

Computeranimation

Lesson 3 – Collision





Introduction

Primitive Test
Bounding Volumes
Collision Response
Application





Motivation

Topics

- Rigid Transformation
- Animation
- Collision
- Dynamic
- Mass-Spring Simulation
- Rigging and Skeletal Animation
- Motion Capturing using RGB-D Sensor





Introduction

Collision Basics

- Collision Handling in general is divided into two phases
- 1. Collision-Detection: Determine Locations where collisions occur
- **2. Collision-Response**: Resolve colliding actors

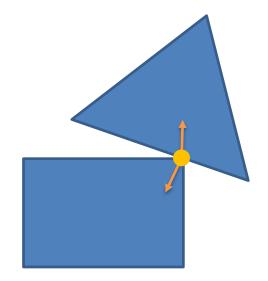






- In this phase all data for a proper collision handling is determined
- The collision state consists of:

- Contact Position(s)
- Contact Normal(s)





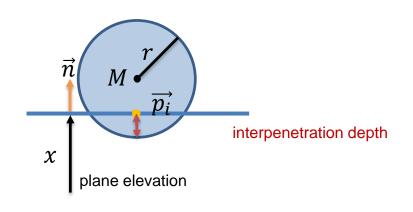


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Sphere-Plane Intersection



intersection point

$$\overrightarrow{p_i} = M - (r - x)\overrightarrow{p}$$

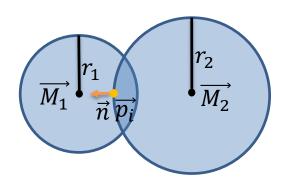
intersection normal

 \vec{n}





Sphere-Sphere Intersection



intersection point

$$\overrightarrow{p_i} = M_2 + r_2 \cdot (\overrightarrow{M_1} - \overrightarrow{M_2})$$

intersection normal

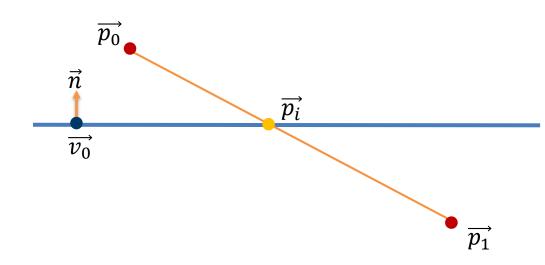
$$\vec{n} = \frac{\overrightarrow{M_1} - \overrightarrow{M_2}}{\left\| \overrightarrow{M_1} - \overrightarrow{M_2} \right\|}$$





Segment-Plane intersection

- important for many intersection tests including triangle meshes
- also important for raytracing



intersection point

$$\overrightarrow{p_i} = \overrightarrow{p_o} + \boldsymbol{r} \cdot (\overrightarrow{p_1} - \overrightarrow{p_0})$$

$$r = rac{\overrightarrow{n} \cdot (\overrightarrow{v_0} - \overrightarrow{p_0})}{\overrightarrow{n} \cdot (\overrightarrow{p_1} - \overrightarrow{p_0})}$$

If denominator equals zero, segment is parallel to plane





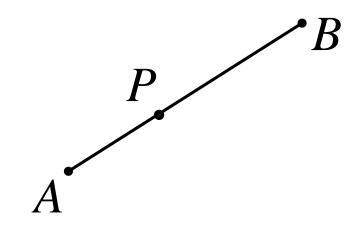
Barycentric Coordinates

- Used to define a point within a segment/triangle

1D Segment:

$$P = (1-t)A + tB \quad t \in [0,1]$$
$$= \alpha A + \beta B$$

condition:
$$\alpha + \beta = 1$$







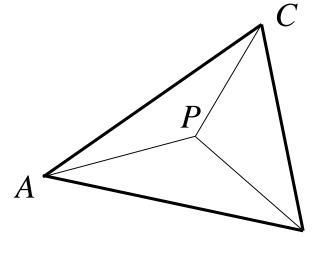
Barycentric Coordinates

- Used to define a point within a segment/triangle

2D Segment:

$$P = \alpha A + \beta B + \gamma C$$

condition: $\alpha + \beta + \gamma = 1$



R





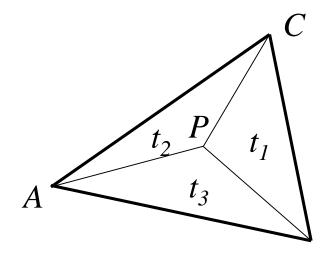
Barycentric Coordinates

- Used to define a point within a segment/triangle

2D Segment:

$$P = \alpha A + \beta B + \gamma C$$

$$\alpha = \frac{t_1}{S}; \beta = \frac{t_2}{S}; \gamma = \frac{t_3}{S}$$



S = area(ABC)

 $t_1 = area(PBC)$

 $t_2 = area(PCA)$

 $t_3 = area(PAB)$

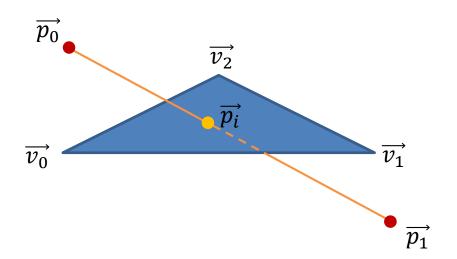


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segment-triangle intersection

- important for many intersection tests including triangle meshes
- also important for raytracing



intersection point

$$\vec{u} = (\vec{v_1} - \vec{v_0})$$

$$\vec{v} = (\vec{v_2} - \vec{v_0})$$

$$\vec{p_i} = \vec{v_0} + \vec{s} \cdot \vec{u} + \vec{t} \cdot \vec{v}$$

$$\vec{w} = (\vec{p_i} - \vec{v_0})$$

$$\vec{s} = \frac{(\vec{u} \cdot \vec{v})(\vec{w} \cdot \vec{v}) - (\vec{v} \cdot \vec{v})(\vec{w} \cdot \vec{u})}{(\vec{u} \cdot \vec{v})^2 - (\vec{u} \cdot \vec{u})(\vec{v} \cdot \vec{v})}$$

$$\vec{t} = \frac{(\vec{u} \cdot \vec{v})(\vec{w} \cdot \vec{u}) - (u \cdot \vec{u})(\vec{w} \cdot \vec{v})}{(\vec{u} \cdot \vec{v})^2 - (\vec{u} \cdot \vec{u})(\vec{v} \cdot \vec{v})}$$





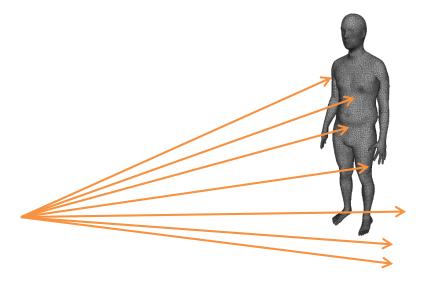
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Motivation

- Intersection tests are expensive computations
- e.g. a ray has to be tested against **each** triangle
- even rays that miss the object !!!





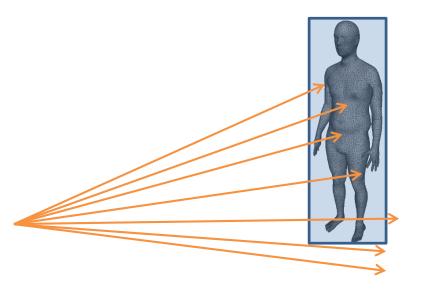


Motivation

- Intersection tests are expensive computations
- e.g. a ray has to be tested against **each** triangle
- even rays that miss the object !!!

Idea

- Embed object in a host geometry (simple box)
- Test each ray with the box first



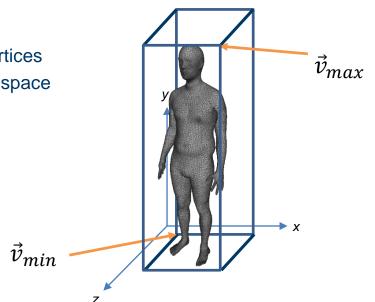




Axis-Aligned-Bounding-Box (AABB)

- A host geometry that contains all object's vertices
- and is aligned to the axis of the surrounding space
- AABB is uniquely defined by $ec{v}_{min}$ and $ec{v}_{max}$

AABB by expansion:







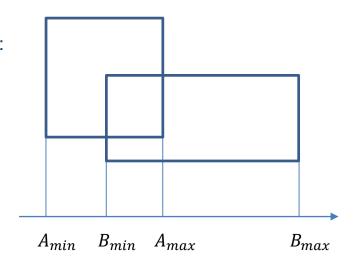
Intersecting two AABBs

- There is **no** intersection **if** for all three coordinate axis holds:

$$A_{min} > B_{max} \parallel B_{min} > A_{max}$$

Discussion

- Advantage: Fast computation, easy to implement
- Disadvantage: Update for moving/rotating objects



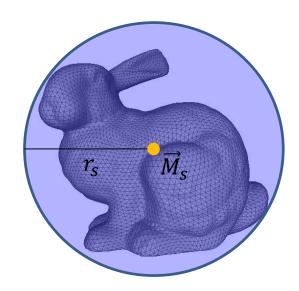




Bounding-Spheres

- Similar Idea as AABB, but with Spheres as enclosing Objects
- Advantage: Intersection tests are simple (simple distance test)
- Advantage: Rotation invariant
- Disadvantage: works well only for compact objects

```
\overrightarrow{\boldsymbol{M}}_{s} = \frac{1}{N} \sum_{i=0}^{numVertices-1} \overrightarrow{\boldsymbol{v}}_{i} \; ; \qquad \text{// center of mass} r_{s} = 0.0; \qquad \text{// radius} \text{for i = 1 to numVertices-1}} \text{if } (\|\overrightarrow{\boldsymbol{M}}_{s} - \overrightarrow{\boldsymbol{v}}_{i}\| > r_{s}) \text{ then } r_{s} = \|\overrightarrow{\boldsymbol{M}}_{s} - \overrightarrow{\boldsymbol{v}}_{i}\| \text{ end} end
```







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Collision Response

Introduction

- Once a collision is detected, a proper reaction has to be performed
- We only consider *rigid object collision*

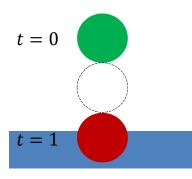


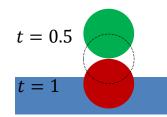


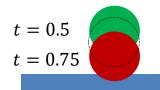
Collision Response

Interval Halving

- Find collision in time and space accurately
- Halving the interval. If Sphere at midpoint does not intersect → new lower bound
- If sphere at midpoint intersects → new upper bound













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