## Computational Intelligence Master in Artificial Intelligence 2021-22

#### **Evolutionary Computation**

Genetic Algorithms - Complementary Slides





# Selection methods: implementation details - I

#### Roulette wheel

- $p_i = rac{f_i}{\sum\limits_{j=1}^{\mu} f_j}$  is the probability of selecting individual i, with fitness  $f_i$ .
- $w_i = \sum\limits_{j=1}^i p_j \in [0,1]$ , for  $i=1,..,\mu$ , points to the end of the i-th sector.

Let r be a random number in [0,1), the position of the roulette pointer.

Then, the selected individual s is given by  $s = \min\{i : w_i > r\}$ 

### Stochastic universal sampling

Let r be a random number in  $[0,1/\mu)$ , and define, for  $k=1,..,\mu$ ,  $r_k=r+(k-1)/\mu$  as  $\mu$  equally spaced roulette pointers.

Then,  $\mu$  selected individuals are  $s_k = \min\{i : w_i > r_k\}$ , for  $k = 1, ..., \mu$ .

## Selection methods: implementation details - II

### Remainder stochastic sampling

- $a_i = \frac{f_i}{(\sum\limits_{i=1}^{\mu} f_i)/\mu} = \frac{\mu f_i}{\sum\limits_{i=1}^{\mu} f_i}$  is the ratio of individual i over average fitness.
- $a_i=c_i+r_i$ , where  $c_i=\lfloor a_i \rfloor$  and  $r_i=a_i-c_i$  (integer part and remainder). Note that  $\sum_{i=1}^{\mu}a_i=\mu$ , but  $\sum_{i=1}^{\mu}c_i\leq \mu$ .

Then, first select  $c_i$  copies of each individual i, and the rest  $\mu - \sum_{i=1}^{\mu} c_i$  are selected by standard roulette wheel using  $p_i = \frac{r_i}{\sum\limits_{i=1}^{\mu} r_i}$  as probability.

#### Rank selection

Let  $r_i \in \{1,..,\mu\}$  be the rank of individual i, where  $r_i = 1$  means the best. Define probability  $p_i = \frac{(\mu + 1 - r_i)}{\mu(\mu + 1)/2}$  and apply standard roulette wheel.

## Real-number representation in bits

### Before applying Gray coding:

We want to represent a real number r within the range [a,b] using n bits, thus determining the attainable precision.

Let i be an integer with such n-length bit representation.

Then  $q(i) = \frac{i}{2^n - 1}$  is a real-value between 0 and 1.

And r = a + q(i)(b - a) is a real-value between a and b, as desired, associated with integer i.

### The Schema Theorem

#### The Schema Theorem

Let  $n_s$  be the number of individuals represented by schema s in a population of size  $\mu$ ,

and let  $f(s) = \frac{\sum\limits_{j \in s} f_j}{n_s}$  be their average fitness.

 $a_s = \frac{f(s)}{(\sum\limits_{i=1}^{\mu} f_i)/\mu} = \sum\limits_{i=1}^{\mu f(s)} f_i$  is the ratio of schema s over average fitness.

For consecutive generations g, (g+1), ..., (g+m) of the population,

**if** schema s is short and low-order then  $n_s^{g+m} \approx n_s^g \prod_{g'=g}^{g+m-1} a_s^{g'}$ .