# Week 2

ML/DL Basic 안태영

# **Lecture 06: Softmax Regression**

### **Multinomial Classification**

- Binary classfication 모델을 여러 개 만들어서 여러가지 군으로 분리하는 것
- 2차원 행렬을 연산하여 진행한다
- ex) 3개의 label을 분류한다 했을 때는

$$w_{11}x_1+w_{12}x_2+w_{13}x_3, w_{21}x_1+w_{22}x_2+w_{23}x_3, w_{31}x_1+w_{32}x_2+w_{33}x_3\cdots$$
 이런식으로 나열해야 한다 하지만

행렬 연산을 진행 했을땐, 
$$egin{bmatrix} w_{11}w_{12}w_{13} \ w_{21}w_{22}w_{23} \ w_{31}w_{32}w_{33} \end{bmatrix} \cdot egin{bmatrix} x_1 \ x_2 \ x_3 \end{bmatrix}$$
로 표현 가능함

#### Softmax

- 어떤 입력 값에 대해서 각각의 원소에 대한 확률을 나타내주는 형태의 sigmoid 대체 함수
- 값들은 0과 1사이이다
- 각각의 원소의 합들이 1로 나타내어 진다
- $S(y_i) = rac{e^{y_i}}{\sum e^{y_j}}$

### **One-Hot Encoding**

- Softmax 함수를 거쳐서 나온 값중 가장 큰 값의 확률을 1로 바꾸는 과정
- tensorflow에서는 argmax라는 함수가 담당한다

# **Lecture 06: Softmax Regression**

### **Cross Entropy**

- Multi label classification에서 cost
- - $\sum_i L_i \log S_i = \sum_i L_i * (-\log S_i)$

#### **Cost Function**

- $Loss = rac{1}{N}\sum_i D(S(wx_i+b),L_i)$
- 여기서  $S(wx_i + b)$ 는 y 값,  $L_i$ 는 확률 값이다

#### **Gradient Descent**

• 이번엔 각각의 weight 벡터에 대한 gradient의 편미분을 말하는 것이다

```
[26] 1 import tensorflow as tf
2 import numpy as np
3 import matplotlib.pyplot as plt
4
5 tf.random.set_seed(777) # for reproducibility
```

### Data를 벡터 형태로 담는다

#### nb\_class

→ nb\_class는 몇개의 sector로 분류할 것인지에 대한 변수로, 행의 개수를 정의하는 것이다

```
[5] 1 #Data
        2 \times data = [[1, 2, 1, 1],
                   [2, 1, 3, 2],
       4
                    [3, 1, 3, 4],
                   [4, 1, 5, 5],
                   [1, 7, 5, 5],
                   [1, 2, 5, 6],
                   [1, 6, 6, 6],
        9
                   [1, 7, 7, 7]]
       10 \text{ y\_data} = [[0, 0, 1],
       11
                    [0, 0, 1],
       1.2
                   [0, 0, 1],
       13
                   [0, 1, 0],
       14
                   [0, 1, 0],
       15
                   [0, 1, 0],
       16
                   [1, 0, 0],
       1.7
                   [1, 0, 0]]
       18
       19 #convert into numpy and float format
       20 x_data = np.asarray(x_data, dtype=np.float32)
       21 y_data = np.asarray(y_data, dtype=np.float32)
       22
       23 #nb_classes
       24 nb_classes = 3
       25 print (x_data.shape)
       26 print (y_data.shape)
      (8, 4)
      (8, 3)
```

Hyopothesis에 들어갈 weight값과 bias 설정

[3,23390484e-01 5.90759404e-02 6.17533624e-01] [3,62997366e-06 6.20727221e-08 9.99996245e-01] [2,62520202e-02 1.07279625e-02 9.63019967e-01] [1,56525093e-05 4.21802724e-07 9.99983847e-01]

[2.94076904e-06 3.81133241e-08 9.99996960e-01]], shape=(8, 3), dtype=float32)

#### Hypothesis

#### Softmax funciton

```
[8] 1 sample_db = [[8,2,1,4]]
2 sample_db = np.asarray(sample_db, dtype=np.float32)
3
4
5 print(hypothesis(sample_db))
```

#### Cost function

```
[9] 1 def cost_fn(X, Y):
2     logits = hypothesis(X)
3     cost = -tf.reduce_sum(Y * tf.math.log(logits), axis=1)
4     cost_mean = tf.reduce_mean(cost)
5
6     return cost_mean
7
8 print(cost_fn(x_data, y_data))
```

tf.Tensor(6.07932, shape=(), dtype=float32)

### **Gradient Tapee**

```
[10] 1 x = tf.constant(3.0)
2 with tf.GradientTape() as g:
3     g.watch(x)
4     y = x * x # x^2
5 dy_dx = g.gradient(y, x) # Will compute to 6.0
6 print(dy_dx)
```

tf.Tensor(6.0, shape=(), dtype=float32)

#### Model fitting

```
[12] 1 def fit(X, Y, epochs=2000, verbose=100):
            optimizer = tf.keras.optimizers.SGD(learning_rate=0.1)
           for I in range (epochs):
                grads = grad_fn(X, Y)
      6
                optimizer.apply_gradients(zip(grads, variables))
                if (i==0) | ((i+1)\%verbose==0):
                    print('Loss at epoch %d: %f' %(i+1, cost_fn(X, Y).numpy()))
     10 fit(x_data, y_data)
    Loss at epoch 1: 2.849417
    Loss at epoch 100: 0.684151
    Loss at epoch 200: 0.613813
    Loss at epoch 300: 0,558204
    Loss at epoch 400: 0.508306
    Loss at epoch 500: 0.461058
    Loss at epoch 600: 0.415072
    Loss at epoch 700: 0,369636
    Loss at epoch 800: 0,324533
    Loss at epoch 900: 0.280721
    Loss at epoch 1000: 0.246752
    Loss at epoch 1100: 0.232798
     Loss at epoch 1200: 0.221645
     Loss at epoch 1300: 0.211476
     Loss at epoch 1400: 0.202164
     Loss at epoch 1500: 0.193606
    Loss at epoch 1600: 0.185714
     Loss at epoch 1700: 0.178415
    Loss at epoch 1800: 0.171645
    Loss at epoch 1900: 0.165351
    Loss at epoch 2000: 0.159483
```

### Argmax를 이용한 정확도 측정

```
1 sample data = [[2,1,3,2]] # answer label [[0,0,1]]
 2 sample_data = np.asarray(sample_data, dtype=np.float32)
 4 a = hypothesis(sample data)
 6 print(a)
 7 print(tf.argmax(a, 1)) #index: 2
9 b = hypothesis(x_data)
10 print(b)
11 print(tf.argmax(b, 1))
12 print(tf.argmax(y_data, 1)) # matches with y_data
tf.Tensor([[0.00112886 0.08154673 0.9173244 ]], shape=(1, 3), dtype=float32)
tf.Tensor([2], shape=(1,), dtype=int64)
tf.Tensor(
[[2.1976039e-06 1.2331199e-03 9.9876475e-01]
[1.1288594e-03 8.1546724e-02 9.1732436e-01]
[2.2205660e-07 1.6418649e-01 8.3581328e-01]
 [6.3921934e-06 8.5045439e-01 1.4953916e-01]
[2.6150793e-01 7.2644734e-01 1.2044546e-02]
 [1.3783264e-01 8.6213988e-01 2.7417602e-05]
[7.4242103e-01 2.5754192e-01 3.6978636e-05]
[9.2197543e-01 7.8024052e-02 6.0005920e-07]], shape=(8, 3), dtype=float32)
tf.Tensor([2 2 2 1 1 1 0 0], shape=(8,), dtype=int64)
tf.Tensor([2 2 2 1 1 1 0 0], shape=(8,), dtype=int64)
```

### tf.onehot()

- → 내가 원하는 행의 개수 만큼 행렬을 변환해주는 method
- → 3차원으로 반환

(101, 16) (101, 7)

### tf.reshape()

- → 원하는 형태의 행렬로 재배열 해준다
- → 앞서 3차원으로 반환 되었지만 2차원 형태로 model fitting을 해야하기 때문에 reshape를 사용한다

```
1 xy = np.loadtxt('data-04-zoo.csv', delimiter=',', dtype=np.float32)
2 x_data = xy[:, 0:-1]
3 y_data = xy[:, -1]
4
5 nb_classes = 7 # 0 ~ 6
6
7 # Make Y data as onehot shape
8 #2차원에서 3차원으로 변환
9 #tf.one_hot()을 쓰면 3차원으로 반환을 해주기 때문에
10 Y_one_hot = tf.one_hot(y_data.astype(np.int32), nb_classes)
11 Y_one_hot = tf.reshape(Y_one_hot, [-1, nb_classes])
12 print(x_data.shape, Y_one_hot.shape)
```

#### tf.onehot()

- → 내가 원하는 행의 개수 만큼 행렬을 변환해주는 method
- → 3차원으로 반환

### tf.reshape()

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8 #2차원에서 3차원으로 변환
9 #tf.one_hot()을 쓰면 3차원으로 반환을 해주기 때문에
10 Y_one_hot = tf.one_hot(y_data.astype(np.int32), nb_classes)
11 Y_one_hot = tf.reshape(Y_one_hot, [-1, nb_classes])
12 print(x_data.shape, Y_one_hot.shape)
(101, 16) (101, 7)
```

### Weight와 Bias

→ 전과 같음

### Logit Function, Hypothesis

→ 나중에 정확도 관련 값을 구할때 필요하기 때문에 따로 정의한다

### **Cross Entropy**

→ tf.keras.losses.categorical\_crossentropy() 이용

### tf.argmax()

→ 가장 큰값을 가지는 index를 리턴해준다

#### Prediction

→ Accuracy를 알려주는 함수

```
1 #Weight and blas setting
 2 W = tf. Variable(tf.random.normal((16, nb_classes)), name='weight')
 3 b = tf. Variable(tf.random.normal((nb_classes,)), name='bias')
 4 variables = [W. b]
 6 # tf.nn.softmax computes softmax activations
 7 # softmax = exp(logits) / reduce_sum(exp(logits), dim)
 9 #####logit과 hypothesis를 다르게 함
10 def logit fn(X):
11 return tf.matmul(X, W) + b
12
13 def hypothesis(X):
14    return tf.nn.softmax(logit_fn(X))
15
16 def cost_fn(X, Y):
17 logits = logit_fn(X)
18 cost_i = tf.keras.losses.categorical_crossentropy(y_true=Y, y_pred=logits,
19
                                                     from_logits=True)
20   cost = tf.reduce_mean(cost_i)
21
   return cost
22
23 #이전과 동일
24 def grad fn(X, Y):
25 with tf.GradientTape() as tape:
         loss = cost fn(X, Y)
27
          grads = tape.gradient(loss, variables)
28
          return grads
29
30 #정확도를 나타내주는것이 추가됨
31 #tf.argmax 알아보기
32 def prediction(X, Y):
pred = tf.argmax(hypothesis(X), 1)
34 correct_prediction = tf.equal(pred, tf.argmax(Y, 1))
35
   accuracy = tf.reduce_mean(tf.cast(correct_prediction, tf.float32))
36
      return accuracy
```

Steps: 500 Loss: 0.19246312975883484, Acc: 0.9603960514068604 Steps: 600 Loss: 0.16442003846168518, Acc: 0.9603960514068604 Steps: 700 Loss: 0.14311201870441437, Acc: 0.9603960514068604 Steps: 800 Loss: 0.12642519176006317, Acc: 0.9603960514068604 Steps: 900 Loss: 0.11306187510490417, Acc: 0.9900990128517151 Steps: 1000 Loss: 0.10216663777828217, Acc: 0.9900990128517151

```
[16] 1 def fit(X, Y, epochs=1000, verbose=100):
            optimizer = tf.keras.optimizers.SGD(learning rate=0.1)
      3
            for i in range(epochs):
      4
      5
                grads = grad_fn(X, Y)
      6
                optimizer.apply gradients(zip(grads, variables))
                If (i==0) | ((i+1)\%verbose==0):
                      print('Loss at epoch %d: %f' %(i+1, cost_fn(X, Y).numpy()))
      8 #
      9
                    acc = prediction(X, Y).numpy()
     10
                    loss = cost_fn(X, Y).numpy()
                    print('Steps: {} Loss: {}, Acc: {}'.format(i+1, loss, acc))
     11
     12
     13 fit(x_data, Y_one_hot)
     Steps: 1 Loss: 5.610101222991943, Acc: 0.1683168262243271
     Steps: 100 Loss: 0.6019306182861328, Acc: 0.8415841460227966
     Steps: 200 Loss: 0.38190874457359314, Acc: 0.9108911156654358
     Steps: 300 Loss: 0.2877010405063629, Acc: 0.9405940771102905
     Steps: 400 Loss: 0.23101474344730377, Acc: 0.9504950642585754
```

### **Learning Rate**

- → Learnging Rate 값이 크면 Overshootiing 현상이 생긴다. 즉, 다음 weight 값이 최소 점보다 더 멀리 나아가 발산한다.
- → Laerning Rate 값이 작으면 시간이 오래 걸려 Overfitting이나 발산형태로 나아간다.

#### **Exponential Decay**

```
• \alpha = \alpha_0 e^{-kt}
```

```
[21] 1 """
      2 0: Exponential Decay
      3 1: Inverse Time Decay
      4 2: Cosine Daecay
      5 3: Piecewise Decay
      7 .....
     9 EPOCHS = 1001
     11 for step in range(EPOCHS):
           for features, labels in iter(dataset):
               features = tf.cast(features, tf.float32)
     14
              labels = tf.cast(labels, tf.float32)
     15
               grads = grad(softmax_fn(features), features, labels)
     16
               optimizer = learningRate(0)
     17
     18
               optimizer.apply_gradients(grads_and_vars=zip(grads,[W,b]))
                   print("Iter: {}, Loss: {:.4f}".format(step, loss_fn(softmax_fn(features),features,labels)))
     21 x_test = tf.cast(x_test, tf.float32)
     22 y_test = tf.cast(y_test, tf.float32)
     23 test_acc = accuracy_fn(softmax_fn(x_test),y_test)
     24 print("Testset Accuracy: {:.4f}".format(test_acc))
     Iter: 0, Loss: 12.4497
     Iter: 100, Loss: 0.6930
     Iter: 200, Loss: 0.5960
     Iter: 300, Loss: 0.5394
     Iter: 400, Loss: 0.4986
     Iter: 500, Loss: 0.4665
     Iter: 600, Loss: 0.4401
     Iter: 700, Loss: 0.4177
     Iter: 800, Loss: 0.3984
     Iter: 900, Loss: 0.3814
     Iter: 1000, Loss: 0.3664
    Testset Accuracy: 1.0000
```

```
Inverse Time Decay 
ightarrow lpha = rac{lpha_0}{1+kt}
```

```
[22] 1 """
      2 0: Exponential Decay
      3 1: Inverse Time Decay
      4 2: Cosine Daecay
      5 3: Piecewise Decay
      7 8 8 8
      9 EPOCHS = 1001
     11 for step in range (EPOCHS):
     12 for features, labels in iter(dataset):
     13
                features = tf.cast(features, tf.float32)
     14
                labels = tf.cast(labels, tf.float32)
     15
                grads = grad(softmax_fn(features), features, labels)
     16
                optimizer = learningRate(1)
     17
     18
                optimizer.apply gradients(grads and vars=zip(grads,[W,b]))
     19
                if step % 100 == 0:
                    print("Iter: {}, Loss: {:.4f}".format(step, loss_fn(softmax_fn(features), features, labels)))
     21 x_test = tf.cast(x_test, tf.float32)
     22 y_test = tf.cast(y_test, tf.float32)
     23 test_acc = accuracy_fn(softmax_fn(x_test),y_test)
     24 print("Testset Accuracy: {:.4f}".format(test_acc))
     Iter: 0, Loss: 0,3662
     Iter: 100, Loss: 0.3528
     Iter: 200, Loss: 0.3407
     Iter: 300, Loss: 0.3296
     Iter: 400, Loss: 0.3195
     Iter: 500, Loss: 0.3102
     Iter: 600, Loss: 0.3016
     Iter: 700, Loss: 0.2936
     Iter: 800, Loss: 0.2861
     Iter: 900, Loss: 0.2792
     Iter: 1000, Loss: 0.2726
     Testset Accuracy: 1.0000
```

Iter: 1000, Loss: 0.2228

```
Cosine Annealing
       • lpha = lpha_{min}^i + rac{1}{2}(lpha_{max}^i - lpha_{min}^i)(1 + \cos(rac{T_{current}}{T_i}\pi))
       • lpha_{min}, lpha_{max}: 학습전 설정된 learning rate의 최대 최소값
       • T<sub>current</sub>: 현재 Epoch
       • T_i: Cosine Annealing을 실행하는 주기
23] 1 """
     20: Exponential Decay
     3 1: Inverse Time Decay
     4 2: Cosine Daecay
     53: Piecewise Decay
     9 EPOCHS = 1001
    11 for step in range(EPOCHS):
    12 for features, labels in iter(dataset):
            features = tf.cast(features, tf.float32)
               labels = tf.cast(labels, tf.float32)
               grads = grad(softmax_fn(features), features, labels)
               optimizer = learningRate(2)
    17
               optimizer.apply_gradients(grads_and_vars=zip(grads,[W,b]))
               if step % 100 == 0:
                   print("Iter: {}, Loss: {:.4f}".format(step, loss_fn(softmax_fn(features),features,labels)))
    21 x_test = tf.cast(x_test, tf.float32)
    22 y_test = tf.cast(y_test, tf.float32)
    28 test_acc = accuracy_fn(softmax_fn(x_test),y_test)
    24 print("Testset Accuracy: {:.4f}".format(test_acc))
    Iter: 0, Loss: 0,2725
    Iter: 100, Loss: 0.2664
    Iter: 200, Loss: 0.2605
    Iter: 300, Loss: 0.2550
    Iter: 400, Loss: 0.2497
    Iter: 500, Loss: 0.2447
    Iter: 600, Loss: 0.2399
    Iter: 700, Loss: 0.2354
    Iter: 800, Loss: 0.2310
    Iter: 900, Loss: 0.2268
```

#### Piecewise Annealing

- 특정 Epoch에 도달할 때 특정 값을 learning rate로 바꾼다
- · keras.optimizers.schedules.PiecewiseConstantDecay( boundaries, values)
- boudary와 value는 순서가 있는 객체로 선언해야함

```
2 0: Exponential Decay
 3 1: Inverse Time Decay
 4 2: Cosine Daecay
 5 3: Piecewise Decay
7 ....
 8
9 EPOCHS = 1001
11 for step in range(EPOCHS):
12 for features, labels in iter(dataset):
           features = tf.cast(features, tf.float32)
           labels = tf.cast(labels, tf.float32)
15
          grads = grad(softmax_fn(features), features, labels)
16
          optimizer = learningRate(3)
18
           optimizer.apply_gradients(grads_and_vars=zip(grads,[W,b]))
19
           if step % 100 == 0:
              print("Iter: {}, Loss: {:.4f}".format(step, loss_fn(softmax_fn(features), features, labels)))
21 x_test = tf.cast(x_test, tf.float32)
22 y_test = tf.cast(y_test, tf.float32)
28 test_acc = accuracy_fn(softmax_fn(x_test),y_test)
24 print("Testset Accuracy: {:.4f}".format(test_acc))
Iter: 0, Loss: 0.2224
```

Iter: 100, Loss: 0.2224
Iter: 100, Loss: 3.9286
Iter: 200, Loss: 7.1143
Iter: 200, Loss: 5.5011
Iter: 400, Loss: 7.2813
Iter: 500, Loss: 4.4398
Iter: 600, Loss: 6.1004
Iter: 700, Loss: 1.2818
Iter: 800, Loss: 2.3291
Iter: 900, Loss: 0.1078
Iter: 1000, Loss: 0.0225
Testset Accuracy: 1.0000

# → Lab 07-2: linear regression(without min/max)

### Normalization

→ 데이터의 값을 0과1 사이로 만들어주는 과정

$$x_{new} = rac{x-\mu}{\sigma}$$

### Standardization

→ 평균과 얼마나 떨어져 있는지에 대해서 평균에 대해 정규화 하는 과정

$$x_{new} = rac{x - x_{min}}{x_{max} - x_{min}}$$

```
1 def normalization(data):
2 numerator = data - np.min(data, 0)
3 denominator = np.max(data, 0) - np.min(data, 0)
4 return numerator / denominator
5
6 def standardization(data):
7 numerator = data - np.mean(data)
8 denominator = sgrt(np.sum(data - np.mean(data))^2/np.count(data))
```

# → Lab 07-3: Overfitting

### Overfitting

→ model이 너무 train data에 취중해서 fitting 됨

### Over fitting 줄이는 방법

- train data를 많이 받는다
- feature 수를 줄인다 (차원 축소)
- feature 수를 늘린다 (hypothesis의 식을 더 많이)

#### Data Set and Validation

→ train data와 test data의 비율을 잘 조정해서 data를 구성해야 한다

### Fine tuning

ightarrow model을 Learning 하는 과정에서 모델의 특정 분류 방법을 고치거나 기존 모델에 또 다른 기법을 추가해서 fitting 하는 과정

## Lab 07-3-2: Mnist

#### Mnist data set

→ 0부터 9까지 모아 놓은 손글씨 data set

#### Model

```
1 model = tf.keras.models.Sequential([
2     tf.keras.layers.Flatten(),
3     tf.keras.layers.Dense(512, activation=tf.nn.relu),
4     tf.keras.layers.Dropout(0.2),
5     tf.keras.layers.Dense(10, activation=tf.nn.softmax)
6 ])
```

#### Model

```
i model = tf.keras.models.Sequential([
    tf.keras.layers.Flatten(),
    tf.keras.layers.Dense(512, activation=tf.nn.relu),
    tf.keras.layers.Dropout(0.2),
    tf.keras.layers.Dense(10, activation=tf.nn.softmax)
    []
```

#### Optimizer, Cross Entropy

```
1 model.compile(optimizer='adam',
2 loss='sparse_categorical_crossentropy',
3 metrics=['accuracy'])
```

#### Model fitting

```
1 model.fit(x_train, y_train, epochs=5)
```

#### **Evaluation**

#### **Fasion mnist**

→ 10가지의 옷의 labe을 가진 data

```
1 plt.figure()
2 plt.imshow(train_images[3])
3 plt.colorbar()
4 plt.grid(False)
5 train_images = train_images / 255.0
6 test_images = test_images / 255.0
7
8 plt.figure(figsize=(10,10))
9 for i in range(25):
10    pit.subplot(5,5,i+1)
11    pit.xticks([])
12    pit.yticks([])
13    pit.grid(False)
14    plt.imshow(train_images[i], cmap=plt.cm.binary)
15    plt.xlabel(class_names[train_labels[i]])
```

