtime

[aka data profile]

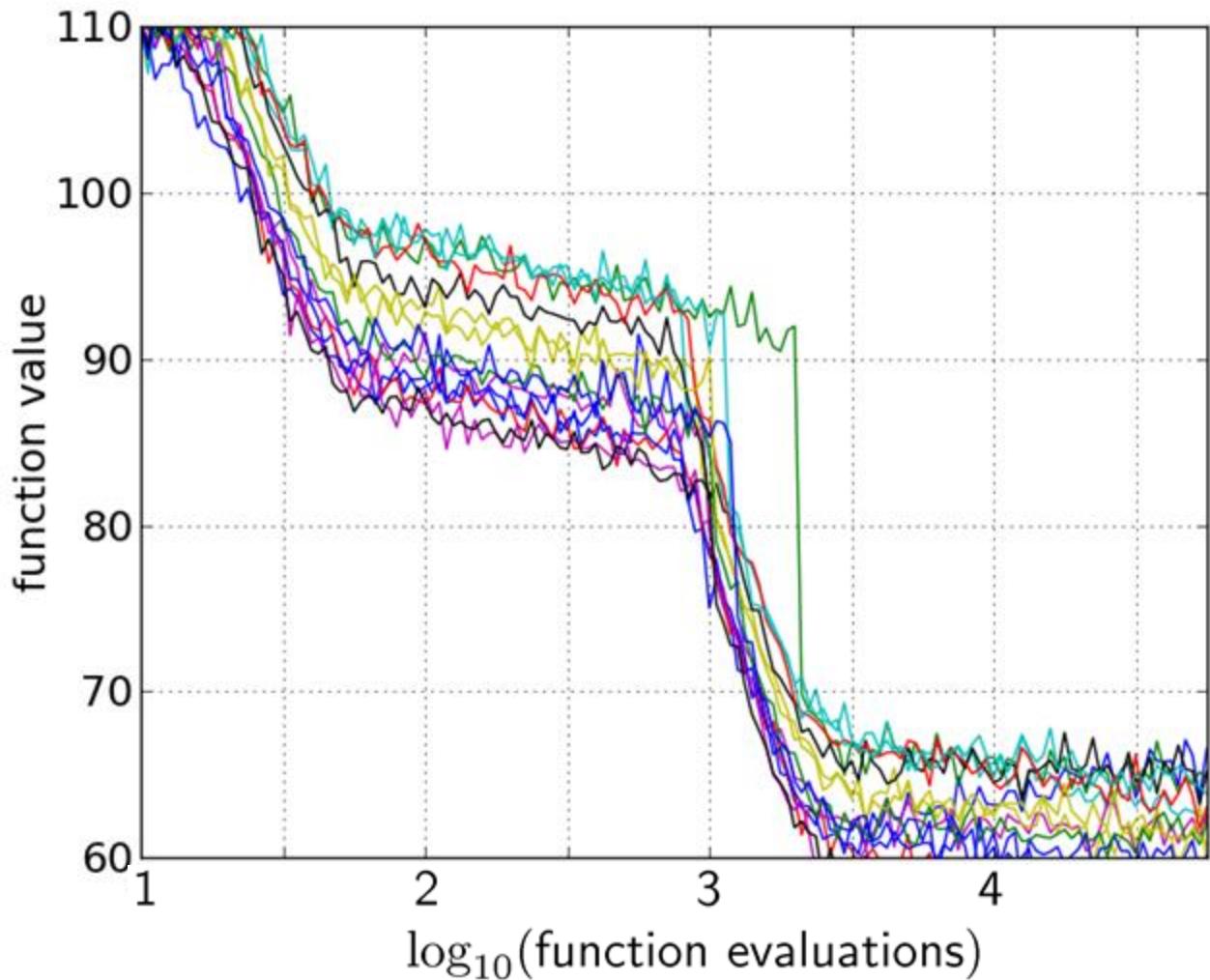
A Convergence Graph



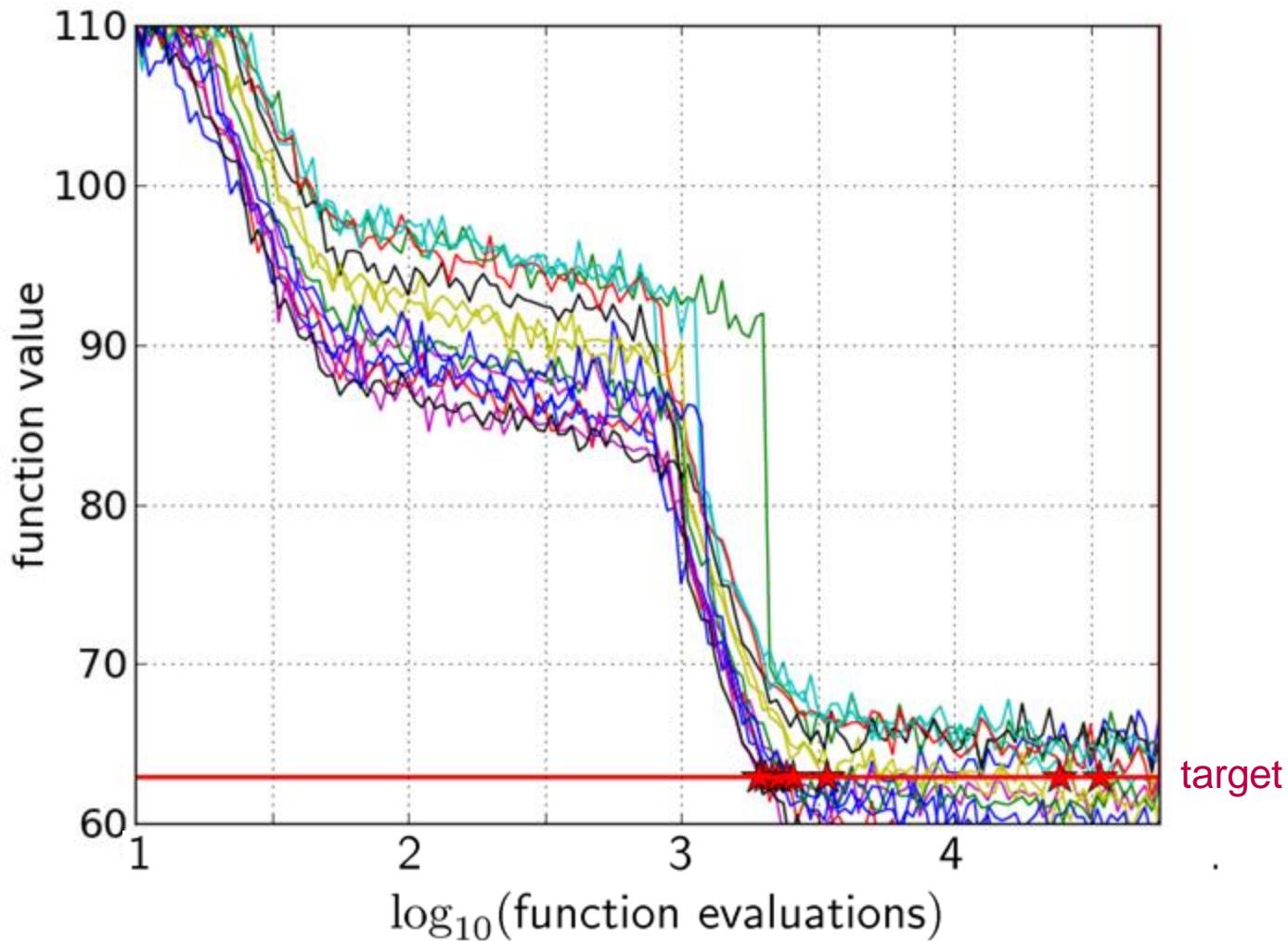
First Hitting Time is Monotonous



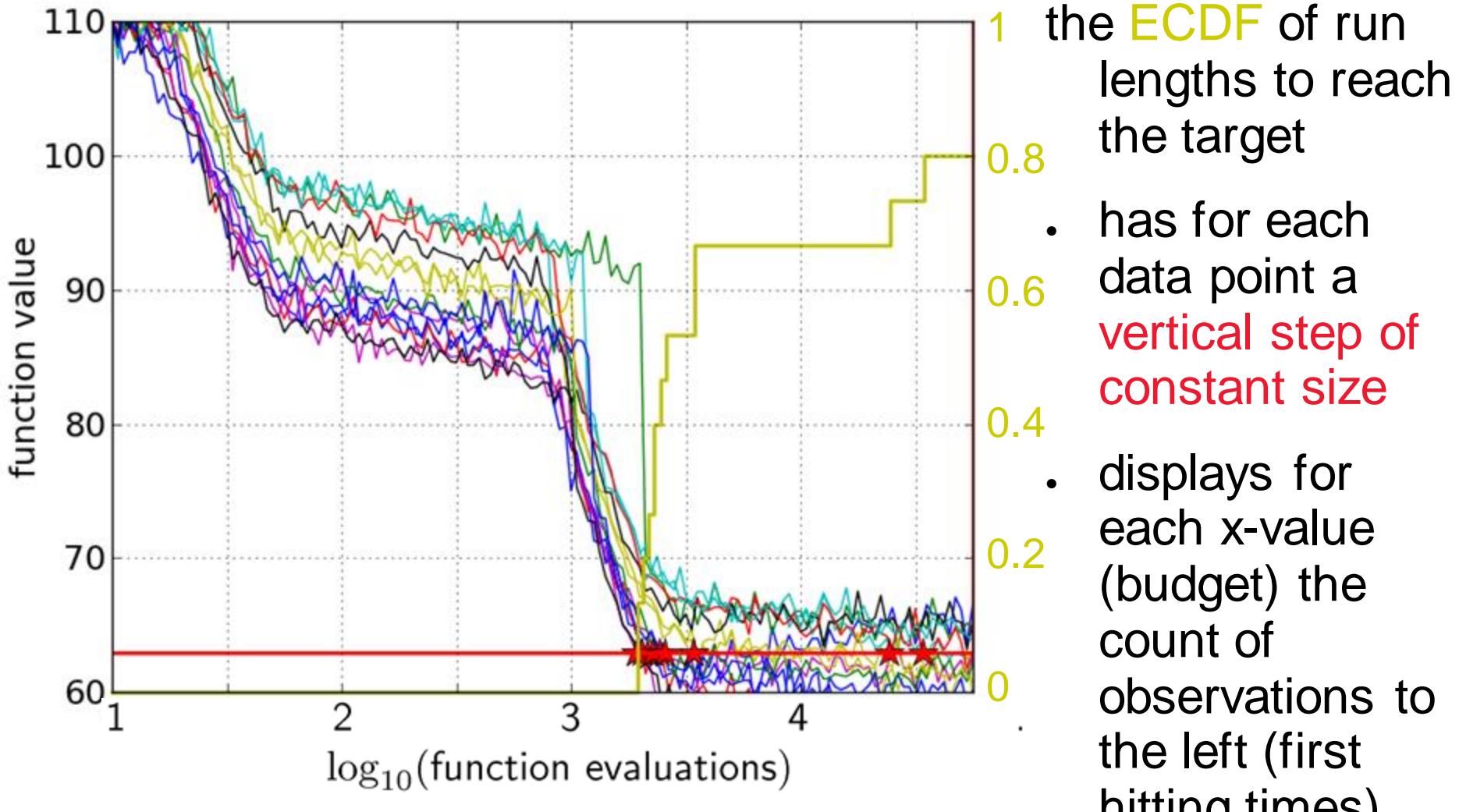
15 Runs



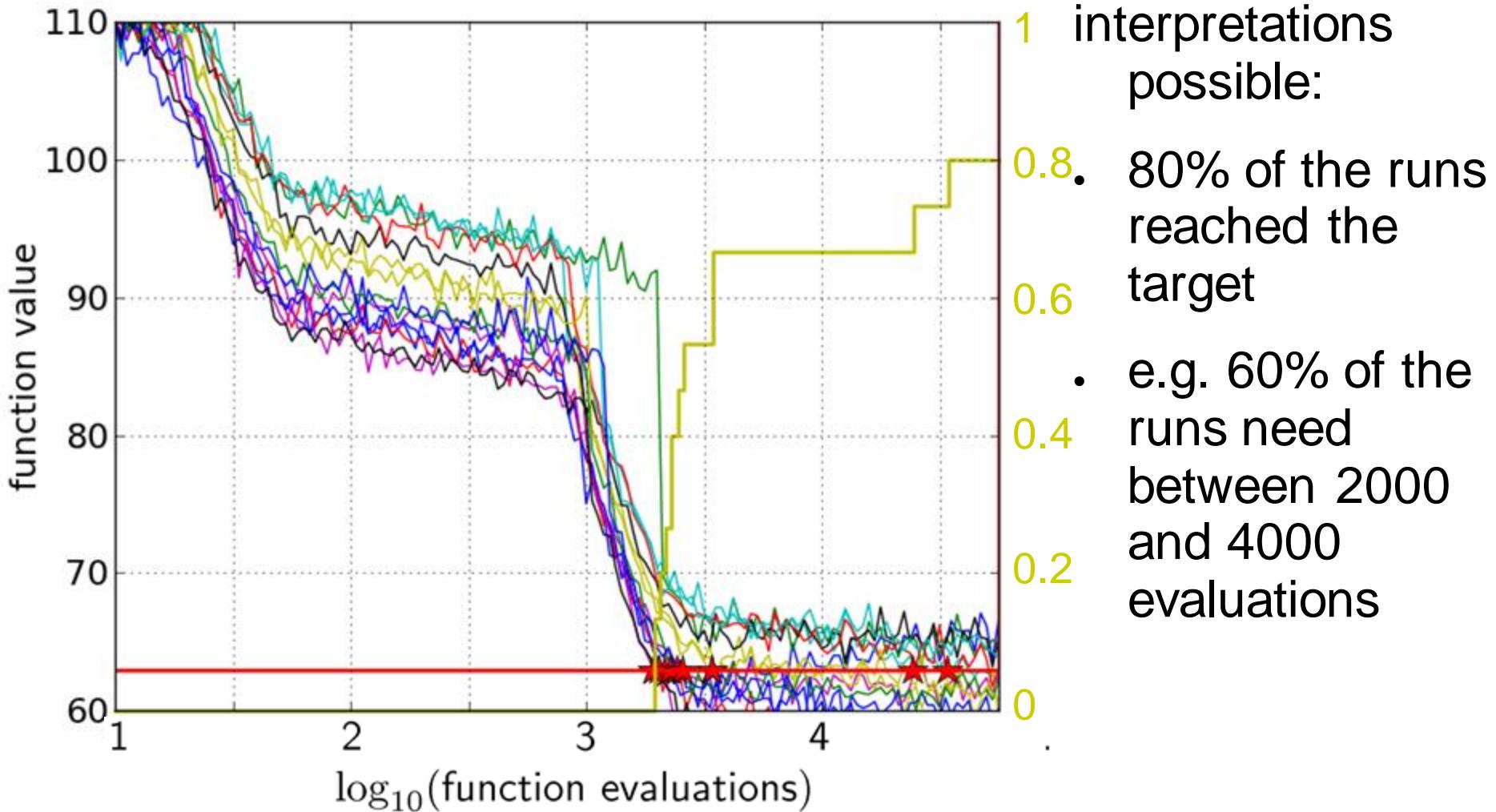
15 Runs \leq 15 Runtime Data Points



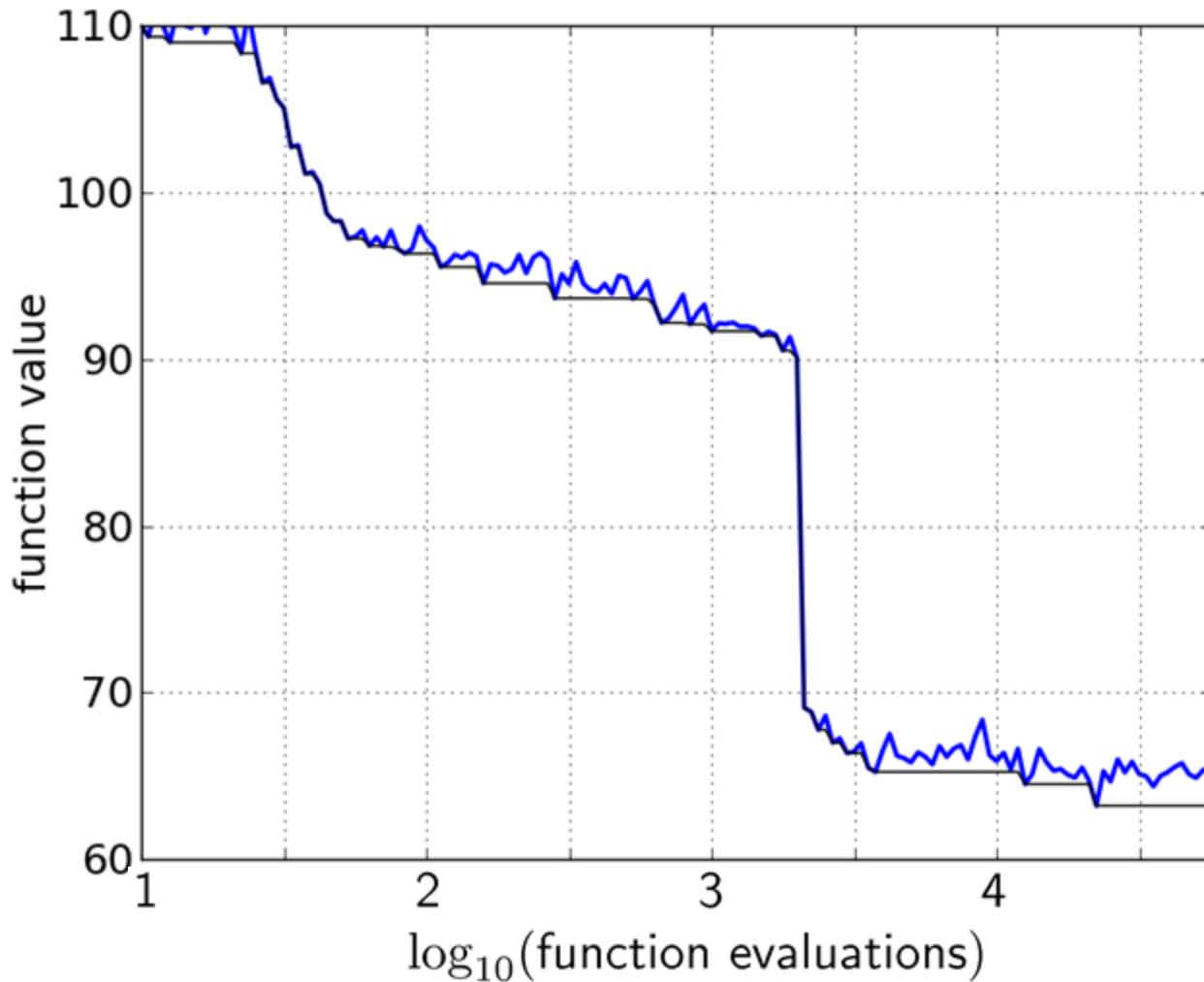
Empirical Cumulative Distribution



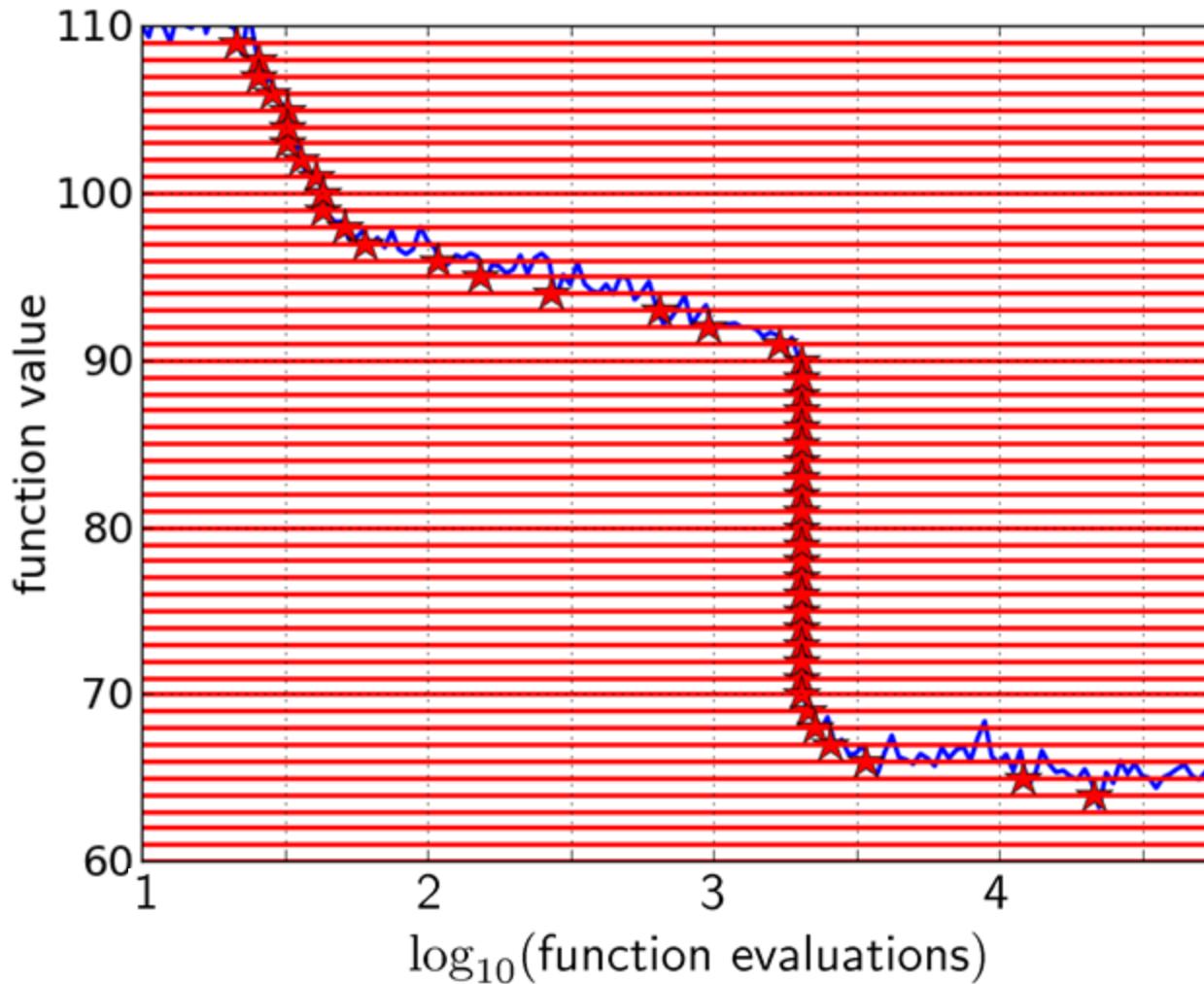
Empirical Cumulative Distribution



Reconstructing A Single Run

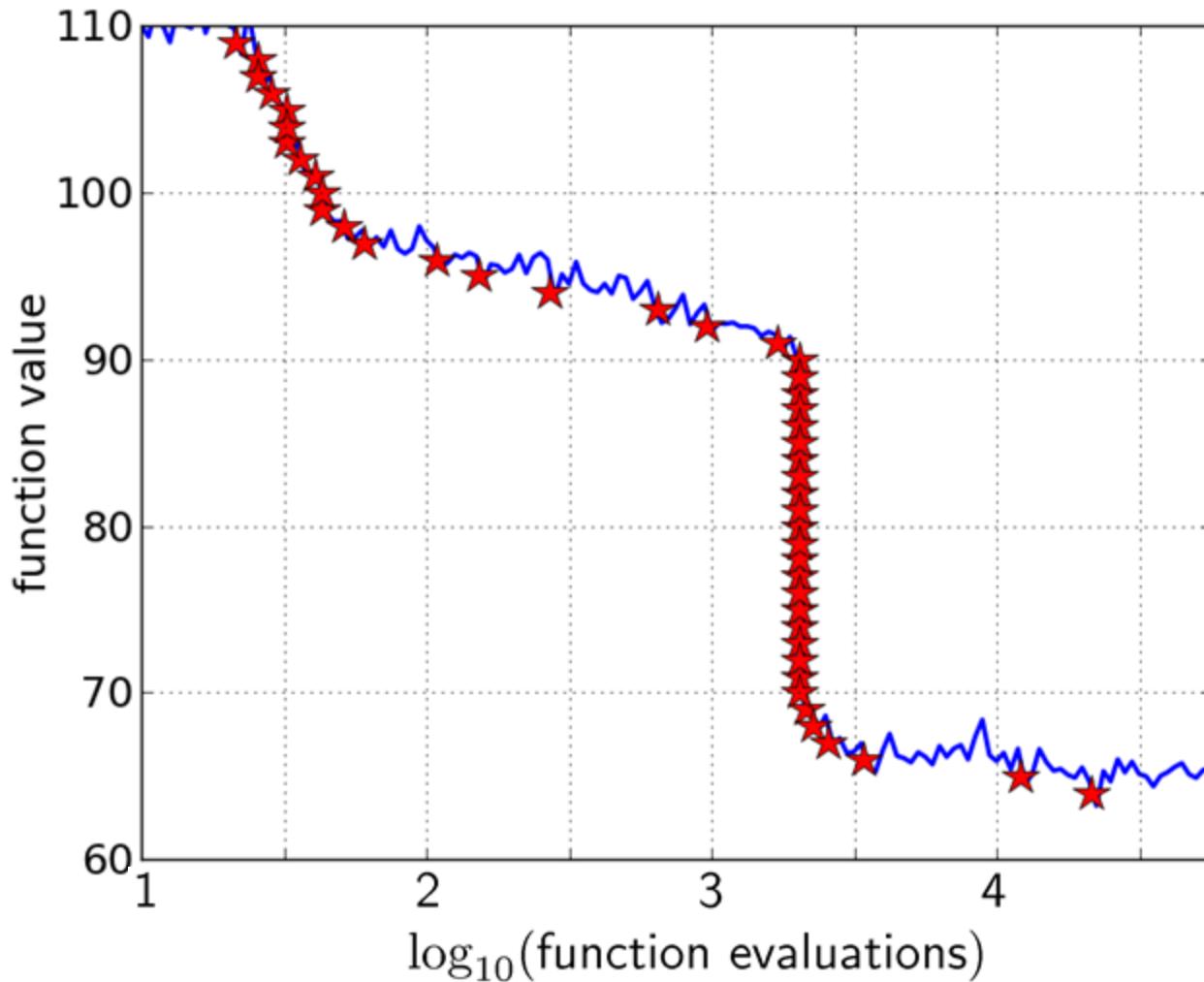


Reconstructing A Single Run

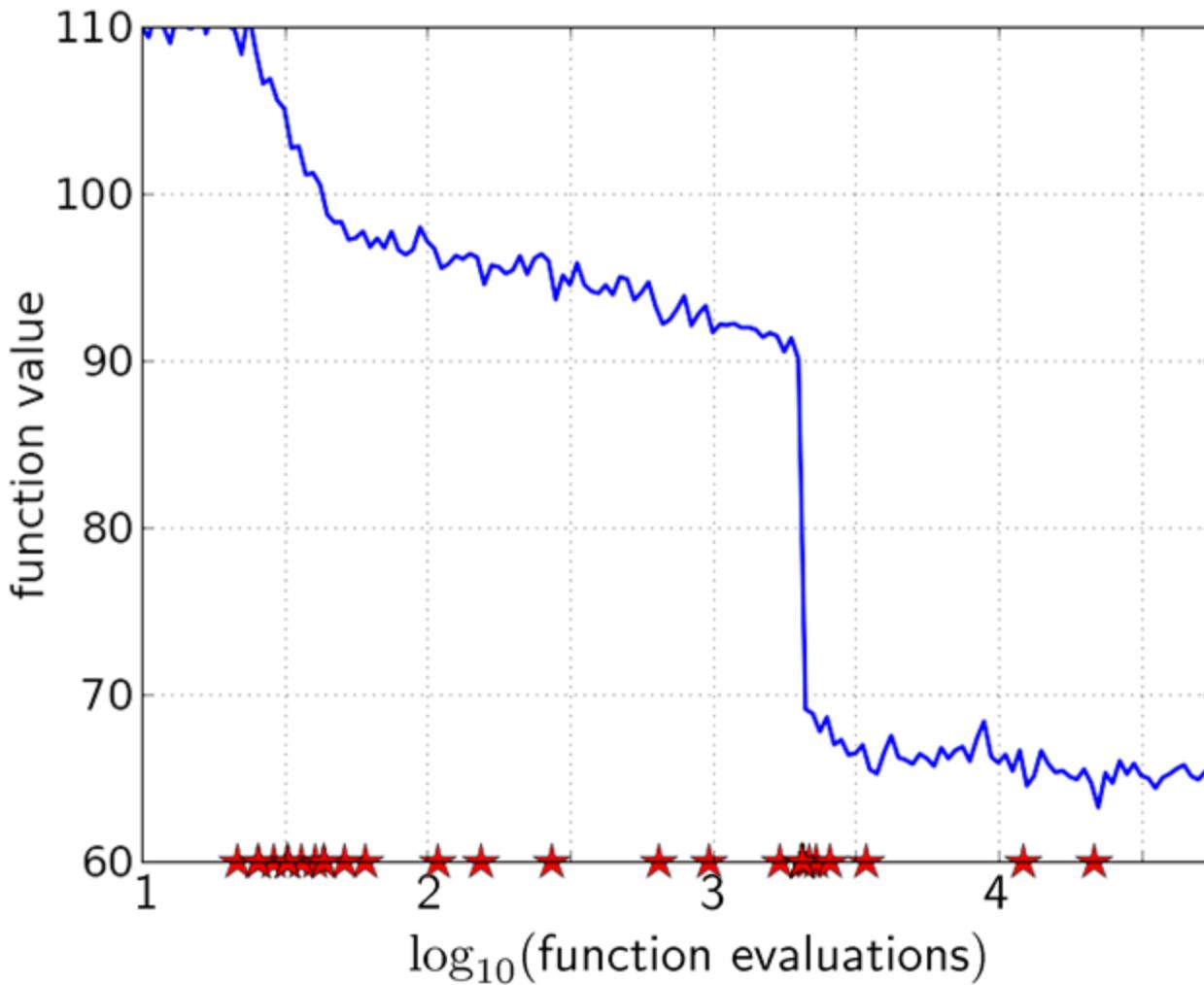


50 equally
spaced targets

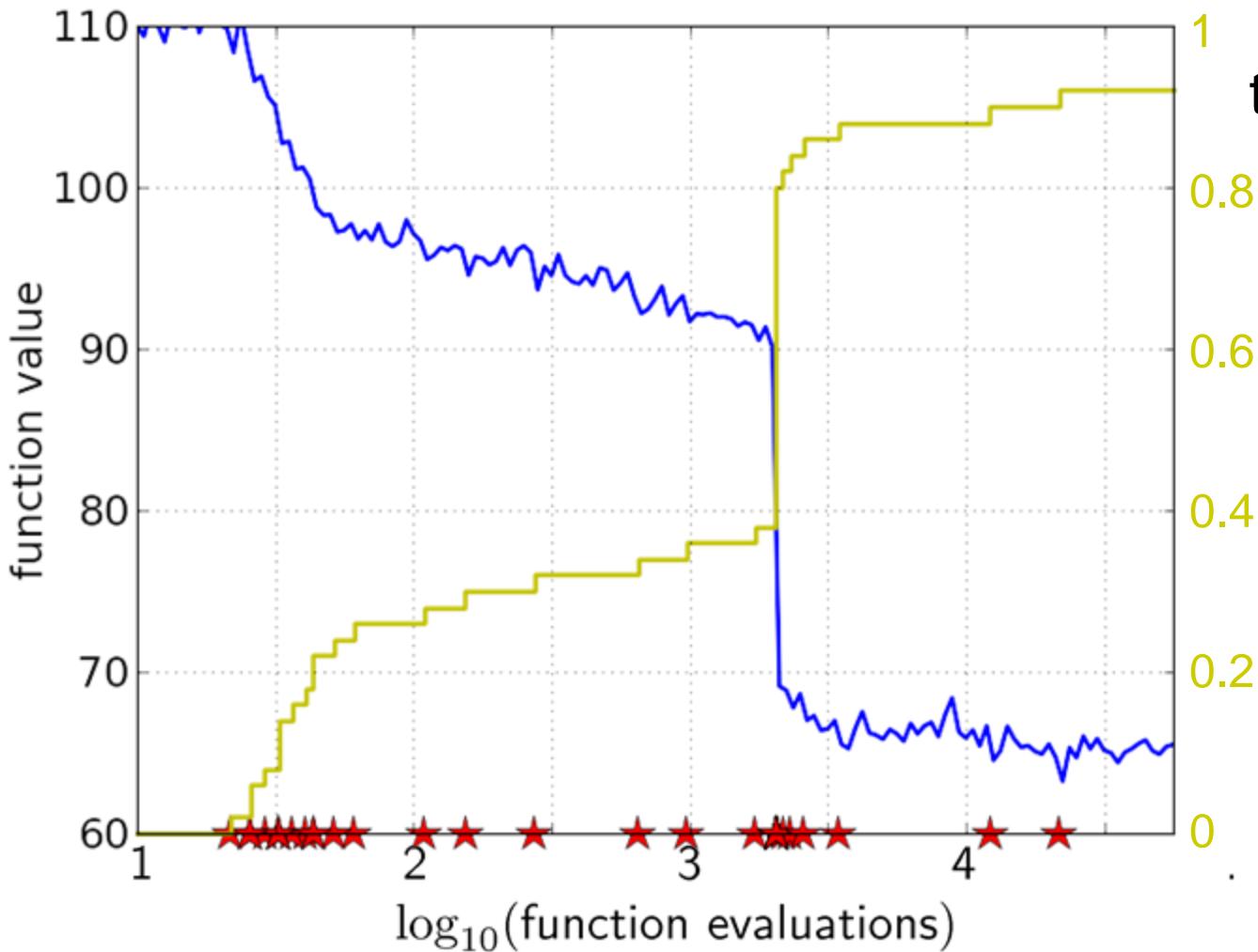
Reconstructing A Single Run



Reconstructing A Single Run

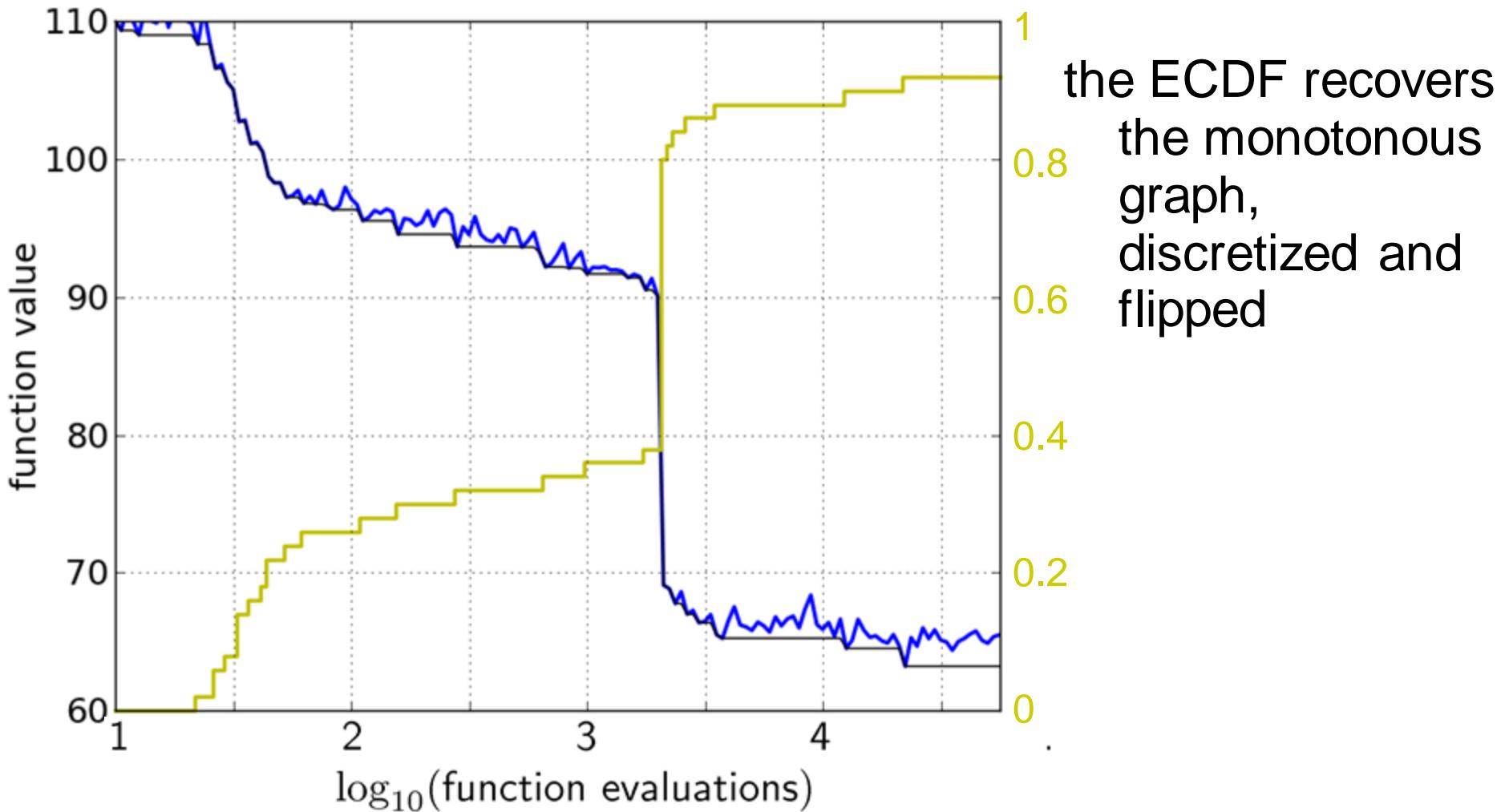


Reconstructing A Single Run

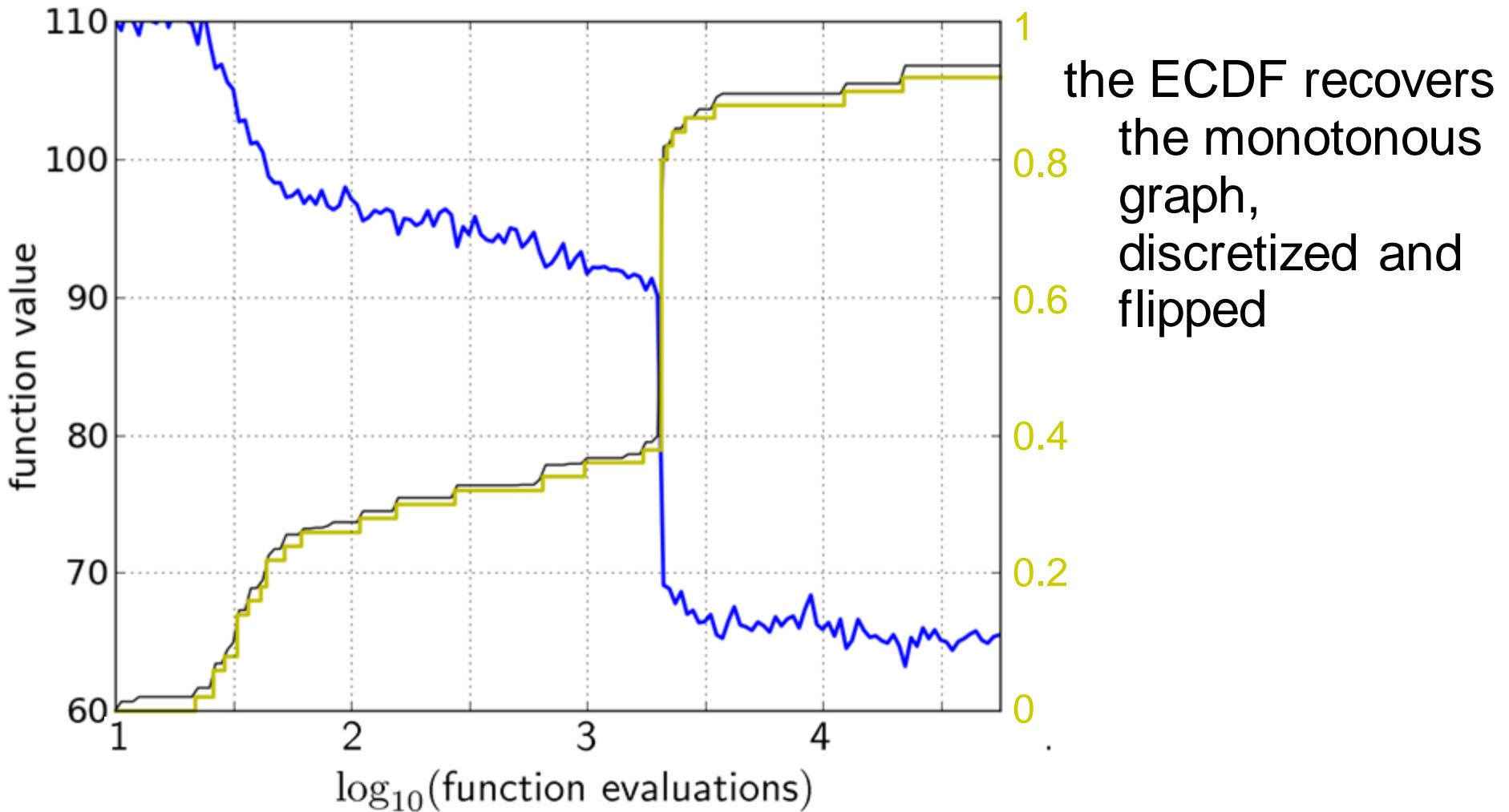


the empirical CDF makes a step for each star, is monotonous and displays for each budget the fraction of targets achieved within the budget

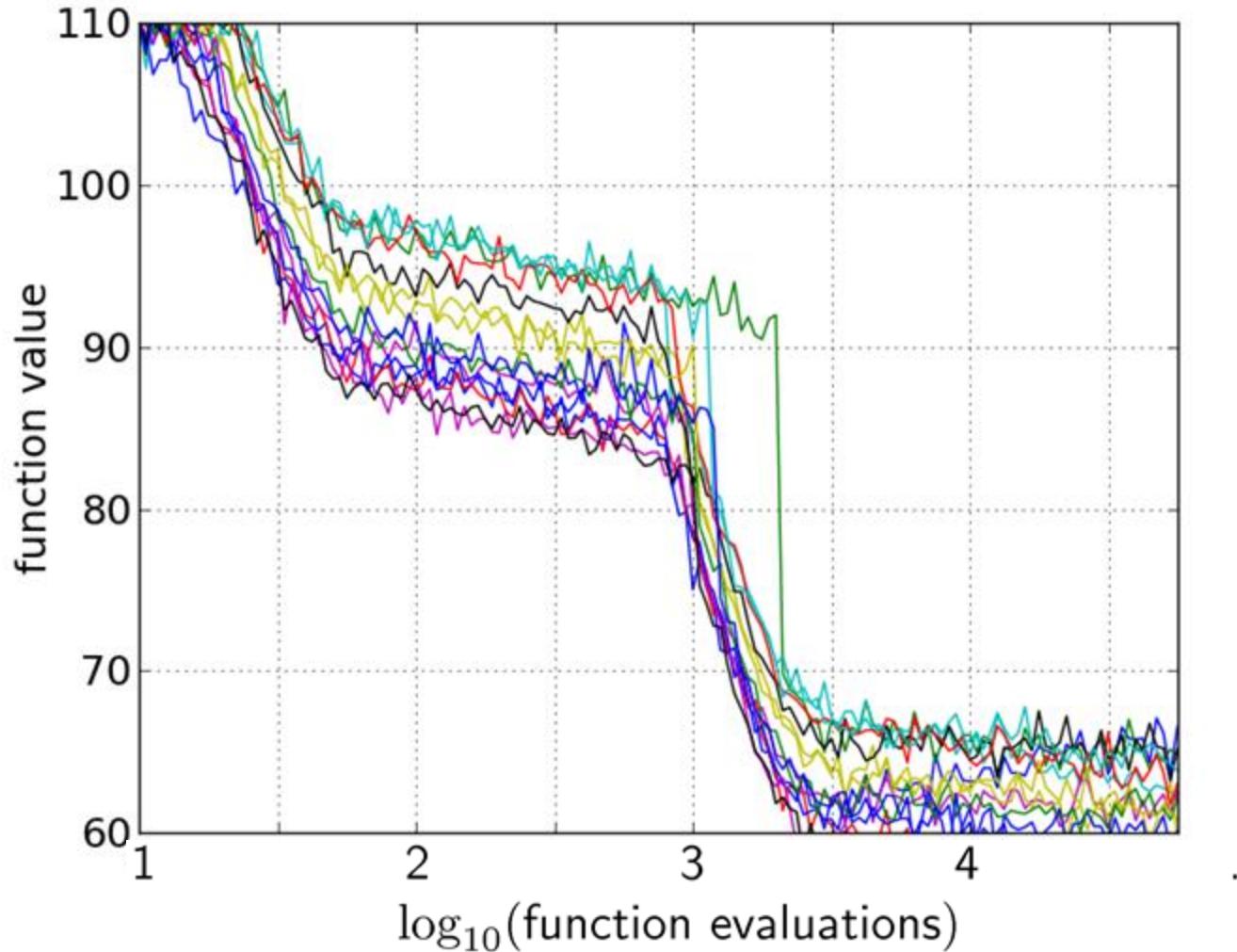
Reconstructing A Single Run



Reconstructing A Single Run

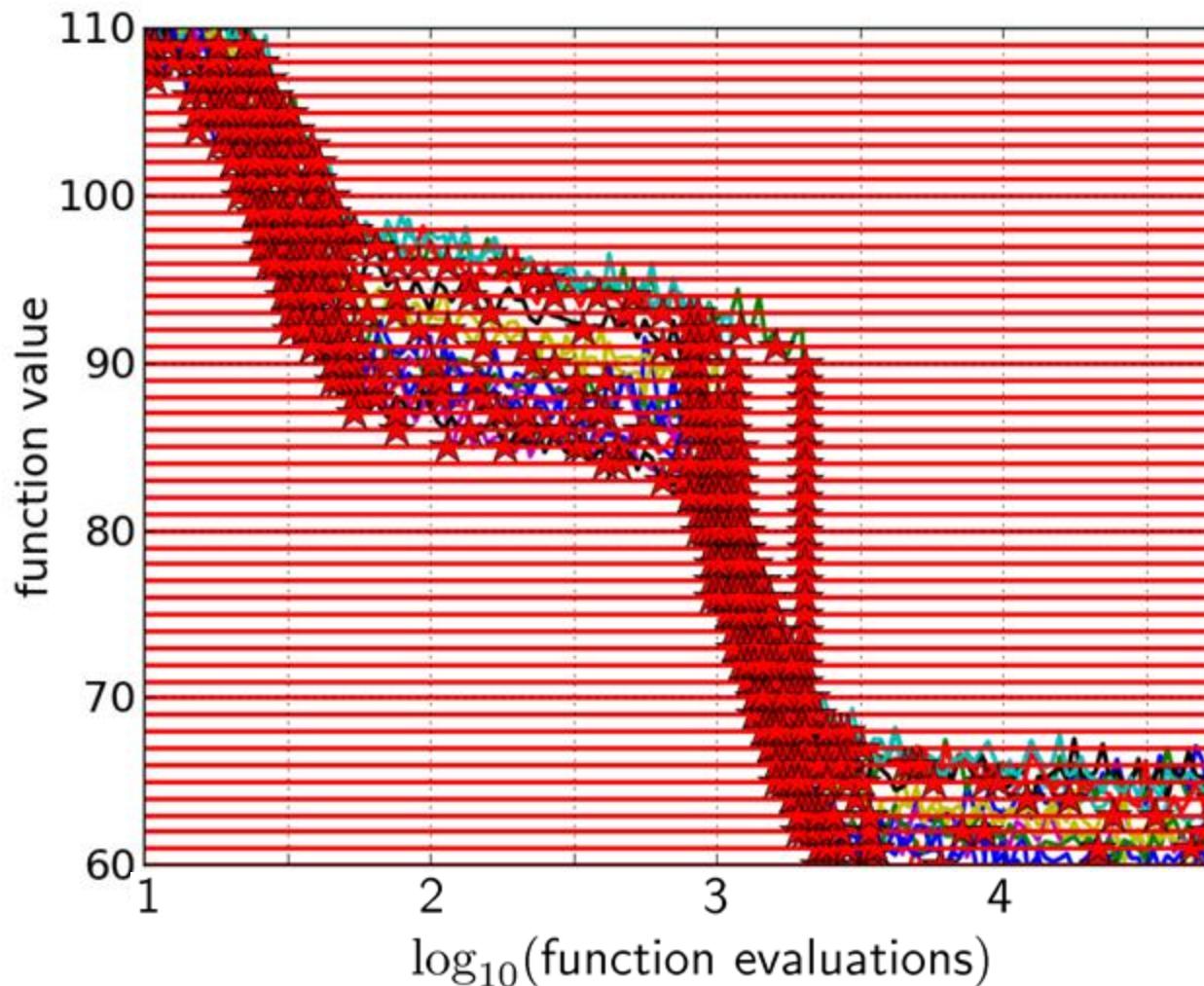


Aggregation



15 runs

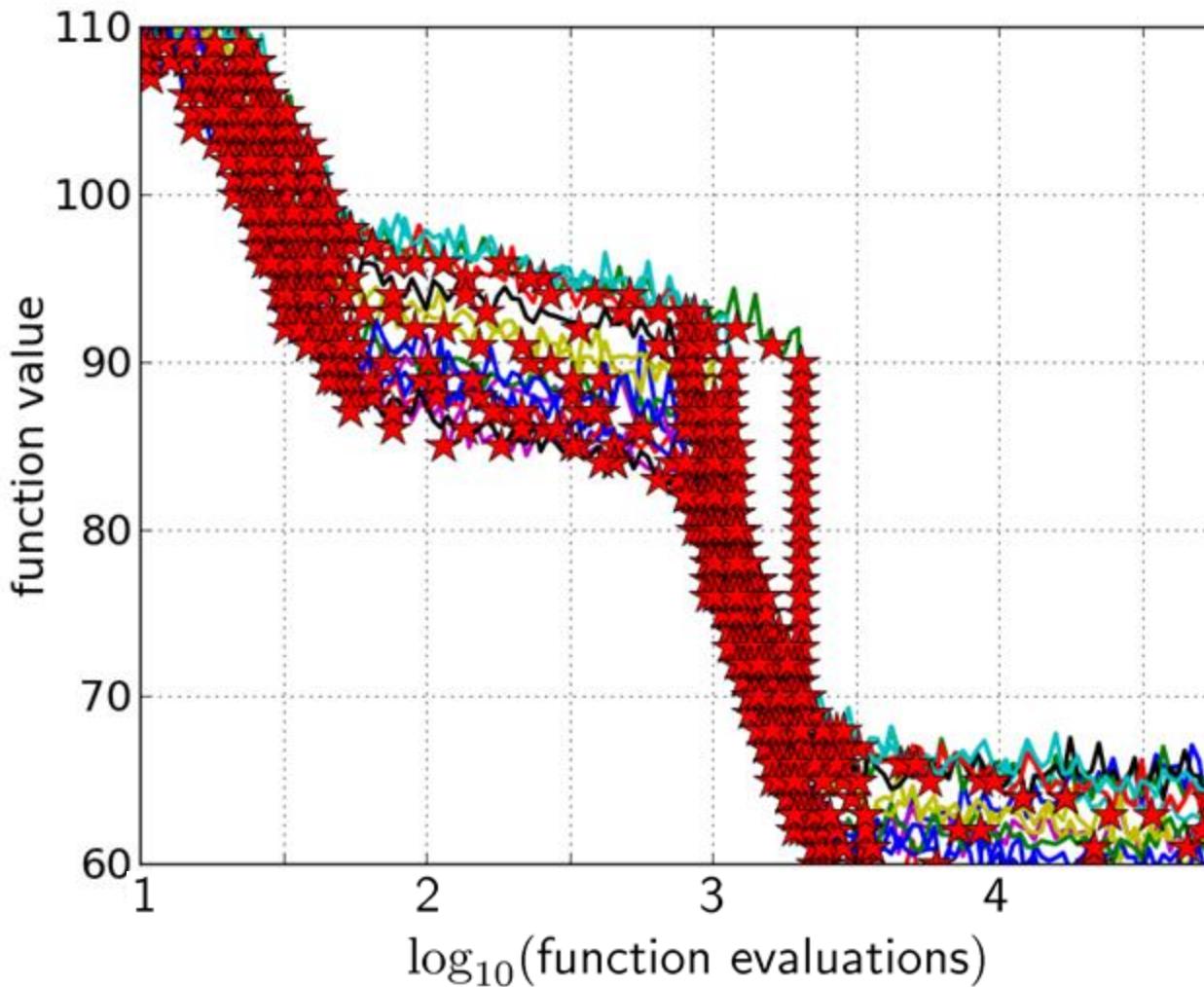
Aggregation



15 runs

50 targets

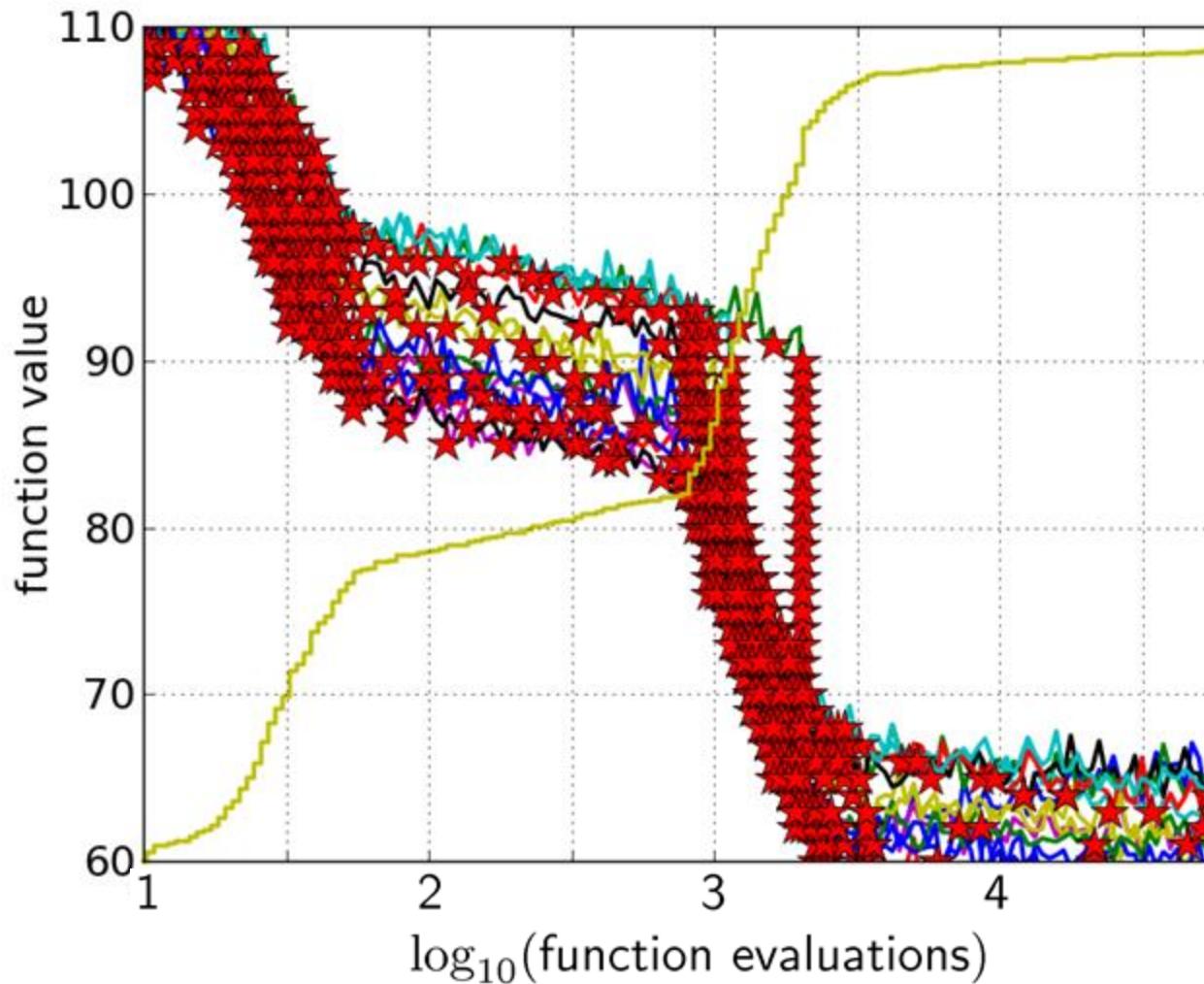
Aggregation



15 runs

50 targets

Aggregation

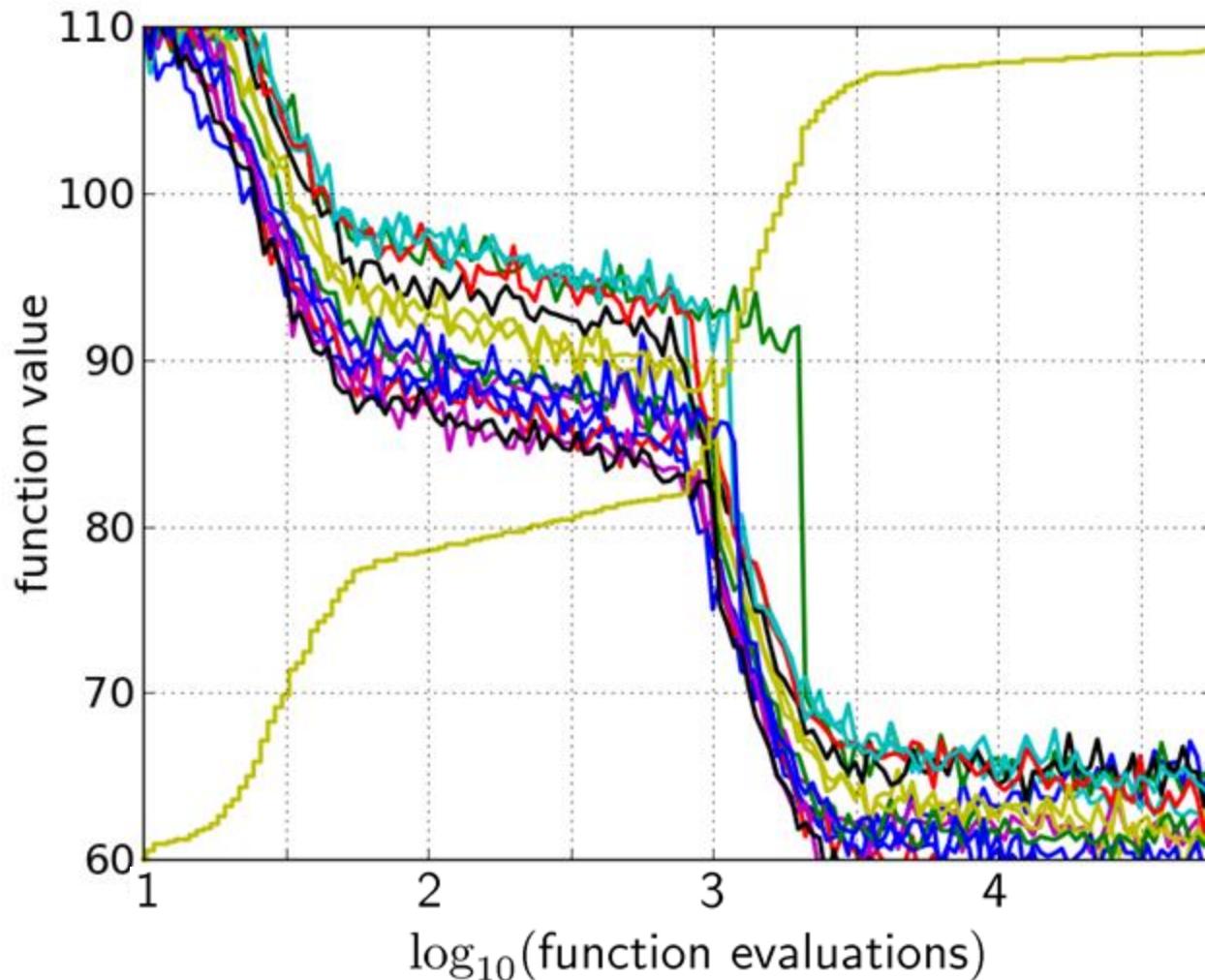


15 runs

50 targets

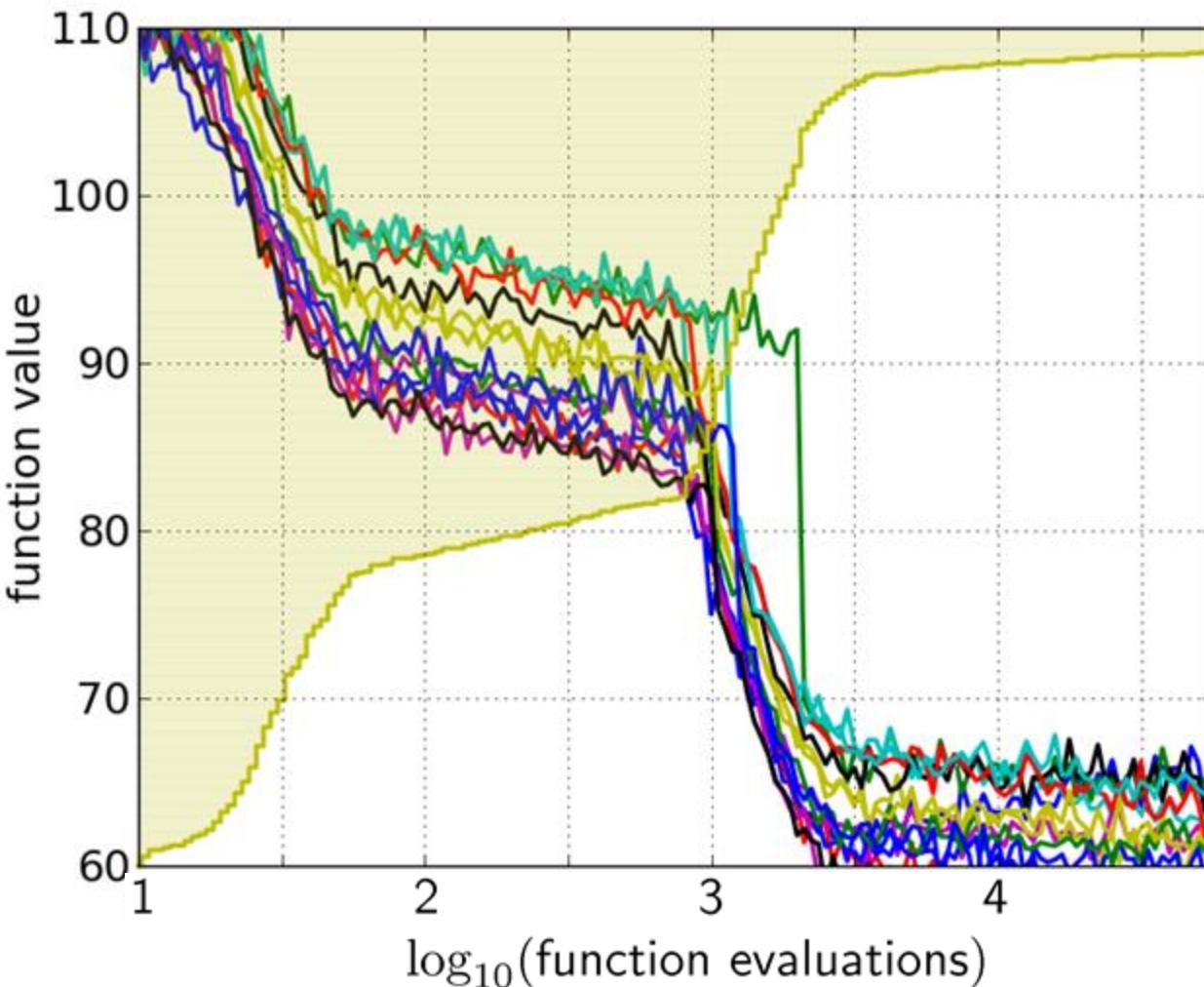
ECDF with 750
steps

Aggregation



50 targets from
15 runs
...integrated in a
single graph

Interpretation



50 targets from
15 runs
integrated in a
single graph

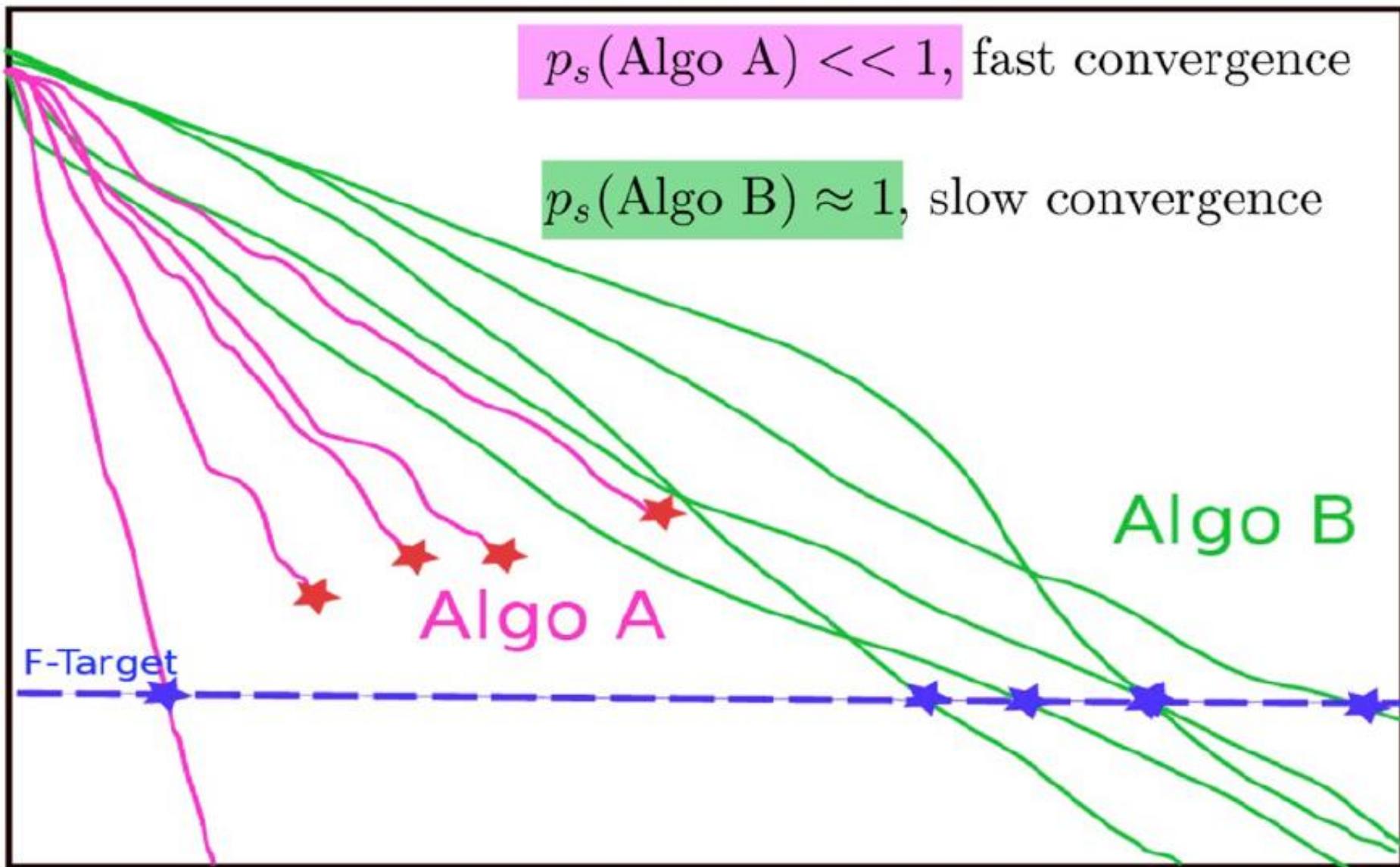
area over the
ECDF curve

=

average log
runtime

(or geometric avg.
runtime) over all
targets (difficult and
easy) and all runs

Fixed-target: Measuring Runtime



Fixed-target: Measuring Runtime

- Algo Restart A:



- Algo Restart B:



Fixed-target: Measuring Runtime

- Expected running time of the restarted algorithm:

$$E[RT^r] = \frac{1 - p_s}{p_s} E[RT_{unsuccessful}] + E[RT_{successful}]$$

- Estimator average running time (aRT):

$$\hat{p}_s = \frac{\text{\#successes}}{\text{\#runs}}$$

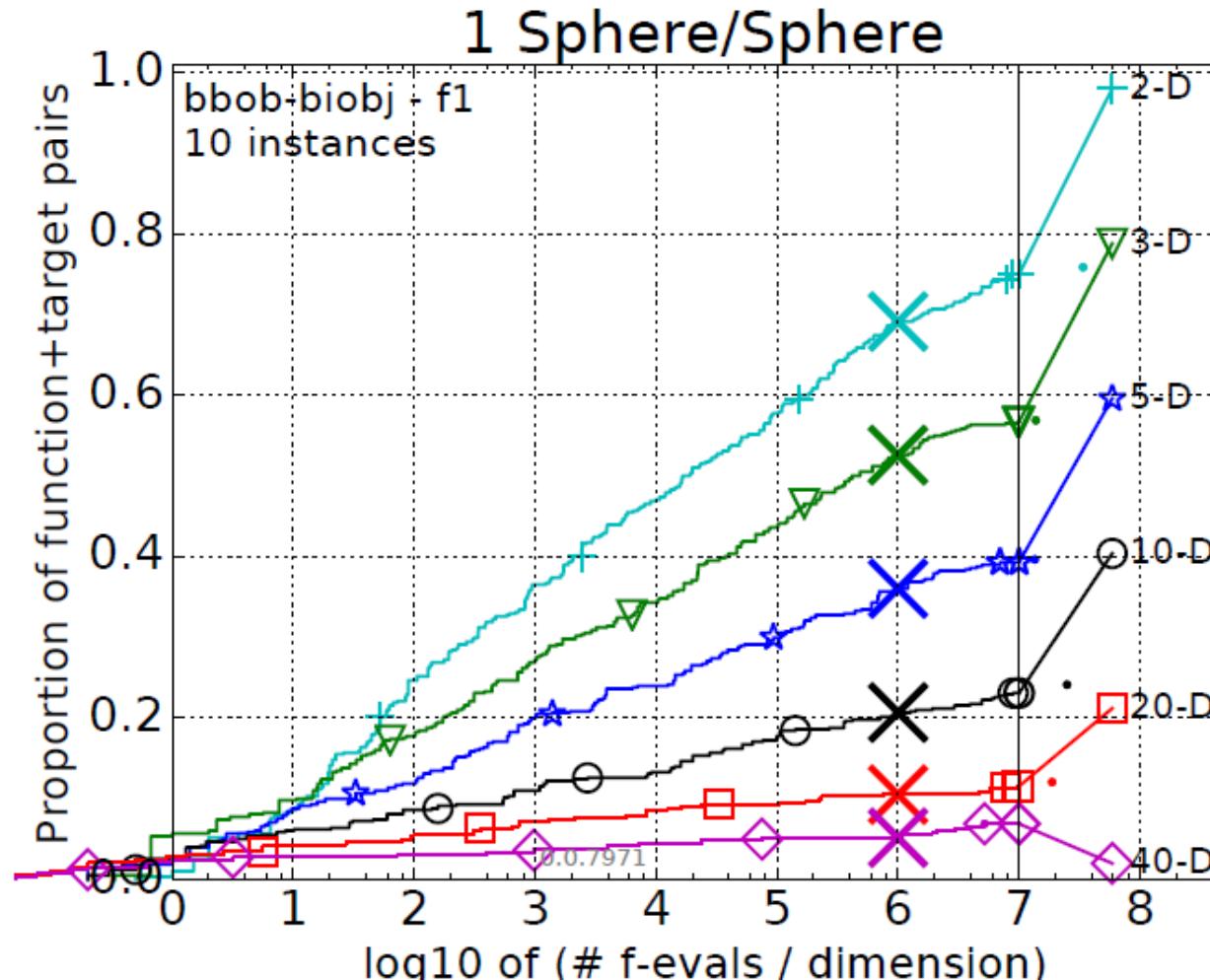
\widehat{RT}_{unsucc} = Average evals of unsuccessful runs

\widehat{RT}_{succ} = Average evals of successful runs

$$aRT = \frac{\text{total \#evals}}{\text{\#successes}}$$

ECDFs with Simulated Restarts

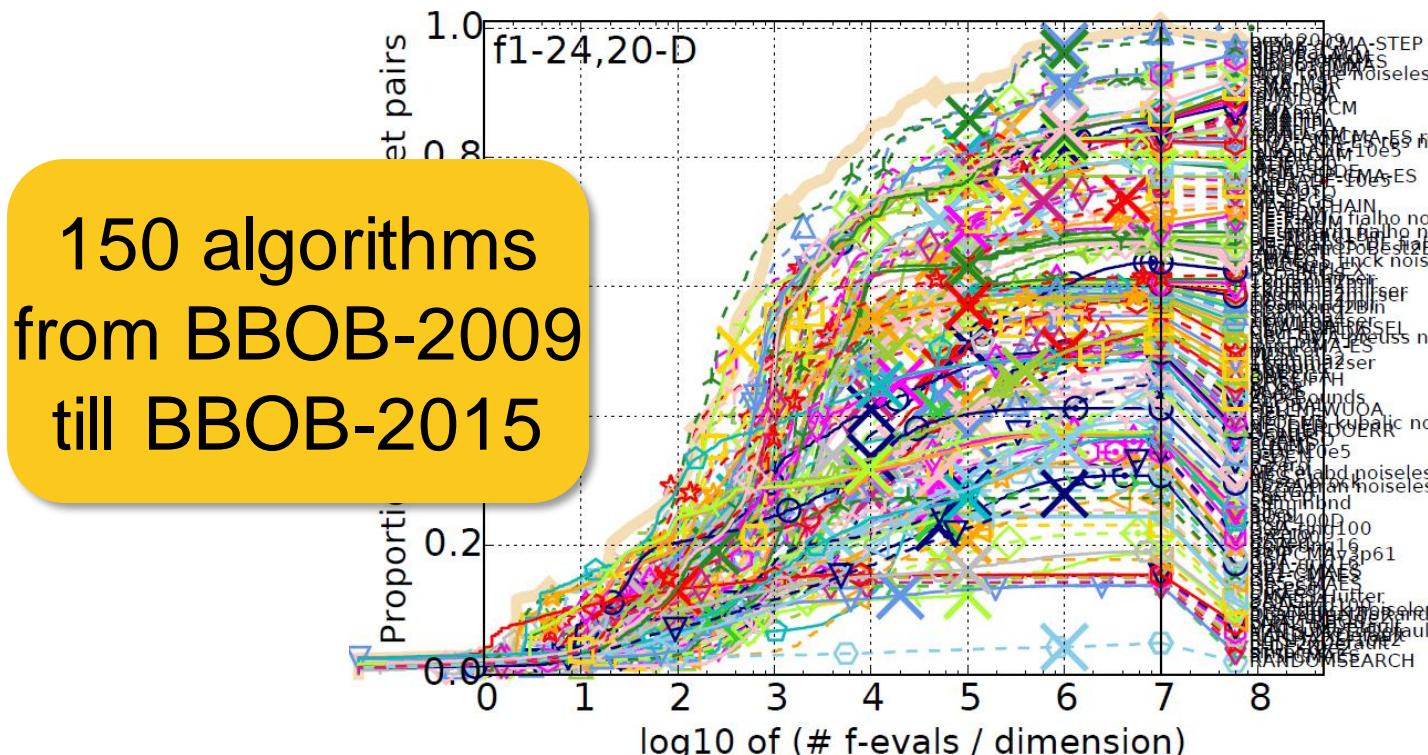
What we typically plot are ECDFs of the simulated restarted algorithms:



Worth to Note: ECDFs in COCO

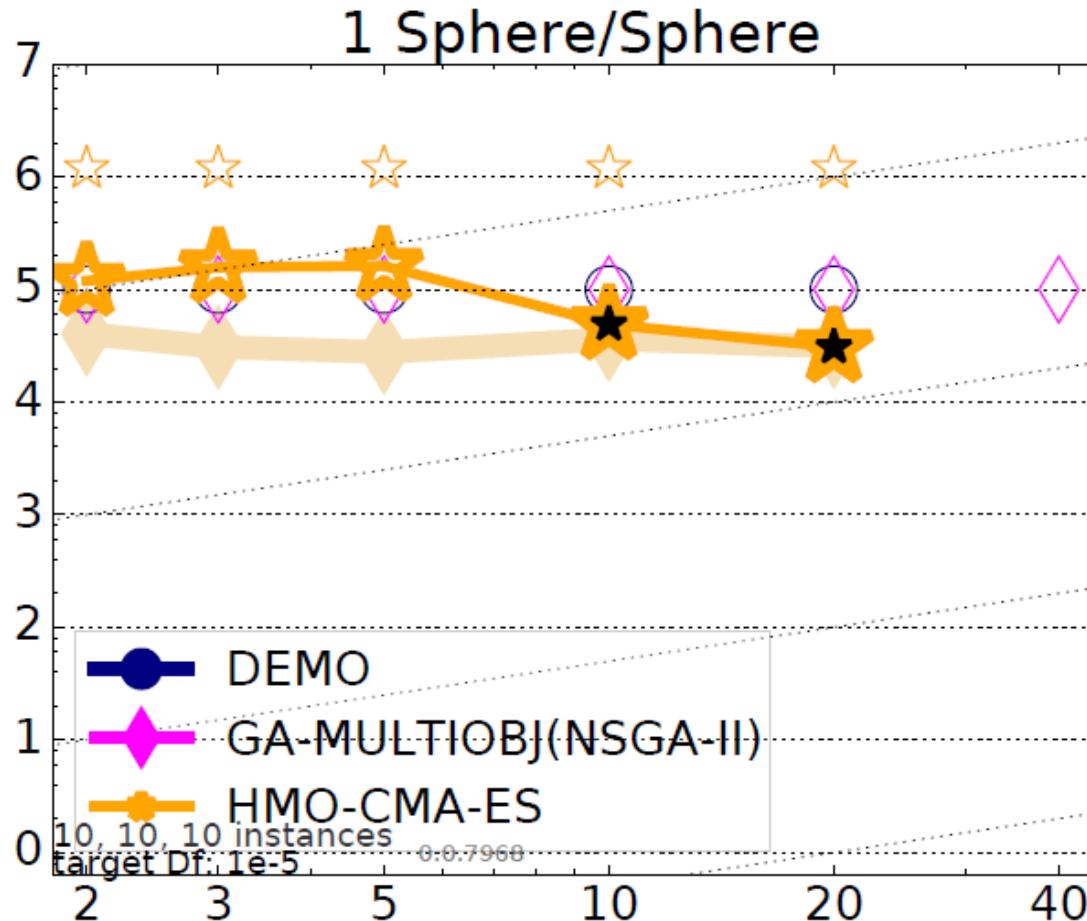
In COCO, ECDF graphs

- never aggregate over dimension
 - but often over targets and functions
- can show data of more than 1 algorithm at a time



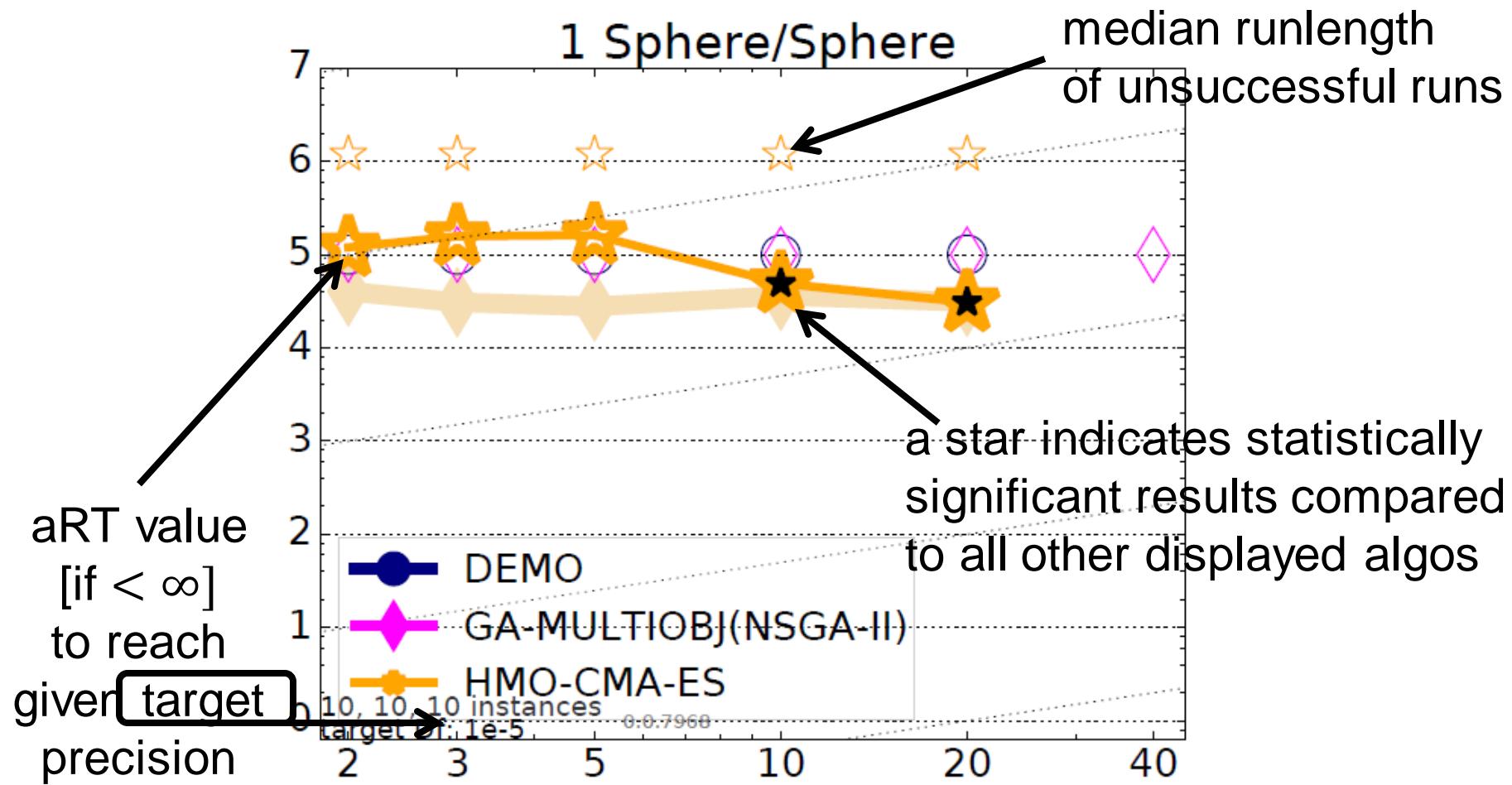
Another Interesting Plot...

...comparing aRT values over several algorithms



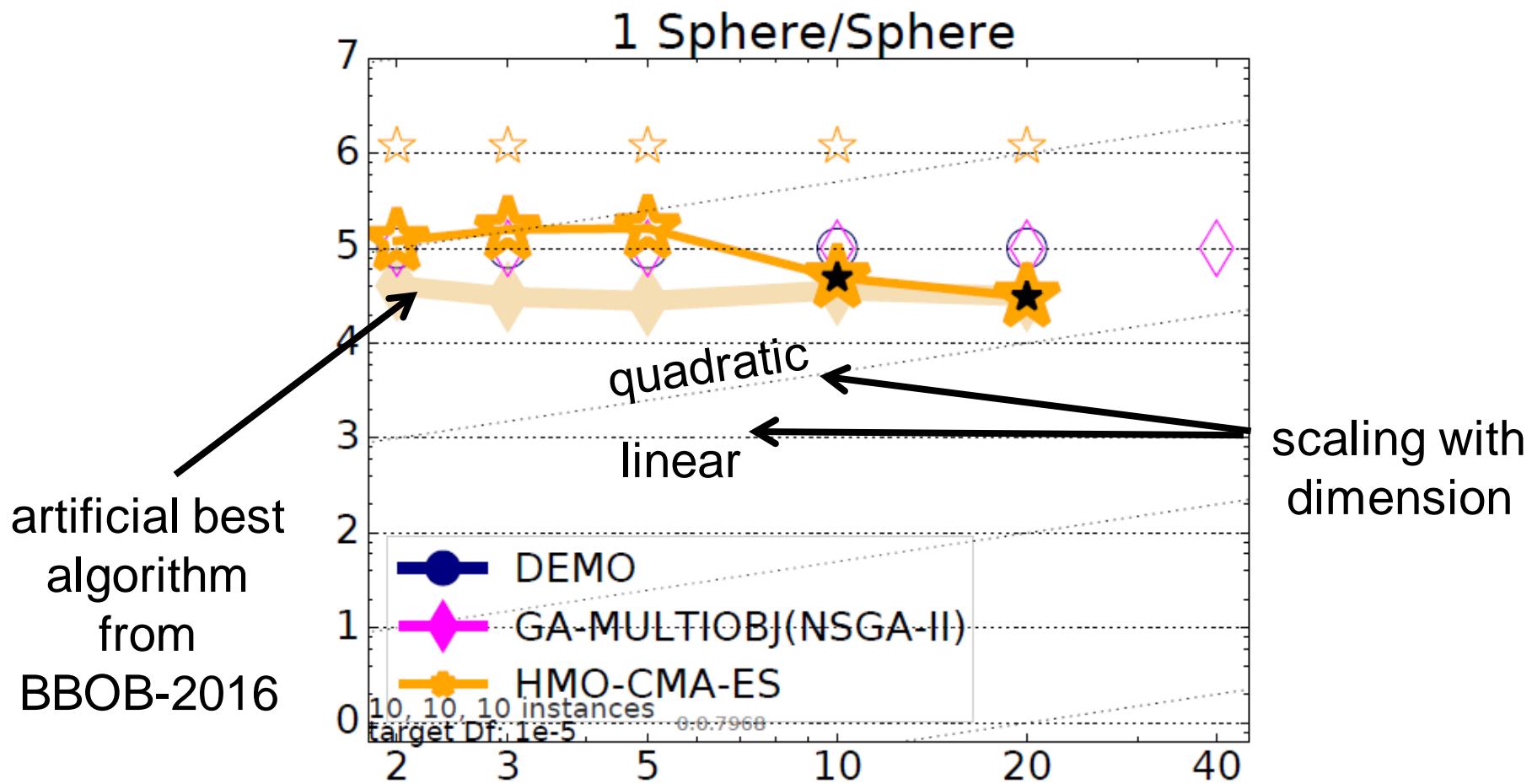
Another Interesting Plot...

...comparing aRT values over several algorithms



Another Interesting Plot...

...comparing aRT values over several algorithms

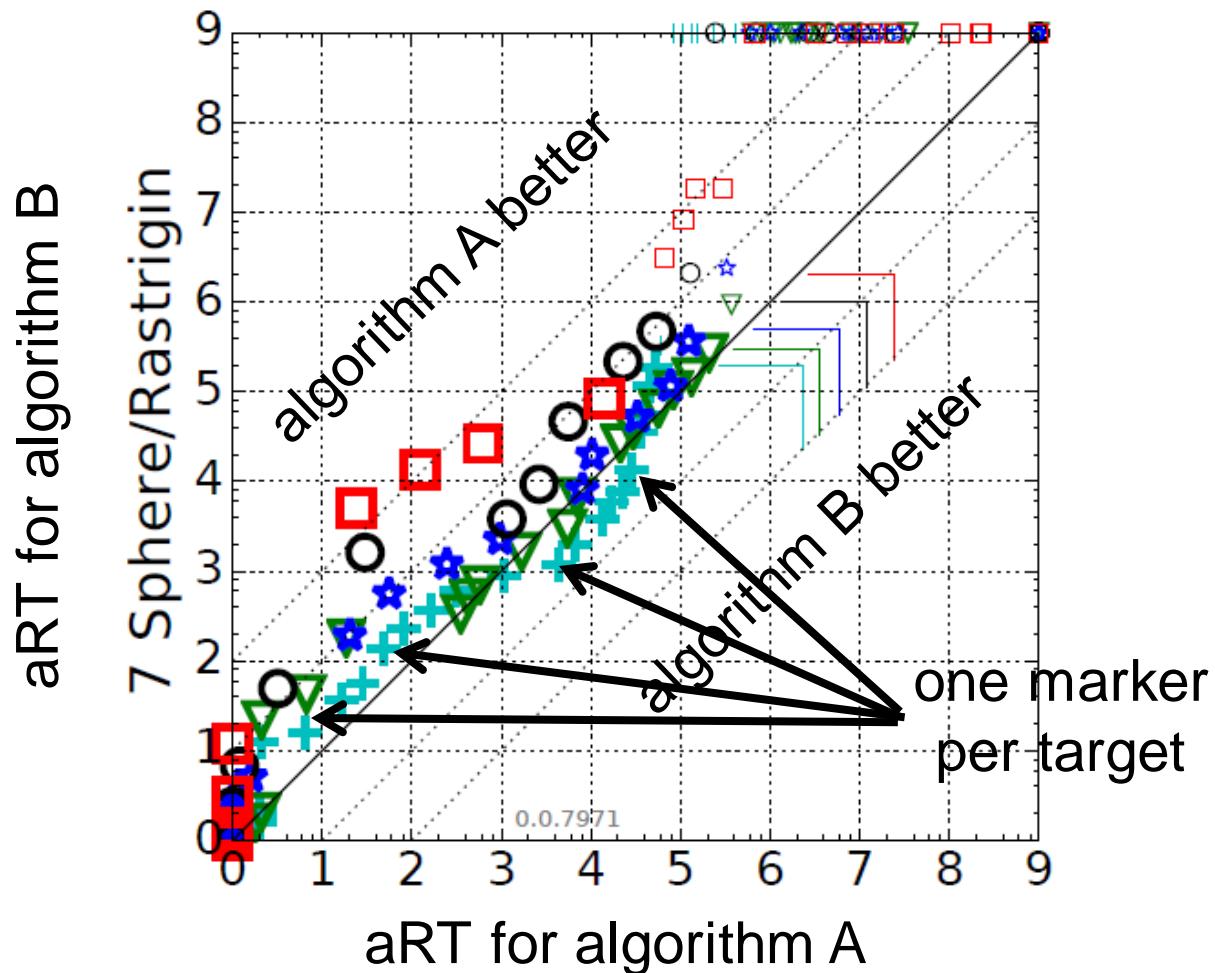


Interesting for 2 Algorithms...

...are scatter plots

dimensions:

2:+, 3: ∇ , 5: \star , 10: \circ , 20: \square , 40: \diamond .



There are more Plots...

...but they are probably less interesting for us here

The single-objective BBOB functions

bbob Testbed

- 24 functions in 5 groups:

1 Separable Functions	
f1	Sphere Function
f2	Ellipsoidal Function
f3	Rastrigin Function
f4	Büche-Rastrigin Function
f5	Linear Slope
2 Functions with low or moderate conditioning	
f6	Attractive Sector Function
f7	Step Ellipsoidal Function
f8	Rosenbrock Function, original
f9	Rosenbrock Function, rotated
3 Functions with high conditioning and unimodal	
f10	Ellipsoidal Function
f11	Discus Function
f12	Bent Cigar Function
f13	Sharp Ridge Function
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4 Multi-modal functions with adequate global structure	
f15	Rastrigin Function
f16	Weierstrass Function
f17	Schaffers F7 Function
f18	Schaffers F7 Functions, moderately ill-conditioned
f19	Composite Griewank-Rosenbrock Function F8F2
5 Multi-modal functions with weak global structure	
f20	Schwefel Function
f21	Gallagher's Gaussian 101-me Peaks Function
f22	Gallagher's Gaussian 21-hi Peaks Function
f23	Katsuura Function
f24	Lunacek bi-Rastrigin Function

- 6 dimensions: 2, 3, 5, 10, 20, (40 optional)

Notion of Instances

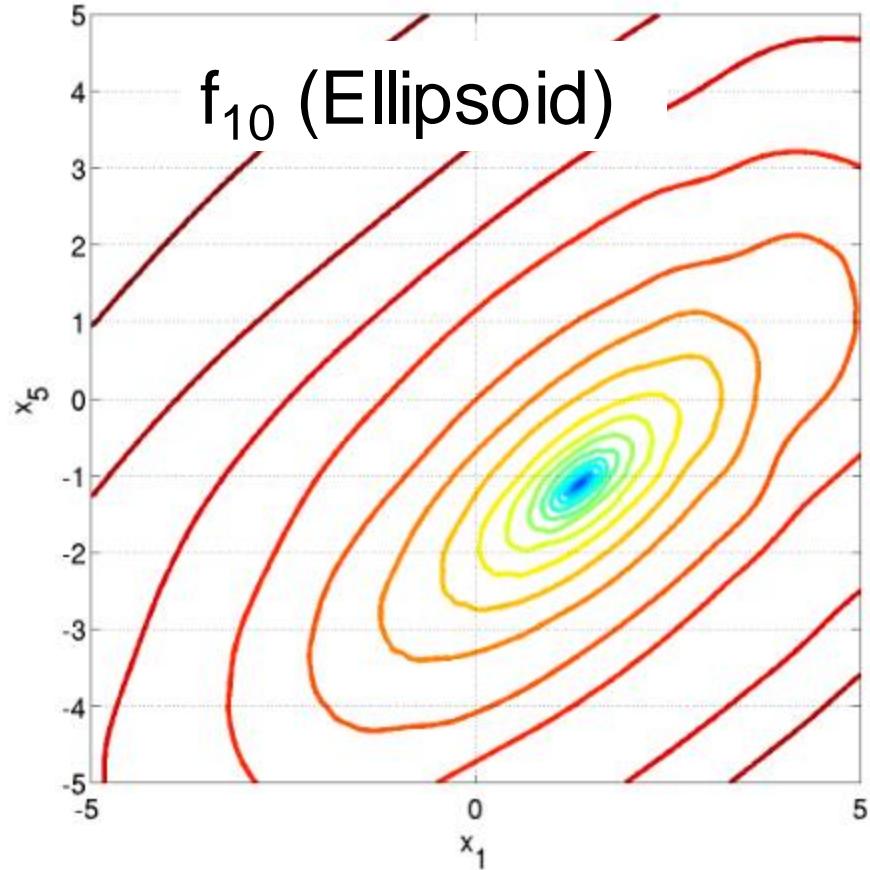
- All COCO problems come in form of instances
 - e.g. as translated/rotated versions of the same function
- Prescribed instances typically change from year to year
 - avoid overfitting
 - 5 instances are always kept the same

Plus:

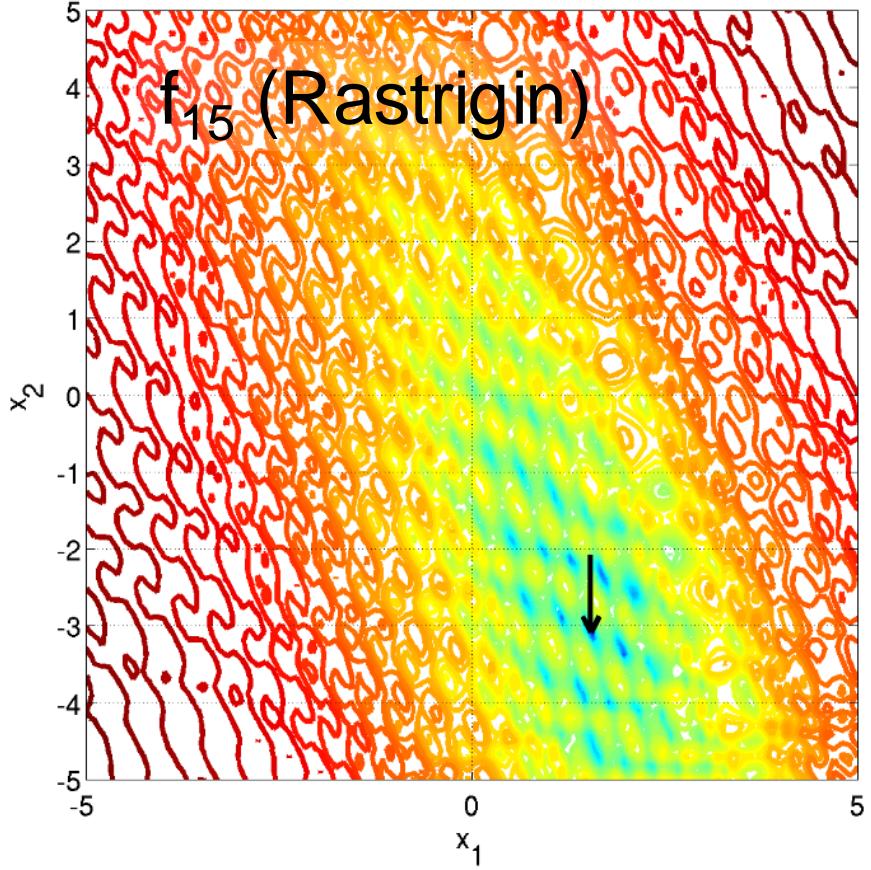
- the bbo functions are locally perturbed by non-linear transformations

Notion of Instances

- All optimization problems come in form of instances



linear transformations

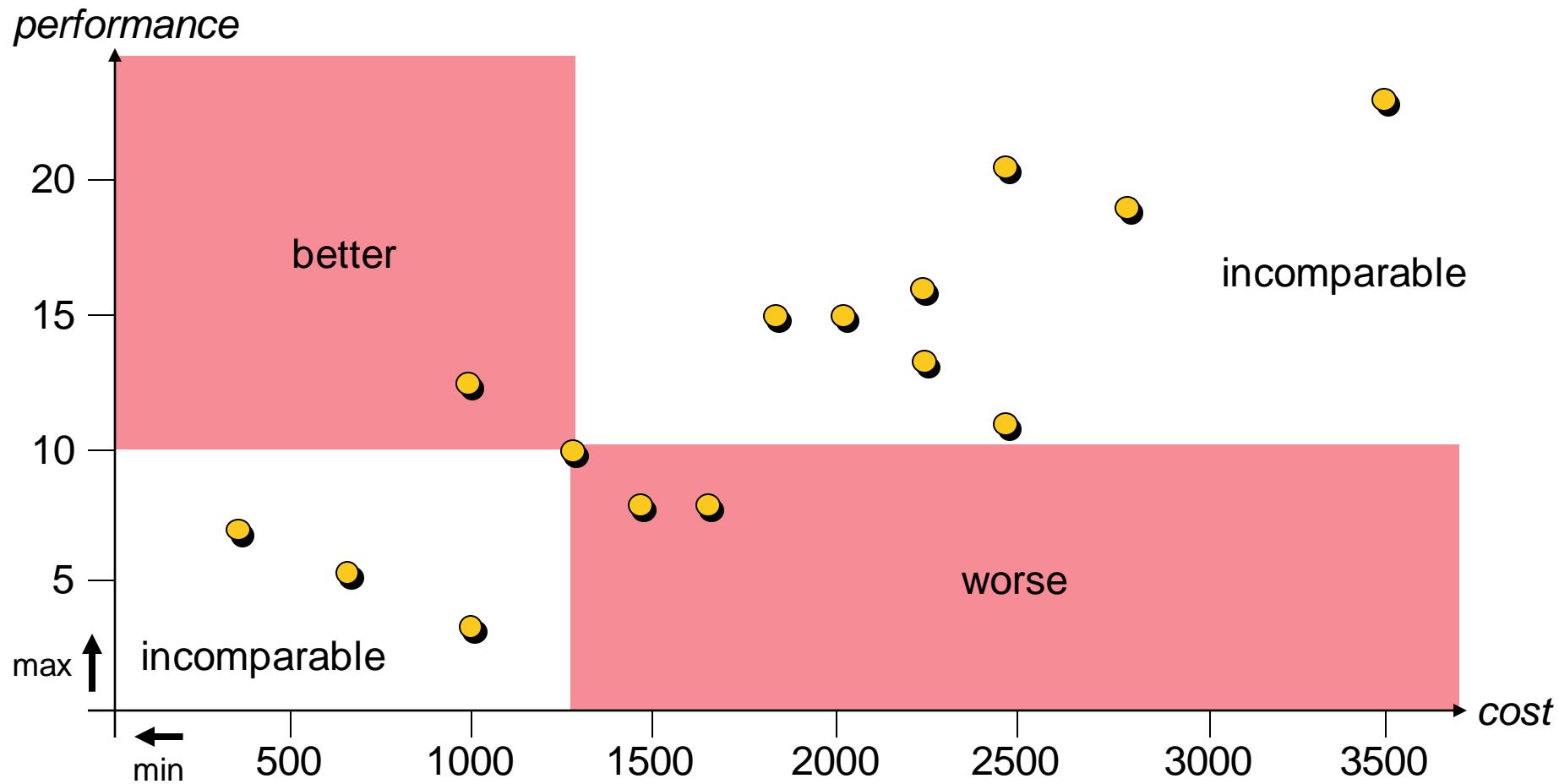


**the recent extension to
multi-objective optimization**

A Brief Introduction to Multiobjective Optimization

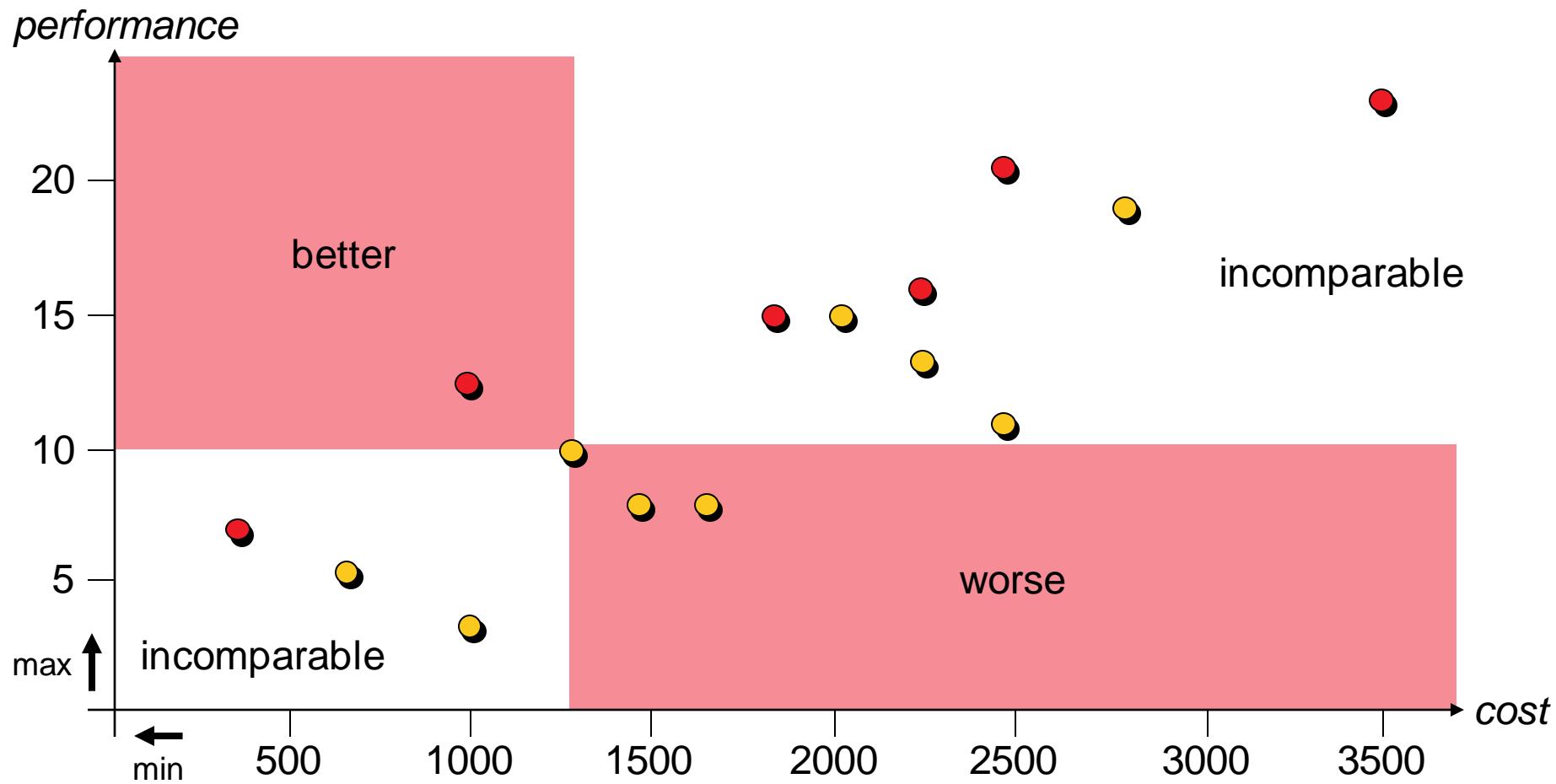
Multiobjective Optimization (MOO)

Multiple objectives that have to be optimized simultaneously



A Brief Introduction to Multiobjective Optimization

Observations: ① there is no single optimal solution, but
② some solutions (●) are better than others (○)

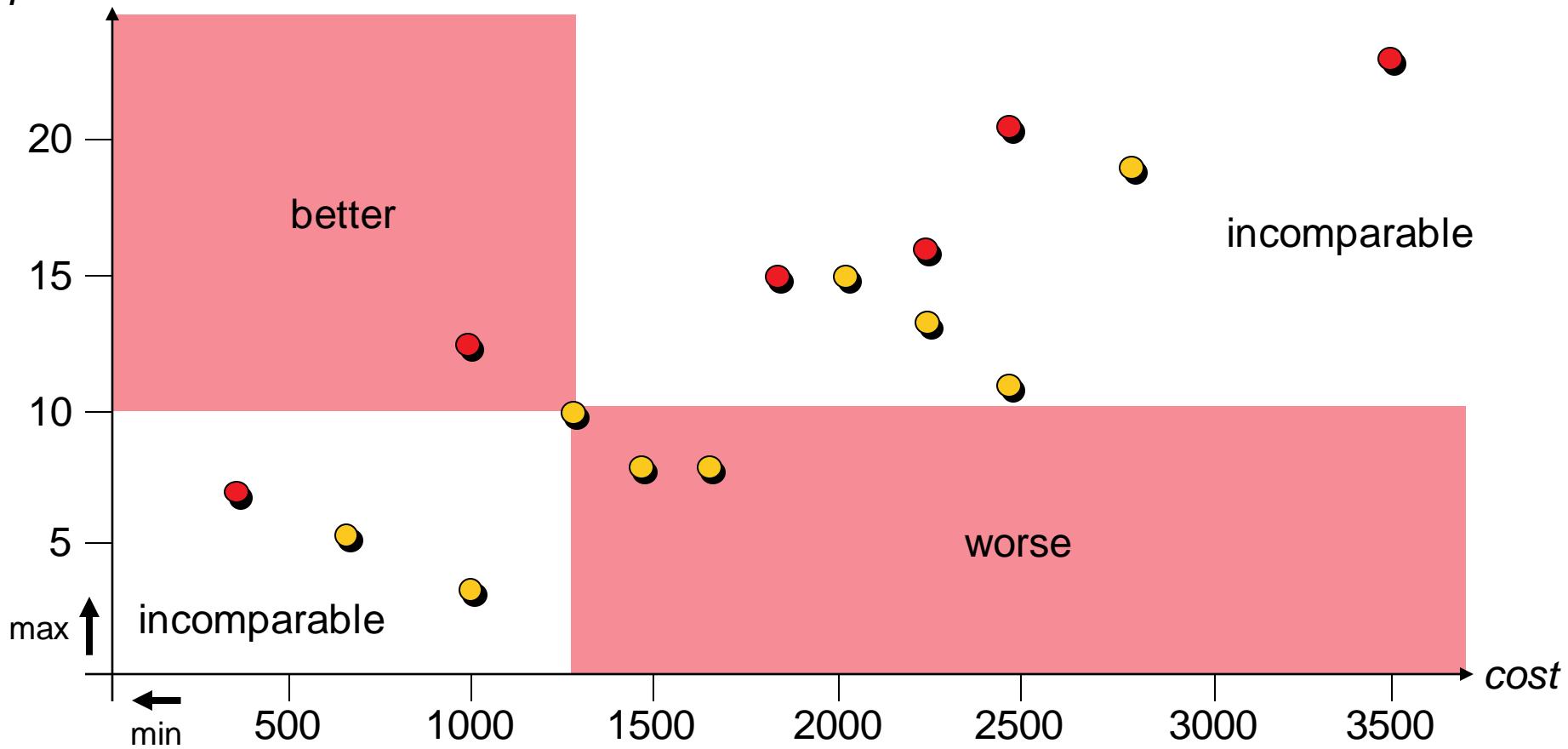


A Brief Introduction to Multiobjective Optimization

u weakly Pareto dominates v ($u \leqslant_{par} v$): $\forall 1 \leq i \leq k : f_i(u) \leq f_i(v)$

u Pareto dominates v ($u <_{par} v$): $u \leqslant_{par} v \wedge v \not\leqslant_{par} u$

performance

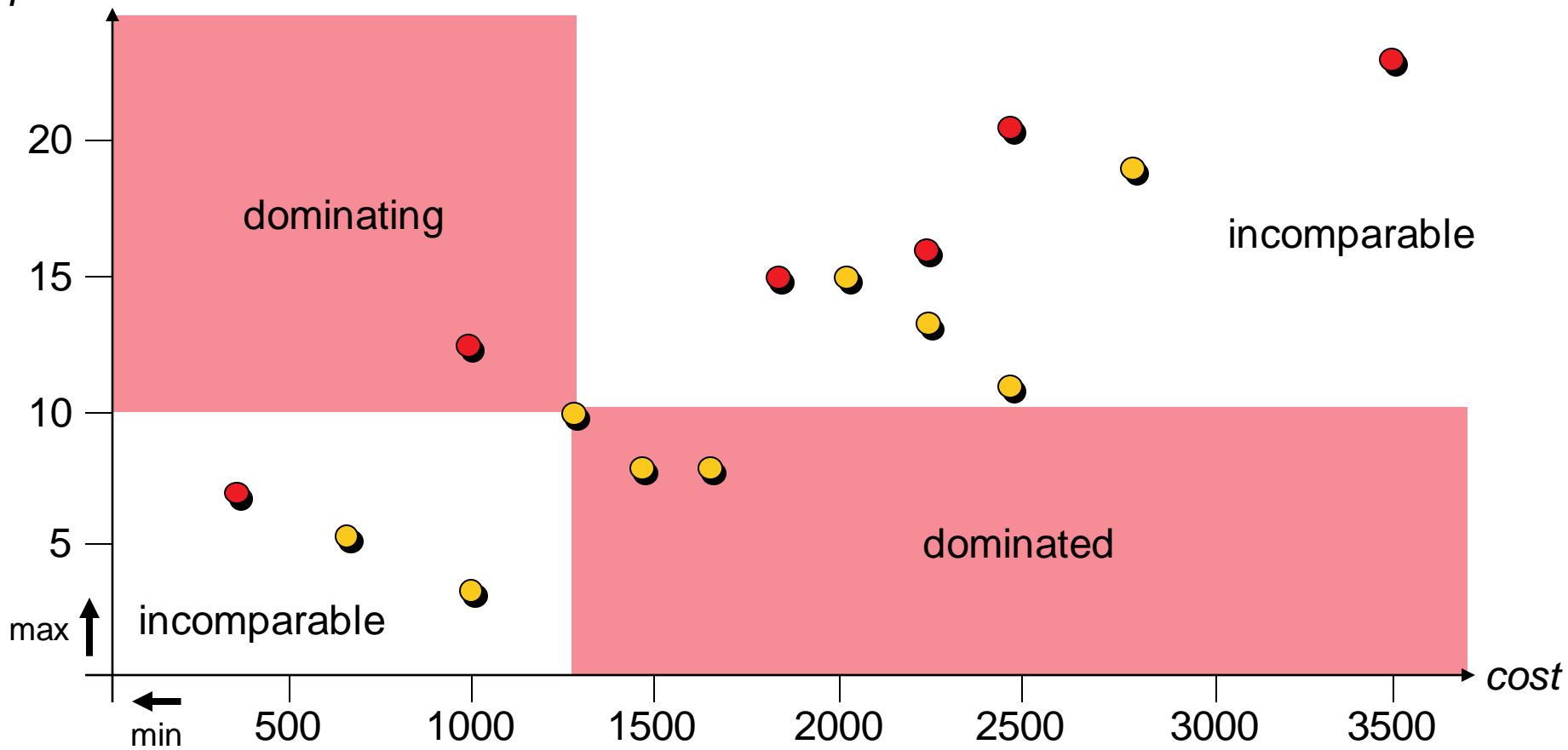


A Brief Introduction to Multiobjective Optimization

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u Pareto dominates v ($u <_{par} v$): $u \leqslant_{par} v \wedge v \not\leqslant_{par} u$

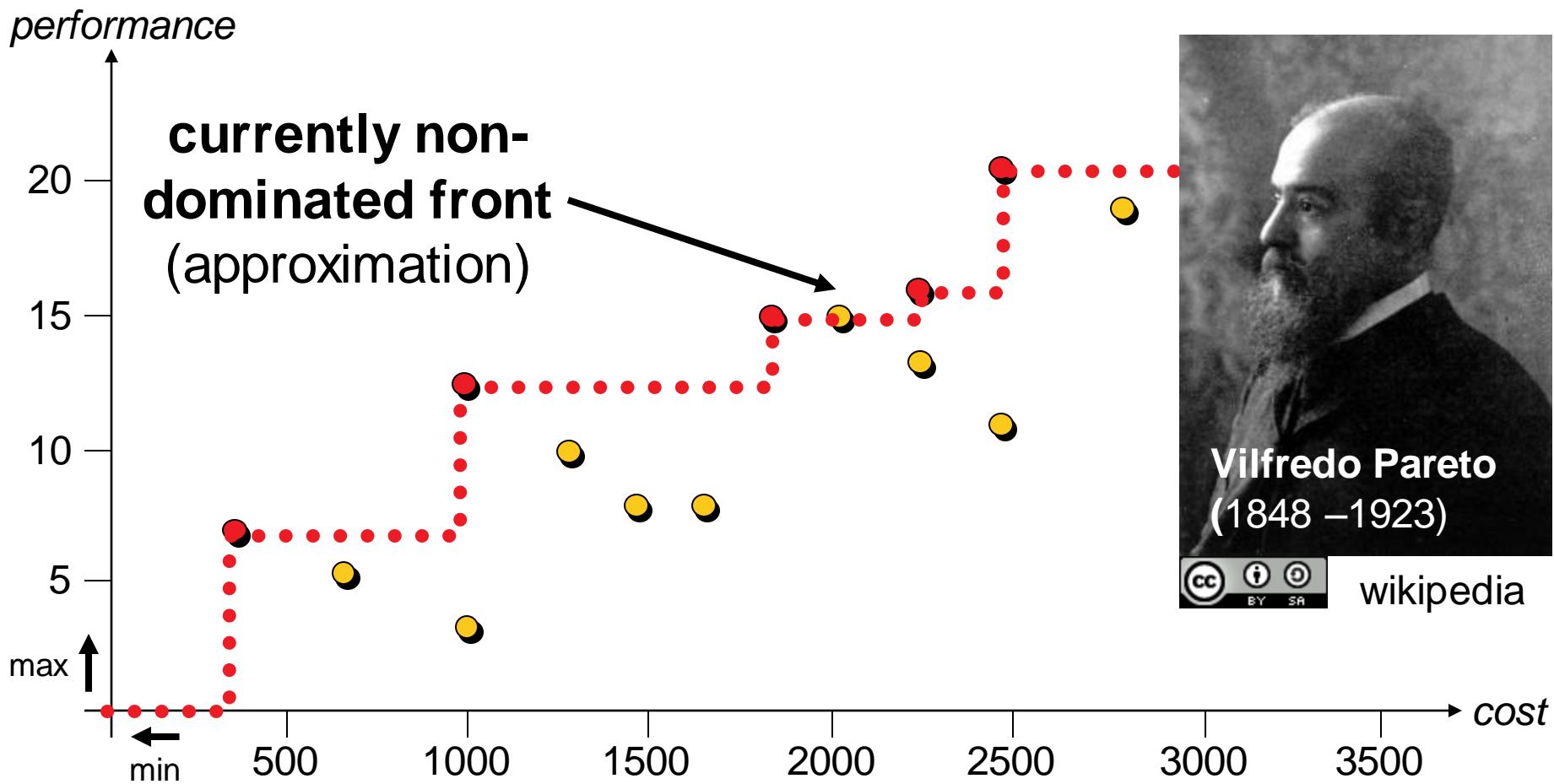
performance



A Brief Introduction to Multiobjective Optimization

Pareto set: set of all non-dominated solutions (decision space)

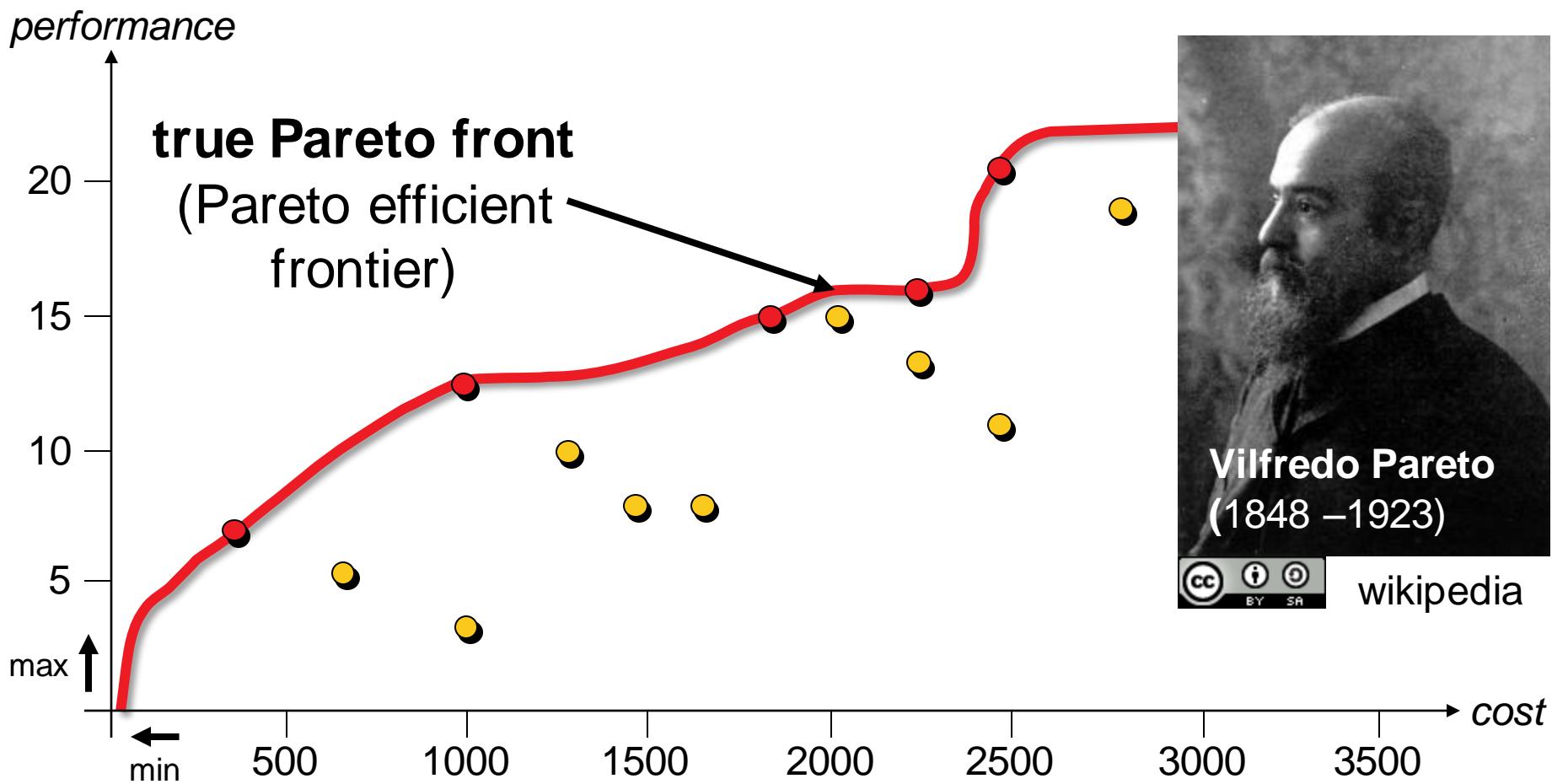
Pareto front: its image in the objective space



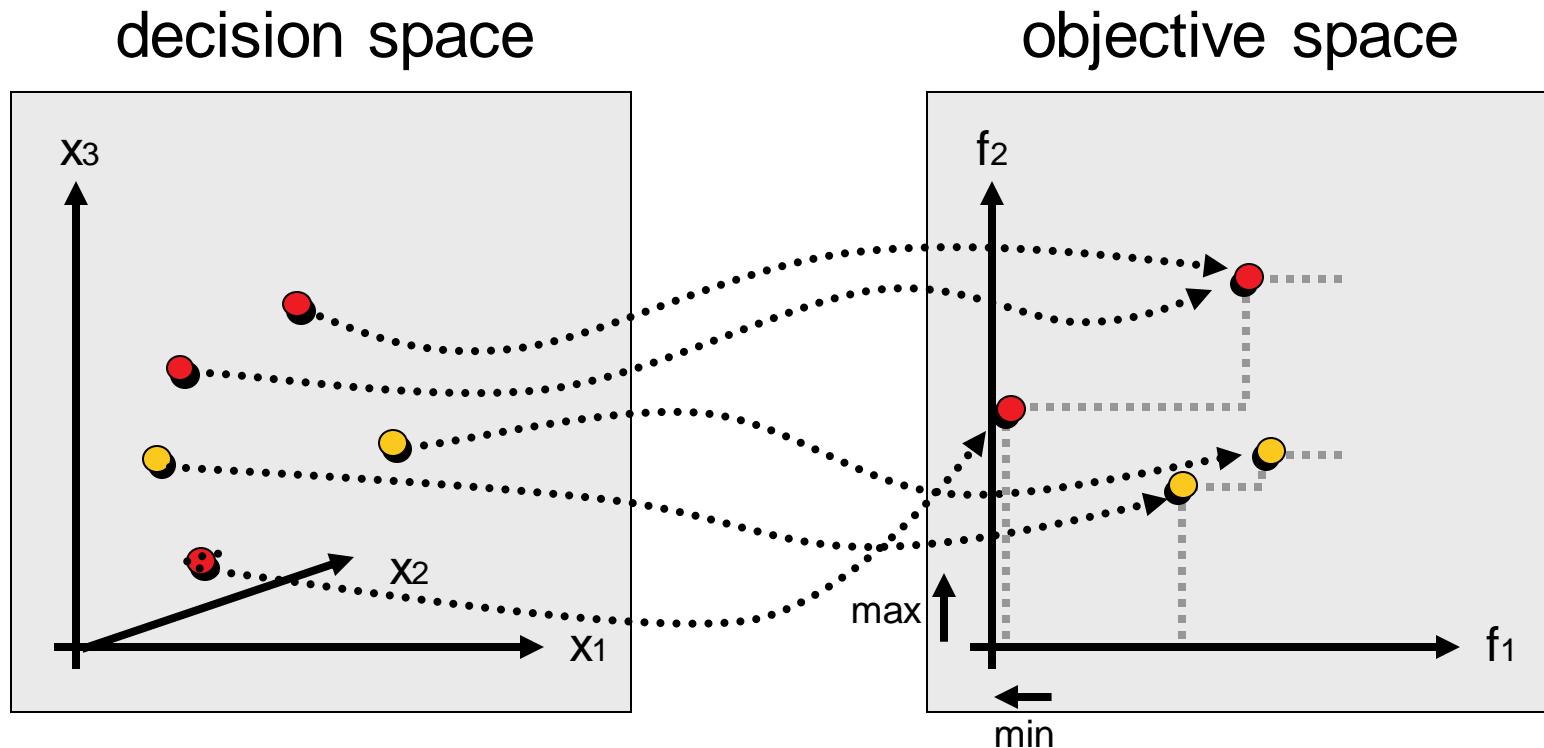
A Brief Introduction to Multiobjective Optimization

Pareto set: set of all non-dominated solutions (decision space)

Pareto front: its image in the objective space



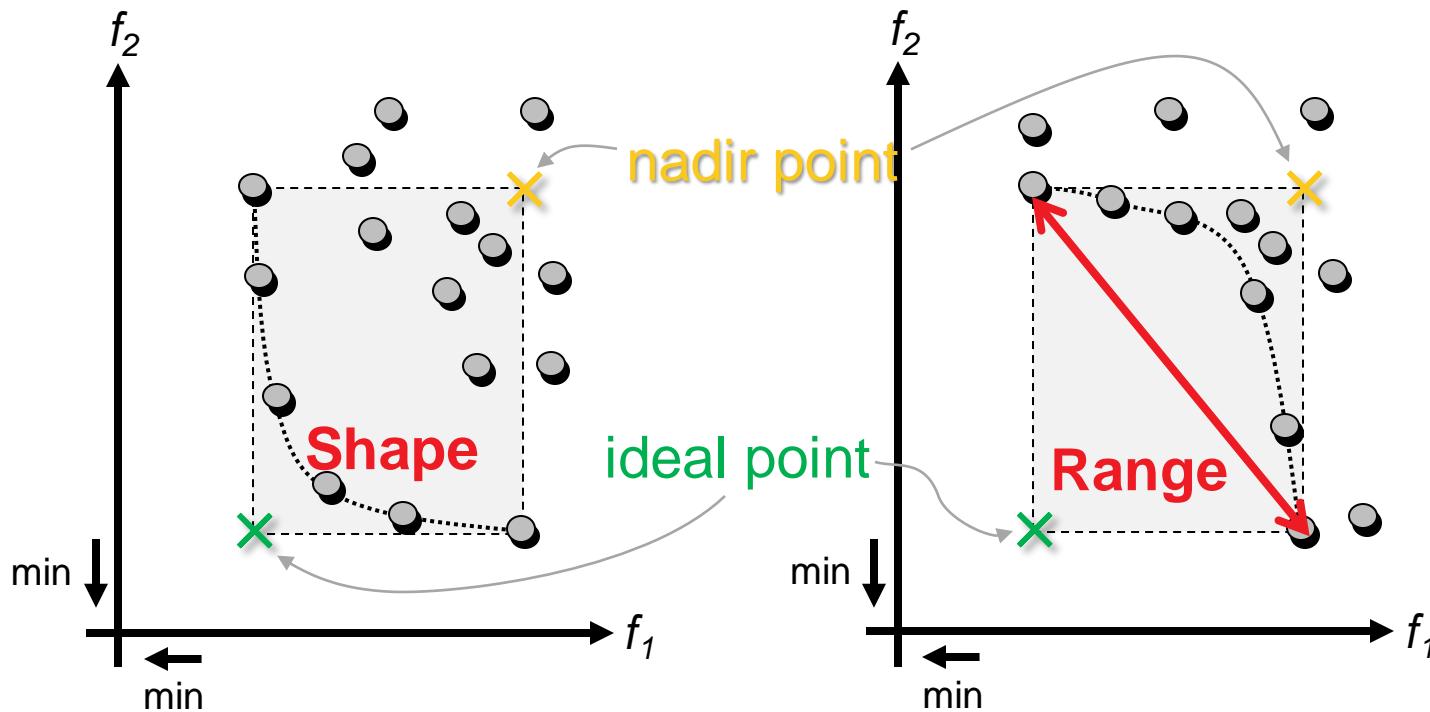
A Brief Introduction to Multiobjective Optimization



solution of Pareto-optimal set
non-optimal **decision vector**

- vector of Pareto-optimal front
- non-optimal **objective vector**

A Brief Introduction to Multiobjective Optimization



ideal point: best values
nadir point: worst values } obtained for *Pareto-optimal* points

Quality Indicator Approach to MOO

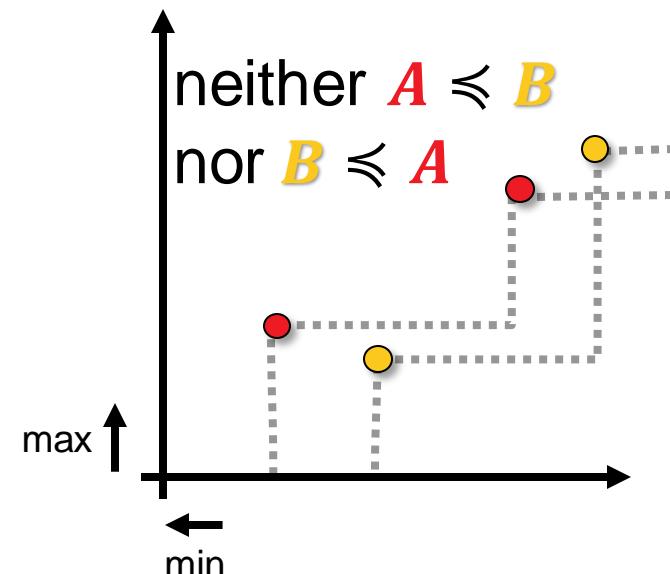
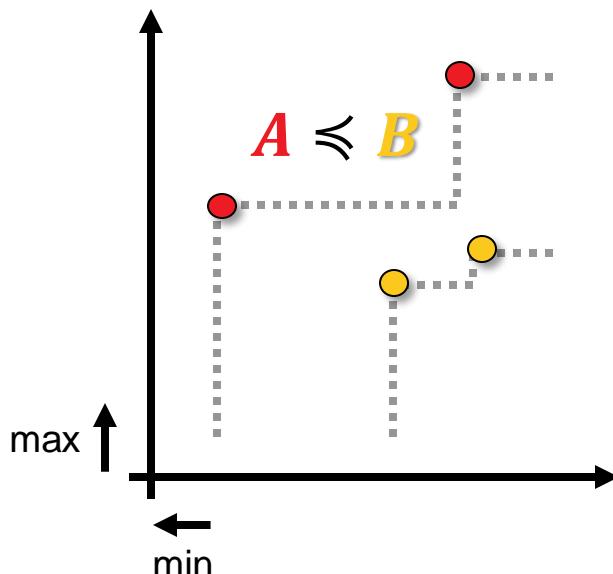
Idea:

- transfer multiobjective problem into a set problem
- define an objective function (“quality indicator”) on sets

Important:

⇒ Underlying dominance relation (**on sets**) should be reflected by the resulting set comparisons!

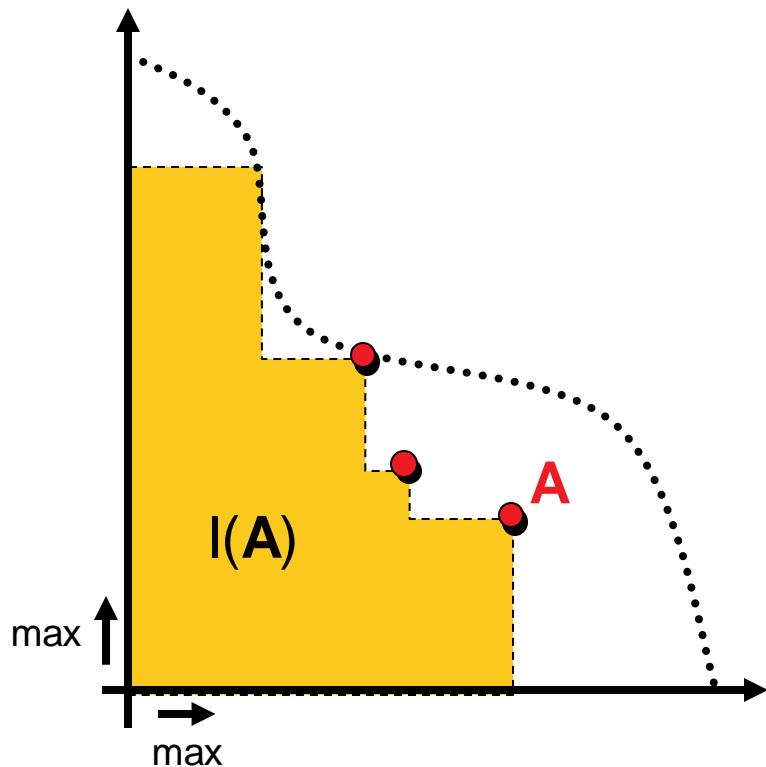
$$A \preceq B : \Leftrightarrow \forall_{y \in B} \exists_{x \in A} x \leq_{par} y$$



Examples of Quality Indicators

$$A \stackrel{\text{ref}}{\preccurlyeq} B : \Leftrightarrow I(A) \geq I(B)$$

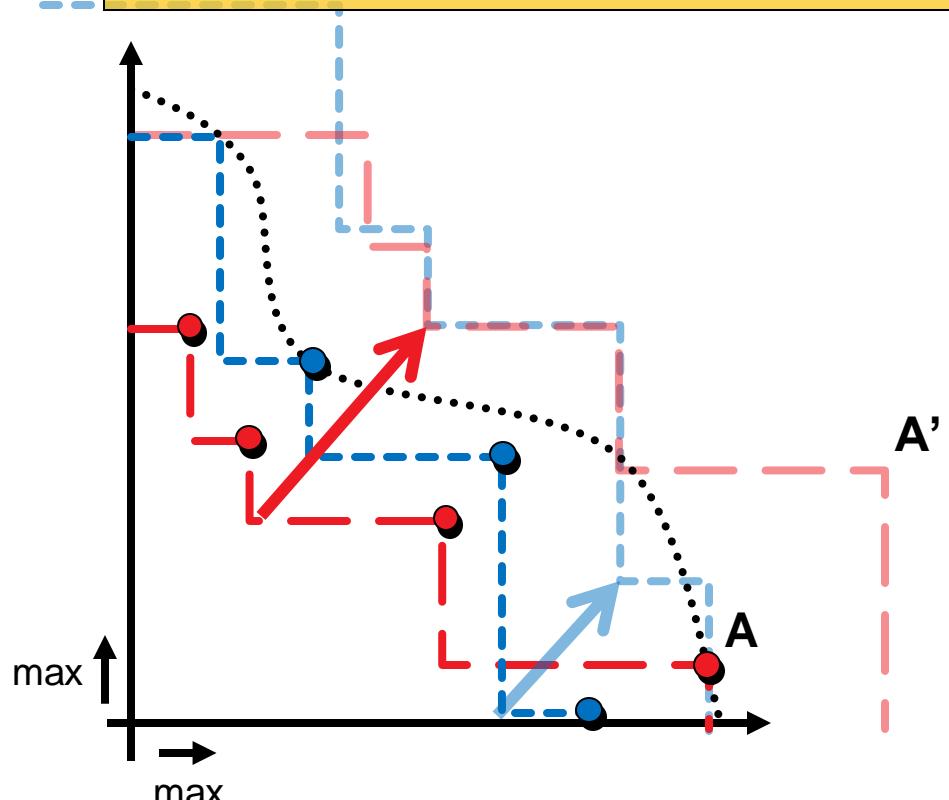
$I(A)$ = volume of the weakly dominated area in objective space



unary hypervolume indicator

$$A \stackrel{\text{ref}}{\preccurlyeq} B : \Leftrightarrow I(A,B) \leq I(B,A)$$

$I(A,B)$ = how much needs A to be moved to weakly dominate B

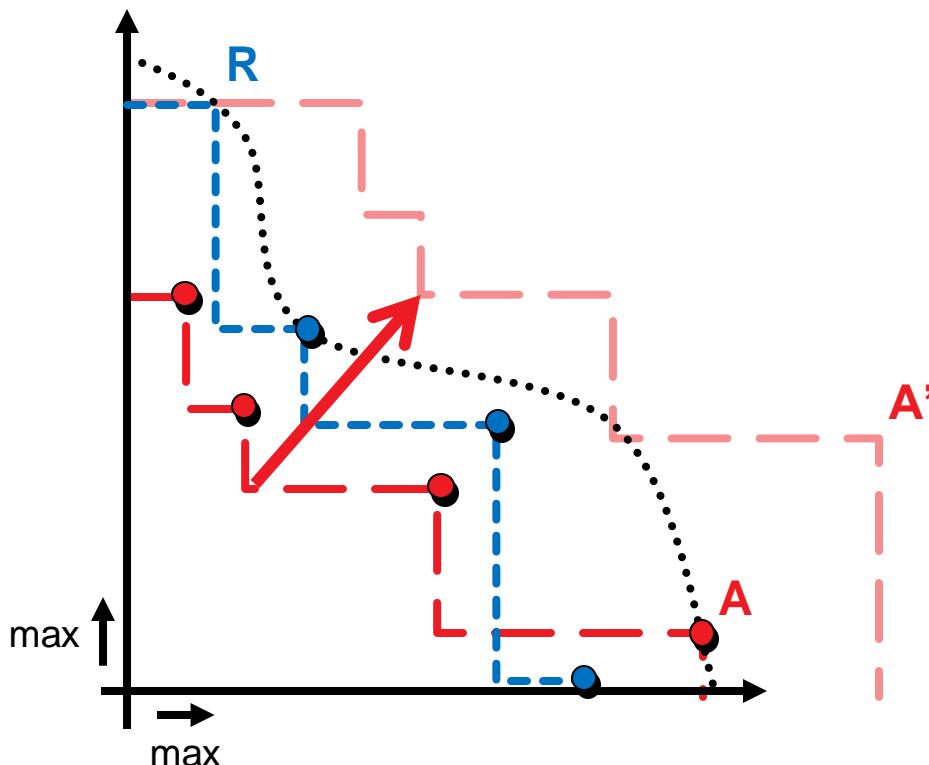


binary epsilon indicator

Examples of Quality Indicators II

$$A \stackrel{\text{ref}}{\preccurlyeq} B : \Leftrightarrow I(A, R) \leq I(B, R)$$

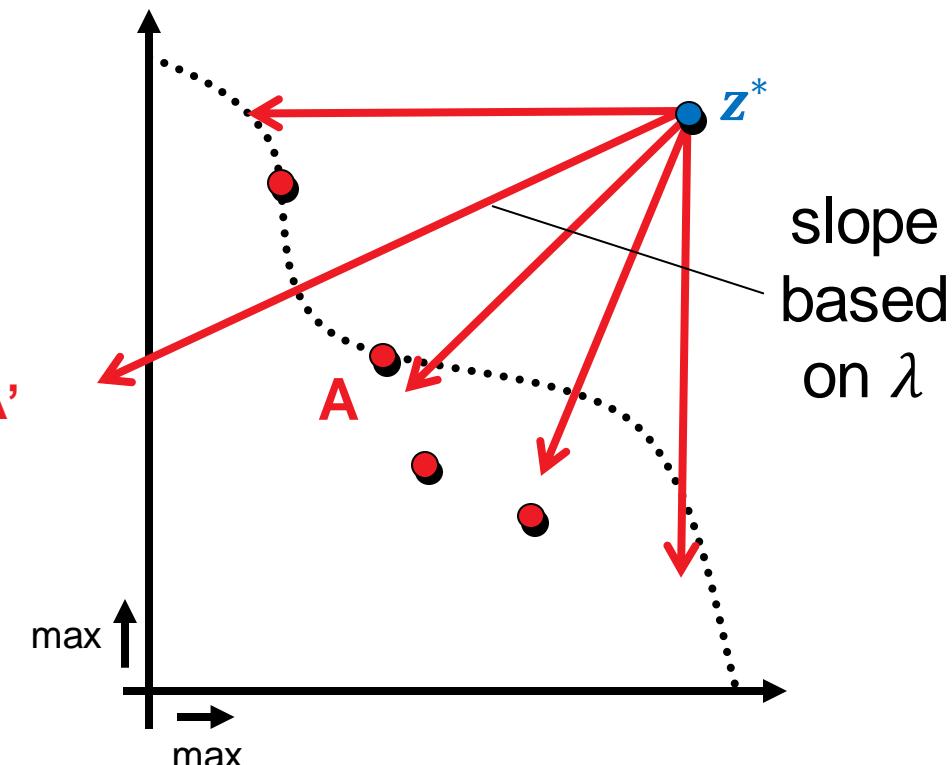
$I(A, R) =$ how much needs A to be moved to weakly dominate R



unary epsilon indicator

$$A \stackrel{\text{ref}}{\preccurlyeq} B : \Leftrightarrow I(A) \leq I(B)$$

$$I(A) = \frac{1}{|\Lambda|} \sum_{\lambda \in \Lambda} \min_{a \in A} \left(\max_{j=1..m} \lambda_j |z_j^* - a_j| \right)$$

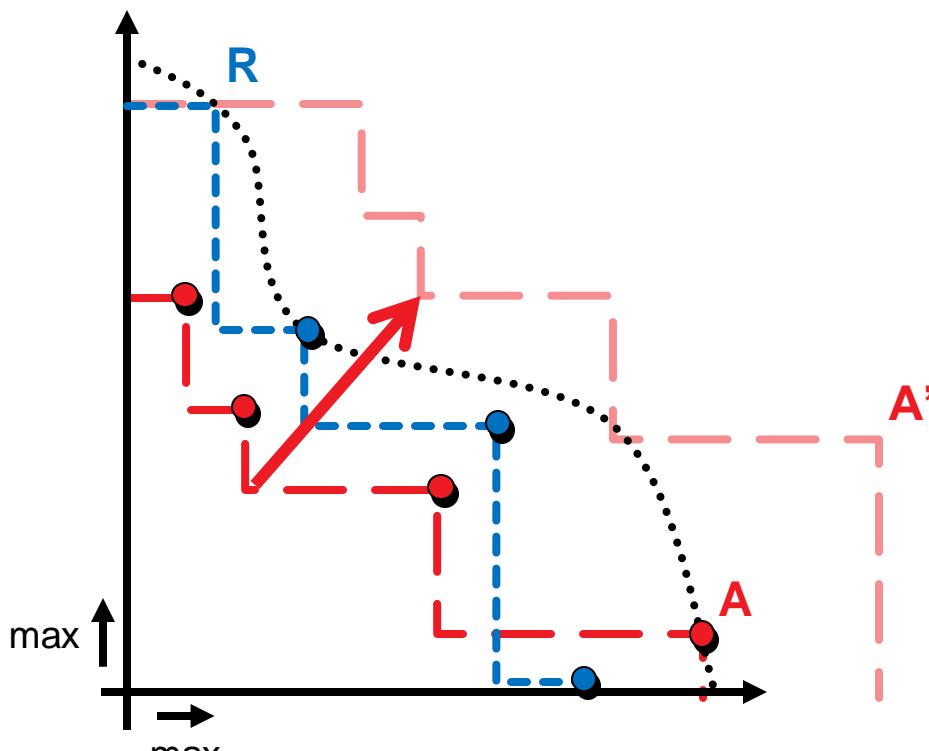


unary R2 indicator

Examples of Quality Indicators II

$$A \stackrel{\text{ref}}{\preccurlyeq} B : \Leftrightarrow I(A, R) \leq I(B, R)$$

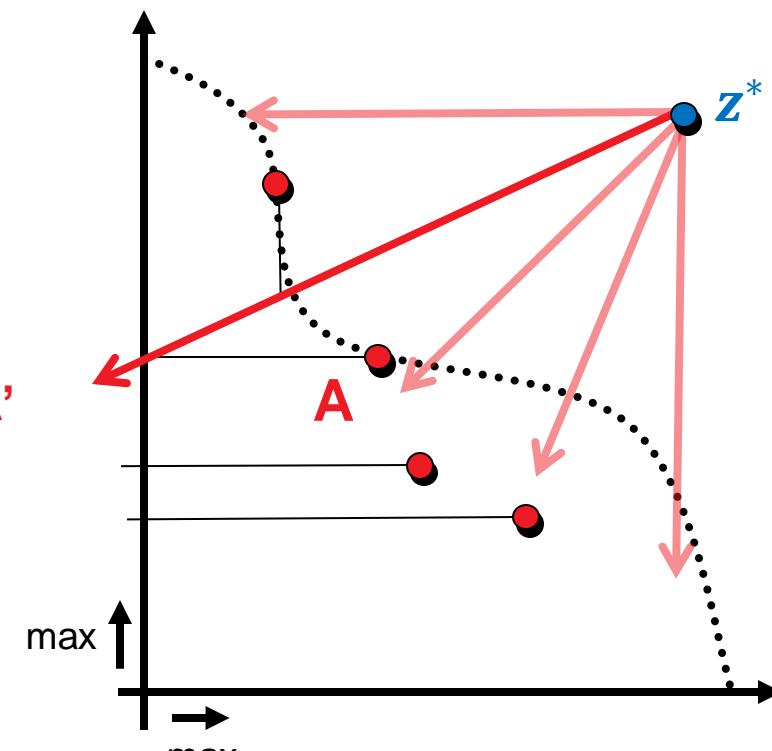
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unary epsilon indicator

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unary R2 indicator

bbob-biobj Testbed

- 55 functions by combining 2 b_{bbob} functions

1 Separable Functions	
f1	Sphere Function ✓
f2	Ellipsoidal Function ✓
f3	Rastrigin Function
f4	Büche-Rastrigin Function
f5	Linear Slope
2 Functions with low or moderate conditioning	
f6	Attractive Sector Function ✓
f7	Step Ellipsoidal Function
f8	Rosenbrock Function, original ✓
f9	Rosenbrock Function, rotated
3 Functions with high conditioning and unimodal	
f10	Ellipsoidal Function
f11	Discus Function
f12	Bent Cigar Function
f13	Sharp Ridge Function ✓
f14	Different Powers Function ✓
4 Multi-modal functions with adequate global structure	
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f17	Schaffers F7 Function ✓
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f23	Katsuura Function
f24	Lunacek bi-Rastrigin Function

bbob-biobj Testbed

- 55 functions by combining 2 bbof functions

bbob-biobj Testbed

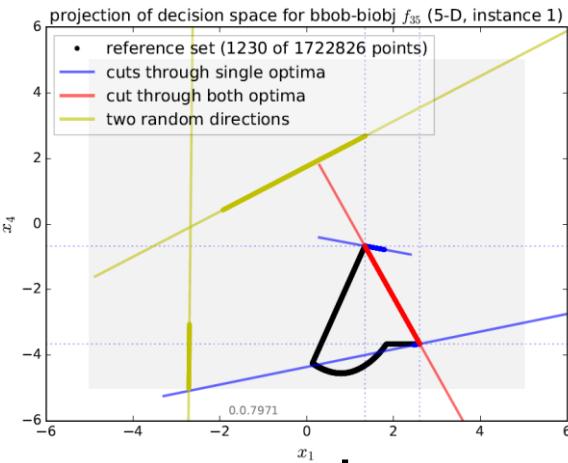
- 55 functions by combining 2 **bbob** functions
- 15 function groups with 3-4 functions each
 - separable – separable, separable – moderate, separable - ill-conditioned, ...
- 6 dimensions: 2, 3, 5, 10, 20, (40 optional)
- instances derived from **bbob** instances:
- no normalization (algo has to cope with different orders of magnitude)
- for performance assessment: ideal/nadir points known

bbob-biobj Testbed (cont'd)

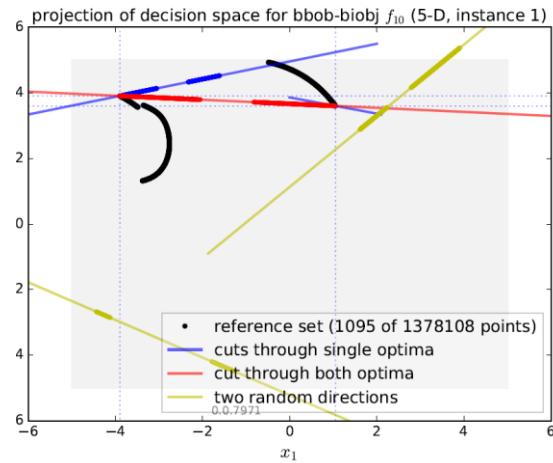
- Pareto set and Pareto front **unknown**
 - but we have a good idea of where they are by running quite some algorithms and keeping track of all non-dominated points found so far
- Various types of shapes

bbob-biobj Testbed (cont'd)

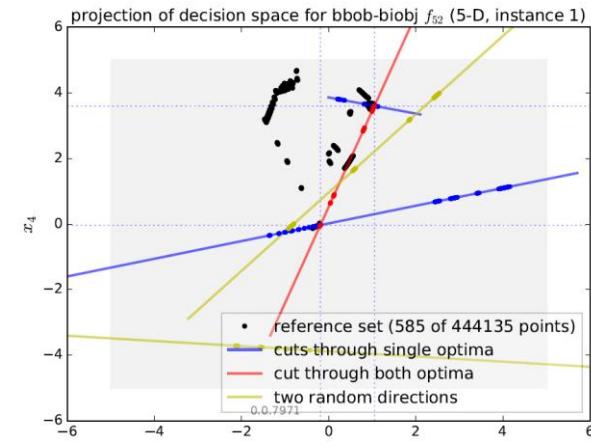
search space



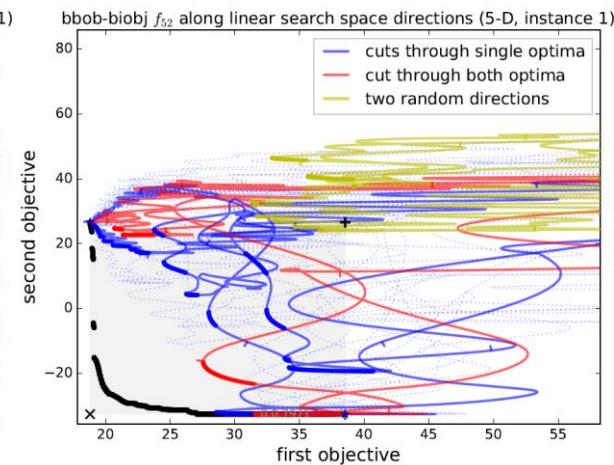
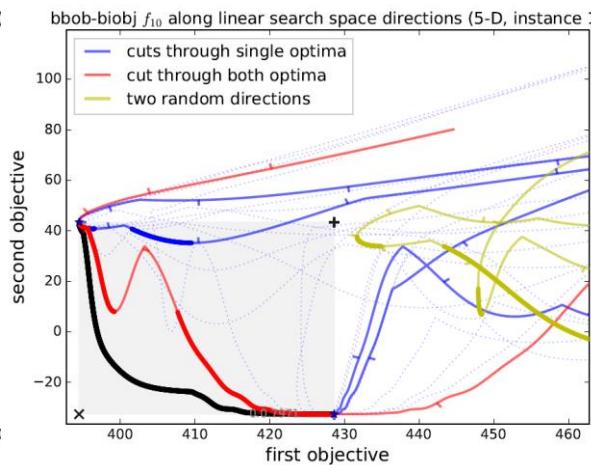
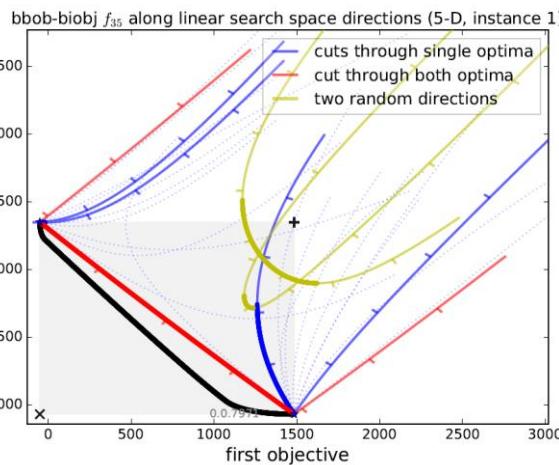
connected
uni-modal



disconnected
multi-modal



objective space



Bi-objective Performance Assessment

algorithm quality =

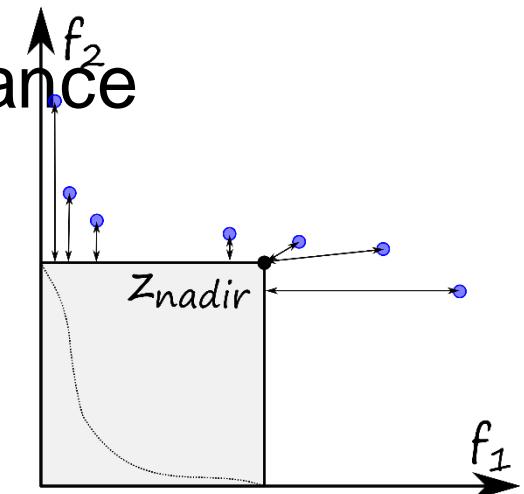
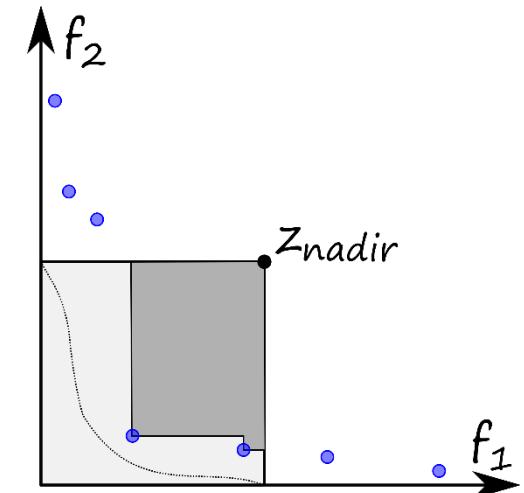
normalized* hypervolume (HV)
of all non-dominated solutions

if a point dominates nadir

closest normalized* negative distance
to region of interest $[0,1]^2$

if no point dominates nadir

* such that ideal=[0,0] and nadir=[1,1]



Bi-objective Performance Assessment

We measure runtimes to reach (HV indicator) targets:

- relative to a **reference set**, given as the best Pareto front approximation known (since exact Pareto set not known)
- actual **absolute hypervolume targets** used are

$$\text{HV}(\text{refset}) - \text{targetprecision}$$

with 58 **fixed** targetprecisions between +1 and -10^{-4} (same for all functions, dimensions, and instances) in the displays

Course Overview

1	Mon, 18.9.2017 Tue, 19.9.2017	first lecture groups defined via wiki everybody went (actively!) through the Getting Started part of github.com/numbbo/coco
2	Wed, 20.9.2017	❷ today's lecture "Benchmarking", ❶ final adjustments of groups everybody can run and postprocess the example experiment (❸ ~1h for final questions/help during the lecture)
3	Fri, 22.9.2017	lecture "Introduction to Continuous Optimization"
4	Fri, 29.9.2017	lecture "Gradient-Based Algorithms"
5	Fri, 6.10.2017	lecture "Stochastic Algorithms and DFO"
6	Fri, 13.10.2017	lecture "Discrete Optimization I: graphs, greedy algos, dyn. progr." deadline for submitting data sets
	Wed, 18.10.2017	deadline for paper submission
7	Fri, 20.10.2017	final lecture "Discrete Optimization II: dyn. progr., B&B, heuristics"
	Thu, 26.10.2017 / Fri, 27.10.2017	oral presentations (individual time slots)
	after 30.10.2017	vacation aka learning for the exams
	Fri, 10.11.2017	written exam

All deadlines:
23:59pm Paris time

Conclusions Benchmarking Continuous Optimizers

I hope it became clear...

...what are the **important issues** in algorithm benchmarking

...which **functionality** is behind the COCO platform

...and **how to measure performance** in particular

...what are the basics of **multiobjective optimization**

...and what are the next important steps to do:

read the assigned paper and **implement** the algorithm

document everything on the wiki

run COCO **experiment** with your algorithm and **share your data** until Friday 13th of October, 2017

And now...

...time for your questions and problems
around COCO