# Functional Programming Functions

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## Function definition by cases

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Find the absolute value of a number

- if x is positive, result is x
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#### **Definition**

```
-- returns the absolute value of x
absolute :: Integer -> Integer
absolute x | x >= 0 = x
absolute x | x < 0 = - x
```

## Alternative styles of definition

## One equation

## Using if-then-else in an expression

absolute', x = if x >= 0 then x else -x

#### Recursion

Standard approach to define functions in functional languages (no loops!)

- Reduce a problem (e.g., power x n) to a smaller problem of the same kind
- Eventually reach a "smallest" base case
- Solve base case separately
- Build up solutions from smaller solutions

## Example: power

Compute x^n without using the built-in operator

```
-- compute x to n-th power

power x 0 = 1

power x n | n > 0 = x * power x (n - 1)
```

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- Combine the above to I(n) = I(n-1) + n 1

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## Counting intersections

```
-- max number of intersections of n lines intersect :: Integer -> Integer intersect 0 = 0 intersect n | n > 0 = intersect (n - 1) + n - 1
```

## Questions?

