

# KGC: Knowledge Graph Embedding

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**Keywords:** KRL, multi-relation learning and statistical relational learning;

# Task

定义：将知识图谱中实体/关系的语义嵌入到低维向量空间;

关联：通过学习的向量表达使得图谱补全中链接预测的判别过程可计算;

任务分解: Representation Space + Scoring Function + Encoding Models + Auxiliary Information;

目的：在三元组构成的图谱( $h \in \mathbf{E}, t \in \mathbf{R}, r \in \mathbf{E}$ )中构建一个打分，使得真实存在的三元组分数比认为构造假的高

# Simple Linear Model

TransE

$$- \|h + r - t\|$$

TransX (TranH, TranR, TransD)

$$- \|g_{r,1}(h) + r - g_{r,2}(t)\|$$

DistMult

$$\langle h, r, t \rangle$$

Complex

$$\text{Re}(\langle h, r, \bar{t} \rangle)$$

# Relation

- Symmetry / Antisymmetry (对称)

$$(h, r, t) \in G, (t, r, h) \in G$$

e.g. (A, get\_married\_with, B), (B, get\_married\_with, A)

- Inversion (可逆)

$$(h, r, t) \in G, (t, r^{-1}, h) \in G$$

e.g. (A, is\_son\_of, B), (B, is\_father\_of, A)

- Composition (组合)

$$(h, r_1, t_1), (h_n, r_n, t) \rightarrow (h, r, t)$$

e.g. (A, is\_the\_mother\_of, B), (B, is\_son\_of, C)  $\rightarrow$  (A, is\_the\_wife\_of, B)

# With Score Fuction

- Symmetry / Antisymetry (对称)

$$f_r(h, t) = f_r(t, h)$$

$$f_r(h, t) \neq f_r(t, h)$$

- Inversion (可逆)

$$f_r(h, t) = f_{r^{-1}}(t, h)$$

- Composition (组合)

$$f_{r_1}(h, z) \cap f_{r_2}(z, t) \Rightarrow f_r(h, t)$$

# Analysis-TransE

$$\begin{aligned} f_r(h, t) &= -\|h + r - t\| \\ &= -(\|h\|_2^2 + \|r\|_2^2 + \|t\|_2^2 - 2(h^T t + r^T (t - h))) \\ &\Rightarrow h^T t + r^T (t - h) \end{aligned}$$

- 推得： $-r = r$ 。当且仅当 $r=0$ 时，满足对称关系约束，因此TransE并不能有区分地建模任一对称关系；其他关系都能够建模。
- 推得： $-r_1 = r_2$ 。能够满足可逆关系
- 推得： $h + (r_1 + r_2) = t$ 。能够满足组合关系

# Analysis-DistMult

$$f_r(h, t) = h^T M_r t$$

- 明显的, 总存在  $h^T M_r t = t^T M_r h$ 。因此表示对称关系, 无法描述非对称关系和可逆关系。
- 往往会将  $h, t$  限制为标准向量, 则有  $h^T M_r t \approx 1 \Rightarrow h^T M_r \approx t^T$ , 因此有  $h^T M_{r_1} \approx z^T, z^T M_{r_2} \approx t^T \Rightarrow h^T M_{r_1} M_{r_2} \approx t^T$ , 能够描述组合关系。

# Analysis

Method	Score Function	Symmetry	Anti-	Inversion	Composition
TransE	$-\ h + r - t\ $	X	O	O	O
TransX	$-\ g_{r,1}(h) + r - g_{r,2}(t)\ $	O	O	X	X
DistMult	$\langle h, r, t \rangle$	O	X	X	<i>O</i>
ComplEx	$Re(\langle h, r, \bar{t} \rangle)$	O	O	O	X

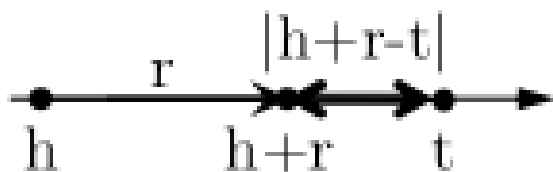


# RotatE

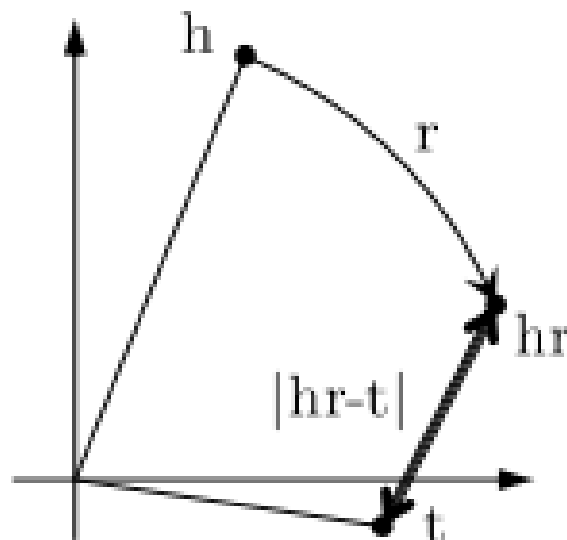
$$t = h \circ r, \text{ where } |r_i| = 1,$$

- $r$  是对称关系时, 当且仅当  $r$  的每一个分量  $r_i$  满足:  $r_i = e^{0/i\pi} = \pm 1$  ;
- 两个关系  $r_1$  和  $r_2$  是逆关系时, 当且仅当他们的嵌入是共轭向量:  $r_2 = \bar{r}_1$  ;
- 某个关系  $r_3 = e^{i\theta_3}$  是其他两个关系  $r_1 = e^{i\theta_1}$  和  $r_2 = e^{i\theta_2}$  的组合时, 当且仅当  $r_3 = r_1 \circ r_2$  (即,  $\theta_3 = \theta_1 + \theta_2$  ).

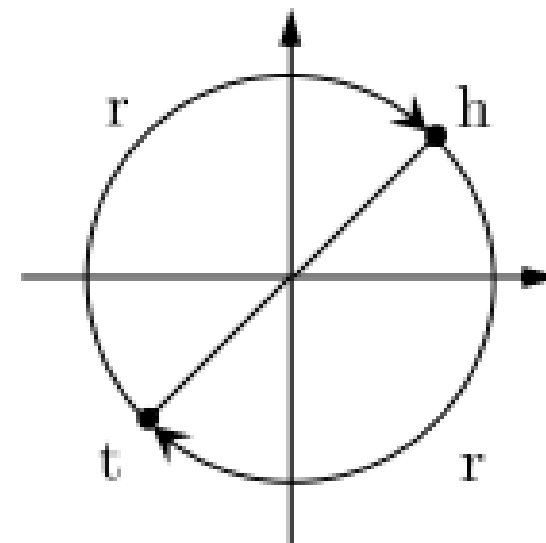
# Visualization



(a) TransE models  $r$  as translation in real line.



(b) RotatE models  $r$  as rotation in complex plane.



(c) RotatE: an example of modeling symmetric relations  $r$  with  $r_i = -1$

Figure 1: Illustrations of TransE and RotatE with only 1 dimension of embedding.

# Tucker

$$W \times_1 h \times_2 r \times_3 h$$

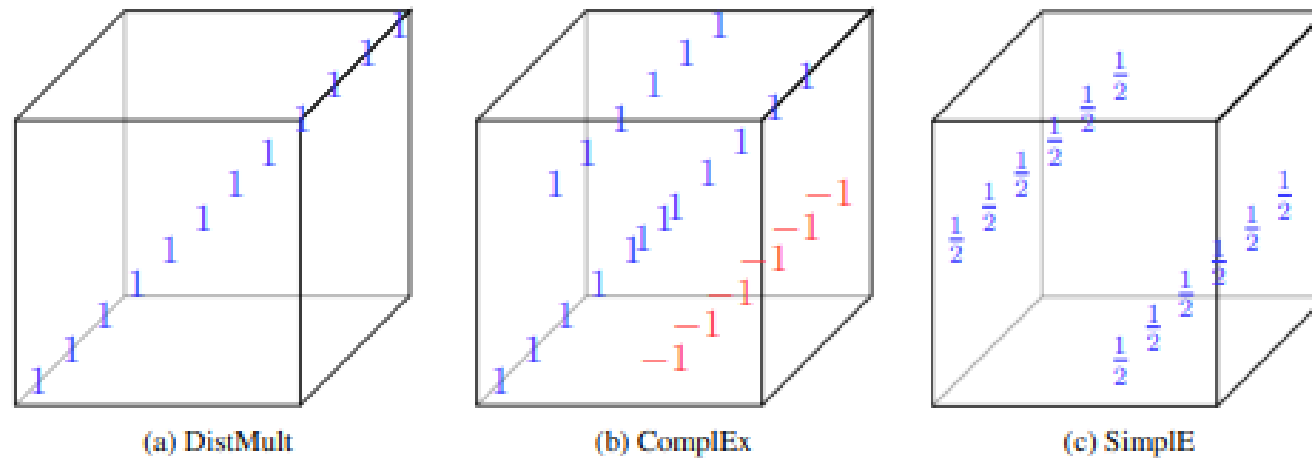


Figure 2: Constraints imposed on the values of core tensor  $Z \in \mathbb{R}^{d_e \times d_e \times d_e}$  for DistMult and  $Z \in \mathbb{R}^{2d_e \times 2d_e \times 2d_e}$  for ComplEx and Simple. Elements that are set to 0 are represented in white.

# NN-Based Method

ConvE

$$f(\text{vec}(f([h; r] * w))W)t$$

ConvKB

$$\text{cat}(f([h; r; t] * w))W$$

SACN

$$f(\text{vec}(M(h, t))W)t$$

HypER

$$f(\text{vec}(h * \text{vec}^{-1}(rH))W)t$$

其中,  $*$ 为卷积操作,  $\text{vec}(\cdot)$ 为reshape为向量,  $[;;]$ 为向量拼接

# Inference

	WN18RR					FB15k-237				
	MR	MRR	H@10	H@3	H@1	MR	MRR	H@10	H@3	H@1
<b>TransE</b>	3384	.226	.501			357	.294	.465		
DistMult	5110	.430	.490	.440	.390	254	.241	.419	.263	.155
ComplEx	5261	.440	.510	.460	.410	339	.247	.428	.275	.158
RotatE	—	—	—	—	—	<b>185</b>	.297	.480	.328	.205
<b>TuckER</b>		.470	.526	.482	.443		.358	.544	.394	.266
ConvE	<b>4187</b>	.430	.520	.440	.400	244	.325	.501	.356	.237
HypER	5798	<b>.465</b>	<b>.522</b>	<b>.477</b>	<b>.436</b>	250	<b>.341</b>	<b>.520</b>	<b>.376</b>	<b>.252</b>

# Others

## A. '1v1' versus '1vN'

- Faster Inference
- FROM Ranking-based loss TO Multi-Label Classification

## B. Unified Strategy