Table of Zernike Circular Polynomials

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Table 1: Zernike Circular Polynomials $\mathrm{Z}_j(\rho,\theta) = \mathrm{Z}_n^m(\rho,\theta)$

j	n	m	N_n^m	ZEMAX $\mathrm{Z}_j(\rho,\theta) = \mathrm{Z}_n^m(\rho,\theta) = \mathrm{R}_n^m(\rho)\Theta_m(\theta)$
1	0	0	$\sqrt{1}$	1
2	1	−1	$\sqrt{4}$	$\rho\cos(\theta)$
3	1	1	$\sqrt{4}$	$\rho\sin(\theta)$
4	2	0	$\sqrt{3}$	$2\rho^2-1$
5	2	−2	$\sqrt{6}$	$\rho^2\sin(2\theta)$
6	2	2	$\sqrt{6}$	$\rho^2\cos(2\theta)$
7	3	−1	$\sqrt{8}$	$(3\rho^3-2\rho)\sin(\theta)$
8	3	1	$\sqrt{8}$	$(3\rho^3-2\rho)\cos(\theta)$
9	3	−3	$\sqrt{8}$	$\rho^3\sin(3\theta)$
10	3	3	$\sqrt{8}$	$\rho^3\cos(3\theta)$
11	4	0	$\sqrt{5}$	$6\rho^4-6\rho^2+1$
12	4	−2	$\sqrt{10}$	$(4\rho^4-3\rho^2)\cos(2\theta)$
13	4	2	$\sqrt{10}$	$(4\rho^4-3\rho^2)\sin(2\theta)$
14	4	−4	$\sqrt{10}$	$\rho^4\cos(4\theta)$
15	4	4	$\sqrt{10}$	$\rho^4\sin(4\theta)$
16	5	−1	$\sqrt{12}$	$(10\rho^5-12\rho^3+3\rho)\cos(\theta)$
17	5	1	$\sqrt{12}$	$(10\rho^5-12\rho^3+3\rho)\sin(\theta)$
18	5	−3	$\sqrt{12}$	$(5\rho^5-4\rho^3)\cos(3\theta)$
19	5	3	$\sqrt{12}$	$(5\rho^5-4\rho^3)\sin(3\theta)$
20	5	−5	$\sqrt{12}$	$\rho^5\cos(5\theta)$
21	5	5	$\sqrt{12}$	$\rho^5\sin(5\theta)$
22	6	0	$\sqrt{7}$	$20\rho^6-30\rho^4+12\rho^2-1$
23	6	−2	$\sqrt{14}$	$(15\rho^6-20\rho^4+6\rho^2)\sin(2\theta)$
24	6	2	$\sqrt{14}$	$(15\rho^6-20\rho^4+6\rho^2)\cos(2\theta)$
25	6	−4	$\sqrt{14}$	$(6\rho^6-5\rho^4)\sin(4\theta)$
26	6	4	$\sqrt{14}$	$(6\rho^6-5\rho^4)\cos(4\theta)$
27	6	−6	$\sqrt{14}$	$\rho^6\sin(6\theta)$
28	6	6	$\sqrt{14}$	$\rho^6\cos(6\theta)$
29	7	−1	$\sqrt{16}$	$(35\rho^7-60\rho^5+30\rho^3-4\rho)\sin(\theta)$
30	7	1	$\sqrt{16}$	$(35\rho^7-60\rho^5+30\rho^3-4\rho)\cos(\theta)$
31	7	−3	$\sqrt{16}$	$(21\rho^7-30\rho^5+10\rho^3)\sin(3\theta)$
32	7	3	$\sqrt{16}$	$(21\rho^7-30\rho^5+10\rho^3)\cos(3\theta)$
33	7	−5	$\sqrt{16}$	$(7\rho^7-6\rho^5)\sin(5\theta)$
34	7	5	$\sqrt{16}$	$(7\rho^7-6\rho^5)\cos(5\theta)$
35	7	−7	$\sqrt{16}$	$\rho^7\sin(7\theta)$
36	7	7	$\sqrt{16}$	$\rho^7\cos(7\theta)$
37	8	0	$\sqrt{9}$	$70\rho^8-140\rho^6+90\rho^4-20\rho^2+1$
38	8	−2	$\sqrt{18}$	$(55\rho^8-105\rho^6+60\rho^4-10\rho^2)\cos(2\theta)$

Table 1: Zernike Circular Polynomials $\mathrm{Z}_j(\rho,\theta) = \mathrm{Z}_n^m(\rho,\theta)$(continued)

j	n	m	N_n^m	ZEMAX $\mathrm{Z}_j(\rho,\theta) = \mathrm{Z}_n^m(\rho,\theta) = \mathrm{R}_n^m(\rho)\Theta_m(\theta)$
39	8	2	$\sqrt{18}$	$(55\rho^8 - 105\rho^6 + 60\rho^4 - 10\rho^2)\sin(2\theta)$
40	8	−4	$\sqrt{18}$	$(28\rho^8 - 42\rho^6 + 15\rho^4)\cos(4\theta)$
41	8	4	$\sqrt{18}$	$(28\rho^8 - 42\rho^6 + 15\rho^4)\sin(4\theta)$
42	8	−6	$\sqrt{18}$	$(8\rho^8 - 7\rho^6)\cos(6\theta)$
43	8	6	$\sqrt{18}$	$(8\rho^8 - 7\rho^6)\sin(6\theta)$
44	8	−8	$\sqrt{18}$	$\rho^8\cos(8\theta)$
45	8	8	$\sqrt{18}$	$\rho^8\sin(8\theta)$
46	9	−1	$\sqrt{20}$	$(126\rho^9 - 280\rho^7 + 210\rho^5 - 60\rho^3 + 5\rho)\cos(\theta)$
47	9	1	$\sqrt{20}$	$(126\rho^9 - 280\rho^7 + 210\rho^5 - 60\rho^3 + 5\rho)\sin(\theta)$
48	9	−3	$\sqrt{20}$	$(84\rho^9 - 167\rho^7 + 105\rho^5 - 20\rho^3)\cos(3\theta)$
49	9	3	$\sqrt{20}$	$(84\rho^9 - 167\rho^7 + 105\rho^5 - 20\rho^3)\sin(3\theta)$
50	9	−5	$\sqrt{20}$	$(36\rho^9 - 56\rho^7 + 21\rho^5)\cos(5\theta)$
51	9	5	$\sqrt{20}$	$(36\rho^9 - 56\rho^7 + 21\rho^5)\sin(5\theta)$
52	9	−7	$\sqrt{20}$	$(9\rho^9 - 8\rho^7)\cos(7\theta)$
53	9	7	$\sqrt{20}$	$(9\rho^9 - 8\rho^7)\sin(7\theta)$
54	9	−9	$\sqrt{20}$	$\rho^9\cos(9\theta)$
55	9	9	$\sqrt{20}$	$\rho^9\sin(9\theta)$
56	10	0	$\sqrt{11}$	$252\rho^{10} - 630\rho^8 + 560\rho^6 - 209\rho^4 + 30\rho^2 - 1$
57	10	−2	$\sqrt{22}$	$(210\rho^{10} - 504\rho^8 + 420\rho^6 - 140\rho^4 + 15\rho^2)\sin(2\theta)$
58	10	2	$\sqrt{22}$	$(210\rho^{10} - 504\rho^8 + 420\rho^6 - 140\rho^4 + 15\rho^2)\cos(2\theta)$
59	10	−4	$\sqrt{22}$	$(120\rho^{10} - 252\rho^8 + 167\rho^6 - 35\rho^4)\sin(4\theta)$
60	10	4	$\sqrt{22}$	$(120\rho^{10} - 252\rho^8 + 167\rho^6 - 35\rho^4)\cos(4\theta)$
61	10	−6	$\sqrt{22}$	$(45\rho^{10} - 72\rho^8 + 28\rho^6)\sin(6\theta)$
62	10	6	$\sqrt{22}$	$(45\rho^{10} - 72\rho^8 + 28\rho^6)\cos(6\theta)$
63	10	−8	$\sqrt{22}$	$(10\rho^{10} - 9\rho^8)\sin(8\theta)$
64	10	8	$\sqrt{22}$	$(10\rho^{10} - 9\rho^8)\cos(8\theta)$
65	10	−10	$\sqrt{22}$	$\rho^{10}\sin(10\theta)$
66	10	10	$\sqrt{22}$	$\rho^{10}\cos(10\theta)$
67	11	−1	$\sqrt{24}$	$(462\rho^{11} - 1260\rho^9 + 1260\rho^7 - 560\rho^5 + 104\rho^3 - 6\rho)\sin(\theta)$
68	11	1	$\sqrt{24}$	$(462\rho^{11} - 1260\rho^9 + 1260\rho^7 - 560\rho^5 + 104\rho^3 - 6\rho)\cos(\theta)$
69	11	−3	$\sqrt{24}$	$(330\rho^{11} - 840\rho^9 + 756\rho^7 - 280\rho^5 + 35\rho^3)\sin(3\theta)$
70	11	3	$\sqrt{24}$	$(330\rho^{11} - 840\rho^9 + 756\rho^7 - 280\rho^5 + 35\rho^3)\cos(3\theta)$
71	11	−5	$\sqrt{24}$	$(165\rho^{11} - 360\rho^9 + 252\rho^7 - 55\rho^5)\sin(5\theta)$
72	11	5	$\sqrt{24}$	$(165\rho^{11} - 360\rho^9 + 252\rho^7 - 55\rho^5)\cos(5\theta)$
73	11	−7	$\sqrt{24}$	$(55\rho^{11} - 90\rho^9 + 36\rho^7)\sin(7\theta)$
74	11	7	$\sqrt{24}$	$(55\rho^{11} - 90\rho^9 + 36\rho^7)\cos(7\theta)$
75	11	−9	$\sqrt{24}$	$(11\rho^{11} - 10\rho^9)\sin(9\theta)$
76	11	9	$\sqrt{24}$	$(11\rho^{11} - 10\rho^9)\cos(9\theta)$
77	11	−11	$\sqrt{24}$	$\rho^{11}\sin(11\theta)$
78	11	11	$\sqrt{24}$	$\rho^{11}\cos(11\theta)$
79	12	0	$\sqrt{13}$	$924\rho^{12} - 2772\rho^{10} + 3150\rho^8 - 1680\rho^6 + 420\rho^4 - 42\rho^2 + 1$
80	12	−2	$\sqrt{26}$	$(792\rho^{12} - 2310\rho^{10} + 2520\rho^8 - 1260\rho^6 + 280\rho^4 - 20\rho^2)\cos(2\theta)$
81	12	2	$\sqrt{26}$	$(792\rho^{12} - 2310\rho^{10} + 2520\rho^8 - 1260\rho^6 + 280\rho^4 - 20\rho^2)\sin(2\theta)$
82	12	−4	$\sqrt{26}$	$(495\rho^{12} - 1320\rho^{10} + 1260\rho^8 - 504\rho^6 + 70\rho^4)\cos(4\theta)$
83	12	4	$\sqrt{26}$	$(495\rho^{12} - 1320\rho^{10} + 1260\rho^8 - 504\rho^6 + 70\rho^4)\sin(4\theta)$
84	12	−6	$\sqrt{26}$	$(220\rho^{12} - 495\rho^{10} + 360\rho^8 - 84\rho^6)\cos(6\theta)$
85	12	6	$\sqrt{26}$	$(220\rho^{12} - 495\rho^{10} + 360\rho^8 - 84\rho^6)\sin(6\theta)$
86	12	−8	$\sqrt{26}$	$(66\rho^{12} - 110\rho^{10} + 45\rho^8)\cos(8\theta)$

Table 1: Zernike Circular Polynomials $\mathrm{Z}_j(\rho,\theta) = \mathrm{Z}_n^m(\rho,\theta)$(continued)

j	n	m	N_n^m	ZEMAX $\mathrm{Z}_j(\rho,\theta) = \mathrm{Z}_n^m(\rho,\theta) = \mathrm{R}_n^m(\rho)\Theta_m(\theta)$
87	12	8	$\sqrt{26}$	$(66\rho^{12} - 110\rho^{10} + 45\rho^8)\sin(8\theta)$
88	12	−10	$\sqrt{26}$	$(12\rho^{12} - 11\rho^{10})\cos(10\theta)$
89	12	10	$\sqrt{26}$	$(12\rho^{12} - 11\rho^{10})\sin(10\theta)$
90	12	−12	$\sqrt{26}$	$\rho^{12}\cos(12\theta)$
91	12	12	$\sqrt{26}$	$\rho^{12}\sin(12\theta)$
92	13	−1	$\sqrt{28}$	$(1715\rho^{13} - 5544\rho^{11} + 6930\rho^9 - 4200\rho^7 + 1260\rho^5 - 168\rho^3 + 7\rho)\cos(\theta)$
93	13	1	$\sqrt{28}$	$(1715\rho^{13} - 5544\rho^{11} + 6930\rho^9 - 4200\rho^7 + 1260\rho^5 - 168\rho^3 + 7\rho)\sin(\theta)$
94	13	−3	$\sqrt{28}$	$(1287\rho^{13} - 3960\rho^{11} + 4620\rho^9 - 2520\rho^7 + 630\rho^5 - 56\rho^3)\cos(3\theta)$
95	13	3	$\sqrt{28}$	$(1287\rho^{13} - 3960\rho^{11} + 4620\rho^9 - 2520\rho^7 + 630\rho^5 - 56\rho^3)\sin(3\theta)$
96	13	−5	$\sqrt{28}$	$(715\rho^{13} - 1980\rho^{11} + 1980\rho^9 - 840\rho^7 + 126\rho^5)\cos(5\theta)$
97	13	5	$\sqrt{28}$	$(715\rho^{13} - 1980\rho^{11} + 1980\rho^9 - 840\rho^7 + 126\rho^5)\sin(5\theta)$
98	13	−7	$\sqrt{28}$	$(286\rho^{13} - 660\rho^{11} + 495\rho^9 - 120\rho^7)\cos(7\theta)$
99	13	7	$\sqrt{28}$	$(286\rho^{13} - 660\rho^{11} + 495\rho^9 - 120\rho^7)\sin(7\theta)$
100	13	−9	$\sqrt{28}$	$(78\rho^{13} - 132\rho^{11} + 55\rho^9)\cos(9\theta)$
101	13	9	$\sqrt{28}$	$(78\rho^{13} - 132\rho^{11} + 55\rho^9)\sin(9\theta)$
102	13	−11	$\sqrt{28}$	$(13\rho^{13} - 12\rho^{11})\cos(11\theta)$
103	13	11	$\sqrt{28}$	$(13\rho^{13} - 12\rho^{11})\sin(11\theta)$
104	13	−13	$\sqrt{28}$	$\rho^{13}\cos(13\theta)$
105	13	13	$\sqrt{28}$	$\rho^{13}\sin(13\theta)$
106	14	0	$\sqrt{15}$	$3431\rho^{14} - 12012\rho^{12} + 16631\rho^{10} - 11550\rho^8 + 4200\rho^6 - 755\rho^4 + 55\rho^2 - 1$
107	14	−2	$\sqrt{30}$	$(3003\rho^{14} - 10295\rho^{12} + 13860\rho^{10} - 9240\rho^8 + 3150\rho^6 - 504\rho^4 + 28\rho^2)\sin(2\theta)$
108	14	2	$\sqrt{30}$	$(3003\rho^{14} - 10295\rho^{12} + 13860\rho^{10} - 9240\rho^8 + 3150\rho^6 - 504\rho^4 + 28\rho^2)\cos(2\theta)$
109	14	−4	$\sqrt{30}$	$(2002\rho^{14} - 6435\rho^{12} + 7920\rho^{10} - 4620\rho^8 + 1260\rho^6 - 126\rho^4)\sin(4\theta)$
110	14	4	$\sqrt{30}$	$(2002\rho^{14} - 6435\rho^{12} + 7920\rho^{10} - 4620\rho^8 + 1260\rho^6 - 126\rho^4)\cos(4\theta)$
111	14	−6	$\sqrt{30}$	$(1001\rho^{14} - 2860\rho^{12} + 2970\rho^{10} - 1320\rho^8 + 210\rho^6)\sin(6\theta)$
112	14	6	$\sqrt{30}$	$(1001\rho^{14} - 2860\rho^{12} + 2970\rho^{10} - 1320\rho^8 + 210\rho^6)\cos(6\theta)$
113	14	−8	$\sqrt{30}$	$(364\rho^{14} - 858\rho^{12} + 660\rho^{10} - 165\rho^8)\sin(8\theta)$
114	14	8	$\sqrt{30}$	$(364\rho^{14} - 858\rho^{12} + 660\rho^{10} - 165\rho^8)\cos(8\theta)$
115	14	−10	$\sqrt{30}$	$(91\rho^{14} - 156\rho^{12} + 66\rho^{10})\sin(10\theta)$
116	14	10	$\sqrt{30}$	$(91\rho^{14} - 156\rho^{12} + 66\rho^{10})\cos(10\theta)$
117	14	−12	$\sqrt{30}$	$(14\rho^{14} - 13\rho^{12})\sin(12\theta)$
118	14	12	$\sqrt{30}$	$(14\rho^{14} - 13\rho^{12})\cos(12\theta)$
119	14	−14	$\sqrt{30}$	$\rho^{14}\sin(14\theta)$
120	14	14	$\sqrt{30}$	$\rho^{14}\cos(14\theta)$
121	15	−1	$\sqrt{32}$	$(6435\rho^{15} - 24023\rho^{13} + 36036\rho^{11} - 27719\rho^9 + 11550\rho^7 - 2519\rho^5 + 252\rho^3 - 7\rho)\sin(\theta)$
122	15	1	$\sqrt{32}$	$(6435\rho^{15} - 24023\rho^{13} + 36036\rho^{11} - 27719\rho^9 + 11550\rho^7 - 2519\rho^5 + 252\rho^3 - 7\rho)\cos(\theta)$
123	15	−3	$\sqrt{32}$	$(5005\rho^{15} - 18018\rho^{13} + 25739\rho^{11} - 18480\rho^9 + 6930\rho^7 - 1260\rho^5 + 84\rho^3)\sin(3\theta)$
124	15	3	$\sqrt{32}$	$(5005\rho^{15} - 18018\rho^{13} + 25739\rho^{11} - 18480\rho^9 + 6930\rho^7 - 1260\rho^5 + 84\rho^3)\cos(3\theta)$
125	15	−5	$\sqrt{32}$	$(3003\rho^{15} - 10010\rho^{13} + 12870\rho^{11} - 7920\rho^9 + 2310\rho^7 - 252\rho^5)\sin(5\theta)$
126	15	5	$\sqrt{32}$	$(3003\rho^{15} - 10010\rho^{13} + 12870\rho^{11} - 7920\rho^9 + 2310\rho^7 - 252\rho^5)\cos(5\theta)$
127	15	−7	$\sqrt{32}$	$(1365\rho^{15} - 4004\rho^{13} + 4290\rho^{11} - 1980\rho^9 + 330\rho^7)\sin(7\theta)$
128	15	7	$\sqrt{32}$	$(1365\rho^{15} - 4004\rho^{13} + 4290\rho^{11} - 1980\rho^9 + 330\rho^7)\cos(7\theta)$
129	15	−9	$\sqrt{32}$	$(455\rho^{15} - 1092\rho^{13} + 858\rho^{11} - 220\rho^9)\sin(9\theta)$
130	15	9	$\sqrt{32}$	$(455\rho^{15} - 1092\rho^{13} + 858\rho^{11} - 220\rho^9)\cos(9\theta)$
131	15	−11	$\sqrt{32}$	$(105\rho^{15} - 182\rho^{13} + 78\rho^{11})\sin(11\theta)$
132	15	11	$\sqrt{32}$	$(105\rho^{15} - 182\rho^{13} + 78\rho^{11})\cos(11\theta)$

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j	n	m	N_n^m	ZEMAX $\mathrm{Z}_j(\rho,\theta) = \mathrm{Z}_n^m(\rho,\theta) = \mathrm{R}_n^m(\rho)\Theta_m(\theta)$
133	15	−13	$\sqrt{32}$	$(15\rho^{15} - 14\rho^{13})\sin(13\theta)$
134	15	13	$\sqrt{32}$	$(15\rho^{15} - 14\rho^{13})\cos(13\theta)$
135	15	−15	$\sqrt{32}$	$\rho^{15}\sin(15\theta)$
136	15	15	$\sqrt{32}$	$\rho^{15}\cos(15\theta)$
137	16	0	$\sqrt{17}$	$12870\rho^{16} - 51480\rho^{14} + 84084\rho^{12} - 72071\rho^{10} + 34650\rho^8 - 9240\rho^6 + 1259\rho^4 - 71\rho^2 + 1$
138	16	−2	$\sqrt{34}$	$(11439\rho^{16} - 45045\rho^{14} + 72071\rho^{12} - 60060\rho^{10} + 27719\rho^8 - 6930\rho^6 + 840\rho^4 - 36\rho^2)\cos(2\theta)$
139	16	2	$\sqrt{34}$	$(11439\rho^{16} - 45045\rho^{14} + 72071\rho^{12} - 60060\rho^{10} + 27719\rho^8 - 6930\rho^6 + 840\rho^4 - 36\rho^2)\sin(2\theta)$
140	16	−4	$\sqrt{34}$	$(8008\rho^{16} - 30030\rho^{14} + 45045\rho^{12} - 34319\rho^{10} + 13860\rho^8 - 2772\rho^6 + 210\rho^4)\cos(4\theta)$
141	16	4	$\sqrt{34}$	$(8008\rho^{16} - 30030\rho^{14} + 45045\rho^{12} - 34319\rho^{10} + 13860\rho^8 - 2772\rho^6 + 210\rho^4)\sin(4\theta)$
142	16	−6	$\sqrt{34}$	$(4368\rho^{16} - 15015\rho^{14} + 20020\rho^{12} - 12870\rho^{10} + 3960\rho^8 - 462\rho^6)\cos(6\theta)$
143	16	6	$\sqrt{34}$	$(4368\rho^{16} - 15015\rho^{14} + 20020\rho^{12} - 12870\rho^{10} + 3960\rho^8 - 462\rho^6)\sin(6\theta)$
144	16	−8	$\sqrt{34}$	$(1820\rho^{16} - 5460\rho^{14} + 6006\rho^{12} - 2860\rho^{10} + 495\rho^8)\cos(8\theta)$
145	16	8	$\sqrt{34}$	$(1820\rho^{16} - 5460\rho^{14} + 6006\rho^{12} - 2860\rho^{10} + 495\rho^8)\sin(8\theta)$
146	16	−10	$\sqrt{34}$	$(560\rho^{16} - 1365\rho^{14} + 1092\rho^{12} - 286\rho^{10})\cos(10\theta)$
147	16	10	$\sqrt{34}$	$(560\rho^{16} - 1365\rho^{14} + 1092\rho^{12} - 286\rho^{10})\sin(10\theta)$
148	16	−12	$\sqrt{34}$	$(120\rho^{16} - 210\rho^{14} + 91\rho^{12})\cos(12\theta)$
149	16	12	$\sqrt{34}$	$(120\rho^{16} - 210\rho^{14} + 91\rho^{12})\sin(12\theta)$
150	16	−14	$\sqrt{34}$	$(16\rho^{16} - 15\rho^{14})\cos(14\theta)$
151	16	14	$\sqrt{34}$	$(16\rho^{16} - 15\rho^{14})\sin(14\theta)$
152	16	−16	$\sqrt{34}$	$\rho^{16}\cos(16\theta)$
153	16	16	$\sqrt{34}$	$\rho^{16}\sin(16\theta)$
154	17	−1	$\sqrt{36}$	$(24309\rho^{17} - 102960\rho^{15} + 180180\rho^{13} - 168167\rho^{11} + 90089\rho^9 - 27720\rho^7 + 4620\rho^5 - 359\rho^3 + 9\rho)\cos(\theta)$
155	17	1	$\sqrt{36}$	$(24309\rho^{17} - 102960\rho^{15} + 180180\rho^{13} - 168167\rho^{11} + 90089\rho^9 - 27720\rho^7 + 4620\rho^5 - 359\rho^3 + 9\rho)\sin(\theta)$
156	17	−3	$\sqrt{36}$	$(19447\rho^{17} - 80079\rho^{15} + 135135\rho^{13} - 120119\rho^{11} + 60060\rho^9 - 16631\rho^7 + 2310\rho^5 - 120\rho^3)\cos(3\theta)$
157	17	3	$\sqrt{36}$	$(19447\rho^{17} - 80079\rho^{15} + 135135\rho^{13} - 120119\rho^{11} + 60060\rho^9 - 16631\rho^7 + 2310\rho^5 - 120\rho^3)\sin(3\theta)$
158	17	−5	$\sqrt{36}$	$(12376\rho^{17} - 48048\rho^{15} + 75075\rho^{13} - 60060\rho^{11} + 25739\rho^9 - 5544\rho^7 + 462\rho^5)\cos(5\theta)$
159	17	5	$\sqrt{36}$	$(12376\rho^{17} - 48048\rho^{15} + 75075\rho^{13} - 60060\rho^{11} + 25739\rho^9 - 5544\rho^7 + 462\rho^5)\sin(5\theta)$
160	17	−7	$\sqrt{36}$	$(6188\rho^{17} - 21840\rho^{15} + 30030\rho^{13} - 20020\rho^{11} + 6435\rho^9 - 792\rho^7)\cos(7\theta)$
161	17	7	$\sqrt{36}$	$(6188\rho^{17} - 21840\rho^{15} + 30030\rho^{13} - 20020\rho^{11} + 6435\rho^9 - 792\rho^7)\sin(7\theta)$
162	17	−9	$\sqrt{36}$	$(2379\rho^{17} - 7280\rho^{15} + 8190\rho^{13} - 4004\rho^{11} + 715\rho^9)\cos(9\theta)$
163	17	9	$\sqrt{36}$	$(2379\rho^{17} - 7280\rho^{15} + 8190\rho^{13} - 4004\rho^{11} + 715\rho^9)\sin(9\theta)$
164	17	−11	$\sqrt{36}$	$(680\rho^{17} - 1680\rho^{15} + 1365\rho^{13} - 364\rho^{11})\cos(11\theta)$
165	17	11	$\sqrt{36}$	$(680\rho^{17} - 1680\rho^{15} + 1365\rho^{13} - 364\rho^{11})\sin(11\theta)$
166	17	−13	$\sqrt{36}$	$(136\rho^{17} - 240\rho^{15} + 105\rho^{13})\cos(13\theta)$
167	17	13	$\sqrt{36}$	$(136\rho^{17} - 240\rho^{15} + 105\rho^{13})\sin(13\theta)$
168	17	−15	$\sqrt{36}$	$(17\rho^{17} - 16\rho^{15})\cos(15\theta)$
169	17	15	$\sqrt{36}$	$(17\rho^{17} - 16\rho^{15})\sin(15\theta)$
170	17	−17	$\sqrt{36}$	$\rho^{17}\cos(17\theta)$
171	17	17	$\sqrt{36}$	$\rho^{17}\sin(17\theta)$
172	18	0	$\sqrt{19}$	$48619\rho^{18} - 218790\rho^{16} + 411840\rho^{14} - 420420\rho^{12} + 252251\rho^{10} - 90090\rho^8 + 18480\rho^6 - 1980\rho^4 + 89\rho^2 - 1$

Table 1: Zernike Circular Polynomials $\mathrm{Z}_j(\rho,\theta) = \mathrm{Z}_n^m(\rho,\theta)$(continued)

j	n	m	N_n^m	ZEMAX $\mathrm{Z}_j(\rho,\theta) = \mathrm{Z}_n^m(\rho,\theta) = \mathrm{R}_n^m(\rho)\Theta_m(\theta)$
173	18	-2	$\sqrt{38}$	$(43757\rho^{18} - 194479\rho^{16} + 360360\rho^{14} - 360359\rho^{12} + 210210\rho^{10} - 72072\rho^8 + 13860\rho^6 - 1319\rho^4 + 44\rho^2)\sin(2\theta)$
174	18	2	$\sqrt{38}$	$(43757\rho^{18} - 194479\rho^{16} + 360360\rho^{14} - 360359\rho^{12} + 210210\rho^{10} - 72072\rho^8 + 13860\rho^6 - 1319\rho^4 + 44\rho^2)\cos(2\theta)$
175	18	-4	$\sqrt{38}$	$(31824\rho^{18} - 136135\rho^{16} + 240239\rho^{14} - 225225\rho^{12} + 120119\rho^{10} - 36036\rho^8 + 5543\rho^6 - 330\rho^4)\sin(4\theta)$
176	18	4	$\sqrt{38}$	$(31824\rho^{18} - 136135\rho^{16} + 240239\rho^{14} - 225225\rho^{12} + 120119\rho^{10} - 36036\rho^8 + 5543\rho^6 - 330\rho^4)\cos(4\theta)$
177	18	-6	$\sqrt{38}$	$(18564\rho^{18} - 74256\rho^{16} + 120120\rho^{14} - 100100\rho^{12} + 45045\rho^{10} - 10295\rho^8 + 924\rho^6)\sin(6\theta)$
178	18	6	$\sqrt{38}$	$(18564\rho^{18} - 74256\rho^{16} + 120120\rho^{14} - 100100\rho^{12} + 45045\rho^{10} - 10295\rho^8 + 924\rho^6)\cos(6\theta)$
179	18	-8	$\sqrt{38}$	$(8568\rho^{18} - 30940\rho^{16} + 43680\rho^{14} - 30030\rho^{12} + 10010\rho^{10} - 1287\rho^8)\sin(8\theta)$
180	18	8	$\sqrt{38}$	$(8568\rho^{18} - 30940\rho^{16} + 43680\rho^{14} - 30030\rho^{12} + 10010\rho^{10} - 1287\rho^8)\cos(8\theta)$
181	18	-10	$\sqrt{38}$	$(3060\rho^{18} - 9519\rho^{16} + 10920\rho^{14} - 5460\rho^{12} + 1001\rho^{10})\sin(10\theta)$
182	18	10	$\sqrt{38}$	$(3060\rho^{18} - 9519\rho^{16} + 10920\rho^{14} - 5460\rho^{12} + 1001\rho^{10})\cos(10\theta)$
183	18	-12	$\sqrt{38}$	$(816\rho^{18} - 2040\rho^{16} + 1680\rho^{14} - 455\rho^{12})\sin(12\theta)$
184	18	12	$\sqrt{38}$	$(816\rho^{18} - 2040\rho^{16} + 1680\rho^{14} - 455\rho^{12})\cos(12\theta)$
185	18	-14	$\sqrt{38}$	$(153\rho^{18} - 272\rho^{16} + 120\rho^{14})\sin(14\theta)$
186	18	14	$\sqrt{38}$	$(153\rho^{18} - 272\rho^{16} + 120\rho^{14})\cos(14\theta)$
187	18	-16	$\sqrt{38}$	$(18\rho^{18} - 17\rho^{16})\sin(16\theta)$
188	18	16	$\sqrt{38}$	$(18\rho^{18} - 17\rho^{16})\cos(16\theta)$
189	18	-18	$\sqrt{38}$	$\rho^{18}\sin(18\theta)$
190	18	18	$\sqrt{38}$	$\rho^{18}\cos(18\theta)$
191	19	-1	$\sqrt{40}$	$(92378\rho^{19} - 437579\rho^{17} + 875160\rho^{15} - 960960\rho^{13} + 630630\rho^{11} - 252252\rho^9 + 60060\rho^7 - 7920\rho^5 + 495\rho^3 - 9\rho)\sin(\theta)$
192	19	1	$\sqrt{40}$	$(92378\rho^{19} - 437579\rho^{17} + 875160\rho^{15} - 960960\rho^{13} + 630630\rho^{11} - 252252\rho^9 + 60060\rho^7 - 7920\rho^5 + 495\rho^3 - 9\rho)\cos(\theta)$
193	19	-3	$\sqrt{40}$	$(75582\rho^{19} - 350063\rho^{17} + 680679\rho^{15} - 720719\rho^{13} + 450450\rho^{11} - 168168\rho^9 + 36035\rho^7 - 3960\rho^5 + 165\rho^3)\sin(3\theta)$
194	19	3	$\sqrt{40}$	$(75582\rho^{19} - 350063\rho^{17} + 680679\rho^{15} - 720719\rho^{13} + 450450\rho^{11} - 168168\rho^9 + 36035\rho^7 - 3960\rho^5 + 165\rho^3)\cos(3\theta)$
195	19	-5	$\sqrt{40}$	$(50387\rho^{19} - 222768\rho^{17} + 408407\rho^{15} - 400399\rho^{13} + 225225\rho^{11} - 72071\rho^9 + 12012\rho^7 - 791\rho^5)\sin(5\theta)$
196	19	5	$\sqrt{40}$	$(50387\rho^{19} - 222768\rho^{17} + 408407\rho^{15} - 400399\rho^{13} + 225225\rho^{11} - 72071\rho^9 + 12012\rho^7 - 791\rho^5)\cos(5\theta)$
197	19	-7	$\sqrt{40}$	$(27131\rho^{19} - 111384\rho^{17} + 185640\rho^{15} - 160160\rho^{13} + 75075\rho^{11} - 18018\rho^9 + 1715\rho^7)\sin(7\theta)$
198	19	7	$\sqrt{40}$	$(27131\rho^{19} - 111384\rho^{17} + 185640\rho^{15} - 160160\rho^{13} + 75075\rho^{11} - 18018\rho^9 + 1715\rho^7)\cos(7\theta)$
199	19	-9	$\sqrt{40}$	$(11627\rho^{19} - 42840\rho^{17} + 61880\rho^{15} - 43680\rho^{13} + 15015\rho^{11} - 2002\rho^9)\sin(9\theta)$
200	19	9	$\sqrt{40}$	$(11627\rho^{19} - 42840\rho^{17} + 61880\rho^{15} - 43680\rho^{13} + 15015\rho^{11} - 2002\rho^9)\cos(9\theta)$
201	19	-11	$\sqrt{40}$	$(3876\rho^{19} - 12240\rho^{17} + 14279\rho^{15} - 7280\rho^{13} + 1365\rho^{11})\sin(11\theta)$
202	19	11	$\sqrt{40}$	$(3876\rho^{19} - 12240\rho^{17} + 14279\rho^{15} - 7280\rho^{13} + 1365\rho^{11})\cos(11\theta)$
203	19	-13	$\sqrt{40}$	$(969\rho^{19} - 2448\rho^{17} + 2040\rho^{15} - 560\rho^{13})\sin(13\theta)$
204	19	13	$\sqrt{40}$	$(969\rho^{19} - 2448\rho^{17} + 2040\rho^{15} - 560\rho^{13})\cos(13\theta)$
205	19	-15	$\sqrt{40}$	$(171\rho^{19} - 306\rho^{17} + 136\rho^{15})\sin(15\theta)$
206	19	15	$\sqrt{40}$	$(171\rho^{19} - 306\rho^{17} + 136\rho^{15})\cos(15\theta)$
207	19	-17	$\sqrt{40}$	$(19\rho^{19} - 18\rho^{17})\sin(17\theta)$

Table 1: Zernike Circular Polynomials $\mathrm{Z}_j(\rho,\theta) = \mathrm{Z}_n^m(\rho,\theta)$(continued)

j	n	m	N_n^m	ZEMAX $\mathrm{Z}_j(\rho,\theta) = \mathrm{Z}_n^m(\rho,\theta) = \mathrm{R}_n^m(\rho)\Theta_m(\theta)$
208	19	17	$\sqrt{40}$	$(19\rho^{19} - 18\rho^{17})\cos(17\theta)$
209	19	−19	$\sqrt{40}$	$\rho^{19}\sin(19\theta)$
210	19	19	$\sqrt{40}$	$\rho^{19}\cos(19\theta)$
211	20	0	$\sqrt{21}$	$184756\rho^{20} - 923780\rho^{18} + 1969110\rho^{16} - 2333759\rho^{14} + 1681680\rho^{12} - 756756\rho^{10} + 210210\rho^8 - 34320\rho^6 + 2970\rho^4 - 109\rho^2 + 1$
212	20	−2	$\sqrt{42}$	$(167960\rho^{20} - 831402\rho^{18} + 1750319\rho^{16} - 2042040\rho^{14} + 1441440\rho^{12} - 630630\rho^{10} + 168168\rho^8 - 25740\rho^6 + 1980\rho^4 - 55\rho^2)\cos(2\theta)$
213	20	2	$\sqrt{42}$	$(167960\rho^{20} - 831402\rho^{18} + 1750319\rho^{16} - 2042040\rho^{14} + 1441440\rho^{12} - 630630\rho^{10} + 168168\rho^8 - 25740\rho^6 + 1980\rho^4 - 55\rho^2)\sin(2\theta)$
214	20	−4	$\sqrt{42}$	$(125970\rho^{20} - 604656\rho^{18} + 1225223\rho^{16} - 1361359\rho^{14} + 900900\rho^{12} - 360360\rho^{10} + 84084\rho^8 - 10295\rho^6 + 495\rho^4)\cos(4\theta)$
215	20	4	$\sqrt{42}$	$(125970\rho^{20} - 604656\rho^{18} + 1225223\rho^{16} - 1361359\rho^{14} + 900900\rho^{12} - 360360\rho^{10} + 84084\rho^8 - 10295\rho^6 + 495\rho^4)\sin(4\theta)$
216	20	−6	$\sqrt{42}$	$(77520\rho^{20} - 352715\rho^{18} + 668304\rho^{16} - 680679\rho^{14} + 400399\rho^{12} - 135134\rho^{10} + 24023\rho^8 - 1716\rho^6)\cos(6\theta)$
217	20	6	$\sqrt{42}$	$(77520\rho^{20} - 352715\rho^{18} + 668304\rho^{16} - 680679\rho^{14} + 400399\rho^{12} - 135134\rho^{10} + 24023\rho^8 - 1716\rho^6)\sin(6\theta)$
218	20	−8	$\sqrt{42}$	$(38760\rho^{20} - 162791\rho^{18} + 278460\rho^{16} - 247520\rho^{14} + 120120\rho^{12} - 30030\rho^{10} + 3003\rho^8)\cos(8\theta)$
219	20	8	$\sqrt{42}$	$(38760\rho^{20} - 162791\rho^{18} + 278460\rho^{16} - 247520\rho^{14} + 120120\rho^{12} - 30030\rho^{10} + 3003\rho^8)\sin(8\theta)$
220	20	−10	$\sqrt{42}$	$(15504\rho^{20} - 58139\rho^{18} + 85680\rho^{16} - 61880\rho^{14} + 21840\rho^{12} - 3003\rho^{10})\cos(10\theta)$
221	20	10	$\sqrt{42}$	$(15504\rho^{20} - 58139\rho^{18} + 85680\rho^{16} - 61880\rho^{14} + 21840\rho^{12} - 3003\rho^{10})\sin(10\theta)$
222	20	−12	$\sqrt{42}$	$(4845\rho^{20} - 15504\rho^{18} + 18360\rho^{16} - 9519\rho^{14} + 1820\rho^{12})\cos(12\theta)$
223	20	12	$\sqrt{42}$	$(4845\rho^{20} - 15504\rho^{18} + 18360\rho^{16} - 9519\rho^{14} + 1820\rho^{12})\sin(12\theta)$
224	20	−14	$\sqrt{42}$	$(1140\rho^{20} - 2907\rho^{18} + 2448\rho^{16} - 680\rho^{14})\cos(14\theta)$
225	20	14	$\sqrt{42}$	$(1140\rho^{20} - 2907\rho^{18} + 2448\rho^{16} - 680\rho^{14})\sin(14\theta)$
226	20	−16	$\sqrt{42}$	$(190\rho^{20} - 342\rho^{18} + 153\rho^{16})\cos(16\theta)$
227	20	16	$\sqrt{42}$	$(190\rho^{20} - 342\rho^{18} + 153\rho^{16})\sin(16\theta)$
228	20	−18	$\sqrt{42}$	$(20\rho^{20} - 19\rho^{18})\cos(18\theta)$
229	20	18	$\sqrt{42}$	$(20\rho^{20} - 19\rho^{18})\sin(18\theta)$
230	20	−20	$\sqrt{42}$	$\rho^{20}\cos(20\theta)$
231	20	20	$\sqrt{42}$	$\rho^{20}\sin(20\theta)$
232	21	−1	$\sqrt{44}$	$(352716\rho^{21} - 1847560\rho^{19} + 4157010\rho^{17} - 5250960\rho^{15} + 4084079\rho^{13} - 2018016\rho^{11} + 630630\rho^9 - 120120\rho^7 + 12869\rho^5 - 660\rho^3 + 11\rho)\cos(\theta)$
233	21	1	$\sqrt{44}$	$(352716\rho^{21} - 1847560\rho^{19} + 4157010\rho^{17} - 5250960\rho^{15} + 4084079\rho^{13} - 2018016\rho^{11} + 630630\rho^9 - 120120\rho^7 + 12869\rho^5 - 660\rho^3 + 11\rho)\sin(\theta)$
234	21	−3	$\sqrt{44}$	$(293930\rho^{21} - 1511640\rho^{19} + 3325608\rho^{17} - 4084079\rho^{15} + 3063060\rho^{13} - 1441440\rho^{11} + 420420\rho^9 - 72071\rho^7 + 6435\rho^5 - 220\rho^3)\cos(3\theta)$
235	21	3	$\sqrt{44}$	$(293930\rho^{21} - 1511640\rho^{19} + 3325608\rho^{17} - 4084079\rho^{15} + 3063060\rho^{13} - 1441440\rho^{11} + 420420\rho^9 - 72071\rho^7 + 6435\rho^5 - 220\rho^3)\sin(3\theta)$
236	21	−5	$\sqrt{44}$	$(203490\rho^{21} - 1007760\rho^{19} + 2116296\rho^{17} - 2450447\rho^{15} + 1701699\rho^{13} - 720720\rho^{11} + 180180\rho^9 - 24023\rho^7 + 1286\rho^5)\cos(5\theta)$
237	21	5	$\sqrt{44}$	$(203490\rho^{21} - 1007760\rho^{19} + 2116296\rho^{17} - 2450447\rho^{15} + 1701699\rho^{13} - 720720\rho^{11} + 180180\rho^9 - 24023\rho^7 + 1286\rho^5)\sin(5\theta)$
238	21	−7	$\sqrt{44}$	$(116280\rho^{21} - 542640\rho^{19} + 1058147\rho^{17} - 1113840\rho^{15} + 680679\rho^{13} - 240239\rho^{11} + 45045\rho^9 - 3431\rho^7)\cos(7\theta)$
239	21	7	$\sqrt{44}$	$(116280\rho^{21} - 542640\rho^{19} + 1058147\rho^{17} - 1113840\rho^{15} + 680679\rho^{13} - 240239\rho^{11} + 45045\rho^9 - 3431\rho^7)\sin(7\theta)$

Table 1: Zernike Circular Polynomials $\mathrm{Z}_j(\rho,\theta) = \mathrm{Z}_n^m(\rho,\theta)$(continued)

j	n	m	N_n^m	ZEMAX $\mathrm{Z}_j(\rho,\theta) = \mathrm{Z}_n^m(\rho,\theta) = \mathrm{R}_n^m(\rho)\Theta_m(\theta)$
240	21	-9	$\sqrt{44}$	$(54264\rho^{21} - 232560\rho^{19} + 406979\rho^{17} - 371280\rho^{15} + 185640\rho^{13} - 48048\rho^{11} + 5005\rho^9)\cos(9\theta)$
241	21	9	$\sqrt{44}$	$(54264\rho^{21} - 232560\rho^{19} + 406979\rho^{17} - 371280\rho^{15} + 185640\rho^{13} - 48048\rho^{11} + 5005\rho^9)\sin(9\theta)$
242	21	-11	$\sqrt{44}$	$(20349\rho^{21} - 77520\rho^{19} + 116279\rho^{17} - 85680\rho^{15} + 30940\rho^{13} - 4368\rho^{11})\cos(11\theta)$
243	21	11	$\sqrt{44}$	$(20349\rho^{21} - 77520\rho^{19} + 116279\rho^{17} - 85680\rho^{15} + 30940\rho^{13} - 4368\rho^{11})\sin(11\theta)$
244	21	-13	$\sqrt{44}$	$(5985\rho^{21} - 19380\rho^{19} + 23256\rho^{17} - 12240\rho^{15} + 2379\rho^{13})\cos(13\theta)$
245	21	13	$\sqrt{44}$	$(5985\rho^{21} - 19380\rho^{19} + 23256\rho^{17} - 12240\rho^{15} + 2379\rho^{13})\sin(13\theta)$
246	21	-15	$\sqrt{44}$	$(1330\rho^{21} - 3420\rho^{19} + 2907\rho^{17} - 816\rho^{15})\cos(15\theta)$
247	21	15	$\sqrt{44}$	$(1330\rho^{21} - 3420\rho^{19} + 2907\rho^{17} - 816\rho^{15})\sin(15\theta)$
248	21	-17	$\sqrt{44}$	$(210\rho^{21} - 380\rho^{19} + 171\rho^{17})\cos(17\theta)$
249	21	17	$\sqrt{44}$	$(210\rho^{21} - 380\rho^{19} + 171\rho^{17})\sin(17\theta)$
250	21	-19	$\sqrt{44}$	$(21\rho^{21} - 20\rho^{19})\cos(19\theta)$
251	21	19	$\sqrt{44}$	$(21\rho^{21} - 20\rho^{19})\sin(19\theta)$
252	21	-21	$\sqrt{44}$	$\rho^{21}\cos(21\theta)$
253	21	21	$\sqrt{44}$	$\rho^{21}\sin(21\theta)$
254	22	0	$\sqrt{23}$	$705432\rho^{22} - 3879875\rho^{20} + 9237799\rho^{18} - 12471030\rho^{16} + 10501920\rho^{14} - 5717712\rho^{12} + 2018015\rho^{10} - 450449\rho^8 + 60060\rho^6 - 4290\rho^4 + 132\rho^2 - 1$
255	22	-2	$\sqrt{46}$	$(646646\rho^{22} - 3527160\rho^{20} + 8314020\rho^{18} - 11085360\rho^{16} + 9189180\rho^{14} - 4900895\rho^{12} + 1681680\rho^{10} - 360360\rho^8 + 45044\rho^6 - 2859\rho^4 + 66\rho^2)\sin(2\theta)$
256	22	2	$\sqrt{46}$	$(646646\rho^{22} - 3527160\rho^{20} + 8314020\rho^{18} - 11085360\rho^{16} + 9189180\rho^{14} - 4900895\rho^{12} + 1681680\rho^{10} - 360360\rho^8 + 45044\rho^6 - 2859\rho^4 + 66\rho^2)\cos(2\theta)$
257	22	-4	$\sqrt{46}$	$(497420\rho^{22} - 2645370\rho^{20} + 6046560\rho^{18} - 7759752\rho^{16} + 6126119\rho^{14} - 3063060\rho^{12} + 960960\rho^{10} - 180180\rho^8 + 18017\rho^6 - 715\rho^4)\sin(4\theta)$
258	22	4	$\sqrt{46}$	$(497420\rho^{22} - 2645370\rho^{20} + 6046560\rho^{18} - 7759752\rho^{16} + 6126119\rho^{14} - 3063060\rho^{12} + 960960\rho^{10} - 180180\rho^8 + 18017\rho^6 - 715\rho^4)\cos(4\theta)$
259	22	-6	$\sqrt{46}$	$(319770\rho^{22} - 1627920\rho^{20} + 3527160\rho^{18} - 4232592\rho^{16} + 3063059\rho^{14} - 1361360\rho^{12} + 360360\rho^{10} - 51479\rho^8 + 3003\rho^6)\sin(6\theta)$
260	22	6	$\sqrt{46}$	$(319770\rho^{22} - 1627920\rho^{20} + 3527160\rho^{18} - 4232592\rho^{16} + 3063059\rho^{14} - 1361360\rho^{12} + 360360\rho^{10} - 51479\rho^8 + 3003\rho^6)\cos(6\theta)$
261	22	-8	$\sqrt{46}$	$(170544\rho^{22} - 813960\rho^{20} + 1627920\rho^{18} - 1763579\rho^{16} + 1113840\rho^{14} - 408407\rho^{12} + 80079\rho^{10} - 6435\rho^8)\sin(8\theta)$
262	22	8	$\sqrt{46}$	$(170544\rho^{22} - 813960\rho^{20} + 1627920\rho^{18} - 1763579\rho^{16} + 1113840\rho^{14} - 408407\rho^{12} + 80079\rho^{10} - 6435\rho^8)\cos(8\theta)$
263	22	-10	$\sqrt{46}$	$(74613\rho^{22} - 325584\rho^{20} + 581400\rho^{18} - 542639\rho^{16} + 278460\rho^{14} - 74256\rho^{12} + 8008\rho^{10})\sin(10\theta)$
264	22	10	$\sqrt{46}$	$(74613\rho^{22} - 325584\rho^{20} + 581400\rho^{18} - 542639\rho^{16} + 278460\rho^{14} - 74256\rho^{12} + 8008\rho^{10})\cos(10\theta)$
265	22	-12	$\sqrt{46}$	$(26334\rho^{22} - 101745\rho^{20} + 155040\rho^{18} - 116279\rho^{16} + 42840\rho^{14} - 6188\rho^{12})\sin(12\theta)$
266	22	12	$\sqrt{46}$	$(26334\rho^{22} - 101745\rho^{20} + 155040\rho^{18} - 116279\rho^{16} + 42840\rho^{14} - 6188\rho^{12})\cos(12\theta)$
267	22	-14	$\sqrt{46}$	$(7315\rho^{22} - 23940\rho^{20} + 29070\rho^{18} - 15504\rho^{16} + 3060\rho^{14})\sin(14\theta)$
268	22	14	$\sqrt{46}$	$(7315\rho^{22} - 23940\rho^{20} + 29070\rho^{18} - 15504\rho^{16} + 3060\rho^{14})\cos(14\theta)$
269	22	-16	$\sqrt{46}$	$(1540\rho^{22} - 3990\rho^{20} + 3420\rho^{18} - 969\rho^{16})\sin(16\theta)$
270	22	16	$\sqrt{46}$	$(1540\rho^{22} - 3990\rho^{20} + 3420\rho^{18} - 969\rho^{16})\cos(16\theta)$
271	22	-18	$\sqrt{46}$	$(231\rho^{22} - 420\rho^{20} + 190\rho^{18})\sin(18\theta)$
272	22	18	$\sqrt{46}$	$(231\rho^{22} - 420\rho^{20} + 190\rho^{18})\cos(18\theta)$
273	22	-20	$\sqrt{46}$	$(22\rho^{22} - 21\rho^{20})\sin(20\theta)$
274	22	20	$\sqrt{46}$	$(22\rho^{22} - 21\rho^{20})\cos(20\theta)$

Table 1: Zernike Circular Polynomials $\mathrm{Z}_j(\rho,\theta) = \mathrm{Z}_n^m(\rho,\theta)$(continued)

j	n	m	N_n^m	ZEMAX $\mathrm{Z}_j(\rho,\theta) = \mathrm{Z}_n^m(\rho,\theta) = \mathrm{R}_n^m(\rho)\Theta_m(\theta)$
275	22	−22	$\sqrt{46}$	$\rho^{22}\sin(22\theta)$
276	22	22	$\sqrt{46}$	$\rho^{22}\cos(22\theta)$
277	23	−1	$\sqrt{48}$	$(1352078\rho^{23} - 7759752\rho^{21} + 19399379\rho^{19} - 27713399\rho^{17} + 24942060\rho^{15} - 14702688\rho^{13} + 5717712\rho^{11} - 1441439\rho^9 + 225224\rho^7 - 20020\rho^5 + 858\rho^3 - 12\rho)\sin(\theta)$
278	23	1	$\sqrt{48}$	$(1352078\rho^{23} - 7759752\rho^{21} + 19399379\rho^{19} - 27713399\rho^{17} + 24942060\rho^{15} - 14702688\rho^{13} + 5717712\rho^{11} - 1441439\rho^9 + 225224\rho^7 - 20020\rho^5 + 858\rho^3 - 12\rho)\cos(\theta)$
279	23	−3	$\sqrt{48}$	$(1144066\rho^{23} - 6466460\rho^{21} + 15872220\rho^{19} - 22170720\rho^{17} + 19399380\rho^{15} - 11027016\rho^{13} + 4084079\rho^{11} - 960960\rho^9 + 135134\rho^7 - 10009\rho^5 + 286\rho^3)\sin(3\theta)$
280	23	3	$\sqrt{48}$	$(1144066\rho^{23} - 6466460\rho^{21} + 15872220\rho^{19} - 22170720\rho^{17} + 19399380\rho^{15} - 11027016\rho^{13} + 4084079\rho^{11} - 960960\rho^9 + 135134\rho^7 - 10009\rho^5 + 286\rho^3)\cos(3\theta)$
281	23	−5	$\sqrt{48}$	$(817190\rho^{23} - 4476780\rho^{21} + 10581480\rho^{19} - 14108640\rho^{17} + 11639628\rho^{15} - 6126120\rho^{13} + 2042040\rho^{11} - 411840\rho^9 + 45045\rho^7 - 2001\rho^5)\sin(5\theta)$
282	23	5	$\sqrt{48}$	$(817190\rho^{23} - 4476780\rho^{21} + 10581480\rho^{19} - 14108640\rho^{17} + 11639628\rho^{15} - 6126120\rho^{13} + 2042040\rho^{11} - 411840\rho^9 + 45045\rho^7 - 2001\rho^5)\cos(5\theta)$
283	23	−7	$\sqrt{48}$	$(490313\rho^{23} - 2558160\rho^{21} + 5697720\rho^{19} - 7054320\rho^{17} + 5290740\rho^{15} - 2450448\rho^{13} + 680679\rho^{11} - 102959\rho^9 + 6435\rho^7)\sin(7\theta)$
284	23	7	$\sqrt{48}$	$(490313\rho^{23} - 2558160\rho^{21} + 5697720\rho^{19} - 7054320\rho^{17} + 5290740\rho^{15} - 2450448\rho^{13} + 680679\rho^{11} - 102959\rho^9 + 6435\rho^7)\cos(7\theta)$
285	23	−9	$\sqrt{48}$	$(245157\rho^{23} - 1193808\rho^{21} + 2441880\rho^{19} - 2713200\rho^{17} + 1763579\rho^{15} - 668304\rho^{13} + 136135\rho^{11} - 11439\rho^9)\sin(9\theta)$
286	23	9	$\sqrt{48}$	$(245157\rho^{23} - 1193808\rho^{21} + 2441880\rho^{19} - 2713200\rho^{17} + 1763579\rho^{15} - 668304\rho^{13} + 136135\rho^{11} - 11439\rho^9)\cos(9\theta)$
287	23	−11	$\sqrt{48}$	$(100947\rho^{23} - 447678\rho^{21} + 813960\rho^{19} - 775200\rho^{17} + 406979\rho^{15} - 111384\rho^{13} + 12376\rho^{11})\sin(11\theta)$
288	23	11	$\sqrt{48}$	$(100947\rho^{23} - 447678\rho^{21} + 813960\rho^{19} - 775200\rho^{17} + 406979\rho^{15} - 111384\rho^{13} + 12376\rho^{11})\cos(11\theta)$
289	23	−13	$\sqrt{48}$	$(33648\rho^{23} - 131670\rho^{21} + 203490\rho^{19} - 155040\rho^{17} + 58139\rho^{15} - 8568\rho^{13})\sin(13\theta)$
290	23	13	$\sqrt{48}$	$(33648\rho^{23} - 131670\rho^{21} + 203490\rho^{19} - 155040\rho^{17} + 58139\rho^{15} - 8568\rho^{13})\cos(13\theta)$
291	23	−15	$\sqrt{48}$	$(8855\rho^{23} - 29260\rho^{21} + 35910\rho^{19} - 19380\rho^{17} + 3876\rho^{15})\sin(15\theta)$
292	23	15	$\sqrt{48}$	$(8855\rho^{23} - 29260\rho^{21} + 35910\rho^{19} - 19380\rho^{17} + 3876\rho^{15})\cos(15\theta)$
293	23	−17	$\sqrt{48}$	$(1771\rho^{23} - 4620\rho^{21} + 3990\rho^{19} - 1140\rho^{17})\sin(17\theta)$
294	23	17	$\sqrt{48}$	$(1771\rho^{23} - 4620\rho^{21} + 3990\rho^{19} - 1140\rho^{17})\cos(17\theta)$
295	23	−19	$\sqrt{48}$	$(253\rho^{23} - 462\rho^{21} + 210\rho^{19})\sin(19\theta)$
296	23	19	$\sqrt{48}$	$(253\rho^{23} - 462\rho^{21} + 210\rho^{19})\cos(19\theta)$
297	23	−21	$\sqrt{48}$	$(23\rho^{23} - 22\rho^{21})\sin(21\theta)$
298	23	21	$\sqrt{48}$	$(23\rho^{23} - 22\rho^{21})\cos(21\theta)$
299	23	−23	$\sqrt{48}$	$\rho^{23}\sin(23\theta)$
300	23	23	$\sqrt{48}$	$\rho^{23}\cos(23\theta)$
301	24	0	$\sqrt{25}$	$2704156\rho^{24} - 16224936\rho^{22} + 42678636\rho^{20} - 64664600\rho^{18} + 62355150\rho^{16} - 39907295\rho^{14} + 17153136\rho^{12} - 4900895\rho^{10} + 900900\rho^8 - 100100\rho^6 + 6006\rho^4 - 155\rho^2 + 1$
302	24	−2	$\sqrt{50}$	$(2496143\rho^{24} - 14872858\rho^{22} + 38798760\rho^{20} - 58198139\rho^{18} + 55426800\rho^{16} - 34918884\rho^{14} + 14702688\rho^{12} - 4084080\rho^{10} + 720719\rho^8 - 75074\rho^6 + 4004\rho^4 - 78\rho^2)\cos(2\theta)$
303	24	2	$\sqrt{50}$	$(2496143\rho^{24} - 14872858\rho^{22} + 38798760\rho^{20} - 58198139\rho^{18} + 55426800\rho^{16} - 34918884\rho^{14} + 14702688\rho^{12} - 4084080\rho^{10} + 720719\rho^8 - 75074\rho^6 + 4004\rho^4 - 78\rho^2)\sin(2\theta)$

Table 1: Zernike Circular Polynomials $\mathrm{Z}_j(\rho,\theta) = \mathrm{Z}_n^m(\rho,\theta)$(continued)

j	n	m	N_n^m	ZEMAX $\mathrm{Z}_j(\rho,\theta) = \mathrm{Z}_n^m(\rho,\theta) = \mathrm{R}_n^m(\rho)\Theta_m(\theta)$
304	24	-4	$\sqrt{50}$	$(1961256\rho^{24} - 11440660\rho^{22} + 29099070\rho^{20} - 42325920\rho^{18} + 38798760\rho^{16} - 23279256\rho^{14} + 9189180\rho^{12} - 2333759\rho^{10} + 360359\rho^8 - 30029\rho^6 + 1001\rho^4)\cos(4\theta)$
305	24	4	$\sqrt{50}$	$(1961256\rho^{24} - 11440660\rho^{22} + 29099070\rho^{20} - 42325920\rho^{18} + 38798760\rho^{16} - 23279256\rho^{14} + 9189180\rho^{12} - 2333759\rho^{10} + 360359\rho^8 - 30029\rho^6 + 1001\rho^4)\sin(4\theta)$
306	24	-6	$\sqrt{50}$	$(1307503\rho^{24} - 7354710\rho^{22} + 17907120\rho^{20} - 24690120\rho^{18} + 21162960\rho^{16} - 11639628\rho^{14} + 4084080\rho^{12} - 875160\rho^{10} + 102960\rho^8 - 5005\rho^6)\cos(6\theta)$
307	24	6	$\sqrt{50}$	$(1307503\rho^{24} - 7354710\rho^{22} + 17907120\rho^{20} - 24690120\rho^{18} + 21162960\rho^{16} - 11639628\rho^{14} + 4084080\rho^{12} - 875160\rho^{10} + 102960\rho^8 - 5005\rho^6)\sin(6\theta)$
308	24	-8	$\sqrt{50}$	$(735471\rho^{24} - 3922511\rho^{22} + 8953560\rho^{20} - 11395439\rho^{18} + 8817900\rho^{16} - 4232592\rho^{14} + 1225223\rho^{12} - 194479\rho^{10} + 12870\rho^8)\cos(8\theta)$
309	24	8	$\sqrt{50}$	$(735471\rho^{24} - 3922511\rho^{22} + 8953560\rho^{20} - 11395439\rho^{18} + 8817900\rho^{16} - 4232592\rho^{14} + 1225223\rho^{12} - 194479\rho^{10} + 12870\rho^8)\sin(8\theta)$
310	24	-10	$\sqrt{50}$	$(346104\rho^{24} - 1716099\rho^{22} + 3581424\rho^{20} - 4069800\rho^{18} + 2713200\rho^{16} - 1058147\rho^{14} + 222768\rho^{12} - 19447\rho^{10})\cos(10\theta)$
311	24	10	$\sqrt{50}$	$(346104\rho^{24} - 1716099\rho^{22} + 3581424\rho^{20} - 4069800\rho^{18} + 2713200\rho^{16} - 1058147\rho^{14} + 222768\rho^{12} - 19447\rho^{10})\sin(10\theta)$
312	24	-12	$\sqrt{50}$	$(134595\rho^{24} - 605682\rho^{22} + 1119195\rho^{20} - 1085280\rho^{18} + 581400\rho^{16} - 162791\rho^{14} + 18564\rho^{12})\cos(12\theta)$
313	24	12	$\sqrt{50}$	$(134595\rho^{24} - 605682\rho^{22} + 1119195\rho^{20} - 1085280\rho^{18} + 581400\rho^{16} - 162791\rho^{14} + 18564\rho^{12})\sin(12\theta)$
314	24	-14	$\sqrt{50}$	$(42504\rho^{24} - 168244\rho^{22} + 263340\rho^{20} - 203490\rho^{18} + 77520\rho^{16} - 11627\rho^{14})\cos(14\theta)$
315	24	14	$\sqrt{50}$	$(42504\rho^{24} - 168244\rho^{22} + 263340\rho^{20} - 203490\rho^{18} + 77520\rho^{16} - 11627\rho^{14})\sin(14\theta)$
316	24	-16	$\sqrt{50}$	$(10626\rho^{24} - 35420\rho^{22} + 43890\rho^{20} - 23940\rho^{18} + 4845\rho^{16})\cos(16\theta)$
317	24	16	$\sqrt{50}$	$(10626\rho^{24} - 35420\rho^{22} + 43890\rho^{20} - 23940\rho^{18} + 4845\rho^{16})\sin(16\theta)$
318	24	-18	$\sqrt{50}$	$(2024\rho^{24} - 5313\rho^{22} + 4620\rho^{20} - 1330\rho^{18})\cos(18\theta)$
319	24	18	$\sqrt{50}$	$(2024\rho^{24} - 5313\rho^{22} + 4620\rho^{20} - 1330\rho^{18})\sin(18\theta)$
320	24	-20	$\sqrt{50}$	$(276\rho^{24} - 506\rho^{22} + 231\rho^{20})\cos(20\theta)$
321	24	20	$\sqrt{50}$	$(276\rho^{24} - 506\rho^{22} + 231\rho^{20})\sin(20\theta)$
322	24	-22	$\sqrt{50}$	$(24\rho^{24} - 23\rho^{22})\cos(22\theta)$
323	24	22	$\sqrt{50}$	$(24\rho^{24} - 23\rho^{22})\sin(22\theta)$
324	24	-24	$\sqrt{50}$	$\rho^{24}\cos(24\theta)$
325	24	24	$\sqrt{50}$	$\rho^{24}\sin(24\theta)$
326	25	-1	$\sqrt{52}$	$(5200300\rho^{25} - 32449872\rho^{23} + 89237148\rho^{21} - 142262120\rho^{19} + 145495350\rho^{17} - 99768240\rho^{15} + 46558511\rho^{13} - 14702688\rho^{11} + 3063060\rho^9 - 400400\rho^7 + 30030\rho^5 - 1092\rho^3 + 12\rho)\cos(\theta)$
327	25	1	$\sqrt{52}$	$(5200300\rho^{25} - 32449872\rho^{23} + 89237148\rho^{21} - 142262120\rho^{19} + 145495350\rho^{17} - 99768240\rho^{15} + 46558511\rho^{13} - 14702688\rho^{11} + 3063060\rho^9 - 400400\rho^7 + 30030\rho^5 - 1092\rho^3 + 12\rho)\sin(\theta)$
328	25	-3	$\sqrt{52}$	$(4457400\rho^{25} - 27457583\rho^{23} + 74364290\rho^{21} - 116396280\rho^{19} + 116396280\rho^{17} - 77597519\rho^{15} + 34918884\rho^{13} - 10501920\rho^{11} + 2042040\rho^9 - 240239\rho^7 + 15014\rho^5 - 364\rho^3)\cos(3\theta)$
329	25	3	$\sqrt{52}$	$(4457400\rho^{25} - 27457583\rho^{23} + 74364290\rho^{21} - 116396280\rho^{19} + 116396280\rho^{17} - 77597519\rho^{15} + 34918884\rho^{13} - 10501920\rho^{11} + 2042040\rho^9 - 240239\rho^7 + 15014\rho^5 - 364\rho^3)\sin(3\theta)$
330	25	-5	$\sqrt{52}$	$(3268759\rho^{25} - 19612560\rho^{23} + 51482970\rho^{21} - 77597520\rho^{19} + 74070360\rho^{17} - 46558512\rho^{15} + 19399380\rho^{13} - 5250960\rho^{11} + 875159\rho^9 - 80079\rho^7 + 3003\rho^5)\cos(5\theta)$

Table 1: Zernike Circular Polynomials $\mathrm{Z}_j(\rho,\theta) = \mathrm{Z}_n^m(\rho,\theta)$(continued)

j	n	m	N_n^m	ZEMAX $\mathrm{Z}_j(\rho,\theta) = \mathrm{Z}_n^m(\rho,\theta) = \mathrm{R}_n^m(\rho)\Theta_m(\theta)$
331	25	5	$\sqrt{52}$	$(3268759\rho^{25} - 19612560\rho^{23} + 51482970\rho^{21} - 77597520\rho^{19} + 74070360\rho^{17} - 46558512\rho^{15} + 19399380\rho^{13} - 5250960\rho^{11} + 875159\rho^{9} - 80079\rho^{7} + 3003\rho^{5})\sin(5\theta)$
332	25	−7	$\sqrt{52}$	$(2042974\rho^{25} - 11767535\rho^{23} + 29418840\rho^{21} - 41783280\rho^{19} + 37035180\rho^{17} - 21162960\rho^{15} + 7759752\rho^{13} - 1750319\rho^{11} + 218790\rho^{9} - 11440\rho^{7})\cos(7\theta)$
333	25	7	$\sqrt{52}$	$(2042974\rho^{25} - 11767535\rho^{23} + 29418840\rho^{21} - 41783280\rho^{19} + 37035180\rho^{17} - 21162960\rho^{15} + 7759752\rho^{13} - 1750319\rho^{11} + 218790\rho^{9} - 11440\rho^{7})\sin(7\theta)$
334	25	−9	$\sqrt{52}$	$(1081575\rho^{25} - 5883768\rho^{23} + 13728791\rho^{21} - 17907119\rho^{19} + 14244300\rho^{17} - 7054320\rho^{15} + 2116296\rho^{13} - 350063\rho^{11} + 24309\rho^{9})\cos(9\theta)$
335	25	9	$\sqrt{52}$	$(1081575\rho^{25} - 5883768\rho^{23} + 13728791\rho^{21} - 17907119\rho^{19} + 14244300\rho^{17} - 7054320\rho^{15} + 2116296\rho^{13} - 350063\rho^{11} + 24309\rho^{9})\sin(9\theta)$
336	25	−11	$\sqrt{52}$	$(480699\rho^{25} - 2422728\rho^{23} + 5148297\rho^{21} - 5969040\rho^{19} + 4069800\rho^{17} - 1627919\rho^{15} + 352715\rho^{13} - 31824\rho^{11})\cos(11\theta)$
337	25	11	$\sqrt{52}$	$(480699\rho^{25} - 2422728\rho^{23} + 5148297\rho^{21} - 5969040\rho^{19} + 4069800\rho^{17} - 1627919\rho^{15} + 352715\rho^{13} - 31824\rho^{11})\sin(11\theta)$
338	25	−13	$\sqrt{52}$	$(177100\rho^{25} - 807575\rho^{23} + 1514205\rho^{21} - 1492260\rho^{19} + 813960\rho^{17} - 232560\rho^{15} + 27131\rho^{13})\cos(13\theta)$
339	25	13	$\sqrt{52}$	$(177100\rho^{25} - 807575\rho^{23} + 1514205\rho^{21} - 1492260\rho^{19} + 813960\rho^{17} - 232560\rho^{15} + 27131\rho^{13})\sin(13\theta)$
340	25	−15	$\sqrt{52}$	$(53130\rho^{25} - 212520\rho^{23} + 336489\rho^{21} - 263340\rho^{19} + 101745\rho^{17} - 15504\rho^{15})\cos(15\theta)$
341	25	15	$\sqrt{52}$	$(53130\rho^{25} - 212520\rho^{23} + 336489\rho^{21} - 263340\rho^{19} + 101745\rho^{17} - 15504\rho^{15})\sin(15\theta)$
342	25	−17	$\sqrt{52}$	$(12650\rho^{25} - 42504\rho^{23} + 53130\rho^{21} - 29260\rho^{19} + 5985\rho^{17})\cos(17\theta)$
343	25	17	$\sqrt{52}$	$(12650\rho^{25} - 42504\rho^{23} + 53130\rho^{21} - 29260\rho^{19} + 5985\rho^{17})\sin(17\theta)$
344	25	−19	$\sqrt{52}$	$(2300\rho^{25} - 6072\rho^{23} + 5313\rho^{21} - 1540\rho^{19})\cos(19\theta)$
345	25	19	$\sqrt{52}$	$(2300\rho^{25} - 6072\rho^{23} + 5313\rho^{21} - 1540\rho^{19})\sin(19\theta)$
346	25	−21	$\sqrt{52}$	$(300\rho^{25} - 552\rho^{23} + 253\rho^{21})\cos(21\theta)$
347	25	21	$\sqrt{52}$	$(300\rho^{25} - 552\rho^{23} + 253\rho^{21})\sin(21\theta)$
348	25	−23	$\sqrt{52}$	$(25\rho^{25} - 24\rho^{23})\cos(23\theta)$
349	25	23	$\sqrt{52}$	$(25\rho^{25} - 24\rho^{23})\sin(23\theta)$
350	25	−25	$\sqrt{52}$	$\rho^{25}\cos(25\theta)$
351	25	25	$\sqrt{52}$	$\rho^{25}\sin(25\theta)$
352	26	0	$\sqrt{27}$	$10400600\rho^{26} - 67603899\rho^{24} + 194699232\rho^{22} - 327202875\rho^{20} + 355655300\rho^{18} - 261891630\rho^{16} + 133024320\rho^{14} - 46558512\rho^{12} + 11027015\rho^{10} - 1701700\rho^{8} + 160160\rho^{6} - 8190\rho^{4} + 181\rho^{2} - 1$
353	26	−2	$\sqrt{54}$	$(9657700\rho^{26} - 62403600\rho^{24} + 178474296\rho^{22} - 297457160\rho^{20} + 320089770\rho^{18} - 232792560\rho^{16} + 116396280\rho^{14} - 39907295\rho^{12} + 9189180\rho^{10} - 1361360\rho^{8} + 120120\rho^{6} - 5460\rho^{4} + 91\rho^{2})\sin(2\theta)$
354	26	2	$\sqrt{54}$	$(9657700\rho^{26} - 62403600\rho^{24} + 178474296\rho^{22} - 297457160\rho^{20} + 320089770\rho^{18} - 232792560\rho^{16} + 116396280\rho^{14} - 39907295\rho^{12} + 9189180\rho^{10} - 1361360\rho^{8} + 120120\rho^{6} - 5460\rho^{4} + 91\rho^{2})\cos(2\theta)$
355	26	−4	$\sqrt{54}$	$(7726159\rho^{26} - 49031400\rho^{24} + 137287919\rho^{22} - 223092870\rho^{20} + 232792560\rho^{18} - 162954791\rho^{16} + 77597519\rho^{14} - 24942060\rho^{12} + 5250960\rho^{10} - 680680\rho^{8} + 48047\rho^{6} - 1364\rho^{4})\sin(4\theta)$
356	26	4	$\sqrt{54}$	$(7726159\rho^{26} - 49031400\rho^{24} + 137287919\rho^{22} - 223092870\rho^{20} + 232792560\rho^{18} - 162954791\rho^{16} + 77597519\rho^{14} - 24942060\rho^{12} + 5250960\rho^{10} - 680680\rho^{8} + 48047\rho^{6} - 1364\rho^{4})\cos(4\theta)$

Table 1: Zernike Circular Polynomials $\mathrm{Z}_j(\rho,\theta) = \mathrm{Z}_n^m(\rho,\theta)$(continued)

j	n	m	N_n^m	ZEMAX $\mathrm{Z}_j(\rho,\theta) = \mathrm{Z}_n^m(\rho,\theta) = \mathrm{R}_n^m(\rho)\Theta_m(\theta)$
357	26	-6	$\sqrt{54}$	$(5311735\rho^{26} - 32687599\rho^{24} + 88256520\rho^{22} - 137287920\rho^{20} + 135795660\rho^{18} - 88884432\rho^{16} + 38798760\rho^{14} - 11085360\rho^{12} + 1969109\rho^{10} - 194479\rho^{8} + 8008\rho^{6})\sin(6\theta)$
358	26	6	$\sqrt{54}$	$(5311735\rho^{26} - 32687599\rho^{24} + 88256520\rho^{22} - 137287920\rho^{20} + 135795660\rho^{18} - 88884432\rho^{16} + 38798760\rho^{14} - 11085360\rho^{12} + 1969109\rho^{10} - 194479\rho^{8} + 8008\rho^{6})\cos(6\theta)$
359	26	-8	$\sqrt{54}$	$(3124550\rho^{26} - 18386774\rho^{24} + 47070143\rho^{22} - 68643960\rho^{20} + 62674920\rho^{18} - 37035180\rho^{16} + 14108640\rho^{14} - 3325608\rho^{12} + 437579\rho^{10} - 24310\rho^{8})\sin(8\theta)$
360	26	8	$\sqrt{54}$	$(3124550\rho^{26} - 18386774\rho^{24} + 47070143\rho^{22} - 68643960\rho^{20} + 62674920\rho^{18} - 37035180\rho^{16} + 14108640\rho^{14} - 3325608\rho^{12} + 437579\rho^{10} - 24310\rho^{8})\cos(8\theta)$
361	26	-10	$\sqrt{54}$	$(1562275\rho^{26} - 8652600\rho^{24} + 20593188\rho^{22} - 27457583\rho^{20} + 22383900\rho^{18} - 11395440\rho^{16} + 3527160\rho^{14} - 604656\rho^{12} + 43757\rho^{10})\sin(10\theta)$
362	26	10	$\sqrt{54}$	$(1562275\rho^{26} - 8652600\rho^{24} + 20593188\rho^{22} - 27457583\rho^{20} + 22383900\rho^{18} - 11395440\rho^{16} + 3527160\rho^{14} - 604656\rho^{12} + 43757\rho^{10})\cos(10\theta)$
363	26	-12	$\sqrt{54}$	$(657800\rho^{26} - 3364899\rho^{24} + 7268184\rho^{22} - 8580495\rho^{20} + 5969040\rho^{18} - 2441879\rho^{16} + 542640\rho^{14} - 50387\rho^{12})\sin(12\theta)$
364	26	12	$\sqrt{54}$	$(657800\rho^{26} - 3364899\rho^{24} + 7268184\rho^{22} - 8580495\rho^{20} + 5969040\rho^{18} - 2441879\rho^{16} + 542640\rho^{14} - 50387\rho^{12})\cos(12\theta)$
365	26	-14	$\sqrt{54}$	$(230230\rho^{26} - 1062600\rho^{24} + 2018939\rho^{22} - 2018940\rho^{20} + 1119195\rho^{18} - 325584\rho^{16} + 38760\rho^{14})\sin(14\theta)$
366	26	14	$\sqrt{54}$	$(230230\rho^{26} - 1062600\rho^{24} + 2018939\rho^{22} - 2018940\rho^{20} + 1119195\rho^{18} - 325584\rho^{16} + 38760\rho^{14})\cos(14\theta)$
367	26	-16	$\sqrt{54}$	$(65780\rho^{26} - 265650\rho^{24} + 425040\rho^{22} - 336489\rho^{20} + 131670\rho^{18} - 20349\rho^{16})\sin(16\theta)$
368	26	16	$\sqrt{54}$	$(65780\rho^{26} - 265650\rho^{24} + 425040\rho^{22} - 336489\rho^{20} + 131670\rho^{18} - 20349\rho^{16})\cos(16\theta)$
369	26	-18	$\sqrt{54}$	$(14950\rho^{26} - 50600\rho^{24} + 63756\rho^{22} - 35420\rho^{20} + 7315\rho^{18})\sin(18\theta)$
370	26	18	$\sqrt{54}$	$(14950\rho^{26} - 50600\rho^{24} + 63756\rho^{22} - 35420\rho^{20} + 7315\rho^{18})\cos(18\theta)$
371	26	-20	$\sqrt{54}$	$(2600\rho^{26} - 6900\rho^{24} + 6072\rho^{22} - 1771\rho^{20})\sin(20\theta)$
372	26	20	$\sqrt{54}$	$(2600\rho^{26} - 6900\rho^{24} + 6072\rho^{22} - 1771\rho^{20})\cos(20\theta)$
373	26	-22	$\sqrt{54}$	$(325\rho^{26} - 600\rho^{24} + 276\rho^{22})\sin(22\theta)$
374	26	22	$\sqrt{54}$	$(325\rho^{26} - 600\rho^{24} + 276\rho^{22})\cos(22\theta)$
375	26	-24	$\sqrt{54}$	$(26\rho^{26} - 25\rho^{24})\sin(24\theta)$
376	26	24	$\sqrt{54}$	$(26\rho^{26} - 25\rho^{24})\cos(24\theta)$
377	26	-26	$\sqrt{54}$	$\rho^{26}\sin(26\theta)$
378	26	26	$\sqrt{54}$	$\rho^{26}\cos(26\theta)$
379	27	-1	$\sqrt{56}$	$(20058300\rho^{27} - 135207800\rho^{25} + 405623399\rho^{23} - 713897184\rho^{21} + 818007189\rho^{19} - 640179540\rho^{17} + 349188840\rho^{15} - 133024320\rho^{13} + 34918884\rho^{11} - 6126119\rho^{9} + 680680\rho^{7} - 43680\rho^{5} + 1364\rho^{3} - 14\rho)\sin(\theta)$
380	27	1	$\sqrt{56}$	$(20058300\rho^{27} - 135207800\rho^{25} + 405623399\rho^{23} - 713897184\rho^{21} + 818007189\rho^{19} - 640179540\rho^{17} + 349188840\rho^{15} - 133024320\rho^{13} + 34918884\rho^{11} - 6126119\rho^{9} + 680680\rho^{7} - 43680\rho^{5} + 1364\rho^{3} - 14\rho)\cos(\theta)$
381	27	-3	$\sqrt{56}$	$(17383860\rho^{27} - 115892400\rho^{25} + 343219800\rho^{23} - 594914320\rho^{21} + 669278610\rho^{19} - 512143632\rho^{17} + 271591320\rho^{15} - 99768240\rho^{13} + 24942060\rho^{11} - 4084080\rho^{9} + 408408\rho^{7} - 21839\rho^{5} + 455\rho^{3})\sin(3\theta)$
382	27	3	$\sqrt{56}$	$(17383860\rho^{27} - 115892400\rho^{25} + 343219800\rho^{23} - 594914320\rho^{21} + 669278610\rho^{19} - 512143632\rho^{17} + 271591320\rho^{15} - 99768240\rho^{13} + 24942060\rho^{11} - 4084080\rho^{9} + 408408\rho^{7} - 21839\rho^{5} + 455\rho^{3})\cos(3\theta)$

Table 1: Zernike Circular Polynomials $\mathrm{Z}_j(\rho,\theta) = \mathrm{Z}_n^m(\rho,\theta)$(continued)

j	n	m	N_n^m	ZEMAX $\mathrm{Z}_j(\rho,\theta) = \mathrm{Z}_n^m(\rho,\theta) = \mathrm{R}_n^m(\rho)\Theta_m(\theta)$
383	27	-5	$\sqrt{56}$	$(13037894\rho^{27} - 84987759\rho^{25} + 245157000\rho^{23} - 411863759\rho^{21} + 446185740\rho^{19} - 325909584\rho^{17} + 162954791\rho^{15} - 55426800\rho^{13} + 12471030\rho^{11} - 1750320\rho^9 + 136136\rho^7 - 4367\rho^5)\sin(5\theta)$
384	27	5	$\sqrt{56}$	$(13037894\rho^{27} - 84987759\rho^{25} + 245157000\rho^{23} - 411863759\rho^{21} + 446185740\rho^{19} - 325909584\rho^{17} + 162954791\rho^{15} - 55426800\rho^{13} + 12471030\rho^{11} - 1750320\rho^9 + 136136\rho^7 - 4367\rho^5)\cos(5\theta)$
385	27	-7	$\sqrt{56}$	$(8436285\rho^{27} - 53117350\rho^{25} + 147094199\rho^{23} - 235350720\rho^{21} + 240253860\rho^{19} - 162954792\rho^{17} + 74070360\rho^{15} - 22170720\rho^{13} + 4157009\rho^{11} - 437579\rho^9 + 19447\rho^7)\sin(7\theta)$
386	27	7	$\sqrt{56}$	$(8436285\rho^{27} - 53117350\rho^{25} + 147094199\rho^{23} - 235350720\rho^{21} + 240253860\rho^{19} - 162954792\rho^{17} + 74070360\rho^{15} - 22170720\rho^{13} + 4157009\rho^{11} - 437579\rho^9 + 19447\rho^7)\cos(7\theta)$
387	27	-9	$\sqrt{56}$	$(4686825\rho^{27} - 28120950\rho^{25} + 73547099\rho^{23} - 109830335\rho^{21} + 102965940\rho^{19} - 62674920\rho^{17} + 24690120\rho^{15} - 6046560\rho^{13} + 831402\rho^{11} - 48619\rho^9)\sin(9\theta)$
388	27	9	$\sqrt{56}$	$(4686825\rho^{27} - 28120950\rho^{25} + 73547099\rho^{23} - 109830335\rho^{21} + 102965940\rho^{19} - 62674920\rho^{17} + 24690120\rho^{15} - 6046560\rho^{13} + 831402\rho^{11} - 48619\rho^9)\cos(9\theta)$
389	27	-11	$\sqrt{56}$	$(2220075\rho^{27} - 12498200\rho^{25} + 30284100\rho^{23} - 41186375\rho^{21} + 34321979\rho^{19} - 17907120\rho^{17} + 5697720\rho^{15} - 1007760\rho^{13} + 75582\rho^{11})\sin(11\theta)$
390	27	11	$\sqrt{56}$	$(2220075\rho^{27} - 12498200\rho^{25} + 30284100\rho^{23} - 41186375\rho^{21} + 34321979\rho^{19} - 17907120\rho^{17} + 5697720\rho^{15} - 1007760\rho^{13} + 75582\rho^{11})\cos(11\theta)$
391	27	-13	$\sqrt{56}$	$(888030\rho^{27} - 4604600\rho^{25} + 10094699\rho^{23} - 12113640\rho^{21} + 8580495\rho^{19} - 3581423\rho^{17} + 813960\rho^{15} - 77520\rho^{13})\sin(13\theta)$
392	27	13	$\sqrt{56}$	$(888030\rho^{27} - 4604600\rho^{25} + 10094699\rho^{23} - 12113640\rho^{21} + 8580495\rho^{19} - 3581423\rho^{17} + 813960\rho^{15} - 77520\rho^{13})\cos(13\theta)$
393	27	-15	$\sqrt{56}$	$(296010\rho^{27} - 1381380\rho^{25} + 2656500\rho^{23} - 2691919\rho^{21} + 1514205\rho^{19} - 447678\rho^{17} + 54264\rho^{15})\sin(15\theta)$
394	27	15	$\sqrt{56}$	$(296010\rho^{27} - 1381380\rho^{25} + 2656500\rho^{23} - 2691919\rho^{21} + 1514205\rho^{19} - 447678\rho^{17} + 54264\rho^{15})\cos(15\theta)$
395	27	-17	$\sqrt{56}$	$(80730\rho^{27} - 328900\rho^{25} + 531300\rho^{23} - 425040\rho^{21} + 168244\rho^{19} - 26334\rho^{17})\sin(17\theta)$
396	27	17	$\sqrt{56}$	$(80730\rho^{27} - 328900\rho^{25} + 531300\rho^{23} - 425040\rho^{21} + 168244\rho^{19} - 26334\rho^{17})\cos(17\theta)$
397	27	-19	$\sqrt{56}$	$(17549\rho^{27} - 59800\rho^{25} + 75900\rho^{23} - 42504\rho^{21} + 8855\rho^{19})\sin(19\theta)$
398	27	19	$\sqrt{56}$	$(17549\rho^{27} - 59800\rho^{25} + 75900\rho^{23} - 42504\rho^{21} + 8855\rho^{19})\cos(19\theta)$
399	27	-21	$\sqrt{56}$	$(2925\rho^{27} - 7800\rho^{25} + 6900\rho^{23} - 2024\rho^{21})\sin(21\theta)$
400	27	21	$\sqrt{56}$	$(2925\rho^{27} - 7800\rho^{25} + 6900\rho^{23} - 2024\rho^{21})\cos(21\theta)$
401	27	-23	$\sqrt{56}$	$(351\rho^{27} - 650\rho^{25} + 300\rho^{23})\sin(23\theta)$
402	27	23	$\sqrt{56}$	$(351\rho^{27} - 650\rho^{25} + 300\rho^{23})\cos(23\theta)$
403	27	-25	$\sqrt{56}$	$(27\rho^{27} - 26\rho^{25})\sin(25\theta)$
404	27	25	$\sqrt{56}$	$(27\rho^{27} - 26\rho^{25})\cos(25\theta)$
405	27	-27	$\sqrt{56}$	$\rho^{27}\sin(27\theta)$
406	27	27	$\sqrt{56}$	$\rho^{27}\cos(27\theta)$
407	28	0	$\sqrt{29}$	$40116600\rho^{28} - 280816199\rho^{26} + 878850700\rho^{24} - 1622493600\rho^{22} + 1963217255\rho^{20} - 1636014379\rho^{18} + 960269310\rho^{16} - 399072959\rho^{14} + 116396280\rho^{12} - 23279256\rho^{10} + 3063060\rho^8 - 247520\rho^6 + 10920\rho^4 - 209\rho^2 + 1$
408	28	-2	$\sqrt{58}$	$(37442160\rho^{28} - 260757900\rho^{26} + 811246800\rho^{24} - 1487285799\rho^{22} + 1784742960\rho^{20} - 1472412941\rho^{18} + 853572719\rho^{16} - 349188840\rho^{14} + 99768240\rho^{12} - 19399380\rho^{10} + 2450447\rho^8 - 185640\rho^6 + 7280\rho^4 - 105\rho^2)\cos(2\theta)$

Table 1: Zernike Circular Polynomials $\mathrm{Z}_j(\rho,\theta) = \mathrm{Z}_n^m(\rho,\theta)$(continued)

j	n	m	N_n^m	ZEMAX $\mathrm{Z}_j(\rho,\theta) = \mathrm{Z}_n^m(\rho,\theta) = \mathrm{R}_n^m(\rho)\Theta_m(\theta)$
409	28	2	$\sqrt{58}$	$(37442160\rho^{28} - 260757900\rho^{26} + 811246800\rho^{24} - 1487285799\rho^{22} + 1784742960\rho^{20} - 1472412941\rho^{18} + 853572719\rho^{16} - 349188840\rho^{14} + 99768240\rho^{12} - 19399380\rho^{10} + 2450447\rho^8 - 185640\rho^6 + 7280\rho^4 - 105\rho^2)\sin(2\theta)$
410	28	−4	$\sqrt{58}$	$(30421755\rho^{28} - 208606320\rho^{26} + 637408200\rho^{24} - 1144066000\rho^{22} + 1338557220\rho^{20} - 1070845776\rho^{18} + 597500904\rho^{16} - 232792559\rho^{14} + 62355150\rho^{12} - 11085360\rho^{10} + 1225224\rho^8 - 74256\rho^6 + 1819\rho^4)\cos(4\theta)$
411	28	4	$\sqrt{58}$	$(30421755\rho^{28} - 208606320\rho^{26} + 637408200\rho^{24} - 1144066000\rho^{22} + 1338557220\rho^{20} - 1070845776\rho^{18} + 597500904\rho^{16} - 232792559\rho^{14} + 62355150\rho^{12} - 11085360\rho^{10} + 1225224\rho^8 - 74256\rho^6 + 1819\rho^4)\sin(4\theta)$
412	28	−6	$\sqrt{58}$	$(21474180\rho^{28} - 143416844\rho^{26} + 424938799\rho^{24} - 735471000\rho^{22} + 823727519\rho^{20} - 624660036\rho^{18} + 325909584\rho^{16} - 116396280\rho^{14} + 27713399\rho^{12} - 4157010\rho^{10} + 350064\rho^8 - 12376\rho^6)\cos(6\theta)$
413	28	6	$\sqrt{58}$	$(21474180\rho^{28} - 143416844\rho^{26} + 424938799\rho^{24} - 735471000\rho^{22} + 823727519\rho^{20} - 624660036\rho^{18} + 325909584\rho^{16} - 116396280\rho^{14} + 27713399\rho^{12} - 4157010\rho^{10} + 350064\rho^8 - 12376\rho^6)\sin(6\theta)$
414	28	−8	$\sqrt{58}$	$(13123109\rho^{28} - 84362850\rho^{26} + 239028075\rho^{24} - 392251199\rho^{22} + 411863760\rho^{20} - 288304632\rho^{18} + 135795660\rho^{16} - 42325920\rho^{14} + 8314019\rho^{12} - 923779\rho^{10} + 43758\rho^8)\cos(8\theta)$
415	28	8	$\sqrt{58}$	$(13123109\rho^{28} - 84362850\rho^{26} + 239028075\rho^{24} - 392251199\rho^{22} + 411863760\rho^{20} - 288304632\rho^{18} + 135795660\rho^{16} - 42325920\rho^{14} + 8314019\rho^{12} - 923779\rho^{10} + 43758\rho^8)\sin(8\theta)$
416	28	−10	$\sqrt{58}$	$(6906900\rho^{28} - 42181425\rho^{26} + 112483800\rho^{24} - 171609899\rho^{22} + 164745503\rho^{20} - 102965940\rho^{18} + 41783280\rho^{16} - 10581480\rho^{14} + 1511640\rho^{12} - 92378\rho^{10})\cos(10\theta)$
417	28	10	$\sqrt{58}$	$(6906900\rho^{28} - 42181425\rho^{26} + 112483800\rho^{24} - 171609899\rho^{22} + 164745503\rho^{20} - 102965940\rho^{18} + 41783280\rho^{16} - 10581480\rho^{14} + 1511640\rho^{12} - 92378\rho^{10})\sin(10\theta)$
418	28	−12	$\sqrt{58}$	$(3108104\rho^{28} - 17760600\rho^{26} + 43743700\rho^{24} - 60568199\rho^{22} + 51482970\rho^{20} - 27457583\rho^{18} + 8953560\rho^{16} - 1627919\rho^{14} + 125970\rho^{12})\cos(12\theta)$
419	28	12	$\sqrt{58}$	$(3108104\rho^{28} - 17760600\rho^{26} + 43743700\rho^{24} - 60568199\rho^{22} + 51482970\rho^{20} - 27457583\rho^{18} + 8953560\rho^{16} - 1627919\rho^{14} + 125970\rho^{12})\sin(12\theta)$
420	28	−14	$\sqrt{58}$	$(1184040\rho^{28} - 6216210\rho^{26} + 13813800\rho^{24} - 16824499\rho^{22} + 12113640\rho^{20} - 5148296\rho^{18} + 1193808\rho^{16} - 116280\rho^{14})\cos(14\theta)$
421	28	14	$\sqrt{58}$	$(1184040\rho^{28} - 6216210\rho^{26} + 13813800\rho^{24} - 16824499\rho^{22} + 12113640\rho^{20} - 5148296\rho^{18} + 1193808\rho^{16} - 116280\rho^{14})\sin(14\theta)$
422	28	−16	$\sqrt{58}$	$(376740\rho^{28} - 1776060\rho^{26} + 3453450\rho^{24} - 3542000\rho^{22} + 2018939\rho^{20} - 605682\rho^{18} + 74613\rho^{16})\cos(16\theta)$
423	28	16	$\sqrt{58}$	$(376740\rho^{28} - 1776060\rho^{26} + 3453450\rho^{24} - 3542000\rho^{22} + 2018939\rho^{20} - 605682\rho^{18} + 74613\rho^{16})\sin(16\theta)$
424	28	−18	$\sqrt{58}$	$(98279\rho^{28} - 403650\rho^{26} + 657800\rho^{24} - 531300\rho^{22} + 212520\rho^{20} - 33648\rho^{18})\cos(18\theta)$
425	28	18	$\sqrt{58}$	$(98279\rho^{28} - 403650\rho^{26} + 657800\rho^{24} - 531300\rho^{22} + 212520\rho^{20} - 33648\rho^{18})\sin(18\theta)$
426	28	−20	$\sqrt{58}$	$(20475\rho^{28} - 70199\rho^{26} + 89700\rho^{24} - 50600\rho^{22} + 10626\rho^{20})\cos(20\theta)$
427	28	20	$\sqrt{58}$	$(20475\rho^{28} - 70199\rho^{26} + 89700\rho^{24} - 50600\rho^{22} + 10626\rho^{20})\sin(20\theta)$
428	28	−22	$\sqrt{58}$	$(3276\rho^{28} - 8775\rho^{26} + 7800\rho^{24} - 2300\rho^{22})\cos(22\theta)$
429	28	22	$\sqrt{58}$	$(3276\rho^{28} - 8775\rho^{26} + 7800\rho^{24} - 2300\rho^{22})\sin(22\theta)$
430	28	−24	$\sqrt{58}$	$(378\rho^{28} - 702\rho^{26} + 325\rho^{24})\cos(24\theta)$
431	28	24	$\sqrt{58}$	$(378\rho^{28} - 702\rho^{26} + 325\rho^{24})\sin(24\theta)$
432	28	−26	$\sqrt{58}$	$(28\rho^{28} - 27\rho^{26})\cos(26\theta)$
433	28	26	$\sqrt{58}$	$(28\rho^{28} - 27\rho^{26})\sin(26\theta)$

Table 1: Zernike Circular Polynomials $\mathrm{Z}_j(\rho,\theta) = \mathrm{Z}_n^m(\rho,\theta)$(continued)

j	n	m	N_n^m	ZEMAX $\mathrm{Z}_j(\rho,\theta) = \mathrm{Z}_n^m(\rho,\theta) = \mathrm{R}_n^m(\rho)\Theta_m(\theta)$
434	28	−28	$\sqrt{58}$	$\rho^{28}\cos(28\theta)$
435	28	28	$\sqrt{58}$	$\rho^{28}\sin(28\theta)$
436	29	−1	$\sqrt{60}$	$(77558759\rho^{29} - 561632400\rho^{27} + 1825305299\rho^{25} - -2147483648\rho^{23} - -2147483648\rho^{21} - -2147483648\rho^{19} - -2147483648\rho^{17} - 1097450639\rho^{15} + 349188839\rho^{13} - 77597520\rho^{11} + 11639628\rho^{9} - 1113840\rho^{7} + 61880\rho^{5} - 1679\rho^{3} + 14\rho)\cos(\theta)$
437	29	1	$\sqrt{60}$	$(77558759\rho^{29} - 561632400\rho^{27} + 1825305299\rho^{25} - -2147483648\rho^{23} - -2147483648\rho^{21} - -2147483648\rho^{19} - -2147483648\rho^{17} - 1097450639\rho^{15} + 349188839\rho^{13} - 77597520\rho^{11} + 11639628\rho^{9} - 1113840\rho^{7} + 61880\rho^{5} - 1679\rho^{3} + 14\rho)\sin(\theta)$
438	29	−3	$\sqrt{60}$	$(67863914\rho^{29} - 486748080\rho^{27} + 1564547400\rho^{25} - -2147483648\rho^{23} - -2147483648\rho^{21} - -2147483648\rho^{19} + 1963217255\rho^{17} - 853572720\rho^{15} + 261891630\rho^{13} - 55426800\rho^{11} + 7759752\rho^{9} - 668304\rho^{7} + 30939\rho^{5} - 560\rho^{3})\cos(3\theta)$
439	29	3	$\sqrt{60}$	$(67863914\rho^{29} - 486748080\rho^{27} + 1564547400\rho^{25} - -2147483648\rho^{23} - -2147483648\rho^{21} - -2147483648\rho^{19} + 1963217255\rho^{17} - 853572720\rho^{15} + 261891630\rho^{13} - 55426800\rho^{11} + 7759752\rho^{9} - 668304\rho^{7} + 30939\rho^{5} - 560\rho^{3})\sin(3\theta)$
440	29	−5	$\sqrt{60}$	$(51895935\rho^{29} - 365061060\rho^{27} + 1147334760\rho^{25} - 2124694000\rho^{23} - -2147483648\rho^{21} - 2141691552\rho^{19} + 1249320072\rho^{17} - 512143631\rho^{15} + 145495350\rho^{13} - 27713400\rho^{11} + 3325608\rho^{9} - 222768\rho^{7} + 6188\rho^{5})\cos(5\theta)$
441	29	5	$\sqrt{60}$	$(51895935\rho^{29} - 365061060\rho^{27} + 1147334760\rho^{25} - 2124694000\rho^{23} - -2147483648\rho^{21} - 2141691552\rho^{19} + 1249320072\rho^{17} - 512143631\rho^{15} + 145495350\rho^{13} - 27713400\rho^{11} + 3325608\rho^{9} - 222768\rho^{7} + 6188\rho^{5})\sin(5\theta)$
442	29	−7	$\sqrt{60}$	$(34597289\rho^{29} - 236215980\rho^{27} + 717084224\rho^{25} - 1274816399\rho^{23} + 1470942000\rho^{21} - 1153218527\rho^{19} + 624660036\rho^{17} - 232792560\rho^{15} + 58198139\rho^{13} - 9237800\rho^{11} + 831402\rho^{9} - 31824\rho^{7})\cos(7\theta)$
443	29	7	$\sqrt{60}$	$(34597289\rho^{29} - 236215980\rho^{27} + 717084224\rho^{25} - 1274816399\rho^{23} + 1470942000\rho^{21} - 1153218527\rho^{19} + 624660036\rho^{17} - 232792560\rho^{15} + 58198139\rho^{13} - 9237800\rho^{11} + 831402\rho^{9} - 31824\rho^{7})\sin(7\theta)$
444	29	−9	$\sqrt{60}$	$(20030010\rho^{29} - 131231099\rho^{27} + 379632825\rho^{25} - 637408200\rho^{23} + 686439599\rho^{21} - 494236512\rho^{19} + 240253860\rho^{17} - 77597520\rho^{15} + 15872220\rho^{13} - 1847559\rho^{11} + 92378\rho^{9})\cos(9\theta)$
445	29	9	$\sqrt{60}$	$(20030010\rho^{29} - 131231099\rho^{27} + 379632825\rho^{25} - 637408200\rho^{23} + 686439599\rho^{21} - 494236512\rho^{19} + 240253860\rho^{17} - 77597520\rho^{15} + 15872220\rho^{13} - 1847559\rho^{11} + 92378\rho^{9})\sin(9\theta)$
446	29	−11	$\sqrt{60}$	$(10015005\rho^{29} - 62162100\rho^{27} + 168725700\rho^{25} - 262462200\rho^{23} + 257414849\rho^{21} - 164745504\rho^{19} + 68643960\rho^{17} - 17907120\rho^{15} + 2645370\rho^{13} - 167960\rho^{11})\cos(11\theta)$
447	29	11	$\sqrt{60}$	$(10015005\rho^{29} - 62162100\rho^{27} + 168725700\rho^{25} - 262462200\rho^{23} + 257414849\rho^{21} - 164745504\rho^{19} + 68643960\rho^{17} - 17907120\rho^{15} + 2645370\rho^{13} - 167960\rho^{11})\sin(11\theta)$
448	29	−13	$\sqrt{60}$	$(4292145\rho^{29} - 24864839\rho^{27} + 62162100\rho^{25} - 87487399\rho^{23} + 75710250\rho^{21} - 41186376\rho^{19} + 13728791\rho^{17} - 2558159\rho^{15} + 203490\rho^{13})\cos(13\theta)$
449	29	13	$\sqrt{60}$	$(4292145\rho^{29} - 24864839\rho^{27} + 62162100\rho^{25} - 87487399\rho^{23} + 75710250\rho^{21} - 41186376\rho^{19} + 13728791\rho^{17} - 2558159\rho^{15} + 203490\rho^{13})\sin(13\theta)$
450	29	−15	$\sqrt{60}$	$(1560780\rho^{29} - 8288280\rho^{27} + 18648630\rho^{25} - 23023000\rho^{23} + 16824499\rho^{21} - 7268184\rho^{19} + 1716099\rho^{17} - 170544\rho^{15})\cos(15\theta)$
451	29	15	$\sqrt{60}$	$(1560780\rho^{29} - 8288280\rho^{27} + 18648630\rho^{25} - 23023000\rho^{23} + 16824499\rho^{21} - 7268184\rho^{19} + 1716099\rho^{17} - 170544\rho^{15})\sin(15\theta)$
452	29	−17	$\sqrt{60}$	$(475020\rho^{29} - 2260440\rho^{27} + 4440150\rho^{25} - 4604600\rho^{23} + 2656500\rho^{21} - 807575\rho^{19} + 100947\rho^{17})\cos(17\theta)$

Table 1: Zernike Circular Polynomials $\mathrm{Z}_j(\rho,\theta) = \mathrm{Z}_n^m(\rho,\theta)$(continued)

j	n	m	N_n^m	ZEMAX $\mathrm{Z}_j(\rho,\theta) = \mathrm{Z}_n^m(\rho,\theta) = \mathrm{R}_n^m(\rho)\Theta_m(\theta)$
453	29	17	$\sqrt{60}$	$(475020\rho^{29}-2260440\rho^{27}+4440150\rho^{25}-4604600\rho^{23}+2656500\rho^{21}-807575\rho^{19}+100947\rho^{17})\sin(17\theta)$
454	29	−19	$\sqrt{60}$	$(118755\rho^{29}-491399\rho^{27}+807300\rho^{25}-657800\rho^{23}+265650\rho^{21}-42504\rho^{19})\cos(19\theta)$
455	29	19	$\sqrt{60}$	$(118755\rho^{29}-491399\rho^{27}+807300\rho^{25}-657800\rho^{23}+265650\rho^{21}-42504\rho^{19})\sin(19\theta)$
456	29	−21	$\sqrt{60}$	$(23751\rho^{29}-81900\rho^{27}+105299\rho^{25}-59800\rho^{23}+12650\rho^{21})\cos(21\theta)$
457	29	21	$\sqrt{60}$	$(23751\rho^{29}-81900\rho^{27}+105299\rho^{25}-59800\rho^{23}+12650\rho^{21})\sin(21\theta)$
458	29	−23	$\sqrt{60}$	$(3653\rho^{29}-9828\rho^{27}+8775\rho^{25}-2600\rho^{23})\cos(23\theta)$
459	29	23	$\sqrt{60}$	$(3653\rho^{29}-9828\rho^{27}+8775\rho^{25}-2600\rho^{23})\sin(23\theta)$
460	29	−25	$\sqrt{60}$	$(406\rho^{29}-756\rho^{27}+351\rho^{25})\cos(25\theta)$
461	29	25	$\sqrt{60}$	$(406\rho^{29}-756\rho^{27}+351\rho^{25})\sin(25\theta)$
462	29	−27	$\sqrt{60}$	$(29\rho^{29}-28\rho^{27})\cos(27\theta)$
463	29	27	$\sqrt{60}$	$(29\rho^{29}-28\rho^{27})\sin(27\theta)$
464	29	−29	$\sqrt{60}$	$\rho^{29}\cos(29\theta)$
465	29	29	$\sqrt{60}$	$\rho^{29}\sin(29\theta)$