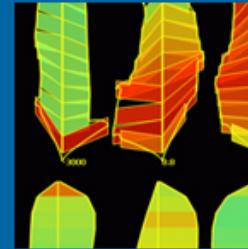
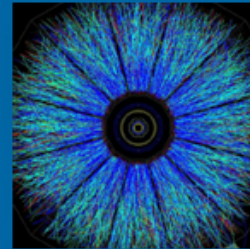
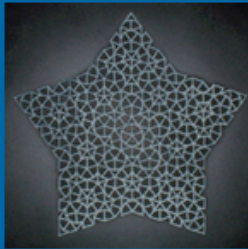




Swansea University  
Prifysgol Abertawe

# CS130: Professional Issues

## Cryptography and Data Security: Solving the Key Exchange Problem



# Topic Learning Goals

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How does encryption secure a message?

What is Diffie-Hellman key exchange?

What is RSA Public Key/Private Key encryption?

What maths underpin modern encryption?

# Encryption as a Locked Box

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Picture encryption as a box that you secure a message in by locking it with a key (shared secret)

- But everything is digital so it can be copied infinitely...

The sender locks up the box and hands it along in pass-the-parcel style

When it reaches the intended recipient, they then open the box with their key

*But how does the recipient get their key?*

# Diffie-Hellman Principles

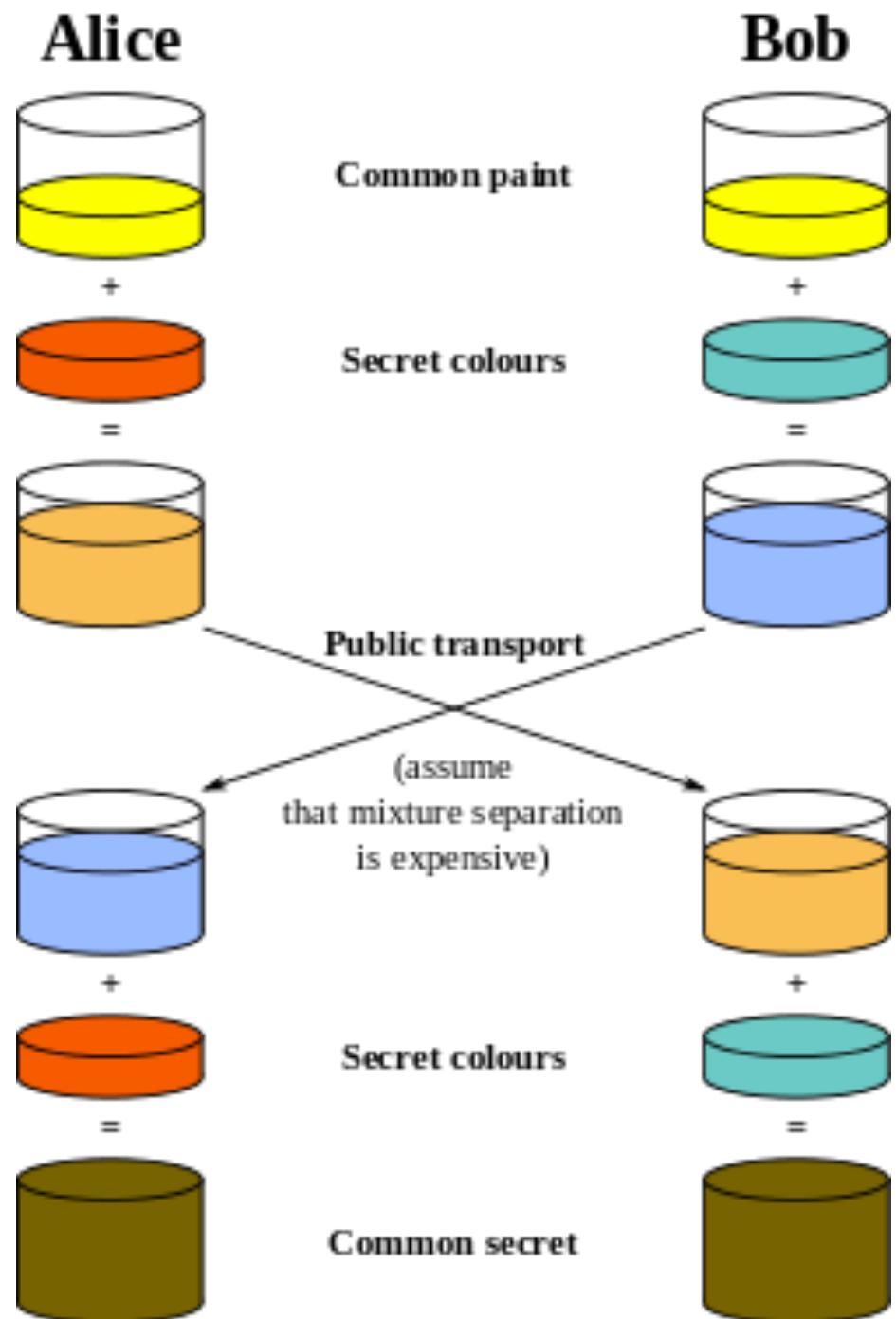
A way to establish a shared secret between two parties where communication can be seen by Eve

Relies on maths that works like paint works

- Specifically factorisation

What is the weakness of this approach?

- ???



# Diffie-Hellman Principles

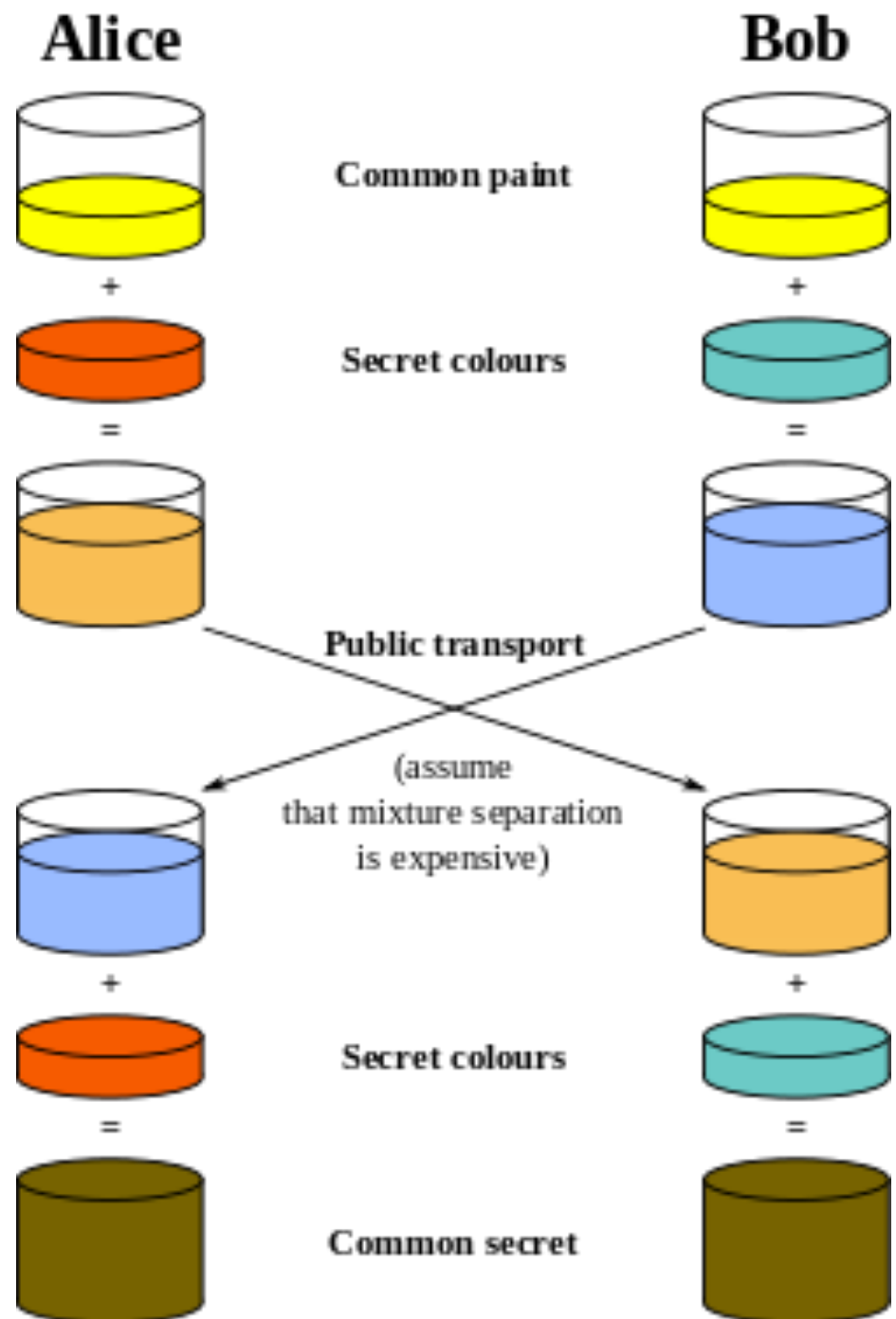
A way to establish a shared secret between two parties where communication can be seen by Eve

Relies on maths that works like paint works

- Specifically factorisation

What is the weakness of this approach?

- The Man in the Middle Attack where Eve intercepts and pretends to be Alice and Bob



# Public Key/Private Key Pairs - RSA

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A “lock” anyone can close (encrypt) with your public key but only your private key can open

RSA generates a ***public key*** and a ***private key***

- You publish the public key online and let anyone use it to lock up their message to you in a box
- You keep the private key a secret that only you know and only it can open the messages encrypted with the public key

Anybody can encode a message to send to you using the public key but only the private key can decrypt it


# Public Key, Private Key Encryption

```
// Code to run on Sender's machine
private Message pkEncrypt(Message originalMessage, PublicKey pk)
{
    new Message em = SomeFunkyMaths(originalMessage,pk);
    return em;
}

// em is sent over the internet to the recipient

// code to run on Recipients machine
private Message pkDecrypt(Message em, PrivateKey k)
{
    new Message decryptedMessage = reverseFunkyMaths(em,k);
    return decrypted;
}

// now decrypted should equal the original message
```




# Key Idea: This Doesn't Work

```
// A malicious user intercepts your message and tries to
// decrypt it using your Public Key

private Message pkDecrypt(Message em, PublicKey k)
{
    new Message decryptedMessage = reverseFunkyMaths(em,k);
    return decrypted;
}

// decrypted will still be unreadable in this case
```





# Encryption foundation: One way functions

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Trapdoor or one way functions, easy to calculate the result with inputs but hard to reverse

Easy:  $2 \times 2 \times 2 \times 3 = ?$

# Solving the Problem: Public Key Encryption

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Trapdoor or one way functions, easy to calculate the result with inputs but hard to reverse

Easy:  $2 \times 2 \times 2 \times 3 = 24$

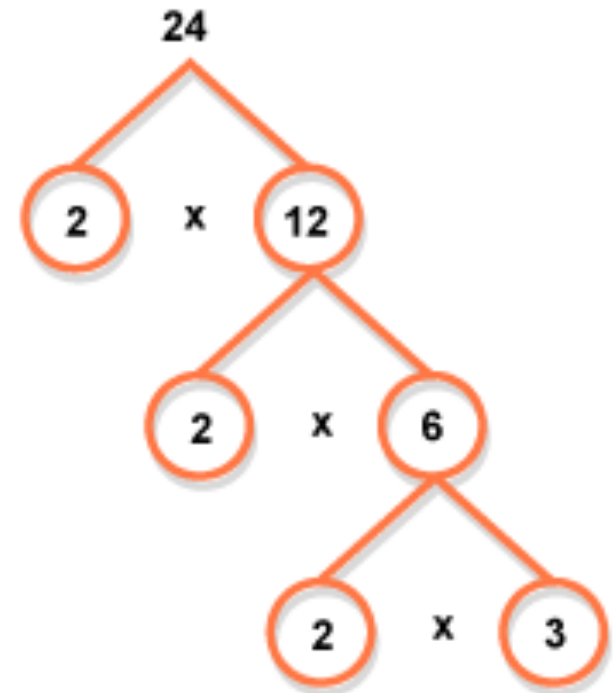
Hard: Prime factorisation of 24

# Solving the Problem: Public Key Encryption

Trapdoor or one way functions, easy to calculate the result with inputs but hard to reverse

Easy:  $2 \times 2 \times 2 \times 3 = 24$

Hard: Prime factorisation of 24



# Solving the Problem: Public Key Encryption

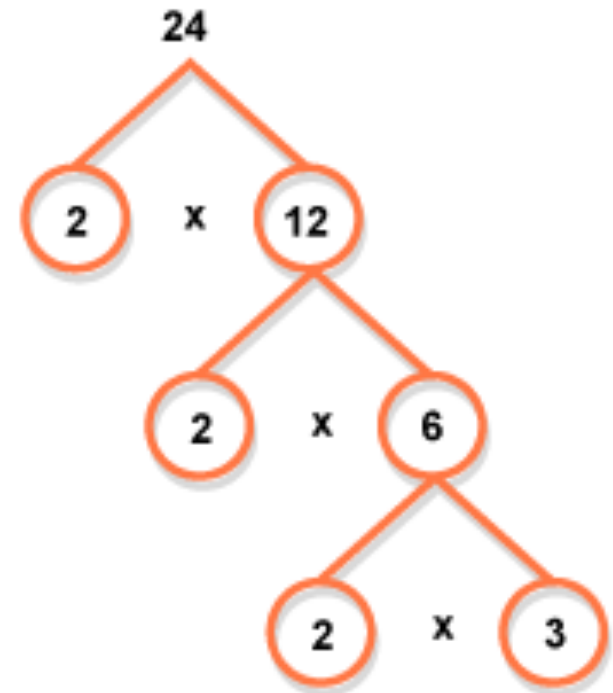
Trapdoor or one way functions, easy to calculate the result with inputs but hard to reverse

Easy:  $2 \times 2 \times 2 \times 3 = 24$  (PrivKey)

Hard: Prime factorisation of 24 (PubKey)

So, we encrypt using functions that are easily decrypted (reversed) if you know their prime factors like Eulers totient function

- Still more to this like block size we will not get into



- 
1. Select 4 prime numbers - private key
  2. Multiply them to get your public key
  3. Swap with a friend and figure out their private key

2, 3, 5, 7, 11, 13, 17, 19, 23, 29

# Public Key Encryption – How Big?

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20395687835640197740576586692903457728019399331

# Public Key Encryption – How Big?

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203956878356401977405765866929034577280193  
993314348263094772646453283062722701277632  
936616063144088173312372882677123879538709  
400158306567338328279154499698366071906766  
440037074217117805690872792848149112022286  
332144876183376326512083574821647933992961  
249731983621930427428024380310401500056379  
0123

# Public Key Encryption – UK Population

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203956878356401977405765866929034577280193  
993314348263094772646453283062722701277632  
936616063144088173312372882677123879538709  
400158306567338328279154499698366071906766  
440037074217117805690872792848149112022286  
332144876183376326512083574821647933992961  
249731983621930427428024380310401500056379  
0123



# Public Key Encryption – World Population

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203956878356401977405765866929034577280193  
993314348263094772646453283062722701277632  
936616063144088173312372882677123879538709  
400158306567338328279154499698366071906766  
440037074217117805690872792848149112022286  
332144876183376326512083574821647933992961  
249731983621930427428024380310401500056379  
0123

# People who've ever lived

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203956878356401977405765866929034577280193  
993314348263094772646453283062722701277632  
936616063144088173312372882677123879538709  
400158306567338328279154499698366071906766  
440037074217117805690872792848149112022286  
332144876183376326512083574821647933992961  
249731983621930427428024380310401500056379  
0123

# Grains of sand on earth

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203956878356401977405765866929034577280193  
993314348263094772646453283062722701277632  
936616063144088173312372882677123879538709  
400158306567338328279154499698366071906766  
440037074217117805690872792848149112022286  
332144876183376326512083574821647933992961  
249731983621930427428024380310401500056379  
0123

# Age of the Universe (in seconds)

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203956878356401977405765866929034577280193  
993314348263094772646453283062722701277632  
936616063144088173312372882677123879538709  
400158306567338328279154499698366071906766  
440037074217117805690872792848149112022286  
332144876183376326512083574821647933992961  
249731983621930427428024380310401500056379  
0123

# Atoms in the Universe

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203956878356401977405765866929034577280193  
993314348263094772646453283062722701277632  
936616063144088173312372882677123879538709  
400158306567338328279154499698366071906766  
440037074217117805690872792848149112022286  
332144876183376326512083574821647933992961  
249731983621930427428024380310401500056379  
0123

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We still have a major problem

Public Key Encryption is the  
foundation of the modern Internet but  
how do you know the owner of a  
Public Key is who they claim to be?

# Topic Learning Goals

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How does encryption secure a message?

What is Diffie-Hellman key exchange?

What is RSA Public Key/Private Key encryption?

What maths underpin modern encryption?

# Topic Learning Goals

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How does encryption secure a message?

It locks it in a “box” that you need a key to open

What is Diffie-Hellman key exchange?

A system that mixes numbers together to allow public sharing of keys albeit with a vulnerability

What is RSA Public Key/Private Key encryption?

Locked boxes using two different keys, one which locks and one which unlocks

What maths underpin modern encryption?

Trapdoor functions like prime factorisation