

Assignment 3 Question 4

Friday, October 9, 2020 9:48 AM

"My X is a boy"

chosen randomly

Atsa is named X here for short notation

50-50 if Boy-Girl

This is crucial for the numbers to hold.

$$P\left(\frac{\text{Boy-Girl}}{1 \text{ is a Boy}}\right) = P\left(\frac{X \text{ is a Boy}}{\text{Boy-Girl}}\right) \frac{P(\text{Boy-Girl})}{P(X \text{ is a Boy})}$$

All terms are also conditioned on
→ At least 1 Boy of the 2

* Boy-Girl is unordered in our notation

$$\Rightarrow P(\text{Boy-Girl}) = 0.66$$

$$P\left(\frac{X \text{ is a Boy}}{\text{Boy-Girl}}\right) = 0.5$$

$$P(X \text{ is a Boy}) = 0.66$$

$\begin{matrix} \checkmark & \checkmark \\ B & B \\ \checkmark & \checkmark \\ B & G \\ G & B \\ \checkmark & \checkmark \\ \cancel{G} & \cancel{G} \end{matrix}$

$$\begin{aligned} \text{Alternatively } P(X \text{ is a boy}) &= P(\text{Boy-Girl}) P\left(\frac{X \text{ is a boy}}{\text{Boy-Girl}}\right) + P(\text{Boy-Boy}) P\left(\frac{X \text{ is a boy}}{\text{Boy-Boy}}\right) \\ &= \frac{1}{2} \times \frac{2}{3} + \frac{1}{1} \times \frac{1}{3} = \frac{4}{3} = \frac{2}{3} \end{aligned}$$

$$\therefore P\left(\frac{\text{Boy-Girl}}{X \text{ is a boy}}\right) = 0.5 \cdot \frac{0.66}{0.66} = 0.5$$

Everything adds up

Information FAIR was gained when we got a sampling from the 2 children

If the parent is such that he will always name the boy, no information will be gained

Hand-wavy point:

My X is a boy
My boy is named X

✓
X

information
no-information