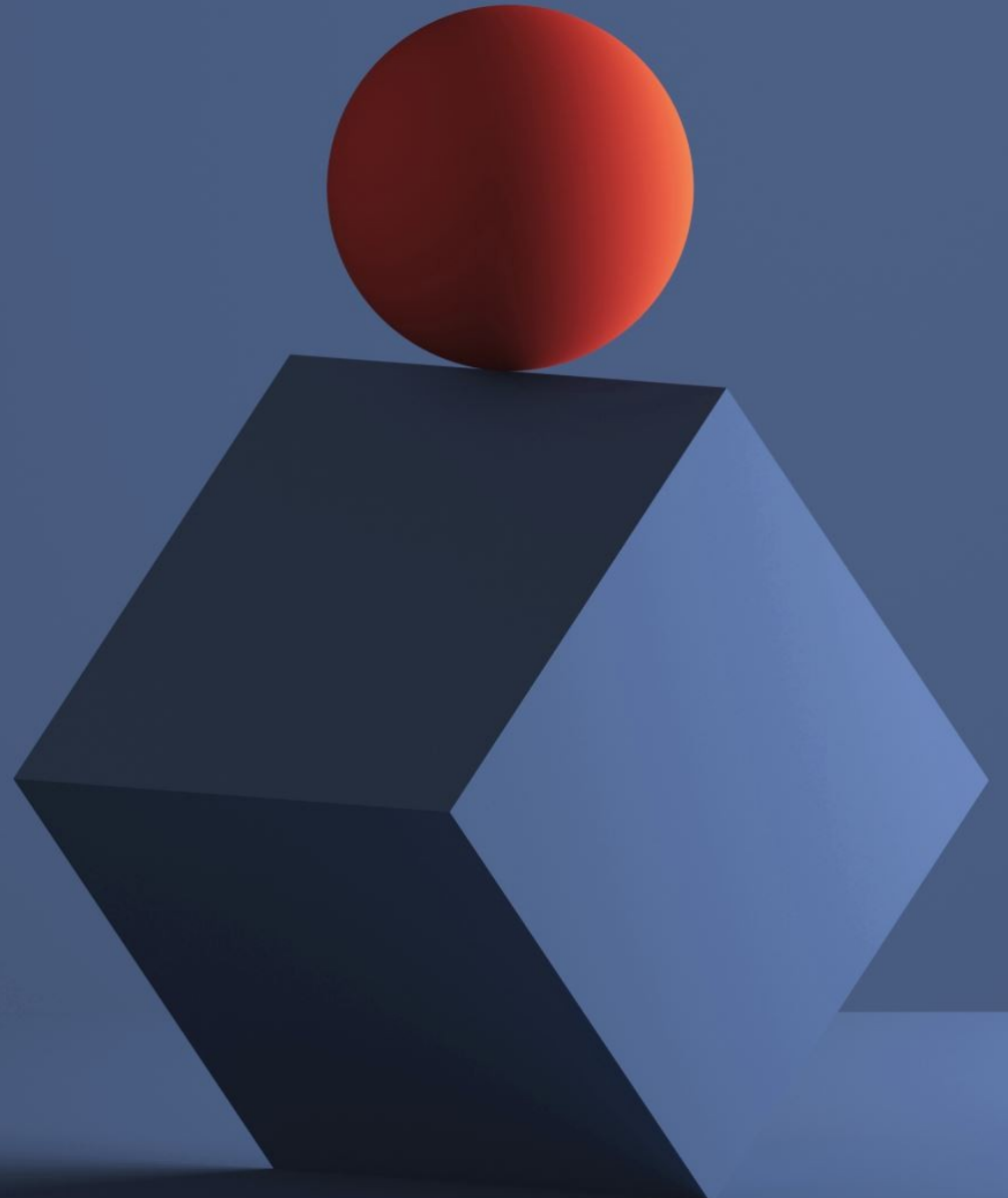


# Tutorial 5

Probability and Statistics



## » Solution to problem in previous slide...part-2

$$p_n = p p_{n-1} + p(1-p) p_{n-2},$$

with

$$p_1 = 0$$

$$p_2 = (1-p)^2$$

Solution for  
recurrence  
from class

A coin is tossed until two successive tails are obtained.  $P(\text{heads}) = p$ . Find the probability that experiment is completed on  $n$ -th toss.

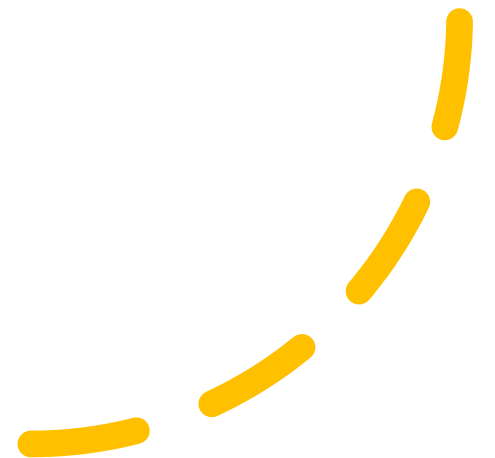
# Question 1: Children and coins

1.  $N$  children are sitting in a circle.
2. Each child has one coin.
3. Each child chooses a neighbor (left/right) with 50% probability and gives their coin to that selected neighbor.
4. On average, how many children will be left without any coin?



# Question 2

- In a sequence of Bernoulli trials with probability  $p$  for success, find the
  1. probability that  $x$  successes will occur before  $y$  failures.



# Question 3

- Colorblindness appears in 1 per cent of the people in a certain population.
- How large must a random sample (with replacements) be if the probability of its containing a colorblind person is to, be 0.95 or more?



# Question 4

- A book of  $n$  pages contains on the average  $A$  misprints per page. Estimate the probability that at least one page will contain more than  $k$  misprints.

