Table 1: Dataset

The dataset consists of five samples x_1, x_2, x_3, x_4, x_5 . For each sample, we can observe the features A_1, A_2, A_3 and the corresponding response.

Solution:

Solution:

$$i \hat{Z} = \{x_1, x_2, x_3, x_4, x_5\}$$

Entropy $(S) = -\frac{1}{5} \log_2(\frac{1}{5}) - \frac{1}{5} \log_2(\frac{1}{5})$
 $= 0.971$

Fraction $(S, A_1) = Entropy(S) - \sum_{u \in Value(A_1)} |S_1| Entropy(S_u)$
 $= Entropy(S) - \frac{1}{5} Entropy(A_1^+) - \frac{1}{5} Entropy(A_1^-)$
 $= 0.971 - \frac{1}{5} \times |S_1| = Entropy(A_1^-)$
 $= 0.971 - \frac{1}{5} \times |S_1| = Entropy(S_u)$
 $= 0.971 - \frac{1}{5} \times |S_1| = Entropy(A_1^-) = \frac{1}{5} (S_u) =$

=0.020. 放选择 Az.

A₂=1

A₂=0

S₁

S₁

S₂

=
$$\{X_3, X_4, X_5\}$$

= $\{X_1, X_2\}$
= $\{0, 0\}$

Entropy

 $\{S_1\}$
= $\{S_4\}$
 $\{X_3, X_4, X_5\}$

Entropy

 $\{S_1\}$
= $\{S_4\}$
 $\{S_4\}$
= $\{S$



$$g(x) = -\sum_{i=1}^{n} H_i \log(f_i(x)),$$

where $H \in \mathbb{R}^n$ is a one-hot vector.

Solution:

$$\frac{\partial f_{i}(x)}{\partial x_{i}} = \frac{\exp(x_{i}) \frac{\partial}{\partial x_{i}} \exp(x_{i}) - (\exp(x_{i}))^{2}}{\left(\frac{\partial}{\partial x_{i}} \exp(x_{i})\right)^{2}} = \frac{\exp(x_{i}) - (\exp(x_{i}))^{2}}{\frac{\partial}{\partial x_{i}} \exp(x_{i})} - \frac{\exp(x_{i}) - (\exp(x_{i}))^{2}}{\frac{\partial}{\partial x_{i}} \exp(x_{i})} = \frac{\exp(x_{$$

- (a) The convolutinal layer parameters are denoted as "conv(niter size)-(number of filters)".
- (b) The fully connected layer parameters are denoted as "FC(number of neurons)".
- (c) The window size of pooling layers is 3.
- (d) The stride of convolutinal layers is 1.
- (e) The stride of pooling layers is 3.
- (f) There is no padding in both convolutional and pooling layers.
- (g) For convenience, we assume that there is no activation function and bias.

Suppose that the input is a 386×386 RGB image. Please derive the size of all feature maps and the number of parameters.

conv3-64	max pool	conv3-256	conv1-512	max pool	FC-2048	FC-1000

Table 2: The architecture of convolutional neural network

Solution:

1.
$$\frac{\partial f_i(x)}{\partial x_i} = \frac{1}{n}$$
.
 $\nabla f_i(x) = \begin{pmatrix} \frac{1}{n} \\ \frac{1}{n} \end{pmatrix}$ 7 nf.

3, 2,

m

con (a) 先考虑、二催 仪、从了 酚情况

$$f_2(\chi) = \max \{\chi_1, \chi_2\}$$

$$= \frac{1}{2}(\chi_1 + \chi_2 + |\chi_1 - \chi_2|)$$

考虑. 多维情况

设 Xi, 分为 Xi, Xi, … Xi 中最大的两个数

$$f_2(x) = \max\{x_1, x_2, \dots x_n = \max\{x_i, x_j\}$$

$$= \frac{1}{2}(x_i + x_j + |x_i - x_j|)$$

同上讨论知在《XX=XX时行(X)不可张 XX+XX外行(X) 可微。

政可微点组会的集合 C 为

(b)

Ril

=
$$x_j + y_j - x_j = y_j \leq \max_{i} x_i y_i y_i = f_{i}(y)$$

parameters 3. feature maps 9×64 64x(386-3)x(3863) CONV3-64 = 576 无 max-pool = 1048576 9x256 CONV 3-256 26×64× (3434) 384-3+1) = 2304 = 260112384 1x512 5/2×256×64×(126-1+1)(126-1+1) Conv1-512 =512 = 133177540608 5 | 2 × 256 × 64 × 126 × 126 无 max-pool = 14797504512 14797504512×2048×3 FC-2048 2048 = 90915867721728 2048×1000 ≠ 经过第一个FC后的特征已当不区分 RGB三个通道, FC-1000 1000 成无需设计X3 = 2048000

Exercise 4: Matrix Calculus 20pts

Let L = f(h(Ax + b)), where $A \in \mathbb{R}^{m \times n}$, $x \in \mathbb{R}^n$, $b \in \mathbb{R}^m$, and $f : \mathbb{R}^m \to \mathbb{R}$. Define $z = Ax + b \in \mathbb{R}^m$ and $w = h(z) = (\sigma(z_1), \dots, \sigma(z_n))^\top$, where z_i is the i^{th} component of zand

$$\sigma(z_i) = \frac{1}{1 + \exp(-z_i)}.$$

Assume $\nabla_w f$ is known.

- 1. Please derive $\nabla_x L$.
- 2. Please derive

$$abla_A L = \left[egin{array}{ccccc} rac{\partial L}{\partial A_{11}} & \cdots & rac{\partial L}{\partial A_{1j}} & \cdots & rac{\partial L}{\partial A_{1n}} \ & \cdots & \cdots & \cdots & \cdots \ rac{\partial L}{\partial A_{i1}} & \cdots & rac{\partial L}{\partial A_{ij}} & \cdots & rac{\partial L}{\partial A_{in}} \ & \cdots & \cdots & \cdots & \cdots \ rac{\partial L}{\partial A_{m1}} & \cdots & rac{\partial L}{\partial A_{mn}} & \cdots & rac{\partial L}{\partial A_{mn}} \end{array}
ight],$$

where $A_{i,j}$ is the entry in the i^{th} row, j^{th} column of the matrix A.

Solution:

$$\nabla_{x}L = \nabla_{x}z \nabla_{z}\omega \nabla_{w}f$$

$$\nabla_{x}z = A^{T}$$

$$(\nabla_{z}\omega)_{ij} = \begin{cases} \frac{\exp(-z_{i})}{(1+\exp(-z_{i}))^{2}}, \ \dot{\tau}=\dot{j} \\ 0, \ \dot{\tau}+\dot{j} \end{cases}$$

$$\nabla_{x}L = A^{T} \begin{pmatrix} \frac{\exp(-z_{i})}{(1+\exp(-z_{i}))^{2}}, \ \dot{\tau}=\dot{j} \end{pmatrix} \nabla_{w}f$$

$$\frac{\exp(-z_{i})}{(1+\exp(-z_{i}))^{2}}$$

2,

$$\frac{\partial L}{\partial Aij} = \frac{\partial \mathcal{L}}{\partial w_i} \cdot \frac{\partial w_i}{\partial \mathcal{L}_i} \cdot \frac{\partial \mathcal{L}_i}{\partial Aij}$$

$$= (\nabla w f)_i \frac{\exp(-\partial i)}{(1 + \exp(-\partial i))^2} \cdot \chi_j$$