$$m_{\text{eff}} = \frac{4}{R}$$
  $\times 2$   $m_{\text{eff}} = \frac{3}{R}$   $\times 2$ 

 $m_{\rm eff} = \frac{1}{R}$ 

$$m_{\text{eff}} = \frac{2}{R}$$
  $\times 2$   $m_{\text{eff}} = \frac{2}{R}$   $\times 2$ 

on a  $S^1$ , is linear and every mode other than the massless is doubly degenerated (corresponding to eigenvalues  $\pm n$ .

The spectrum of a Kaluza-Klein reduction of a real massless scalar field