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## Backstory

Zenda and Reece have determined Doc Trine's cell number in hyperjail. Searching through Trine's notebooks, they find another note, explaining how the hypercube is patrolled by a fearsome quantum warden, which is able to place itself in a superposition and inspect multiple cells at once. To avoid detection and rescue Doc Trine, they need to build a quantum radar!

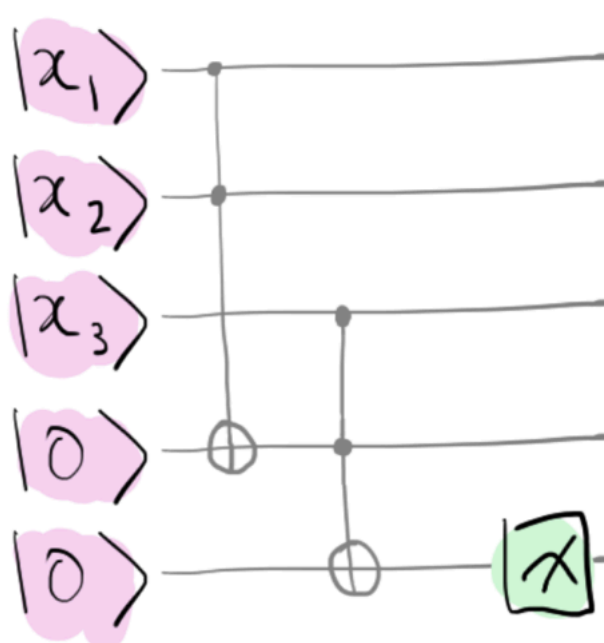
## A quantum radar

The quantum guard can place itself in a superposition

$$|\text{guard}\rangle = \sum_x g_x |x\rangle,$$

where  $x \in \{0, 1\}^5$  ranges over all cell numbers, and  $g_x$  are complex-valued amplitudes. Seen in this way,  $|g_x|^2$  is the probability that the guard is at position  $|x\rangle$ . They know that Doc Trine is located in a cell  $c = (1, 1, 0, 0, 1)$ . Ideally, they would like to wait until the guard's attention, captured by the probability  $|g_c|^2$ , is sufficiently low.

In this challenge, we will look for a way to be able to measure  $|g_c|^2$ . Unfortunately, there isn't much equipment in the office, and what is there is noisy! But Trine has left a collection of "Toffoli cascades" lying around, circuits made from a string of noisy Toffoli gates. Here is an example for three input qubits  $|x_1\rangle|x_2\rangle|x_3\rangle$ :



Measuring the last qubit in the computational basis gives  $|x_1 \cdot x_2 \cdot x_3\rangle$  with probability 1, where  $x_1 \cdot x_2 \cdot x_3$  indicates the *product* of classical bits  $x_1$ ,  $x_2$ , and  $x_3$ . There is a Toffoli cascade acting on 5 input qubits (and with four auxiliary qubits) that Zenda and Reece can use, as well as some Pauli  $X$  gates. All are subject to *depolarizing noise*, such that after each gate, the state on each qubit is replaced with something random with probability  $\lambda$ .

Your task: use noisy Toffoli cascades and noisy-Pauli X gates to build a *quantum radar*, which outputs  $|g_c|^2$ , the guard's attention on Trine's cell. The guard state will be an input, along with four auxiliary qubits starting in the  $|0\rangle$  state.

### Challenge code

In the code below, you are given various functions:

- `noisy_PauliX`: which applies the Pauli-X gate and then a layer of depolarizing noise with parameter `lmbda`. (The noise is added for you.)
- `Toffoli_cascade`: a cascade of noisy Toffoli gates (noise parameter `lmbda`) which help compute a product, as in the circuit pictured above, with the input qubits on `in_wires` and auxiliary system `aux_wires`. (The noise is added for you.)
- `cascadar`: which takes a `guard_state` (`numpy.tensor`) and returns  $|g_c|^2$ , using noisy equipment with parameter `lmbda`. **You must complete this function**

## Inputs

The noisy quantum radar `cascaadar` takes as input the guard state `guard_state` (`numpy.tensor`), and a noise parameter `lmbda` (`float`) controlling the depolarizing noise.

## Output

Your `cascadar` function should give the correct probability  $|q_c|^2$  for test cases, including the effects of noise.

If your solution matches the correct one within the given tolerance specified in `check` (in this case it's a `1e-4` relative error tolerance), the output will be "Correct!" Otherwise, you will receive a "Wrong answer" prompt.

 Help

```

1 import json
2 import pennylane as qml
3 import pennylane.numpy as np


4 def noisy_PauliX(wire, lmbda):
5     """A Pauli-X gate followed by depolarizing noise.
6
7     Args:
8         lmbda (float): The parameter defining the depolarizing channel.
9         wire (int): The wire the depolarizing channel acts on.
10
11     """
12     qml.PauliX(wire)
13     qml.DepolarizingChannel(lmbda, wires=wire)
14
15 def Toffoli_cascade(in_wires, aux_wires, lmbda):
16     """A cascade of noisy Toffolis to help compute the product.
17
18     Args:
19         in_wires (list(int)): The input qubits.
20         aux_wires (list(int)): The auxiliary qubits.
21         lmbda (float): The probability of erasing the state of a qubit.
22
23     """
24     n = len(in_wires)
25     qml.Toffoli(wires=[in_wires[0], in_wires[1], aux_wires[0]])
26     qml.DepolarizingChannel(lmbda, wires=in_wires[0])
27     qml.DepolarizingChannel(lmbda, wires=in_wires[1])
28     qml.DepolarizingChannel(lmbda, wires=aux_wires[0])
29     for i in range(n - 2):
30         qml.Toffoli(wires=[in_wires[i + 2], aux_wires[i], aux_wires[i + 1]])
31         qml.DepolarizingChannel(lmbda, wires=in_wires[i + 2])
32         qml.DepolarizingChannel(lmbda, wires=aux_wires[i])
33         qml.DepolarizingChannel(lmbda, wires=aux_wires[i + 1])
34
35 # Build a quantum radar to check how much attention is on Trine's cell
36 def cascadar(guard_state, lmbda):
37     """Return the squared amplitude |g_c|^2 of the guard state, for c = (1, 1, 0, 0, 1).
38
39     Args:
40         guard_state (numpy.tensor): A 2**5 = 32 component vector encoding the guard state.
41         lmbda (float): The probability of erasing the state of a qubit.
42
43     """
44
45
46
47
48
49
50
51
52
53
54
55 # Put your code here #
56
57 return
58
59 output = circuit()
60
61 # if you want to post-process the output, put code here also #
62
63 return
64
65
66
67 # These functions are responsible for testing the solution.
68 def run(test_case_input: str) -> str:
69
70     guard_state, lmbda = json.loads(test_case_input)
71     output = cascadar(guard_state, lmbda)
72
73
74     return str(output)
75
76 def check(solution_output: str, expected_output: str) -> None:
77
78     solution_output = json.loads(solution_output)
79     expected_output = json.loads(expected_output)
80     assert np.allclose(
81         solution_output, expected_output, rtol=1e-4
82     ), "Your quantum radar isn't quite working properly!"
83
84
85 test_cases = [[["[0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0]"], [0.0]]]
86
87
88 for i, (input_, expected_output) in enumerate(test_cases):
89     print(f"Running test case {i} with input '{input_}'...")
90
91     try:
92         output = run(input_)
93
94     except Exception as exc:
95         print(f"Runtime Error. {exc}")
96
97     else:
98         if message := check(output, expected_output):
99             print(f"Wrong Answer. Have: '{output}'. Want: '{expected_output}'.")
100
101         else:
102             print("Correct!")

```