# Functional Programming

## Type definitions

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# Type aliases

Explaining the meaning of data in comments is bad!
Introduce new, self explaining types.

```
type Name = String
type Title = String
type Year = Int
type Age = Int

type User = (Name,    Year)
--           ^ name   ^ Year of birth
type Film = (Title, Age)
--                  ^ fsk
type Purchase = (Name, Title, Year) -- <---+
--              ^ user name ^ item name     ^ date of purchase
users :: [User]
```

# Datatypes

## Example scenario

- model a card game (hearts)
- represent the game items!
- define game logic on the representations!

# Intermezzo: The game

## Microsoft Hearts (Wikipedia link)

- computer game based on card game "Hearts"
- included in Windows 3.1 through Windows 7
- discontinued

# The game

## Gameplay

- Four players (three simulated)
- Trick-taking game
- Each player plays one card to a trick
- Trick won by highest card of the suit led; no Trump!
- Suit must be followed
- Heart cannot lead until
  - either Heart has been broken — a player played Heart
  - or the leading player has only Heart
- Points are scored by any Hearts (1 point) and the Queen of Spades (13 points)

# The game

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## Objective

- Avoid gaining points **or** gain all 26 points

# Data model for card games

- A card has a **Suit** and a **Rank**
- A card beats another card if it has the same suit, but higher rank
- Todo:
  - represent cards
  - define when one card beats another
  - define a function that chooses a beating card from a hand of cards, if possible

# Define new data types

## A card has a Suit

```
data Suit = Spades | Hearts | Diamonds | Clubs
```

## Explanation

- new type consisting of (exactly) four values
- `Suit`: the name of the new type
- `Spades`, `Hearts`, ...: the names of its **constructors**.
- Type and constructor names must be capitalized

# Printing new data types

```
Main> Spades

<interactive>:3:1:
  No instance for (Show Suit) arising from
  a use of ‘print’
  Possible fix: [...]
```

**Oops!**

- Haskell does not know how to print a `Suit`
- but we can ask for a default (or write our own printer)

# Printing derived

```
data Suit = Spades | Hearts | Diamonds | Clubs
  deriving (Show) -- makes 'Suit' printable
```

Defines a function `show` for `Suit`, which is automatically called by Haskell's printer

```
Main> Spades
Spades
Main> show Spades
"Spades"
Main> :t show
show :: Show a => a -> String
```

# Functions on data types

Each suit has a color:

```
data Color = Black | Red
  deriving (Show)
```

Define a color function by pattern matching

```
color :: Suit -> Color
color = undefined
```

# More data

A card has a suit and a **rank**:

```
data Rank = Numeric Integer | Jack | Queen
          | King | Ace
  deriving Show
```

The constructor `Numeric` is different: it takes an argument.

```
Main> :t Numeric
Numeric :: Integer -> Rank
```

# Comparing ranks

## Situation

- Let `r2` be the highest rank on the table
- Let `r1` be the card played
- Assuming the suits match, does `r1` get the trick?

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## Need an ordering of ranks

```
-- |rankBeats r1 r2
-- returns True, if r1 beats r2
-- i.e. r1 is strictly greater than r2
rankBeats :: Rank -> Rank -> Bool
rankBeats r1 r2 = undefined
```

# Ordering ranks by pattern matching

```
-- rankBeats r1 r2 returns True, if r1 beats r2
rankBeats :: Rank -> Rank -> Bool
rankBeats _  Ace     = False
rankBeats Ace _      = True
rankBeats _ King     = False
rankBeats King _     = True
rankBeats _  Queen   = False
rankBeats Queen _    = True
rankBeats _ Jack     = False
rankBeats Jack _     = True
rankBeats (Numeric n1) (Numeric n2) = n1 > n2
--          ^^ pattern match on constructor
--             yields its argument
```

# Letting Haskell order the ranks

- definition of `rankBeats` is repetitive
- boilerplate code
- let Haskell generate it for us!

## Deriving an order

<=, < etc are overloaded and can be extended to new types

```
data Rank = Numeric Integer | Jack | Queen
          | King | Ace
  deriving (Show, Ord)

rankBeats' r1 r2 = r1 > r2
```

# Oops...

```
M04Cards.hs:17:27: error:
    • No instance for (Eq Rank)
        arising from the 'deriving' clause of a data type decl
      Possible fix:
        use a standalone 'deriving instance' declaration,
          so you can specify the instance context yourself
    • When deriving the instance for (Ord Rank)
```

# Oops...

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M04Cards.hs:17:27: error:
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```

## Explanation

`Ord` defines < and then

```
x <= y = x < y || x == y
```

but how do we compare two ranks for equality?

# Equality of ranks

- could be defined by pattern matching, but
- boilerplate code
- let Haskell generate it for us!

## Deriving equality

==, /= are overloaded and can be extended to new types

```
data Rank = Numeric Integer | Jack | Queen
          | King | Ace
  deriving (Show, Eq, Ord)

rankBeats' r1 r2 = r1 > r2
```

# Equality of ranks

- could be defined by pattern matching, but
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==, /= are overloaded and can be extended to new types

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rankBeats' r1 r2 = r1 > r2
```

## Are they the same?

How do we know that `rankBeats` = `rankBeats'`? Let's defer that.

# Cards, finally

A card has a `Suit` and a `Rank`

```
data Card = Card Rank Suit
  deriving (Show)

rank :: Card -> Rank
rank (Card r s) = r

suit :: Card -> Suit
suit (Card r s) = s
```

- single constructor with two parameters
- (in principle, a tuple with a special name)
- `rank`, `suit` are **selector functions**

# Comparing Cards

A card **beats** another card, if it has the same suit, but a higher rank

```
cardBeats :: Card -> Card -> Bool
cardBeats givenCard c = suit givenCard == suit c
                        && rankBeats (rank givenCard)
                                     (rank c)
```

# Hand of Cards

```
type Hand = [Card]

chooseCard :: Card -> Hand -> Card
chooseCard givenCard h = undefined
```

To develop `chooseCard` refine `h` by pattern matching

# Choose a card

```
type Hand = [Card]

chooseCard :: Card -> Hand -> Card
chooseCard givenCard [] = undefined -- ???
chooseCard givenCard (x:xs) = undefined
```

- What should we do if the hand is empty?
- Avoid by defining only non-empty hands!

# Non-empty hands

```
data Hand = Last Card | Next Card Hand
  deriving (Show, Eq)
```

- Recursive datatype definition
- `Last Card` is the **base case**

# Get card from non-empty hand

- A `Hand` is never empty
- Thus we can always obtain a card

```
topCard :: Hand -> Card
topCard (Last c)  = c
topCard (Next c _) = c
```

# Choosing from non-empty hand

```
-- choose a beating card, if possible
chooseCard :: Card -> Hand -> Card
chooseCard = undefined
```

# Choosing from non-empty hand

```
-- choose a beating card, if possible
chooseCard :: Card -> Hand -> Card
chooseCard gc (Last c) = c -- may beat, or not
chooseCard gc (Next c h) | cardBeats gc c = c
                         | otherwise      = chooseCard gc h
```

# Break Time — Questions?