Functional Programming Type definitions

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Type aliases

Explaining the meaning of data in comments is bad! Introduce new, self explaining types.

```
type Name = String
type Title = String
type Year = Int
type Age = Int
type User = (Name, Year)
         type Film = (Title, Age)
              ^ fsk
type Purchase = (Name, Title, Year) -- <---+
           users :: [User]
```

Datatypes

Example scenario

- model a card game (hearts)
- represent the game items!
- define game logic on the representations!

Intermezzo: The game

Microsoft Hearts (Wikipedia link)

- computer game based on card game "Hearts"
- included in Windows 3.1 through Windows 7
- discontinued

The game

Gameplay

- Four players (three simulated)
- Trick-taking game
- Each player plays one card to a trick
- Trick won by highest card of the suit led; no trump
- Suit must be followed
- Heart cannot lead until
 - either Heart has been broken a player played Heart
 - or the leading player has only Heart
- Points are scored by any Hearts (1 point) and the Queen of Spades (13 points)

The game

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Objective

Avoid gaining points or gain all 26 points

Data model for card games

- A card has a Suit and a Rank
- A card beats another card if it has the same suit, but higher rank
- Todo:
 - represent cards
 - define when one card beats another
 - define a function that chooses a beating card from a hand of cards, if possible

Define new data types

A card has a Suit

data Suit = Spades | Hearts | Diamonds | Clubs

Explanation

- new type consisting of (exactly) four values
- Suit: the name of the new type
- Spades, Hearts, ...: the names of its constructors.
- Type and constructor names must be capitalized

Printing new data types

```
Main> Spades

<interactive>:3:1:
  No instance for (Show Suit) arising from a use of 'print'
  Possible fix: [...]
```

Oops!

- Haskell does not know how to print a Suit
- but we can ask for a default (or write our own printer)

Printing derived

```
data Suit = Spades | Hearts | Diamonds | Clubs
  deriving (Show) -- makes 'Suit' printable
```

Defines a function show for Suit, which is automatically called by Haskell's printer

```
Main> Spades
Spades
Main> show Spades
"Spades"
Main> :t show
show :: Show a => a -> String
```

Functions on data types

```
Each suit has a color:
```

```
data Color = Black | Red
deriving (Show)
```

Define a color function by pattern matching

```
color :: Suit -> Color
color = undefined
```

More data

A card has a suit and a rank:

The constructor Numeric is different: it takes an argument.

```
Main> :t Numeric
```

Numeric :: Integer -> Rank

Comparing ranks

```
-- |rankBeats r1 r2
-- returns True, if r1 beats r2
rankBeats :: Rank -> Rank -> Bool
rankBeats r1 r2 = undefined
```

To continue, we need an ordering on ranks

Ordering ranks by pattern matching

```
-- rankBeats r1 r2 returns True, if r1 beats r2
rankBeats :: Rank -> Rank -> Bool
rankBeats Ace = False
rankBeats Ace _ = True
rankBeats _ King = False
rankBeats King _ = True
rankBeats _ Queen = False
rankBeats Queen _ = True
rankBeats _ Jack = False
rankBeats Jack _ = True
rankBeats (Numeric n1) (Numeric n2) = n1 > n2
           ^ pattern match on constructor
              yields its argument
```

Cards, finally

A card has a Suit and a Rank

data Card = Card Rank Suit
 deriving (Show)

rank :: Card -> Rank
rank (Card r s) = r

suit :: Card -> Suit
suit (Card r s) = s

- single constructor with two parameters
- (in principle, a tuple with a special name)
- rank, suit are selector functions

Comparing Cards

A card beats another card, if it has the same suit, but a higher rank

Hand of Cards

```
type Hand = [Card]
```

```
chooseCard :: Card -> Hand -> Card
chooseCard givenCard h = undefined
```

To develop chooseCard refine h by pattern matching

Choose a card

```
type Hand = [Card]
```

```
chooseCard :: Card -> Hand -> Card
chooseCard givenCard [] = undefined -- ???
chooseCard givenCard (x:xs) = undefined
```

- What should we do if the hand is empty?
- Avoid by defining only non-empty hands!

Non-empty hands

```
data Hand = Last Card | Next Card Hand
  deriving (Show, Eq)
```

- Recursive datatype definition
- Last Card is the base case

Get card from non-empty hand

- A Hand is never empty
- Thus we can always obtain a card

```
topCard :: Hand -> Card
topCard (Last c) = c
topCard (Next c _) = c
```

Choosing from non-empty hand

```
-- choose a beating card, if possible
chooseCard :: Card -> Hand -> Card
chooseCard = undefined
```

Choosing from non-empty hand

Break Time — Questions?

